

Bordered and Pentagonal Magic Squares Multiples of 7

Inder J. Taneja¹

Abstract

During past years author worked with **block-wise borderedmagic squares** of even order blocks. It includes blocks of orders 4, 6, 8, 10, etc. Most of the cases are with equal sums magic squares. This type of work is an extension of classical bordered magic squares. In case of multiples of 4, the extension is made for **pentagonal** magic squares [23]. For multiples of order 6 refer Taneja [24]. Recently, author worked on multiples of 3 and 5, based on different sums magic squares of order 3 [29] and order 5 [30]. This work is for bordered of magic squares multiples of magic squares of order 7. It is done with seven different types of magic squares of order 7. These includes, **pandiagonal**, **bordered**, **double digits**, **corners**, etc type magic squares. This work is up to order 35. Higher orders examples can be seen in **Excel file** attached with the work. The total work is up to order 140. **Pandiagonal** magic squares based on equal sums pandiagonal magic squares of order 7 are also included in the **Excel file**.

¹Formerly, Professor of Mathematics, Federal University of Santa Catarina, Florianópolis, SC, Brazil (1978-2012). Also worked at Delhi University, India (1976-1978).

E-mail: ijtaneja@gmail.com;

Web-sites: <http://inderjtaneja.com>; [http://numbers-magic.com](https://numbers-magic.com);

Twitter: @IJTANEJA; Instagram: @crazynumbers.

Contents

1	Introduction	2
1.1	Classification of Bordered Magic Squares	3
2	Bordered Magic Squares Multiples of Magic Squares of Order 7	4
2.1	Magic Squares of Orders 140 and 133	5
2.2	Magic Squares of Order 28	9
2.3	Magic Squares of Order 21	17
3	Pentagonal Magic Squares Multiples 7	23
3.1	Pentagonal Magic Square of Order 7	24
3.2	Pentagonal Magic Square of Order 21	24
3.3	Pentagonal Magic Square of Order 35	25
4	Author's Contribution to Recreation of Numbers and Magic Squares	27

1 Introduction

During past years author [2, 3, 4, 5, 6, 7, 8] worked with **block-wise** magic squares from orders 12 to 47. Author [9, 10, 11, 12, 13, 14] also worked with **bordered** magic squares. The study on **bordered** magic squares is extended to **block-bordered** magic squares [15, 16, 17]. This is specially done for the magic squares of orders p and p^2 , where p is a prime number. This study is still extended to **block-wise bordered** magic squares [18, 19, 20, 21]. Some connection with Pythagorean triples and area-representations are also made [23, 24, 25, 26, 27]. The main property of **bordered** magic squares is that if we remove external borders, still we get **sub-bordered** magic squares, i.e., each layer in itself lead us to magic squares. In many cases, the properties of **bordered** magic square are separated by **even** and **odd** orders magic squares. In many cases, we get good properties for the **even** order **bordered** magic squares. In many cases, we have to use fractional numbers entries, specially to reach minimum perfect square sum of entries. For more study on **bordered** magic squares refer H. White's web-site [1].

The aim of this work is to combine the study of **block-wise** and **bordered** magic squares. This kind of study still

not seen by author. In this case we consider blocks of magic squares such as magic squares of order 4 and then put them in such a way that every time removing external borders, still we are left with magic squares. Based on this idea, we wrote with **block-wise bordered** magic squares of orders 108 and 104. Every time when we remove the external, we are left with **block-wise bordered** magic squares with minus order 8. For example, in case of order 108, removing external orders we are left with orders 100, 92, 84, etc. and in case of orders 104, removing external orders we are left with orders 96, 88, 80, etc. Thus alternatively we complete all order magic squares multiples of 4. The first two orders 4 and 8 are not **block-wise bordered** magic squares. From order 12 onwards, we always get **block-wise bordered** magic squares multiples of 4, i.e., of orders 12, 16, 20, etc. In all the situations the constructions of magic squares of order 4 are **pentagonal** and of equal sums, while the **block-wise bordered** magic squares are not **pentagonal**. In each case, if we redistribute the blocks of order 4 already constructed we reach to **pentagonal** magic squares of orders 12, 16, 20, etc. but unfortunately they are no more **block-wise bordered** magic squares. Before proceeding further, let's classify the idea of bordered magic squares:

1.1 Classification of Bordered Magic Squares

- **Single Digit:** Bordered magic squares based on single digit [9, 10, 1].
- **Two Digits:** Bordered magic squares based on magic rectangles multiples of 2 [58, 59, 60, 61, 61].
- **Three Digits:** Bordered magic squares based on magic squares of order 3 [29].
- **Four Digits:** Bordered magic squares based on magic squares of order 4 [23].
- **Five Digits:** Bordered magic squares based on magic squares of order 5 [30]
- **Six Digits:** Bordered magic squares based on magic squares of order 6 [24], etc.

It is revised version of author's previous work. In the previous work we worked only with two magic squares of order 7. Here are working with 7 magic square of order 7. The procedure, how to these bordered magic squares are obtained is also given. Pentagonal magic squares multiples of 7 are also given. Here, the work is only up to order 28. Higher orders examples can be seen in **Excel file** is attached with this work.

2 Bordered Magic Squares Multiples of Magic Squares of Order 7

Below are seven magic squares of order 7. Based these, we shall write bordered magic squares multiples of order 7. The total work is up to order 140.

pan	175	175	175	175	175	175	175
175	1	9	17	25	33	41	49
175	40	48	7	8	16	24	32
175	23	31	39	47	6	14	15
175	13	21	22	30	38	46	5
175	45	4	12	20	28	29	37
175	35	36	44	3	11	19	27
	18	26	34	42	43	2	10
1	175	175	175	175	175	175	175

2 mgc	200	190	180	170	160	150	175
42	38	40	5	4	2	44	175
1	34	37	17	19	18	49	175
3	14	24	29	22	36	47	175
43	15	23	25	27	35	7	175
41	30	28	21	26	20	9	175
39	32	13	33	31	16	11	175
6	12	10	45	46	48	8	175
	175	175	175	175	175	175	175

3 mgc	207	194	197	174	134	144	175
4	30	44	32	15	13	37	175
46	20	6	18	35	9	41	175
34	16	26	21	28	17	33	175
42	8	27	25	23	47	3	175
43	7	22	29	24	39	11	175
1	49	48	12	19	36	10	175
5	45	2	38	31	14	40	175
	175	175	175	175	175	175	175

4 mgc	170	222	99	211	175	173	175
26	21	28	30	20	8	42	175
27	25	23	33	17	12	38	175
22	29	24	14	36	48	2	175
34	32	31	13	15	45	5	175
16	18	19	35	37	10	40	175
46	49	7	47	6	11	9	175
4	1	43	3	44	41	39	175
	175	175	175	175	175	175	175

5 mgc	153	206	107	200	175	209	175
13	19	25	31	37	12	38	175
30	36	17	18	24	8	42	175
22	23	29	35	16	48	2	175
34	15	21	27	28	45	5	175
26	32	33	14	20	10	40	175
46	49	7	47	6	11	9	175
4	1	43	3	44	41	39	175
	175	175	175	175	175	175	175

6 mgc	200	203	98	179	175	195	175
34	37	19	17	18	12	38	175
14	24	29	22	36	8	42	175
30	23	25	27	20	48	2	175
15	28	21	26	35	45	5	175
32	13	31	33	16	10	40	175
47	49	7	46	6	11	9	175
3	1	43	4	44	41	39	175
	175	175	175	175	175	175	175

7 mgc	200	190	180	170	160	150	175
42	38	40	5	4	2	44	175
1	26	21	28	30	20	49	175
3	27	25	23	33	17	47	175
43	22	29	24	14	36	7	175
41	34	32	31	13	15	9	175
39	16	18	19	35	37	11	175
6	12	10	45	46	48	8	175
	175	175	175	175	175	175	175

These magic squares are of type pandiagonal, bordered double digits and cornered.

2.1 Magic Squares of Orders 140 and 133

Let's consider bordered magic square of orders 19 and 20 given by

19x19																			3439
344	326	328	330	332	334	336	338	340	17	16	14	12	10	8	6	4	2	342	3439
35	310	294	296	298	300	302	304	306	51	50	48	46	44	42	40	38	308	327	3439
33	67	280	266	268	270	272	274	276	81	80	78	76	74	72	70	278	295	329	3439
31	65	95	254	242	244	246	248	250	107	106	104	102	100	98	252	267	297	331	3439
29	63	93	119	232	222	224	226	228	129	128	126	124	122	230	243	269	299	333	3439
27	61	91	117	139	214	206	208	210	147	146	144	142	212	223	245	271	301	335	3439
25	59	89	115	137	155	200	194	196	161	160	158	198	207	225	247	273	303	337	3439
23	57	87	113	135	153	167	190	186	171	170	188	195	209	227	249	275	305	339	3439
21	55	85	111	133	151	165	175	184	177	182	187	197	211	229	251	277	307	341	3439
19	53	83	109	131	149	163	173	179	181	183	189	199	213	231	253	279	309	343	3439
347	313	283	257	235	217	203	193	180	185	178	169	159	145	127	105	79	49	15	3439
349	315	285	259	237	219	205	174	176	191	192	172	157	143	125	103	77	47	13	3439
351	317	287	261	239	221	164	168	166	201	202	204	162	141	123	101	75	45	11	3439
353	319	289	263	241	150	156	154	152	215	216	218	220	148	121	99	73	43	9	3439
355	321	291	265	132	140	138	136	134	233	234	236	238	240	130	97	71	41	7	3439
357	323	293	110	120	118	116	114	112	255	256	258	260	262	264	108	69	39	5	3439
359	325	84	96	94	92	90	88	86	281	282	284	286	288	290	292	82	37	3	3439
361	54	68	66	64	62	60	58	56	311	312	314	316	318	320	322	324	52	1	3439
20	36	34	32	30	28	26	24	22	345	346	348	350	352	354	356	358	360	18	3439
3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439	3439

20x20	4010																			
381	364	366	368	370	393	395	397	399	38	36	34	32	30	9	7	5	3	1	382	4010
29	345	330	332	334	336	356	358	360	72	70	68	66	64	46	44	42	40	346	372	4010
27	63	313	300	302	304	323	325	327	102	100	98	96	79	77	75	73	314	338	374	4010
25	61	95	285	274	276	278	294	296	128	126	124	122	108	106	104	286	306	340	376	4010
22	59	93	121	261	252	254	269	271	150	148	146	133	131	129	262	280	308	342	379	4010
21	57	90	119	145	241	234	236	248	168	166	164	154	152	242	256	282	311	344	380	4010
16	53	89	117	142	163	225	220	231	182	180	171	169	226	238	259	284	312	348	385	4010
14	51	84	113	141	161	178	213	210	192	190	184	214	223	240	260	288	317	350	387	4010
12	49	82	111	136	157	177	189	208	205	196	193	212	224	244	265	290	319	352	389	4010
10	39	80	103	134	151	172	183	194	195	206	207	218	229	250	267	298	321	362	391	4010
373	339	307	281	257	239	222	215	197	200	201	204	186	179	162	144	120	94	62	28	4010
375	341	309	283	258	243	227	216	203	202	199	198	185	174	158	143	118	92	60	26	4010
377	343	310	287	263	245	228	187	191	209	211	217	188	173	156	138	114	91	58	24	4010
378	347	315	289	264	246	175	181	170	219	221	230	232	176	155	137	112	86	54	23	4010
383	349	316	291	266	159	167	165	153	233	235	237	247	249	160	135	110	85	52	18	4010
384	351	318	292	139	149	147	132	130	251	253	255	268	270	272	140	109	83	50	17	4010
386	353	320	115	127	125	123	107	105	273	275	277	279	293	295	297	116	81	48	15	4010
388	354	87	101	99	97	78	76	74	299	301	303	305	322	324	326	328	88	47	13	4010
390	55	71	69	67	65	45	43	41	329	331	333	335	337	355	357	359	361	56	11	4010
19	37	35	33	31	8	6	4	2	363	365	367	369	371	392	394	396	398	400	20	4010
4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010	4010

The entries of above two magic squares are sequential numbers starting from 1:

$$D_{29 \times 29} := \{1, 2, \dots, 360, 361\}$$

$$D_{30 \times 30} := \{1, 2, \dots, 399, 400\}$$

These two magic squares are such that replacing the upper border still we are left with magic squares of lower orders in sequential values. Sometimes, these are called as **nested** or **embedded** magic squares.

Multiplying each entry by 49, we get

19x19	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511
16856	15974	16072	16170	16268	16366	16464	16562	16660	833	784	686	588	490	392	294	196	98	16758	168511
1715	15190	14406	14504	14602	14700	14798	14896	14994	2499	2450	2352	2254	2156	2058	1960	1862	15092	16023	168511
1617	3283	13720	13034	13132	13230	13328	13426	13524	3969	3920	3822	3724	3626	3528	3430	33622	14455	16121	168511
1519	3185	4655	12446	11858	11956	12054	12152	12250	5243	5194	5096	4998	4900	4802	12348	13083	14553	16219	168511
1421	3087	4557	5831	11368	10878	10976	11074	11172	6321	6272	6174	6076	5978	11270	11907	13181	14651	16317	168511
1323	2989	4459	5733	6811	10486	10094	10192	10290	7203	7154	7056	6958	10388	10927	12005	13279	14749	16415	168511
1225	2891	4361	5635	6713	7595	9800	9506	9604	7889	7840	7742	9702	10143	11025	12103	13377	14847	16513	168511
1127	2793	4263	5537	6615	7497	8183	9310	9114	8379	8330	9212	9555	10241	11123	12201	13475	14945	16611	168511
1029	2695	4165	5439	6517	7399	8085	8575	9016	8673	8918	9163	9653	10339	11221	12299	13573	15043	16709	168511
931	2597	4067	5341	6419	7301	7987	8477	8771	8869	8967	9261	9751	10437	11319	12397	13671	15141	16807	168511
17003	15337	13867	12593	11515	10633	9947	9457	8820	9065	8722	8281	7791	7105	6223	5145	3871	2401	735	168511
17101	15435	13965	12691	11613	10731	10045	8526	8624	9359	9408	8428	7693	7007	6125	5047	3773	2303	637	168511
17199	15533	14063	12789	11711	10829	8036	8232	8134	9849	9898	9996	7938	6909	6027	4949	3675	2205	539	168511
17297	15631	14161	12887	11809	7350	7644	7546	7448	10535	10584	10682	10780	7252	5929	4851	3577	2107	441	168511
17395	15729	14259	12985	6468	6860	6762	6664	6566	11417	11466	11564	11662	11760	6370	4753	3479	2009	343	168511
17493	15827	14357	5390	5880	5782	5684	5586	5488	12495	12544	12642	12740	12838	12936	5292	3381	1911	245	168511
17591	15925	4116	4704	4606	4508	4410	4312	4214	13769	13818	13916	14014	14112	14210	14308	4018	1813	147	168511
17689	2646	3332	3234	3136	3038	2940	2842	2744	15239	15288	15386	15484	15582	15680	15778	15876	2548	49	168511
980	1764	1666	1568	1470	1372	1274	1176	1078	16905	16954	17052	17150	17248	17346	17444	17542	17640	882	168511
168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511	168511

20x20	196490																			
18669	17836	17934	18032	18130	19257	19355	19453	19551	1862	1764	1666	1568	1470	441	343	245	147	49	18718	196490
1421	16905	16170	16268	16366	16464	17444	17542	17640	3528	3430	3332	3234	3136	2254	2156	2058	1960	16954	18228	196490
1323	3087	15337	14700	14798	14896	15827	15925	16023	4998	4900	4802	4704	3871	3773	3675	3577	15386	16562	18326	196490
1225	2989	4655	13965	13426	13524	13622	14406	14504	6272	6174	6076	5978	5292	5194	5096	14014	14994	16660	18424	196490
1078	2891	4557	5929	12789	12348	12446	13181	13279	7350	7252	7154	6517	6419	6321	12838	13720	15092	16758	18571	196490
1029	2793	4410	5831	7105	11809	11466	11564	12152	8232	8134	8036	7546	7448	11858	12544	13818	15239	16856	18620	196490
784	2597	4361	5733	6958	7987	11025	10780	11319	8918	8820	8379	8281	11074	11662	12691	13916	15288	17052	18865	196490
686	2499	4116	5537	6909	7889	8722	10437	10290	9408	9310	9016	10486	10927	11760	12740	14112	15533	17150	18963	196490
588	2401	4018	5439	6664	7693	8673	9261	10192	10045	9604	9457	10388	10976	11956	12985	14210	15631	17248	19061	196490
490	1911	3920	5047	6566	7399	8428	8967	9506	9555	10094	10143	10682	11221	12250	13083	14602	15729	17738	19159	196490
18277	16611	15043	13769	12593	11711	10878	10535	9653	9800	9849	9996	9114	8771	7938	7056	5880	4606	3038	1372	196490
18375	16709	15141	13867	12642	11907	11123	10584	9947	9898	9751	9702	9065	8526	7742	7007	5782	4508	2940	1274	196490
18473	16807	15190	14063	12887	12005	11172	9163	9359	10241	10339	10633	9212	8477	7644	6762	5586	4459	2842	1176	196490
18522	17003	15435	14161	12936	12054	8575	8869	8330	10731	10829	11270	11368	8624	7595	6713	5488	4214	2646	1127	196490
18767	17101	15484	14259	13034	7791	8183	8085	7497	11417	11515	11613	12103	12201	7840	6615	5390	4165	2548	882	196490
18816	17199	15582	14308	6811	7301	7203	6468	6370	12299	12397	12495	13132	13230	13328	6860	5341	4067	2450	833	196490
18914	17297	15680	5635	6223	6125	6027	5243	5145	13377	13475	13573	13671	14357	14455	14553	5684	3969	2352	735	196490
19012	17346	4263	4949	4851	4753	3822	3724	3626	14651	14749	14847	14945	15778	15876	15974	16072	4312	2303	637	196490
19110	2695	3479	3381	3283	3185	2205	2107	2009	16121	16219	16317	16415	16513	17395	17493	17591	17689	2744	539	196490
931	1813	1715	1617	1519	392	294	196	98	17787	17885	17983	18081	18179	19208	19306	19404	19502	19600	980	196490
	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490	196490

The distributions of these two magic squares are given by

$$D_{19 \times 19} := \{49, 98, \dots, 17640, 17689\}$$

$$D_{20 \times 20} := \{49, 98, \dots, 19551, 19600\}$$

In both the cases the difference between entries is 25. Now in each case replace the entries by magic squares of order 5 formed by the entries as given below:

$$\begin{aligned}49 &\rightarrow 1, 2, \dots, 49 \\98 &\rightarrow 50, 51, \dots, 98 \\147 &\rightarrow 99, 100, \dots, 147 \\\dots &\rightarrow \dots \quad \dots \\\dots &\rightarrow \dots \quad \dots\end{aligned}$$

This lead us to two magic squares of orders 140 and 133. Since these magic squares are very big to put in this work, these can be seen in an **excel file** attached in with the work. Below are few examples of magic squares obtained from above two magic squares. These are of orders 21 and 28.

2.2 Magic Squares of Order 28

These magic squares are obtained from the magic squares of order 140 by using the formula $\frac{a^2 - b^2}{2}$, $a > b$. Removing the external borders of order 7 and then subtracting $\frac{145^2 - 35^2}{2} := 9408$ from each entry, we get 7 magic squares of orders 28 given by

2.3 Magic Squares of Order 21

These magic squares are obtained from the magic squares of order 133 by using the formula $\frac{a^2 - b^2}{2}$, $a > b$. Removing the external borders of order 7 and then subtracting $\frac{133^2 - 21^2}{2} := 8624$ from each entry, we get 7 magic squares of orders 21 given by

1	mgc	5082	5523	5964	6405	6846	7287	7728	6846	5964	5082	4200	3318	2436	1554	1995	2436	2877	3318	3759	4200	4641
	344	352	360	368	376	384	392	1	9	17	25	33	41	49	246	254	262	270	278	286	294	4641
	383	391	350	351	359	367	375	40	48	7	8	16	24	32	285	293	252	253	261	269	277	4641
	366	374	382	390	349	357	358	23	31	39	47	6	14	15	268	276	284	292	251	259	260	4641
	356	364	365	373	381	389	348	13	21	22	30	38	46	5	258	266	267	275	283	291	250	4641
	388	347	355	363	371	372	380	45	4	12	20	28	29	37	290	249	257	265	273	274	282	4641
	378	379	387	346	354	362	370	35	36	44	3	11	19	27	280	281	289	248	256	264	272	4641
	361	369	377	385	386	345	353	18	26	34	42	43	2	10	263	271	279	287	288	247	255	4641
	99	107	115	123	131	139	147	197	205	213	221	229	237	245	295	303	311	319	327	335	343	4641
	138	146	105	106	114	122	130	236	244	203	204	212	220	228	334	342	301	302	310	318	326	4641
	121	129	137	145	104	112	113	219	227	235	243	202	210	211	317	325	333	341	300	308	309	4641
	111	119	120	128	136	144	103	209	217	218	226	234	242	201	307	315	316	324	332	340	299	4641
	143	102	110	118	126	127	135	241	200	208	216	224	225	233	339	298	306	314	322	323	331	4641
	133	134	142	101	109	117	125	231	232	240	199	207	215	223	329	330	338	297	305	313	321	4641
	116	124	132	140	141	100	108	214	222	230	238	239	198	206	312	320	328	336	337	296	304	4641
	148	156	164	172	180	188	196	393	401	409	417	425	433	441	50	58	66	74	82	90	98	4641
	187	195	154	155	163	171	179	432	440	399	400	408	416	424	89	97	56	57	65	73	81	4641
	170	178	186	194	153	161	162	415	423	431	439	398	406	407	72	80	88	96	55	63	64	4641
	160	168	169	177	185	193	152	405	413	414	422	430	438	397	62	70	71	79	87	95	54	4641
	192	151	159	167	175	176	184	437	396	404	412	420	421	429	94	53	61	69	77	78	86	4641
	182	183	191	150	158	166	174	427	428	436	395	403	411	419	84	85	93	52	60	68	76	4641
	165	173	181	189	190	149	157	410	418	426	434	435	394	402	67	75	83	91	92	51	59	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

2	mgc	5157	5568	5979	6390	6801	7212	7728	6921	6009	5097	4185	3273	2361	1554	2070	2481	2892	3303	3714	4125	4641	
		385	381	383	348	347	345	387	42	38	40	5	4	2	44	287	283	285	250	249	247	289	4641
		344	377	380	360	362	361	392	1	34	37	17	19	18	49	246	279	282	262	264	263	294	4641
		346	357	367	372	365	379	390	3	14	24	29	22	36	47	248	259	269	274	267	281	292	4641
		386	358	366	368	370	378	350	43	15	23	25	27	35	7	288	260	268	270	272	280	252	4641
		384	373	371	364	369	363	352	41	30	28	21	26	20	9	286	275	273	266	271	265	254	4641
		382	375	356	376	374	359	354	39	32	13	33	31	16	11	284	277	258	278	276	261	256	4641
		349	355	353	388	389	391	351	6	12	10	45	46	48	8	251	257	255	290	291	293	253	4641
		140	136	138	103	102	100	142	238	234	236	201	200	198	240	336	332	334	299	298	296	338	4641
		99	132	135	115	117	116	147	197	230	233	213	215	214	245	295	328	331	311	313	312	343	4641
		101	112	122	127	120	134	145	199	210	220	225	218	232	243	297	308	318	323	316	330	341	4641
		141	113	121	123	125	133	105	239	211	219	221	223	231	203	337	309	317	319	321	329	301	4641
		139	128	126	119	124	118	107	237	226	224	217	222	216	205	335	324	322	315	320	314	303	4641
		137	130	111	131	129	114	109	235	228	209	229	227	212	207	333	326	307	327	325	310	305	4641
		104	110	108	143	144	146	106	202	208	206	241	242	244	204	300	306	304	339	340	342	302	4641
		189	185	187	152	151	149	191	434	430	432	397	396	394	436	91	87	89	54	53	51	93	4641
		148	181	184	164	166	165	196	393	426	429	409	411	410	441	50	83	86	66	68	67	98	4641
		150	161	171	176	169	183	194	395	406	416	421	414	428	439	52	63	73	78	71	85	96	4641
		190	162	170	172	174	182	154	435	407	415	417	419	427	399	92	64	72	74	76	84	56	4641
		188	177	175	168	173	167	156	433	422	420	413	418	412	401	90	79	77	70	75	69	58	4641
		186	179	160	180	178	163	158	431	424	405	425	423	408	403	88	81	62	82	80	65	60	4641
		153	159	157	192	193	195	155	398	404	402	437	438	440	400	55	61	59	94	95	97	57	4641
		4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

3	mgc	4986	5466	5898	6408	6969	7380	7728	6750	5907	5016	4203	3441	2529	1554	1899	2379	2811	3321	3882	4293	4641
	389	363	349	361	378	380	356	46	20	6	18	35	37	13	291	265	251	263	280	282	258	4641
	347	373	387	375	358	384	352	4	30	44	32	15	41	9	249	275	289	277	260	286	254	4641
	359	377	367	372	365	376	360	16	34	24	29	22	33	17	261	279	269	274	267	278	262	4641
	351	385	366	368	370	346	390	8	42	23	25	27	3	47	253	287	268	270	272	248	292	4641
	350	386	371	364	369	354	382	7	43	28	21	26	11	39	252	288	273	266	271	256	284	4641
	392	344	345	381	374	357	383	49	1	2	38	31	14	40	294	246	247	283	276	259	285	4641
	388	348	391	355	362	379	353	45	5	48	12	19	36	10	290	250	293	257	264	281	255	4641
	144	118	104	116	133	135	111	242	216	202	214	231	233	209	340	314	300	312	329	331	307	4641
	102	128	142	130	113	139	107	200	226	240	228	211	237	205	298	324	338	326	309	335	303	4641
	114	132	122	127	120	131	115	212	230	220	225	218	229	213	310	328	318	323	316	327	311	4641
	106	140	121	123	125	101	145	204	238	219	221	223	199	243	302	336	317	319	321	297	341	4641
	105	141	126	119	124	109	137	203	239	224	217	222	207	235	301	337	322	315	320	305	333	4641
	147	99	100	136	129	112	138	245	197	198	234	227	210	236	343	295	296	332	325	308	334	4641
	143	103	146	110	117	134	108	241	201	244	208	215	232	206	339	299	342	306	313	330	304	4641
	193	167	153	165	182	184	160	438	412	398	410	427	429	405	95	69	55	67	84	86	62	4641
	151	177	191	179	162	188	156	396	422	436	424	407	433	401	53	79	93	81	64	90	58	4641
	163	181	171	176	169	180	164	408	426	416	421	414	425	409	65	83	73	78	71	82	66	4641
	155	189	170	172	174	150	194	400	434	415	417	419	395	439	57	91	72	74	76	52	96	4641
	154	190	175	168	173	158	186	399	435	420	413	418	403	431	56	92	77	70	75	60	88	4641
	196	148	149	185	178	161	187	441	393	394	430	423	406	432	98	50	51	87	80	63	89	4641
	192	152	195	159	166	183	157	437	397	440	404	411	428	402	94	54	97	61	68	85	59	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

4	mgc	5097	5382	6192	6297	6846	7293	7728	6861	5823	5310	4092	3318	2442	1554	2010	2295	3105	3210	3759	4206	4641	
		367	372	365	363	373	385	351	24	29	22	20	30	42	8	269	274	267	265	275	287	253	4641
		366	368	370	360	376	381	355	23	25	27	17	33	38	12	268	270	272	262	278	283	257	4641
		371	364	369	379	357	345	391	28	21	26	36	14	2	48	273	266	271	281	259	247	293	4641
		359	361	362	380	378	348	388	16	18	19	37	35	5	45	261	263	264	282	280	250	290	4641
		377	375	374	358	356	383	353	34	32	31	15	13	40	10	279	277	276	260	258	285	255	4641
		347	344	386	346	387	382	384	4	1	43	3	44	39	41	249	246	288	248	289	284	286	4641
		389	392	350	390	349	352	354	46	49	7	47	6	9	11	291	294	252	292	251	254	256	4641
		122	127	120	118	128	140	106	220	225	218	216	226	238	204	318	323	316	314	324	336	302	4641
		121	123	125	115	131	136	110	219	221	223	213	229	234	208	317	319	321	311	327	332	306	4641
		126	119	124	134	112	100	146	224	217	222	232	210	198	244	322	315	320	330	308	296	342	4641
		114	116	117	135	133	103	143	212	214	215	233	231	201	241	310	312	313	331	329	299	339	4641
		132	130	129	113	111	138	108	230	228	227	211	209	236	206	328	326	325	309	307	334	304	4641
		102	99	141	101	142	137	139	200	197	239	199	240	235	237	298	295	337	297	338	333	335	4641
		144	147	105	145	104	107	109	242	245	203	243	202	205	207	340	343	301	341	300	303	305	4641
		171	176	169	167	177	189	155	416	421	414	412	422	434	400	73	78	71	69	79	91	57	4641
		170	172	174	164	180	185	159	415	417	419	409	425	430	404	72	74	76	66	82	87	61	4641
		175	168	173	183	161	149	195	420	413	418	428	406	394	440	77	70	75	85	63	51	97	4641
		163	165	166	184	182	152	192	408	410	411	429	427	397	437	65	67	68	86	84	54	94	4641
		181	179	178	162	160	187	157	426	424	423	407	405	432	402	83	81	80	64	62	89	59	4641
		151	148	190	150	191	186	188	396	393	435	395	436	431	433	53	50	92	52	93	88	90	4641
		193	196	154	194	153	156	158	438	441	399	439	398	401	403	95	98	56	96	55	58	60	4641
		4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

5	mgc	5148	5430	6168	6330	6846	7185	7728	6912	5871	5286	4125	3318	2334	1554	2061	2343	3081	3243	3759	4098	4641
	380	374	368	362	356	381	355	37	31	25	19	13	38	12	282	276	270	264	258	283	257	4641
	363	357	376	375	369	385	351	20	14	33	32	26	42	8	265	259	278	277	271	287	253	4641
	371	370	364	358	377	345	391	28	27	21	15	34	2	48	273	272	266	260	279	247	293	4641
	359	378	372	366	365	348	388	16	35	29	23	22	5	45	261	280	274	268	267	250	290	4641
	367	361	360	379	373	383	353	24	18	17	36	30	40	10	269	263	262	281	275	285	255	4641
	347	344	386	346	387	382	384	4	1	43	3	44	39	41	249	246	288	248	289	284	286	4641
	389	392	350	390	349	352	354	46	49	7	47	6	9	11	291	294	252	292	251	254	256	4641
	135	129	123	117	111	136	110	233	227	221	215	209	234	208	331	325	319	313	307	332	306	4641
	118	112	131	130	124	140	106	216	210	229	228	222	238	204	314	308	327	326	320	336	302	4641
	126	125	119	113	132	100	146	224	223	217	211	230	198	244	322	321	315	309	328	296	342	4641
	114	133	127	121	120	103	143	212	231	225	219	218	201	241	310	329	323	317	316	299	339	4641
	122	116	115	134	128	138	108	220	214	213	232	226	236	206	318	312	311	330	324	334	304	4641
	102	99	141	101	142	137	139	200	197	239	199	240	235	237	298	295	337	297	338	333	335	4641
	144	147	105	145	104	107	109	242	245	203	243	202	205	207	340	343	301	341	300	303	305	4641
	184	178	172	166	160	185	159	429	423	417	411	405	430	404	86	80	74	68	62	87	61	4641
	167	161	180	179	173	189	155	412	406	425	424	418	434	400	69	63	82	81	75	91	57	4641
	175	174	168	162	181	149	195	420	419	413	407	426	394	440	77	76	70	64	83	51	97	4641
	163	182	176	170	169	152	192	408	427	421	415	414	397	437	65	84	78	72	71	54	94	4641
	171	165	164	183	177	187	157	416	410	409	428	422	432	402	73	67	66	85	79	89	59	4641
	151	148	190	150	191	186	188	396	393	435	395	436	431	433	53	50	92	52	93	88	90	4641
	193	196	154	194	153	156	158	438	441	399	439	398	401	403	95	98	56	96	55	58	60	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

6	mgc	5007	5439	6195	6393	6846	7227	7728	6771	5880	5313	4188	3318	2376	1554	1920	2352	3108	3306	3759	4140	4641
		359	356	374	376	375	381	355	16	13	31	33	32	38	12	261	258	276	278	277	283	257
		379	369	364	371	357	385	351	36	26	21	28	14	42	8	281	271	266	273	259	287	253
		363	370	368	366	373	345	391	20	27	25	23	30	2	48	265	272	270	268	275	247	293
		378	365	372	367	358	348	388	35	22	29	24	15	5	45	280	267	274	269	260	250	290
		361	380	362	360	377	383	353	18	37	19	17	34	40	10	263	282	264	262	279	285	255
		346	344	386	347	387	382	384	3	1	43	4	44	39	41	248	246	288	249	289	284	286
		390	392	350	389	349	352	354	47	49	7	46	6	9	11	292	294	252	291	251	254	256
		114	111	129	131	130	136	110	212	209	227	229	228	234	208	310	307	325	327	326	332	306
		134	124	119	126	112	140	106	232	222	217	224	210	238	204	330	320	315	322	308	336	302
		118	125	123	121	128	100	146	216	223	221	219	226	198	244	314	321	319	317	324	296	342
		133	120	127	122	113	103	143	231	218	225	220	211	201	241	329	316	323	318	309	299	339
		116	135	117	115	132	138	108	214	233	215	213	230	236	206	312	331	313	311	328	334	304
		101	99	141	102	142	137	139	199	197	239	200	240	235	237	297	295	337	298	338	333	335
		145	147	105	144	104	107	109	243	245	203	242	202	205	207	341	343	301	340	300	303	305
		163	160	178	180	179	185	159	408	405	423	425	424	430	404	65	62	80	82	81	87	61
		183	173	168	175	161	189	155	428	418	413	420	406	434	400	85	75	70	77	63	91	57
		167	174	172	170	177	149	195	412	419	417	415	422	394	440	69	76	74	72	79	51	97
		182	169	176	171	162	152	192	427	414	421	416	407	397	437	84	71	78	73	64	54	94
		165	184	166	164	181	187	157	410	429	411	409	426	432	402	67	86	68	66	83	89	59
		150	148	190	151	191	186	188	395	393	435	396	436	431	433	52	50	92	53	93	88	90
		194	196	154	193	153	156	158	439	441	399	438	398	401	403	96	98	56	95	55	58	60
		4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

7	mgc	5058	5556	5976	6366	6834	7317	7728	6822	5997	5094	4161	3306	2466	1554	1971	2469	2889	3279	3747	4230	4641
351	355	353	388	389	391	349	8	12	10	45	46	48	6	253	257	255	290	291	293	251	4641	
392	367	372	365	363	373	344	49	24	29	22	20	30	1	294	269	274	267	265	275	246	4641	
390	366	368	370	360	376	346	47	23	25	27	17	33	3	292	268	270	272	262	278	248	4641	
350	371	364	369	379	357	386	7	28	21	26	36	14	43	252	273	266	271	281	259	288	4641	
352	359	361	362	380	378	384	9	16	18	19	37	35	41	254	261	263	264	282	280	286	4641	
354	377	375	374	358	356	382	11	34	32	31	15	13	39	256	279	277	276	260	258	284	4641	
387	381	383	348	347	345	385	44	38	40	5	4	2	42	289	283	285	250	249	247	287	4641	
106	110	108	143	144	146	104	204	208	206	241	242	244	202	302	306	304	339	340	342	300	4641	
147	122	127	120	118	128	99	245	220	225	218	216	226	197	343	318	323	316	314	324	295	4641	
145	121	123	125	115	131	101	243	219	221	223	213	229	199	341	317	319	321	311	327	297	4641	
105	126	119	124	134	112	141	203	224	217	222	232	210	239	301	322	315	320	330	308	337	4641	
107	114	116	117	135	133	139	205	212	214	215	233	231	237	303	310	312	313	331	329	335	4641	
109	132	130	129	113	111	137	207	230	228	227	211	209	235	305	328	326	325	309	307	333	4641	
142	136	138	103	102	100	140	240	234	236	201	200	198	238	338	332	334	299	298	296	336	4641	
155	159	157	192	193	195	153	400	404	402	437	438	440	398	57	61	59	94	95	97	55	4641	
196	171	176	169	167	177	148	441	416	421	414	412	422	393	98	73	78	71	69	79	50	4641	
194	170	172	174	164	180	150	439	415	417	419	409	425	395	96	72	74	76	66	82	52	4641	
154	175	168	173	183	161	190	399	420	413	418	428	406	435	56	77	70	75	85	63	92	4641	
156	163	165	166	184	182	188	401	408	410	411	429	427	433	58	65	67	68	86	84	90	4641	
158	181	179	178	162	160	186	403	426	424	423	407	405	431	60	83	81	80	64	62	88	4641	
191	185	187	152	151	149	189	436	430	432	397	396	394	434	93	87	89	54	53	51	91	4641	
4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

Above seven magic squares of order 21 formed by multiples blocks of magic squares of order 7 and are with entries

$$D_{35 \times 35} := \{1, 2, \dots, 440, 441\}.$$

3 Pentagonal Magic Squares Multiples 7

This section brings pentagonal magic squares multiples 7. It includes magic squares of orders 7, 21, 28 and 35. The details are excluded as these are studied extensively in author's previous works [5, 7, 20].

3.1 Pentagonal Magic Square of Order 7

Below is a **pentagonal** magic squares of order 7.

	pan	175	175	175	175	175	175	175	175
175	1	9	17	25	33	41	49	175	
175	40	48	7	8	16	24	32	175	
175	23	31	39	47	6	14	15	175	
175	13	21	22	30	38	46	5	175	
175	45	4	12	20	28	29	37	175	
175	35	36	44	3	11	19	27	175	
	18	26	34	42	43	2	10	175	
	175	175	175	175	175	175	175	175	175

It is the same magic square given in the beginning of Section 2.

3.2 Pentagonal Magic Square of Order 21

Below is a **pentagonal** magic squares of order 15.

pan	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641
4641	1	111	155	243	265	375	397	3	110	154	242	266	374	398	2	109	156	241	267	373	399	4641		
4641	370	396	19	106	153	239	264	371	395	20	108	152	238	263	372	394	21	107	151	240	262	4641		
4641	237	260	369	391	18	124	148	236	259	368	392	17	125	150	235	261	367	393	16	126	149	4641		
4641	123	166	232	258	365	390	13	122	167	234	257	364	389	14	121	168	233	256	366	388	15	4641		
4641	386	12	118	165	250	253	363	385	11	119	164	251	255	362	387	10	120	163	252	254	361	4641		
4641	271	358	384	8	117	160	249	272	360	383	7	116	161	248	273	359	382	9	115	162	247	4641		
4641	159	244	270	376	379	6	113	158	245	269	377	381	5	112	157	246	268	378	380	4	114	4641		
4641	43	90	134	222	286	354	418	45	89	133	221	287	353	419	44	88	135	220	288	352	420	4641		
4641	349	417	61	85	132	218	285	350	416	62	87	131	217	284	351	415	63	86	130	219	283	4641		
4641	216	281	348	412	60	103	127	215	280	347	413	59	104	129	214	282	346	414	58	105	128	4641		
4641	102	145	211	279	344	411	55	101	146	213	278	343	410	56	100	147	212	277	345	409	57	4641		
4641	407	54	97	144	229	274	342	406	53	98	143	230	276	341	408	52	99	142	231	275	340	4641		
4641	292	337	405	50	96	139	228	293	339	404	49	95	140	227	294	338	403	51	94	141	226	4641		
4641	138	223	291	355	400	48	92	137	224	290	356	402	47	91	136	225	289	357	401	46	93	4641		
4641	22	69	176	201	307	333	439	24	68	175	200	308	332	440	23	67	177	199	309	331	441	4641		
4641	328	438	40	64	174	197	306	329	437	41	66	173	196	305	330	436	42	65	172	198	304	4641		
4641	195	302	327	433	39	82	169	194	301	326	434	38	83	171	193	303	325	435	37	84	170	4641		
4641	81	187	190	300	323	432	34	80	188	192	299	322	431	35	79	189	191	298	324	430	36	4641		
4641	428	33	76	186	208	295	321	427	32	77	185	209	297	320	429	31	78	184	210	296	319	4641		
4641	313	316	426	29	75	181	207	314	318	425	28	74	182	206	315	317	424	30	73	183	205	4641		
4641	180	202	312	334	421	27	71	179	203	311	335	423	26	70	178	204	310	336	422	25	72	4641		
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

The blocks of order 7 are **equal sums** magic squares, i.e., $M_{7 \times 7} := 1547$

3.3 Pentagonal Magic Square of Order 35

Below is a **pentagonal** magic squares of order 35.

4 Author's Contribution to Recreation of Numbers and Magic Squares

- **Inder J. Taneja**, Recreation of Numbers - <https://numbers-magic.com/?p=671>.
- **Inder J. Taneja**, Magic Squares - <https://numbers-magic.com/?cat=3>.

References

• Block-Wise Magic Squares

- [1] **H. White**, Bordered Magic Squares - <http://budshaw.ca/BorderedMagicSquares.html>
- [2] **Inder J. Taneja**, Block-Wise Constructions of Magic and Bimagic Squares of Orders 8 to 108, May 15, 2019, pp. 1-43, **Zenodo**, <http://doi.org/10.5281/zenodo.2843326>.
- [3] **Inder J. Taneja**, Block-Wise Equal Sums Pandiagonal Magic Squares of Order 4k, **Zenodo**, January 31, 2019, pp. 1-17, <http://doi.org/10.5281/zenodo.2554288>.
- [4] **Inder J. Taneja**, Magic Rectangles in Construction of Block-Wise Pandiagonal Magic Squares, **Zenodo**, January 31, 2019, pp. 1-49, <http://doi.org/10.5281/zenodo.2554520>.
- [5] **Inder J. Taneja**, Block-Wise Equal Sums Magic Squares of Orders 3k and 6k, **Zenodo**, February 1, 2019, pp. 1-55, <http://doi.org/10.5281/zenodo.2554895>.
- [6] **Inder J. Taneja**, Block-Wise Unequal Sums Magic Squares, **Zenodo**, February 1, 2019, pp. 1-52, <http://doi.org/10.5281/zenodo.2555260>.
- [7] **Inder J. Taneja**, Block-Wise Magic and Bimagic Squares of Orders 12 to 36, **Zenodo**, February 1, 2019, pp. 1-53, <http://doi.org/10.5281/zenodo.2555343>.
- [8] **Inder J. Taneja**, Block-Wise Magic and Bimagic Squares of Orders 39 to 45, **Zenodo**, February 2, 2019, pp. 1-73, <http://doi.org/10.5281/zenodo.2555889>.

• Bordered Magic Squares

- [9] **Inder J. Taneja**, Nested Magic Squares With Perfect Square Sums, Pythagorean Triples, and Borders Differences, **Zenodo**, June 14, 2019, pp. 1-59, <http://doi.org/10.5281/zenodo.3246586>.
- [10] **Inder J. Taneja**, Symmetric Properties of Nested Magic Squares, **Zenodo**, June 29, 2019, pp. 1-55, <http://doi.org/10.5281/zenodo.3262170>.
- [11] **Inder J. Taneja**, General Sum Symmetric and Positive Entries Nested Magic Squares, **Zenodo**, July 04, 2019, pp. 1-55, <http://doi.org/10.5281/zenodo.3268877>.
- [12] **Inder J. Taneja**, Bordered Magic Squares With Order Square Magic Sums, **Zenodo**, January 20, 2020, pp. 1-26, <http://doi.org/10.5281/zenodo.3613690>.
- [13] **Inder J. Taneja**, Fractional and Decimal Type Bordered Magic Squares With Magic Sum 2020. **Zenodo**, January 20, 2020, pp.1-25. <http://doi.org/10.5281/zenodo.3613698>.
- [14] **Inder J. Taneja**, Fractional and Decimal Type Bordered Magic Squares With Magic Sum 2021, **Zenodo**, December 16, 2020, pp. 1-33, <http://doi.org/10.5281/zenodo.4327333>.
- [15] **Inder J. Taneja**, Inder J. Taneja, Block-Wise and Block-Bordered Magic Squares With Magic Sum 2022, **Zenodo**, December 28, 2021, pp. 1-38, <https://doi.org/10.5281/zenodo.5807789>

• Block-Bordered Magic Squares

- [16] **Inder J. Taneja**, Block-Bordered Magic Squares of Prime and Double Prime Numbers - I, **Zenodo**, August 18, 2020, pp. 1-81, <http://doi.org/10.5281/zenodo.3990291>.
- [17] **Inder J. Taneja**, Block-Bordered Magic Squares of Prime and Double Prime Numbers - II, **Zenodo**, August 18, 2020, pp. 1-90, <http://doi.org/10.5281/zenodo.3990293>.
- [18] **Inder J. Taneja**, Block-Bordered Magic Squares of Prime and Double Prime Numbers - III, **Zenodo**, September 01, 2020, pp. 1-93, <http://doi.org/10.5281/zenodo.4011213>.

• Block-Wise and Block-Bordered Magic Squares

- [19] **Inder J. Taneja**, Block-Wise and Block-Bordered Magic and Bimagic Squares With Magic Sums 21, 21^2 and 2021. **Zenodo**, December 16, 2020, pp. 1-118, <http://doi.org/10.5281/zenodo.4380343>.
- [20] **Inder J. Taneja**, Block-Wise and Block-Bordered Magic and Bimagic Squares of Orders 10 to 47. **Zenodo**, January 14, 2021, pp. 1-185, <http://doi.org/10.5281/zenodo.4437783>.
- [21] **Inder J. Taneja**, Bordered and Block-Wise Bordered Magic Squares: Odd Order Multiples, **Zenodo**, Feburary 10, 2021, pp. 1-75, <http://doi.org/10.5281/zenodo.4527739>
- [22] **Inder J. Taneja**, Bordered and Block-Wise Bordered Magic Squares: Even Order Multiples, **Zenodo**, Feburary 10, 2021, pp. 1-96, <http://doi.org/10.5281/zenodo.4527746>

• Multiple Orders Bordered Magic Squares

- [23] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 4, **Zenodo**, August 31, 2021, pp. 1-148, <https://doi.org/10.5281/zenodo.5347897>.
- [24] **Inder J. Taneja**, Block-Wise Bordered Magic Squares Multiples of Magic and Bordered Magic Squares of Order 6, **Zenodo**, September 10, pp. 1-99 <https://doi.org/10.5281/zenodo.5500134>.
- [25] **Inder J. Taneja**, Block-Wise Bordered Magic Squares Multiples of 8, **Zenodo**, September 17, pp. 1-80, <https://doi.org/10.5281/zenodo.5514396>.
- [26] **Inder J. Taneja**, Block-Wise Bordered Magic Squares Multiples of 10, **Zenodo**, September 17, pp. 1-170, <https://doi.org/10.5281/zenodo.5514398>.
- [27] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 12, **Zenodo**, September 23, pp. 1-170, <https://doi.org/10.5281/zenodo.5523608>.
- [28] **Inder J. Taneja**, Block-Wise Bordered Magic Squares Multiples of 14, **Zenodo**, September 26, pp. 1-198, <https://doi.org/10.5281/zenodo.5528867>.

- [29] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 3, **Zenodo**, May 05, pp. 1-29, 2023, <https://doi.org/10.5281/zenodo.7898383>.
- [30] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 5, **Zenodo**, July 23, 2023, pp. 1-36, <https://doi.org/10.5281/zenodo.8175759>.
- [31] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 7, **Zenodo**, July 23, pp. 1-34, 2023, <https://doi.org/10.5281/zenodo.8176061>.

• Magic Squares With Bordered Magic Rectangles

- [32] **Inder J. Taneja**, Different Styles of Magic Squares of Orders 6, 8, 10 and 12 Using Bordered Magic Rectangles, **Zenodo**, November 14, 2022, pp. 1-26, <https://doi.org/10.5281/zenodo.7319985>.
- [33] **Inder J. Taneja**, Different Styles of Magic Squares of Order 14 Using Bordered Magic Rectangles, **Zenodo**, November 14, 2022, pp. 1-40, <https://doi.org/10.5281/zenodo.7319787>.
- [34] **Inder J. Taneja**, Different Styles of Magic Squares of Order 16 Using Bordered Magic Rectangles, **Zenodo**, November 14, 2022, pp. 1-63, <https://doi.org/10.5281/zenodo.7320116>.
- [35] **Inder J. Taneja**, Different Styles of Magic Squares of Order 18 Using Bordered Magic Rectangles, **Zenodo**, November 14, 2022, pp. 1-85, <https://doi.org/10.5281/zenodo.7320131>.
- [36] **Inder J. Taneja**, Different Styles of Magic Squares of Order 20 Using Bordered Magic Rectangles, **Zenodo**, November 14, 2022, pp. 1-88, <https://doi.org/10.5281/zenodo.7320877>.
- [37] **Inder J. Taneja**, Few Examples of Magic Squares of Even Orders 6 to 18 Using Bordered Magic Rectangles, **Zenodo**, October 19, 2022, pp. 1-30, <https://doi.org/10.5281/zenodo.7225854>.
- [38] **Inder J. Taneja**, Few Examples of Magic Squares of Even Orders 20 to 30 Using Bordered Magic Rectangles, **Zenodo**, October 19, 2022, pp. 1-100, <https://doi.org/10.5281/zenodo.7225886>.
- [39] **Inder J. Taneja**, Single Crossed Bordered Magic Rectangles and Magic Squares of Order 40, **Zenodo**, January 24, 2023, pp. 1-76, <https://doi.org/10.5281/zenodo.7565946>

- [40] **Inder J. Taneja**, Double Crossed Bordered Magic Rectangles and Magic Squares of Order 40, **Zenodo**, January 30, 2023, pp. 1-102, <https://doi.org/10.5281/zenodo.7585787>
- [41] **Inder J. Taneja**, Magic Squares of Order 42 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, March 03, 2023, pp. 1-92, <https://doi.org/10.5281/zenodo.7695834>.
- [42] **Inder J. Taneja**, Single-Cross Bordered Magic Rectangles and Magic Squares of Order 42, **Zenodo**, March 03, 2023, pp. 1-69, <https://doi.org/10.5281/zenodo.7695939>
- [43] **Inder J. Taneja**, Double-Cross Bordered Magic Rectangles and Magic Squares of Order 42, **Zenodo**, March 03, 2023, pp. 1-59, <https://doi.org/10.5281/zenodo.7696070>.
- [44] **Inder J. Taneja**, Closed Double-Cross Bordered Magic Rectangles and Magic Squares of Order 42, **Zenodo**, March 03, 2023, pp. 1-28, <https://doi.org/10.5281/zenodo.7696181>.
- [45] **Inder J. Taneja**, 8000+ Magic Squares of Order 22 in Different Styles, Models and Designs, **Zenodo**, April 08, pp. 1-135, <https://doi.org/10.5281/zenodo.7809478>.

• Figured Magic Squares and Bordered Magic Rectangles

- [46] **Inder J. Taneja**, Figured Magic Squares of Orders 6, 10, 12, 14 and 16 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, November 29, 2022, pp. 1-31, <https://doi.org/10.5281/zenodo.7377674>.
- [47] **Inder J. Taneja**, Figured Magic Squares of Orders 18 and 20 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, November 29, 2022, pp. 1-87, <https://doi.org/10.5281/zenodo.7377689>.
- [48] **Inder J. Taneja**, Figured Magic Squares of Order 22 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, November 29, 2022, pp. 1-61, <https://doi.org/10.5281/zenodo.7377706>.
- [49] **Inder J. Taneja**, Figured Magic Squares of Order 24 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, November 29, 2022, pp. 1-104, <https://doi.org/10.5281/zenodo.7377779>.
- [50] **Inder J. Taneja**, Figured Magic Squares of Order 26 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, November 29, 2022, pp. 1-88, <https://doi.org/10.5281/zenodo.7377794>.

- [51] **Inder J. Taneja**, Figured Magic Squares of Order 28 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, December 02, 2022, pp. 1-179, <https://doi.org/10.5281/zenodo.7390666>.
- [52] **Inder J. Taneja**, Figured Magic Squares of Order 30 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, December 02, 2022, pp. 1-179, <https://doi.org/10.5281/zenodo.7390705>.
- [53] **Inder J. Taneja**, Figured Magic Squares of Order 32 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, December 22, 2022, pp. 1-310, <https://doi.org/10.5281/zenodo.7472891>.
- [54] **Inder J. Taneja**, Figured Magic Squares of Order 34 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, December 27, 2022, pp. 1-193, <https://doi.org/10.5281/zenodo.7486540>.
- [55] **Inder J. Taneja**, Figured Magic Squares of Order 36 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, December 27, 2022, pp. 1-140, <https://doi.org/10.5281/zenodo.7486548>.
- [56] **Inder J. Taneja**, Figured Magic Squares of Order 38 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, January 03, 2023, pp. 1-133, <https://doi.org/110.5281/zenodo.7500188>.
- [57] **Inder J. Taneja**, Figured Magic Squares of Order 40 Using Bordered Magic Rectangles: A Systematic Procedure, **Zenodo**, January 03, 2023, pp. 1-157, <https://doi.org/10.5281/zenodo.7500192>.

• Double Digits Bordered Magic Squares

- [58] **Inder J. Taneja**, Two Digits Bordered Magic Squares Multiples of 4: Orders 8 to 24, **Zenodo**, April, 26, 2023, pp. 1-43, <https://doi.org/10.5281/zenodo.7866956>.
- [59] **Inder J. Taneja**, Two Digits Bordered Magic Squares of Orders 28 and 32, **Zenodo**, April, 26, 2023, pp. 1-36, <https://doi.org/10.5281/zenodo.7866981>.
- [60] **Inder J. Taneja**, Two Digits Bordered Magic Squares of Orders 10, 14, 18 and 22, **Zenodo**, April, 30, 2023, pp. 1-43, <https://doi.org/10.5281/zenodo.7880931>.
- [61] **Inder J. Taneja**, Two Digits Bordered Magic Squares of Orders 26 and 30, **Zenodo**, April, 30, 2023, pp. 1-45, <https://doi.org/10.5281/zenodo.7880937>.

[62] **Inder J. Taneja**, Two Digits Bordered Magic Squares of Orders 36 and 40, **Zenodo**, May, 04, 2023, pp. 1-41, <https://doi.org/10.5281/zenodo.7896709>.

[63] **Inder J. Taneja**, Two digits Bordered Magic Squares of Orders 34 and 38, **Zenodo**, May 10, 2023, pp. 1-45, <https://doi.org/10.5281/zenodo.7922571>.

• Odd Order Magic Squares

[64] **Inder J. Taneja**, Odd Order Magic Squares: Orders 3 to 15, **Zenodo**, June 15, 2023, pp. 1-43, <https://doi.org/10.5281/zenodo.8043030>.

[65] **Inder J. Taneja**, Magic Squares of Orders 17 and 19, **Zenodo**, June 15, 2023, pp. 1-38, <https://doi.org/10.5281/zenodo.8043105>.

[66] **Inder J. Taneja**, Magic Squares of Orders 21 and 23, **Zenodo**, June 15, 2023, pp. 1-43, <https://doi.org/10.5281/zenodo.8043198>.

[67] **Inder J. Taneja**, Magic Squares of Order 25, **Zenodo**, June 15, 2023, pp. 1-27, <https://doi.org/10.5281/zenodo.8043228>.

• Cornered Magic Squares

[68] **Inder J. Taneja**, Cornered Magic Squares of Order 6, **Zenodo**, May 23, 2023, pp. 1-23, <https://doi.org/10.5281/zenodo.7960679>.

[69] **Inder J. Taneja**, Cornered Magic Squares of Orders 5 to 13, **Zenodo**, June 03, 2023, pp. 1-71, <https://doi.org/10.5281/zenodo.8000467>.

[70] **Inder J. Taneja**, Cornered Magic Squares of Orders 14 to 24, **Zenodo**, June 03, 2023, pp. 1-39, <https://doi.org/10.5281/zenodo.8000471>.

• Creative Magic Squares

- [71] **Inder J. Taneja**, Creative Magic Squares: Area Representations, **Zenodo**, June 22, pp. 1-45, 2021,
<http://doi.org/10.5281/zenodo.5009224>.
-