

Battery sizing and rule-based operation of grid-connected photovoltaic-battery system: A case study in Sweden

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Abstract: The optimal components design for grid-connected photovoltaic-battery systems should be determined with consideration of system operation. This study proposes a method to simultaneously optimize the battery capacity and rule-based operation strategy. The investigated photovoltaic-battery system is modeled using single diode photovoltaic model and Improved Shepherd battery model. Three rule-based operation strategies — including the conventional operation strategy, the dynamic price load shifting strategy, and the hybrid operation strategy — are designed and evaluated. The rule-based operation strategies introduce different operation parameters to run the system operation. multi-objective Genetic Algorithm is employed to optimize the decisional variables, including battery capacity and operation parameters, towards maximizing the system's Self Sufficiency Ratio and Net Present Value. The results indicate that employing battery with the conventional operation strategy is not profitable, although it increases Self Sufficiency Ratio. The dynamic price load shifting strategy has similar performance with the conventional operation strategy because the electricity price variation is not large enough. The proposed hybrid operation strategy outperforms other investigated strategies. When the battery capacity is lower than 72 kWh, Self Sufficiency Ratio and Net Present Value increase simultaneously with the battery capacity.

Keywords: Photovoltaic; Battery; Operation Strategy; Optimization; Genetic Algorithm

22 **Nomenclature**

Symbol	Description
$C_{O\&M,y}$	Operation and maintenance cost at year y
$C_{R,y}$	Replacement cost at year y
CAP_i	Capacity for component i
d_r	Discount rate
$El_{r,t}$	Retail electricity price at time t
$El_{w,t}$	Wholesale electricity price at time t
$El_{r,H}$	High retail electricity price
$El_{r,L}$	Low retail electricity price
Inv	Investment cost
$P_{B,t}$	Battery power at time t
$P_{G,t}$	Grid power at time t
$P_{G,peak}$	Grid peak power
$P_{Gim,t}$	Imported grid power at time t
$P_{Gex,t}$	Exported grid power at time t
$P_{L,t}$	Load at time t
$P_{Mdisc,t}$	Maximal discharge power at time t
$P_{Mchar,t}$	Maximal charge power at time t
$P_{Net,t}$	Net power at time t
$P_{PV,t}$	PV power production at time t
P_H	High power limit
P_L	Low power limit
R_y	System revenue at year y
$R_{ER,y}$	Electricity reduction revenue at year y
$R_{EX,y}$	Export revenue at year y
$R_{PS,y}$	Peak shaving revenue at year y
$r_{O\&M,i}$	O&M Ratio for component i
SOC_t	State of Charge at time t
t_s	Conventional operation start time
t_e	Conventional operation end time
t_{peak}	The appearance time of $P_{G,peak}$
UIC_i	Unit Investment Cost for component i
η_{inv}	Inverter efficiency

23

24 **Abbreviations**

Abbreviations	Description
DOD	Depth of Discharge
Elspot	Electricity Spot
EMS	Energy Management System
GA	Genetic Algorithm
LOC	Level of Confidence
NPV	Net Present Value
SOC	State of Charge
SSR	Self Sufficiency Ratio
TOU	Time-of-Use

25

26 **1 Introduction**

27 The installed Photovoltaic (PV) capacity has increased rapidly in recent years. The installed
28 capacity has reached 177 GW at the end of 2014 [1]. Supporting policies, including feed-in-
29 tariff (Fit) and net-metering, are important incentives [2]. However, due to the intermittent na-
30 ture of solar energy, the accumulated PV capacity in the grid brings in technical issues with
31 power quality, frequency stability [3], and reliability. Batteries can not only smooth the PV
32 output and alleviate the technical challenges [4], but also increase the economic benefits [5].
33 The interest in the grid-connected PV-battery system is increasing among researchers and own-
34 ers [6].

35 Batteries can subject to different operation strategies and bring in different economic bene-
36 fits. In the first place, batteries increase the self-consumed electricity through storing excess PV
37 generation and discharging to supply consumption later [5]. The self-consumed electricity in-
38 creases the economic benefits due to the higher economic value than exported electricity. A
39 further battery management strategy is to charge it when the electricity price is low and dis-
40 charge it during high price times (loading shifting) [7]. In this case, benefits can be achieved
41 from the difference in electricity price. Furthermore, if the electricity user is partly charged
42 based on the peak power, battery can be discharged during the peak demand (peak shaving) [8].
43 In this case, benefits are achieved through reducing the user's peak power.

44 During the planning stage of the grid-connected PV-battery system, PV and battery capaci-
45 ties need to be decided. Meanwhile, different operation strategies need to be taken into account
46 to enhance the economic benefits. This is an optimization problem that simultaneously takes
47 into account PV capacity, battery capacity, and operation strategy [9]. However, the literature
48 survey indicates that component sizing and operation strategy are generally studied separately.

49 There are many researches addressing the component sizing issue, especially for the off-grid
50 systems. For example, Yang et al. used Genetic Algorithm and obtained the PV, wind turbine

51 and battery capacity for a stand-alone system [10]. Paliwal et al. introduced particle swarm
52 optimization method to determine the system configuration [11]. Xu et al. studied the possible
53 combinations of various PV, wind turbine and battery capacities, and obtained the system de-
54 sign under either grid-connected or stand-alone condition [12]. Mulder et al. studied the rela-
55 tionship between battery capacity and exported electricity to the grid in a grid-connected PV-
56 battery system. The relationship is further used to dimension the battery size [13]. Bortolini et
57 al. carried out a techno-economic analysis and determined the PV and battery capacity to min-
58 imize the levelized cost of electricity in grid-connected PV-battery system [14]. Zhou et al.
59 addressed the battery sizing issue with consideration of demand response under Time-of-Use
60 (TOU) tariff [15]. Mokhtari et al. determined the component size through the optimization to-
61 wards different objectives (i.e. maximizing power export) [16]. The above studies cover the
62 component sizing issue. However, the issue of maximizing economic benefits with different
63 operation strategies is not well addressed.

64 The optimal operation of a given system, which is achieved by Energy Management System
65 (EMS), also attracts lots of research attention [17]. A short-term power scheduling model for a
66 grid-connected PV-battery system was proposed by Lu et al. using a Lagrangian relaxation-
67 based optimization algorithm [18]. Riffonneau et al. used dynamic programming and obtained
68 the 24-hour ahead power scheduling based on the accurate prediction of weather and load [19].
69 Li et al. used dynamic programming to get predictive charge control strategies for different
70 objectives (i.e. maximizing battery life, maximizing self-sufficiency) [20]. Marzband et al. pro-
71 posed a power scheduling method based on mixed-integer nonlinear programming and verified
72 it with test bench [21]. An EMS that was based on multi-layer ant colony optimization was
73 reported to decrease the energy cost by 20% compared with the conventional EMS [22]. Grav-
74 itational Search Algorithm was demonstrated as an effective tool for peak consumption reduc-
75 tion and electricity generation cost minimization [23]. Imperialist competition algorithm was

76 used in EMS to provide multiple optimum solutions [24]. When considering demand response
77 of customers in the microgrid, further decrease of energy cost (30%) was achieved [25]. The
78 above studies obtained short-term power scheduling based on forecasted weather and load data.
79 The optimal operation issue is well addressed. However, the components in the studied systems
80 have pre-assumed and fixed sizes.

81 The literature survey indicates that studies on component sizing or optimal operation employ
82 different approaches, which are differentiated by decisional variables (component sizes / power
83 scheduling), input data (historical and representative data / forecasted data) and simulation time
84 frame (year / day).

85 Studies that take into account both sizing and scheduling problems are generally scarce. Ru
86 et al. determined the battery capacity in grid-connected PV-battery system with consideration
87 of load shifting and peak shaving under TOU tariff [26]. However, the optimal battery capacity
88 is determined based on the simulation of one typical day, indication that the seasonal variation
89 of solar irradiation and load is not considered. Gitizadeh et al. [27] extended the research by Ru
90 et al. Instead of one typical day, multiple typical operation scenarios, which are obtained from
91 Fuzzy Clustering Method, are used in solving the optimization problem. Khalilpour and Vas-
92 sallo proposed a decision support tool to decide system size concurrently with finding the opti-
93 mal operation schedule [28]. The support tool offers users to choose among different PV and
94 battery modules. The above studies merged component sizing and optimal scheduling. They
95 carried out long period simulation (several days or one year) using the historical data as input,
96 and determined the decisional variables including component sizes and power scheduling.
97 However, because of the extremely large amount of decisional variables (i.e. 18, 659, 330 in
98 Khalilpour and Vassallo [28]), the complex non-linear system was reduced to linear system to
99 facilitate the problem solving. Moreover, the studies assumed that correct weather and load
100 forecasting can be ensured during the real-time operation.

101 In this study, a new approach of determining the battery capacity and operation strategy is
102 proposed. Instead of determining the power scheduling, the new approach is based on rule-
103 based operation strategy. The approach largely decreases the numbers of decisional variables
104 and enables carrying out optimization with non-linear system. Specially, batteries are complex
105 electrochemical devices. Their efficiency, power constraints and lifetime are all influenced by
106 the operation condition. The approach enables to employ a more detailed model.

107 The main contributions of the paper are summarized below: 1) an approach that determines
108 battery capacity with consideration of system operation is proposed. The approach differs with
109 previous studies in using rule-based operation strategy and optimizing the operation parameters;
110 2) multi-objective optimization is carried out to analyze the feasibility of employing battery to
111 improve PV system's performance in both the renewable energy penetration level and economic
112 aspect; 3) a hybrid operation strategy is proposed and compared with other rule-based operation
113 strategies; 4) the studied case locates in cold-climate area with serious seasonal mismatch be-
114 tween generation and consumption, and it belongs to a deregulated electricity market. Similar
115 cases are rare in existing literature.

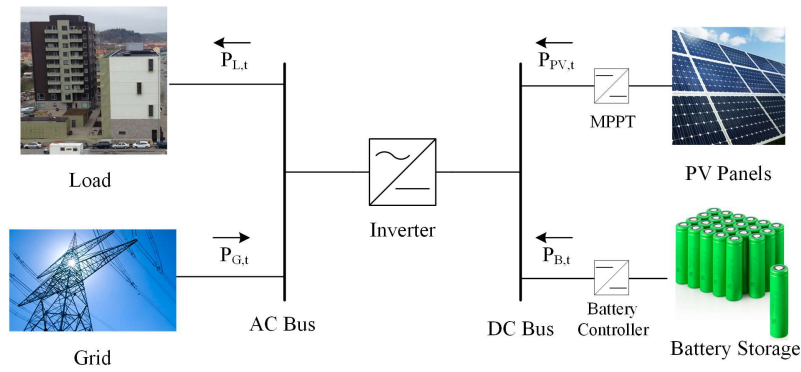
116 The article is organized as follows: Section 1 is introduction; Section 2 describes the methods;
117 Section 3 presents results and carries out discussion; Section 4 summarizes the results and draws
118 conclusion.

119 **2 Methods**

120 Sections 2.1-2.5 describe the grid-connected PV-battery system modeling. The major com-
121 ponents as well as the employed mathematical models are described. Section 2.6 presents three
122 operation strategies. Section 2.7 introduces the optimization objectives. Sections 2.8 describes
123 the Genetic Algorithm.

124 **2.1 System Schematic Layout**

125 The system schematic layout is shown in Fig. 1. The system is grid-connected and consists
 126 of PV panels, battery packs, load of a typical residential building and grid. The PV panels and
 127 battery packs are respectively connected to the DC bus via MPPT (Maximal Power Point Track-
 128 ing) converters and battery controllers. The load and grid are directly connected to the 230 V
 129 AC bus. The AC and DC buses are connected through bi-directional inverters. The inverter is
 130 assumed with fixed efficiency of 0.95 (η_{inv}) [26]. The schematic layout in Fig. 1, as the sim-
 131 plified architecture of the actual system, is widely used in studies on component sizing [12] and
 132 power scheduling [19]. The sign of power flows represents their direction. The arrows above
 133 each term indicate the directions of positive power flows. Negative values indicate that the
 134 power flows are in opposite directions. For example, positive and negative $P_{B,t}$ represent dis-
 135 charging and charging the battery, respectively. When $P_{G,t}$ is zero, the system works in islanded
 136 mode. The power flow equation and constraints, including power balance and physical con-
 137 straints of system components, are detailed in Section 2.6.



138
139 Fig. 1. System schematic layout

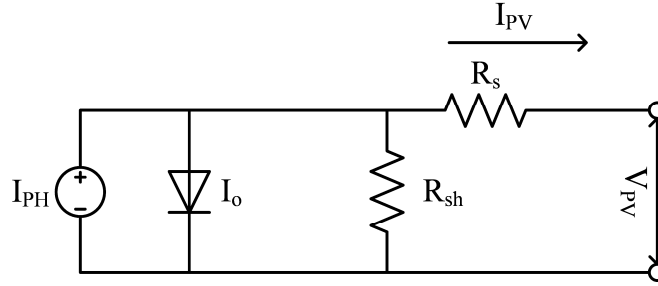
140
141 The system simulation and optimization is carried out with MATLAB® 2015b environment,
142 and part of the code is based on open-source code, OptiCE [29].

143 2.2 Single Diode Photovoltaic Model

144 The single diode model [30] is represented by the electric circuit shown in Fig. 2. The non-
145 linear I-V curve of the PV module is obtained through Eq. (1):

146
$$I_{PV} = I_{PH} - I_0 \left[\exp\left(\frac{V_{PV} + I_{PV} \cdot R_s}{a}\right) - 1 \right] - \frac{V_{PV} + I_{PV} \cdot R_s}{R_{sh}} \quad (1)$$

147 where, I_{PH} is the photocurrent (A); I_0 is the diode reverse saturation current (A); a is the ideal-
 148 ity factor (V); R_{sh} is the shunt resistance (Ω); R_s is the series resistance (Ω). They are calculated
 149 with the method in Duffie and Beckman [31] and De Soto et al.[30]. The cell temperature T_c is
 150 approximated with method in Dolara et al. [32].



151
 152 Fig. 2. Single Diode Model

153
 154 MPPT can ensure the maximal power output from PV. There are many studies about the
 155 MPPT topology design [33] and optimization [34]. In this study, MPPT controller is simulated
 156 with simplified approach described in Eq. (2) [35].

157
$$P_{PV, mpp} = \max(I_{PV} \cdot V_{PV}) \quad (2)$$

158 The PV module in this study comes from SUNTECH power and module No. is STP255-
 159 20/Wd. This polycrystalline module has a maximal power output of 255 W. The single diode
 160 model characterizing parameters are taken from the System Advisory Model [36]. The param-
 161 eters are summarized in the Appendix (Table A1).

162 The azimuth angle and tilt angle of the PV are determined as 0° and 36° , which maximize
 163 the total yearly electricity production. The hourly production profile from single PV module is
 164 shown in Fig. 3.

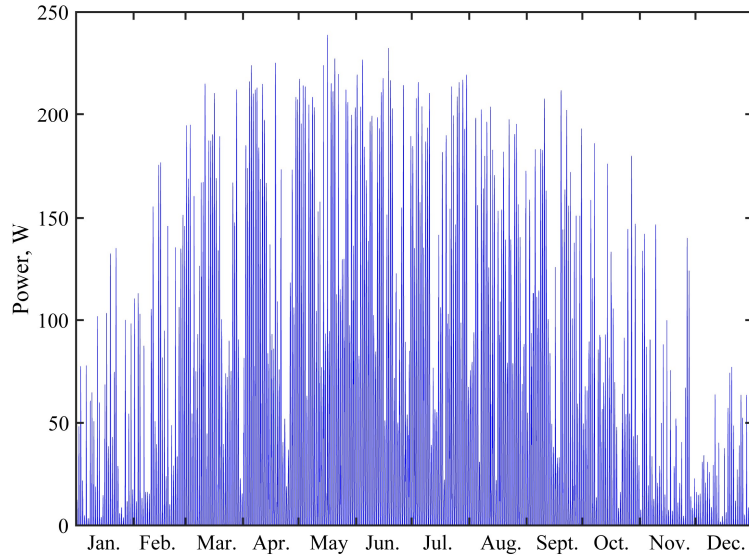


Fig. 3. Single module hourly power production with azimuth angle of 0° and tilt angle of 36°

2.3 Battery Model

There are several types of battery suitable for energy storage. Lithium ion battery outperforms other types in energy density, power density and round trip efficiency. It also has long cycle life, which means less replacement times and cost [37]. In recent years, with the strong boost from electrical vehicle industry, the lithium ion battery cost has dropped substantially and is expected to drop continuously [38]. In this study, lithium ion battery is used for energy storage.

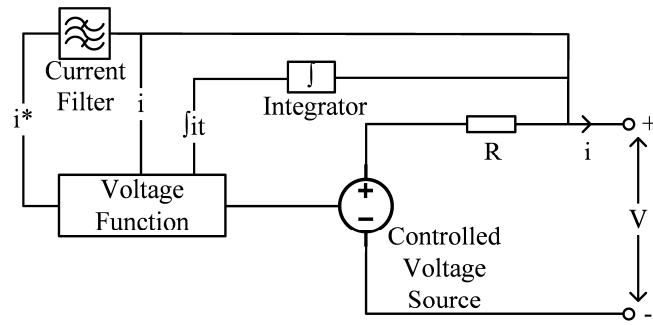
2.3.1 Battery Voltage Current Model

Improved Shepherd model, developed by Tremblay et al. [39], is employed in this study. The model describes the voltage-current relationship with consideration of SOC. The battery equivalent circuit is shown in Fig. 4. The charge and discharge characteristics are represented by Eqs. (3) and (4), respectively:

$$V = E_0 - K \frac{Q}{0.1Q + f \cdot it} \cdot i^* - K \frac{Q}{Q - f \cdot it} \int it + A \cdot e^{-B \cdot f \cdot it} - i \cdot R \quad (3)$$

$$V = E_0 - K \frac{Q}{Q - f \cdot it} \cdot i^* - K \frac{Q}{Q - f \cdot it} \int it + A \cdot e^{-B \cdot f \cdot it} - i \cdot R \quad (4)$$

182 where, V is the battery voltage (V); E_0 is the battery open circuit voltage (V); K stands for the
 183 polarization constant (V/(Ah)) and polarization resistance (Ω); Q is the battery capacity; $\int it$ is
 184 the accumulated battery charge; A is the exponential zone amplitude (V); i is the battery current;
 185 i^* is the filtered current; R is the internal resistance(Ω); B is the exponential zone time constant
 186 inverse (Ah)⁻¹.



187
 188 Fig. 4. Battery equivalent circuit

189 The battery parameters are taken from Tremblay et al. [39] and summarized in the Appendix
 190 (Table A2).

191 2.3.2 Battery Life Time Model

192 The battery lifetime is usually tested with standard charging and discharging cycles. As
 193 shown in Fig. 5, the number of life cycles decreases with the Depth of Discharge (DOD). The
 194 data from Wang et al. [40] is fitted with the three-parameter equation Eq. (5) [41].

$$195 \quad N = \frac{C}{(DOD-d)^m} \quad (5)$$

196 N is the number of cycles before the end of life (i.e. 80% remaining capacity), DOD is the
 197 depth of discharge, C , d and m are parameters to be decided through fitting.

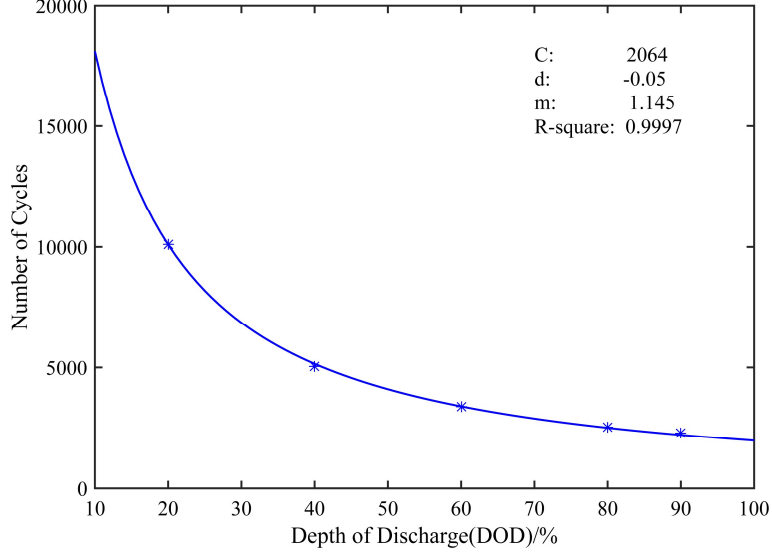


Fig. 5. Number of cycles vs. battery DOD, data from Wang et al. [40] and fitting result

198
199
200

201 The battery charge and discharge cycles under working conditions are composed of several
202 micro cycles with different DOD. The Rainflow counting method is employed to decompose
203 the complex cycles to micro cycles of different DOD. The method is firstly reported by Down-
204 ing et al.[42] and has been employed in renewable energy system study [43]. The decomposed
205 micro cycles with different DOD are further converted to standard cycles at 80% DOD (N_{red}),
206 and the cycle lifetime (L_{cycle}) is calculated with Eq. (6):

$$L_{cycle} = \frac{N_{st}}{N_{red}} = \frac{N_{st}}{\sum \left(\frac{DOD_i - d}{DOD_{ST} - d} \right)^m \times R_i} \quad (6)$$

208 where, subscript i indicates for i^{th} microcycle; N_{st} is the cycle numbers at standard test condi-
209 tion; DOD_{ST} is the DOD under standard test condition (80%); R_i is 0.5 (Half Cycle) or 1 (Full
210 cycle).

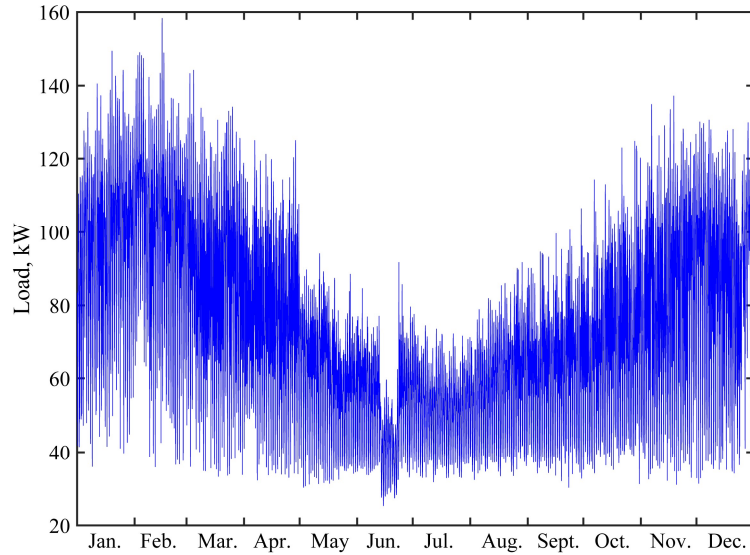
211 Battery lifetime is further evaluated with consideration of the calendar life, which is 15 years
212 in this study [44].

$$L = \min(L_{cycle}, L_{calendar}) \quad (7)$$

213
214
215

216 **2.4 Load and Weather Profiles**

217 The hourly electricity consumption (Fig. 6) of a rental multi-apartment building (Fig. 7) in
218 Gothenburg (N 57.70°, W 11.98°) is recorded from the building owner, Wallenstam AB.



219

220

Fig. 6 Hourly electricity consumption of the studied case



221

222

Fig. 7. The studied case: a rental multi-apartment building in Gothenburg

223

224 The weather data in Gothenburg — including global horizontal radiation (W/m^2), diffuse
225 horizontal radiation (W/m^2), wind speed (m/s) and ambient temperature ($^{\circ}C$) — is taken from
226 a global climatic database, Meteonorm [45].

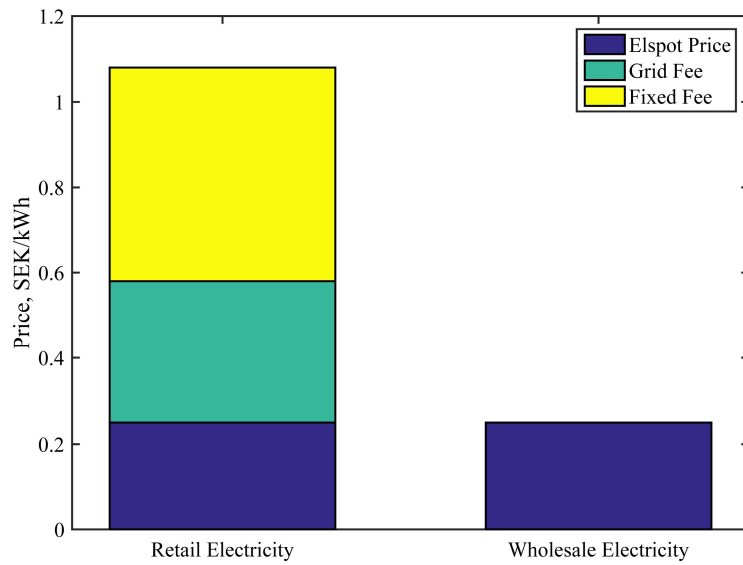
227 Seasonal mismatch can be found between PV production profile (Fig. 3) and load profile
228 (Fig. 6). During cold months, the PV production is low, while the consumption is high. Vice
229 versa during warm months. More detailed analysis about the mismatch, including average daily
230 profile in typical months, can be found in our previous study [46].

231 **2.5 Local Electricity Market and System Revenue**

232 The retail electricity price in Sweden depends on factors including client types, areas, local
233 electricity market, taxes, etc. [47]. For the studied building, the retail electricity price can be
234 decomposed into two variable components (Electricity Spot Price and Grid Fee) and one fixed
235 component (Fixed Fee), as shown in Fig. 8. The Electricity Spot Price (Elspot price) is the day
236 ahead hourly price from the bidding electricity market Nord Pool [48]. The fixed fee includes
237 energy tax, green electricity certificate, fixed grid charge, VAT, etc. The grid fee depends on
238 the maximal hourly power within the calendar year.

239 The hourly Elspot price in 2014 and its histogram are shown in Fig. 9. Throughout the whole
240 year, the Elspot price varies between 0-0.95 SEK/kWh, while it mainly remains between 0.2
241 and 0.4 SEK/kWh (8046 hours of 8760 hours).

242 Under the local electricity market policy, the economic benefits from the PV-battery system
243 can be categorized into three parts. The first part is the electricity reduction revenue ($R_{ER,y}$),
244 which comes from the load met by the PV-battery system. The self-consumed electricity price
245 is the retail price ($El_{r,t}$), which is assumed to be the Elspot price plus 0.83 SEK/kWh (including
246 grid fee and fixed fee). This is based on the current contract between the building owner and
247 distribution system operator. This is consistent with the study by Sommerfeldt et al. [5].

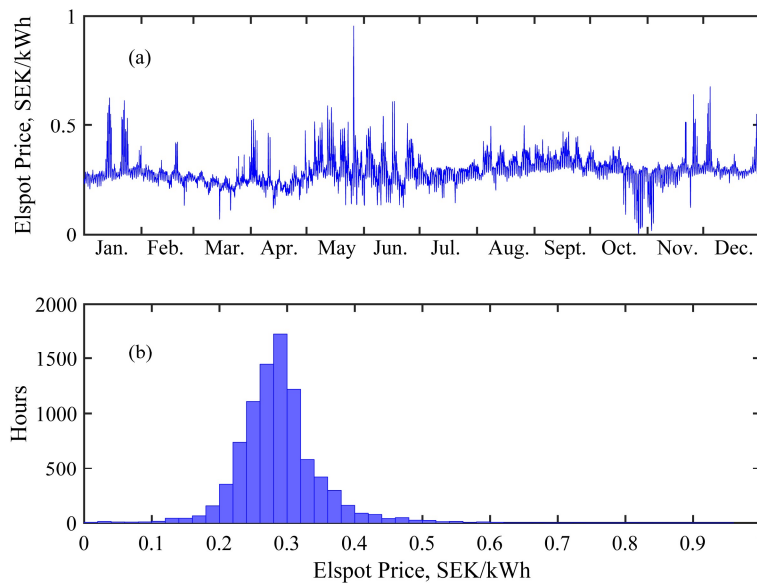


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Fig. 8. Retail and wholesale electricity price



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252

253

Fig. 9. (a) Hourly profile and (b) histogram of the Elspot price.

254 The second part is the electricity export revenue ($R_{EX,y}$), which means that the surplus elec-
 255 tricity generated by the system will be exported to the grid. The exported electricity is sold at
 256 the wholesale price ($El_{w,t}$), namely the Elspot price [5]. Although there are some subsidies for
 257 the exported electricity, like grid benefit compensation and green electricity certificate [47],
 258 they are not taken into account due to uncertainties of these subsidies in the future [6].

259 The third part originates from carrying out peak shaving, thereby decreasing the grid fee
 260 (peak shaving revenue, $R_{PS,y}$). Detailed description of the peak shaving strategy is discussed in
 261 section 2.6. The reduced grid fee is assumed to be 1500 SEK/kW·Year, which is obtained from
 262 the building owner according to the current contract.

263 The system revenue is summarized in Eq. (8):

$$264 \quad R_y = R_{ER,y} + R_{EX,y} + R_{PS,y} \quad (8)$$

265 where, $R_{ER,y}$ is calculated with Eq. (9), $R_{EX,y}$ is calculated with Eq. (10), and $R_{PS,y}$ is calcu-
 266 lated with Eq. (11).

$$267 \quad R_{ER,y} = \sum_{t=1}^{8760} (P_{L,t} - P_{Gim,t}) \cdot El_{r,t} \quad (9)$$

$$268 \quad R_{EX,y} = \sum_{t=1}^{8760} P_{Gex,t} \cdot El_{w,t} \quad (10)$$

$$269 \quad R_{PS,y} = (\max(P_{L,t}) - \max(P_{Gim,t})) \times 1500 \quad (11)$$

$$270 \quad P_{Gex,t} = \begin{cases} |P_{G,t}|, & P_{G,t} \leq 0 \\ 0, & P_{G,t} > 0 \end{cases} \quad (12)$$

$$271 \quad P_{Gim,t} = \begin{cases} P_{G,t}, & P_{G,t} > 0 \\ 0, & P_{G,t} \leq 0 \end{cases} \quad (13)$$

272 $P_{L,t}$ is the load at time t ; $P_{Gim,t}$ and $P_{Gex,t}$ are imported and exported grid power at time t .

273 2.6 Operation Strategies

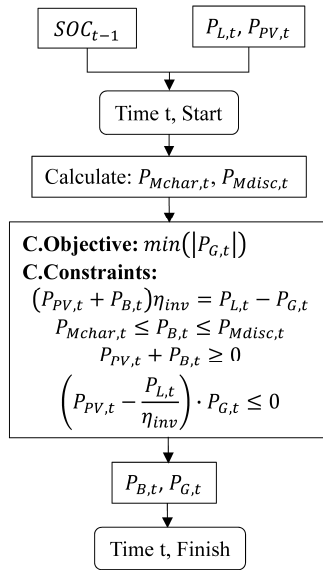
274 Three rule-based operation strategies are described in this section. Within each operation
 275 strategy, there are different operation conditions that are determined by the operation parame-
 276 ters. Each operation condition is represented by a linear programming problem. At time t , load
 277 ($P_{L,t}$) and PV production ($P_{PV,t}$) are known values. Battery power ($P_{B,t}$) and grid power ($P_{G,t}$)
 278 are determined through solving the linear programming problem.

279 2.6.1 Conventional Operation Strategy

280 The commonly employed operation strategy [14] (“Conventional Operation Strategy”) for
 281 PV-battery system works as follows: when there is excess power ($P_{PV,t} - \frac{P_{L,t}}{\eta_{inv}} > 0$), the battery

282 is charged; surplus power after charging the battery is exported to the grid; when the PV pro-
 283 duction cannot meet the load ($P_{PV,t} - \frac{P_{L,t}}{\eta_{inv}} < 0$), the battery is discharged; if energy gap still
 284 exists, the grid power is used. Batteries in the conventional operation strategy act as buffers
 285 between generation and consumption. They increase the self-consumed electricity and system
 286 revenue.

287 The operation strategy has one operation condition as depicted in Fig. 10. The objective
 288 (C.Objective) is to minimize the absolute value of grid power $P_{G,t}$. Constraint ($P_{PV,t} +$
 289 $P_{Batt,t})\eta_{inv} = P_{L,t} - P_{G,t}$ is the power flow equation, which has to be satisfied at time t to en-
 290 sure the system reliability. Constraint $(P_{PV,t} - \frac{P_{L,t}}{\eta_{inv}}) \cdot P_{G,t} \leq 0$ indicates that $P_{G,t}$ and $(P_{PV,t} -$
 291 $\frac{P_{L,t}}{\eta_{inv}})$ have opposite signs. Constraint $P_{PV,t} + P_{B,t} \geq 0$ indicates that the DC side always exports
 292 electricity to the AC side and that battery is not charged from AC side power. $P_{Mdisc,t}$ and
 293 $P_{Mchar,t}$ are the maximal discharge and charge power (discharge power has positive sign). They
 294 are determined by constraints including voltage, current and SOC, which are built inside the
 295 battery model.



296
 297
 298

Fig. 10. Flowchart of the conventional operation strategy

2.6.2 Dynamic Price Load Shifting Strategy

The PV-battery system can get extra benefits from the dynamic electricity price. The battery stores electricity at low price and provides electricity at high price. To realize this (“Dynamic Price Load Shifting Strategy” in the study), two operation parameters (high retail electricity price $El_{r,H}$ and low retail electricity price $El_{r,L}$) are introduced with referring to Dusonchet et al. [7]. The 24-hour ahead price information is fed to the controller to determine the system operation condition at time t . The flowchart of the operation strategy, which has three operation conditions, is depicted in Fig. 11.

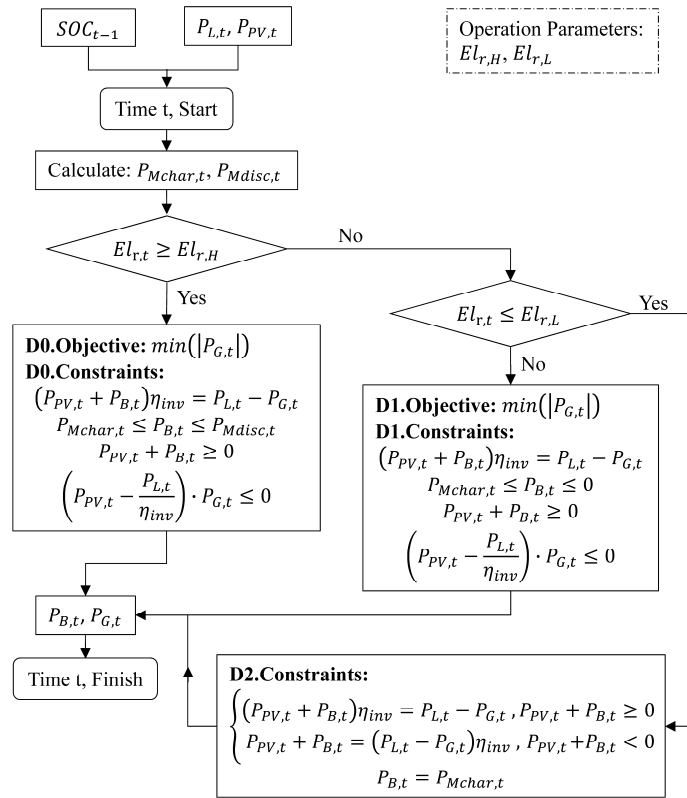


Fig. 11. Flowchart of the dynamic price load shifting strategy

If $El_{r,t}$ is higher than $El_{r,H}$, the system follows the operation condition D0 (same as the operation condition C). If $El_{r,t}$ is lower than $El_{r,L}$ (operation condition D2), battery is charged at $P_{Mchar,t}$. The system power balance is represented by two equations considering the power flow direction through the inverter. When $El_{r,t}$ is between $El_{r,L}$ and $El_{r,H}$ (operation condition D1),

314 the battery is not allowed to be discharged (constraint $P_{Mch,t} \leq P_{B,t} \leq 0$), but can be charged
315 if there is excess PV production.

316 When employing this operation strategy, three decisional variables, including battery capac-
317 ity CAP_{batt} and two operation parameters ($EL_{r,H}$ and $EL_{r,L}$), should be optimized.

318 **2.6.3 Hybrid Operation Strategy**

319 Rule-based peak shaving is achieved through maintaining high battery SOC [19]. While with
320 the conventional operation strategy, battery SOC is more flexible that it changes with the load
321 and production. There is conflict between the two operation strategies.

322 As previously analyzed in section 2.4, PV production and load show significant seasonal
323 variation. This suggests that single operation strategy (either conventional operation or peak
324 shaving strategy) may not be appropriate all the year around. During cold and dark months,
325 when PV production is low, the battery contributes little to improving the system performance
326 with the conventional operation strategy. However, electricity demand is high at this time, thus
327 the battery can be effectively used to decrease the peak power. While during warm months, the
328 peak shaving strategy is no longer advantageous, since it prevents the battery from storing ex-
329 cess electricity and increasing the revenue.

330 Based on the discussion above, an overall approach (“Hybrid Operation Strategy” in this
331 study), which includes both conventional operation and peak shaving, is proposed. The opera-
332 tion strategy includes four operation conditions, which are summarized in Fig. 12.

333 Four operation parameters (P_H , P_L , t_s and t_e) are introduced to realize the hybrid operation
334 strategy. When time t is between the conventional operation start time t_s and end time t_e , the
335 system follows the operation condition H0 (same as the operation condition C in Fig. 10). When
336 time t locates outside, the system carries out peak shaving, which is achieved through three
337 operation conditions. At each time t , the net power $P_{Net,t}$ ($P_{Net,t} = (P_{L,t} - P_{PV,t} \cdot \eta_{inv})$) is

338 compared with high power limit P_H and low power limit P_L . When $P_{Net,t}$ is higher than P_H (op-
339 eration condition H1), the battery is discharged. The discharge process maintains the grid power,
340 if possible, to be P_H (objective: $\min(P_{G,t})$ and constraint: $P_{G,t} \geq P_H$). The battery is not dis-
341 charged at the highest available power. Therefore, it reserves stored electricity and prepares for
342 the possible future peak. When $P_{Net,t}$ is lower than P_L (operation condition H3), the battery is
343 charged. The charge process is different from that in the dynamic price load shifting strategy
344 because grid power is limited below P_H . When $P_{Net,t}$ is between P_H and P_L , the battery is nei-
345 ther charged nor discharged. A Figure that presents $P_{Net,t}$, t_s , t_e , P_H and P_L is shown in Fig. 13.
346 When PV capacity is fixed, there are five decisional variables (CAP_{batt} , P_H , P_L , t_s and t_e).

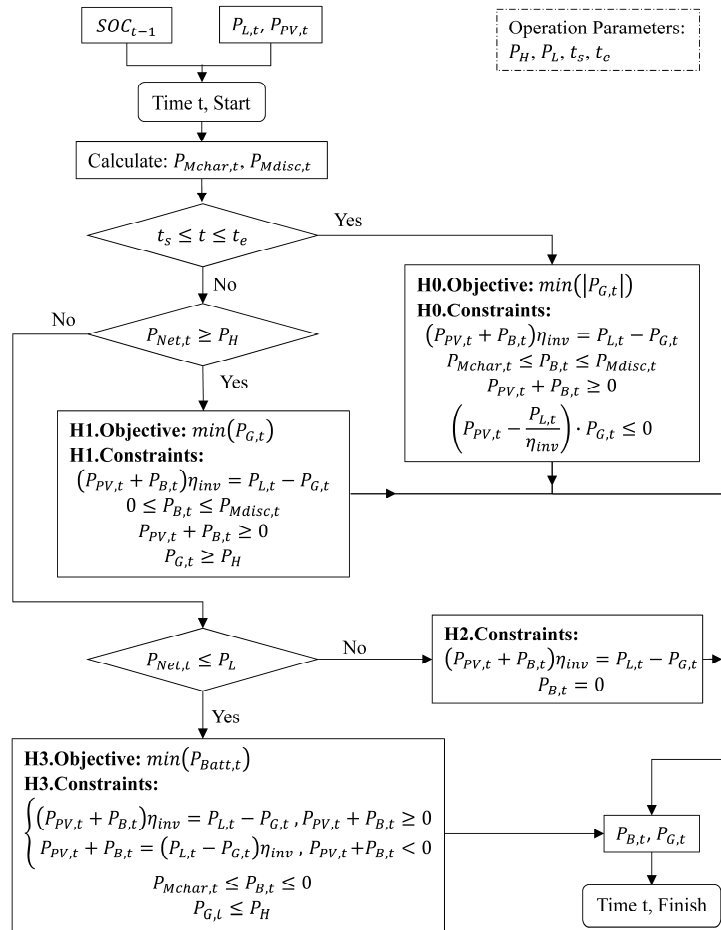


Fig. 12. Flowchart of the hybrid operation strategy

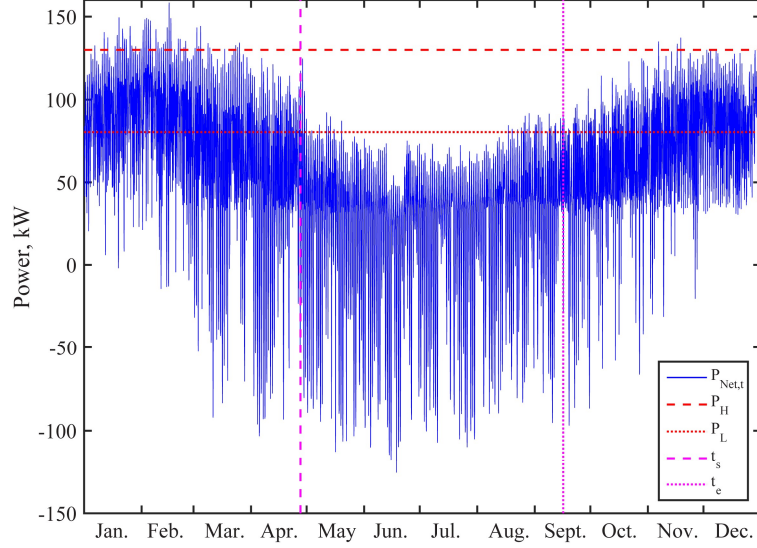


Fig. 13. Net power and the hybrid operation strategy parameters

2.7 Objectives

In renewable energy systems, there is usually trade-off between the economic and environmental goals. Two objectives, which are maximizing Net Present Value (NPV) and maximizing Self Sufficiency Ratio (SSR), are used to represent the economic goal and environmental goal, respectively.

NPV represents the economic benefits of the system. NPV (Eq. (14)) takes into account the system investment cost (Inv), Operation and Maintenance cost ($C_{O\&M,y}$), replacement cost ($C_{R,y}$) and system revenues (R_y) within the system life time (25 years). The discount rate (d_r) is chosen as 2%, considering current loan rate [49] and interest deduction for PV-related systems in Sweden [47].

$$NPV = \sum_{y=1}^{25} \frac{(R_y - C_{O\&M,y} - C_{R,y})}{(1+d_r)^{y-1}} - Inv \quad (14)$$

The cost information for battery system and PV system is listed in Table 1. Battery system price is taken from Tesla Powerwall [50], which includes battery pack and charge controller. PV system price is obtained from the Swedish PV market report of 2014 [47]. The price is turnkey cost, including inverter, installing and balance-of-plant cost. Because all components

368 in the PV-battery system has been included in either battery system or PV system, it is assumed
 369 that the PV-battery system cost equals the PV system cost and the battery system cost, as rep-
 370 resented in Eq. (15).

$$371 \quad Inv = UIC_{batt} \cdot CAP_{batt} + UIC_{PV} \cdot CAP_{PV} \quad (15)$$

372 Table 1. Unit investment cost, lifetime and O&M ratio of different components.

Module	Unit Investment Cost (UIC)	Life Time	O&M Ratio ($r_{O\&M}$)
Lithium ion Battery System	3966 SEK/kWh	Life time model	0.5%/Year
PV system	12900 SEK/kW _p	25 Years	1%/Year

373

374 $C_{R,y}$ is assumed same as the investment cost. The battery replacement time is determined by
 375 the lifetime model. $C_{O\&M,y}$ is assumed same in each year. It is calculated as:

$$376 \quad C_{O\&M,y} = UIC_{batt} \cdot CAP_{batt} \cdot r_{O\&M,batt} + UIC_{PV} \cdot CAP_{PV} \cdot r_{O\&M,PV} \quad (16)$$

377 SSR is another objective. SSR is defined with Eq. (17) [6]. It represents the renewable energy
 378 penetration level of the system. The higher the SSR, the “greener” the system is.

$$379 \quad SSR = \left(1 - \frac{\sum_1^{8760} P_{Gim,t}}{\sum_1^{8760} P_{L,t}} \right) \cdot 100\% \quad (17)$$

380 2.8 Genetic Algorithm

381 During the system planning stage of grid-connected PV-battery system, the decisional vari-
 382 ables include component sizes and operation parameters (Section 2.6). The objectives include
 383 NPV and SSR. The attempt to go through all the combinations of decisional variables is unsuit-
 384 able because of the extremely large amount of possible combinations and high computational
 385 time (Appendix, Table A3). Moreover, due to the complexity of the system (non-linear, non-
 386 differentiable), traditional iterative methods cannot be applied either. To solve this multi-objec-
 387 tive optimization problem, Genetic Algorithm (GA) is employed. As a population-based ap-
 388 proach, GA is one of the most popular heuristic approach to multi-objective optimization prob-
 389 lems [51]. Its advantages mainly include supporting black-box simulation models, being suita-
 390 ble for both continuous and discreet problem, etc. Moreover, it is inherently parallel, which
 391 makes it quite advantageous to carry out distributed computation. It has been extensively used

392 and tested in the studies of renewable energy systems. Examples are summarized in a review
 393 paper of Chauhan and Saini [52].

394 The overall flowchart of the optimization process is shown in Fig. 14. The employed GA
 395 comes from the global optimization toolbox of MATLAB® and the configuration parameters
 396 (Table 2) are following MATLAB® suggestion. This study employs the adaptive stop criterion.
 397 If the weighted average relative change in the spread of the Pareto solutions over 100 (Stall
 398 Generations) generations is less than 0.0001 (Function Tolerance), the optimization algorithm
 399 stops. To avoid endless iterations when the optimization fails to converge, additional stop cri-
 400 terion with maximal generations of 300, is added. In this study, all the performed optimizations
 401 are terminated by the adaptive stop criterion.

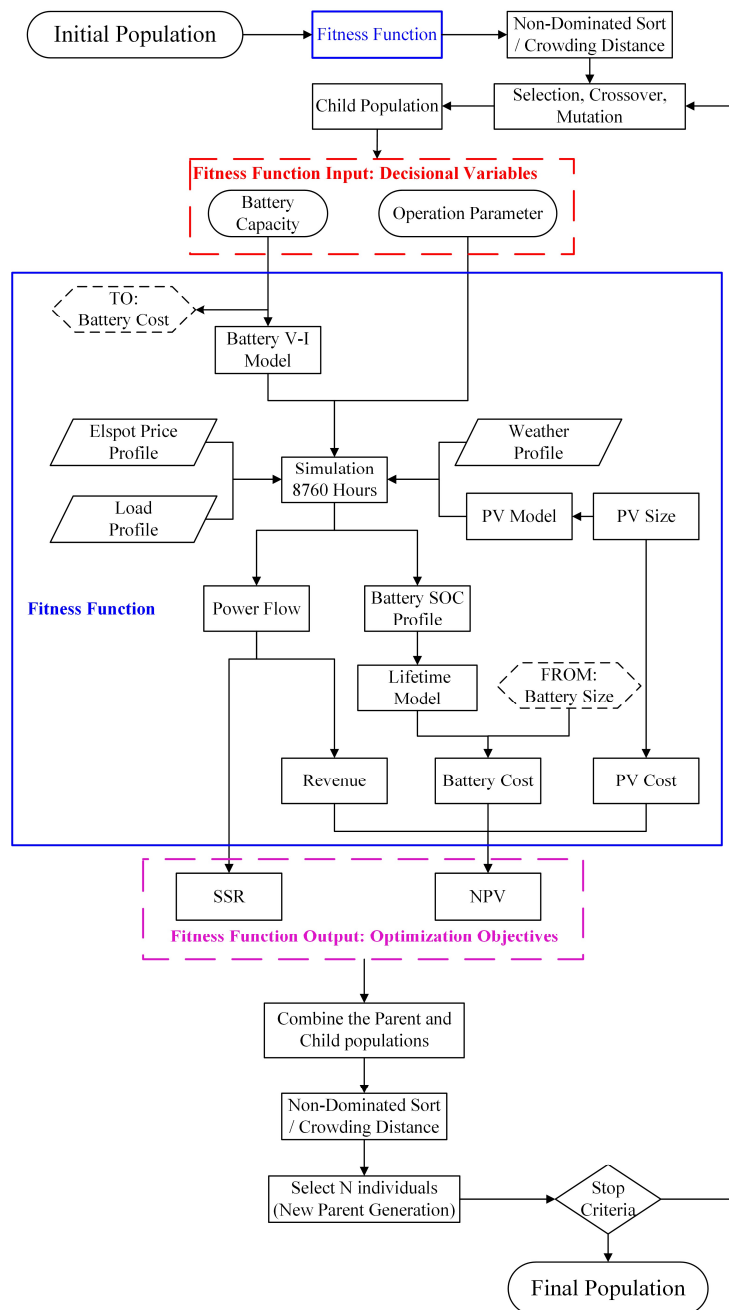
402 Table 2. GA configuration parameters

GA Configuration Parameter	Description
Population size	50* / 200
Algorithm	Variant of NSGA II [53]
Elite fraction	0.05
Distance crowding	Phenotype (function space)
Pareto fraction	0.6* / 0.35
Selection	Tournament
Tournament size	4
Crossover function	Heuristic
Crossover ratio	1.2
Mutation function	Adaptive Feasible
Maximal generations	300
Stall generations	100
Function tolerance	0.0001

403 * For GA with the dynamic price load shifting strategy (Section 3.2)

404
 405 Ideally, GA helps to solve the optimization problem and provide the relationship between
 406 SSR and NPV in the form of Pareto front. However, as GA is a heuristic tool, it cannot guaran-
 407 tee to reach the globally optimal solution. The near-optimal Pareto front is thus obtained. It
 408 should be noted that GA employs unguided mutation, which could lead to convergence at local

409 minima. To avoid this problem, this study repeats the optimization with different configuration
 410 parameters. Other heuristic tools, including Ant Colony Optimization and Particle Swarm Op-
 411 timization, are used in the study of renewable systems and might also be applicable to this study.
 412 However, the comparison between different optimization tools is not carried out because be-
 413 yond the scope of this study.



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415

416

Fig. 14. Flowchart of the optimization process by GA

417 **3 Results and Discussion**

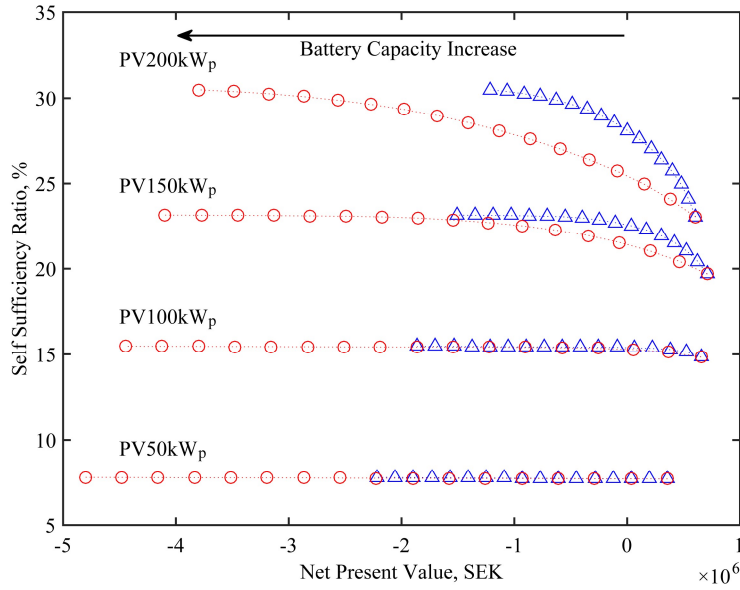
418 Three rule-based operation strategies are compared in this section. When under the conven-
419 tional operation strategy, the system's SSR and NPV are obtained with different combinations
420 of PV capacities and battery capacities. For the system under the dynamic price load shifting
421 strategy and the hybrid operation strategy, the relationships between SSR and NPV are repre-
422 sented by the near-optimal Pareto fronts, which are obtained from GA.

423 **3.1 Conventional Operation Strategy**

424 The system simulations are carried out with different combinations of battery capacities (0
425 to 800 kWh, 50 kWh interval) and PV capacities (50, 100, 150 and 200 kW_p). The obtained
426 SSR and NPV are shown in Fig. 15 (Red Circle Marker).

427 At fixed PV size, with the increase of battery capacity, SSR increases until reaching a plateau,
428 while the NPV continuously decreases. This indicates that employing battery will increase the
429 renewable energy penetration level, while the economic performance becomes poorer. The ben-
430 efit of increased self-consumed electricity is lower than the battery cost. Therefore, it is not
431 attractive for users to install battery for PV systems.

432 A sensitivity study about the battery price is carried out. When the battery price drops 50%,
433 SSR and NPV of different combinations are shown in Fig. 15 (Blue Triangle Marker). The
434 economic performance is improved. However, the highest NPV values are still with the systems
435 without battery. It indicates that having battery is not economically beneficial even when the
436 battery price drops 50%. The sensitivity study emphasizes that the battery must be better uti-
437 lized to achieve more economic benefits.



438

439 Fig. 15. SSR and NPV for different combinations of PV capacities and battery capacities (Red Circle Marker:

440

100% Battery Price, Blue Triangle Marker: 50% Battery Price)

441

442 3.2 Dynamic Price Load Shifting Strategy

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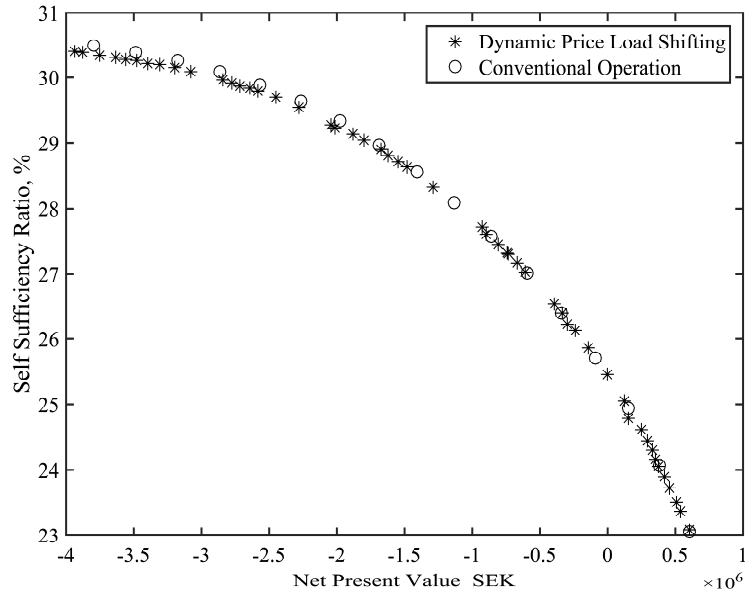
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In this section, the dynamic price load shifting strategy is compared with the conventional operation strategy at fixed PV capacity of 200 kW_p. As shown in Fig. 16, the near-optimal Pareto front for the dynamic price load shifting strategy follows the SSR-NPV curve of the conventional operation strategy. This indicates that the dynamic price load shifting strategy cannot help to improve the system performance regarding SSR and NPV. In the near-optimal Pareto front population, the individuals' decisional variables with respect to their NPV are shown in Fig. 17. The CAP_{batt} -NPV curve from the dynamic price load shifting strategy overlaps with that from the conventional operation strategy. The high ($EL_{r,H}$) and low ($EL_{r,L}$) retail electricity price (Fig. 17b) are around 1.05 and 0.85 SEK/kWh, corresponding to 0.22 and 0.02 SEK/kWh of the Elspot Price. The Elspot price histogram in Fig. 9b shows that there are 712 hours when the Elspot price is lower than 0.22 SEK/kWh. This indicates that at most time of the year, the system follows the operation condition D0, which is identical to the conventional operation strategy.

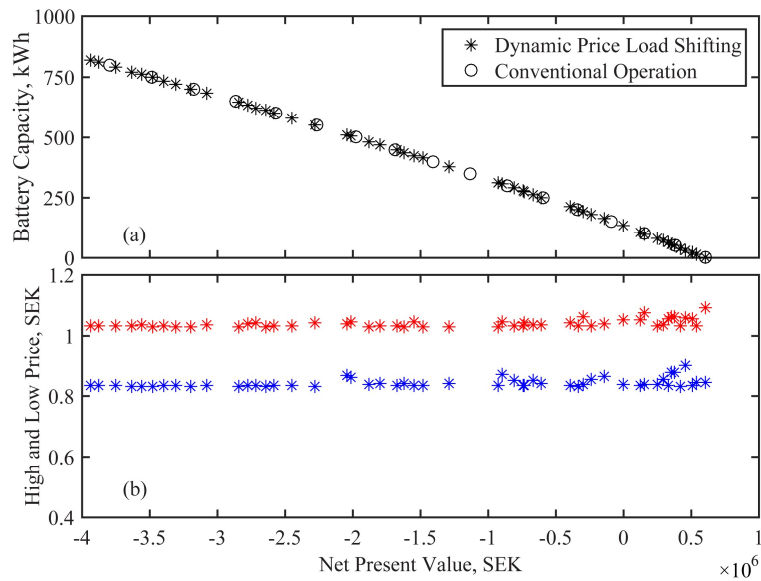


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Fig. 16. Comparison between the conventional operation strategy and the dynamic price load shifting strategy

458



459

460

Fig. 17. Variables in the near-optimal Pareto front population: (a) battery capacity (CAP_{batt}) and (b) high ($EL_{r,H}$)

461

and low ($EL_{r,L}$) retail electricity price

462

463

Comparison between the two strategies suggests that the variation in the retail price is not

464

large enough for the dynamic price load shifting strategy to gain extra benefits. Graditi et al.

465

carried out a techno-economic analysis of the load shifting strategy with battery storage system

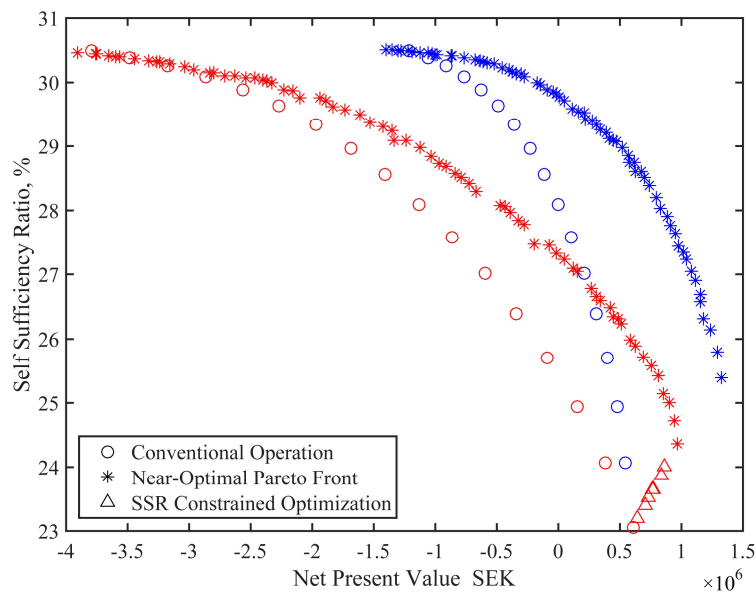
466

under TOU tariff in Italy [54]. The study also concludes that employing lithium ion battery for

467 load shifting is economically unfavorable under the current TOU tariff. However, it should be
 468 noted that electricity market is under rapid development. Stable and cheap hydro and nuclear
 469 power accounts for the major part of electricity supply now (83.7% in 2014 [55]). With the
 470 increasing capacity of intermittent renewable energy and the gradually shutting down of nuclear
 471 power plants, higher variation in the electricity market is expected.

472 3.3 Hybrid Operation Strategy

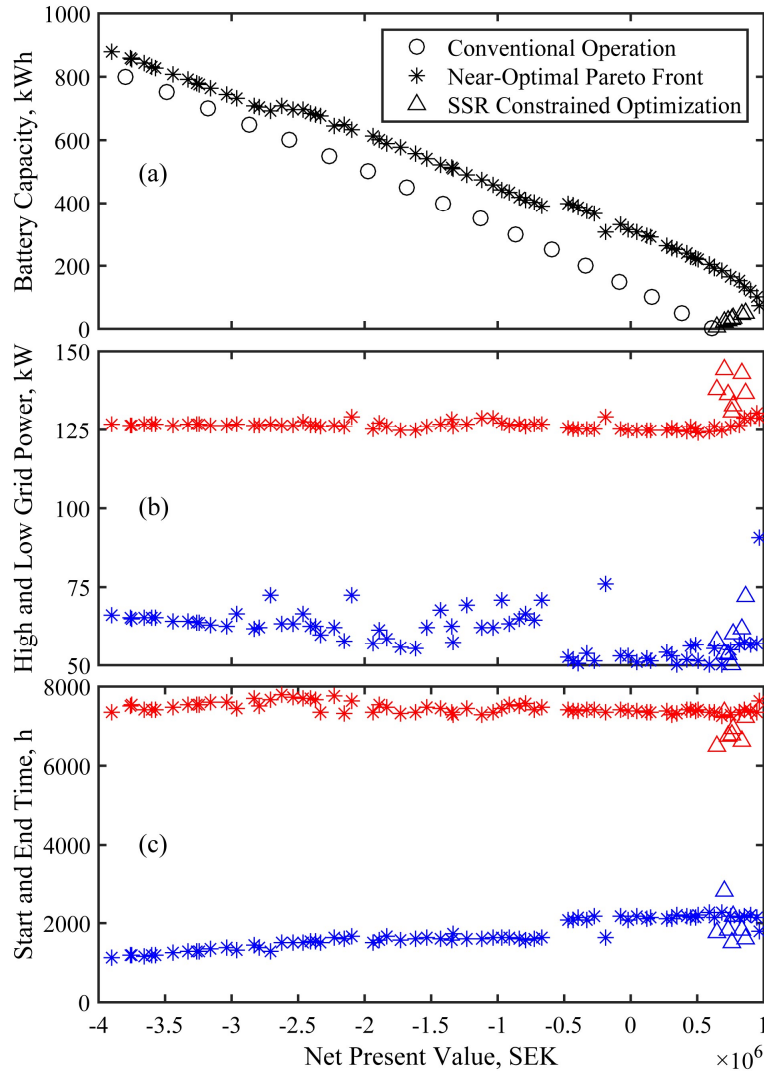
473 In this section, the hybrid operation strategy is employed and compared with the conven-
 474 tional operation strategy. The PV capacity is also fixed at 200 kW_p. As shown in Fig. 18 (Red
 475 Marker), the hybrid operation strategy (near-optimal Pareto front) outperforms the conventional
 476 operation strategy. At low SSR, the hybrid operation strategy has higher NPV than the conven-
 477 tional operation strategy. The NPV difference gradually decreases with the increase of SSR.



478
 479 Fig. 18. Comparison between the conventional operation strategy and the hybrid operation strategy (Red Marker:
 480 100% Battery Price, Blue Marker:50% Battery Price)

481 The individuals' decisional variables in the near-optimal Pareto front population are shown
 482 in Fig. 19. The individual with the highest NPV (9.7×10^5 SEK) as well as the lowest SSR
 483 (24.4 %) has the smallest battery capacity (72 kWh). With the same battery capacity, if the
 484 system only follows the conventional operation strategy, NPV and SSR are 2.8×10^5 SEK and
 485

486 24.5 %; while if the system only follows the peak shaving strategy, NPV and SSR are 8.3×10^5
 487 SEK and 23.0 %. The hybrid operation strategy achieves higher NPV than both conventional
 488 operation and peak shaving strategies, while slightly lower SSR than the conventional operation
 489 strategy.



490
 491 Fig. 19. Variables in the near-optimal Pareto front population: (a) battery capacity (CAP_{batt}); (b) high (P_H) and
 492 low (P_L) power limit; (c) conventional operation start (t_s) and end (t_e) time

493
 494 The individual with smaller battery capacity (than 72 kWh) is not obtained through GA. This
 495 indicates that the individuals with smaller battery capacities are determined as dominated solu-
 496 tions, and are excluded from the Elitism process.

497 Another multi-objective optimization, which constrains battery capacity between 0 and 72
498 kWh, is carried out. The obtained individuals are not scattered but overlapped (results not
499 shown). Battery capacities in the obtained individuals are crowded between 71 and 72 kWh.
500 This indicates that with small battery capacity, SSR and NPV no longer conflict with each other,
501 since otherwise near-optimal Pareto front rather than overlapped individuals would be obtained.
502 To complete the SSR-NPV relationship, the missing individuals are supplemented through sin-
503 gular objective GA optimization with constraint of SSR. In this approach, SSR is constrained
504 lower than certain set value through a non-linear constraint function, and single objective opti-
505 mization is carried out to get the individual which achieves the highest NPV while meeting the
506 constraint of SSR. This approach is repeated with different SSR set values, and the obtained
507 individuals' SSR, NPV and variables are shown in Fig. 18 and Fig. 19 (Triangle Marker).

508 The SSR-NPV relationship (Fig. 18) and the CAP_{batt} -NPV relationship (Fig. 19) indicate
509 that with the increase of battery capacity, both SSR and NPV firstly increase until the turning
510 point. After that, with the increase of battery capacity, SSR increases while NPV decreases. The
511 turning point represents the maximal NPV that the system can achieve under the hybrid opera-
512 tion strategy.

513 The results indicate that when battery is smaller than 72 kWh, the previously conflicting
514 SSR and NPV change to be consistent. The hybrid operation strategy provides incentive for
515 deploying batteries to PV system, because both higher renewable energy penetration level and
516 better economic performance can be achieved. If batteries are combined with PV, the local grid
517 will also benefit from the improved power quality.

518 A sensitivity study about the battery price is also carried out. If the battery price drops 50%,
519 the near-optimal Pareto front with the hybrid operation strategy and the SSR-NPV curve with
520 the conventional operation strategy will change, as shown in Fig. 18 (Blue Marker). Compared
521 with full price scenarios, the NPV difference between the hybrid operation strategy and the

522 conventional operation strategy enlarges, indicating that the hybrid operation strategy becomes
 523 more favorable with the decrease of battery price.

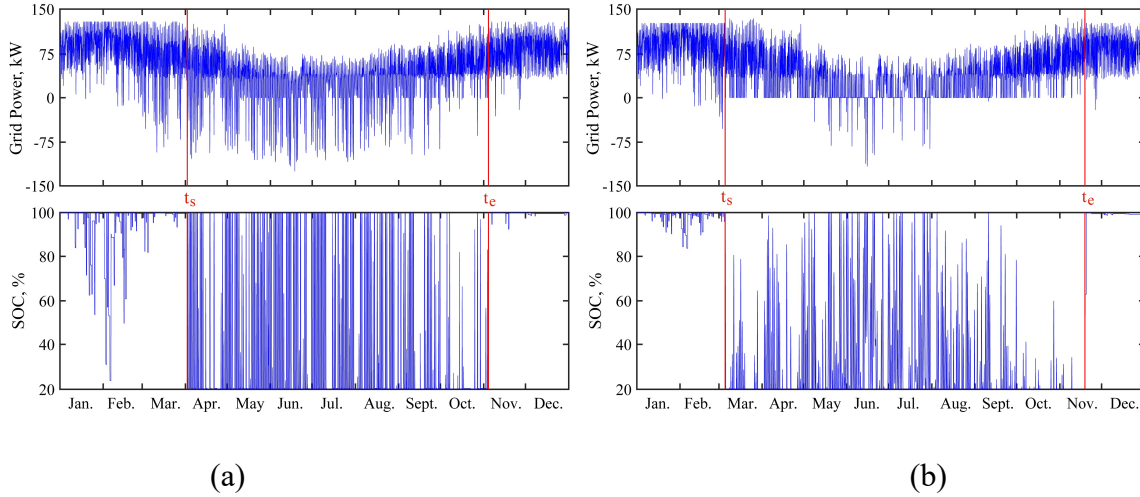
524 As shown in Fig. 19b, with the increase of battery capacity, the assigned time for conven-
 525 tional operation continuously increases (t_s decreases and t_e remains almost the same). The rea-
 526 son is further analyzed through two example individuals, which have relatively small and large
 527 battery capacity, respectively. The selected individuals' decisional variables, system revenue in
 528 the first year and peak power information are presented in Table 3. The two individuals' $P_{G,t}$
 529 and SOC profiles are shown in Fig. 20.

530 Table 3. Detailed information of two individuals from the near-optimal Pareto front.

Item	Small Battery Individual	Large Battery Individual
NPV (SEK)	901184	-2539753
SSR	25.00%	30.07%
CAP_{batt} (kWh)	122	696
P_H (kW)	129	126
P_L (kW)	57	63
t_s (h)	2192	1523
t_e (h)	7378	7728
$R_{ER,1}$ (SEK)	183193	219603
$R_{EX,1}$ (SEK)	11439	1201
$R_{PS,1}$ (SEK)	44143	31650
R_1 (SEK)	238775	252454
$P_{G,peak}$ (kW)	129	137
t_{peak} (h)	548	7723

531
 532 The $P_{G,t}$ and SOC profiles indicate that both individuals carry out peak shaving during cold
 533 and dark months and follow conventional operation during warm months. The system revenue
 534 (R_1) of the small battery individual does not have significant difference with the large battery
 535 individual. The decomposed revenue indicates that the increase in $R_{EX,1}$ (export revenue) and
 536 $R_{PS,1}$ (peak shaving revenue) largely compensates the decrease in $R_{ER,1}$ (electricity reduction
 537 revenue). As shown in Fig. 20, more electricity is exported (negative grid power) with the small

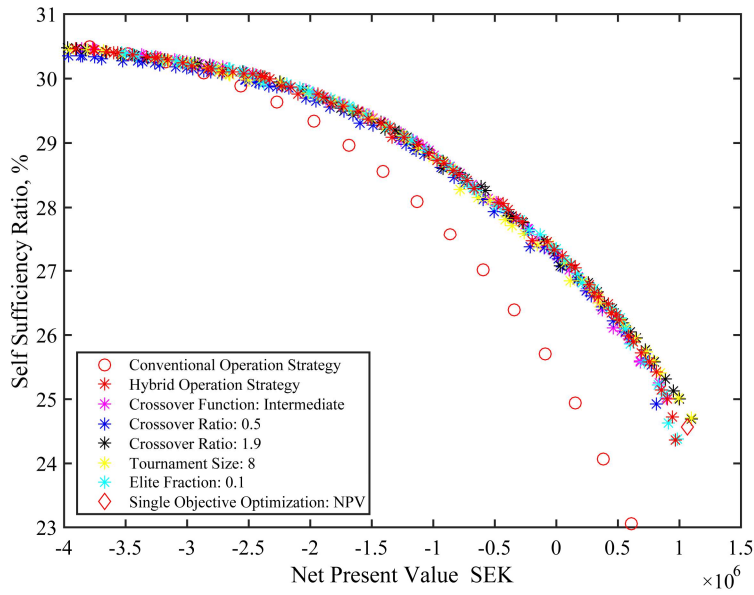
538 battery individual, because its ability for storing excess electricity is lower. Thus, it is less ad-
 539 vantageous for small battery individual to follow conventional operation than large battery in-
 540 dividual. Therefore, GA assigns more time to carry out peak shaving with the smaller battery
 541 individual.



544 Fig. 20. $P_{G,t}$ and SOC of the individual with (a) small and (b) large battery capacity

545

546 As stated in Section 2.8, GA might lead to the convergence at local minima. To avoid this
 547 problem as well as to ensure reproducible results, the optimizations are repeated with different
 548 GA configuration parameters. As shown in Fig. 21, the near-optimal solutions with different
 549 GA configuration parameters overlap with each other, indicating good reproducibility. Some
 550 individuals dominate the individuals of the base case (red asterisk), indicating that GA cannot
 551 guarantee optimal solution. However, because of the optimization problem complexity (non-
 552 linear, non-differentiable), the optimality gap cannot be estimated currently. As depicted in Fig.
 553 21, it can be also concluded that the hybrid operation strategy shows better performance com-
 554 pared to the conventional operation strategy. Indeed, all the near-optimal Pareto fronts outper-
 555 form the SSR-NPV curve of the conventional operation strategy.



556

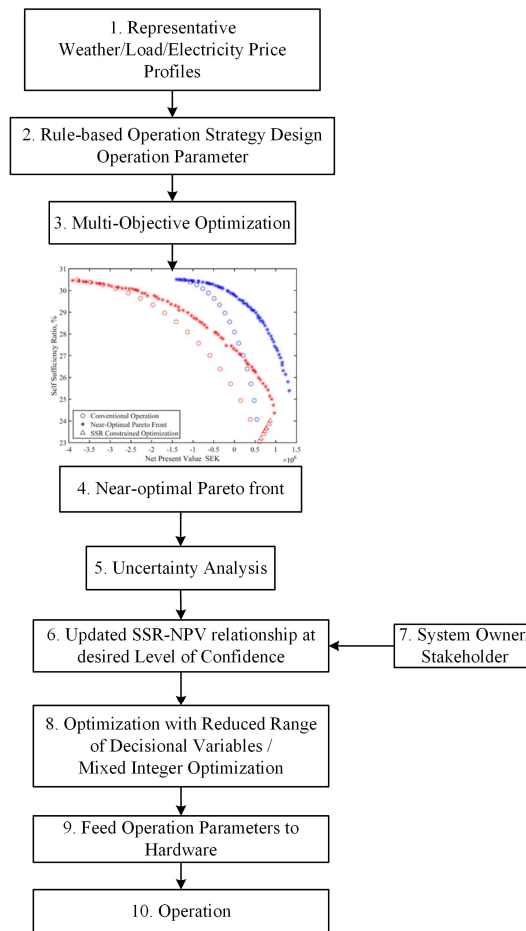
557 Fig. 21. The near-optimal Pareto fronts obtained from GA with different configuration parameters (Base case:
 558 red asterisk, with configuration parameters in Table 2. Changes to the base case are shown in the legend).

559

560 3.4 Overall Approach with Rule-based Operation Strategy and Practical Evaluation

561 The flowchart of employing rule-based operation strategy is summarized in Fig. 22. The
 562 flowchart covers stages from system planning to operation. This study focuses on Steps 1-4 and
 563 obtains the near-optimal Pareto front. Steps 1-4 are deterministic since they employ representa-
 564 tive weather profile, load profile, etc. to obtain the component size and operation parameters.
 565 Within Steps 1-4, the uncertainties of weather and load are taken into account, since the em-
 566 ployed representative hourly profiles reflect not only the seasonal and daily variations but also
 567 the randomness of the values. Moreover, the proposed approach can be easily extended to cover
 568 longer period of simulation (i.e. 3 years), which helps to better address the un-certainty issue
 569 with longer typical profiles. However, because one-year simulation with hourly interval is
 570 widely accepted in current researches [14], this study does not extend to longer period simula-
 571 tion. Steps 1-4 are the foundation for further analysis, and the following steps are briefly illus-
 572 trated to give an overview.

573 Uncertainty analysis is important for system sizing in achieving robust system design. The
574 uncertainties in both generation and consumption can influence the system performance both
575 in terms of NPV and SSR. For each deterministic individual from the near-optimal Pareto front,
576 Monte Carlo simulation can be used to evaluate NPV and SSR at certain Level of Confidence
577 (LOC) [56].



578
579 Fig. 22. The overall flowchart of the approach with rule-based operation strategy: from system planning to oper-
580 ation.

581
582 The uncertain parameters, as well as their range and form of distribution, are provided in
583 Table 4. The desired LOC are set as 95%. The system simulations (with determined decisional
584 variables) are repeated 2000 times with random uncertain parameters, which are subjected to
585 the given distribution. An example that refers to the small battery individual of Table 3 is pro-
586 vided in Fig. 23. The NPV and SSR at LOC 95% are respectively determined when the number

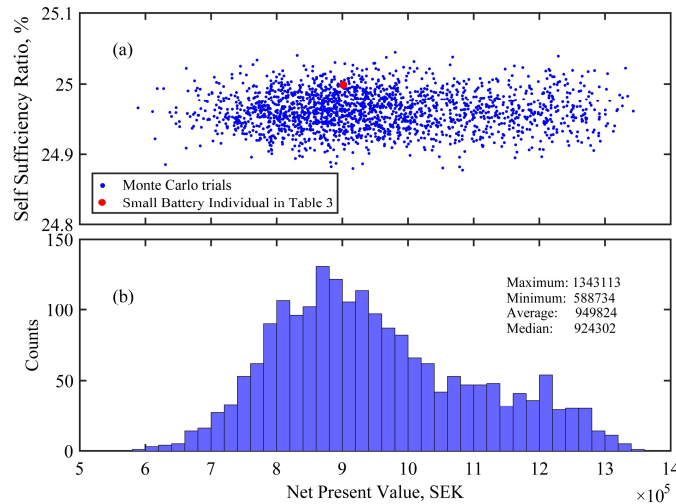
587 of trials with higher value is 1900 (95% of 2000). The NPV and SSR at LOC 95% are deter-
 588 mined as 738346 SEK and 24.91 %, respectively. The current uncertainty analysis assumes
 589 decisional variables remain unchanged regardless of the PV production and load. However, the
 590 operation parameters can be adjusted to fit into the variation in production and load. Less vari-
 591 ation and better economic performance can be expected.

592 Table 4. Uncertainties in PV production, load and Elspot price

Uncertain Parameter	Distribution
$P_{L,t}$	Uniform ($\delta=0.10$)
$P_{PV,t}$	Uniform ($\delta=0.10$)
$El_{w,t}$	Uniform ($\delta=0.10$)

593 δ is the variation limit as a fraction of mean value.

594



595

596 Fig. 23. Uncertainty analysis of the small battery individual from Table 3: (a) scattered plot of SSR vs NPV; (b)
 597 histogram of NPV.

598

599 With the Monte Carlo simulations, all the individuals of the near-optimal Pareto front can
 600 be updated with SSR and NPV at certain LOC. The updated SSR-NPV relationship can give
 601 intuitive support for decision-making. Within the following steps, system owner's input (i.e.
 602 expected SSR) is required to narrow down the search range; and practical constraint, such as
 603 the available battery capacities, need to be included. In Step 9, the hardware layout of carrying

604 out the rule-based control can refer to the study by Graditi et al. [57], which presented a proto-
605 type for the interface between grid and PV-Lithium ion batteries. The computational require-
606 ment during operation is limited because the controller only needs to follow certain rules.

607 In summary, the proposed approach helps the system owners and designers during the sys-
608 tem planning stage to decide the battery capacity with consideration of the operation after in-
609 stallation. The obtained rule-based operation strategy is used to run the system during operation
610 stage.

611 The battery sizing methods in Ru et al. [26], Gitizadeh et al. [27] and Khalilpour et al. [28]
612 rely on the correct forecasting data. The methods throw little light on the real condition opera-
613 tion when forecasting data cannot be certain. In other words, the optimal scheduling cannot be
614 guaranteed (an example of peak shaving failure due to forecasting error is given in Riffonneau
615 et al. [19]). Moreover, the availability of forecasting equipment has to be practically evaluated
616 for the distributed prosumers.

617 This study employs a different approach. The optimization process obtains battery capacity
618 and operation parameters. The obtained operation parameters are then used in rule-based oper-
619 ation strategy for real condition operation. The approach actually merges the component sizing
620 and real condition operation as a whole. Moreover, the proposed approach avoids the necessity
621 of forecasting and reduces the complexity of the system. More rapid industrial development
622 can be expected.

623 One major concern regarding the proposed approach is the applicability to other cases. The
624 studied case has seasonal mismatch between generation and consumption, which provides the
625 chance of employing the proposed hybrid operation strategy. Moreover, the studied case locates
626 in a deregulated electricity market, which provides the building owner access to these economic
627 opportunities [58]. The proposed approach should be tested with more cases and more sophis-
628 ticated rule-based operation strategies.

629 The accuracy of the system is also questioned by the assumptions. The major assumptions
630 include fixed inverter efficiency [26] and that the electricity price policy of the local electricity
631 market remains unchanged within the project life. The system employs single diode PV model
632 [30] and Improved Shepherd Model [39], which respectively has their own assumptions. How-
633 ever, it should also be noted that the approach applies to non-linear and non-differentiable sys-
634 tems. So more detailed models can be incorporated in future works.

635 **4 Conclusion**

636 During the planning of grid-connected PV-battery systems, the optimal component sizes
637 need to be determined with consideration of the system operation. In this study, a method that
638 optimizes the battery capacity as well as the rule-based operation strategy is carried out with
639 the multi-objective Genetic Algorithm. The grid-connected PV-battery system is simulated us-
640 ing single diode PV model and Improved Shepherd battery model. Three rule-based operation
641 strategies are designed and compared, drawing the following conclusion:

642 1) The conventional operation strategy does not bring in economic incentive for PV system
643 to deploy battery even when battery price is lowered 50%.

644 2) The dynamic price load shifting strategy aims to benefit from the electricity price differ-
645 ence. However, the electricity price variation of the studied case is not significant enough for
646 this operation strategy to gain benefits.

647 3) The hybrid operation strategy outperforms the conventional operation strategy. Sensitivity
648 study indicates that lowering battery price makes the hybrid operation strategy more favorable.
649 For the studied case, when the battery capacity is larger than 72 kWh, there is a trade-off be-
650 tween SSR and NPV. Whereas when the battery capacity is smaller than 72 kWh, SSR and
651 NPV increase together with the battery capacity. The hybrid operation strategy assigns more
652 operation time to carry out peak shaving for individual with smaller battery capacity.

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657 building load profile and Nord Pool Spot with market price data. Yang Zhang acknowledges
658 the financial support from China Scholarship Council (CSC).

660 Table A1. Characterizing parameters in PV single diode model [36].

Parameter	Explanation	Value
G_{STC} (W/m ²)	Irradiance at Standard Test Condition (STC)	1000
T_{STC} (K)	STC Temperature (Cell Temperature)	298.15
$I_{PH,STC}$ (A)	Photocurrent at STC	8.731
μ_{ISC} (A/K)	Short current temperature coefficient	0.005
$I_{o,STC}$ (A)	Diode reverse saturation current	4.41×10^{-10}
$E_{g,STC}$ (eV)	Material band gap energy at STC	1.121
a_{STC} (V)	Ideality factor at STC	1.5819
$R_{sh,STC}$ (Ω)	Shunt Resistance at STC	1519.11
R_s (Ω)	Series Resistance	0.232
$NOCT$ ($^{\circ}C$)	Nominal Operating Cell Temperature	43.7

661

662 Table A2. Battery model parameters [39].

Battery Type	Lithium Ion
Nominal Voltage (V)	3.3
Nominal Capacity (Ah)	2.3
E_0 (V)	3.366
K (V/(Ah) or Ω)	0.0076
R (Ω)	0.01
A (V)	0.26422
B (Ah) ⁻¹	26.5487
Cut off voltage(V)	3
Charge control voltage (V)	4
Maximal Current	C/3

663

664 Table A3. Estimated computational time for covering possible combinations of the decisional variables

Decisional Variables	Range	Interval	Points
CAP_{batt} (kWh)	0-1000	10	100
P_H (kW)	110-160	5	10
P_L (kW)	50-120	5	14
t_s	1000-3000	100	20
t_e	6000-8000	100	20
Total Combinations			5600000
Estimated Computational Time (Parallel Computing with i7-4790 CPU)			1.3 Years

665

666 **References:**

- 667 [1] IEA-PVPS. Snapshot of global PV markets. 2015 <<http://www.iea-pvps.org/>>.
- 668 [2] IEA-PVPS. Trends 2014 in Photovoltaic applications. 2014 <<http://www.iea-pvps.org/>>.
- 669 [3] Marzband M, Moghaddam MM, Akorede MF, Khomeyrani G. Adaptive load shedding scheme for
670 frequency stability enhancement in microgrids. *Electr Pow Syst Res* 2016; 140: 78-86.
- 671 [4] Teleke S, Baran ME, Bhattacharya S, Huang AQ. Rule-based control of battery energy storage for
672 dispatching intermittent renewable sources. *IEEE Trans Sustain Energy* 2010; 1: 117-24.
- 673 [5] Sommerfeldt N, Madani H. On the use of hourly pricing in techno-economic analyses for solar
674 photovoltaic systems. *Energy Convers Manage* 2015; 102: 180-9.
- 675 [6] Luthander R, Widén J, Nilsson D, Palm J. Photovoltaic self-consumption in buildings: A review.
676 *Appl Energy* 2015; 142: 80-94.
- 677 [7] Dusonchet L, Ippolito MG, Telaretti E, Zizzo G, Graditi G. An optimal operating strategy for
678 combined RES-based generators and electric storage systems for load shifting applications. Fourth
679 International Conference on Power Engineering, Energy and Electrical Drives 2013. pp. 552-7.
- 680 [8] Zheng M, Meinrenken CJ, Lackner KS. Smart households: Dispatch strategies and economic
681 analysis of distributed energy storage for residential peak shaving. *Appl Energy* 2015; 147: 246-57.
- 682 [9] Lu Y, Wang S, Shan K. Design optimization and optimal control of grid-connected and standalone
683 nearly/net zero energy buildings. *Appl Energy* 2015; 155: 463-77.
- 684 [10] Yang H, Zhou W, Lou C. Optimal design and techno-economic analysis of a hybrid solar–wind
685 power generation system. *Appl Energy* 2009; 86: 163-9.
- 686 [11] Paliwal P, Patidar NP, Nema RK. Determination of reliability constrained optimal resource mix for
687 an autonomous hybrid power system using particle swarm optimization. *Renew Energy* 2014; 63:
688 194-204.
- 689 [12] Xu L, Ruan X, Mao C, Zhang B, Luo Y. An improved optimal sizing method for wind-solar-battery
690 hybrid power system. *IEEE Trans Sustain Energy* 2013; 4: 774-85.
- 691 [13] Mulder G, Ridder FD, Six D. Electricity storage for grid-connected household dwellings with PV
692 panels. *Sol Energy* 2010; 84: 1284-93.
- 693 [14] Bortolini M, Gamberi M, Graziani A. Technical and economic design of photovoltaic and battery
694 energy storage system. *Energy Convers Manage* 2014; 86: 81-92.
- 695 [15] Zhou N, Liu N, Zhang J, Lei J. Multi-objective optimal sizing for battery storage of PV-based
696 microgrid with demand Response. *Energies* 2016; 9: 591.
- 697 [16] Mokhtari G, Nourbakhsh G, Gosh A. Optimal sizing of combined PV- energy storage for a grid-
698 connected residential building. *Advances in Energy Engineering* 2013; 1: 53-65.
- 699 [17] Marzband M, Sumper A, Ruiz-Álvarez A, Domínguez-García JL, Tomoiagă B. Experimental
700 evaluation of a real time energy management system for stand-alone microgrids in day-ahead
701 markets. *Appl Energy* 2013; 106: 365-76.
- 702 [18] Lu B, Shahidehpour M. Short-term scheduling of battery in a grid-connected PV/battery system.
703 *IEEE Trans Power Syst* 2005; 20: 1053-61.
- 704 [19] Riffonneau Y, Bacha S, Barruel F, Ploix S. Optimal power flow management for grid connected PV
705 systems with batteries. *IEEE Trans Sustain Energy* 2011; 2: 309-20.
- 706 [20] Li J, Danzer MA. Optimal charge control strategies for stationary photovoltaic battery systems. *J*
707 *Power Sources* 2014; 258: 365-73.
- 708 [21] Marzband M, Sumper A, Domínguez-García JL, Gumara-Ferret R. Experimental validation of a
709 real time energy management system for microgrids in islanded mode using a local day-ahead
710 electricity market and MINLP. *Energy Convers Manage* 2013; 76: 314-22.
- 711 [22] Marzband M, Yousefnejad E, Sumper A, Domínguez-García JL. Real time experimental
712 implementation of optimum energy management system in standalone Microgrid by using multi-
713 layer ant colony optimization. *International Journal of Electrical Power & Energy Systems* 2016; 75:
714 265-74.

715 [23] Marzband M, Ghadimi M, Sumper A, Domínguez-García JL. Experimental validation of a real-time
716 energy management system using multi-period gravitational search algorithm for microgrids in
717 islanded mode. *Appl Energy* 2014; 128: 164-74.

718 [24] Marzband M, Parhizi N, Adabi J. Optimal energy management for stand-alone microgrids based
719 on multi-period imperialist competition algorithm considering uncertainties: experimental validation.
720 *Int Trans Electr Energy Syst* 2016; 26: 1358-72.

721 [25] Marzband M, Azarinejadian F, Savaghebi M, Guerrero JM. An optimal energy management
722 system for islanded microgrids based on multiperiod artificial bee colony combined with markov
723 chain. *IEEE Syst J* 2015; PP: 1-11.

724 [26] Ru Y, Jan K, Sonia M. Storage size determination for grid-connected Photovoltaic systems. *IEEE*
725 *Trans Sustain Energy* 2013; 4: 68-81.

726 [27] Gitizadeh M, Fakhrazadegan H. Battery capacity determination with respect to optimized energy
727 dispatch schedule in grid-connected photovoltaic (PV) systems. *Energy* 2014; 65: 665-74.

728 [28] Khalilpour R, Vassallo A. Planning and operation scheduling of PV-battery systems: A novel
729 methodology. *Renew Sust Energy Rev* 2016; 53: 194-208.

730 [29] OptiCE. <www.optice.net> [assessed 11.8.2016].

731 [30] De Soto W, Klein SA, Beckman WA. Improvement and validation of a model for photovoltaic
732 array performance. *Sol Energy* 2006; 80: 78-88.

733 [31] Duffie JA, Beckman WA. *Solar engineering of thermal processes*. 4th ed. Wiley New York
734 etc.2013.

735 [32] Dolara A, Leva S, Manzolini G. Comparison of different physical models for PV power output
736 prediction. *Sol Energy* 2015; 119: 83-99.

737 [33] Aurilio G, Balato M, Graditi G, Landi C, Luiso M, Vitelli M. Fast hybrid MPPT technique for
738 Photovoltaic applications: numerical and experimental Validation. *Advances in Power Electronics*
739 2014; 2014: 15.

740 [34] Adinolfi G, Graditi G, Siano P, Piccolo A. Multiobjective Optimal Design of Photovoltaic
741 Synchronous Boost Converters Assessing Efficiency, Reliability, and Cost Savings. *IEEE Trans Ind*
742 *Informat* 2015; 11: 1038-48.

743 [35] Merei G, Berger C, Sauer DU. Optimization of an off-grid hybrid PV–Wind–Diesel system with
744 different battery technologies using genetic algorithm. *Sol Energy* 2013; 97: 460-73.

745 [36] Blair N, Dobos AP, Freeman J, Neises T, Wagner M, Ferguson T, et al. System advisor model, sam
746 2014.1. 14: general description. 2014 <<https://www.nrel.gov/publications>>.

747 [37] Dunn B, Kamath H, Tarascon J-M. Electrical energy storage for the grid: A battery of choices.
748 *Science* 2011; 334: 928-35.

749 [38] Nykvist B, Nilsson M. Rapidly falling costs of battery packs for electric vehicles. *Nat Clim Change*
750 2015; 5: 329-32.

751 [39] Tremblay O, Dessaint L-A. Experimental validation of a battery dynamic model for EV
752 applications. *World Electric Vehicle Journal* 2009; 3: 1-10.

753 [40] Wang J, Liu P, Hicks-Garner J, Sherman E, Soukiazian S, Verbrugge M, et al. Cycle-life model for
754 graphite-LiFePO4 cells. *J Power Sources* 2011; 196: 3942-8.

755 [41] Mansor NII, Abdullah S, Ariffin AK, Syarif J. A review of the fatigue failure mechanism of metallic
756 materials under a corroded environment. *Eng Fail Anal* 2014; 42: 353-65.

757 [42] Downing SD, Socie DF. Simple rainflow counting algorithms. *Int J Fatigue* 1982; 4: 31-40.

758 [43] Zhang Z, Wang J, Wang X. An improved charging/discharging strategy of lithium batteries
759 considering depreciation cost in day-ahead microgrid scheduling. *Energy Convers Manage* 2015; 105:
760 675-84.

761 [44] Yang Z, Zhang J, Kintner-Meyer MCW, Lu X, Choi D, Lemmon JP, et al. Electrochemical energy
762 storage for green grid. *Chem Rev* 2011; 111: 3577-613.

763 [45] List of all Meteororm features <<http://www.meteororm.com/>> [assessed 15.3.2016].

764 [46] Zhang Y, Lundblad A, Campana PE, Yan J. Employing battery storage to increase photovoltaic
765 self-sufficiency in a residential building of Sweden. *Energy Proc* 2016; 88: 455-61.

766 [47] Lindahl J. National survey report of PV power applications in SWEDEN. 2015 <[http://www.iea-](http://www.iea-pvps.org/)
767 [pvps.org/](http://www.iea-pvps.org/)>.
768 [48] Nord Pool Spot. <<http://www.nordpoolspot.com/>> [assessed 11.3.2016].
769 [49] Sweden interest rates. <<http://sweden.deposits.org/>> [assessed 16.5.2016].
770 [50] Tesla home battery. <<https://www.tesla.com/powerwall>> [assessed 11.8.2016].
771 [51] Konak A, Coit DW, Smith AE. Multi-objective optimization using genetic algorithms: A tutorial.
772 Reliab Eng Syst Safe 2006; 91: 992-1007.
773 [52] Chauhan A, Saini RP. A review on Integrated Renewable Energy System based power generation
774 for stand-alone applications: Configurations, storage options, sizing methodologies and control.
775 Renew Sust Energy Rev 2014; 38: 99-120.
776 [53] Deb K, Agrawal S, Pratap A, Meyarivan T. A fast elitist non-dominated sorting genetic algorithm
777 for multi-objective optimization: NSGA-II. International Conference on Parallel Problem Solving From
778 Nature. Springer, Berlin Heidelberg, 2000. pp. 849-58.
779 [54] Graditi G, Ippolito MG, Telaretti E, Zizzo G. Technical and economical assessment of distributed
780 electrochemical storages for load shifting applications: An Italian case study. Renew Sust Energy Rev
781 2016; 57: 515-23.
782 [55] Statistics Sweden-Energy. <[http://www.scb.se/en_/Finding-statistics/Statistics-by-subject-](http://www.scb.se/en_/Finding-statistics/Statistics-by-subject-area/Energy/)
783 [area/Energy/](http://www.scb.se/en_/Finding-statistics/Statistics-by-subject-area/Energy/)> [assessed 24.5.2016].
784 [56] Maheri A. Multi-objective design optimisation of standalone hybrid wind-PV-diesel systems
785 under uncertainties. Renew Energy 2014; 66: 650-61.
786 [57] Graditi G, Ippolito MG, Telaretti E, Zizzo G. An innovative conversion device to the grid interface
787 of combined RES-based generators and electric storage systems. IEEE Trans Ind Electron 2015; 62:
788 2540-50.
789 [58] Marzband M, Javadi M, Dom JL, xed, nguez G, xed, et al. Non-cooperative game theory based
790 energy management systems for energy district in the retail market considering DER uncertainties.
791 IET Gener Transm Distrib 2016; 10: 2999-3009.

792