Block-Wise Bordered Magic Squares Multiples of 11

Inder J. Taneja¹

Abstract

During past years author worked with **block-wise borderedmagic squares** of even number blocks. These are based on equal sums magic squares of orders 4, 6, 8, 10, etc. This type of work is an extension of classical bordered magic squares. In case of multiples of 4, the extension is made for pandiagonal magic squares [23]. For multiples of order 6 refer Taneja [24]. For the first time, we are presenting here bordered magic squares of odd number blocks. Recently, author worked on multiples of 3, 5, 7 and 9. These are based on different sums of magic squares of order 3, 5, 7 and 9 [29, 30, 31, 32]. This work is for multiples of 11. This we have done with three different types of magic squares of order 11. Higher order examples can be seen in **Excel files** attached with the work. The total work is up to order 154.

¹Formerly, Professor of Mathematics, Federal University of Santa Catarina, Florianópolis, SC, Brazil (1978-2012). Also worked at Delhi University, India (1976-1978). *E-mail:* ijtaneja@gmail.com; *Web-sites:* http://inderjtaneja.com; http://numbers-magic.com; Twitter: @IJTANEJA; Instagram: @crazynumbers.

Contents

1	Introduction	2
	1.1 Summary of Bordered Magic Squares	3
	1.1.1 Odd Numbers Multiples	3
	1.1.2 Even Numbers Multiples	3
	Block-Wise Bordered Magic Squares Multiples of 11	3
	2.1 Bordered Magic Squares of Orders 13 and 14	3
	2.2 Magic Squares of Order 55	6
	2.3 Magic Squares of Order 44	10
	2.4 Magic Squares of Order 33	14
3	Author's Contribution to Recreation of Numbers and Magic Squares	17

Introduction 1

During past years author [2, 3, 4, 5, 6, 7, 8] worked with **block-wise** magic squares from orders 12 to 47. Author [9, 10, 11, 12, 13, 14] also worked with **bordered** magic squares. The study on **bordered** magic squares is extended to **block-bordered** magic squares [15, 16, 17]. This is specially done for the magic squares of orders p and 2p, where p is a prime number. This study is still extended to **block-wise bordered** magic squares [18, 19, 20, 21]. Some conection with Pythagorean triples and area-representations are also made [23, 24, 25, 26, 27]. The main property of bordered magic squares is that if we remove external borders, still we get **sub-bordered** magic squares, i.e., each layer in itself lead us to magic squares. In many cases, the properties of bordered magic square are seperated by even and odd orders magic squares. In many cases, we get good properties for the even order bordered magic squares. In some cases, we have to use fractional numbers to reach minimum perfect square sum of entries. For more study on **bordered** magic squares refer H. White's web-site [1].

The idea of bordered magic squares is already discussed by H. White's web-site [1] where the borders are of single digits. Borders multiples of even numbers starting from order 4 are done extensively by author [23, 24, 25, 26, 27, 28].

Recently, for the first time, we presented bordered magic squares of odd number blocks. In case of multiples of 3, we worked with different sums magic squares of order 3. In case of multiples of 5, 7 and 9, we worked with **pandiagonal** and **bordered** magic squares of orders 5, 7 and 9. This work is for multiples of 11. Here also we work with three types of magic squares of order 11. One of them is **pandiagonal** and another two are **bordered** and **block**bordered magic squares of order 11. The procedure, how to get these block-wise bordered magic squares is also explained. This work is up to order 55. Higher orders examples can be seen in Excel files attached with this work. Before proceeding further, let's summarize, the idea of block-wise bordered magic squares:

1.1 Summary of Bordered Magic Squares

1.1.1 Odd Numbers Multiples

- **Single Digit:** Bordered magic squares based on single digit [9, 10, 1].
- Three Digits: Bordered magic squares based on magic squares of order 3 [29].
- Five Digits: Bordered magic squares based on magic squares of order 5 [30].
- Seven Digits: Bordered magic squares based on magic squares of order 7 [31].
- Nine Digits: Bordered magic squares based on magic squares of order 9 [32]
- Eleven Digits: Bordered magic squares based on magic squares of order 11 [33] (This work)

1.1.2 **Even Numbers Multiples**

- Two Digits: Bordered magic squares based on magic rectangles multiples of 2 [60, 61, 62, 63, 63, 64].
- Four Digits: Bordered magic squares based on magic squares of order 4 [23].
- Six Digits: Bordered magic squares based on magic squares of order 6 [24].
- **Eight Digits:** Bordered magic squares based on magic squares of order 8 [25].
- **Ten Digits:** Bordered magic squares based on magic squares of order 10 [26].
- **Twelve Digits:** Bordered magic squares based on magic squares of order 12 [27].
- Fourteen Digits: Bordered magic squares based on magic squares of order 14 [28].

The advantage in working with even number multiples is that we can work with equal sums blocks of magic squares.

Let's see below the some examples of **block-wise bordered** magic squares multiples 11, where magic squares of order 11 are considered in two different ways.

Block-Wise Bordered Magic Squares Multiples of 11 2

Bordered Magic Squares of Orders 13 and 14 2.1

Let's consider **bordered** magic square of orders 13 and 14 given by

													1105
15	3 146	148	150	152	154	11	10	8	6	4	2	156	1105
23	136	126	128	130	132	33	32	30	28	26	134	147	1105
2'	43	118	110	112	114	51	50	48	46	116	127	149	1105
19	41	59	104	98	100	65	64	62	102	111	129	151	1105
17	39	57	71	94	90	75	74	92	99	113	131	153	1105
15	37	55	69	79	88	81	86	91	101	115	133	155	1105
13	35	53	67	77	83	85	87	93	103	117	135	157	1105
16	1 139	121	107	97	84	89	82	73	63	49	31	9	1105
16	3 141	123	109	78	80	95	96	76	61	47	29	7	1105
6	5 143	125	68	72	70	105	106	108	66	45	27	5	1105
6	7 145	54	60	58	56	119	120	122	124	52	25	3	1105
6	36	44	42	40	38	137	138	140	142	144	34	1	1105
14	24	22	20	18	16	159	160	162	164	166	168	12	1105
10	5 1105	1105	1105	1105	1105	1105	1105	1105	1105	1105	1105	1105	1105

The entries of above two magic squares are sequential numbers starting from 1:

 $D_{13\times 13} := \{1, 2, \dots, 168, 169\}$ $D_{14\times 14} := \{1, 2, \dots, 195, 196\}$

The property of **bordered** magic squares is that removing the upper borders still we are left with magic squares of sequential values. Multiplying each entry of above two magic squares of orders 13 and 14 by 121, we get

													133705
19118	17666	17908	18150	18392	18634	1331	1210	968	726	484	242	18876	133705
2783	16456	15246	15488	15730	15972	3993	3872	3630	3388	3146	16214	17787	133705
2541	5203	14278	13310	13552	13794	6171	6050	5808	5566	14036	15367	18029	133705
2299	4961	7139	12584	11858	12100	7865	7744	7502	12342	13431	15609	18271	133705
2057	4719	6897	8591	11374	10890	9075	8954	11132	11979	13673	15851	18513	133705
1815	4477	6655	8349	9559	10648	9801	10406	11011	12221	13915	16093	18755	133705
1573	4235	6413	8107	9317	10043	10285	10527	11253	12463	14157	16335	18997	133705
19481	16819	14641	12947	11737	10164	10769	9922	8833	7623	5929	3751	1089	133705
19723	17061	14883	13189	9438	9680	11495	11616	9196	7381	5687	3509	847	133705
19965	17303	15125	8228	8712	8470	12705	12826	13068	7986	5445	3267	605	133705
20207	17545	6534	7260	7018	6776	14399	14520	14762	15004	6292	3025	363	133705
20449	4356	5324	5082	4840	4598	16577	16698	16940	17182	17424	4114	121	133705
1694	2904	2662	2420	2178	1936	19239	19360	19602	19844	20086	20328	1452	133705
133705	133705	133705	133705	133705	133705	133705	133705	133705	133705	133705	133705	133705	133705

	Block-
May 2	4, 2023,

														166859
22143	20812	21054	21296	23232	23474	3146	2904	2662	2420	726	484	242	22264	166859
2299	19239	18150	18392	20207	20449	5808	5566	5324	3751	3509	3267	19360	21538	166859
2057	5203	16819	15972	16214	17666	7986	7744	7502	6292	6050	16940	18634	21780	166859
1815	4840	7381	14883	14278	15609	9680	9438	8349	8107	15004	16456	18997	22022	166859
1331	4719	7139	9196	13431	13068	10890	10648	9922	13552	14641	16698	19118	22506	166859
1089	4114	6655	9075	10527	12826	12463	11374	11011	13310	14762	17182	19723	22748	166859
121	3872	5929	8470	9801	11132	11253	12584	12705	14036	15367	17908	19965	23716	166859
21659	18755	16577	14520	13673	11495	11858	11979	12342	10164	9317	7260	5082	2178	166859
21901	18876	17061	15125	13794	12221	12100	11737	11616	10043	8712	6776	4961	1936	166859
22385	19481	17303	15246	10285	10769	12947	13189	13915	10406	8591	6534	4356	1452	166859
22627	19602	17424	8833	9559	8228	14157	14399	15488	15730	8954	6413	4235	1210	166859
22869	19844	6897	7865	7623	6171	15851	16093	16335	17545	17787	7018	3993	968	166859
22990	4477	5687	5445	3630	3388	18029	18271	18513	20086	20328	20570	4598	847	166859
1573	3025	2783	2541	605	363	20691	20933	21175	21417	23111	23353	23595	1694	166859
166859	166859	166859	166859	166859	166859	166859	166859	166859	166859	166859	166859	166859	166859	166859

In this case, the entries distributions of these two magic squares are given by

 $D_{13\times 13} := \{121, 242, \dots, 20328, 20449\}$ $D_{14\times 14} := \{121, 242, \dots, 23595, 23716\}.$

Let's consider following three magic squares of order 11.

	pan	671	671	671	671	671	671	671	671	671	671	671
671	1	21	30	39	48	57	77	86	95	104	113	671
671	101	121	9	18	27	36	45	65	74	83	92	671
671	80	89	109	118	6	15	24	44	53	62	71	671
671	59	68	88	97	106	115	3	12	32	41	50	671
671	38	47	56	76	85	94	103	112	11	20	29	671
671	17	26	35	55	64	73	82	91	100	120	8	671
671	117	5	14	23	43	52	61	70	79	99	108	671
671	96	105	114	2	22	31	40	49	58	67	87	671
671	75	84	93	102	111	10	19	28	37	46	66	671
671	54	63	72	81	90	110	119	7	16	25	34	671
	33	42	51	60	69	78	98	107	116	4	13	671
	671	671	671	671	671	671	671	671	671	671	671	671

											671
12	20	18	16	14	113	114	116	118	120	10	671
121	28	100	98	96	95	32	34	36	30	1	671
119	21	78	74	76	41	40	38	80	101	3	671
117	23	37	70	73	53	55	54	85	99	5	671
115	25	39	50	60	65	58	72	83	97	7	671
11	93	79	51	59	61	63	71	43	29	111	671
13	91	77	66	64	57	62	56	45	31	109	671
15	89	75	68	49	69	67	52	47	33	107	671
17	87	42	48	46	81	82	84	44	35	105	671
19	92	22	24	26	27	90	88	86	94	103	671
112	102	104	106	108	9	8	6	4	2	110	671
671	671	671	671	671	671	671	671	671	671	671	671

											671
12	20	18	16	14	113	114	116	118	120	10	671
121	42	91	50	47	84	52	40	89	54	1	671
119	55	41	87	48	43	92	53	45	85	3	671
117	86	51	46	88	56	39	90	49	44	5	671
115	60	28	95	65	21	97	58	26	99	7	671
11	100	59	24	93	61	29	98	63	22	111	671
13	23	96	64	25	101	57	27	94	62	109	671
15	78	73	32	83	66	34	76	71	36	107	671
17	37	77	69	30	79	74	35	81	67	105	671
19	68	33	82	70	38	75	72	31	80	103	671
112	102	104	106	108	9	8	6	4	2	110	671
671	671	671	671	671	671	671	671	671	671	671	671

Let's replace each entry in above two magic squares of orders 13 and 14 by above two magic squares of order 11. The entries chosen in these magic squares are as given below:

> $121 \rightarrow 1, 2, \dots, 121$ $242 \rightarrow 122, 123, \dots, 242$ $363 \rightarrow 243, 244, \dots, 363$ $\ldots \rightarrow \ldots$ \ldots $23595 \rightarrow 23475, 23476, \dots, 23595$ $23716 \rightarrow 23596, 23597..., 23716$

This lead us to two big **block-bordered** magic squares of orders 143 and 154. Since these two magic squares are very big, these are given in two **excel** files attached with this work.

The multiples blocks are two different kinds of magic squares of order 11. Based on these two big magic squares we get the following magic squares.

Magic Squares of Order 55 2.2

Below are three magic squares of order 55 obtained from magic squares of order 143. It is obtained by the application of the formula ormula $\frac{a^2 - b^2}{2}$, a > b, i.e., subtract $\frac{143^2 - 55^2}{2} := 8712$ from each entry of magic squares order 143, we get the following two magic squares of order 55:

				83215
2542 2562 2571 2580 2589 2598 2618 2627 2636 2645 2654	54 2058 2078 2087 2096 2105 2114 2134 2143 2152 2161 2170 243	3 263 272 281 290 299 319 328 337 346 355	122 142 151 160 169 178 198 207 216 225 234	2300 2320 2329 2338 2347 2356 2376 2385 2394 2403 2412 83215
2642 2662 2550 2559 2568 2577 2586 2606 2615 2624 263	33 2158 2178 2066 2075 2084 2093 2102 2122 2131 2140 2149 343	3 363 251 260 269 278 287 307 316 325 334	222 242 130 139 148 157 166 186 195 204 213	2400 2420 2308 2317 2326 2335 2344 2364 2373 2382 2391 83215
2621 2630 2650 2659 2547 2556 2565 2585 2594 2603 2612	12 2137 2146 2166 2175 2063 2072 2081 2101 2110 2119 2128 322	2 331 351 360 248 257 266 286 295 304 313	201 210 230 239 127 136 145 165 174 183 192	2379 2388 2408 2417 2305 2314 2323 2343 2352 2361 2370 83215
2600 2609 2629 2638 2647 2656 2544 2553 2573 2582 259	91 2116 2125 2145 2154 2163 2172 2060 2069 2089 2098 2107 301	1 310 330 339 348 357 245 254 274 283 292	180 189 209 218 227 236 124 133 153 162 171	2358 2367 2387 2396 2405 2414 2302 2311 2331 2340 2349 <mark>83215</mark>
2579 2588 2597 2617 2626 2635 2644 2653 2552 2561 2570	70 2095 2104 2113 2133 2142 2151 2160 2169 2068 2077 2086 280	0 289 298 318 327 336 345 354 253 262 271	159 168 177 197 206 215 224 233 132 141 150	2337 2346 2355 2375 2384 2393 2402 2411 2310 2319 2328 83215
2558 2567 2576 2596 2605 2614 2623 2632 2641 2661 2549	49 2074 2083 2092 2112 2121 2130 2139 2148 2157 2177 2065 259	9 268 277 297 306 315 324 333 342 362 250	138 147 156 176 185 194 203 212 221 241 129	2316 2325 2334 2354 2363 2372 2381 2390 2399 2419 2307 83215
2658 2546 2555 2564 2584 2593 2602 2611 2620 2640 2649	49 2174 2062 2071 2080 2100 2109 2118 2127 2136 2156 2165 359	9 247 256 265 285 294 303 312 321 341 350	238 126 135 144 164 173 182 191 200 220 229	2416 2304 2313 2322 2342 2351 2360 2369 2378 2398 2407 83215
2637 2646 2655 2543 2563 2572 2581 2590 2599 2608 2628	28 2153 2162 2171 2059 2079 2088 2097 2106 2115 2124 2144 338	8 347 356 244 264 273 282 291 300 309 329		2395 2404 2413 2301 2321 2330 2339 2348 2357 2366 2386 83215
	07 2132 2141 2150 2159 2168 2067 2076 2085 2094 2103 2123 317			2374 2383 2392 2401 2410 2309 2318 2327 2336 2345 2365 83215
	75 2111 2120 2129 2138 2147 2167 2176 2064 2073 2082 2091 296			2353 2362 2371 2380 2389 2409 2418 2306 2315 2324 2333 83215
	54 2090 2099 2108 2117 2126 2135 2155 2164 2173 2061 2070 275			
	9 1816 1836 1845 1854 1863 1872 1892 1901 1910 1919 1928 969			
	8 1916 1936 1824 1833 1842 1851 1860 1880 1889 1898 1907 1069 7 1895 1904 1924 1933 1821 1830 1839 1859 1868 1877 1886 1048			
	6 1874 1883 1903 1912 1921 1930 1818 1827 1847 1856 1865 1027			
	5 1853 1862 1871 1891 1900 1909 1918 1927 1826 1835 1844 1006			
	4 1832 1841 1850 1870 1879 1888 1897 1906 1915 1935 1823 985			
	4 1932 1820 1829 1838 1858 1867 1876 1885 1894 1914 1923 1085			
	3 1911 1920 1929 1817 1837 1846 1855 1864 1873 1882 1902 1064			
801 810 819 828 837 736 745 754 763 772 792	2 1890 1899 1908 1917 1926 1825 1834 1843 1852 1861 1881 1043	3 1052 1061 1070 1079 978 987 996 1005 1014 1034	648 1657 1666 1675 1684 1583 1592 1601 1610 1619 1639	2253 2262 2271 2280 2289 2188 2197 2206 2215 2224 2244 83215
780 789 798 807 816 836 845 733 742 751 760	0 1869 1878 1887 1896 1905 1925 1934 1822 1831 1840 1849 1022	2 1031 1040 1049 1058 1078 1087 975 984 993 1002	627 1636 1645 1654 1663 1683 1692 1580 1589 1598 1607	2232 2241 2250 2259 2268 2288 2297 2185 2194 2203 2212 83215
759 768 777 786 795 804 824 833 842 730 739	9 1848 1857 1866 1875 1884 1893 1913 1922 1931 1819 1828 1001	01 1010 1019 1028 1037 1046 1066 1075 1084 972 981	606 1615 1624 1633 1642 1651 1671 1680 1689 1577 1586	2211 2220 2229 2238 2247 2256 2276 2285 2294 2182 2191 83215
485 505 514 523 532 541 561 570 579 588 597	7 1211 1231 1240 1249 1258 1267 1287 1296 1305 1314 1323 1453	3 1473 1482 1491 1500 1509 1529 1538 1547 1556 1565	695 1715 1724 1733 1742 1751 1771 1780 1789 1798 1807	2421 2441 2450 2459 2468 2477 2497 2506 2515 2524 2533 83215
585 605 493 502 511 520 529 549 558 567 576	<mark>6</mark> 1311 1331 1219 1228 1237 1246 1255 1275 1284 1293 1302 1553	3 1573 1461 1470 1479 1488 1497 1517 1526 1535 1544	795 1815 1703 1712 1721 1730 1739 1759 1768 1777 1786	2521 2541 2429 2438 2447 2456 2465 2485 2494 2503 2512 <mark>83215</mark>
564 573 593 602 490 499 508 528 537 546 555	<mark>5</mark> 1290 1299 1319 1328 1216 1225 1234 1254 1263 1272 1281 1532	2 1541 1561 1570 1458 1467 1476 1496 1505 1514 1523	1774 1783 1803 1812 1700 1709 1718 1738 1747 1756 1765	2500 2509 2529 2538 2426 2435 2444 2464 2473 2482 2491 <mark>83215</mark>
543 552 572 581 590 599 487 496 516 525 534	<mark>4</mark> 1269 1278 1298 1307 1316 1325 1213 1222 1242 1251 1260 1511	1 1520 1540 1549 1558 1567 1455 1464 1484 1493 1502	753 1762 1782 1791 1800 1809 1697 1706 1726 1735 1744	2479 2488 2508 2517 2526 2535 2423 2432 2452 2461 2470 83215
522 531 540 560 569 578 587 596 495 504 513	<mark>3</mark> 1248 1257 1266 1286 1295 1304 1313 1322 1221 1230 1239 1490	0 1499 1508 1528 1537 1546 1555 1564 1463 1472 1481	732 1741 1750 1770 1779 1788 1797 1806 1705 1714 1723	2458 2467 2476 2496 2505 2514 2523 2532 2431 2440 2449 83215
501 510 519 539 548 557 566 575 584 604 492	<mark>2</mark> 1227 1236 1245 1265 1274 1283 1292 1301 1310 1330 1218 1469	9 1478 1487 1507 1516 1525 1534 1543 1552 1572 1460	1711 1720 1729 1749 1758 1767 1776 1785 1794 1814 1702	2437 2446 2455 2475 2484 2493 2502 2511 2520 2540 2428 83215
601 489 498 507 527 536 545 554 563 583 592	<mark>2</mark> 1327 1215 1224 1233 1253 1262 1271 1280 1289 1309 1318 1569	9 1457 1466 1475 1495 1504 1513 1522 1531 1551 1560	1811 1699 1708 1717 1737 1746 1755 1764 1773 1793 1802	2537 2425 2434 2443 2463 2472 2481 2490 2499 2519 2528 83215
	<mark>1 1306 1315 1324 1212 1232 1241 1250 1259 1268 1277 1297</mark> 1548			
	0 1285 1294 1303 1312 1321 1220 1229 1238 1247 1256 1276 1527			
	8 1264 1273 1282 1291 1300 1320 1329 1217 1226 1235 1244 1506			
	7 1243 1252 1261 1270 1279 1288 1308 1317 1326 1214 1223 1485			
	17 1332 1352 1361 1370 1379 1388 1408 1417 1426 1435 1444 1937 16 1432 1452 1340 1349 1358 1367 1376 1396 1405 1414 1423 2037			1 21 30 39 48 57 77 86 95 104 113 83215 101 121 9 18 27 36 45 65 74 83 92 83215
	75 1411 1420 1440 1449 1337 1346 1355 1375 1384 1393 1402 2016			
	4 1390 1399 1419 1428 1437 1446 1334 1334 1343 1363 1372 1381 1995			
	3 1369 1378 1387 1407 1416 1425 1434 1443 1342 1351 1360 1974			
	12 1348 1357 1366 1386 1395 1404 1413 1422 1431 1451 1339 1953			
3021 2909 2918 2927 2947 2956 2965 2974 2983 3003 3012	12 1448 1336 1345 1354 1374 1383 1392 1401 1410 1430 1439 2053	3 1941 1950 1959 1979 1988 1997 2006 2015 2035 2044	206 1094 1103 1112 1132 1141 1150 1159 1168 1188 1197	117 5 14 23 43 52 61 70 79 99 108 83215
3000 3009 3018 2906 2926 2935 2944 2953 2962 2971 299	91 1427 1436 1445 1333 1353 1362 1371 1380 1389 1398 1418 2032	2 2041 2050 1938 1958 1967 1976 1985 1994 2003 2023	185 1194 1203 1091 1111 1120 1129 1138 1147 1156 1176	96 105 114 2 22 31 40 49 58 67 87 83215
2979 2988 2997 3006 3015 2914 2923 2932 2941 2950 2970	70 1406 1415 1424 1433 1442 1341 1350 1359 1368 1377 1397 2011	11 2020 2029 2038 2047 1946 1955 1964 1973 1982 2002	164 1173 1182 1191 1200 1099 1108 1117 1126 1135 1155	75 84 93 102 111 10 19 28 37 46 66 83215
2958 2967 2976 2985 2994 3014 3023 2911 2920 2929 2938	<mark>38</mark> 1385 1394 1403 1412 1421 1441 1450 1338 1347 1356 1365 1990	0 1999 2008 2017 2026 2046 2055 1943 1952 1961 1970	143 1152 1161 1170 1179 1199 1208 1096 1105 1114 1123	54 63 72 81 90 110 119 7 16 25 34 83215
2937 2946 2955 2964 2973 2982 3002 3011 3020 2908 2917	17 1364 1373 1382 1391 1400 1409 1429 1438 1447 1335 1344 1969	9 1978 1987 1996 2005 2014 2034 2043 2052 1940 1949	122 1131 1140 1149 1158 1167 1187 1196 1205 1093 1102	33 42 51 60 69 78 98 107 116 4 13 83215
606 626 635 644 653 662 682 691 700 709 718	8 848 868 877 886 895 904 924 933 942 951 960 2663	3 2683 2692 2701 2710 2719 2739 2748 2757 2766 2775 2	2784 2804 2813 2822 2831 2840 2860 2869 2878 2887 2896	364 384 393 402 411 420 440 449 458 467 476 <mark>83215</mark>
706 726 614 623 632 641 650 670 679 688 697	7 948 968 856 865 874 883 892 912 921 930 939 2763	63 2783 2671 2680 2689 2698 2707 2727 2736 2745 2754 <mark>2</mark>	884 2904 2792 2801 2810 2819 2828 2848 2857 2866 2875	464 484 372 381 390 399 408 428 437 446 455 83215
685 694 714 723 611 620 629 649 658 667 676	6 927 936 956 965 853 862 871 891 900 909 918 2742	¹ 2 2751 2771 2780 2668 2677 2686 2706 2715 2724 2733 2	863 2872 2892 2901 2789 2798 2807 2827 2836 2845 2854	443 452 472 481 369 378 387 407 416 425 434 83215
	5 906 915 935 944 953 962 850 859 879 888 897 2721			
	4 885 894 903 923 932 941 950 959 858 867 876 2700			
	3 864 873 882 902 911 920 929 938 947 967 855 2679			
	3 964 852 861 870 890 899 908 917 926 946 955 2779			
	2 943 952 961 849 869 878 887 896 905 914 934 2758			
	1 922 931 940 949 958 857 866 875 884 893 913 2737 9 901 910 919 928 937 957 966 854 863 872 881 2716			
	9 901 910 919 928 937 957 966 854 863 872 881 2716 8 880 889 898 907 916 925 945 954 963 851 860 2695			
	15 832			
0719 0719 0719 03219 03219 03219 03219 03219 03219 03213 03213 03213	2 02712 02712 02712 02712 02712 02712 02712 02712 02712 02712 02712 02712	22 02 13 03 13 03 13 03 13 03 13 03 13 03 13 03 13 03 13 03 13 03 13	STID OFTO OFTO OFTO OFTO OFTO OFTO OFTO OFT	STEP STEP STEP STEP STEP STEP STEP STEP

83215
2553 2561 2559 2557 2555 2654 2655 2657 2659 2661 2551 2069 2077 2075 2073 2071 2170 2171 2173 2175 2177 2067 254 262 260 258 256 355 356 358 360 362 252 133 141 139 137 135 234 235 237 239 241 131 2311 2319 2317 2315 2313 2412 2413 2415 2417 2419 2309 83215
2662 2569 2641 2639 2637 2636 2573 2575 2577 2571 2542 2178 2085 2157 2155 2153 2152 2089 2091 2093 2087 2058 363 270 342 340 338 337 274 276 278 272 243 242 149 221 219 217 216 153 155 157 151 122 2420 2327 2399 2397 2395 2394 2331 2333 2335 2329 2300 83215
2660 2562 2619 2615 2617 2582 2581 2579 2621 2642 2544 2176 2078 2135 2131 2133 2098 2097 2095 2137 2158 2060 361 263 320 316 318 283 282 280 322 343 245 240 142 199 195 197 162 161 159 201 222 124 2418 2320 2377 2373 2375 2340 2339 2337 2379 2400 2302 83215
2658 2564 2578 2611 2614 2594 2596 2595 2626 2640 2546 2174 2080 2094 2127 2130 2110 2112 2111 2142 2156 2062 359 265 279 312 315 295 297 296 327 341 247 238 144 158 191 194 174 176 175 206 220 126 2416 2322 2336 2369 2372 2352 2354 2353 2384 2398 2304 83215
2656 2566 2580 2591 2601 2606 2599 2613 2624 2638 2548 2172 2082 2096 2107 2117 2122 2115 2129 2140 2154 2064 357 267 281 292 302 307 300 314 325 339 249 236 146 160 171 181 186 179 193 204 218 128 2414 2324 2338 2349 2359 2364 2357 2371 2382 2396 2306 83215 2396 2306 83215 2396 2396 2396 2396 2396 2396 2396 2396
255 263 260 260 260 260 260 260 260 260 260 260
2556 2630 2616 2609 2590 2610 2608 2593 2586 2572 2660 270 2146 2132 2125 2106 2136 2357 2366 23
2558 2628 2583 2589 2587 2622 2623 2625 2585 2576 2646 2074 2144 2099 2105 2103 2138 2139 2141 2101 2092 2162 259 329 284 290 288 323 324 326 286 277 347 138 208 163 169 167 202 203 205 165 156 226 2316 2380 2381 2383 2383 2384 2394 83215
2560 2633 2563 2565 2567 2568 2631 2629 2627 2635 2644 2076 2149 2079 2081 2083 2084 2147 2145 2143 2151 2160 261 334 264 266 268 269 332 330 328 336 345 140 213 143 145 147 148 211 209 207 215 224 2318 2391 2321 2323 2325 2326 2389 2387 2385 2393 2402 83215
2653 2643 2645 2647 2649 2550 2549 2547 2545 2543 2651 2169 2159 2161 2163 2165 2066 2065 2063 2061 2059 2167 354 344 346 348 350 251 250 248 246 244 352 233 223 225 227 229 130 129 127 125 123 231 2411 2401 2403 2405 2407 2308 2307 2305 2303 2301 2409 83215
738 746 744 742 740 839 840 842 844 846 736 1827 1835 1833 1831 1829 1928 1929 1931 1933 1935 1825 980 988 986 984 982 1081 1082 1084 1086 1088 978 1585 1593 1591 1589 1587 1686 1687 1689 1691 1693 1583 2196 2198 2196 2194 2192 2291 2292 2294 2296 2298 2188 83215
847 754 826 824 822 821 758 760 762 756 727 1936 1843 1915 1913 1911 1910 1847 1849 1851 1845 1816 1089 996 1068 1066 1064 1063 1000 1002 1004 998 969 1694 1601 1673 1671 1669 1668 1605 1607 1609 1603 1574 2299 2206 2278 2276 2274 2273 2210 2212 2214 2208 2179 83215
845 747 804 800 802 767 766 764 806 827 729 1934 1836 1893 1889 1891 1856 1855 1853 1895 1916 1818 1087 989 1046 1042 1044 1009 1008 1006 1048 1069 971 1692 1594 1651 1647 1649 1614 1613 1611 1653 1674 1576 2297 2199 2256 2252 2254 2219 2218 2216 2258 2279 2181 83215
843 749 763 796 799 779 781 780 811 825 731 1932 1838 1852 1885 1888 1868 1870 1869 1900 1914 1820 1085 991 1005 1038 1041 1021 1023 1022 1053 1067 973 1690 1596 1610 1643 1646 1626 1628 1627 1658 1672 1578 2295 2201 215 2248 2251 2231 2233 2232 2263 2277 2183 8 3215
841 751 765 776 786 791 784 798 809 823 733 1930 1840 1854 1865 1875 1880 1873 1887 1898 1912 1822 1083 993 1007 1018 1028 1033 1026 1040 1051 1065 975 1688 1598 1612 1623 1633 1638 1631 1645 1656 1670 1580 2293 2203 2217 2228 2238 2243 2236 2250 2261 2275 2185 83215
737 819 805 777 785 787 789 797 769 755 837 1826 1908 1894 1866 1874 1876 1878 1886 1858 1844 1926 979 1061 1047 1019 1027 1029 1031 1039 1011 997 1079 1584 1666 1652 1624 1632 1634 1636 1644 1616 1602 1684 2189 2271 2257 2229 2237 2239 2241 2249 2221 2207 2289 83215 2249 2237 2239 2241 2249 2221 2207 2289 83215 2249 2237 2239 2241 2249 2221 2207 2289 83215 2249 2237 2239 2241 2249 2221 2207 2289 83215 2249 2237 2239 2241 2249 2237 2239 2237 2239 2241 2249 2237 2349 2349 2349 2349 2349 2349 2349 2349
739 817 803 792 790 783 788 782 771 757 835 1828 1906 1879 1871 1871 1870 1871 </td
741 813 801 134 173 733 733 778 773 739 833 1830 1904 1890 1863 1864 1862 1867 1867 1867 1867 1867 1867 1867 1867
745 818 748 750 752 753 816 814 812 820 829 1834 1907 1837 1839 1841 1842 1905 1903 1901 1909 1918 987 1060 990 992 994 995 1058 1056 1054 1052 1054 1055 1657 1619 1663 1661 1659 1667 1676 2197 2270 2200 2202 2204 2205 2268 2266 2264 2272 2281 83215
838 828 830 832 834 735 734 732 730 728 836 1927 1917 1919 1921 1923 1824 1823 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2282 2284 2286 2187 2186 2184 2182 2180 2288 83215
496 504 502 500 498 597 598 600 602 604 494 1222 1230 1228 1226 1224 1323 1324 1326 1328 1330 1220 1464 1472 1470 1468 1466 1565 1566 1568 1570 1572 1462 1706 1714 1712 1710 1708 1807 1808 1810 1812 1814 1704 2432 2440 2438 2436 2434 2533 2534 2536 2538 2540 2430
605 512 584 582 580 579 516 518 520 514 485 1331 1238 1310 1308 1306 1305 1242 1244 1246 1240 1211 1573 1480 1552 1550 1548 1547 1484 1486 1488 1482 1453 1815 1722 1794 1792 1790 1789 1726 1728 1730 1724 1695 2541 2448 2520 2518 2516 2515 2452 2454 2456 2450 2421 83215
603 505 562 558 560 525 524 522 564 585 487 1329 1231 1288 1284 1286 1251 1250 1248 1290 1311 1213 1571 1473 1530 1526 1528 1493 1492 1490 1532 1553 1455 1813 1715 1772 1768 1770 1735 1734 1732 1774 1795 1697 2539 2441 2498 2494 2496 2461 2460 2458 2500 2521 2423 83215
601 507 521 554 557 537 539 538 569 583 489 1327 1233 1247 1280 1283 1263 1263 1265 1264 1295 1309 1215 1569 1475 1489 1522 1525 1505 1507 1506 1537 151 1457 1811 1717 1731 1764 1767 1747 1749 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1748 1779 1749 1748 1749 1749 1748 1749 1749 1748 1749 1749 1748 1749 1749 1748 1749 1748 174
599 509 523 534 544 549 542 556 567 581 491 1325 1235 1249 1260 1270 1275 1268 1282 1293 1307 1217 150 1477 1491 1502 1512 1517 1510 1524 1535 1549 1459 1809 1719 1733 1744 1754 1759 1752 1766 1777 1791 1701 2535 2445 2459 2470 2480 2485 2478 2492 2503 2517 2427 83215
495 577 563 535 543 545 547 55 527 513 595 1221 1303 1289 1261 1269 1271 1273 1281 1253 1249 1261 1269 1271 1273 1281 1253 1249 1261 1269 1271 1273 1281 1253 1249 1241 1253 1249 1241 1253 1249 1241 1253 1249 1241 1243 1244 1243 1244 1243 1244 1244
497 575 561 550 548 541 546 540 529 515 593 1223 1301 1287 1276 1274 1267 1272 1266 1255 1241 1319 1465 1543 1529 1518 1516 1509 1514 1508 1497 1483 1561 1707 1785 1771 1760 1758 1751 1756 1750 1739 1725 1803 2433 2511 2497 2486 2484 2477 2482 2476 2465 2451 2529 83215
499 573 559 552 533 553 551 536 531 517 591 1225 1299 1285 1278 1259 1277 1262 1257 1243 1317 1467 1541 1527 1520 1501 1521 1519 1504 1499 1485 1559 1709 1783 1769 1762 1743 1763 1761 1746 1741 1727 1801 2435 2509 2495 2488 2469 2489 2487 2472 2467 2453 2527 83215
501 571 526 532 530 565 566 568 528 519 589 1227 1297 1252 1258 1256 1291 1292 1294 1254 1245 1315 1469 1539 1494 1500 1498 1533 1534 1536 1496 1487 1557 1711 1781 1786 1742 1740 1775 1776 1778 1738 1729 179 2437 2507 2462 2468 2466 2501 2502 2504 2464 2456 2457 2502 83215 503 576 506 508 510 511 574 572 570 578 587 1229 1302 1232 1234 1236 1237 1300 1298 1296 1304 1313 1471 1544 1476 1478 1479 1542 1540 1538 1546 1555 1713 1786 1716 1718 1720 1721 1784 1782 1780 1788 1797 2439 2512 2442 2444 2446 2447 2510 2508 2506 2514 2523 83215
596 586 588 590 592 493 492 490 488 486 594 1322 1312 1314 1316 1318 1219 1218 1216 1214 1212 1320 1564 1554 1556 1558 1560 1461 1460 1458 1456 1454 1562 1806 1796 1798 1800 1802 1703 1702 1700 1698 1696 1804 2532 2522 2524 2526 2528 2429 2428 2426 2424 2422 2530 83215
2916 2924 2922 2920 2918 3017 3018 3020 3022 3024 2914 1343 1351 1349 1347 1345 1444 1445 1447 1449 1451 1341 1948 1956 1954 1952 1950 2049 2050 2052 2054 2056 1946 1101 1109 1107 1105 1103 1202 1203 1205 1207 1209 1099 12 20 18 16 14 113 114 116 118 120 10
3025 2932 3004 3002 3000 2999 2936 2938 2940 2934 2905 1452 1359 1431 1429 1427 1426 1363 1365 1367 1361 1332 2057 1964 2036 2034 2032 2031 1968 1970 1972 1966 1937 1210 1117 1189 1187 1185 1184 1121 1123 1125 1119 1090 121 28 100 98 96 95 32 34 36 30 1 83215
3023 2925 2982 2978 2980 2945 2944 2942 2984 3005 2907 1450 1352 1409 1405 1407 1372 1371 1369 1411 1432 1334 2055 1957 2014 2010 2012 1977 1976 1974 2016 2037 1939 1208 1110 1167 1163 1165 1130 1129 1127 1169 1190 1092 119 21 78 74 76 41 40 38 80 101 3 83215
3021 2927 2941 2974 2977 2957 2959 2958 2989 3003 2909 1448 1354 1368 1401 1404 1384 1386 1385 1416 1430 1336 2053 1959 1973 2006 2009 1989 1991 1990 2021 2035 1941 120 1126 1159 1162 1142 1144 1143 1174 1188 1094 117 23 37 70 73 53 55 54 85 99 5 83215
301 291 144 135 139 149 139 294 295 295 295 295 295 295 295 295 295 295
2915 2997 2983 2955 2963 2965 2967 2975 2963 2965 2967 2975 2947 2933 3015 1342 1424 1410 1382 1390 1392 1394 1402 1374 1360 1442 1947 2029 2015 1987 1995 1997 1999 2007 1979 1965 2047 1100 1182 1168 1140 1148 1150 1152 1160 1132 1118 1200 11 93 79 51 59 61 63 71 43 29 111 83215
2917 2995 2981 2970 2968 2961 2960 2949 2935 3013 1344 1422 1408 1397 1395 1388 1393 1387 1376 1362 1440 1949 2027 2013 2002 2000 1993 1998 1992 1981 1967 2045 1102 1180 116 1155 1153 1146 1151 1145 1134 1120 1198 13 91 77 66 64 57 62 56 45 31 109 8 3215
2919 2993 2979 2972 2953 2973 2971 2956 2951 2937 3011 1346 1420 1406 1399 1380 1400 1398 1383 1378 1364 1438 1951 2025 2011 2004 1985 2005 2003 1988 1983 1969 2043 1104 1178 1164 1157 1138 1156 1141 1136 1122 1196 15 89 75 68 49 69 67 52 47 33 107 83215
2921 2991 2946 2952 2950 2985 2986 2988 2948 2939 3009 1348 1418 1373 1379 1377 1412 1413 1415 1375 1366 1436 1953 2023 1978 1984 1982 2017 2018 2020 1980 1971 2041 1106 1176 1131 1137 1135 1170 1171 1173 1133 1124 1194 17 87 42 48 46 81 82 84 44 35 105 83215
2923 2996 2926 2928 2930 2931 2994 2992 2990 2998 3007 1350 1423 1353 1355 1357 1358 1421 1419 1417 1425 1434 1955 2028 1958 1960 1962 1963 2026 2024 2022 2030 2039 1108 1181 1111 1113 1115 1116 1179 1177 1175 1183 1192 19 92 22 24 26 27 90 88 86 94 103 83215 3016 3006 3008 3010 3012 2913 2912 2910 2908 2906 3014 1443 1433 1435 1437 1439 1340 1339 1337 1335 1333 1441 2048 2038 2040 2042 2044 1945 1944 1945 1944 1945 1944 1945 1940 1938 2046 1201 1191 1193 1195 1197 1098 1097 1095 1093 1091 1199 112 102 104 106 108 9 8 6 4 2 110 83215
617 625 623 621 619 718 719 721 723 725 615 859 867 865 863 861 960 961 963 965 967 857 1267 42682 2680 2678 2676 2775 2776 2778 2780 2782 2672 1795 2803 2801 2799 2797 2896 2897 2899 2901 2903 2793 375 383 381 379 377 476 477 479 481 483 373 83215
726 633 705 703 701 700 637 639 641 635 606 968 875 947 945 943 942 879 881 883 877 848 12783 2690 2752 2760 2758 2757 2694 2692 2663 2904 2811 2883 2881 2879 2878 2815 2817 2819 2813 2784 484 391 463 461 459 458 395 397 399 393 364 83215
724 626 683 679 681 646 645 643 685 706 608 966 868 925 921 923 888 887 885 927 948 850 2781 2683 2740 2736 2738 2703 2702 2700 2742 2763 2665 2902 2804 2861 2857 2859 2824 2823 2821 2863 2884 2786 482 384 441 437 439 404 403 401 443 464 366 83215
722 628 642 675 678 658 660 659 690 704 610 964 870 884 917 920 900 902 901 932 946 852 2779 2685 2699 2732 2735 2715 2717 2716 2747 2761 2667 2900 2806 2820 2853 2856 2836 2838 2837 2868 2882 2788 480 386 400 433 436 416 418 417 448 462 368 83215
720 630 644 655 665 670 663 677 688 702 612 962 872 886 897 907 912 905 919 930 944 854 277 2687 270 273 2727 2720 2734 2745 2759 2669 2898 2803 2843 2843 2843 2843 2843 2843 2855 2866 2880 2790 478 388 402 413 423 428 421 435 446 460 370 83215
6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
6 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
620 694 680 673 654 674 672 657 652 638 712 862 936 922 915 896 916 914 899 894 880 954 2677 2751 2737 2730 2711 2731 2729 2714 2709 2695 2769 279 2858 2851 2832 2852 2850 2835 2830 2816 2890 378 452 438 431 412 432 430 415 410 396 470 83215
622 692 647 653 651 686 687 689 649 640 710 864 934 889 895 893 928 929 931 891 882 952 2679 2749 2704 2710 2708 2743 2744 2746 2706 2697 2767 2800 2870 2825 2831 2829 2864 2865 2867 2827 2818 288 380 450 405 411 409 444 445 447 407 398 468 83215
624 697 627 629 631 632 695 693 691 699 708 866 939 869 871 873 874 937 935 933 941 950 2681 2754 2684 2686 2688 2689 2752 2750 2748 2756 2802 2875 2809 2810 2873 2871 2869 2877 2886 382 455 385 387 389 390 453 451 449 457 466 83215
83215 83215

8321
2553 2561 2559 2557 2555 2654 2655 2657 2659 2661 2551 2069 2077 2075 2073 2071 2170 2171 2173 2175 2177 2067 254 262 260 258 256 355 356 358 360 362 252 133 141 139 137 135 234 235 237 239 241 131 2311 2319 2317 2315 2313 2412 2413 2415 2417 2419 2309 8321
2662 2583 2632 2591 2588 2625 2593 2581 2630 2595 2542 2178 2099 2148 2107 2104 2141 2109 2097 2146 2111 2058 363 284 333 292 289 326 294 282 331 296 243 242 163 212 171 168 205 173 161 210 175 122 2420 2341 2390 2349 2346 2383 2351 2339 2388 2353 2300 8321
2660 2596 2582 2628 2589 2584 2633 2594 2586 2626 2544 2176 2112 2098 2144 2105 2100 2149 2110 2102 2142 2060 361 297 283 329 290 285 334 295 287 327 245 240 176 162 208 169 164 213 174 166 206 124 2418 2354 2340 2386 2347 2342 2391 2352 2344 2384 2302 8321
2658 267 2592 2587 2629 2597 2580 2631 2590 2585 2546 2174 2143 2108 2103 2145 2113 2096 2147 2106 2101 2062 359 328 293 288 330 298 281 332 291 286 247 238 207 172 167 209 177 160 211 170 165 126 2416 2385 2350 2345 2387 2355 2338 2389 2348 2343 2304 8321
2656 2601 2569 2636 2606 2562 2638 2599 2567 2640 2548 2172 2117 2085 2152 2122 2078 2154 2115 2083 2156 2064 357 302 270 337 307 263 339 300 268 341 249 236 181 149 216 186 142 218 179 147 220 128 2414 2359 2327 2394 2364 2320 2396 2357 2325 2398 2306 8321 249 236 181 149 216 186 142 218 179 147 220 128 2414 2359 2327 2394 2364 2320 2396 2357 2325 2398 2306 2357 2325 2398 2306 8321 249 236 181 149 216 186 142 218 179 147 220 128 2414 2359 2327 2394 2364 2320 2396 2357 2325 2398 2306 2357 2325 2398 2306 8321 249 236 181 149 216 186 142 218 179 147 220 128 2414 2359 2327 2394 2364 2320 2396 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2306 2357 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2307 2325 2325 2398 2327 2325 2325 2398 2327 2325 2325 2398 2325 2325 2325 2398 2325 2325 2325 2325 2325 2325 2325 232
2552 2641 2600 2555 2634 2602 2570 2639 2604 2563 2652 2068 2157 2116 2081 2150 2118 2086 2155 2120 2079 2168 253 342 301 266 335 303 271 340 305 264 353 132 221 180 145 214 182 150 219 184 143 232 2310 2399 2358 2323 2392 2360 2328 2397 2362 2321 2410 8321 254 254 254 254 254 2637 2605 2566 2642 2598 2568 2635 2603 2650 2070 2080 2153 2121 2082 2158 2114 2084 2151 2119 2166 255 265 338 306 267 343 299 269 336 304 351 134 144 217 185 146 222 178 148 215 183 230 2312 2322 2395 2363 2324 2400 2356 2326 2393 2361 2408 8321
2554 2557 2562 2642 2557 2662 2642 2556 2642 2556 2655 2603 2650 2055 212 2062 2155 2120 2060 2155 2
2558 2578 2618 2610 2571 2620 2615 2576 2622 2608 2646 2074 2094 2134 2126 2087 2136 2131 2092 2138 2124 2162 259 279 319 311 272 321 316 277 323 309 347 138 158 198 190 151 200 195 156 202 188 226 2316 2336 2376 2368 2329 2378 2373 2334 2380 2366 2404 8321
2560 2609 2574 2623 2611 2579 2616 2613 2572 2621 2644 2076 2125 2090 2139 2127 2095 2132 2129 2088 2137 2160 261 310 275 324 312 280 317 314 273 322 345 140 189 154 203 191 159 196 193 152 201 224 2318 2367 2332 2381 2369 2337 2374 2371 2330 2379 2402 8321
738 746 744 742 740 839 840 842 844 846 736 1827 1835 1833 1831 1829 1928 1929 1931 1933 1935 1825 980 988 986 984 982 1081 1082 1084 1086 1088 978 1585 1593 1591 1589 1587 1686 1687 1689 1691 1693 1583 2190 2198 2196 2194 2192 2291 2292 2294 2296 2298 2188 8321
847 768 817 776 773 810 778 766 815 780 727 1936 1857 1906 1865 1862 1899 1867 1855 1904 1869 1816 1089 1010 1059 1018 1015 1052 1020 1008 1057 1022 969 1694 1615 1664 1623 1620 1657 1625 1613 1662 1627 1574 2299 2220 2269 2228 2225 2262 2230 2218 2267 2232 2179 8321
845 781 767 813 774 769 818 779 771 811 729 1934 1870 1856 1902 1863 1858 1907 1868 1860 1900 1818 1087 1023 1009 1055 1016 1011 1060 1021 1013 1053 971 1692 1628 1614 1660 1621 1616 1655 1626 1618 1658 1576 2297 2233 2219 2265 2226 2221 2270 2231 2223 2263 2181 8321
843 812 777 772 814 782 765 816 775 770 731 1932 1901 1866 1861 1903 1871 1854 1905 1864 1859 1820 1085 1054 1019 1014 1056 1024 1007 1058 1017 1012 973 1690 1659 1624 1619 1661 1629 1612 1663 1622 1617 1578 2295 2264 2229 2224 2266 2234 2217 2268 2227 2222 2183 8321
841 786 754 821 791 747 823 784 752 825 73 1930 1875 1843 1910 1880 1836 1912 1873 1841 1914 182 108 906 1063 1033 989 1065 1026 994 1067 975 1688 1633 1601 1668 1638 1594 1670 1631 1599 1672 1580 2293 2238 2206 2273 2243 2199 2275 2236 2204 2277 2185 8321
737 826 785 750 819 787 755 824 789 748 837 1826 1915 1874 1839 1908 1876 1844 1913 1878 1837 1926 979 1068 1027 992 1061 1029 997 1066 1031 990 1079 1584 1673 1632 1597 1666 1634 1602 1671 1636 1595 1684 2189 2278 2237 2202 2271 2239 2207 2276 2241 2200 2289 8321
739 749 822 790 751 827 783 753 820 788 1828 1838 1911 1879 1842 1909 1877 1924 981 991 1064 1032 993 1069 1025 995 1062 1030 1077 1586 1596 1669 1637 1580 1600 1667 1635 1682 2191 2201 2274 2242 2203 2279 2235 2205 2272 2240 2287 8321
741 804 799 758 809 792 760 802 797 762 833 1830 1893 1888 1847 1898 1881 1849 1891 1886 1851 1922 983 1046 1041 1000 1051 1034 1002 1044 1039 1004 1075 1588 1651 1646 1605 1656 1639 1607 1649 1644 1609 1680 2193 2256 2251 2210 2261 2244 2212 2254 2249 2214 2285 8321
743 763 803 795 856 800 761 807 793 831 1832 1852 1894 1894 1896<
745 794 759 808 796 764 801 798 757 806 829 1834 1883 1848 1897 1885 1853 1890 1887 1846 1895 1918 987 1036 1001 1050 1038 1006 1043 1040 999 1048 1071 1592 1641 1606 1655 1643 1611 1648 1645 1604 1653 1676 2197 2246 2211 2260 2248 2216 2253 2250 2209 2258 2281 8321
838 828 830 832 834 735 734 732 730 728 836 1927 1917 1919 1921 1923 1824 1823 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 1821 1819 1817 1925 1080 1070 1072 1074 1076 977 976 974 972 970 1078 1685 1675 1677 1679 1681 1582 1581 1579 1577 1575 1683 2290 2280 2282 2284 2286 2187 2186 2184 2182 2180 2288 832 180 288 832 180 288 832 180 288 832 180 288 832 180 288 832 180 288 832 180 288 832 180 288 830 180 180 180 180 180 180 180 180 180 18
496 504 502 500 498 597 598 600 602 604 494 1222 1230 1228 1226 1224 1323 1324 1326 1328 1330 1220 1464 1472 1470 1468 1466 1565 1566 1568 1570 1572 1462 170 1708 1807 1808 1810 1812 1814 1704 2432 2440 2438 2436 2434 2533 2534 2536 2538 2540 2430 8321
605 526 575 534 531 568 536 524 573 538 485 1331 1252 1301 1260 1257 1294 1262 1250 1299 1264 1211 1573 1494 1543 1502 1499 1536 1504 1492 1541 1576 1734 1748 1746 1734 1783 1748 1695 2541 2462 2511 2470 2467 2504 2472 2460 2509 2474 2421 8321 1573 1494 1543 1502 1499 1536 1504 1492 1541 1576 1734 1748 1746 1734 1783 1748 1695 2541 2462 2511 2470 2467 2504 2472 2460 2509 2474 2421 8321 1573 1494 1543 1502 1499 1536 1504 1492 1541 1576 1734 1748 1746 1734 1783 1748 1695 2541 2462 2511 2470 2467 2504 2472 2460 2509 2474 2421 8321 1573 1494 1543 1502 1499 1536 1504 1492 1541 1576 1734 1748 1746 1734 1783 1748 1695 2541 2462 2511 2470 2467 2504 2472 2460 2509 2474 2421 8321 1575 1495 1495 1495 1495 1495 1495 1495 149
603 539 525 571 532 527 576 537 529 569 487 1329 1265 1251 1297 1258 1253 1302 1263 1255 1295 1213 1571 1507 1493 1539 1500 1495 1544 1505 1497 1537 1455 1813 1749 1735 1781 1742 1737 1786 1747 1739 1779 1697 2539 2475 2461 2507 2468 2463 2512 2473 2465 2505 2423 8321 1297 1258 1253 1302 1263 1255 1295 1263 1295 1263 1255 1295 1263 1295 1295 1263 1295 1295 1263 1295 1295 1263 1295 1295 1295 1295 1295 1295 1295 1295
601 570 535 530 572 540 523 574 533 528 489 1327 1296 1261 1256 1298 1266 1249 1300 1259 1254 1215 1569 1538 1503 1498 1540 1508 1491 1542 1501 1496 1457 1811 1780 1745 1740 1782 1750 1733 1784 1743 1738 1699 2537 2506 2471 2466 2508 2476 2459 2510 2469 2464 2425 8321 1501 1496 1457 151 151 159 1510 1567 1512 1480 1547 1517 1473 1549 1510 1478 1551 1459 1809 1754 1722 1789 1759 1715 1791 1752 1720 1793 1701 2535 2480 2448 2515 2485 2441 2517 2478 2446 2519 2478 2478 2478 2478 2478 2478 2478 2478
495 584 543 508 577 545 513 582 547 506 595 1221 1310 1269 1234 1303 1271 1239 1308 1273 1231 1307 1312 1403 1552 1515 1474 1563 1705 1794 1755 1723 1792 1755 1723 1792 1757 1716 1805 2431 2520 2479 2444 2513 2481 249 2518 2483 2442 2513 2483 244
497 507 580 548 509 585 541 511 578 546 593 1223 1233 1306 1274 1235 1311 1267 1237 1304 1272 1319 1465 1475 1553 1509 1479 1546 1514 1561 1707 1717 1790 1758 1719 1795 1751 1721 1788 1756 1803 2433 2443 2516 2484 2445 2521 2477 2447 2514 2482 2529 8321
499 562 557 516 567 550 518 560 555 520 591 1225 1288 1283 1242 1293 1276 1244 1286 1281 1246 1317 1467 1530 1525 1484 1535 1518 1486 1528 1523 1488 1559 1709 1772 1767 1726 1777 1760 1728 1770 1765 1730 1801 2435 2498 2493 2452 2503 2486 2454 2496 2491 2456 2527 8321
501 521 561 553 514 563 558 519 565 551 589 1227 1247 1287 1279 1240 1289 1284 1245 1291 1277 1315 1469 1489 1529 1521 1482 1531 1526 1487 1533 1519 1557 1711 1731 1771 1763 1724 1773 1768 1729 1775 1761 1799 2437 2457 2497 2489 2450 2499 2494 2455 2501 2487 2558 2558 2568 2568 2568 2568 2568 2568
503 552 517 566 554 522 559 556 515 564 587 1229 1278 1243 1292 1280 1248 1285 1282 1241 1290 1313 1471 1520 1485 1534 1522 1490 1527 1524 1483 1532 155 1713 1762 1727 1776 1764 1732 1769 1766 1725 1774 1797 2439 2488 2453 2502 2490 2458 2495 2492 2451 2500 2523 8321
596 586 588 590 592 493 492 490 488 486 594 1322 1312 1314 1316 1318 1219 1218 1216 1214 1212 1320 1564 1556 1558 1560 1461 1460 1458 1456 1454 1562 1806 1796 1798 1800 1802 1703 1702 1700 1698 1696 1804 2532 2522 2524 2526 2528 2429 2428 2426 2424 2422 2530 8321
2916 2924 2922 2920 2918 3017 3018 3020 3022 3024 2914 1343 1351 1349 1347 1345 1444 1445 1447 1449 1451 1449 1451 1341 1948 1956 1954 1952 1950 2049 2050 2052 2054 2056 1946 1101 1109 1107 1105 1103 1202 1203 1205 1207 1209 1099 12 20 18 16 14 113 114 116 118 120 10
3025 2946 2995 2954 2951 2988 2956 2944 2993 2958 2956 2944 2993 2958 2905 1452 1373 1422 1381 1378 1415 1383 1371 1420 1385 1332 2057 1978 2027 1986 1983 2020 1988 1976 2025 1990 1937 1210 1131 1180 1139 1136 1173 1141 1129 1178 1143 1090 121 42 91 50 47 84 52 40 89 54 1 8321
3023 2959 2945 2991 2952 2947 2996 2957 2949 2989 2907 1450 1386 1372 1418 1379 1374 1423 1384 1376 1416 1334 2055 1991 1977 2023 1984 1979 2028 1989 1981 2021 1939 1208 1144 1130 1176 1137 1132 1181 1142 1134 1174 1092 119 55 41 87 48 43 92 53 45 85 3 45 85 3
3021 2990 2955 2950 2992 2960 2943 2994 2953 2948 2909 1448 1417 1382 1377 1419 1387 1370 1421 1380 1375 1336 2053 2022 1987 1982 2024 1992 1975 2026 1985 1980 1941 120 1175 1140 1135 1177 1145 1128 1179 1138 1133 1094 117 86 51 46 88 56 39 90 49 44 5 8321
3019 2964 2932 2999 2969 2925 3001 2962 2930 3003 2911 1446 1391 1359 1426 1396 1352 1428 1389 1357 1430 1338 2051 1996 1964 2031 2001 1957 2033 1994 1962 2035 1943 1204 1149 1117 1184 1154 1110 1186 1147 1115 1188 1096 115 60 28 95 65 21 97 58 26 99 7 8321
2915 3004 2963 2928 2997 2965 2933 3002 2967 2926 3015 1342 1431 1390 1355 1424 1392 1360 1429 1394 1353 1442 1947 2036 1995 1960 2029 1997 1965 2034 1999 1958 2047 1100 1189 1148 1113 1182 1150 1118 1187 1152 1111 1200 11 100 59 24 93 61 29 98 63 22 111 8321
2917 2927 3000 2968 2929 3005 2961 2931 2998 2966 3013 1344 1354 1427 1395 1356 1432 1388 1358 1425 1393 1440 1949 1959 2032 2000 1961 2037 1993 1963 2030 1998 2045 1102 1112 1185 1153 1114 1190 1146 1116 1183 1151 1198 13 23 96 64 25 101 57 27 94 62 109 8321
2919 2982 2977 2936 2987 2970 2938 2980 2975 2940 3011 1346 1409 1404 1363 1414 1397 1365 1407 1402 1367 1438 1951 2014 2009 1968 2019 2002 1970 2012 2007 1972 2043 1104 1167 1162 1121 1172 1155 1123 1165 1160 1125 1196 15 78 73 32 83 66 34 76 71 36 107 1402 1367 14
2921 2941 2961 2973 2963 2978 2939 2963 2971 3009 1348 1368 1408 1400 1361 1410 1409 1366 1412 1398 147 37 77 69 30 79 74 33 61 67 103 071 2923 2972 2937 2986 2974 2942 2979 2976 2935 2984 3007 1350 1399 1364 1413 1401 1369 1406 1403 1362 1411 1434 1955 2004 1969 2018 2006 1974 2011 2008 1967 2016 2039 1108 1157 1122 1171 1159 1127 1164 1161 1120 1169 1192 19 68 33 82 70 38 75 72 31 80 103 132
3016 3006 3018 3010 3012 2913 2912 2910 2908 2906 3014 1443 1433 1435 1437 1439 1340 1339 1337 1335 1333 1441 2048 2038 2040 2042 2044 1945 1944 1945 1946 104 105 1195 1197 1098 1097 1095 1093 1091 1199 112 102 104 106 108 9 8 6 4 2 110 832
617 625 623 621 619 718 719 721 723 725 615 859 867 865 863 861 960 961 963 965 967 857 2674 2682 2680 2678 2676 2775 2776 2778 2780 2782 2672 2795 2803 2801 2799 2797 2896 2897 2899 2901 2903 2793 375 383 381 379 377 476 477 479 481 483 373 8321
726 647 696 655 652 689 657 645 694 659 606 968 889 938 897 894 931 899 887 936 901 848 2783 2704 2753 2712 2709 2746 2714 2702 2751 2716 2663 2904 2825 2874 2833 2830 2867 2835 2823 2872 2837 2784 484 405 454 413 410 447 415 403 452 417 364 8321
724 660 646 692 653 648 697 658 650 690 608 966 902 888 934 895 890 939 900 892 932 850 2781 2717 2703 2749 2710 2705 2754 2715 2707 2747 2665 2902 2838 2824 2870 2831 2826 2875 2836 2828 2868 2786 482 418 404 450 411 406 455 416 408 448 366 8321
722 691 656 651 693 661 644 695 654 649 610 964 933 898 893 935 903 886 937 896 891 852 277 2748 2713 2708 2750 2718 2701 2752 2711 2706 2667 2900 2869 2834 2829 2873 2832 2827 2833 2822 2873 2832 2827 278 480 449 414 409 451 419 402 453 412 407 368 8321
720 665 633 700 670 626 702 663 631 704 61 962 907 875 942 912 868 944 905 873 946 854 277 272 2690 2757 272 2690 2757 272 2690 2757 272 2683 275 272 2690 2757 2690 2690 2690 2690 2690 2690 2690 2690
6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
618 628 701 669 630 706 662 632 699 667 71 860 870 943 911 872 948 904 874 941 909 95 67 2685 2758 272 2685 2758 272 2685 2758 272 2685 2758 272 2685 2758 272 2685 2758 272 2685 2758 272 2685 2758 272 271 279 2806 2879 2847 2808 2884 2840 2810 2877 2845 289 370 386 459 427 388 464 420 390 457 425 472 388 464 420 390 457 425 472 388 464 420 390 457 425 472 388 464 420 390 457 455 472 388 455 472 388 455 472 388 455 472 388 455 472 388 455 475 475
620 683 678 637 688 671 639 681 676 641 712 862 925 920 879 930 913 881 923 918 883 954 2677 2740 2735 2694 2745 2728 2696 2738 2733 2698 2769 2798 2861 2856 2819 2866 2849 2817 2859 2854 2819 2890 378 441 436 395 446 429 397 439 434 399 470 8321
622 642 682 674 635 684 679 640 686 672 710 864 884 924 916 877 926 921 882 928 914 952 2679 2699 2739 2731 2692 2741 2736 2697 2743 2729 2767 2800 2820 2860 2852 2813 2862 2857 2818 2864 2850 2888 380 400 440 432 393 442 437 398 444 430 468 8321 are already and already
624 673 638 687 675 643 680 677 636 685 708 866 915 880 929 917 885 922 919 878 927 950 2681 2730 2695 2744 2732 2700 2737 2734 2693 2742 2765 2802 2851 2816 2865 2853 2821 2858 2855 2814 2863 2886 382 431 396 445 433 401 438 435 394 443 466 8321
717 707 709 711 713 614 613 611 609 607 715 959 949 951 953 955 856 855 853 851 849 957 2774 2764 2766 2768 2770 2671 2670 2668 2666 2664 2772 2895 2885 2887 2889 2891 2792 2791 2785 2893 475 465 467 469 471 372 371 369 367 365 473 8321

2.3 Magic Squares of Order 44

Below are three magic squares of order 44 obtained from magic squares of order 154. It is obtained by the application of the formula ormula $\frac{a^2 - b^2}{2}$, a > b, i.e., subtract $\frac{154^2 - 44^2}{2} := 10890$ from each entry of magic square order 154, we get the following three magic squares of order 44:

				42614
<mark>1816 1836 1845 1854 1863 1872 1892 1901 1910 1919 1928</mark>	1453 1473 1482 1491 1500 1509 1529 1538	3 1547 1556 1565 364 384 393 4	402 411 420 440 449 458 467 476	1 21 30 39 48 57 77 86 95 104 113 <mark>42614</mark>
1916 1936 1824 1833 1842 1851 1860 1880 1889 1898 1907	1553 1573 1461 1470 1479 1488 1497 1517	1526 1535 1544 464 484 372	381 390 399 408 428 437 446 455	101 121 9 18 27 36 45 65 74 83 92 <mark>42614</mark>
1895 1904 1924 1933 1821 1830 1839 1859 1868 1877 1886	1532 1541 1561 1570 1458 1467 1476 1496	5 1505 1514 1523 443 452 472	481 369 378 387 407 416 425 434	80 89 109 118 6 15 24 44 53 62 71 42614
1874 1883 1903 1912 1921 1930 1818 1827 1847 1856 1865	1511 1520 1540 1549 1558 1567 1455 1464	1484 1493 1502 422 431 451 4	460 469 478 366 375 395 404 413	59 68 88 97 106 115 3 12 32 41 50 42614
1853 1862 1871 1891 1900 1909 1918 1927 1826 1835 1844	1490 1499 1508 1528 1537 1546 1555 1564	1463 1472 1481 401 410 419 4	439 448 457 466 475 374 383 392	<u>38 47 56 76 85 94 103 112 11 20 29 42614</u>
1832 1841 1850 1870 1879 1888 1897 1906 1915 1935 1823	1469 1478 1487 1507 1516 1525 1534 1543	1552 1572 1460 380 389 398	418 427 436 445 454 463 483 371	17 26 35 55 64 73 82 91 100 120 8 42614
<mark>1932 1820 1829 1838 1858 1867 1876 1885 1894 1914 1923</mark>	1569 1457 1466 1475 1495 1504 1513 1522	2 1531 1551 1560 480 368 377	386 406 415 424 433 442 462 471	117 5 14 23 43 52 61 70 79 99 108 42614
1911 1920 1929 1817 1837 1846 1855 1864 1873 1882 1902	1548 1557 1566 1454 1474 1483 1492 1501	1510 1519 1539 459 468 477	365 385 394 403 412 421 430 450	96 105 114 2 22 31 40 49 58 67 87 42614
1890 1899 1908 1917 1926 1825 1834 1843 1852 1861 1881	1527 1536 1545 1554 1563 1462 1471 1480	0 1489 1498 1518 438 447 456	465 474 373 382 391 400 409 429	75 84 93 102 111 10 19 28 37 46 66 42614
1869 1878 1887 1896 1905 1925 1934 1822 1831 1840 1849	1506 1515 1524 1533 1542 1562 1571 1459	1468 1477 1486 417 426 435	444 453 473 482 370 379 388 397	54 63 72 81 90 110 119 7 16 25 34 42614
1848 1857 1866 1875 1884 1893 1913 1922 1931 1819 1828	1485 1494 1503 1512 1521 1530 1550 1559	9 1568 1456 1465 396 405 414	423 432 441 461 470 479 367 376	33 42 51 60 69 78 98 107 116 4 13 42614
122 142 151 160 169 178 198 207 216 225 234	243 263 272 281 290 299 319 328	337 346 355 1574 1594 1603 1	1612 1621 1630 1650 1659 1668 1677 1686	1695 1715 1724 1733 1742 1751 1771 1780 1789 1798 1807 42614
222 242 130 139 148 157 166 186 195 204 213	343 363 251 260 269 278 287 307	316 325 334 1674 1694 1582 1	1591 1600 1609 1618 1638 1647 1656 1665	1795 1815 1703 1712 1721 1730 1739 1759 1768 1777 1786 42614
201 210 230 239 127 136 145 165 174 183 192	322 331 351 360 248 257 266 286	295 304 313 1653 1662 1682 1	1691 1579 1588 1597 1617 1626 1635 1644	1774 1783 1803 1812 1700 1709 1718 1738 1747 1756 1765 42614
180 189 209 218 227 236 124 133 153 162 171				1753 1762 1782 1791 1800 1809 1697 1706 1726 1735 1744 42614
159 168 177 197 206 215 224 233 132 141 150	280 289 298 318 327 336 345 354			1732 1741 1750 1770 1779 1788 1797 1806 1705 1714 1723 42614
	259 268 277 297 306 315 324 333			1711 1720 1729 1749 1758 1767 1776 1785 1794 1814 1702 42614
	359 247 256 265 285 294 303 312			1811 1699 1708 1717 1737 1746 1755 1764 1773 1793 1802 42614
	338 347 356 244 264 273 282 291			1790 1799 1808 1696 1716 1725 1734 1743 1752 1761 1781 42614
196 205 214 223 232 131 140 149 158 167 187	317 326 335 344 353 252 261 270			1769 1778 1787 1796 1805 1704 1713 1722 1731 1740 1760 42614
175 184 193 202 211 231 240 128 137 146 155				1748 1757 1766 1775 1784 1804 1813 1701 1710 1719 1728 42614
				1727 1736 1745 1754 1763 1772 1792 1801 1810 1698 1707 42614
485 505 514 523 532 541 561 570 579 588 597				<u>1332 1352 1361 1370 1379 1388 1408 1417 1426 1435 1444</u> 42614
	948 968 856 865 874 883 892 912	921 930 939 1069 1089 977		1432 1452 1340 1349 1358 1367 1376 1396 1405 1414 1423 42614
	927 936 956 965 853 862 871 891	900 909 918 1048 1057 1077 1		1411 1420 1440 1449 1337 1346 1355 1375 1384 1393 1402 42614
	906 915 935 944 953 962 850 859	879 888 897 1027 1036 1056 1		1390 1399 1419 1428 1437 1446 1334 1343 1363 1372 1381 42614
	885 894 903 923 932 941 950 959	858 867 876 1006 1015 1024 1		1369 1378 1387 1407 1416 1425 1434 1443 1342 1351 1360 42614
	864 873 882 902 911 920 929 938	947 967 855 985 994 1003 1		
601 489 498 507 527 536 545 554 563 583 592				1448 1336 1345 1354 1374 1383 1392 1401 1410 1430 1439 42614
				1427 1436 1445 1333 1353 1362 1371 1380 1389 1398 1418 42614
				1406 1415 1424 1433 1442 1341 1350 1359 1368 1377 1397 42614
				1385 1394 1403 1412 1421 1441 1450 1338 1347 1356 1365 42614
				1364 1373 1382 1391 1400 1409 1429 1438 1447 1335 1344 42614
				606 626 635 644 653 662 682 691 700 709 718 42614
				706 726 614 623 632 641 650 670 679 688 697 42614 CRE CDA 714 733 C11 C30 C30 C40 CER CC7 C7C 43614
				685 694 714 723 611 620 629 649 658 667 676 42614 664 672 693 703 711 730 608 617 637 646 655 42614
				664 673 693 702 711 720 608 617 637 646 655 42614 642 652 661 681 690 699 708 717 616 625 634 42614
1248 1257 1266 1286 1295 1304 1313 1322 1221 1230 1239				
1227 1236 1245 1265 1274 1283 1292 1301 1310 1330 1218				
				722 610 619 628 648 657 666 675 684 704 713 42614 701 710 719 607 627 626 645 664 662 672 692 42614
				701 710 719 607 627 636 645 654 663 672 692 42614
				680 689 698 707 716 615 624 633 642 651 671 42614 CED CCD CTT CDC CD5 715 724 C12 C21 C20 C20 42614
				659 668 677 686 695 715 724 612 621 630 639 42614 639 647 656 675 674 693 703 713 731 699 619 1361
				638 647 656 665 674 683 703 712 721 609 618 42614
42614 42614 42614 42614 42614 42614 42614 42614 42614 42614 42614 42614	42614 42614 42614 42614 42614 42614 42614 42614	4 42614 42614 42614 42614 42614 42614 4	42614 42614 42614 42614 42614 42614 42614 42614 42614 4	42614 42614 42614 42614 42614 42614 42614 42614 42614 42614 42614 42614 42614

	·	·						, i		, in the second s																								, ,	1									42614
182	7_183	35 18	3 <mark>33</mark> 18	31 18	329 19	<mark>28 19</mark>	29 19	931	1933	1935	1825	1464	1472	1470	1468	1466	1565	1566	1568	1570	1572	1462	375	383	381	379	377	476	477	479	481	483	373	12	20	18	16	14	113	114	116 1	18 12	<mark>0 10</mark>	42614
193	5 184	43 _1	915 19	13 19	911 19	10 18	47 18	349	1851	1845	1816	1573	1480	1552	1550	1548	1547	1484	1486	1488	1482	1453	484	391	463	461	459	458	395	397	399	393	364	121	28	100	98	96	95	32	34 3	36 30	ວ <mark>1</mark>	42614
193	183	36 18	393 18	89 18	891 18	56 18	55 18	353	1895	1916	1818	1571	1473	1530	1526	1528	1493	1492	1490	1532	1553	1455	482	384	441	437	439	404	403	401	443	464	366	119	21	78	74	76	41	40	38 8	80 10	/1 3	42614
193	2 183	38 18	352 18	85_18	388 18	68 18	70 18	369	1900	1914	1820	1569	1475	1489	1522	1525	1505	1507	1506	1537	1551	1457	480	386	400	433	436	416	418	417	448	462	368	117	23	37	70	73	53	55	54 8	85 99	э 5	42614
193) 184	40 18	354 18	65 18	375 18	80 18	73 18	387	1898	1912	1822	1567	1477	1491	1502	1512	1517	1510	1524	1535	1549	1459	478	388	402	413	423	428	421	435	446	460	370	115	25	39	50	60	65	58	72 8	83 97	7 7	42614
182	5 190	08 18	3 <mark>94</mark> 18	66 18	374 18	76 18	78 18	386	1858	1844	1926	1463	1545	1531	1503	1511	1513	1515	1523	1495	1481	1563	374	456	442	414	422	424	426	434	406	392	474	11	93	79	51	59	61	63	71 4	43 29	9 111	1 42614
182	3 190	06 18	392 18	81 18	379 18	72 18	77 18	871	1860	1846	1924	1465	1543	1529	1518	1516	1509	1514	1508	1497	1483	1561	376	454	440	429	427	420	425	419	408	394	472	13	91	77	66	64	57	62	56 4	45 3 ⁻	1 109	9 42614
183) 190	04 18	3 <mark>90</mark> 18	83 18	364 18	84 18	82 18	367	1862	1848	1922	1467	1541	1527	1520	1501	1521	1519	1504	1499	1485	1559	378	452	438	431	412	432	430	415	410	396	470	15	89	75	68	49	69	67	52 4	47 33	3 107	7 42614
183	2 190	02 18	357 18	63 18	861 18	96 18	97 18	399	1859	1850	1920	1469	1539	1494	1500	1498	1533	1534	1536	1496	1487	1557	380	450	405	411	409	444	445	447	407	398	468	17	87	42	48	46	81	82	84 4	44 35	5 10 <mark>5</mark>	5 42614
183	190	07 18	337 18	39 18	841 18	42 19	05 19	903	1901	1909	1918	1471	1544	1474	1476	1478	1479	1542	1540	1538	1546	1555	382	455	385	387	389	390	453	451	449	457	466	19	92	22	24	26	27	90	88 8	86 94	4 <u>10</u> 3	3 42614
192	7 191	17 1	919 19	21 19	923 18	24 18	23 18	821	1819	1817	1925	1564	1554	1556	1558	1560	1461	1460	1458	1456	1454	1562	475	465	467	469	471	372	371	369	367	365	473	112	102	104	106	108	9	8	6	<mark>4 2</mark>	. 110) 42614
133	14	11 1	<mark>39 1</mark> 3	<mark>87 1</mark>	35 2	34 23	35 2	37	239	241	131	254	262	260	258	256	355	356	358	360	362	252	1585	1593	1591	1589	1587	1686	1687	1689	1691	1693	1583	1706	1714	1712	1710 1	1708	<mark>1807</mark> 1	1808 1	1810 18	3 <mark>12 18</mark> 1	<mark>14 170</mark>	4 42614
242	14	9 2	21 21	19 2	217 2	16 15	3 1	55	157	151	122	363	270	342	340	338	337	274	276	278	272	243	1694	1601	1673	1671	1669	1668	1605	1607	1609	1603	1574	1815	1722 _	1794	1792 1	1790	1789 1	726 1	728 17	30 172	24 <mark>169</mark>	<mark>5</mark> 42614
24(14	2 1	99 19	95 1	97 16	52 16	51 1	59	201	222	124	361	263	320	316	318	283	282	280	322	343	245	1692	1594	1651	1647	1649	1614	1613	1611	1653	1674	1576	1813	1715	1772 _	1768 (1770	1735 1	734 1	732 17	74 175	95 <mark>169</mark>	7 42614
238	14	4 1	58 19	91 1	94 17	4 17	<u>6</u> 1	75	206	220	126	359	265	279	312	315	295	297	296	327	341	247	1690	1596	1610	1643	1646	1626	1628	1627	1658	1672	1578	1811	1717	1731	1764 _	1767	1747 1	749 1	748 17	79 175)3 <mark>169</mark>	9 42614
236	14	6 1	60 17	71 1	181 18	86 17	'9 1	93	204	218	128	357	267	281	292	302	307	300	314	325	339	249	1688	1598	1612	1623	1633	1638	1631	1645	1656	1670	1580	1809	1719 1	1733	1744 1	1754	1759 1	752 1	766 17	77 179	э1 <mark>170</mark>	1 42614
132	21	4 2	00 17	2 1	80 18	82 18	84 1	92	164	150	232	253	335	321	293	301	303	305	313	285	271	353	1584	1666	1652	1624	1632	1634	1636	1644	1616	1602	1684	1705	1787	1773	1745 1	1753	1755 1	1757 1	765 17	'37 <mark>172</mark>	23 <mark>180</mark>	<mark>5</mark> 42614
134	21	2 1	<mark>98</mark> 18	37 1	85 17	78 18	3 <mark>3</mark> 1	77	166	152	230	255	333	319	308	306	299	304	298	287	273	351	1586	1664	1650	1639	1637	1630	1635	1629	1618	1604	1682	1707	1785	1771	1760 1	1758	1751 1	1 <mark>756</mark> 1	750 17	39 172	25 <mark>180</mark>	3 42614
136	21	10	96 18	39 1 [°]	70 19	0 18	88 1	73	168	154	228	257	331	317	310	291	311	309	294	289	275	349	1588	1662	1648	1641	1622	1642	1640	1625	1620	1606	1680 ⁻	1709	1783 1	1769	1762 1	1743	1763 ⁻	1761 1	746 17	/41 177	27 <mark>180</mark>	1 42614
138	20	8 1	63 16	59 1	67 2	02 20)3 2	05	165	156	226	259	329	284	290	288	323	324	326	286	277	347	1590	1660	1615	1621	1619	1654	1655	1657	1617	1608	1678	1711	1781	1736	1742 1	1740	1775 1	1776 1	1778 17	38 172	29 <mark>179</mark>	9 42614
140	21	3 1	43 14	15 1	47 14	8 2	11 2	09	207	215	224	261	334	264	266	268	269	332	330	328	336	345	1592	1665	1595	1597	1599	1600	1663	1661	1659	1667	1676	1713	1786	1716	1718 1	1720	1721 1	784 1	782 17	80 178	38 179 [°]	7 42614
233	22	23 2	25 22	27 2	29 13	80 12	.9 1	27	125	123	231	354	344	346	348	350	251	250	248	246	244	352	1685	1675	1677	1679	1681	1582	1581	1579	1577	1575	1683 ⁻	1806	1796 -	1798	1800 1	1802	1703 1	702 1	700 16	<mark>,98 16</mark> 9	<mark>)6 180</mark>	4 42614
496	50)4 5	02 50	00 4	98 5	97 59	98 6	00	602	604	494	859	867	865	863	861	960	961	963	965	967	857	980	988	986	984	982	1081	1082	1084	1086	1088	978 ⁻	1343	1351 (1349	1347 1	1345	1444 1	445 1	447 14	<mark>49 14</mark>	<mark>51 134</mark>	42614
605	51	2 5	84 58	32 5	80 5	79 51	16 5	518	520	514	485	968	875	947	945	943	942	879	881	883	877	848	1089	996	1068	1066	1064	1063	1000	1002	1004	998	969 ⁻	l452	1359 _	1431	1429 1	1427	1426 1	363 1	365 13	67 130	61 <mark>133</mark>	2 42614
603	50)5 5	62 55	58 5	60 5	25 52	24 5	22	564	585	487	966	868	925	921	923	888	887	885	927	948	850	1087				1044		1008			1069	971	1450	1352 1	1409 _	1405 1	1407	1372 ′	1371 1	369 1	411 143	32 133	4 42614
60	50)7 5	521 55	54 5	57 5	37 53	39 5	38	569	583	489	964	870	884	917	920	900	902	901	932	946	852	1085	991	1005	1038	1041	1021	1023	1022	1053	1067	973	1448	1354 1	1368	1401 _1	1404	1384 1	386 1	385 14	416 <mark>14</mark> 3	30 133	6 42614
599	50	9 5	23 53	34 5	44 54	49 54	12 5	56	567	581	491	962	872	886	897	907	912	905	919	930	944	854	1083	993	1007	1018	1028	1033	1026	1040	1051	1065	975	1446	1356 1	1370	1381	1391	1396 1	389 1	403 14	414 147	28 133	8 42614
495			63 53	35 5	43 54	45 54	47 5	55		513		858				906	908	910	918	890	876			1061	1047	1019		1029							1424									42614
		5 5			48 5		<mark>16</mark> 5					860				911																												42614
																				1																								8 42614
50	57	71 5	26 53	32 5	30 5	55 56	56 5	68	528	519	589	864	934	889	895	893	928	929	931	891	882	952	985	1055	1010	1016	1014	1049	1050	1052	1012	1003	1073	1348	1418	1373	1379	1377	1412	1413 1	1415 13	75 136	56 <mark>143</mark>	6 42614
503	57	6 5	06 50	08 5	510 5	11 57	74 5	72	570	578	587	866	939	869	871	873	874	937	935	933	941	950	987	1060	990	992	994	995	1058	1056	1054	1062	1071	1350	1423	1353	1355 1	1357	1358	1421 1	1419 14	117 142	25 143	4 42614
596	58	36 5	88 59	90 5	92 4										953	955	856	855	853	851	849	957	1080	1070	1072	1074	1076	977	976	974	972	970	1078	1443	1433	1435	1437 1	1439	1340 1	339 1	337 13	35 133	3 144	42614
	_		228 12						1328							1103	1202	1203				-			744			839	840	• • •	844			617	625	623	621	619	718	719	721 7	23 72	5 615	5 42614
		_												-							-				-				758						_								-	6 42614
																				1																_								8 42614
																			-																		_							0 42614
																																												2 42614
																																												<mark>5</mark> 42614
															·				1																		L							4 42614
																				J																								2 42614
														L																									686	687 (42614
													L									-		L					816										632	695 (8 42614
																													734															<mark>5</mark> 42614
4261	4 426	514 42	2614 42	614 42	2614 42	514 42	514 42	2614 4	42614 4	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614	42614 4	42614 4	42614 4	42614 4	2614 4	2614 4	2614 4	2614 4	42614 4	42614 4	42614 4	2614 4	2614 42	614 426	14 426	14 42614

																																											4	42614
1827			<mark>3 1831</mark>	-						7																	476	477	479	481	483	373	12	20	18	16	14	113	114	116	118	<mark>120 1</mark>	10 4	42614
1936	1857	/ 190	6 1865	1862	2 1899	1867	1855	1904	1869	1816	1573	1494	1543	1502	1499	1536 1	1504 1	1492	1541	1506	1453	484	405	454	413	410	447	415	403	452	417	364	121	42	91	50	47	84	52	40	89	54	1	42614
1934	1870	185	6 1902	1863	3 1858	1907	1868	1860	1900	1818	1571	1507	1493	1539	1500	1495 1	1544 1	1505	1497	1537	1455	482	418	404	450	411	406	455	416	408	448	366	119	55	41	87	48	43	92	53	45	85	3 4	42614
1932			6 1861																								419		453	412	407	368	117	86	51	46	88	56	39	90	49	44	5	42614
1930			3 1910																											389	462	370	115	60	28	95	65	21	97	58		99	7 4	42614
1826			4 1839																													474	11	100	59	24	93	61	29	98		22 1		42614
1828			1 1879																										390		425	472	13	23	96	64	25	101	57	27				42614
1830			8 1847																															78	73	32	83	66	34	76				42614
1832			2 1884																													468	17	37	77	69	30	79	74	35			05 4	
1834	1883		8 1897				1887					L			1522	1490	1527						L			433	401	438	435	394	443	466	19	68	33	82	70	38	75	72	31		103 4	
1927	1917	191	9 1921				1821		1817						1560	1461 1	460			1454				467		471	372	371	369	367	365	473	112	102	104	106	108	9	8	6	4		110 4	
133	141	139	9 137		234				241							355	356						1593				1686	1687	1689	1691	1693	1583	1706	1714	1712	1710	1708	1807	1808	1810		1814 17		
242	163	212	2 171		205																																					1748 16		
240	176	162	2 208		164																																					1779 16		
238	207		2 167		9 177					-																																1738 16		
236	181	149	9 216		142				220																																	1793 17		
132	221	180) 145		182																																					1716 18		
134	144				222		148																																			1756 18		
136	199	194	4 153		187																																					1730 18		
138	158	198	3 190		200				188																		1652															1761 17		
140	189	154	4 203	191	159	196	193	152	201		261						317						1641	1606	1655	1643	1611	1648	1645	1604	1653	1676	1/13	1762	1727	1//6	1/64	1/32	1/69			1774 17		
233	223	225	5 227	229	9 130	129	127	125	123		354			348		251	250			244				1677	1679	1681	1582	1581	1579	1577	1575	1683	1806	1/96	1/98	1800	1802	1/03	1/02			1696 18		
496							1			7																																1451 13		
605			5 534																																							1385 13		
603	539																																									1416 13		
601	570									-																																1375 13		
599																																										1430 13		
495			3 508																																							1353 14		
				_						_																																1393 14		
																																										1367 14		
																																										1398 14 1411 14		
												L											L																			1333 14		
																																										725 6		
				_						-																																659 6		
																																										690 6		
																																										649 6		
				-			_			-																																704 6		
																																										627 7		
																																										667 7		
				-						-																																641 7		
																																										672 7		
																																										685 7		
												L											L											L								607 7		
																																										42614 42	_	
42014	42014	+ 420	14 42014	+201	+ +2014	+ +2014	+ +2014	42014	+ +2014	42014	42014	42014	42014	42014	42014	+2014 4	2014 4	2014 4	2014	42014	72014	+2014	42014	42014	42014	42014	42014	42014	+2014	42014	42014	+2014	42014	42014	42014	42014	42014	42014	42014	42014	+2014 4	2014 42	.014 2	12014

2.4 Magic Squares of Order 33

Below are three magic squares of order 33 obtained from magic squares of order 143. It is obtained by the application of the formula ormula $\frac{a^2 - b^2}{2}$, a > b,

i.e., subtract $\frac{143^2 - 33^2}{2} := 9680$ from each entry of magic square order 143, we get the following three magic squares of order 33:

																																		17985
848	3	868	877	886	895	904	924	933	942	951	960	1	21	30	39	48	57	77	86	95	104	113	606	626	635	644	653	662	682	691	700	709	718	17985
94	3	968	856	865	874	883	892	912	921	930	939	101	121	9	18	27	36	45	65	74	83	92	706	726	614	623	632	641	650	670	679	688	697	17985
92	7	936	956	965	853	862	871	891	900	909	918	80	89	109	118	6	15	24	44	53	62	71	685	694	714	723	611	620	629	649	658	667	676	17985
90	5	915	935	944	953	962	850	859	879	888	897	59	68	88	97	106	115	3	12	32	41	50	664	673	693	702	711	720	608	617	637	646	655	17985
88	5	894	903	923	932	941	950	959	858	867	876	38	47	56	76	85	94	103	112	11	20	29	643	652	661	681	690	699	708	717	616	625	634	17985
864	1	873	882	902	911	920	929	938	947	967	855	17	26	35	55	64	73	82	91	100	120	8	622	631	640	660	669	678	687	696	705	725	613	17985
964	1	852	861	870	890	899	908	917	926	946	955	117	5	14	23	43	52	61	70	79	99	108	722	610	619	628	648	657	666	675	684	704	713	17985
94	3	952	961	849	869	878	887	896	905	914	934	96	105	114	2	22	31	40	49	58	67	87	701	710	719	607	627	636	645	654	663	672	692	17985
922	2	931	940	949	958	857	866	875	884	893	913	75	84	93	102	111	10	19	28	37	46	66	680	689	698	707	716	615	624	633	642	651	671	17985
90	I	910	919	928	937	957	966	854	863	872	881	54	63	72	81	90	110	119	7	16	25	34	659	668	677	686	695	715	724	612	621	630	639	17985
88)	889	898	907	916	925	945	954	963	851	860	33	42	51	60	69	78	98	107	116	4	13	638	647	656	665	674	683	703	712	721	609	618	17985
243	3	263	272	281	290	299	319	328	337	346	355	485	505	514	523	532	541	561	570	579	588	597	727	747	756	765	774	783	803	812	821	830	839	17985
343	3	363	251	260	269	278	287	307	316	325	334	585	605	493	502	511	520	529	549	558	567	576	827	847	735	744	753	762	771	791	800	809	818	17985
322	2	331	351	360	248	257	266	286	295	304	313	564	573	593	602	490	499	508	528	537	546	555	806	815	835	844	732	741	750	770	779	788	797	17985
30	I	310	330	339	348	357	245	254	274	283	292	543	552	572	581	590	599	487	496	516	525	534	785	794	814	823	832	841	729	738	758	767	776	17985
28)	289	298	318	327	336	345	354	253	262	271	522	531	540	560	569	578	587	596	495	504	513	764	773	782	802	811	820	829	838	737	746	755	17985
25)	268	277	297	306	315	324	333	342	362	250	501	510	519	539	548	557	566	575	584	604	492	743	752	761	781	790	799	808	817	826	846	734	17985
35)	247	256	265	285	294	303	312	321	341	350	601	489	498	507	527	536	545	554	563	583	592	843	731	740	749	769	778	787	796	805	825	834	17985
33	3	347	356	244	264	273	282	291	300	309	329	580	589	598	486	506	515	524	533	542	551	571	822	831	840	728	748	757	766	775	784	793	813	17985
317	'	326	335	344	353	252	261	270	279	288	308	559	568	577	586	595	494	503	512	521	530	550	801	810	819	828	837	736	745	754	763	772	792	17985
29	5	305	314	323	332	352	361	249	258	267	276	538	547	556	565	574	594	603	491	500	509	518	780	789	798	807	816	836	845	733	742	751	760	17985
27	5	284	293	302	311	320	340	349	358	246	255	517	526	535	544	553	562	582	591	600	488	497	759	768	777	786	795	804	824	833	842	730	739	17985
364	1	384	393	402	411	420	440	449	458	467	476	969	989	998	1007	1016	1025	1045	1054	1063	1072	1081	122	142	151	160	169	178	198	207	216	225	234	17985
464	4	484	372	381	390	399	408	428	437	446	455	1069	1089	977	986	995	1004	1013	1033	1042	1051	1060	222	242	130	139	148	157	166	186	195	204	213	17985
443	3	452	472	481	369	378	387	407	416	425	434	1048	1057	1077	1086	974	983	992	1012	1021	1030	1039	201	210	230	239	127	136	145	165	174	183	192	17985
422	2	431	451	460	469	478	366	375	395	404	413	1027	1036	1056	1065	1074	1083	971	980	1000	1009	1018	180	189	209	218	227	236	124	133	153	162	171	17985
40	1	410	419	439	448	457	466	475	374	383	392	1006	1015	1024	1044	1053	1062	1071	1080	979	988	997	159	168	177	197	206	215	224	233	132	141	150	17985
38)	389	398	418	427	436	445	454	463	483	371	985	994	1003	1023	1032	1041	1050	1059	1068	1088	976	138	147	156	176	185	194	203	212	221	241	129	17985
48		368	377	386	406	415	424	433	442	462	471	1085	973	982	991	1011	1020	1029	1038	1047	1067	1076	238	126	135	144	164	173	182	191	200	220		17985
45)	468	477	365	385	394	403	412	421	430	450	1064	1073	1082	970	990	999	1008	1017	1026	1035		217	226	235	123	143	152	161	170	179	188		17985
438		447	456	465	474	373	382	391	400	409	429	1043	1052	1061	1070	1079	978	987	996	1005	1014	1034	196	205	214	223	232	131	140	149	158	167		17985
417	'	426	435	444	453	473	482	370	379	388	397	1022	1031	1040	1049	1058	1078	1087	975	984	993	1002	175	184	193	202	211	231	240	128	137	146		17985
39	5	405	414	423	432	441	461	470	479	367	376	1001	1010	1019	1028	1037	1046	1066	1075	1084	972	981	154	163	172	181	190	199	219	228	237	125	134	17985
1798	85 1	7985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985

																																	17985
859	867	865	863	861	960	961	963	965	967	857	12	20	18	16	14	113	114	116	118	120	10	617	625	623	621	619	718	719	721	723	725	615	17985
968	875	947	945	943	942	879	881	883	877	848	121	28	100	98	96	95	32	34	36	30	1	726	633	705	703	701	700	637	639	641	635	606	17985
966	868	925	921	923	888	887	885	927	948	850	119	21	78	74	76	41	40	38	80	101	3	724	626	683	679	681	646	645	643	685	706	608	17985
964	870	884	917	920	900	902	901	932	946	852	117	23	37	70	73	53	55	54	85	99	5	722	628	642	675	678	658	660	659	690	704	610	17985
962	872	886	897	907	912	905	919	930	944	854	115	25	39	50	60	65	58	72	83	97	7	720	630	644	655	665	670	663	677	688	702	612	17985
858	940	926	898	906	908	910	918	890	876	958	11	93	79	51	59	61	63	71	43	29	111	616	698	684	656	664	666	668	676	648	634	716	17985
860	938	924	913	911	904	909	903	892	878	956	13	91	77	66	64	57	62	56	45	31	109	618	696	682	671	669	662	667	661	650	636	714	17985
862	936	922	915	896	916	914	899	894	880	954	15	89	75	68	49	69	67	52	47	33	107	620	694	680	673	654	674	672	657	652	638	712	17985
864	934	889	895	893	928	929	931	891	882	952	17	87	42	48	46	81	82	84	44	35	105	622	692	647	653	651	686	687	689	649	640	710	17985
866	939	869	871	873	874	937	935	933	941	950	19	92	22	24	26	27	90	88	86	94	103	624	697	627	629	631	632	695	693	691	699	708	17985
959	949	951	953	955	856	855	853	851	849	957	112	102	104	106	108	9	8	6	4	2	110	717	707	709	711	713	614	613	611	609	607	715	17985
254	262	260	258	256	355	356	358	360	362	252	496	504	502	500	498	597	598	600	602	604	494	738	746	744	742	740	839	840	842	844	846	736	17985
363	270	342	340	338	337	274	276	278	272	243	605	512	584	582	580	579	516	518	520	514	485	847	754	826	824	822	821	758	760	762	756	727	17985
361	263	320	316	318	283	282	280	322	343	245	603	505	562	558	560	525	524	522	564	585	487	845	747	804	800	802	767	766	764	806	827	729	17985
359	265	279	312	315	295	297	296	327	341	247	601	507	521	554	557	537	539	538	569	583	489	843	749	763	796	799	779	781	780	811	825	731	17985
357	267	281	292	302	307	300	314	325	339	249	599	509	523	534	544	549	542	556	567	581	491	841	751	765	776	786	791	784	798	809	823	733	17985
253	335	321	293	301	303	305	313	285	271	353	495	577	563	535	543	545	547	555	527	513	595	737	819	805	777	785	787	789	797	769	755	837	17985
255	333	319	308	306	299	304	298	287	273	351	497	575	561	550	548	541	546	540	529	515	593	739	817	803	792	790	783	788	782	771	757	835	17985
257	331	317	310	291	311	309	294	289	275	349	499	573	559	552	533	553	551	536	531	517	591	741	815	801	794	775	795	793	778	773	759	833	17985
259	329	284	290	288	323	324	326	286	277	347	501	571	526	532	530	565	566	568	528	519	589	743	813	768	774	772	807	808	810	770	761	831	17985
261	334	264	266	268	269	332	330	328	336	345	503	576	506	508	510	511	574	572	570	578	587	745	818	748	750	752	753	816	814	812	820	829	17985
354	344	346	348	350	251	250	248	246	244	352	596	586	588	590	592	493	492	490	488	486	594	838	828	830	832	834	735	734	732	730	728	836	17985
375	383	381	379	377	476	477	479	481	483	373	980	988	986	984	982	1081	1082	1084	1086	1088	978	133	141	139	137	135	234	235	237	239	241	131	17985
484	391	463	461	459	458	395	397	399	393	364	1089	996	1068	1066	1064	1063	1000	1002	1004	998	969	242	149	221	219	217	216	153	155	157	151	122	17985
482	384	441	437	439	404	403	401	443	464	366	1087	989	1046	1042	1044	1009	1008	1006	1048	1069	971	240	142	199	195	197	162	161	159	201	222	124	17985
480	386	400	433	436	416	418	417	448	462	368	1085	991	1005	1038	1041	1021	1023	1022	1053	1067	973	238	144	158	191	194	174	176	175	206	220	126	17985
478	388	402	413	423	428	421	435	446	460	370	1083	993	1007	1018	1028	1033	1026	1040	1051	1065	975	236	146	160	171	181	186	179	193	204	218	128	17985
374	456	442	414	422	424	426	434	406	392	474	979	1061	1047	1019	1027	1029	1031	1039	1011	997	1079	132	214	200	172	180	182	184	192	164	150	232	17985
376	454	440	429	427	420	425	419	408	394	472	981	1059	1045	1034	1032	1025	1030	1024	1013	999	1077	134	212	198	187	185	178	183	177	166	152	230	17985
378	452	438	431	412	432	430	415	410	396	470	983	1057	1043	1036	1017	1037	1035	1020	1015	1001	1075	136	210	196	189	170	190	188	173	168	154	228	17985
380	450	405	411	409	444	445	447	407	398	468	985	1055	1010	1016	1014	1049	1050	1052	1012	1003	1073	138	208	163	169	167	202	203	205	165	156	226	17985
382	455	385	387	389	390	453	451	449	457	466	987	1060	990	992	994	995	1058	1056	1054	1062	1071	140	213	143	145	147	148	211	209	207	215	224	17985
475	465	467	469	471	372	371	369	367	365	473	1080	1070	1072	1074	1076	977	976	974	972	970	1078	233	223	225	227	229	130	129	127	125	123	231	17985
17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985

																																		17985
85	9	867	865	863	861	960	961	963	965	967	857	12	20	18	16	14	113	114	116	118	120	10	617	625	623	621	619	718	719	721	723	725	615	17985
96	8	889	938	897	894	931	899	887	936	901	848	121	42	91	50	47	84	52	40	89	54	1	726	647	696	655	652	689	657	645	694	659	606	17985
96	6	902	888	934	895	890	939	900	892	932	850	119	55	41	87	48	43	92	53	45	85	3	724	660	646	692	653	648	697	658	650	690	608	17985
96	4	933	898	893	935	903	886	937	896	891	852	117	86	51	46	88	56	39	90	49	44	5	722	691	656	651	693	661	644	695	654	649	610	17985
96	2	907	875	942	912	868	944	905	873	946	854	115	60	28	95	65	21	97	58	26	99	7	720	665	633	700	670	626	702	663	631	704	612	17985
85	8	947	906	871	940	908	876	945	910	869	958	11	100	59	24	93	61	29	98	63	22	111	616	705	664	629	698	666	634	703	668	627	716	17985
86	0	870	943	911	872	948	904	874	941	909	956	13	23	96	64	25	101	57	27	94	62	109	618	628	701	669	630	706	662	632	699	667	714	17985
86	2	925	920	879	930	913	881	923	918	883	954	15	78	73	32	83	66	34	76	71	36	107	620	683	678	637	688	671	639	681	676	641	712	17985
86	4	884	924	916	877	926	921	882	928	914	952	17	37	77	69	30	79	74	35	81	67	105	622	642	682	674	635	684	679	640	686	672	710	17985
86	6	915	880	929	917	885	922	919	878	927	950	19	68	33	82	70	38	75	72	31	80	103	624	673	638	687	675	643	680	677	636	685	708	17985
95	9	949	951	953	955	856	855	853	851	849	957	112	102	104	106	108	9	8	6	4	2	110	717	707	709	711	713	614	613	611	609	607	715	17985
25	4 _	262	260	258	256	355	356	358	360	362	252	496	504	502	500	498	597	598	600	602	604	494	738	746	744	742	740	839	840	842	844	846	736	17985
36	3	284	333	292	289	326	294	282	331	296	243	605	526	575	534	531	568	536	524	573	538	485	847	768	817	776	773	810	778	766	815	780	727	17985
36	1	297	283	329	290	285	334	295	287	327	245	603	539	525	571	532	527	576	537	529	569	487	845	781	767	813	774	769	818	779	771	811	729	17985
35	9	328	293	288	330	298	281	332	291	286	247	601	570	535	530	572	540	523	574	533	528	489	843	812	777	772	814	782	765	816	775	770	731	17985
35	7	302	270	337	307	263	339	300	268	341	249	599	544	512	579	549	505	581	542	510	583	491	841	786	754	821	791	747	823	784	752	825	733	17985
25	3	342	301	266	335	303	271	340	305	264	353	495	584	543	508	577	545	513	582	547	506	595	737	826	785	750	819	787	755	824	789	748	837	17985
25	5	265	338	306	267	343	299	269	336	304	351	497	507	580	548	509	585	541	511	578	546	593	739	749	822	790	751	827	783	753	820	788	835	17985
25	7	320	315	274	325	308	276	318	313	278	349	499	562	557	516	567	550	518	560	555	520	591	741	804	799	758	809	792	760	802	797	762	833	17985
25	9	279	319	311	272	321	316	277	323	309	347	501	521	561	553	514	563	558	519	565	551	589	743	763	803	795	756	805	800	761	807	793	831	17985
26	1	310	275	324	312	280	317	314	273	322	345	503	552	517	566	554	522	559	556	515	564	587	745	794	759	808	796	764	801	798	757	806	829	17985
35	4	344	346	348	350	251	250	248	246	244	352	596	586	588	590	592	493	492	490	488	486	594	838	828	830	832	834	735	734	732	730	728	836	17985
37	5	383	381	379	377	476	477	479	481	483	373	980	988	986	984	982	1081	1082	1084	1086	1088	978	133	141	139	137	135	234	235	237	239	241	131	17985
48	4	405	454	413	410	447	415	403	452	417	364	1089	1010	1059	1018	1015	1052	1020	1008	1057	1022	969	242	163	212	171	168	205	173	161	210	175	122	17985
48	2	418	404	450	411	406	455	416	408	448	366	1087	1023	1009	1055	1016	1011	1060	1021	1013	1053	971	240	176	162	208	169	164	213	174	166	206	124	17985
48	0	449	414	409	451	419	402	453	412	407	368	1085	1054	1019	1014	1056	1024	1007	1058	1017	1012	973	238	207	172	167	209	177	160	211	170	165	126	17985
47	B	423	391	458	428	384	460	421	389	462	370	1083	1028	996	1063	1033	989	1065	1026	994	1067	975	236	181	149	216	186	142	218	179	147	220	128	17985
37	4	463	422	387	456	424	392	461	426	385	474	979	1068	1027	992	1061	1029	997	1066	1031	990	1079	132	221	180	145	214	182	150	219	184	143	232	17985
37	6	386	459	427	388	464	420	390	457	425	472	981	991	1064	1032	993	1069	1025	995	1062	1030	1077	134	144	217	185	146	222	178	148	215	183	230	17985
37	B	441	436	395	446	429	397	439	434	399	470	983	1046	1041	1000	1051	1034	1002	1044	1039	1004	1075	136	199	194	153	204	187	155	197	192	157	228	17985
38	0	400	440	432	393	442	437	398	444	430	468	985	1005	1045	1037	998	1047	1042	1003	1049	1035	1073	138	158	198	190	151	200	195	156	202	188	226	17985
38	2	431	396	445	433	401	438	435	394	443	466	987	1036	1001	1050	1038	1006	1043	1040	999	1048	1071	140	189	154	203	191	159	196	193	152	201	224	17985
47	5	465	467	469	471	372	371	369	367	365	473	1080	1070	1072	1074	1076	977	976	974	972	970	1078	233	223	225	227	229	130	129	127	125	123	231	17985
179	35 1	7985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985	17985

More examples of higher order can also be obtained in a similar way. See the attached **Excel files** giving **block-wise** bordered magic squares from orders 11 to 154.

3 Author's Contribution to Recreation of Numbers and Magic Squares

- Inder J. Taneja, Recreation of Numbers https://numbers-magic.com/?p=671.
- Inder J. Taneja, Magic Squares https://numbers-magic.com/?cat=3.

References

• Block-Wise Magic Squares

- [1] **H. White**, Bordered Magic Squares *http://budshaw.ca/BorderedMagicSquares.html*
- [2] Inder J. Taneja, Block-Wise Constructions of Magic and Bimagic Squares of Orders 8 to 108, May 15, 2019, pp. 1-43, Zenodo, http://doi.org/10.5281/zenodo.2843326.
- [3] Inder J. Taneja, Block-Wise Equal Sums Pandiagonal Magic Squares of Order 4k, Zenodo, January 31, 2019, pp. 1-17, http://doi.org/10.5281/zenodo.2554288.
- [4] Inder J. Taneja, Magic Rectangles in Construction of Block-Wise Pandiagonal Magic Squares, Zenodo, January 31, 2019, pp. 1-49, http://doi.org/10.5281/zenodo.2554520.
- [5] Inder J. Taneja, Block-Wise Equal Sums Magic Squares of Orders 3k and 6k, Zenodo, February 1, 2019, pp. 1-55, http://doi.org/10.5281/zenodo.2554895.
- [6] Inder J. Taneja, Block-Wise Unequal Sums Magic Squares, Zenodo, February 1, 2019, pp. 1-52, http://doi.org/10.5281/zenodo.2555260.
- [7] Inder J. Taneja, Block-Wise Magic and Bimagic Squares of Orders 12 to 36, Zenodo, February 1, 2019, pp. 1-53, http://doi.org/10.5281/zenodo.2555343.
- [8] Inder J. Taneja, Block-Wise Magic and Bimagic Squares of Orders 39 to 45, Zenodo, February 2, 2019, pp. 1-73, http://doi.org/10.5281/zenodo.2555889.

• Bordered Magic Squares

- [9] Inder J. Taneja, Nested Magic Squares With Perfect Square Sums, Pythagorean Triples, and Borders Differences, Zenodo, June 14, 2019, pp. 1-59, http://doi.org/10.5281/zenodo.3246586.
- [10] Inder J. Taneja, Symmetric Properties of Nested Magic Squares, Zenodo, June 29, 2019, pp. 1-55, http://doi.org/10.5281/zenodo.3262170.

- [11] Inder J. Taneja, General Sum Symmetric and Positive Entries Nested Magic Squares, Zenodo, July 04, 2019, pp. 1-55, http://doi.org/10.5281/zenodo.3268877.
- [12] Inder J. Taneja, Bordered Magic Squares With Order Square Magic Sums, Zenodo, January 20, 2020, pp. 1-26, http://doi.org/10.5281/zenodo.3613690.
- [13] Inder J. Taneja, Fractional and Decimal Type Bordered Magic Squares With Magic Sum 2020. Zenodo, January 20, 2020, pp.1-25. http://doi.org/10.5281/zenodo.3613698.
- [14] Inder J. Taneja, Fractional and Decimal Type Bordered Magic Squares With Magic Sum 2021, Zenodo, December 16, 2020, pp. 1-33, http://doi.org/10.5281/zenodo.4327333.
- [15] Inder J. Taneja, Inder J. Taneja, Block-Wise and Block-Bordered Magic Squares With Magic Sum 2022, Zenodo, December 28, 2021, pp. 1-38, https://doi.org/10.5281/zenodo.5807789

Block-Bordered Magic Squares

- [16] Inder J. Taneja, Block-Bordered Magic Squares of Prime and Double Prime Numbers I, Zenodo, August 18, 2020, pp. 1-81, http://doi.org/10.5281/zenodo.3990291.
- [17] Inder J. Taneja, Block-Bordered Magic Squares of Prime and Double Prime Numbers II, Zenodo, August 18, 2020, pp. 1-90, http://doi.org/10.5281/zenodo.3990293.
- [18] Inder J. Taneja, Block-Bordered Magic Squares of Prime and Double Prime Numbers III, Zenodo, September 01, 2020, pp. 1-93, http://doi.org/10.5281/zenodo.4011213.

Block-Wise and Block-Bordered Magic Squares

- [19] Inder J. Taneja, Block-Wise and Block-Bordered Magic and Bimagic Squares With Magic Sums 21, 21² and 2021. Zenodo, December 16, 2020, pp. 1-118, http://doi.org/10.5281/zenodo.4380343.
- [20] Inder J. Taneja, Block-Wise and Block-Bordered Magic and Bimagic Squares of Orders 10 to 47. Zenodo, January 14, 2021, pp. 1-185, http://doi.org/10.5281/zenodo.4437783.
- [21] Inder J. Taneja, Bordered and Block-Wise Bordered Magic Squares: Odd Order Multiples, Zenodo, Feburary 10, 2021, pp. 1-75, http://doi.org/10.5281/zenodo.4527739

[22] Inder J. Taneja, Bordered and Block-Wise Bordered Magic Squares: Even Order Multiples, Zenodo, Feburary 10, 2021, pp. 1-96, http://doi.org/10.5281/zenodo.4527746

Block-Wise Bordered Magic Squares

- [23] Inder J. Taneja, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 4, Zenodo, August 31, 2021, pp. 1-148, https://doi.org/10.5281/zenodo.5347897.
- [24] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of Magic and Bordered Magic Squares of Order 6, Zenodo, September 10, pp. 1-99 https://doi.org/10.5281/zenodo.5500134.
- [25] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of 8, Zenodo, September 17, pp. 1-80, https://doi.org/10.5281/zenodo.5514396.
- [26] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of 10, Zenodo, September 17, pp. 1-170, https://doi.org/10.5281/zenodo.5514398.
- [27] Inder J. Taneja, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 12, Zenodo, September 23, pp. 1-170, https://doi.org/10.5281/zenodo.5523608.
- [28] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of 14, Zenodo, September 26, pp. 1-198, https://doi.org/10.5281/zenodo.5528867.
- [29] Inder J. Taneja, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 3, Z https://doi.org/10.5281/zenodo.7898383.
- [30] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 5, **Z** https://doi.org/10.5281/zenodo.7903412.
- [31] **Inder J. Taneja**, Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 7, **Z** https://doi.org/10.5281/zenodo.7903420.
- [32] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of 9, Zenodo, May 24, pp. 1-21, 2023, https://doi.org/10.5281/zenodo.7966756.
- [33] Inder J. Taneja, Block-Wise Bordered Magic Squares Multiples of 11, Zenodo, May 24, pp. 1-21, 2023, https://doi.org/10.5281/zenodo.7967254.

Zenodo,	May	05,	pp.	1-29,	2023,
Zenodo,	May	06,	pp.	1-31,	2023,
Zenodo,	May	06,	pp.	1-28,	2023,

• Magic Squares With Bordered Magic Rectangles

- [34] Inder J. Taneja, Different Styles of Magic Squares of Orders 6, 8, 10 and 12 Using Bordered Magic Rectangles, Zenodo, November 14, 2022, pp. 1-26, https://doi.org/10.5281/zenodo.7319985.
- [35] Inder J. Taneja, Different Styles of Magic Squares of Order 14 Using Bordered Magic Rectangles, Zenodo, November 14, 2022, pp. 1-40, https://doi.org/10.5281/zenodo.7319787.
- [36] Inder J. Taneja, Different Styles of Magic Squares of Order 16 Using Bordered Magic Rectangles, Zenodo, November 14, 2022, pp. 1-63, https://doi.org/10.5281/zenodo.7320116.
- [37] Inder J. Taneja, Different Styles of Magic Squares of Order 18 Using Bordered Magic Rectangles, Zenodo, November 14, 2022, pp. 1-85, https://doi.org/10.5281/zenodo.7320131.
- [38] Inder J. Taneja, Different Styles of Magic Squares of Order 20 Using Bordered Magic Rectangles, Zenodo, November 14, 2022, pp. 1-88, https://doi.org/10.5281/zenodo.7320877.
- [39] Inder J. Taneja, Few Examples of Magic Squares of Even Orders 6 to 18 Using Bordered Magic Rectangles, Zenodo, October 19, 2022, pp. 1-30, https://doi.org/10.5281/zenodo.7225854.
- [40] Inder J. Taneja, Few Examples of Magic Squares of Even Orders 20 to 30 Using Bordered Magic Rectangles, Zenodo, October 19, 2022, pp. 1-100, https://doi.org/10.5281/zenodo.7225886.
- [41] Inder J. Taneja, Single Crossed Bordered Magic Rectangles and Magic Squares of Order 40, Zenodo, January 24, 2023, pp. 1-76, https://doi.org/10.5281/zenodo.7565946
- [42] Inder J. Taneja, Double Crossed Bordered Magic Rectangles and Magic Squares of Order 40, Zenodo, January 30, 2023, pp. 1-102, https://doi.org/10.5281/zenodo.7585787
- [43] Inder J. Taneja, Magic Squares of Order 42 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, March 03, 2023, pp. 1-92, https://doi.org/10.5281/zenodo.7695834.
- [44] Inder J. Taneja, Single-Cross Bordered Magic Rectangles and Magic Squares of Order 42, Zenodo, March 03, 2023, pp. 1-69, https://doi.org/10.5281/zenodo.7695939
- [45] Inder J. Taneja, Double-Cross Bordered Magic Rectangles and Magic Squares of Order 42, Zenodo, March 03, 2023, pp. 1-59, https://doi.org/10.5281/zenodo.7696070.

- [46] Inder J. Taneja, Closed Double-Cross Bordered Magic Rectangles and Magic Squares of Order 42, Zenodo, March 03, 2023, pp. 1-28, https://doi.org/10.5281/zenodo.7696181.
- [47] Inder J. Taneja, 8000+ Magic Squares of Order 22 in Different Styles, Models and Designs, Zenodo, April 08, pp. 1-135, https://doi.org/10.5281/zenodo.7809478.

• Figured Magic Squares and Bordered Magic Rectangles

- [48] Inder J. Taneja, Figured Magic Squares of Orders 6, 10, 12, 14 and 16 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, November 29, 2022, pp. 1-31, https://doi.org/10.5281/zenodo.7377674.
- [49] Inder J. Taneja, Figured Magic Squares of Orders 18 and 20 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, November 29, 2022, pp. 1-87, https://doi.org/10.5281/zenodo.7377689.
- [50] Inder J. Taneja, Figured Magic Squares of Order 22 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, November 29, 2022, pp. 1-61, https://doi.org/10.5281/zenodo.7377706.
- [51] Inder J. Taneja, Figured Magic Squares of Order 24 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, November 29, 2022, pp. 1-104, https://doi.org/10.5281/zenodo.7377779.
- [52] Inder J. Taneja, Figured Magic Squares of Order 26 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, November 29, 2022, pp. 1-88, https://doi.org/10.5281/zenodo.7377794.
- [53] Inder J. Taneja, Figured Magic Squares of Order 28 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, December 02, 2022, pp. 1-179, https://doi.org/10.5281/zenodo.7390666.
- [54] Inder J. Taneja, Figured Magic Squares of Order 30 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, December 02, 2022, pp. 1-179, https://doi.org/10.5281/zenodo.7390705.
- [55] Inder J. Taneja, Figured Magic Squares of Order 32 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, December 22, 2022, pp. 1-310, https://doi.org/10.5281/zenodo.7472891.
- [56] Inder J. Taneja, Figured Magic Squares of Order 34 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, December 27, 2022, pp. 1-193, https://doi.org/10.5281/zenodo.7486540.

- [57] Inder J. Taneja, Figured Magic Squares of Order 36 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, December 27, 2022, pp. 1-140, https://doi.org/10.5281/zenodo.7486548.
- [58] Inder J. Taneja, Figured Magic Squares of Order 38 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, January 03, 2023, pp. 1-133, https://doi.org/110.5281/zenodo.7500188.
- [59] Inder J. Taneja, Figured Magic Squares of Order 40 Using Bordered Magic Rectangles: A Systematic Procedure, Zenodo, January 03, 2023, pp. 1-157, https://doi.org/10.5281/zenodo.7500192.

• Two Digits Bordered Magic Squares

- [60] Inder J. Taneja, Two Digits Bordered Magic Squares Multiples of 4: Orders 8 to 24, Zenodo, April, 26, 2023, pp. 1-43, https://doi.org/10.5281/zenodo.7866956.
- [61] Inder J. Taneja, Two Digits Bordered Magic Squares of Orders 28 and 32, Zenodo, April, 26, 2023, pp. 1-36, https://doi.org/10.5281/zenodo.7866981.
- [62] Inder J. Taneja, Two Digits Bordered Magic Squares of Orders 10, 14, 18 and 22, Zenodo, April, 30, 2023, pp. 1-43, https://doi.org/10.5281/zenodo.7880931.
- [63] Inder J. Taneja, Two Digits Bordered Magic Squares of Orders 26 and 30, Zenodo, April, 30, 2023, pp. 1-45, https://doi.org/10.5281/zenodo.7880937.
- [64] Inder J. Taneja, Two Digits Bordered Magic Squares of Orders 36 and 40, Zenodo, May, 04, 2023, pp. 1-41, https://doi.org/10.5281/zenodo.7896709.

• Cornered Magic Squares of Order 6

[65] Inder J. Taneja, Cornered Magic Squares of Order 6, Zenodo, May 23, 2023, pp. 1-23, https://10.5281/zenodo.7960679

• Creative Magic Squares

[66] Inder J. Taneja, Creative Magic Squares: Area Representations, Zenodo, June 22, pp. 1-45, 2021, http://doi.org/10.5281/zenodo.5009224.