

Using SMB modelling and ICESat-2 to uncover ice sheet mass budget processes

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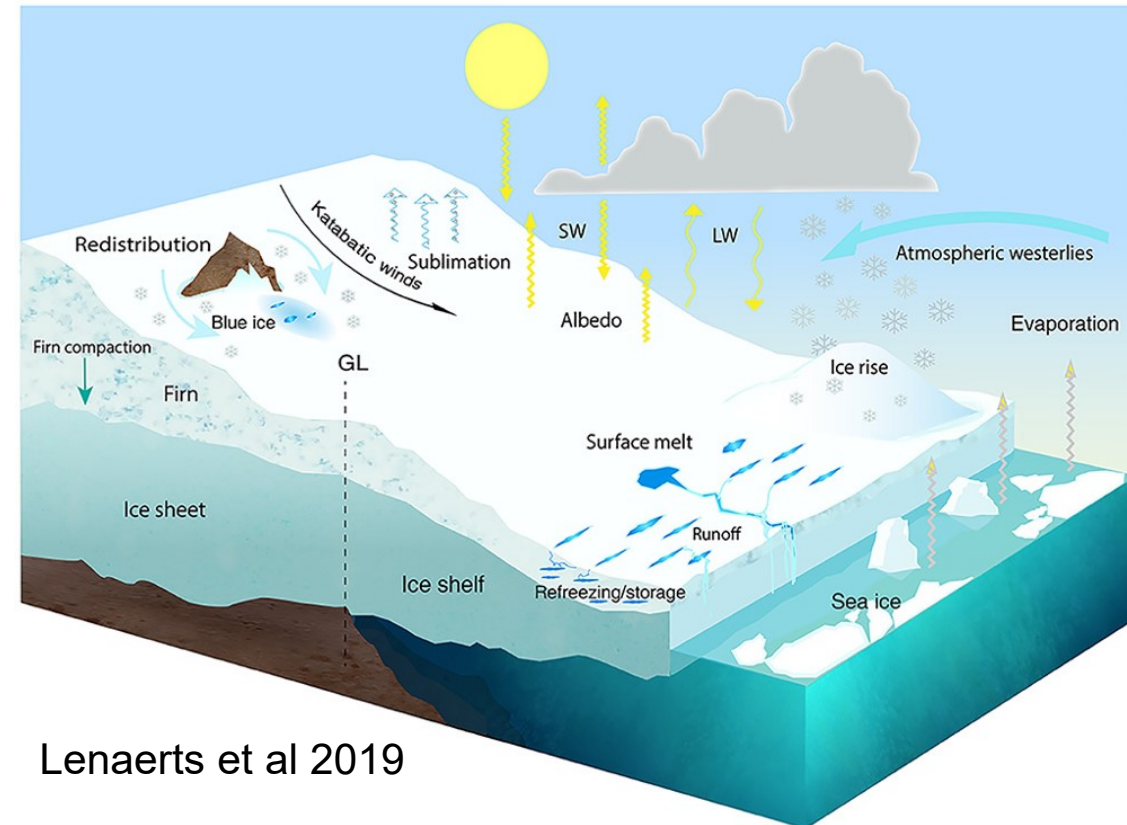
What is the (surface) mass balance?

$$MB = SMB - D$$

$$SMB = \text{precipitation} - \text{runoff} - \text{evaporation} - \text{sublimation}$$

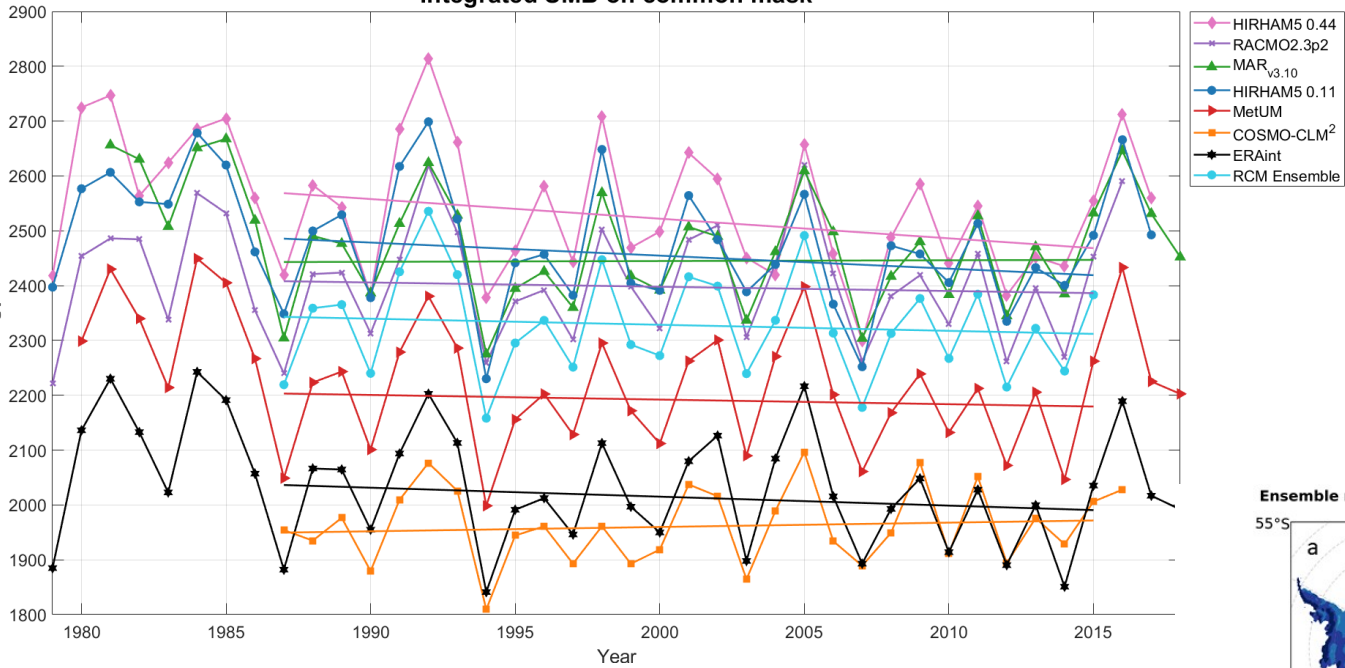
$$D = \text{discharge}$$

Discharge when crossing the GL



Lenaerts et al 2019

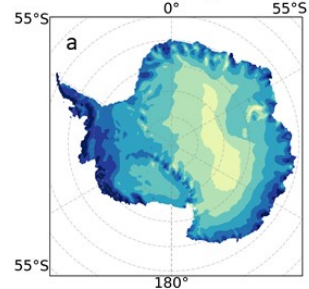
Integrated SMB on common mask



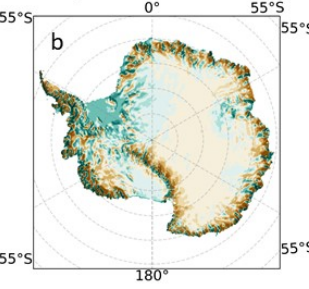
- Ice mask => area bias
- Model spread of 550 Gt per year
 - Equivalent to nearly 2 mm sea level change per year
- HIRHAM5

Mottram et al 2021

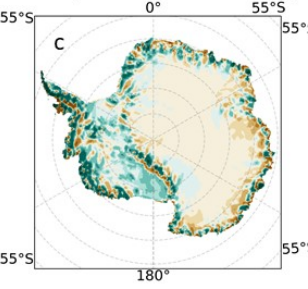
Ensemble mean Reanalysis 1987-2015



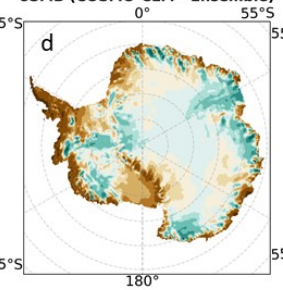
6SMB (HIRHAM5 0.11 - Ensemble)



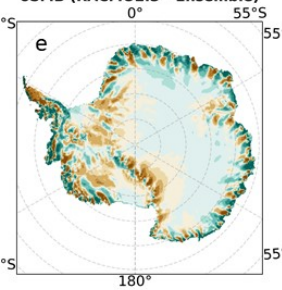
6SMB (HIRHAM5 0.44 - Ensemble)



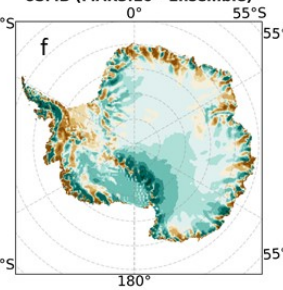
6SMB (COSMO-CLM - Ensemble)



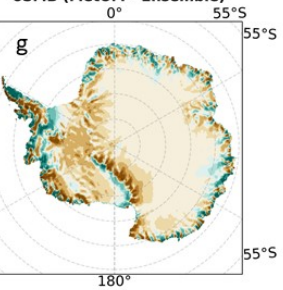
6SMB (RACMO2.3 - Ensemble)



6SMB (MAR3.10 - Ensemble)

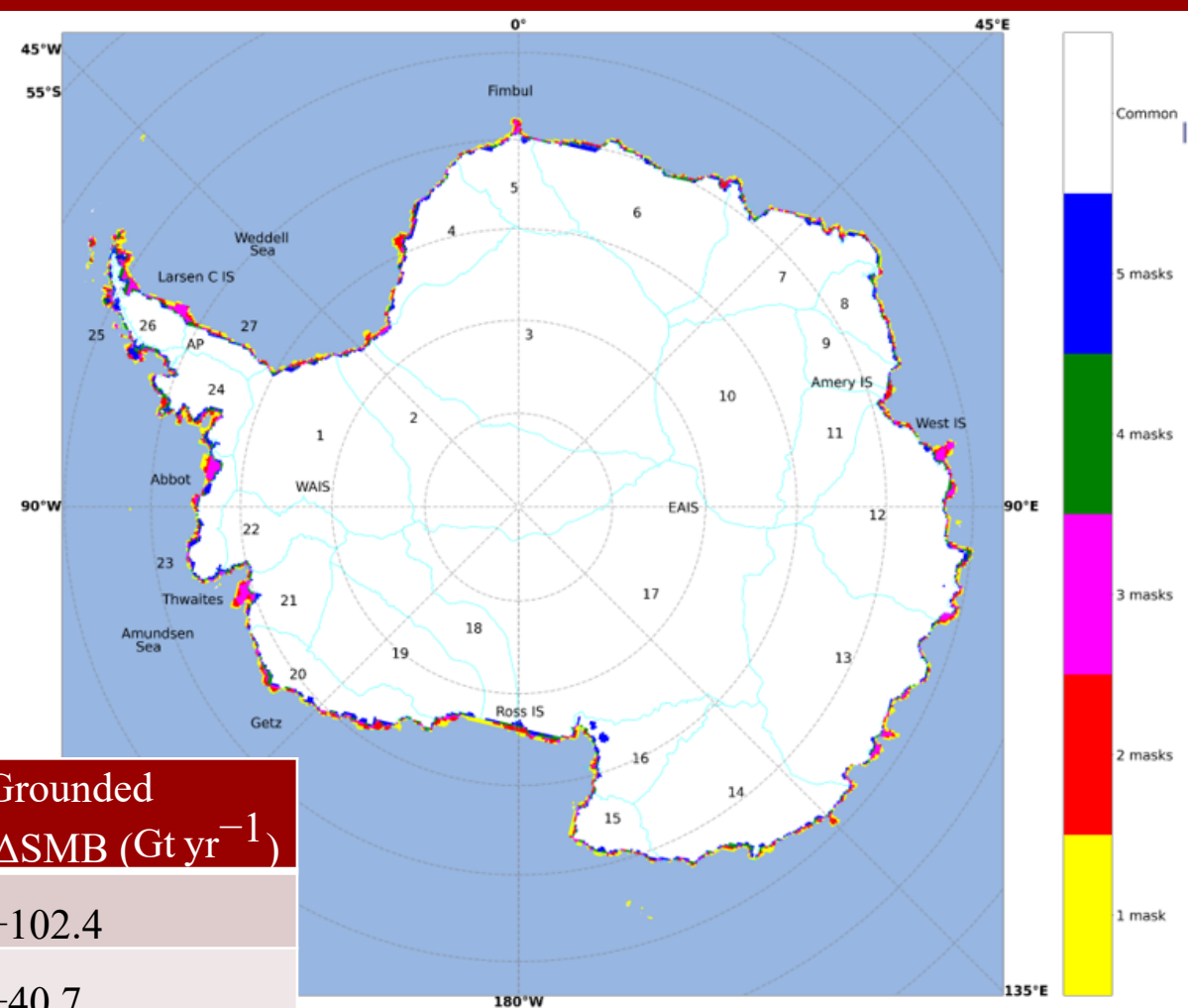


6SMB (MetUM - Ensemble)



The ice masks results

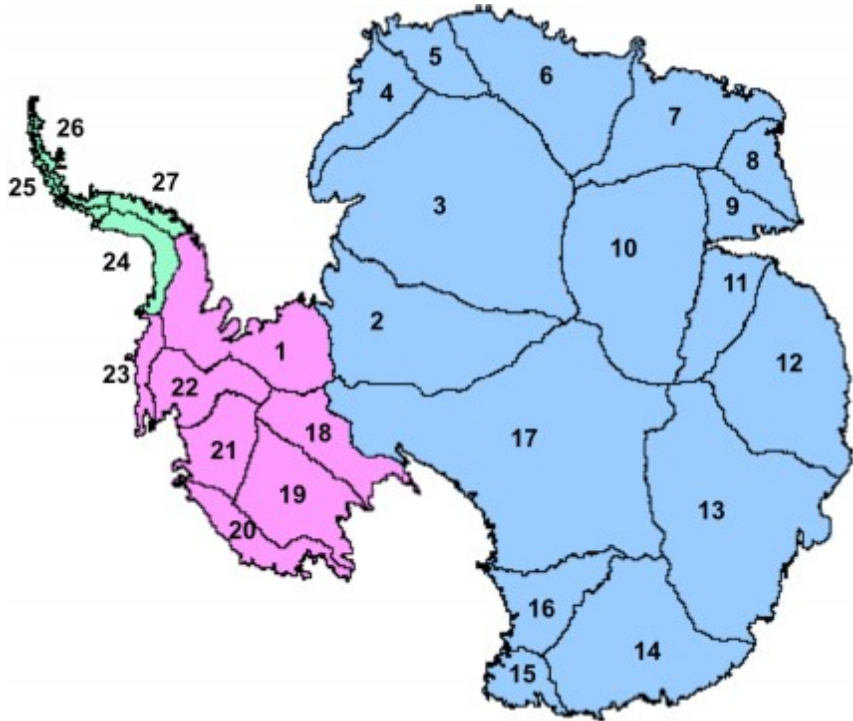
Ensemble mean from Mottram et al 2021= 2329 Gt per year



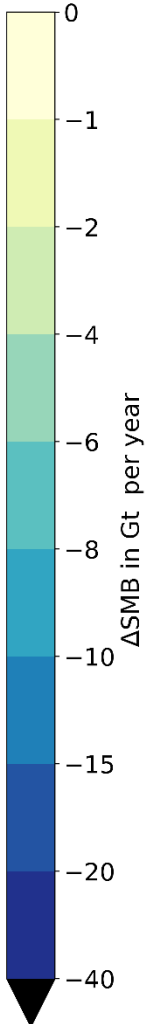
Common ice mask vs. native ice mask

MB=-109 ± 56 Gt per year

Model	Δ area (%)	Δ SMB(Gt yr^{-1})	Δ SMB (%)	SMB (Gt yr^{-1})	Grounded Δ SMB (Gt yr^{-1})
HIRHAM5 0.11°	-2.43	-140.6	-6.04	2452±107	-102.4
HIRHAM5 0.44°	-2.49	-69.5	-2.99	2518±118	-40.7
MARv3.10	-2.89	-91.9	-3.95	2445±91	-54.1
COSMO-CLM2	-1.94	-40.5	-1.77	1961±70	-20.1
RACMO2.3p2	-1.85	-119.6	-5.13	2399±101	-74.0
MetUM	-2.49	-57.6	-2.47	2191±101	-33.9

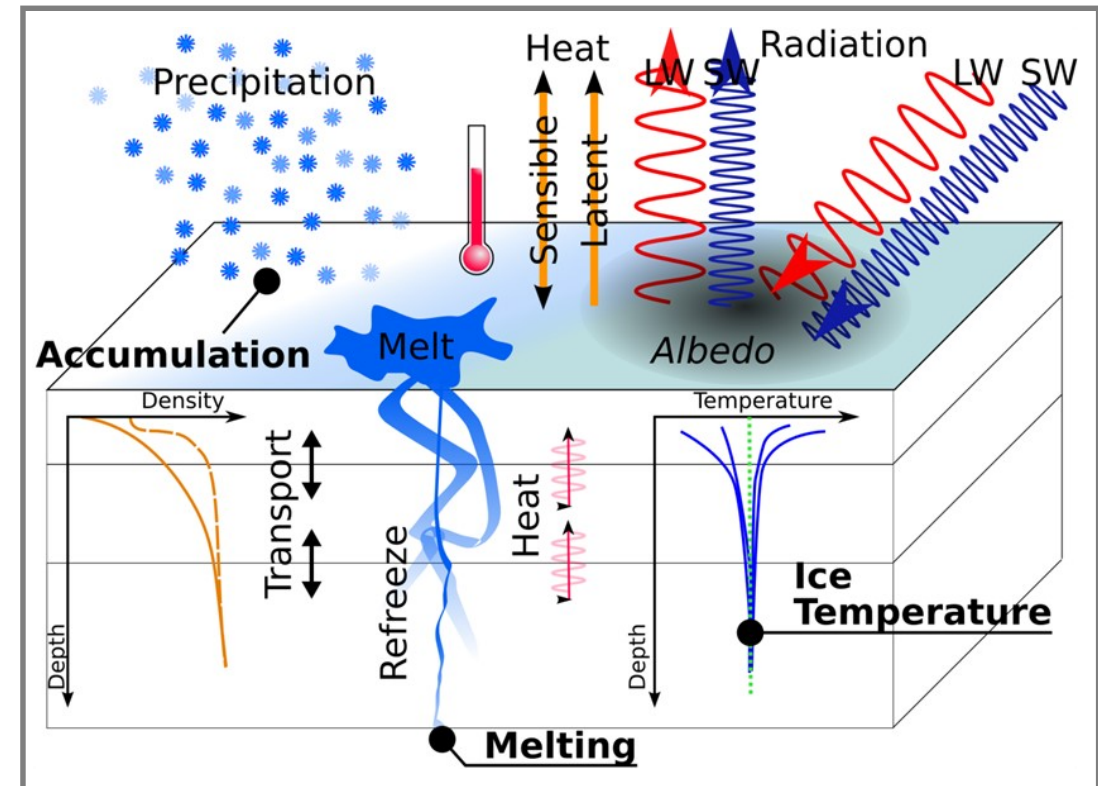


	HIRHAM5 0.11	HIRHAM5 0.44	MAR v3.10	MetUM	RACMO2.3p2	COSMO-CLM ²
Basin 1	-0.45 -0.43	-0.36 -0.41	-0.98 -1.10	0.44 0.44	-1.17 -1.12	-0.50 -0.68
Basin 2	-0.30 -0.08	-0.17 -0.06	-0.41 -0.14	-0.25 -0.08	-0.54 -0.13	-0.07 -0.05
Basin 3	-0.21 -0.05	-0.19 -0.05	-0.08 -0.03	-0.07 -0.02	-0.20 -0.05	-0.09 -0.04
Basin 4	-5.06 -2.91	-2.02 -1.75	-7.08 -6.46	-4.20 -2.63	-8.70 -3.86	-3.71 -3.97
Basin 5	-4.13 -2.28	-3.75 -2.10	-2.82 -1.80	-1.88 -0.90	-3.05 -1.62	-2.55 -1.98
Basin 6	-6.92 -2.15	-3.54 -1.53	-7.38 -3.19	-2.29 -0.77	-7.10 -2.92	-4.33 -2.71
Basin 7	-9.30 -2.47	-4.81 -1.87	-6.25 -2.82	-3.13 -0.89	-8.42 -2.81	-3.59 -2.16
Basin 8	-3.30 -4.14	-1.31 -2.58	-1.98 -4.24	-0.36 -0.83	-4.32 -3.87	-1.39 -3.31
Basin 9	-3.04 -0.96	-0.67 -0.26	-3.83 -1.83	-2.55 -0.87	-4.20 -1.57	-0.39 -0.35
Basin 10	0.00 0.00	-0.18 -0.03	-1.43 -0.25	-0.23 -0.03	-1.48 -0.23	-0.09 -0.05
Basin 11	-0.29 -0.05	-1.19 -0.33	-1.55 -0.33	0.00 0.00	-1.19 -0.27	-0.15 -0.05
Basin 12	-4.91 -1.60	-3.03 -1.35	-2.62 -1.49	-2.82 -1.08	-3.00 -1.21	-2.05 -1.79
Basin 13	-2.88 -0.71	-1.45 -0.46	-1.36 -0.69	-1.63 -0.42	-2.15 -0.62	-0.95 -0.55
Basin 14	-5.06 -1.49	-2.73 -1.07	-3.57 -1.68	-3.79 -1.17	-4.82 -1.55	-1.52 -0.82
Basin 15	-13.14 -5.62	-3.54 -3.11	-7.69 -6.22	-6.00 -3.23	-10.32 -5.62	-6.45 -4.55
Basin 16	-2.77 -3.80	-1.80 -2.71	-1.49 -2.71	-2.62 -2.42	-3.12 -3.34	-1.35 -2.65
Basin 17	-0.76 -0.24	-0.14 -0.09	-0.45 -0.33	-0.53 -0.17	-0.84 -0.33	-0.25 -0.26
Basin 18	-0.21 -0.15	-0.37 -0.44	-0.75 -0.66	-0.57 -0.33	-1.03 -0.74	-0.05 -0.15
Basin 19	-0.20 -0.13	-0.15 -0.13	-0.02 -0.03	-0.17 -0.13	-0.12 -0.09	-0.11 -0.13
Basin 20	-6.00 -4.52	-3.84 -3.01	-8.87 -8.97	-5.22 -4.32	-9.97 -7.55	-4.49 -3.73
Basin 21	-2.46 -0.93	-1.88 -0.93	-0.68 -0.47	-1.26 -0.66	-1.51 -0.73	-0.78 -0.60
Basin 22	-0.47 -0.21	-0.69 -0.48	0.62 0.62	-0.52 -0.28	-1.04 -0.62	-0.46 -0.55
Basin 23	-13.98 -8.83	-9.32 -8.30	-10.93 -12.32	-4.18 -4.48	-12.81 -11.46	-9.03 -10.41
Basin 24	-8.74 -4.72	-4.27 -3.58	-6.01 -7.62	-7.08 -5.79	-9.21 -7.08	-4.51 -6.55
Basin 25	-50.79 -40.49	-24.15 -24.54	-36.03 -41.10	-14.67 -13.50	-36.74 -32.52	-26.16 -40.49
Basin 26	-3.63 -2.73	-1.70 -3.03	-2.02 -3.79	-1.62 -2.12	-2.49 -2.73	-0.99 -2.12
Basin 27	-5.17 -5.48	-3.38 -4.57	-3.90 -5.71	-3.41 -3.42	-4.82 -5.48	-4.10 -4.79
Total SMB	-140.58	-69.56	-91.88	-57.60	-119.56	-40.46



The SMB model

- Models the physical properties of the firn
 - Melt-albedo feedback
 - Densification
 - Grain growth
 - Water/snow/ice fractions
 - Temperature
- 1-D columns
- Offline model



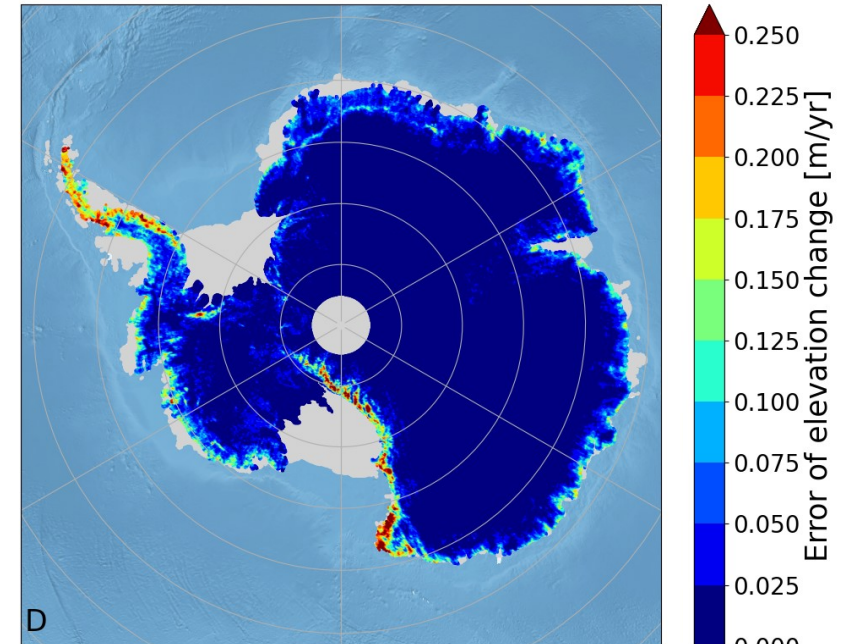
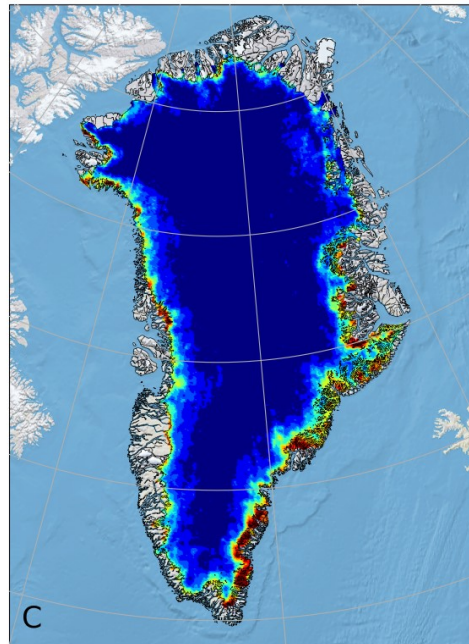
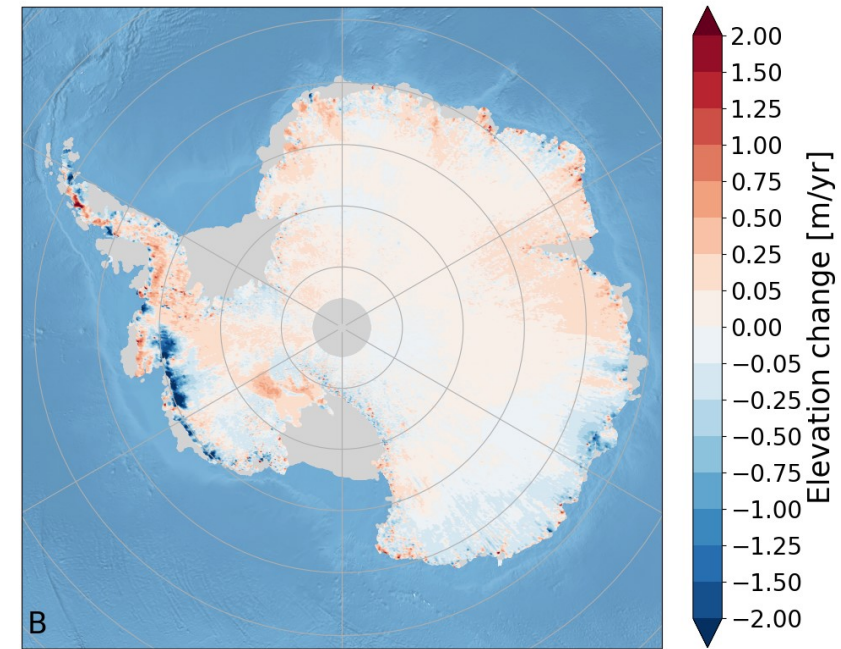
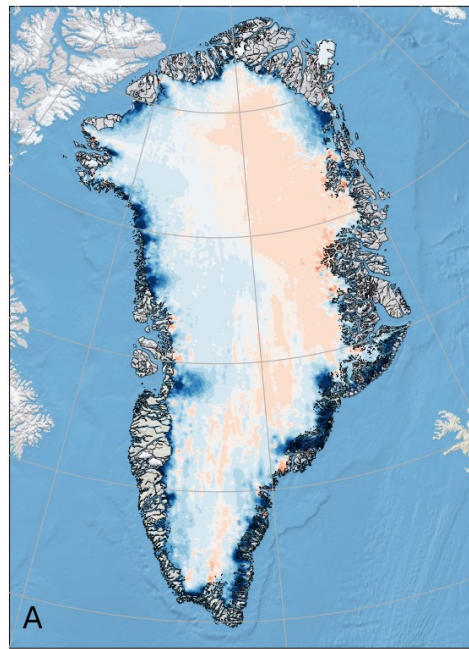
Quick outline of our ICESat-2 study

- We use ICESat-2 to derive the surface elevation change over the ice sheets
- October 2018 to September 2021
- Our methodology closely follows the Sørensen et al. (2011) repeat track method for ICESat
- We update the ICESat-2 processing chain and the model assumptions
- We make a new density parameterization for deriving mass balance in a consistent manner for both ice sheets

SEC as seen by ICESat-2

$$\frac{dH}{dt} = \frac{\dot{b}}{\rho} + w_c + w_{ice} + \frac{\dot{b}_m}{\rho} + w_{br} - u_s \frac{dS}{dx} - u_b \frac{dB}{dx}$$

- \dot{b} *SMB*
- ρ *density*
- w_c *firn compaction*
- w_{ice} *vertical ice velocity*
- \dot{b}_m *basal melt*
- w_{br} *vertical bedrock movement*
- u_s *horizontal ice velocity at the surface*
- u_b *horizontal ice velocity at the bed*



SEC as seen by ICESat-2

$$\frac{dH}{dt} = \frac{\dot{b}}{\rho} + w_c + w_{ice} + \frac{\dot{b}_m}{\rho} + w_{br} - u_s \frac{dS}{dx} - u_b \frac{dB}{dx}$$

\dot{b} *SMB*

ρ *density*

w_c *firn compaction*

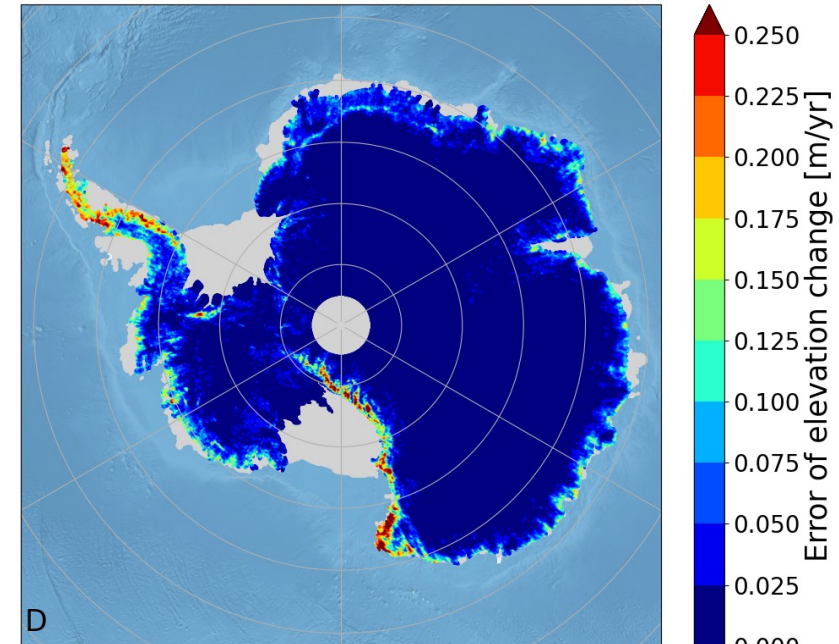
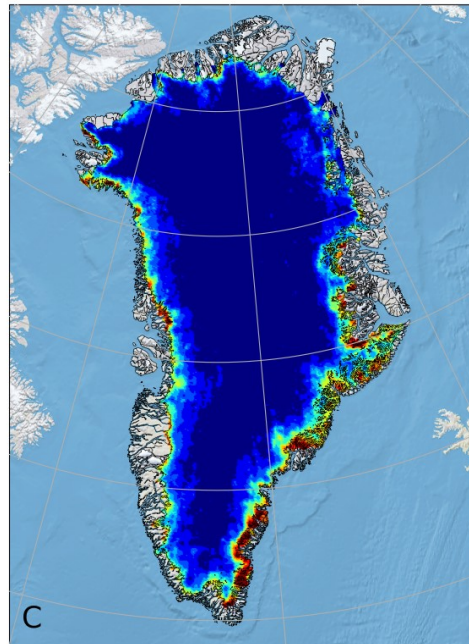
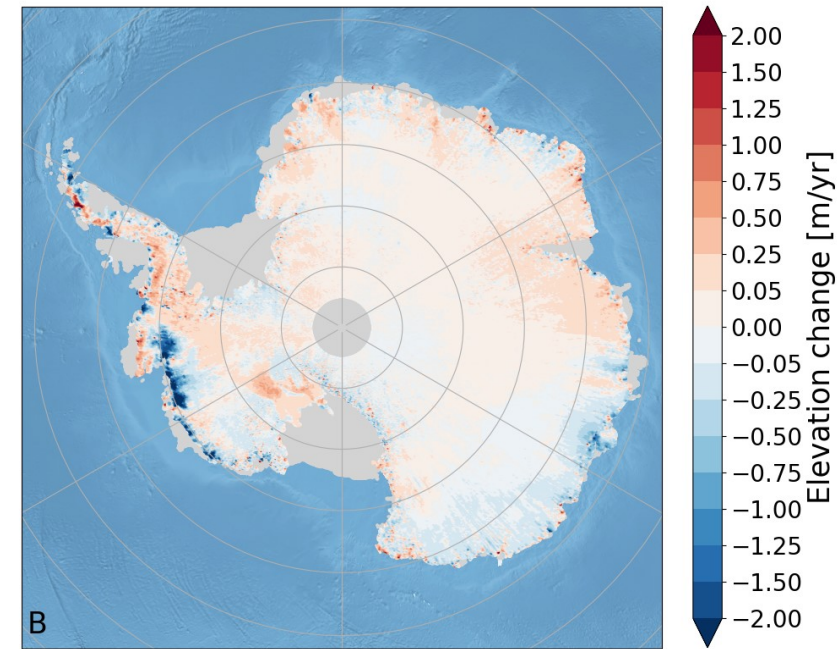
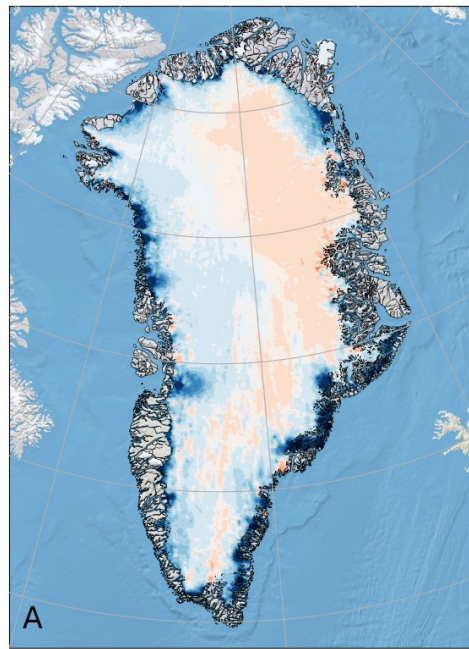
w_{ice} *vertical ice velocity*

\dot{b}_m *basal melt*

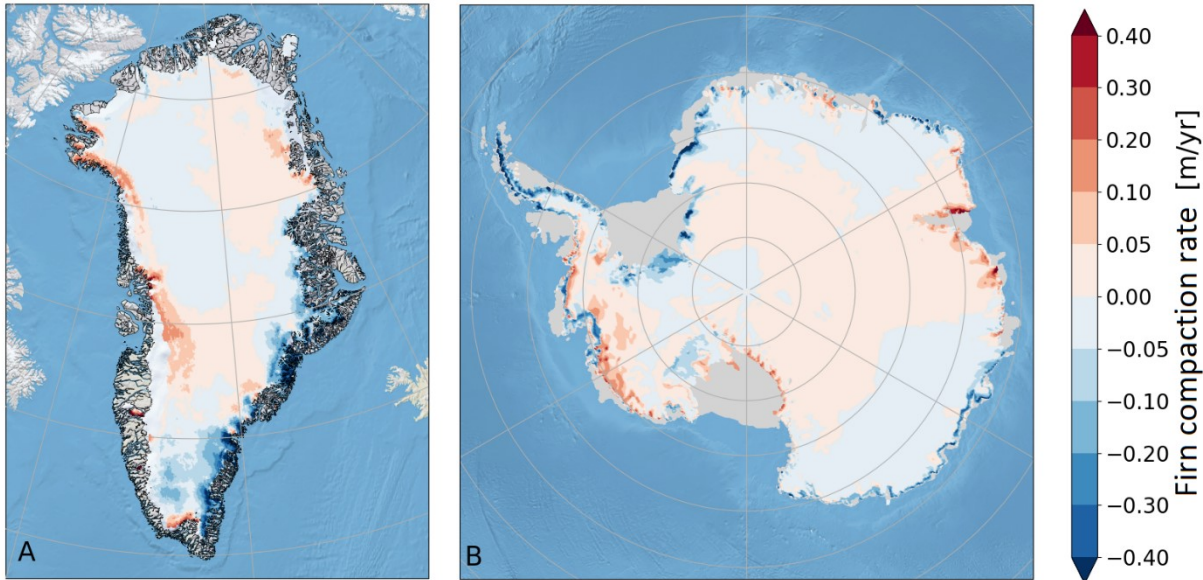
w_{br} *vertical bedrock movement*

u_s *horizontal ice velocity at the surface*

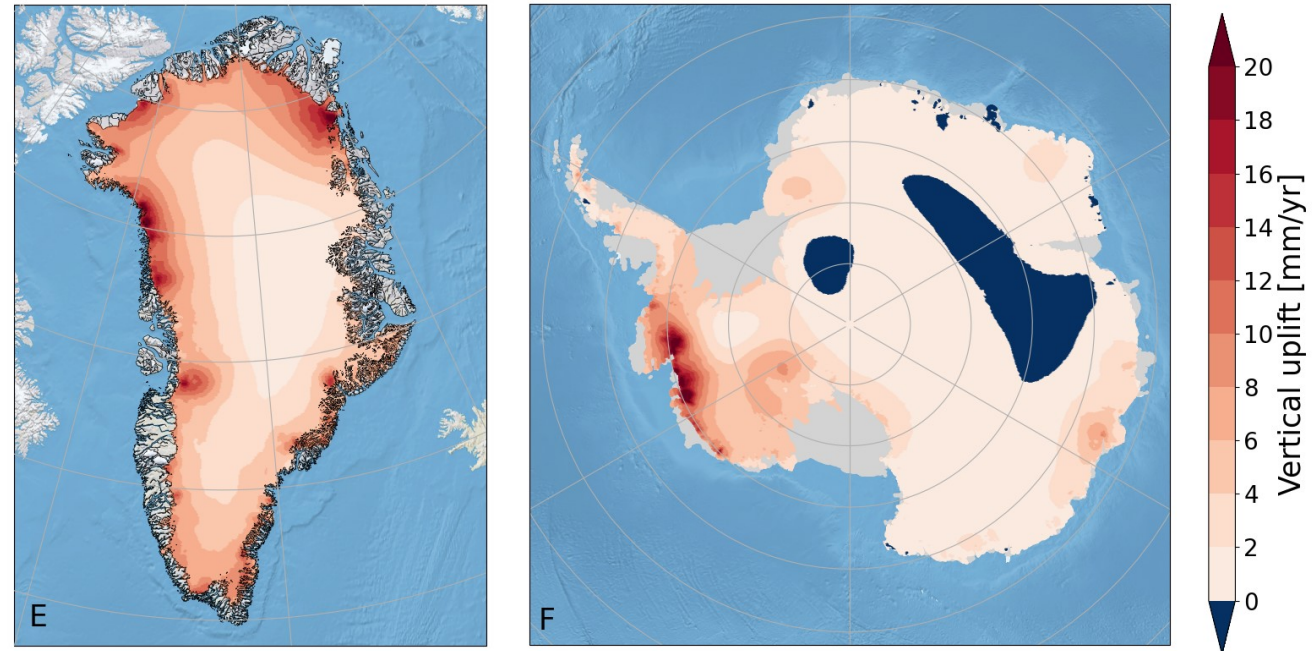
u_b *horizontal ice velocity at the bed*



Firn compaction and bedrock movement are non-mass-related processes



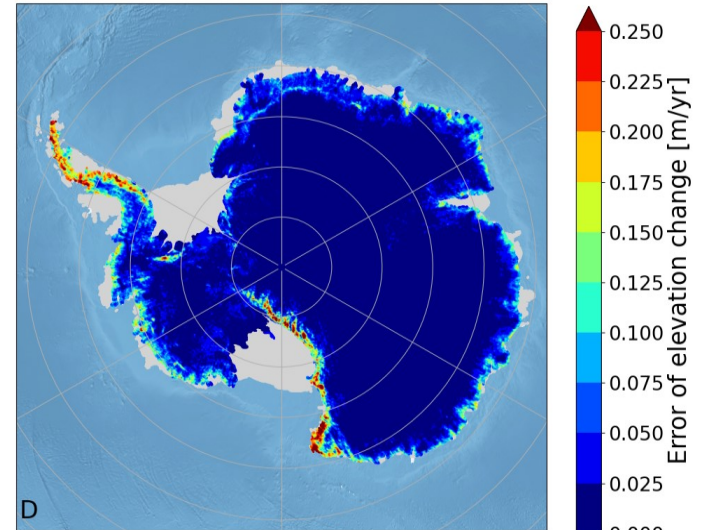
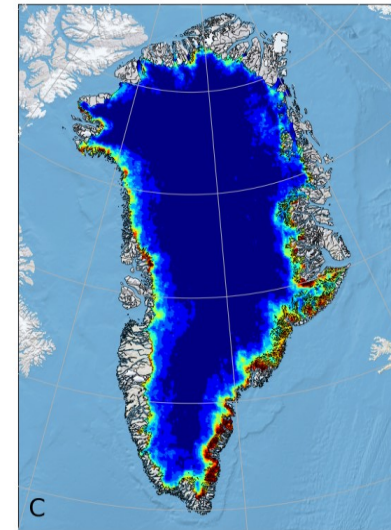
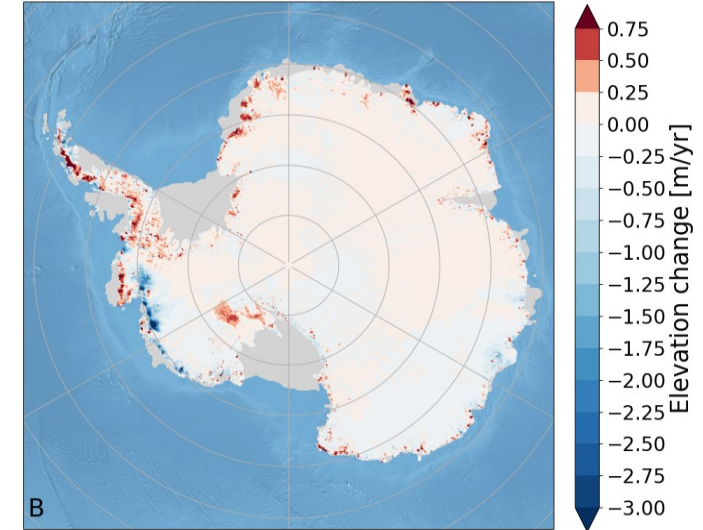
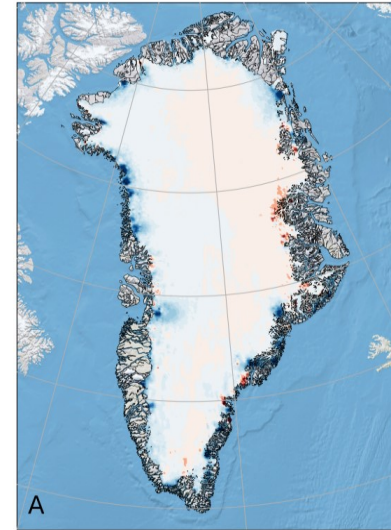
GIA + ER



Dynamical ice build-up in Kamb ice stream (Shepherd et al., 2019)

Volume to mass conversion

$$\frac{dM}{dt} = \frac{dH_{corrected}}{dt} \tilde{\rho}$$

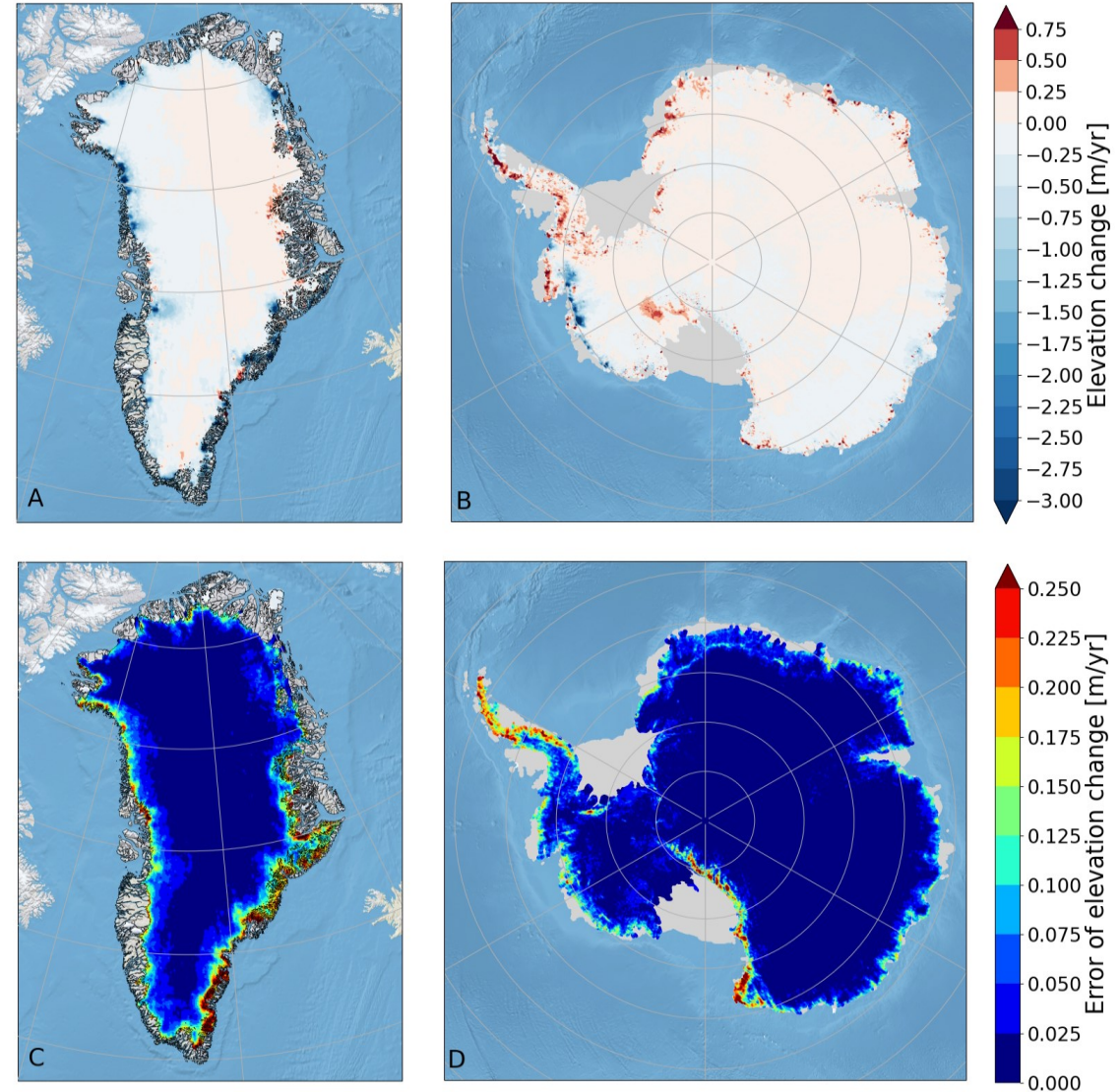


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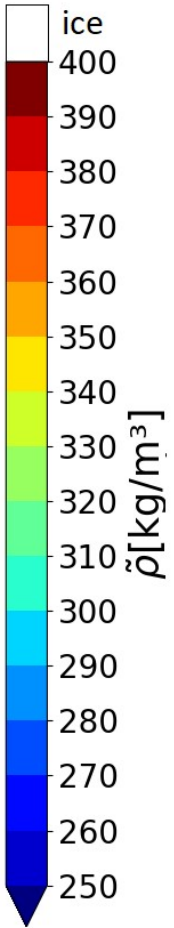
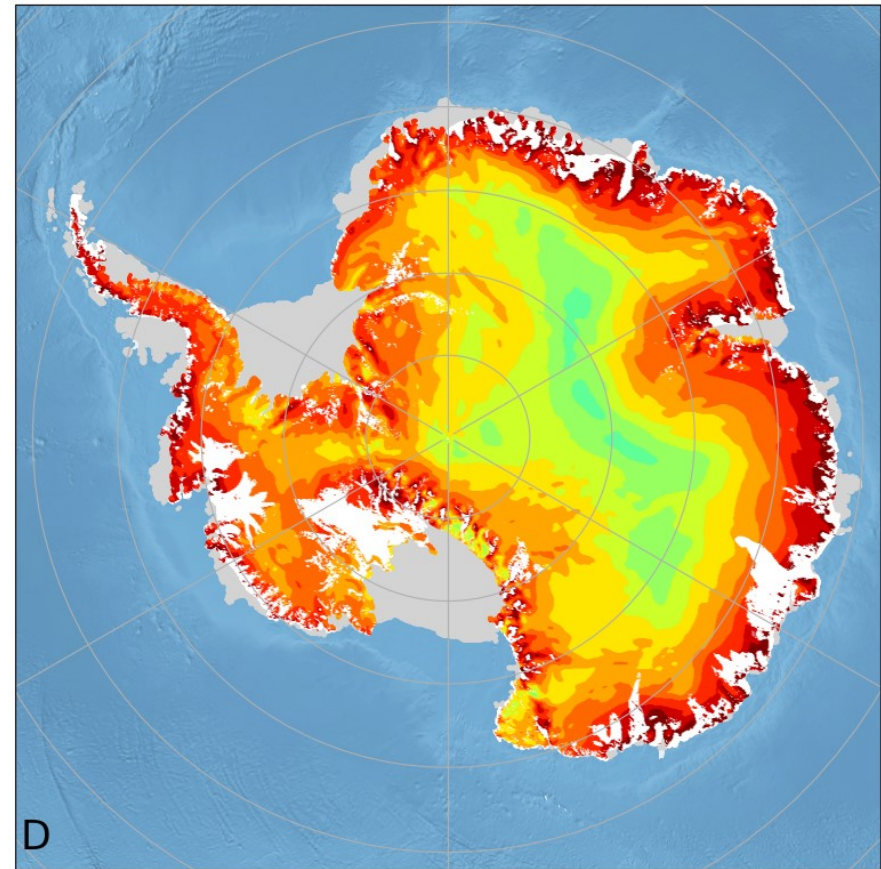
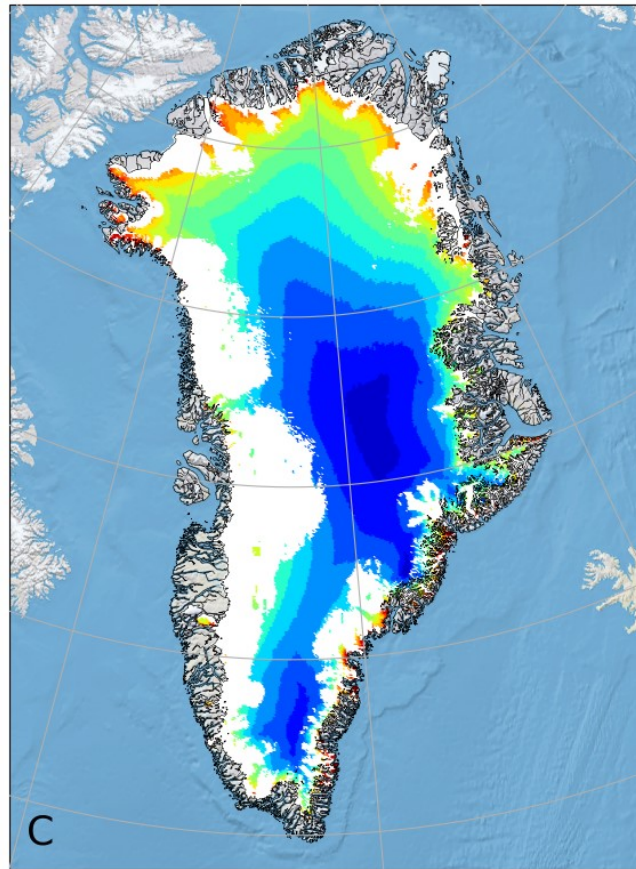
What is $\tilde{\rho}$?



$$\tilde{\rho} = \begin{cases} \rho_i, \text{ if } V_{surf} > 30 \frac{m}{yr} \text{ and } \frac{dH_{corrected}}{dt} \leq 0 \\ \rho_i, \text{ if } H \leq ELA \\ \rho_i, \text{ if dynamical ice build up is known} \\ \rho_s, \text{ elsewhere} \end{cases}$$

Volume to mass conversion

$$\tilde{\rho} = \begin{cases} \rho_i, & \text{if } V_{surf} > 30 \frac{m}{yr} \text{ and } \frac{dH_{corrected}}{dt} \leq 0 \\ \rho_i & \text{if } H \leq ELA \\ \rho_i' & \text{if dynamical ice build up is known} \\ \rho_s' & \text{elsewhere} \end{cases}$$



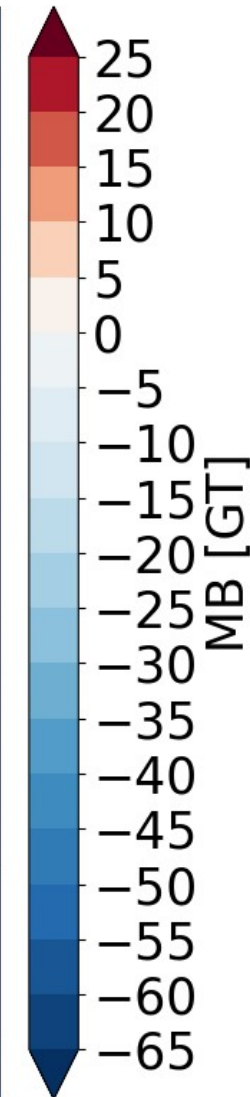
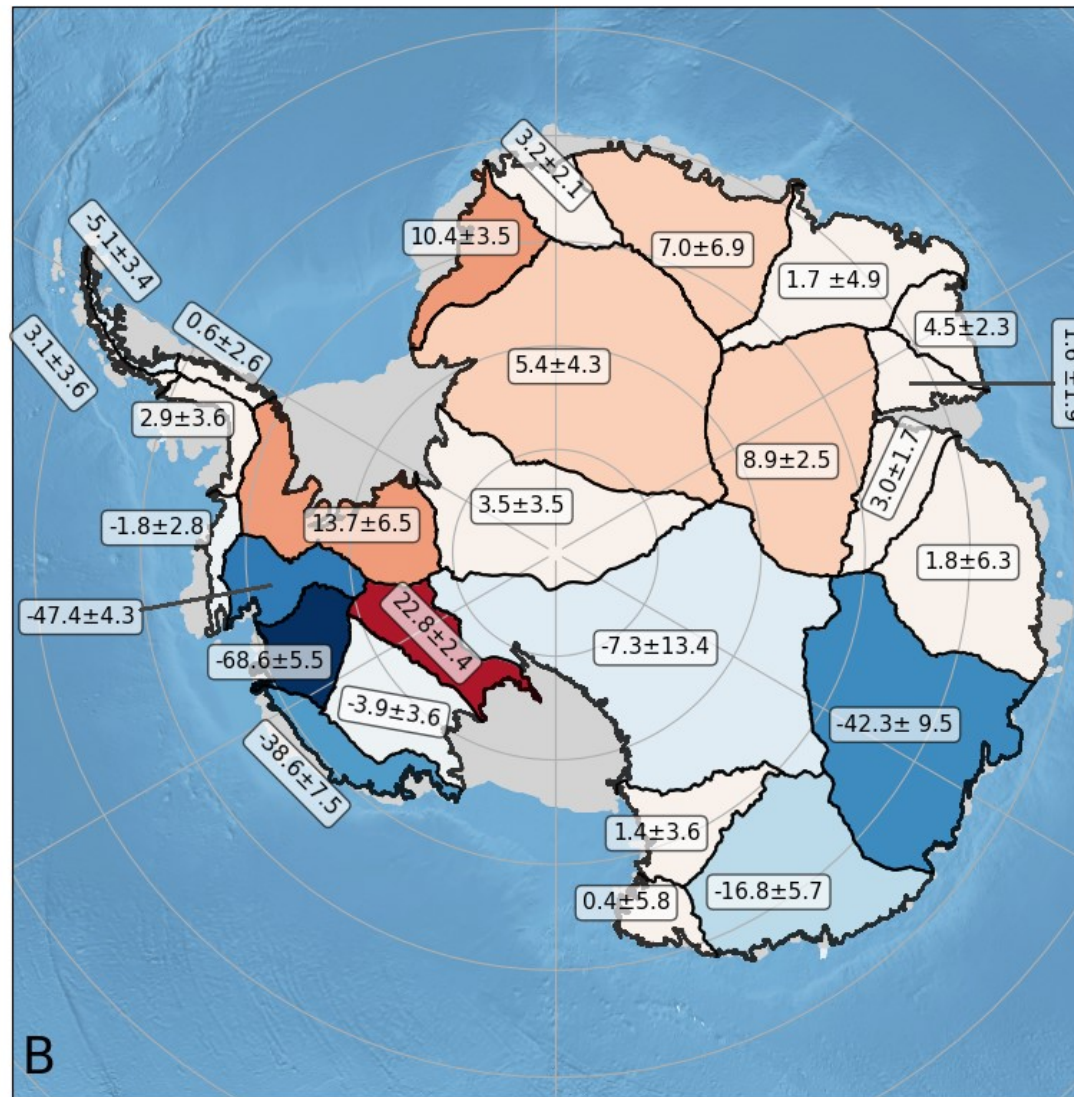
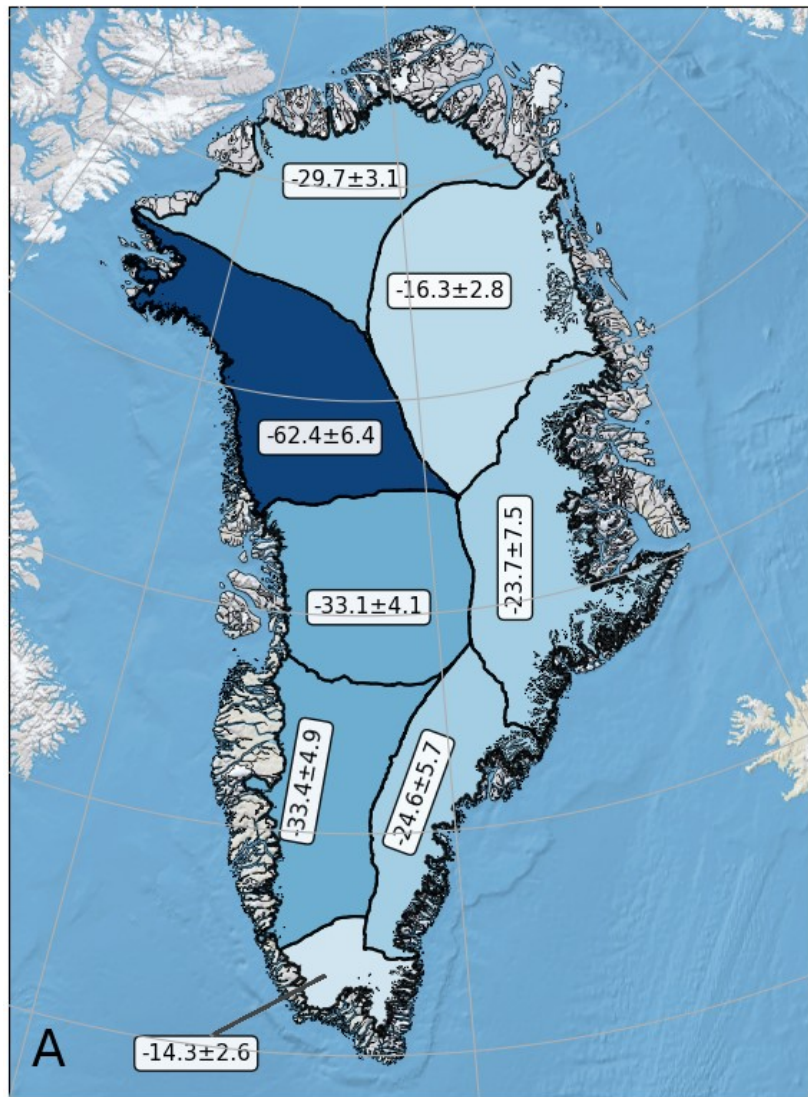
		Greenland			Antarctica			
	Unit	Total	>2000 m	<2000 m	Total	AP	WAIS	EAIS
ICESat-2	Km ³ /yr	-279.3±21.0	-19.3±7.4	-260.1±13.6	-42.9±54.0	11.0±12.9	-103.4±22.9	49.5±47.2
Firn Corr.	Km ³ /yr	-21.5± 4.5	-14.8±2.4	-6.7±2.2	-46.7±9.4	-17.1±2.2	-1.5±6.0	-28.0±6.9
Vert. Corr.	Km ³ /yr	8.10±0.01	3.29±0.00	4.81±0.01	21.80±0.03	0.80±0.01	11.22±0.02	9.78±0.02
MB	Gt/yr	-237.5±14.0	-18.7±3.6	-218.8±10.7	-135.7±27.3	1.5±6.7	-123.7±13.1	-13.5±23.0

The combined mass loss from AIS and GrIS is **-373.2 ±41.3** Gt per year, or 1.03 ± 0.11 mm global sea level rise per year

Results mass balance on basin scale

-237.5 ± 14.0

-135.7 ± 27.3



Compare to GRACE-FO

Barbara Jenny et al. 2023 (EGU23)

Jenny et al. compare different GRACE-FO solutions in the time period.

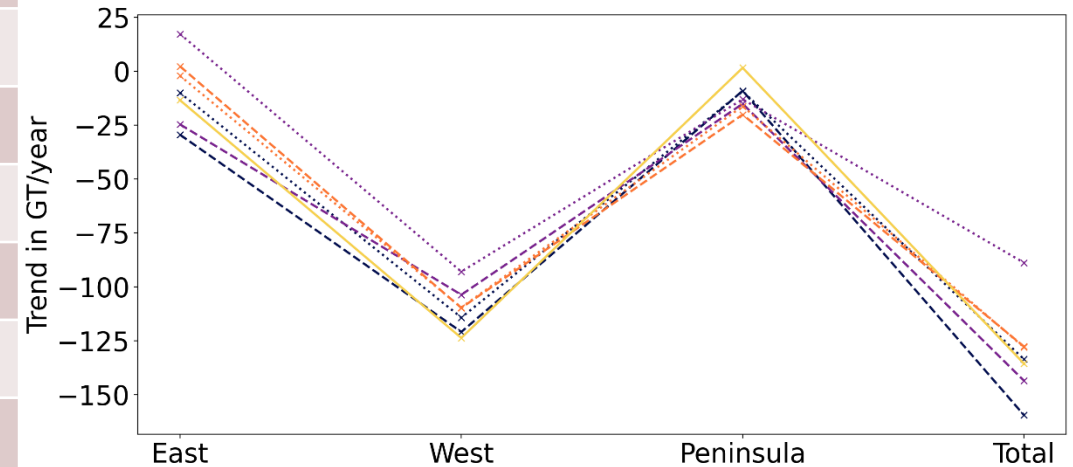
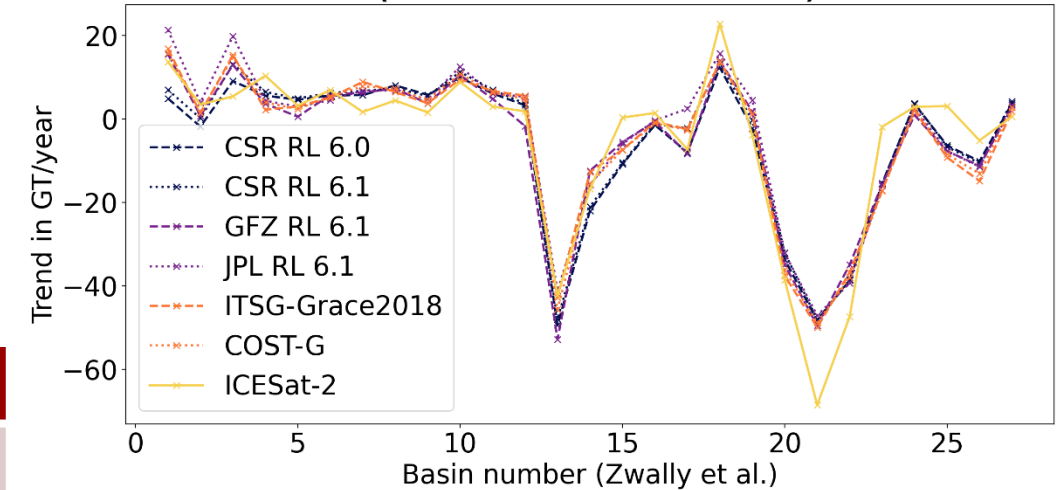
Notice: JPL is an outlier.

All numbers are in Gt per year.

Uncertainty analysis is not done yet for the GRACE-FO results
 GRACE-FO might underestimate the MB in basins 21 and 22 due to leakage

	East	West	AP	Total
CSR0600	-29.5	-120.9	-9.1	-159.6
CSR0601	-10.1	-114.3	-9.3	-133.7
ITSG	2.2	-109.8	-20.2	-127.7
GFZ	-24.7	-103.7	-15.2	-143.6
JPL	17.2	-93.0	-13.1	-88.9
COSTG	-2.2	-109.6	-16.3	-128.1
ICESat-2	-13.5±23.0	-123.7±13.1	1.5±6.7	-135.7±27.3

Trend of ice mass loss in Antarctica (10/2018 - 09/2021)

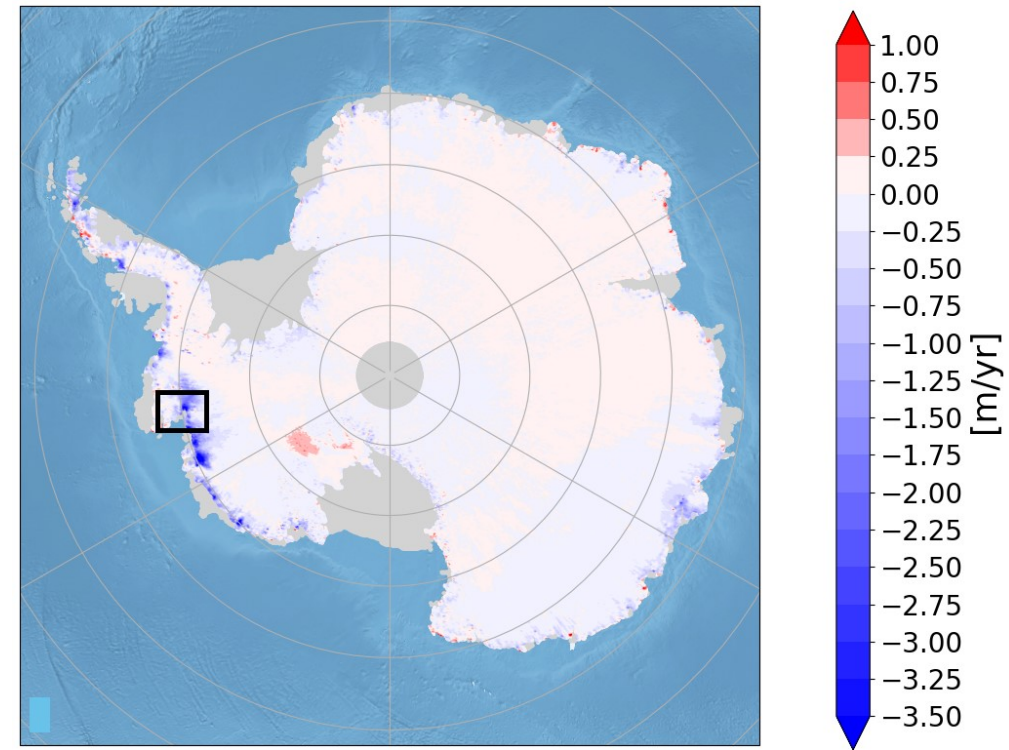


Overall the GRACE-FO agrees with our ICESat-2 analysis

Potential impact of ice mask



Developed by the Norwegian Polar Institute. Visit npolar.no/quantarctica



- The grounded AIS has lost **135.7 ±27.3** Gt per year GrIS has lost **237.5 ±14.0** Gt per year
- We emphasize the importance of accurately representing **the density** of snow and firn
- New **density parameterization** for volume-to-mass conversion

- Read our pre-print in The Cryosphere soon (submitted Monday the 24th of April)
“Revisiting ice sheet Mass balance: insights into changing dynamics in Greenland and Antarctica from ICESat-2”