Tuning phonon energies in lanthanide-doped potassium lead halide nanocrystals for enhanced nonlinearity and upconversion

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Abstract

Optical applications of lanthanide-doped nanoparticles such as sub-diffraction imaging, photodynamic therapy, and quantum cutting require materials with low phonon energies to minimize nonradiative relaxation and facilitate nonlinear processes such as photon upconversion. Heavy halide hosts offer low phonon energies, but controlled synthesis of stable, doped colloidal nanocrystals has proven challenging. Here, we synthesize low-phononenergy, KPb₂X₅ (X = Cl, Br) nanoparticles with control of diameter (from 9 to 150 nm), and we demonstrate the ability to tune nanocrystal phonon energies as low as 128 cm⁻¹ by careful selection and mixing of halide precursors. These nanoparticles are moisture resistant over 12 weeks and can be efficiently doped with lighter lanthanides. The low phonon energies of KPb2X5 nanoparticles promote upconversion emission from lanthanide excited states often quenched by multiphonon relaxation and enable highly nonlinear, avalanche-like emission from KPb₂Cl₅:Nd³⁺ nanoparticles. The realization of nanoparticles with tunable, ultra-low phonon energies provides an approach for discovering nanomaterials with phonon-dependent properties precisely engineered for applications in nanoscale imaging, sensing, and energy conversion.

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Inorganic nanocrystals embedded with lanthanide (Ln^{3+}) ions can generate photostable luminescence that drives applications in near-infrared microscopy,¹ sub-diffraction imaging,^{2,3} lasing,⁴ therapeutics,⁵ sensing,^{6,7} optogenetics,⁸ and quantum cutting.^{9,10} The optical performance of these doped materials is strongly influenced by the maximum phonon energy ($\hbar \omega_{\text{max}}$) of the nanocrystal host matrix. At moderate and high $\hbar \omega_{\text{max}}$, luminescence is quenched as Ln^{3+} excited states nonradiatively relax via phonon emission, and emission lines are modulated further *via* phonon-assisted energy transfer (PAET). Precise methods for tuning phonon energies would be valuable for manipulating the complex photophysical networks in Ln^{3+} -based nanocrystals¹¹ and for improving efficiencies of nonlinear optical processes such as upconversion, downconversion,^{9,10} and photon avalanching.¹²

To generate upconverted luminescence, Ln^{3+} ions are frequently doped or alloyed into fluoride matrices such as β -NaYF₄ to leverage their low $\hbar\omega_{\text{max}}$ values (300-500 cm⁻¹)¹³⁻¹⁶ relative to alternate hosts like oxides (500-600 cm⁻¹), oxysulfides (~520 cm⁻¹), vanadates (~890 cm⁻¹), and garnets (900-1400 cm⁻¹).¹⁷ Low phonon energies discourage multi-phonon relaxation (MPR) because MPR rates decrease exponentially as a greater number of phonons ($\Delta E/\hbar\omega_{\rm max}$) are needed to bridge the energy gap ΔE between adjacent Ln^{3+} states (**Figure 1A**). However, MPR is still prevalent in fluoride nanoparticles (NPs), lowering their quantum yields¹⁸ and limiting applications.

Host matrices based on chlorides, bromides, and iodides exhibit lower phonon energies (120-260 cm⁻¹)^{19,20} than corresponding fluorides, but synthesis of these halides as doped nanocrystals remains challenging. In addition, many, like LaCl₃ ($\hbar \omega_{\text{max}} \approx 250 \text{ cm}^{-1}$),²¹ are hygroscopic and decompose in ambient conditions, limiting their development and utility. Bulk KPb₂Cl₅ and KPb₂Br₅ crystals are reportedly more moisture-tolerant than other halides and have bandgaps (3.77 and 3.46 eV, respectively)^{22,23} sufficiently wide to be transparent to visible luminescence. While bulk and microscale $(>200 \text{ nm})^{24}$ crystals of KPb₂Cl₅ have been reported, robust methods for size-controlled synthesis and doping of their NPs analogues are needed, in addition to characterization of their luminescence, stability, and technological applicability. Here, we describe colloidal synthesis of $Ln³⁺$ -doped nanocrystals with ultra-low phonon energies using KPb_2X_5 ($X = Cl$, Br) host matrices (**Figure 1A**), and characterize their luminescence and environmental stability. We demonstrate that KPb_2X_5 NP phonon energies can be tuned readily through alloying of their halide ions, and that these perovskite-like nanomaterials are stable under high humidity. The ultra-low $\hbar \omega_{max}$ of these NPs promote upconversion luminescence from Ln³⁺ excited states typically quenched in conventional matrices with higher $\hbar \omega_{max}$ and give rise to steeply nonlinear luminescence in Nd^{3+} -doped KPb₂Cl₅.

To synthesize KPb₂X₅ NPs, we rapidly injected myristoyl halide precursors into 100-310 °C solutions of Pb(OAc)4, K2CO3, oleylamine (OM), oleic acid (OA), and octadecene (ODE) (see full synthetic protocols in Supporting Information). Acyl halides react readily with nucleophiles such as OM and oleate ions to release hydrohalic acids (HX) that can react with metal precursors to nucleate and grow KPb_2X_5 NPs.²⁵ We selected myristoyl halides as precursors due to their high boiling points (\sim 250 °C), which allows for higher reaction temperatures that promote crystallinity and size control of NPs via temporally distinct nucleation.

High-resolution transmission electron microscopy (HRTEM) of KPb₂Cl₅ NPs (**Figure S1**) shows 2.70 Å lattice spacings corresponding to the (311) crystal plane of monoclinic KPb₂Cl₅ with P21/c space group, matching measured and reference (PDF# 01-073-4316) powder X-ray diffraction (XRD) patterns (**Figure 1B)**. 24

Figure 1. (A) Monoclinic KPb2Cl5 lattice and the impact of its low phonon energy (*ħ*w*max***) on the multi-phonon relaxation (wavy arrows) of Ln3+ excited states (E1/E2, populations represented by numbers of circles). (B) XRD patterns of KPb2Cl5, KPb2(BrxCl1-x)5, and KPb2Br5 NPs synthesized with 6:1 OA/OM. (C-E) TEM of KPb2Cl5 NPs synthesized by tuning OA/OM.** (F-H) TEM of KPb₂Cl₅, KPb₂(Br_xCl_{1-x)5}, and KPb₂Br₅ NPs synthesized with 6:1 OA/OM. Scale bars in C-H are **50 nm. (I) Diameter vs reaction temperature for KPb2Cl5 NPs synthesized with 6:1 OA/OM. (J) Diameter vs OA/OM at 240 °C. Error bars in (I,J) represent ±1 standard deviation in size distribution.**

Reaction temperature and OA/OM ratio can each be varied to tune NP size (**Figure 1C-E**, **S2-4**) while maintaining reasonable polydispersity. Varying reaction temperature from 100 to 310 °C produces KPb2Cl5 NPs with diameters ranging from 8.9 to 155.0 nm at 6:1 OA/OM (**Figure 1I**). Meanwhile, varying OA/OM from 1:1 to 8:1 fine-tunes diameters from 11.9 to 49.7 nm (240 °C, **Figure 1J**). NP size distributions range from 7 to 50%, (**Figure S3-4**), with the narrowest distributions at low OA/OM and temperature. Increasing OA/OM may increase size and polydispersity by promoting protonation of OM by OA and their condensation into N-oleyloleamide.26 These reactions can deactivate OM as a nucleophile for acyl halide decomposition, suppressing nucleation.^{26,27} OA may also increase NP size by increasing the solubility of metal salts, decreasing nucleation and nuclei growth rates²⁸ while promoting Ostwald ripening (see Supporting Information). 29

To determine if this synthetic scheme could produce metal halide nanocrystals with even lower and more tunable phonon energies, we combined appropriate ratios of chloride and bromide precursors to synthesize KPb₂Br₅ and mixed-halide KPb₂(Br_xCl_{1-x})₅ NPs (**Figure 1F-H**). Under the same reaction conditions (240 °C and 6:1 OA/OM), KPb2Cl5, KPb2(Br0.375Cl0.625)5, and KPb2Br5 NPs were synthesized with similar sizes (~40 nm, **Figure S5**). XRD patterns of KPb2Cl5, KPb2(Br0.375Cl0.625)5, and KPb2Br5 NPs (**Figure 1B**) show pure monoclinic phases, and the single [211] peak of KPb₂(Br_{0.375}Cl_{0.625}) (2 θ =23.39°) is positioned between the peaks of pure KPb₂Cl₅ (24.14°) and KPb₂Br₅ (22.94°), corroborating the 5:3 Br:Cl atomic ratio measured by energy-dispersive X-ray spectroscopy (EDS, **Figure S6**) and confirming their successful alloying. Amplitude-averaged phonon energies, extracted from Raman spectra (**Figure 2A**), were 152, 136, and 128 cm⁻¹ for undoped KPb₂Cl₅, KPb₂(Br_{0.375}Cl_{0.625})₅ and KPb₂Br₅ NPs, respectively. These phonon energies are consistent with those measured for bulk crystals and decrease with the increasing mass of

the halide ion.¹⁹ Notably, KPb₂Cl₅ nanocrystal phonon energies are 2-fold smaller than the \sim 309 cm⁻¹ average phonon energy of β -NaYF₄ NPs (**Figure 2A**) most commonly used in Ln^{3+} -based photon upconversion.

Figure 2. (A) Raman spectra of undoped KPb2Cl5, KPb2(Br0.375Cl0.625)5, KPb2Br5, and NaYF4 NPs. (B) Upconverted emission spectra of Yb3+, Er3+-codoped KPb2X5 and NaYF4 NPs under 980 nm excitation (101 W/cm2). Peaks are labeled by radiative state. *Second order laser artifact.

We further investigated if KPb_2X_5 nanocrystals could host Ln^{3+} ions, and how lower phonon energies influence their luminescence, by incorporating Yb³⁺ and Er³⁺ into reaction solutions. To confirm doping, we measured the elemental compositions of the resulting KPb2X5 NPs using EDS (**Figure S8-9**), X-ray photoelectron spectroscopy (**Figure S10**) and inductively coupled plasma optical emission spectroscopy (ICP-OES, **Table S1-2**). Upconversion luminescence spectra of dried KPb₂X₅:Yb³⁺, Er³⁺ NPs were measured at ambient conditions under 980 nm excitation and examined for differences with canonical NaYF4:Yb³⁺, Er³⁺ UCNPs. Compared to their NaYF4 counterparts, KPb₂Cl₅: 2.9% Yb³⁺, 0.6% Er³⁺ NPs show significantly stronger 525 nm emission (Er³⁺:²H_{11/2}→⁴I_{15/2}) with respect to their 545 nm (${}^4S_{3/2} \rightarrow {}^4I_{15/2}$) band, approaching a 1:1 ratio. In NaYF₄, the Er³⁺:²H_{11/2} and ${}^4S_{3/2}$ manifolds are assumed to be thermally equilibrated since the small, \sim 700 cm⁻¹ energy gap between them is readily bridged by 2 phonons. The enhanced population of the ²H_{11/2} level in KPb₂Cl₅, suggests a dramatic reduction in MPR rate owing to the 2-fold lower $\hbar \omega_{max}$. The NPs also exhibit significantly diminished 660 nm emission ($Er^{3+4}F_{9/2} \rightarrow {}^{4}I_{15/2}$) relative to green emission peaks and a prominent emission band around 490 nm $(^{4}F_{7/2} \rightarrow ^{4}I_{15/2})$ (**Figure 2B**, **Figure S11-12**). This 490 nm band is typically absent in NaYF4:Yb³⁺,Er³⁺ UCNPs; its intensity is enhanced as $\hbar \omega_{max}$ of the host decreases [compare KPb2(Br0.375Cl0.625)5 and KPb2Br5 in **Figure 2B**], providing additional evidence for reduced MPR. To understand the origins of these spectral differences, we used rate equation models (see Supporting Information) to show that 660 nm emission from $KPb_2Cl_5:Yb^{3+},Er^{3+}$ is suppressed due to reduced rates of phonon-assisted transitions that populate the ⁴F_{9/2} manifold, e.g., MPR from the Er³⁺:⁴S_{3/2} manifold (Figure S23A) and cross-relaxation involving the MPR-populated Er³⁺:⁴I_{13/2} manifold (**Figure S23B**).^{16,30} In contrast, emission at 490 and 525 nm is enhanced due to reduced MPR from corresponding Er^{3+} :⁴ $F_{7/2}$ and ² $H_{11/2}$ radiative states (**Figure S23C**). For a complete mechanistic

discussion, see Supporting Information Section S6. We note that KPb₂X₅ NPs are not always brighter, and often dimmer, than their NaYF₄ analogues. These comparisons highlight the fact that low-phonon-energy hosts alone may not necessarily improve upconversion intensities, since MPR or PAET is often required to populate states critical to luminescence pathways. Still, the ability to manipulate MPR and PAET rates by tuning host phonon energies provides a method to modulate luminescence from $Ln³⁺$ -doped NPs and promote emission from excited states normally quenched by MPR, as shown in unconventional upconversion and downshifting spectra of KPb2Cl₅ NPs doped with Ho^{3+} , Pr^{3+} , Nd^{3+} , Dy^{3+} , and Im^{3+} (**Figure S14**).

Considering the hygroscopicity and instability of other low-phonon-energy materials, we evaluated the chemicaland photo-stability of the KPb₂Cl₅:Yb³⁺,Er³⁺ NPs under ambient conditions at relative humidities (RH) of 65 and 100%. Films of KPb2Cl5 NPs are chemically stable over the course of three months under 65% RH, as demonstrated by the invariance of XRD patterns and upconversion emission intensity (**Figure 3A** and inset). Even at 100% RH, emission spectra (**Figure 3B**) and XRD patterns (**Figure S15**) do not show notable changes after 12 h. KPb2Cl5:Yb3+,Er3+ NPs are also photostable under continuous 980 nm laser irradiation (35 W/cm2) for 15 h (**Figure S16**), similar to NaYF₄ UCNPs. However, immersing powder samples in water causes decomposition of KPb₂Cl₅ NPs (**Figure S17-18**), indicating that additional surface passivation is necessary for aqueous applications.

Figure 3. Stability of KPb2Cl5:Yb3+, Er3+ NPs exposed to (A) 65% RH over 12 weeks, measured by XRD, and to (B) 100% RH over 12 hours, investigated with in situ upconverted luminescence. Insets show temporal evolution of upconversion intensity. XRD pattern colors in (A) indicate exposure times shown in inset.

ICP-OES of Er^{3+}/Yb^{3+} doping into KPb₂X₅ NPs reveals that these heavy Ln³⁺ ions are not efficiently incorporated, regardless of reaction stoichiometry (**Table S1-2**), likely due to differences in charge and ionic radii between Ln^{3+} and Pb^{2+} ions.^{31–34} Because the larger radii of lighter Ln³⁺ ions have smaller mismatch with the Pb²⁺-based matrix, we doped KPb₂Cl₅ NPs with Nd³⁺ ions, commonly used to sensitize 800 nm excitation. ICP-OES shows that KPb₂Cl₅ NPs can be doped with Nd³⁺ ions, with the actual Nd³⁺ composition measured to be 36% of nominal inputs (**Figure 4A**, Table S3). Under 800 nm excitation at ambient conditions, KPb₂Cl₅:0.4% Nd³⁺ NPs demonstrate downshifted NIR emission (883, 1062, 1340 nm) and visible upconversion to 533, 595, and 660 nm (**Figure 4B, Figure S19**), which is notable since upconversion in Nd³⁺-co-doped NaYF₄ has only been observed at >10⁶ W/cm² excitation in single UCNPs.³⁵ The ability to control Nd³⁺ doping in KPb₂Cl₅ was also confirmed by the monotonic decrease of the $4F_{3/2}$

excited-state lifetime (**Figure 4B** inset, **Figure S19**); this quenching is associated with cross-relaxation between Nd³⁺ ions at high concentrations. The ${}^{4}F_{3/2}$ lifetime in KPb₂Cl₅:4.1% Nd³⁺ NPs (220 µs) is greater than that of core/shell NaGdF4:5%Nd³⁺@NaGdF4 NPs (136 µs),³⁶ and is the result of reduced MPR in KPb2Cl5.

Figure 4. (A) Actual versus nominal [Nd3+] incorporation in KPb2Cl5:Nd3+ NPs, measured by ICP-OES. (B) Upconverted (*left*) and downshifted (*right*) luminescence spectra of KPb₂Cl₅:0.4% Nd³⁺ NPs under 800 nm (14 W/cm²) excitation. Inset: $4E_{32}$ excitation are approximately as a set of the lifetimes vs nominal INd³⁺¹ $^{4}F_{3/2}$ excited state lifetimes vs nominal [Nd³⁺].

The low phonon energy of KPb₂Cl₅ allows us to observe highly nonlinear upconversion emission at visible and NIR wavelengths from heavily doped KPb2Cl5:16% Nd3+ NPs excited at 1064 nm at room temperature (**Figure 5A**). As the excitation power density (P) is increased above a threshold of \sim 10 kW/cm², the luminescence intensities (I) of major emission lines increase nonlinearly (**Figure 5B**) with power dependence *s* reaching 9 and 12, at 595 nm and 810 nm, respectively (where $I \propto P^s$). We ascribe this steep power dependence to an energy looping mechanism³⁷ that nonlinearly amplifies Nd^{3+} excited state populations through repeated cycles of excited state absorption and crossrelaxation (**Figure S24**). Energy looping and its extreme form, photon avalanching (PA),² have been predicted in NaYF4:Nd³⁺ NPs but not observed experimentally.³⁸ KPb₂Cl₅:16% Nd³⁺ NPs meet some (but not all) criteria for PA, including threshold-like behavior (**Figure 5B**) and luminescence rise times that lengthen significantly, to \sim 70 ms, near avalanching thresholds (**Figure S21**). Such steep nonlinearities suggest that these Nd³⁺-doped, low-phonon-energy NPs may be useful as probes for sub-diffraction confocal imaging, since the nonlinear Abbe resolution $\delta =$ $\lambda/(2 NA\sqrt{s})$ is 100 nm for $s = 12$ at 1064 nm pump wavelength (λ) and 1.4 numerical aperture (NA).

Figure 5. (A) Visible and NIR upconversion spectrum of KPb2Cl5: 16%Nd3+ NPs under 1064 nm excitation. (B) Emission intensity vs excitation power of the most intense Nd3+ upconversion bands, showing steeply nonlinear upconversion. Dashed lines are linear fits at maximum slope *s* **for each curve.**

We have demonstrated the size-controlled synthesis of low-phonon-energy, $Ln³⁺$ -doped KPb₂X₅ NPs stable towards humidity. The ultra-low phonon energies of these materials (120-160 cm⁻¹) enabled discovery of highly nonlinear, avalanche-like Nd^{3+} emission and Ln^{3+} emission lines not observed in fluoride UCNPs, facilitating multicolor widefield and sub-diffraction imaging. Finally, intensities of low-phonon-energy NPs suggest that Ln³⁺ luminescence is maximized not at the lowest phonon energies, but at phonon energies that simultaneously minimize deleterious MPR while maintaining critical phonon-assisted pathways. The mixed-halide alloying approach demonstrated here will facilitate such optimization and will be valuable for manipulating complex photophysical networks in Ln³⁺-based nanomaterials and other phonon-dependent systems.

Author Contributions

#These authors contributed equally. All authors have given approval to the final manuscript.

Notes

The authors declare no competing financial interest.

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