Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 7

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Abstract

During past years author worked with **block-wise borderedmagic squares** of even number blocks. These are based on equal sums magic squares of orders 4, 6, 8, 10, etc. This type of work is an extension of classical bordered magic squares. In case of multiples of 4, the extension is made for **pandiagonal** magic squares [23]. For multiples of order 6 refer Taneja [24]. For the first time, we are presenting here bordered magic squares of odd number blocks. Recently, author worked on multiples of 3, based on different sums magic squares of order 3 [29]. The work for the borders multiples of 5 refer [30]. It is done with two types of magic squares of order 5. One type is pandiagonal magic squares, and anotheras bordered magic squares. Based on same procedure we worked with multiples of 7 based on magic squares of order 7. Padiagonal magic squares of orders 21, 28, 35 and 49 are also given. Higher order examples can be seen in **Excel file** attached with the work. The total work is up to order 140. Pandiagonal magic squares based on equal sums pandiagonal magic squares of order 7 are also included in the Excel file.

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Introduction 1

During past years author [2, 3, 4, 5, 6, 7, 8] worked with **block-wise** magic squares from orders 12 to 47. Author [9, 10, 11, 12, 13, 14] also worked with **bordered** magic squares. The study on **bordered** magic squares is extended to **block-bordered** magic squares [15, 16, 17]. This is specially done for the magic squares of orders p and 2p, where p is a prime number. This study is still extended to **block-wise bordered** magic squares [18, 19, 20, 21]. Some conection with Pythagorean triples and area-representations are also made [23, 24, 25, 26, 27]. The main property of bordered magic squares is that if we remove external borders, still we get sub-bordered magic squares, i.e., each layer in itself lead us to magic squares. In many cases, the properties of **bordered** magic square are seperated by **even** and **odd** orders magic squares. In many cases, we get good properties for the even order bordered magic squares. In some cases, we have to use fractional numbers to reach minimum perfect square sum of entries. For more study on **bordered** magic squares refer H. White's web-site [1].

The idea of bordered magic squares is already discussed by H. White's web-site [1] where the borders are of single digits. Borders multiples of even numbers starting from 4 are done extensively by author [23, 24, 25, 26, 27, 28].

Recently, for the first time, we presented bordered magic squares of odd number blocks. In case of multiples of 3, we worked with different sums magic squares of order 3. In case of multiples of 5, we worked with **pandiagonal** and **bordered** magic squares of order 5. This work is for multiples of 7. Here also we worked with two types of magic squares of order 7. One **pandiagonal** and another is **bordered** magic squares of order 7. The procedure, how to get these **block-wise bordered** magic squares is also explained. **Pandiagonal** magic squares multiples of 7 are also given. This work is up to order 49. Higher orders examples can be seen in **Excel file** attached with this work. Before proceeding further, let's summarize, the idea of **block-wise bordered** magic squares:

Classification of Bordered Magic Squares 1.1

- Single Digit: Bordered magic squares based on single digit [9, 10, 1].
- Two Digits: Bordered magic squares based on magic rectangles multiples of 2 [58, 59, 60, 61, 61].
- Three Digits: Bordered magic squares based on magic squares of order 3 [29].
- Four Digits: Bordered magic squares based on magic squares of order 4 [23].
- Five Digits: Bordered magic squares based on magic squares of order 5 [30].
- Six Digits: Bordered magic squares based on magic squares of order 6 [24].
- Seven Digits: Bordered magic squares based on magic squares of order 7 (This work).

For further even number multiples refer the following works of author:

- Eight Digits: Bordered magic squares based on magic squares of order 8 [25].
- **Ten Digits:** Bordered magic squares based on magic squares of order 10 [26].
- **Twelve Digits:** Bordered magic squares based on magic squares of order 12 [27].
- Fourteen Digits: Bordered magic squares based on magic squares of order 14 [28].

Let's see below the some examples of **block-wise bordered** magic squares multiples 7, where magic squares of order 7 are considered in two different ways.

Block-Wise Bordered Magic Squares 2

2.1 Magic Squares of Orders 42 and 49

Let's consider bordered magic square of orders 6 and 7 given by

6							111
	6	30	3	36	4	32	111
	35	17	22	11	24	2	111
	29	12	23	18	21	8	111
	27	26	13	20	15	10	111
	9	19	16	25	14	28	111
	5	7	34	1	33	31	111
	111	111	111	111	111	111	শগ

7								175
	44	38	40	5	4	2	42	175
	11	34	30	15	14	32	39	175
	9	19	28	21	26	31	41	175
	7	17	23	25	27	33	43	175
	47	37	24	29	22	13	3	175
	49	18	20	35	36	16	1	175
	8	12	10	45	46	48	6	175
	175	175	175	175	175	175	175	175

The entries of above two magic squares are sequential numbers starting from 1:

 $D_{11\times 11} := \{1, 2, \dots, 35, 36\}$ $D_{12\times 12} := \{1, 2, \dots, 48, 49\}$

These two magic squares are such that replacing the upper border still we are left with magic squares of sequential vales. Multiplying each entry by 49, we get

6							5439
	294	1470	147	1764	196	1568	5439
	1715	833	1078	539	1176	98	5439
	1421	588	1127	882	1029	392	5439
	1323	1274	637	980	735	490	5439
	441	931	784	1225	686	1372	5439
	245	343	1666	49	1617	1519	5439
	5439	5439	5439	5439	5439	5439	5439

7								8575
	2156	1862	1960	245	196	98	2058	8575
	539	1666	1470	735	686	1568	1911	8575
	441	931	1372	1029	1274	1519	2009	8575
	343	833	1127	1225	1323	1617	2107	8575
	2303	1813	1176	1421	1078	637	147	8575
	2401	882	980	1715	1764	784	49	8575
	392	588	490	2205	2254	2352	294	8575
	8575	8575	8575	8575	8575	8575	8575	8575

The distributions of these two magic squares are given by

 $D1_{7\times7} := \{49, 98, \dots, 1715, 1764\}$ $D1_{8\times8} := \{49, 98\dots, 2352, 2401\}.$

In both the cases the difference between entries is 25. Now in each case replace the entries by magic squares of order 5 formed by the entries as given below:

49	\rightarrow	$1, 2, \ldots, 49$
98	\rightarrow	$50, 51, \ldots, 98$
147	\rightarrow	$99, 100, \ldots, 147$
	\rightarrow	
2352	\rightarrow	$2304, 2305, \dots, 2352$
2401	\rightarrow	$2353, 2354 \dots, 2401$

This lead us to following two bordered magic squares of orders 42 and 49.

42		37865
294 286 278 270 262 254 246 1470 1462 1454 1446 1438 1430 1422 14	47 139 131 123 115 107 99 1764 1756 1748 1740 1732 1724 17	16 196 188 180 172 164 156 148 1568 1560 1552 1544 1536 1528 1520 37065
255 247 288 287 279 271 263 1431 1423 1464 1463 1455 1447 1439 10	08 100 141 140 132 124 116 1725 1717 1758 1757 1749 1741 17	33 157 149 190 189 181 173 165 1529 1521 1562 1561 1553 1545 1537 37065
272 264 256 248 289 281 280 1448 1440 1432 1424 1465 1457 1456 12	25 117 109 101 142 134 133 1742 1734 1726 1718 1759 1751 17	50 174 166 158 150 191 183 182 1546 1538 1530 1522 1563 1555 1554 37065
282 274 273 265 257 249 290 1458 1450 1449 1441 1433 1425 1466 13	35 127 126 118 110 102 143 1752 1744 1743 1735 1727 1719 17	60 184 176 175 167 159 151 192 1556 1548 1547 1539 1531 1523 1564 37065
250 291 283 275 267 266 258 1426 1467 1459 1451 1443 1442 1434 10	03 144 136 128 120 119 111 1720 1761 1753 1745 1737 1736 17	28 152 193 185 177 169 168 160 1524 1565 1557 1549 1541 1540 1532 37065
		38 162 161 153 194 186 178 170 1534 1533 1525 1566 1558 1550 1542 37065
		55 179 171 163 155 154 195 187 1551 1543 1535 1527 1526 1567 1559 37065
1715 1707 1699 1691 1683 1675 1667 833 825 817 809 801 793 785 107	078 1070 1062 1054 1046 1038 1030 539 531 523 515 507 499 4	91 1176 1168 1160 1152 1144 1136 1128 98 90 82 74 66 58 50 37065
1676 1668 1709 1708 1700 1692 1684 794 786 827 826 818 810 802 103	039 1031 1072 1071 1063 1055 1047 500 492 533 532 524 516 5	08 1137 1129 1170 1169 1161 1153 1145 59 51 92 91 83 75 67 37065
1693 1685 1677 1669 1710 1702 1701 811 803 795 787 828 820 819 105		
1703 1695 1694 1686 1678 1670 1711 821 813 812 804 796 788 829 106		
1671 1712 1704 1696 1688 1687 1679 789 830 822 814 806 805 797 103		
1681 1680 1672 1713 1705 1697 1689 799 798 790 831 823 815 807 104		
1698 1690 1682 1674 1673 1714 1706 816 808 800 792 791 832 824 100		
		34 1029 1021 1013 1005 997 989 981 392 384 376 368 360 352 344 37065
		51 990 982 1023 1022 1014 1006 998 353 345 386 385 377 369 361 37065
		68 1007 999 991 983 1024 1016 1015 370 362 354 346 387 379 378 37065
		78 1017 1009 1008 1000 992 984 1025 380 372 371 363 355 347 388 37065
		46 985 1026 1018 1010 1002 1001 993 <mark>348 389 381 373 365 364 356</mark> 37065
		56 995 994 986 1027 1019 1011 1003 <mark>358 357 349 390 382 374 366</mark> 37065
		73 1012 1004 996 988 987 1028 1020 375 367 359 351 350 391 383 37065
		32 735 727 719 711 703 695 687 490 482 474 466 458 450 442 37065
		49 696 688 729 728 720 712 704 451 443 484 483 475 467 459 37065
		66 713 705 697 689 730 722 721 <mark>468 460 452 444 485 477 476</mark> 37065
		76 723 715 714 706 698 690 731 478 470 469 461 453 445 486 37065
		44 691 732 724 716 708 707 699 446 487 479 471 463 462 454 37065
		54 701 700 692 733 725 717 709 456 455 447 488 480 472 464 37065
		71 718 710 702 694 693 734 726 473 465 457 449 448 489 481 37065
		77 686 678 670 662 654 646 638 1372 1364 1356 1348 1340 1332 1324 37065
		94 647 639 680 679 671 663 655 1333 1325 1366 1365 1357 1349 1341 37065
		211 664 656 648 640 681 673 672 1350 1342 1334 1326 1367 1359 1358 37065
		21 674 666 665 657 649 641 682 1360 1352 1351 1343 1335 1327 1368 37065
		89 642 683 675 667 659 658 650 1328 1369 1361 1353 1345 1344 1336 37065
		99 652 651 643 684 676 668 660 1338 1337 1329 1370 1362 1354 1346 37065
		16 669 661 653 645 644 685 677 1355 1347 1339 1331 1330 1371 1363 37065
		1 1617 1609 1601 1593 1585 1577 1569 1519 1511 1503 1495 1487 1479 1471 37065
		8 1578 1570 1611 1610 1602 1594 1586 1480 1472 1513 1512 1504 1496 1488 37065
		5 1595 1587 1579 1571 1612 1604 1603 1497 1489 1481 1473 1514 1506 1505 37065
		15 1605 1597 1596 1588 1580 1572 1613 1507 1499 1498 1490 1482 1474 1515 37065
		3 1573 1614 1606 1598 1590 1589 1581 1475 1516 1508 1500 1492 1491 1483 37065
		3 1583 1582 1574 1615 1607 1599 1591 1485 1484 1476 1517 1509 1501 1493 37065
		10 1600 1592 1584 1576 1575 1616 1608 1502 1494 1476 1477 1509 1501 1495 37065
		065 370
21002 2	2003 2009 2009 2009 2009 2009 2009 2009	21005 21003

42				37065
251 257 255 290 291 293 253 1427 1433 1431	1466 1467 1469 1429 104 110 108 143 144 146 106	1721 1727 1725 1760 1761 1763 172	3 153 159 157 192 193 195 155 152	25 1531 1529 1564 1565 1567 1527 37065
284 261 265 280 281 263 256 1460 1437 1441	1456 1457 1439 1432 137 114 118 133 134 116 109	1754 1731 1735 1750 1751 1733 1720	6 186 163 167 182 183 165 158 155	8 1535 1539 1554 1555 1537 1530 37065
286 276 267 274 269 264 254 1462 1452 1443	1450 1445 1440 1430 139 129 120 127 122 117 107	1756 1746 1737 1744 1739 1734 172	4 188 178 169 176 171 166 156 156	0 1550 1541 1548 1543 1538 1528 37065
288 278 272 270 268 262 252 1464 1454 1448	1446 1444 1438 1428 141 131 125 123 121 115 105	1758 1748 1742 1740 1738 1732 172	2 190 180 174 172 170 164 154 156	2 1552 1546 1544 1542 1536 1526 37065
	1442 1449 1458 1468 101 111 124 119 126 135 145			
	1436 1435 1455 1470 99 130 128 113 112 132 147			0 1551 1549 1534 1533 1553 1568 37065
287 283 285 250 249 247 289 1463 1459 1461	1426 1425 1423 1465 140 136 138 103 102 100 142	1757 1753 1755 1720 1719 1717 175	9 189 185 187 152 151 149 191 156	51 1557 1559 1524 1523 1521 1563 37065
1672 1678 1676 1711 1712 1714 1674 790 796 794	829 830 832 792 1035 1041 1039 1074 1075 1077 103	7 496 502 500 535 536 538 498	3 1133 1139 1137 1172 1173 1175 1135 55	5 61 59 94 95 97 57 37065
	819 820 802 795 1068 1045 1049 1064 1065 1047 104			
	813 808 803 793 1070 1060 1051 1058 1053 1048 103			
	809 807 801 791 1072 1062 1056 1054 1052 1046 103			
	805 812 821 831 1032 1042 1055 1050 1057 1066 107			
	799 798 818 833 1030 1061 1059 1044 1043 1063 107			
	789 788 786 828 1071 1067 1069 1034 1033 1031 107			
	584 585 587 547 1084 1090 1088 1123 1124 1126 108			
	574 575 557 550 1117 1094 1098 1113 1114 1096 108			
	568 563 558 548 1119 1109 1100 1107 1102 1097 108			
	564 562 556 546 1121 1111 1105 1103 1101 1095 108			
	560 567 576 586 1081 1091 1104 1099 1106 1115 112			
	554 553 573 588 1079 1110 1108 1093 1092 1112 112			
	544 543 541 583 1120 1116 1118 1083 1082 1080 112			
	1270 1271 1273 1233 594 600 598 633 634 636 596			
	1260 1261 1243 1236 627 604 608 623 624 606 599			
	1254 1249 1244 1234 629 619 610 617 612 607 597			
	1250 1248 1242 1232 631 621 615 613 611 605 59			
	1246 1253 1262 1272 591 601 614 609 616 625 63			
	1240 1239 1259 1274 589 620 618 603 602 622 633			
	1230 1229 1227 1269 630 626 628 593 592 590 632			
	927 928 930 890 741 747 745 780 781 783 743			
	917 918 900 893 774 751 755 770 771 753 746			
	911 906 901 891 776 766 757 764 759 754 74			
	907 905 899 889 778 768 762 760 758 752 742			
	903 910 919 929 738 748 761 756 763 772 782			
	897 896 916 931 736 767 765 750 749 769 784			
	887 886 884 926 777 773 775 740 739 737 775 339 340 342 302 1623 1629 1627 1662 1663 1665 162		1574 1580 1578 1613 1614 1616 1576 147	
	329 330 312 305 1656 1633 1637 1652 1653 1635 162			
	323 318 313 303 1658 1648 1639 1646 1641 1636 162		1609 1599 1590 1597 1592 1587 1577 151	
	319 317 311 301 1660 1650 1644 1642 1640 1634 162 315 322 331 341 1620 1630 1643 1628 1645 1654 165			
	<u>315</u> <u>322</u> <u>331</u> <u>341</u> <u>1620</u> <u>1630</u> <u>1643</u> <u>1638</u> <u>1645</u> <u>1654</u> <u>166</u>			
	<u>309 308 328 343 1618 1649 1647 1632 1631 1651 166</u>			
	299 298 296 338 1659 1655 1657 1622 1621 1619 166		1610 1606 1608 1573 1572 1570 1612 151	
37065 37065 37065 37065 37065 37065 37065 37065 37065 37065	37065 37065 37065 37065 37065 37065 37065 37065 37065 37065 3706	5 37065 37065 37065 37065 37065 37065 3706	5 37065 37065 37065 37065 37065 37065 37065 370	05 37065 37065 37065 37065 37065 37065 37065

Above two magic squares of order 42 formed by blocks of magic squares of order 7 are with sequential entries:

 $D_{35\times35} := \{1, 2, \dots, 1763, 1764\}$

Below are two bordered magic squares of order 49 with blocks of magic squares of order 7:

49	58849
2156 2148 2140 2132 2124 2116 2108 1862 1854 1846 1838 1830 1822 1814 1960 1952 1944 1936 1928 1920 1912 245 237 229 221 213 205 197 196 188 180 172 164 156 148 98 90 82 74 66 58 50 2058 2050 2042 2034 2026 2018 2010	58849
2117 2109 2150 2149 2141 2133 2125 1823 1815 1856 1855 1847 1839 1831 1921 1913 1954 1953 1945 1937 1929 206 198 239 238 230 222 214 157 149 190 189 181 173 165 59 51 92 91 83 75 67 2019 2011 2052 2051 2043 2035 2027	58849
2134 2126 2118 2110 2151 2143 2142 1840 1832 1824 1816 1857 1849 1848 1938 1930 1922 1914 1955 1947 1946 223 215 207 199 240 232 231 174 166 158 150 191 183 182 76 68 60 52 93 85 84 2036 2028 2020 2012 2053 2045 2044	58849
2144 2136 2135 2127 2119 2111 2152 1850 1842 1841 1833 1825 1817 1858 1948 1940 1939 1931 1923 1915 1956 233 225 224 216 208 200 241 184 176 175 167 159 151 192 86 78 77 69 61 53 94 2046 2038 2037 2029 2021 2013 2054	58849
2112 2153 2145 2137 2129 2128 2120 1818 1859 1851 1843 1835 1834 1826 1916 1957 1949 1941 1933 1932 1924 201 242 234 226 218 217 209 152 193 185 177 169 168 160 54 95 87 79 71 70 62 2014 2055 2047 2039 2031 2030 2022	58849
2122 2121 2113 2154 2146 2138 2130 1828 1827 1819 1860 1852 1844 1836 1926 1925 1917 1958 1950 1942 1934 211 210 202 243 235 227 219 162 161 153 194 186 178 170 64 63 55 96 88 80 72 2024 2023 2015 2056 2048 2040 2032	58849
2139 2131 2123 2115 2114 2155 2147 1845 1837 1829 1821 1820 1861 1853 1943 1935 1927 1919 1918 1959 1951 228 220 212 204 203 244 236 179 171 163 155 154 195 187 81 73 65 57 56 97 89 2041 2033 2025 2017 2016 2057 2049	58849
539 531 523 515 507 499 491 1666 1658 1650 1642 1634 1626 1618 1470 1462 1454 1446 1438 1430 1422 735 727 719 711 703 695 687 686 678 670 662 654 646 638 1568 1560 1552 1544 1536 1528 1520 1911 1903 1895 1887 1879 1871 1863	58849
500 492 533 532 524 516 508 1627 1619 1660 1659 1651 1643 1635 1431 1423 1464 1463 1455 1447 1439 696 688 729 728 720 712 704 647 639 680 679 671 663 655 1529 1521 1562 1561 1553 1545 1537 1872 1864 1905 1904 1896 1888 1880	58849
517 509 501 493 534 526 525 1644 1636 1628 1620 1661 1653 1652 1448 1440 1432 1424 1465 1457 1456 713 705 697 689 730 722 721 664 656 648 640 681 673 672 1546 1538 1530 1522 1563 1555 1554 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897 1889 1881 1873 1865 1906 1898 1897	58849
527 519 518 510 502 494 535 1654 1646 1645 1637 1629 1621 1662 1458 1450 1449 1441 1433 1425 1466 723 715 714 706 698 690 731 674 666 665 657 649 641 682 1556 1548 1547 1539 1531 1523 1564 1899 1891 1890 1882 1874 1866 1907	58849
495 536 528 520 512 511 503 1622 1663 1655 1647 1639 1638 1630 1426 1467 1459 1451 1443 1442 1434 691 732 724 716 708 707 699 642 683 675 667 659 658 650 1524 1565 1557 1549 1541 1540 1532 1867 1908 1900 1892 1884 1883 1875	58849
505 504 496 537 529 521 513 1632 1631 1623 1664 1656 1648 1640 1436 1435 1427 1468 1460 1452 1444 701 700 692 733 725 717 709 652 651 643 684 676 668 660 1534 1533 1525 1566 1558 1550 1542 1877 1876 1868 1909 1901 1893 1885	58849
522 514 506 498 497 538 530 1649 1641 1633 1625 1624 1665 1657 1453 1445 1437 1429 1428 1469 1461 718 710 702 694 693 734 726 669 661 653 645 644 685 677 1551 1543 1535 1527 1526 1567 1559 1894 1886 1878 1870 1869 1910 1902	58849
441 433 425 417 409 401 393 931 923 915 907 899 891 883 1372 1364 1356 1348 1340 1332 1324 1029 1021 1013 1005 997 989 981 1274 1266 1258 1250 1242 1234 1226 1519 1511 1503 1495 1487 1479 1471 2009 2001 1993 1985 1977 1969 1961	58849
402 394 435 434 426 418 410 892 884 925 924 916 908 900 1333 1325 1366 1365 1357 1349 1341 990 982 1023 1022 1014 1006 998 1235 1227 1268 1267 1259 1251 1243 1480 1472 1513 1512 1504 1496 1488 1970 1962 2003 2002 1994 1986 1978	58849
419 411 403 395 436 428 427 909 901 893 885 926 918 917 1350 1342 1334 1326 1367 1359 1358 1007 999 991 983 1024 1016 1015 1252 1244 1236 1228 1269 1261 1260 1497 1489 1481 1473 1514 1506 1505 1987 1979 1971 1963 2004 1996 1995 1	58849
429 421 420 412 404 396 437 919 911 910 902 894 886 927 1360 1352 1351 1343 1335 1327 1368 1017 1009 1008 1000 992 984 1025 1262 1254 1253 1245 1237 1229 1270 1507 1499 1498 1490 1482 1474 1515 1997 1989 1988 1980 1972 1964 2005	58849
397 438 430 422 414 413 405 887 928 920 912 904 903 895 1328 1369 1361 1353 1345 1344 1336 985 1026 1018 1010 1002 1001 993 1230 1271 1263 1255 1247 1246 1238 1475 1516 1508 1500 1492 1491 1483 1965 2006 1998 1990 1982 1981 1973	58849
407 406 398 439 431 423 415 897 896 888 929 921 913 905 1338 1337 1329 1370 1362 1354 1346 995 994 986 1027 1019 1011 1003 1240 1239 1231 1272 1264 1256 1248 1485 1484 1476 1517 1509 1501 1493 1975 1974 1966 2007 1999 1991 1983	58849
424 416 408 400 399 440 432 914 906 898 890 889 930 922 1355 1347 1339 1331 1330 1371 1363 1012 1004 996 988 987 1028 1020 1257 1249 1241 1233 1232 1273 1265 1502 1494 1486 1478 1477 1518 1510 1992 1984 1976 1968 1967 2008 2000 1	58849
343 335 327 319 311 303 295 833 825 817 809 801 793 785 1127 1119 1111 1103 1095 1087 1079 1225 1217 1209 1201 1193 1185 1177 1323 1315 1307 1299 1291 1283 1275 1617 1609 1601 1593 1585 1577 1569 2107 2099 2091 2083 2075 2067 2059 1000 1000 1000 1000 1000 1000 1000 1	58849
304 296 337 336 328 320 312 794 786 827 826 818 810 802 1088 1080 1121 1120 1112 1104 1096 1186 1178 1219 1218 1210 1202 1194 1284 1276 1317 1316 1308 1300 1292 1578 1570 1611 1610 1602 1594 1586 2068 2060 2101 2100 2092 2084 2076 1	58849
321 313 305 297 338 330 329 811 803 795 787 828 820 819 1105 1097 1089 1081 1122 1114 1113 1203 1195 1187 1179 1220 1212 1211 1301 1293 1285 1277 1318 1310 1309 1595 1587 1579 1571 1612 1604 1603 2085 2077 2069 2061 2102 2094 2093	58849
331 323 322 314 306 298 339 821 813 812 804 796 788 829 1115 1107 1106 1098 1090 1082 1123 1205 1204 1196 1188 1180 1221 1311 1303 1302 1294 1286 1278 1319 1605 1597 1596 1588 1580 1572 1613 2095 2087 2086 2078 2070 2062 2103 1	58849
299 340 332 324 316 315 307 789 830 822 814 806 805 797 1083 1124 1116 1108 1100 1099 1091 1181 1222 1214 1206 1198 1197 1189 1279 1320 1312 1304 1296 1295 1287 1573 1614 1606 1598 1590 1589 1581 2063 2104 2096 2088 2080 2079 2071	58849
309 308 300 341 333 325 317 799 798 790 831 823 815 807 1093 1092 1084 1125 1117 1109 1101 1191 1190 1182 1223 1215 1207 1199 1289 1288 1280 1321 1313 1305 1297 1583 1582 1574 1615 1607 1599 1591 2073 2072 2064 2105 2097 2089 2081	58849
326 318 310 302 301 342 334 816 808 800 792 791 832 824 1110 1102 1094 1086 1085 1126 1118 1208 1200 1192 1184 1183 1224 1216 1306 1298 1290 1282 1281 1322 1314 1600 1592 1584 1576 1575 1616 1608 2090 2082 2074 2066 2065 2106 2098	58849
2303 2295 2287 2279 2271 2263 2255 1813 1805 1797 1789 1781 1773 1765 1176 1168 1160 1152 1144 1136 1128 1421 1413 1405 1397 1389 1381 1373 1078 1070 1062 1054 1046 1038 1030 637 629 621 613 605 597 589 147 139 131 123 115 107 99	58849
2264 2256 2297 2296 2288 2280 2272 1774 1766 1807 1806 1798 1790 1782 1137 1129 1170 1169 1161 1153 1145 1382 1374 1415 1414 1406 1398 1390 1039 1031 1072 1071 1063 1055 1047 598 590 631 630 622 614 606 108 100 141 140 132 124 116	58849
2281 2273 2265 2257 2298 2290 2289 1791 1783 1775 1767 1808 1800 1799 1154 1146 1138 1130 1171 1163 1162 1399 1391 1383 1375 1416 1408 1407 1056 1048 1040 1032 1073 1065 1064 615 607 599 591 632 624 623 125 117 109 101 142 134 133	58849
2291 2283 2282 2274 2266 2258 2299 1801 1793 1792 1784 1776 1768 1809 1164 1156 1155 1147 1139 1131 1172 1409 1401 1400 1392 1384 1376 1417 1066 1058 1057 1049 1041 1033 1074 625 617 616 608 600 592 633 135 127 126 118 110 102 143	58849
2259 2300 2292 2284 2276 2275 2267 1769 1810 1802 1794 1786 1785 1777 1132 1173 1165 1157 1149 1148 1140 1377 1418 1410 1402 1394 1393 1385 1034 1075 1067 1059 1051 1050 1042 593 634 626 618 610 609 601 103 144 136 128 120 119 111	58849
2269 2268 2260 2301 2293 2285 2277 1779 1778 1770 1811 1803 1795 1787 1142 1141 1133 1174 1166 1158 1150 1387 1386 1378 1419 1411 1403 1395 1044 1043 1035 1076 1068 1060 1052 603 602 594 635 627 619 611 113 112 104 145 137 129 121	
2286 2278 2270 2262 2261 2302 2294 1796 1788 1780 1772 1771 1812 1804 1159 1151 1143 1135 1134 1175 1167 1404 1396 1388 1380 1379 1420 1412 1061 1053 1045 1037 1036 1077 1069 620 612 604 596 595 636 628 130 122 114 106 105 146 138	
2401 2393 2385 2377 2369 2361 2353 882 874 866 858 850 842 834 980 972 964 956 948 940 932 1715 1707 1699 1691 1683 1675 1667 1764 1756 1748 1740 1732 1724 1716 784 776 768 760 752 744 736 49 41 33 25 17 9 1	58849
2362 2354 2395 2394 2386 2378 2370 843 835 876 875 867 859 851 941 933 974 973 965 957 949 1676 1668 1709 1708 1700 1692 1684 1725 1717 1758 1757 1749 1741 1733 745 737 778 777 769 761 753 10 2 43 42 34 26 18	58849
2379 2371 2363 2355 2396 2388 2387 860 852 844 836 877 869 868 958 950 942 934 975 967 966 1693 1685 1677 1669 1710 1702 1701 1742 1734 1726 1718 1759 1751 1750 762 754 746 738 779 771 770 27 19 11 3 44 36 35	58849
2389 2381 2380 2372 2364 2356 2397 870 862 861 853 845 837 878 968 960 959 951 943 935 976 1703 1695 1694 1686 1678 1670 1711 1752 1744 1743 1735 1727 1719 1760 772 764 763 755 747 739 780 37 29 28 20 12 4 45	58849
2357 2398 2390 2382 2374 2373 2365 838 879 871 863 855 854 846 936 977 969 961 953 952 944 1671 1712 1704 1696 1688 1687 1679 1720 1761 1753 1745 1737 1736 1728 740 781 773 765 757 756 748 5 46 38 30 22 21 13	
2367 2366 2358 2399 2391 2383 2375 848 847 839 880 872 864 856 946 945 937 978 970 962 954 1681 1680 1672 1713 1705 1697 1689 1730 1729 1721 1762 1754 1746 1738 750 749 741 782 774 766 758 15 14 6 47 39 31 23	58849
2384 2376 2368 2360 2359 2400 2392 865 857 849 841 840 881 873 963 955 947 939 938 979 971 1698 1690 1682 1674 1673 1714 1706 1747 1739 1731 1723 1722 1763 1755 767 759 751 743 742 783 775 32 24 16 8 7 48 40	
392 384 376 368 360 352 344 588 580 572 564 556 548 540 490 482 474 466 458 450 442 2205 2197 2189 2181 2173 2165 2157 2254 2246 2238 2230 2222 2214 2206 2352 2344 2336 2328 2320 2312 2304 294 286 278 270 262 254 246 2	
353 345 386 385 377 369 361 549 541 582 581 573 565 557 451 443 484 483 475 467 459 2166 2158 2199 2198 2190 2182 2174 2215 2207 2248 2247 2239 2231 2223 2313 2305 2346 2345 2337 2329 2321 255 247 288 287 279 271 263	
370 362 354 346 387 379 378 566 558 550 542 583 575 574 468 460 452 444 485 477 476 2183 2175 2167 2159 2200 2192 2191 2232 2224 2216 2208 2249 2241 2240 2330 2322 2314 2306 2347 2339 2338 272 264 256 248 289 281 280	
380 372 371 363 355 347 388 576 568 567 559 551 543 584 478 470 469 461 453 445 486 2193 2185 2184 2176 2168 2160 2201 2242 2234 2233 2225 2217 2209 2250 2340 2332 2331 2323 2315 2307 2348 282 274 273 265 257 249 290	
348 389 381 373 365 364 356 544 585 577 569 561 560 552 446 487 479 471 463 462 454 2161 2202 2194 2186 2178 2177 2169 2210 2251 2243 2235 2227 2226 2218 2308 2349 2341 2333 2325 2324 2316 250 291 283 275 267 266 258	
358 357 349 390 382 374 366 554 553 545 586 578 570 562 456 455 447 488 480 472 464 2171 2170 2162 2203 2195 2187 2179 2220 2219 2211 2252 2244 2236 2228 2318 2317 2309 2350 2342 2334 2326 260 259 251 292 284 276 268	
375 367 359 351 350 391 383 571 563 555 547 546 587 579 473 465 457 449 448 489 481 2188 2180 2172 2164 2163 2204 2196 2237 2229 2221 2213 2212 2253 2245 2335 2327 2319 2311 2310 2351 2343 277 269 261 253 252 293 285	
58849 5	18849

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2113 2119 2117 2152 2153 2155 2115 1819 1825 1823 1858 1859 1861 1821 1917 1923 1921 1956 1957 1959 1919 202 208 206 241 242 244 204 153 159 157 192 193 195 155 55 61 59 94 95 97 57 2015 2021 2019 2054 2055 20	
2146 2123 2127 2142 2143 2125 2118 1852 1829 1833 1848 1849 1831 1824 1950 1927 1931 1946 1947 1929 1922 235 212 216 231 232 214 207 186 163 167 182 183 165 158 88 65 69 84 85 67 60 2048 2025 2029 2044 2045 20	
2148 2138 2129 2136 2131 2126 2116 1854 1844 1835 1842 1837 1832 1822 1952 1942 1933 1940 1935 1930 1920 237 227 218 225 220 215 205 188 178 169 176 171 166 156 90 80 71 78 73 68 58 2050 2040 2031 2038 2033 20	
2150 2140 2134 2132 2130 2124 2114 1856 1846 1840 1838 1836 1830 1820 1954 1944 1938 1936 1934 1928 1918 239 229 223 221 219 213 203 190 180 174 172 170 164 154 92 82 76 74 72 66 56 2052 2042 2036 2034 2032 204	
2110 2120 2133 2128 2135 2144 2154 1816 1826 1839 1834 1841 1850 1860 1914 1924 1937 1932 1939 1948 1958 199 209 222 217 224 233 243 150 160 173 168 175 184 194 52 62 75 70 77 86 96 2012 2022 2035 2030 2037 24	
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496 502 500 535 536 538 498 1623 1629 1627 1662 1663 1665 1625 1427 1433 1431 1466 1467 1469 1429 692 698 696 731 732 734 694 643 649 647 682 683 685 645 1525 1531 1529 1564 1565 1567 1527 1868 1874 1872 1907 1908 1	
529 506 510 525 526 508 501 1656 1633 1637 1652 1653 1635 1625 1625 1625 1635 1625 1625 1635 1625 1625 1635 1625 1625 1635 1625 1625 1635 1635 1625 1625 1635 1635 1625 1625 1635 1635 1625 1625 1635 1635 1625 1625 1635 1635 1625 1635 1635 1635 1635 1635 1635 1635 163	
521 521 512 519 514 509 499 1658 1648 1639 1646 1641 1636 1626 1462 1452 1443 1450 1445 1440 1430 727 717 708 715 710 705 695 678 668 659 666 661 656 646 1560 1550 1541 1548 1543 1538 1528 1903 1893 1884 1891 1886 1	
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493 503 516 511 518 527 537 1620 1630 1643 1638 1645 1654 1664 1424 1434 1447 1442 1449 1458 1468 689 699 712 707 714 723 733 640 650 663 658 665 674 684 1522 1532 1545 1540 1547 1556 1566 1865 1875 1888 1883 1890 18	
491 522 520 505 504 524 539 1618 1649 1647 1632 1631 1651 1666 1422 1453 1451 1436 1435 1455 1470 687 718 716 701 700 720 735 638 669 667 652 651 671 686 1520 1551 1549 1534 1533 1553 1568 1863 1894 1892 1877 1876 18	
532 528 530 495 494 492 534 1659 1655 1657 1622 1621 1619 1661 1463 1459 1461 1426 1425 1423 1465 728 724 726 691 690 688 730 679 675 677 642 641 639 681 1561 1557 1559 1524 1523 1521 1563 1904 1900 1902 1867 1866 18	
398 404 402 437 438 440 400 888 894 892 927 928 930 890 1329 1335 1333 1368 1369 1371 1331 986 992 990 1025 1026 1028 988 1231 1237 1235 1270 1271 1273 1233 1476 1482 1480 1515 1516 1518 1478 1966 1972 1970 2005 2006 20	
431 408 412 427 428 410 403 921 898 902 917 918 900 893 1362 1339 1343 1358 1359 1341 1334 1019 996 1000 1015 1016 998 991 1264 1241 1245 1260 1261 1243 1236 1509 1486 1490 1505 1506 1488 1481 1999 1976 1980 1995 1996 19	
433 423 414 421 416 411 401 923 913 904 911 906 901 891 1364 1354 1352 1347 1342 1332 1021 1011 1002 1009 1004 999 989 1266 1256 1247 1254 1249 1244 1234 1511 1501 1492 1499 1494 1489 1479 2001 1991 1982 1989 1984 19	
435 425 419 417 415 409 399 925 915 909 907 905 899 889 1366 1356 1350 1348 1346 1340 1330 1023 1013 1007 1005 1003 997 987 1268 1252 1250 1248 1242 1232 1513 1503 1497 1495 1493 1487 1477 2003 1993 1987 1985 1983 198	
395 405 418 413 420 429 439 885 895 908 903 910 919 929 1326 1336 1349 1344 1351 1360 1370 983 993 1006 1001 1008 1017 1027 1228 1238 1251 1246 1253 1262 1272 1473 1483 1496 1491 1498 1507 1517 1963 1973 1986 1981 1988 1981 1988 1981 1988 1981 1988 1981 1988 1981 1988 1981 19	
393 424 422 407 406 426 441 883 914 912 897 896 916 931 1324 1355 1353 1338 1337 1357 1372 981 1012 1010 995 994 1014 1029 1226 1257 1255 1240 1239 1259 1274 1471 1502 1500 1485 1484 1504 1519 1961 1992 1990 1975 1974 197 434 430 432 397 396 394 436 924 920 922 887 886 884 926 1365 1361 1363 1328 1327 1325 1367 1022 1018 1020 985 984 982 1024 1267 1263 1265 1230 1229 1227 1269 1512 1508 1510 1475 1474 1472 1514 2002 1998 2000 1965 1964 19	
300 306 304 339 340 342 302 790 796 794 829 830 832 792 1084 1090 1088 1123 1124 1126 1086 1182 1188 1186 1221 1222 1224 1184 1280 1286 1284 1319 1320 1322 1282 1574 1580 1578 1613 1614 1616 1576 2064 2070 2068 2103 2104 2	
333 310 314 329 330 312 305 823 800 804 819 820 802 795 1117 1094 1098 1113 1114 1096 1089 1215 1192 1196 1211 1212 1194 1187 1313 1290 1294 1309 1310 1292 1285 1607 1584 1588 1603 1604 1586 1579 2097 2074 2078 2093 2094 20	
335 325 316 323 318 313 303 825 815 806 813 808 803 793 1119 1109 1100 1107 1102 1097 1087 1217 1207 1198 1205 1200 1195 1185 1315 1305 1296 1303 1298 1293 1283 1609 1599 1590 1597 1592 1587 1577 2099 2089 2080 2087 2082 2087 2082 2087 2082 2087 2082 2087 2082 2087 2082 2087 2087	
337 327 321 319 317 311 301 827 817 811 809 807 801 791 1121 1111 1105 1103 1101 1095 1085 1219 1209 1203 1201 1199 1193 1183 1317 1307 1301 1299 1297 1291 1281 1611 1601 1595 1593 1591 1585 1575 2101 2091 2085 2083 2081 20	
297 307 320 315 322 331 341 787 797 810 805 812 821 831 1081 1091 1104 1099 1106 1115 1125 1179 1189 1202 1197 1204 1213 1223 1277 1287 1300 1295 1302 1311 1321 1571 1581 1594 1589 1596 1605 1615 2061 2071 2084 2079 2086 20	
295 326 324 309 308 328 343 785 816 814 799 798 818 833 1079 1110 1108 1093 1092 1112 1127 1177 1208 1206 1191 1190 1210 1225 1275 1306 1304 1289 1288 1308 1323 1569 1600 1598 1583 1582 1602 1617 2059 2090 2088 2073 2072 2010 2010 2010 2010 2010 2010 2010	
336 332 334 299 298 296 338 826 822 824 789 788 786 828 1120 1116 1118 1083 1082 1080 1122 1218 1214 1216 1181 1180 1178 1220 1316 1312 1314 1279 1278 1276 1318 1610 1606 1608 1573 1572 1570 1612 2100 2096 2098 2063 2062 20	
2293 2270 2274 2289 2290 2272 2265 1803 1780 1784 1799 1800 1782 1775 1166 1143 1147 1162 1163 1145 1138 1411 1388 1392 1407 1408 1390 1383 1068 1045 1049 1064 1065 1047 1040 627 604 608 623 624 606 599 137 114 118 133 134 1	
2295 2285 2276 2283 2278 2273 2263 1805 1795 1786 1793 1788 1783 1773 1168 1158 1149 1156 1151 1146 1136 1413 1403 1394 1401 1396 1391 1381 1070 1060 1051 1058 1053 1048 1038 629 619 610 617 612 607 597 139 129 120 127 122 1	
	15 105 58849
	35 145 58849
2255 2286 2284 2269 2268 2288 2303 1765 1796 1794 1779 1778 1798 1813 1128 1159 1157 1142 1141 1161 1176 1373 1404 1402 1387 1386 1406 1421 1030 1061 1059 1044 1043 1063 1078 589 620 618 603 602 622 637 99 130 128 113 112 1	
2296 2292 2294 2259 2258 2256 2298 1806 1802 1804 1769 1768 1766 1808 1169 1165 1167 1132 1131 1129 1171 1414 1410 1412 1377 1376 1374 1416 1071 1067 1069 1034 1033 1031 1073 630 626 628 593 592 590 632 140 136 138 103 102 1	
2358 2364 2362 2397 2398 2400 2360 839 845 843 878 879 881 841 937 943 941 976 977 979 939 1672 1678 1676 1711 1712 1714 1674 1721 1725 1760 1761 1763 1723 741 747 745 780 781 783 743 6 12 10 45 46	
2391 2368 2372 2387 2388 2370 2363 872 849 853 868 869 851 844 970 947 951 966 967 949 942 1705 1682 1686 1701 1702 1684 1677 1754 1731 1735 1750 1751 1733 1726 774 751 755 770 771 753 746 39 16 20 35 36	
2393 2383 2374 2381 2376 2371 2361 874 864 855 862 857 852 842 972 962 953 960 955 950 940 1707 1697 1688 1695 1690 1685 1675 1756 1746 1737 1744 1739 1734 1724 776 766 757 764 759 754 744 41 31 22 29 24	
2395 2385 2379 2377 2375 2369 2359 876 866 860 858 856 850 840 974 964 958 956 954 948 938 1709 1699 1693 1691 1689 1683 1673 1758 1742 1740 1738 1732 1722 778 768 762 760 758 752 742 43 33 27 25 23	
2355 2365 2378 2373 2380 2389 2399 836 846 859 854 861 870 880 934 944 957 952 959 968 978 1669 1679 1692 1687 1694 1703 1713 1718 1728 1741 1736 1743 1752 1762 738 748 761 756 763 772 782 3 13 26 21 28	
2353 2384 2382 2367 2366 2386 2401 834 865 863 848 847 867 882 932 963 961 946 945 965 980 1667 1698 1696 1681 1680 1700 1715 1716 1747 1745 1730 1729 1749 1764 736 767 765 750 749 769 784 1 32 30 15 14	
2394 2390 2392 2357 2356 2354 2396 875 871 873 838 837 835 877 973 969 971 936 935 933 975 1708 1704 1706 1671 1670 1668 1710 1757 1753 1755 1720 1719 1717 1759 777 773 775 740 739 737 779 42 38 40 5 4	
349 355 353 388 389 391 351 545 551 549 584 585 587 547 447 453 451 486 487 489 449 2162 2168 2166 2201 2202 2204 2164 2211 2217 2215 2250 2251 2253 2213 2309 2315 2313 2348 2349 2351 2311 251 257 255 290 291 2	
382 359 363 378 379 361 354 578 555 559 574 575 557 550 480 457 461 476 477 459 452 2195 2172 2176 2191 2192 2174 2167 2244 2221 2225 2240 2241 2223 2216 2342 2319 2323 2338 2339 2321 2314 284 261 265 280 281 2	
384 374 365 372 367 362 352 580 570 561 568 563 558 548 482 472 463 470 465 460 450 2197 2187 2178 2185 2180 2175 2165 2246 2236 2227 2234 2229 2224 2214 2344 2334 2325 2332 2327 2322 2312 286 276 267 274 269 2	
386 376 370 368 366 360 350 582 572 566 564 562 556 546 484 474 468 466 464 458 448 2199 2189 2183 2181 2179 2173 2163 2248 2232 2230 2228 2222 212 2346 2330 2328 2326 2320 2310 288 278 272 270 268 2	
346 356 369 364 371 380 390 542 552 565 560 567 576 586 444 454 467 462 469 478 488 2159 2169 2182 2177 2184 2193 2203 2208 2218 2231 2226 2233 2242 2252 2306 2316 2329 2324 2331 2340 2350 248 258 271 266 273 2	
344 375 373 358 357 377 392 540 571 569 554 553 573 588 442 473 471 456 455 475 490 2157 2188 2186 2171 2170 2190 2205 2206 2237 2235 2220 2219 2239 2254 2304 2335 2333 2318 2317 2337 2352 246 277 275 260 259 2	
385 381 383 348 347 345 387 581 577 579 544 543 541 583 483 479 481 446 445 443 485 2198 2194 2196 2161 2160 2158 2200 2247 2243 2245 2210 2209 2207 2249 2345 2341 2343 2308 2307 2305 2347 287 283 285 250 249 2	
58849 5	849 58849 58849

Above two magic squares of order 49 formed by blocks of magic squares of order 7 are with sequential entries:

 $D_{40\times 40} := \{1, 2, \dots, 2400, 2401\}.$

These four magic squares are bordered magic squares with border made by pandiagonal and bordered magic squares of order 5. If you remove the external borders, still we are left with magic squares of lower orders. Let's see how it works.

Magic Squares of Order 35 2.2

These magic squares are obtained from above by the application of the formula $\frac{a^2-b^2}{2}$, a > b. Removing the external border of order 7 and then subtracting $\frac{49^2 - 35^2}{2} := 588$ from magic squares of orders 49, we get magic squares of order 35 given by

35																																				21455
	1078	1070	1062	1054	1046	1038	1030	882	874	866	858	850	842	834	147	139	131	123	115	107	99	98	90	82	74	66	58	50	980	972	964	956	948	940	932	21455
	1039	1031	1072	1071	1063	1055	1047	843	835	876	875	867	859	851	108	100	141	140	132	124	116	59	51	92	91	83	75	67	941	933	974	973	965	957	949	21455
	1056	1048	1040	1032	1073	1065	1064	860	852	844	836	877	869	868	125	117	109	101	142	134	133	76	68	60	52	93	85	84	958	950	942	934	975	967	966	21455
	1066	1058	1057	1049	1041	1033	1074	870	862	861	853	845	837	878	135	127	126	118	110	102	143	86	78	77	69	61	53	94	968	960	959	951	943	935	976	21455
	1034	1075	1067	1059	1051	1050	1042	838	879	871	863	855	854	846	103	144	136	128	120	119	111	54	95	87	79	71	70	62	936	977	969	961	953	952	944	21455
	1044	1043	1035	1076	1068	1060	1052	848	847	839	880	872	864	856	113	112	104	145	137	129	121	64	63	55	96	88	80	72	946	945	937	978	970	962	954	21455
	1061	1053	1045	1037	1036	1077	1069	865	857	849	841	840	881	873	130	122	114	106	105	146	138	81	73	65	57	56	97	89	963	955	947	939	938	979	971	21455
	343	335	327	319	311	303	295	784	776	768	760	752	744	736	441	433	425	417	409	401	393	686	678	670	662	654	646	638	931	923	915	907	899	891	883	21455
	304	296	337	336	328	320	312	745	737	778	777	769	761	753	402	394	435	434	426	418	410	647	639	680	679	671	663	655	892	884	925	924	916	908	900	21455
	321	313	305	297	338	330	329	762	754	746	738	779	771	770	419	411	403	395	436	428	427	664	656	648	640	681	673	672	909	901	893	885	926	918	917	21455
	331	323	322	314	306	298	339	772	764	763	755	747	739	780	429	421	420	412	404	396	437	674	666	665	657	649	641	682	919	911	910	902	894	886	927	21455
	299	340	332	324	316	315	307	740	781	773	765	757	756	748	397	438	430	422	414	413	405	642	683	675	667	659	658	650	887	928	920	912	904	903	895	21455
	309	308	300	341	333	325	317	750	749	741	782	774	766	758	407	406	398	439	431	423	415	652	651	643	684	676	668	660	897	896	888	929	921	913	905	21455
	326	318	310	302	301	342	334	767	759	751	743	742	783	775	424	416	408	400	399	440	432	669	661	653	645	644	685	677	914	906	898	890	889	930	922	21455
	245	237	229	221	213	205	197	539	531	523	515	507	499	491	637	629	621	613	605	597	589	735	727	719	711	703	695	687	1029	1021	1013	1005	997	989	981	21455
	206	198	239	238	230	222	214	500	492	533	532	524	516	508	598	590	631	630	622	614	606	696	688	729	728	720	712	704	990	982	1023	1022	1014	1006	998	21455
	223	215	207	199	240	232	231	517	509	501	493	534	526	525	615	607	599	591	632	624	623	713	705	697	689	730	722	721	1007	999	991	983	1024	1016	1015	21455
	233	225	224	216	208	200	241	527	519	518	510	502	494	535	625	617	616	608	600	592	633	723	715	714	706	698	690	731	1017	1009	1008	1000	992	984	1025	21455
	201	242	234	226	218	217	209	495	536	528	520	512	511	503	593	634	626	618	610	609	601	691	732	724	716	708	707	699	985	1026	1018	1010	1002	1001	993	21455
	211														603			635	627	619												1027	1019	1011	1003	21455
															620															1004	996	988	987	1028	1020	21455
															833			809	801		785								49	41	33	25	17	9		21455
															794			826	818		802						467	459	10	2	43	42	34	26		21455
															811			787	828		819					485	477	476	27	19	11	3	44	36		21455
															821											453			37	29	28	20	12	4		21455
															789					805								454	5	46	38	30	22	21		21455
															799			831	823		807					480			15	14	6	47	39	31	23	
															816															24	16	8	7	48		21455
																																		156		
																																		173		
															1105																				182	
																																		151		
	250														1083																			168 179	160 170	
															1093																				170 187	
																																		195		
	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21400	21455	21400	21422

35																																			21455
1035	1041	1039	1074	1075	1077	1037	839	845	843	878	879	881 8	41 1	04	110	108	143	144	146	106	55	61	59	94	95	97	57	937	943	941	976	977	979	939	21455
1068	1045	1049	1064	1065	1047	1040	872	849	853	868	869	851 8	44 1	37 [114	118	133	134	116	109	88	65	69	84	85	67	60	970	947	951	966	967	949	942	21455
1070	1060	1051	1058	1053	1048	1038	874	864	855	862	857 8	352 8	42 1	39	129	120	127	122	117	107	90	80	71	78	73	68	58	972	962	953	960	955	950	940	21455
1072	1062	1056	1054	1052	1046	1036	876	866	860	858	856 8	850 8	40 1	41	131	125	123	121	115	105	92	82	76	74	72	66	56	974	964	958	956	954	948	938	21455
1032	1042	1055	1050	1057	1066	1076	836	846	859	854	861 8	370 8	80 1	01	111	124	119	126	135	145	52	62	75	70	77	86	96	934	944	957	952	959	968	978	21455
1030	1061	1059	1044	1043	1063	1078	834	865	863	848	847 8	367 8	82 9	9	130	128	113	112	132	147	50	81	79	64	63	83	98	932	963	961	946	945	965	980	21455
1071	1067	1069	1034	1033	1031	1073	875	871	873	838	837 8	335 8	77 14	40	136	138	103	102	100	142	91	87	89	54	53	51	93	973	969	971	936	935	933	975	21455
300	306	304	339	340	342	302	741	747	745	780	781	783 7	43 3	98	404	402	437	438	440	400	643	649	647	682	683	685	645	888	894	892	927	928	930	890	21455
333	310	314	329	330	312	305	774	751	755	770	771	753 7	46 4	31	408	412	427	428	410	403	676	653	657	672	673	655	648	921	898	902	917	918	900	893	21455
335	325	316	323	318	313	303	776	766	757	764	759	754 7	44 4	33	423	414	421	416	411	401	678	668	659	666	661	656	646	923	913	904	911	906	901	891	21455
337	327	321	319	317	311	301	778	768	762	760	758	752 7	42 4	35	425	419	417	415	409	399	680	670	664	662	660	654	644	925	915	909	907	905	899	889	21455
297	307	320	315	322	331	341	738	748	761	756	763	772 7	82 3	95	405	418	413	420	429	439	640	650	663	658	665	674	684	885	895	908	903	910	919	929	21455
295	326	324	309	308	328	343	736	767	765	750	749	769 7	84 3	93	424	422	407	406	426	441	638	669	667	652	651	671	686	883	914	912	897	896	916	931	21455
336	332	334	299	298	296	338	777	773	775	740	739	737 7	79 4	34	430	432	397	396	394	436	679	675	677	642	641	639	681	924	920	922	887	886	884	926	21455
202	208	206	241	242	244	204	496	502	500	535	536 !	538 4	98 5	94 _	600	598	633	634	636	596	692	698	696	731	732	734	694	986	992	990	1025	1026	1028	988	21455
235	212	216	231	232	214	207	529	506	510	525	526 !	508 5	01 6	27	604	608	623	624	606	599	725	702	706	721	722	704	697	1019	996	1000	1015	1016	998	991	21455
237	227	218	225	220	215	205	531	521	512	519	514	509 4	99 6	29	619	610	617	612	607	597	727	717	708	715	710	705	695	1021	1011	1002	1009	1004	999	989	21455
239	229	223	221	219	213	203	533	523	517	515	513	507 4	97 6	31	621	615	613	611	605	595	729	719	713	711	709	703	693	1023	1013	1007	1005	1003	997	987	21455
199	209	222	217	224	233	243	493	503	516	511	518	527 5	37 5	91	601	614	609	616	625	635	689	699	712	707	714	723	733	983	993	1006	1001	1008	1017	1027	21455
197	228	226	211	210	230	245	491	522	520	505	504 !	524 5	39 5	89	620	618	603	602	622	637	687	718	716	701	700	720	735	981	1012	1010	995	994	1014	1029	21455
238	234	236	201	200	198	240	532	528	530	495	494 4	492 5	34 6	30	626	628	593	592	590	632	728	724	726	691	690	688	730	1022	1018	1020	985	984	982	1024	21455
1182	1188	1186	1221	1222	1224	1184	545	551	549	584	585 !	587 5	47 7	90 _	796	794	829	830	832	792	447	453	451	486	487	489	449	6	12	10	45	46	48	8	21455
1215					-													820	802	795	480	457	461	476	477	459	452	39	16	20	35	36	18	11	21455
1217	1207	1198	1205	1200	1195	1185	580	570	561	568	563	558 5	48 8	25	815	806	813	808	803	793	482	472	463	470	465	460	450	41	31	22	29	24	19	9	21455
					1193												809	807	801	791	484	474	468	466	464	458	448	43	33	27	25	23	17	7	21455
1179	1189	1202	1197	1204	1213	1223	542	552	565	560	567	576 5	86 7	87	797	810	805	812	821	831	444	454	467	462	469	478	488	3	13	26	21	28	37	47	21455
1177	1208	1206	1191	1190	1210	1225	540	571	569	554	553 9	573 5	88 7	85	816	814	799	798	818	833	442	473	471	456	455	475	490	1	32	30	15	14	34	49	21455
					1178														786				481			443		42	38	40	5	4	2		21455
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21455	21455	21455	21455	21455	21455	21455	21455	5 21455	21455	21455	21455 2	1455 21	455 21	455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455

Above two magic squares of order 35 formed by blocks of magic squares of order 7 are with distributions

 $D_{30\times 30} := \{1, 2, \dots, 1224, 1225\}$

2.3 Magic Squares of Order 28

These magic squares are obtained from above by the application of the formula $\frac{a^2 - b^2}{2}$, a > b. Removing the external border of order 7 and then subtracting $\frac{42^2 - 28^2}{2} := 490$ from magic squares of orders 42, we get magic squares of order 28 given by

	pan	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990
1099	343	335	327	319	311	303	295	588	580	572	564	556	548	540	49	41	33	25	17	9	1	686	678	670	662	654	646	638	10990
1099	304	296	337	336	328	320	312	549	541	582	581	573	565	557	10	2	43	42	34	26	18	647	639	680	679	671	663	655	10990
1099	321	313	305	297	338	330	329	566	558	550	542	583	575	574	27	19	11	3	44	36	35	664	656	648	640	681	673	672	10990
1099	331	323	322	314	306	298	339	576	568	567	559	551	543	584	37	29	28	20	12	4	45	674	666	665	657	649	641	682	10990
1099	299	340	332	324	316	315	307	544	585	577	569	561	560	552	5	46	38	30	22	21	13	642	683	675	667	659	658	650	10990
1099	309	308	300	341	333	325	317	554	553	545	586	578	570	562	15	14	6	47	39	31	23	652	651	643	684	676	668	660	10990
1099	326	318	310	302	301	342	334	571	563	555	547	546	587	579	32	24	16	8	7	48	40	669	661	653	645	644	685	677	10990
1099	98	90	82	74	66	58	50	637	629	621	613	605	597	589	392	384	376	368	360	352	344	539	531	523	515	507	499	491	10990
1099	59	51	92	91	83	75	67	598	590	631	630	622	614	606	353	345	386	385	377	369	361	500	492	533	532	524	516	508	10990
1099	76	68	60	52	93	85														379									
1099	86	78	77	69	61	53														347									
1099		95	87	79	71	70														364									
1099		63	55	96	88	80														374									
1099	¥	73	65	57	56	97														391									
~	784																												10990
~	745																												10990
	762						770																						
~	772																												
~	740																												
~	750																												10990
~	441																												10990
~	402																												10990
~	419																									191			10990
~	429																												10990
~	397																								177				10990
~	407																												10990
	4						432																						10990
28	10990																												<

300	306	304	339	340	342	302	545	551	549	584	585	587	547	6	12	10	45	46	48	8	643	649	647	682	683	685	645
333	310	314	329	330	312	305	578	555	559	574	575	557	550	39	16	20	35	36	18	11	676	653	657	672	673	655	648
335	325	316	323	318	313	303	580	570	561	568	563	558	548	41	31	22	29	24	19	9	678	668	659	666	661	656	646
337	327	321	319	317	311	301	582	572	566	564	562	556	546	43	33	27	25	23	17	7	680	670	664	662	660	654	644
297	307	320	315	322	331	341	542	552	565	560	567	576	586	3	13	26	21	28	37	47	640	650	663	658	665	674	684
295	326	324	309	308	328	343	540	571	569	554	553	573	588	1	32	30	15	14	34	49	638	669	667	652	651	671	686
336	332	334	299	298	296	338	581	577	579	544	543	541	583	42	38	40	5	4	2	44	679	675	677	642	641	639	681
55	61	59	94	95	97	57	594	600	598	633	634	636	596	349	355	353	388	389	391	351	496	502	500	535	536	538	498
88	65	69	84	85	67	60	627	604	608	623	624	606	599	382	359	363	378	379	361	354	529	506	510	525	526	508	501
90	80	71	78	73	68	58	629	619	610	617	612	607	597	384	374	365	372	367	362	352	531	521	512	519	514	509	499
92	82	76	74	72	66	56	631	621	615	613	611	605	595	386	376	370	368	366	360	350	533	523	517	515	513	507	497
52	62	75	70	77	86	96	591	601	614	609	616	625	635	346	356	369	364	371	380	390	493	503	516	511	518	527	537
50	81	79	64	63	83	98	589	620	618	603	602	622	637	344	375	373	358	357	377	392	491	522	520	505	504	524	539
91	87	89	54	53	51	93	630	626	628	593	592	590	632	385	381	383	348	347	345	387	532	528	530	495	494	492	534
741	747	745	780	781	783	743	104	110	108	143	144	146	106	447	453	451	486	487	489	449	202	208	206	241	242	244	204
774	751	755	770	771	753	746	137	114	118	133	134	116	109	480	457	461	476	477	459	452	235	212	216	231	232	214	207
776	766	757	764	759	754	744	139	129	120	127	122	117	107	482	472	463	470	465	460	450	237	227	218	225	220	215	205
778	768	762	760	758	752	742	141	131	125	123	121	115	105	484	474	468	466	464	458	448	239	229	223	221	219	213	203
738	748	761	756	763	772	782	101	111	124	119	126	135	145	444	454	467	462	469	478	488	199	209	222	217	224	233	243
736	767	765	750	749	769	784	99	130	128	113	112	132	147	442	473	471	456	455	475	490	197	228	226	211	210	230	245
777	773	775	740	739	737	779	140	136	138	103	102	100	142	483	479	481	446	445	443	485	238	234	236	201	200	198	240
398	404	402	437	438	440	400	251	257	255	290	291	293	253	692	698	696	731	732	734	694	153	159	157	192	193	195	155
431	408	412	427	428	410	403	284	261	265	280	281	263	256	725	702	706	721	722	704	697	186	163	167	182	183	165	158
433	423	414	421	416	411	401	286	276	267	274	269	264	254	727	717	708	715	710	705	695	188	178	169	176	171	166	156
435	425	419	417	415	409	399	288	278	272	270	268	262	252	729	719	713	711	709	703	693	190	180	174	172	170	164	154
395	405	418	413	420	429	439	248	258	271	266	273	282	292	689	699	712	707	714	723	733	150	160	173	168	175	184	194
393	424	422	407	406	426	441	246	277	275	260	259	279	294	687	718	716	701	700	720	735	148	179	177	162	161	181	196
434	430	432	397	396	394	436	287	283	285	250	249	247	289	728	724	726	691	690	688	730	189	185	187	152	151	149	191
10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990

Above two magic squares of order 28 formed by blocks of magic squares of order 7 are with sequential entries:

 $D_{25\times 25} := \{1, 2, \dots, 783, 784\}$

2.4 Magic Squares of Order 21

These magic squares are obtained from above by the application of the formula $\frac{a^2 - b^2}{2}$, a > b. Removing the external border of order 7 and then subtracting $\frac{35^2 - 21^2}{2} := 392$ from magic squares of orders 35, we get magic squares of order 21 given by

21																						4641
	392	384	376	368	360	352	344	49	41	33	25	17	9	1	294	286	278	270	262	254	246	4641
	353	345	386	385	377	369	361	10	2	43	42	34	26	18	255	247	288	287	279	271	263	4641
	370	362	354	346	387	379	378	27	19	11	3	44	36	35	272	264	256	248	289	281	280	4641
	380	372	371	363	355	347	388	37	29	28	20	12	4	45	282	274	273	265	257	249	290	4641
	348	389	381	373	365	364	356	5	46	38	30	22	21	13	250	291	283	275	267	266	258	4641
						374		15	14	6	47	39	31	23			251					
						391		32	24	16	8	7	48	40			261					
	147				115	107	99			229				197			327			303		
	108	100	141	140	132	124	116			239												4641
	125	117	109		142		133			207							305					
	135	127		118 128	110	102 119	143 111			224 234							322			298 315		
	105		104		120		121			202												4641
		122	114			146				212										342		
	196	188	180		164					425					98	90	82	74	66	58	50	4641
	157		190	189	181	173	165			435				410	59	51	92	91	83	75	67	4641
	174	166	158	150	191	183	182	419	411	403	395	436	428	427	76	68	60	52	93	85	84	4641
	184	176	175	167	159	151	192	429	421	420	412	404	396	437	86	78	77	69	61	53	94	4641
	152	193	185	177	169	168	160	397	438	430	422	414	413	405	54	95	87	79	71	70	62	4641
	162	161	153	194	186	178	170	407	406	398	439	431	423	415	64	63	55	96	88	80	72	4641
	179	171	163	155	154	195	187	424	416	408	400	399	440	432	81	73	65	57	56	97	89	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

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21																						4641
	349	355	353	388	389	391	351	6	12	10	45	46	48	8	251	257	255	290	291	293	253	4641
	382	359	363	378	379	361	354	39	16	20	35	36	18	11	284	261	265	280	281	263	256	4641
	384	374	365	372	367	362	352	41	31	22	29	24	19	9	286	276	267	274	269	264	254	4641
	386	376	370	368	366	360	350	43	33	27	25	23	17	7	288	278	272	270	268	262	252	4641
	346	356	369	364	371	380	390	3	13	26	21	28	37	47	248	258	271	266	273	282	292	4641
	344	375	373	358	357	377	392	1	32	30	15	14	34	49	246	277	275	260	259	279	294	4641
	385	381	383	348	347	345	387	42	38	40	5	4	2	44	287	283	285	250	249	247	289	4641
	104	110	108	143	144	146	106	202	208	206	241	242	244	204	300	306	304	339	340	342	302	4641
	137	114	118	133	134	116	109	235	212			232	1								305	4641
	139	129	120	127	122	117	107	237	227	218	225	220	215	205	335	325	316	323	318	313	303	4641
	141	131			121	115	105					219									301	4641
	101	111	124	119	126	135	145					224	J								341	4641
	99	130	128	113	112	132	147	197	228	226	211	210	230	245	295	326	324	309	308	328	343	4641
	140	136	138	103	102	100	142					200			336	332	334	299	298	296	338	4641
	153	159	157			195	155	398				438	440	400	55	61	59	94	95	97	57	4641
	186	163	167	182	183	1	158	431				428	410	403	88	65	69	84	85	67	60	4641
	188	178	169	176	171	166	156	433	423	414	421	416	411	401	90	80	71	78	73	68	58	4641
	190	180	174	172	170	164	154	435	425	419	417	415	409	399	92	82	76	74	72	66	56	4641
	150	160	173	168	175	184	194	395	405	418	413	420	429	439	52	62	75	70	77	86	96	4641
	148	179	177	162	161	181	196	393	424	422	407	406	426	441	50	81	79	64	63	83	98	4641
	189	185	187	152	151	149	191	434	430	432	397	396	394	436	91	87	89	54	53	51	93	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

Above two magic squares of order 21 formed by blocks of magic squares of order 7 are with sequential entries:

 $D_{20\times 20} := \{1, 2, \dots, 440, 441\}$

Pandiagonal Magic Squares Multiples 7 3

This section brings pandiagonal magic squares multiples 7. It includes magic squares of orders 21, 28, 35 and 49. The details are excluded as these are studied extensively in author's previous works [5, 7, 20].

Pandiagonal Magic Square of Order 21 3.1

Below is a **pandiagonal** magic squares of order 21.

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		140	M	M	M	M	140	140	140	140	140	140	140	4641	M	140	M	M	M	M	140	164
20	1 pun		/	/				<u> </u>	/	/	/	/	/		<u> </u>	/	/					ſ
4641	1						397							398								
``														263								
``														150								4641
$\langle \rangle$							13													388		4641
4641	386	12	118											362					252	254	361	4641
		358		-			249	272	360	383	7	116	161	248	273	359	382	9	115	162	247	4641
4641	159	244	270	376	379	6	113	158	245	269	377	381	5	112	157	246	268	378	380	4	114	4641
4641	43	90	134	222	286	354	418	45	89	133	221	287	353	419	44	88	135	220	288	352	420	4641
4641	349	417	61	85	132	218	285	350	416	62	87	131	217	284	351	415	63	86	130	219	283	4641
4641	216	281	348	412	60	103	127	215	280	347	413	59	104	129	214	282	346	414	58	105	128	4641
4641	102	145	211	279	344	411	55	101	146	213	278	343	410	56	100	147	212	277	345	409	57	4641
4641	407	54	97	144	229	274	342	406	53	98	143	230	276	341	408	52	99	142	231	275	340	4641
4641	292	337	405	50	96	139	228	293	339	404	49	95	140	227	294	338	403	51	94	141	226	4641
4641	138	223	291	355	400	48	92	137	224	290	356	402	47	91	136	225	289	357	401	46	93	4641
4641	22	69	176	201	307	333	439	24	68	175	200	308	332	440	23	67	177	199	309	331	441	4641
4641	328	438	40	64	174	197	306	329	437	41	66	173	196	305	330	436	42	65	172	198	304	4641
4641	195	302	327	433	39	82	169	194	301	326	434	38	83	171	193	303	325	435	37	84	170	4641
4641							34					322			79	189	191	298	324	430	36	4641
$\langle \rangle$	428		76											320						296		4641
		316												206					73		205	
.0.1		202				27	71	179				423		70							72	4641
		4641		4641		4641		4641										4641		4641	4641	L
	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041	4041

The blocks of order 7 are of **equal sums** magic squares, i.e., $M_{7\times7} := 1547$

3.2 Pandiagonal Magic Square of Order 28

Below is a **pandiagonal** magic squares of order 28.

~ `	343	/		/					1,0770	10/10	1,0770	10990	1,0990	10990	1,0990	10990	1,0990	1,0770	1,0770	1,0770	1,0770	1,0110	1,0770	1,0770	1,0770	1,0770	1,07990	10990	10990
10990	•	222	327	319	311	303		<u> </u>		/		/	/				33	25	17	9	$ \sim $		/	/	662	~			<u>r</u>
	304	296	337	336	328	320	312	549	541	582	581	573	565	557	10	2	43	42	34	26	18	647	639	680	679	671	663	655	10990
10990	321	313	305	297	338	330	329	566	558	550	542	583	575	574	27	19	11	3	44	36	35	664	656	648	640	681	673	672	10990
10990	331	323	322	314	306	298	339	576	568	567	559	551	543	584	37	29	28	20	12	4	45	674	666	665	657	649	641	682	10990
10990	299	340	332	324	316	315	307	544	585	577	569	561	560	552	5	46	38	30	22	21	13	642	683	675	667	659	658	650	10990
10990	309	308	300	341	333	325	317	554	553	545	586	578	570	562	15	14	6	47	39	31	23	652	651	643	684	676	668	660	10990
10990	326	318	310	302	301	342	334	571	563	555	547	546	587	579	32	24	16	8	7	48	40	669	661	653	645	644	685	677	10990
10990	98	90	82	74	66	58	50	637	629	621	613	605	597	589	392	384	376	368	360	352	344	539	531	523	515	507	499	491	10990
10990	59	51	92	91	83	75	67	598	590	631	630	622	614	606	353	345	386	385	377	369	361	500	492	533	532	524	516	508	10990
10990	76	68	60	52	93	85														379									
10990	86	78	77	69	61	53	94	625	617	616	608	600	592	633	380	372	371	363	355	347	388	527	519	518	510	502	494	535	10990
10990	54	95	87	79	71	70														364									
10990	64	63	55	96	88	80														374									
10990		73	65	57	56	97														391									-
10990	784																			450									
\sim	745																												
\sim	762																			477									
~ `	772																												
	740																			462									
~ `	750 767																												
~ `	441																												-
\sim	402																									181			
$\langle \rangle$	419																									191			
\sim	429																												
	397																												
~ `	407																												
	1																			734					155				
28	10990																												· · · · ·

The blocks of order 7 are with **different sums** pandiagonal magic squares. It is the same magic square given in previous section.

3.3 Pandiagonal Magic Square of Order 35

Below is a **pandiagonal** magic squares of order 35.

	Dab	21455	91455	21/155	21/155	91455	21/155	91455	91455	91455	91455	21455	21455	21455	21/155	91455	91455	91455	21455	91455	91455	91455	91455	21455	21455	91455	21455	91455	21455	91455	21455	91455	21455	91455	21455 21455
27455	901			1081			109	685		1189		469	1	937	73							-					1045			793					325 21455
21455		118	879	656		1058		14	911	692	195	1161	839		1001			213	497	610	718		555				407	47			1095		373	151	950 21455
21455		848	451	130	888	634	271	811	489	24	924	666		1175				1141	99	243	493			1027			1206					343			382 21455
21455	643	249	1076		428	136	900		1182		461	34	934	679		523	598	707		1138	_	1220		394	70			282		360		968	571		1113 21455
21455	113	906	655	258	1054	866	439	944	689	189	1156	832	475	6	1135	88	231	519	628	703	987	547	292	1192	765	401	44	1050	326	1090	798	367	150	977	583 21455
21455	844	446	124	883	661	270	1063	482	20	916	699	199	1169	806	733	983	1127	85	228	511	624	51	1024	560	302	1202	737	415	955	592	338	1096	775	378	157 21455
21455	276	1075	853	424	131	894	638	1179	819	456	27	930	671	209	508	616	729	1013	1123	77	225	747	387	65	1031	534	315	1212	355	168	962	570	347	1108	781 21455
21455	283	1197	750	403	56	1044	558	1094	805	372	152	947	590	331	907	653	256	1055	868	437	115	691	194	1163	836	480	13	914	90	216	524	619	714	981	1147 21455
21455	1036	554	313	1193	742	400	53	562	345	1101	779	385	162	957	448	122	885	662	268	1061	845	25	923	669	201	1174	813	486	994	1121	97	230	496	629	724 21455
27455	392	50	1033	546	309	1223	738	175	967	572	317	1115	786	359	1073	851	425	133	892	640	277	824	463	31	935	678	179	1181	601	734	1004	1134	71	237	510 21455
27455	1219	768	388	42	1030	543	301	800	366	149	980	582	327	1087	647	255	1082	863	431	110	903	188	1159	831	474	8	941	690	211	517	615	706	1014	1144	84 21455
27455	540	298	1211	764	418	38	1022	337	1097	772	380	156	954	595	116	880	658	262	1060	872	443	918	696	200	1168	809	481	19	1154	94	224	491	622	720	986 21455
27455	68	1018	532	295	1208	756	414	961	569	350	1107	782	352	170	850	452	128	886	635	273	1067	459	26	929	673	206	1180	818	727	1000	1126	104	234	504	596 21455
27455		406	64	1048	528	287	1205				576											<u> </u>	830		4		684	183				1007	1140	76	244 21455
27455			1166		483	17	920		229		626				300			409					777			966		348		665		1062		450	121 21455
21455	28		_		1178				1133		236	509	603		1029				741	419	59		344			357			422		891	639			852 21455
21455	828	466	5	938	682	185	1187			1011		83	214	516	391		1039				755		960				803					107	905		254 21455
21455		1165		478	11	915	693 22		494		719	988	1151	95		762			1049		294		383		952		333				1059		442	117	877 21455
21455 21455			203 933	1172 676	815 180	487 1183	23 822	1128		235 1139	503 78	599 241	726 515	999 608		304 1035			412 1214		1021		1103 563	791	379	173 788	948 371	567 169	127 856	887 429	632 140	275 897	1066 642		455 21455 1080 21455
		32 833			942	688	186				984		89	218		399											1092		257				114		652 21455
		776			959	561					1068				674			817	457	30	926		233		600			1130		1209		416	60		529 21455
21455		316				174	969		134		633		1065		2	940	681		1190				1137		242				1040				754	393	66 21455
21455			584		1086				855		126		663	248		477	12	912	695		1164		711		1148			522			1046			1194	761 21455
21455	771	377	160	951	594	339	1099	659	278	1053	847	435	123	896	205	1171	814	490	22	922	667		500		723		1125	98		739	411	54	1023	556	305 21455
21455	349	1109	784	351	167	965	566	120	893	651	274	1083	843	427	932	677	177	1185	821	464	35	1131	75	238	507	605	732	1003	533	311	1215	748	389	61	1034 21455
21455	972	580	321	1119	794	364	141	873	423	112	890	648	266	1079	471	9	945	687	187	1157	835	710	1012	1143	81	215	518	612	39	1041	544	288	1221	760	398 21455
21455	374	154	946	587	335	1091	804	263	1071	869	453	108	882	645	1167	807	485	16	919	700	197	495	623	717	990	1152	93	221	766	410	48	1019	551	299	1198 21455
21455	79	245	512	607	702	1010	1136	312	1213	746	390	63	1032	535	1111	789	358	171	970	573	319	895	636	279	1074	854	421	132	668	182	1170	823	476	29	943 21455
27455	982	1150	86	219	525	617	712	1043	542	290	1222	758	396	40	585	328	1089	796	369	148	976	434	106	902	650	251	1084	864	21	939	698	178	1162	820	473 21455
27455	630	722	992	1122	100	226	499	408	46	1020	553	297	1200	767	159	953	591	340	1098	774	376	1056	874	444	119	876	657	265	812	470	18	931	694	208	1158 21455
27455	240										58									346	1110	631	272					889	204	1188	808	462	15	928	686 21455
27455	1142										752										579						860			683	196	1184	838	458	7 21455
27455		989																									259			3	917	680	193		834 21455
											1025																881					33	913		190 21455
	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455	21455 21455

The blocks of order 7 are **equal sums pandiagonal** magic squares, i.e., $M_{7\times7} := 4291$.

It is constructed based on magic rectangle of order 5×7 . blocks of order 5 given in previous work [30] is also constructed with same procedures. See the author's work [20].

3.4 Pandiagonal Magic Square of Order 49

Below is a **pandiagonal** magic squares of order 49.

m	IC	942193	307 94209703	8 94202843	94222737	94202157	94213133 9	94217249	94211075	94202843	94221365	94204215	94213819 9	4216563	94217249 942	07645 942	29597 942	06273 9421	307 942206	79 942199	93 942172	49 9423782	9 94217935	94224795	94229597	94232341	94228225 9	4217249 94	4195983 94	206273 9421	4505 9421107	75 94210389	94198041 94	217249 94226	67 9423302	7 94233027	94226167	94217249	94235085 9	4217249 94	4222737 94	4221365 9421	17935 942076	45 94224109	94209703 94217249
pan	5884	9 5884	9 58849	58849	58849	58849	58849	58849	58849	58849	58849	58849	58849	58849	58849 5	8849 5	8849 5	8849 588	49 58849	5884	9 5884	9 58849	58849	58849	58849	58849	58849	58849	58849	58849 588	849 58849	58849	58849	18849 5884	9 58849	58849	58849	58849	58849	58849	58849	58849 58	849 58849) 58849	58849
58849 1	401	1 801	1 1201	1601	2001	2401	334	391	742	1135	1535	1935	2335	268	668 7	25 1	125 14	476 18	6 2269	209	609	1002	1059	1459	1859	2210	192	543	943 1	1343 14	00 1793	2193	133	526 92	5 1277	1677	1734	2134	67	467	867 1	1267 16	60 2011	2068	58849 94217249
58849 199	3 239	3 49	393	793	1193	1593	1927	2327	326	383	783	1134	1527	1868	2268 2	60 6	60 7	17 11	7 1517	185	1 225	1 201	601	1001	1051	1451	1792	2185	184	584 93	35 1335	5 1392	1726 2	126 125	525	918	1318	1669	2052	2060	59	459 8	<mark>59 125</mark> 9	9 1659	58849 94217249
58849 118	5 158	5 198	5 2385	41	441	785	1175	1526	1919	2319	318	375	775	1109	1509 19	909 2	260 2	59 65	2 709	1050	0 1443	3 1843	2243	242	593	993	1327	1384 1	1784 2	2184 17	76 576	976	1310	710 171	8 2118	117	517	917	1251	1651	2051 2	2101 5	51 451	851	58849 94217249
58849 43	833	3 117	7 1577	1977	2377	33	367	767	1167	1567	1918	2311	310	651	701 1	101 1	501 1	901 23	01 251	634	985	5 1042	1442	1835	2235	234	568	968 1	1368 1	1376 17	76 2176	5 175	509	909 130	9 1702	1759	2110	109	443	843	1243 1	1643 20	043 2100) 92	58849 94217249
58849 236	9 25	425	5 825	1225	1569	1969	2310	302	359	759	1159	1559	1959	2293	292 6	43 7	700 10	093 14	3 1893	3 222	7 226	626	1026	1034	1434	1834	2168	167	567	960 13	60 1417	1768	2151	101 50	901	1301	1701	1751	2092	91	484	835 12	.35 1635	5 2035	58849 94217249
58849 161	7 196	1 236	61 17	417	817	1217	1551	1951	2351	301	351	751	1151	1485	1885 22	285 2	284 6	84 69	2 1092	2 1426	6 182	6 2226	218	618	1018	1075	1409	1809	2160	159 55	59 959	1352	1693 1	750 214	3 142	493	893	1293	1627	2027 2	2084	83 4	83 876	1227	58849 94217249
58849 809	120	9 160	9 2009	2353	9	409	743	1143	1543	1943	2343	342	350	733	1084 14	484 1	877 2	277 27	6 676	1010	0 106	7 1467	1818	2218	217	610	951	1351	1401 1	1801 22	01 151	551	885 1	285 168	5 1742	2142	134	534	875	1268	1619 2	2019 20	076 75	475	58849 94217249
58849 143	494	4 894	4 1294	1694	1744	2144	84	477	877	1228	1628	2028	2085	18	418 8	18 1	218 1	611 19	52 2362	2 295	352	2 752	1152	1552	1952	2352	285	685	693 1	1086 14	86 1886	2286	219	619 101	9 1076	1427	1827	2220	160	560	953 1	1353 14	10 1810 IN) 2161	58849 94217249
58849 174	3 213	6 135	5 535	886	1286	1686	2020	2077	76	476	869	1269	1620	2003	2354	10 4	410 8	10 12	0 1610	1944	4 234	4 343	344	744	1144	1544	1878	2278	277	677 73	34 1085	5 1478	1819 2	219 21	611	1011	1068	1468	1802	2202	152	552 9	52 1345	5 1402	58849 94217249
58849 127	3 167	8 173	5 2135	127	527	927	1261	1661	2012	2069	68	468	868	1202	1602 20	002 2	395	2 40	2 802	1136	5 153	6 1936	2336	335	392	736	1126	1477	1870 2	2270 26	669 669	726	1060 1	460 186	0 2211	210	603	1003	1344	1394	1794 2	2194 19	93 544	944	58849 94217249
58849 519	919	131	9 1670	1727	2127	126	460	860	1260	1653	2053	2061	60	394	794 1	194 1	594 19	994 23	94 43	384	784	1128	1528	1928	2328	327	661	718	1118 1	1518 18	69 2262	2 261	602	995 105	2 1452	1852	2252	202	585	936	1336 1	1393 17	786 2186	5 185	58849 94217249
58849 211	9 118	518	3 911	1311	1711	1719	2102	52	452	852	1252	1652	2045	2386	42 4	35 7	/86 11	186 15	86 1986	5 232	0 319	376	776	1176	1520	1920	2261	253	653	710 11	10 1510	1910	2244	243 594	4 994	1044	1444	1844	2178	177	577	977 13	28 1385	5 1785	58849 94217249
58849 170	3 176	0 211	1 110	510	910	1303	1644	2044	2094	93	444	844	1244	1578	1978 2	378	34 4	34 82	7 1178	1568	8 1912	2 2312	311	368	768	1168	1502	1902 2	2302	252 64	45 702	1102	1436 1	836 223	6 235	635	986	1043	1377	1777	2177	169 5	<mark>69 969</mark>	9 1369	58849 94217249
58849 902	130	2 169	5 1752	2152	102	502	836	1236	1636	2036	2093	85	485	826	1219 1	570 1	970 2	370 2	5 426	760	1160	0 1560	1960	2304	303	360	694	1094	1494 1	1894 22	94 293	644	1027 1	035 143	5 1828	2228	227	627	961	1361	1418 1	1769 21	169 168	561	58849 94217249
58849 236	636	5 987	7 1037	1437	1837	2237	170	570	970	1370	1378	1778	2171	111	511 9	04 1	304 17	704 17	51 2112	94	445	845	1245	1645	2038	2095	35	428	828 1	1179 15	79 1979	2379	312	369 769	1169	1562	1913	2313	246	646	703 1	1103 15	03 1903	3 2303	58849 94217249
58849 182														1753	2153 1	03 5	503 9	03 12	6 1696	5 203	7 208	7 86	486	837	1237	1637	1971	2371	27	427 82	20 1220							1561	1895	2295	294	638 6	95 1095	5 1495	58849 94217249
58849 107	7 142	8 182	1 2221	220	620	1020	1354	1411	1811	2162	161	554	954	1295	1688 17	745 2	145 1	44 49	5 895	1229	9 1629	9 2029	2086	78	478					2363 1			1153 1	553 195	3 2346	296	353	753	1087	1487	1887 2	2287 2	86 686	5 687	58849 94217249
58849 612	101	2 106	9 1469	1820	2213	212	553	946	1346	1403	1803	2203	153	536	887 12	287 1	687 1	737 21	37 136	470	870	1270	1621	2021	2078	77	411	811	1211 1	1604 20	04 2355	5 11	345	745 114	5 1545	1945	2345	337	678	735	1079 1	1479 18	379 2279) 278	58849 94217249
58849 221										945	1338	1395			128 5																			336 38						270	670	727 11	27 1471	1871	58849 94217249
58849 145											586																							929 232					1519				62 719		58849 94217249
																																								1111	1511	1911 22	255 254	654	58849 94217249
58849 329																																									796 1	1196 15	596 1989		
58849 192																																								2381	37				58849 94217249
58849 116															1438 18							9 1772												639 203					1180	1580	1980 2		29 429		
58849 362																											504							338 123					421						58849 94217249
58849 234																																		79 479							420				58849 94217249
58849 154																																													58849 94217249
58849 738			8 1938				728																											263 166								1997 23			58849 94217249
58849 72															347 7																			548 94								1282 16			58849 94217249
58849 201															2332 3				9 1539												06 1063			197 196		940			1731	2151 1675 ·	150	530 9			58849 94217249
58849 125 58849 45					456 2105		1197 438			1500		397 2382			1531 19 772 1						4 1514 5 713		2265	204				990 1		2248 19	98 598 47 2247			389 178 980 132		100	588	932	1322 514	014	1725 2	2123 14 1714 17	22 522		58849 94217249 58849 94217249
50940 200	040 7 96		0 1040 7 847	1240	1640		450 2374		1189 430	830	1902	2002			314 3		525 I: 164 11	161 15	23 322 54 1915				705	1105				238		982 10		1839		980 132 172 572		1272	2101	100	2114	514 106	506	006 12	22 2115	6 1762	58849 94217249
58849 163				488			1573			22	1101	822			1956 2		806 3	63 76	3 1156				289	640				1831		230 63				765 216		564	064			100	2155	105 /		3 1298	58849 94217249
																								2280												2157	156						147 146		58849 94217249
			5 1365				qq	499					2156							-														556 141 641 698		1/102	1891								58849 94217249
							1748	2148																												690									58849 94217249
			6 2199				1283								1624 2																			482 188											58849 94217249
58849 54														465					5 075 56 65		5 799			1999										723 112					607						58849 94217249
58849 219															57 4																32 1532					1115									58849 94217249
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The blocks of order 7 are equal sums pandiagonal magic squares with sum $M_{7\times7} := 8407$. Moreover it is bimagic squares with bimagic sum $Sb_{49\times49} := 94220679.$

Remark 1. The excel file attached with this work contains only pandiagonal magic squares with equal sums of order 7 up to order 133, i.e., these are of orders 21, 35, 49, 63, 77, 91, 105, 109, and 133. It is left for the readers to check the other order multiples of 7. Whole the work in Excel file is up to order 140.

Author's Contribution to Recreation of Numbers and Magic Squares 4

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