# Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 7 

## Inder J. Taneja ${ }^{1}$


#### Abstract

During past years author worked with block-wise borderedmagic squares of even number blocks. These are based on equal sums magic squares of orders $4,6,8,10$, etc. This type of work is an extension of classical bordered magic squares. In case of multiples of 4, the extension is made for pandiagonal magic squares [23]. For multiples of order 6 refer Taneja [24]. For the first time, we are presenting here bordered magic squares of odd number blocks. Recently, author worked on multiples of 3, based on different sums magic squares of order 3 [29]. The work for the borders multiples of 5 refer [30]. It is done with two types of magic squares of order 5 . One type is pandiagonal magic squares, and anotheras bordered magic squares. Based on same procedure we worked with multiples of 7 based on magic squares of order 7. Padiagonal magic squares of orders 21, 28, 35 and 49 are also given. Higher order examples can be seen in Excel file attached with the work. The total work is up to order 140. Pandiagonal magic squares based on equal sums pandiagonal magic squares of order 7 are also included in the Excel file.


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## 1 Introduction

During past years author [2, $3,4,5,6,7,8]$ worked with block-wise magic squares from orders 12 to 47. Author [9, 10, 11, 12, 13, 14] also worked with bordered magic squares. The study on bordered magic squares is extended to block-bordered magic squares [15, 16, 17]. This is specially done for the magic squares of orders $p$ and $2 p$, where $p$ is a prime number. This study is still extended to block-wise bordered magic squares [18, 19, 20, 21]. Some conection with Pythagorean triples and area-representations are also made [23, 24, 25, 26, 27]. The main property of bordered magic squares is that if we remove external borders, still we get sub-bordered magic squares, i.e., each layer in itself lead us to magic squares. In many cases, the properties of bordered magic square are seperated by even and odd orders magic squares. In many cases, we get good properties for the even order bordered magic squares. In some cases, we have to use fractional numbers to reach minimum perfect square sum of entries. For more study on bordered magic squares refer H. White's web-site [1].

The idea of bordered magic squares is already discussed by H. White's web-site [1] where the borders are of single digits. Borders multiples of even numbers starting from 4 are done extensively by author [23, 24, 25, 26, 27, 28].

Recently, for the first time, we presented bordered magic squares of odd number blocks. In case of multiples of 3, we worked with different sums magic squares of order 3. In case of multiples of 5 , we worked with pandiagonal and bordered magic squares of order 5 . This work is for multiples of 7. Here also we worked with two types of magic squares of order 7. One pandiagonal and another is bordered magic squares of order 7. The procedure, how to get these block-wise bordered magic squares is also explained. Pandiagonal magic squares multiples of 7 are also given. This work is up to order 49. Higher orders examples can be seen in Excel file attached with this work. Before proceeding further, let's summarize, the idea of block-wise bordered magic squares:

### 1.1 Classification of Bordered Magic Squares

- Single Digit: Bordered magic squares based on single digit [9, 10, 1].
- Two Digits: Bordered magic squares based on magic rectangles multiples of 2 [58, 59, 60, 61, 61].
- Three Digits: Bordered magic squares based on magic squares of order 3 [29].
- Four Digits: Bordered magic squares based on magic squares of order 4 [23].
- Five Digits: Bordered magic squares based on magic squares of order 5 [30].
- Six Digits: Bordered magic squares based on magic squares of order 6 [24].
- Seven Digits: Bordered magic squares based on magic squares of order 7 (This work).

For further even number multiples refer the following works of author:

- Eight Digits: Bordered magic squares based on magic squares of order 8 [25].
- Ten Digits: Bordered magic squares based on magic squares of order 10 [26].
- Twelve Digits: Bordered magic squares based on magic squares of order 12 [27].
- Fourteen Digits: Bordered magic squares based on magic squares of order 14 [28].

Let's see below the some examples of block-wise bordered magic squares multiples 7, where magic squares of order 7 are considered in two different ways.

## 2 Block-Wise Bordered Magic Squares

### 2.1 Magic Squares of Orders 42 and 49

Let's consider bordered magic square of orders 6 and 7 given by
6

| 6 | 30 | 3 | 36 | 4 | 32 | 111 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 35 | 17 | 22 | 11 | 24 | 2 | 111 |
| 29 | 12 | 23 | 18 | 21 | 8 | 111 |
| 27 | 26 | 13 | 20 | 15 | 10 | 111 |
| 9 | 19 | 16 | 25 | 14 | 28 | 111 |
|  | 7 | 34 | 1 | 33 | 31 | 111 |
| 111 | 111 | 111 | 111 | 111 | 111 | 111 |

7

| 44 | 38 | 40 | 5 | 4 | 2 | 42 | 175 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 34 | 30 | 15 | 14 | 32 | 39 | 175 |
| 9 | 19 | 28 | 21 | 26 | 31 | 41 | 175 |
| 7 | 17 | 23 | 25 | 27 | 33 | 43 | 175 |
| 47 | 37 | 24 | 29 | 22 | 13 | 3 | 175 |
| 49 | 18 | 20 | 35 | 36 | 16 | 1 | 175 |
| 8 | 12 | 10 | 45 | 46 | 48 | 6 | 175 |
| 175 | 175 | 175 | 175 | 175 | 175 | 175 | 175 |

The entries of above two magic squares are sequential numbers starting from 1:

$$
\begin{aligned}
D_{11 \times 11} & :=\{1,2, \ldots, 35,36\} \\
D_{12 \times 12} & :=\{1,2, \ldots, 48,49\}
\end{aligned}
$$

These two magic squares are such that replacing the upper border still we are left with magic squares of sequential vales.
Multiplying each entry by 49, we get
6

| 294 | 1470 | 147 | 1764 | 196 | 1568 | 5439 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1715 | 833 | 1078 | 539 | 1176 | 98 | 5439 |
| 1421 | 588 | 1127 | 882 | 1029 | 392 | 5439 |
| 1323 | 1274 | 637 | 980 | 735 | 490 | 5439 |
| 441 | 931 | 784 | 1225 | 686 | 1372 | 5439 |
| 245 | 343 | 1666 | 49 | 1617 | 1519 | 5439 |
| 5439 | 5439 | 5439 | 5439 | 5439 | 5439 | 5439 |

7

| 2156 | 1862 | 1960 | 245 | 196 | 98 | 2058 | 8575 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 539 | 1666 | 1470 | 735 | 686 | 1568 | 1911 | 8575 |
| 441 | 931 | 1372 | 1029 | 1274 | 1519 | 2009 | 8575 |
| 343 | 833 | 1127 | 1225 | 1323 | 1617 | 2107 | 8575 |
| 2303 | 1813 | 1176 | 1421 | 1078 | 637 | 147 | 8575 |
| 2401 | 882 | 980 | 1715 | 1764 | 784 | 49 | 8575 |
| 392 | 588 | 490 | 2205 | 2254 | 2352 | 294 | 8575 |
| 8575 | 8575 | 8575 | 8575 | 8575 | 8575 | 8575 | 8575 |

The distributions of these two magic squares are given by

$$
\begin{aligned}
D 1_{7 \times 7} & :=\{49,98, \ldots, 1715,1764\} \\
D 1_{8 \times 8} & :=\{49,98 \ldots, 2352,2401\}
\end{aligned}
$$

In both the cases the difference between entries is 25 . Now in each case replace the entries by magic squares of order 5 formed by the entries as given below:

$$
\begin{aligned}
49 & \rightarrow 1,2, \ldots, 49 \\
98 & \rightarrow 50,51, \ldots, 98 \\
147 & \rightarrow 99,100, \ldots, 147 \\
\ldots & \rightarrow \ldots \\
2352 & \rightarrow 2304,2305, \ldots, 2352 \\
2401 & \rightarrow 2353,2354 \ldots, 2401
\end{aligned}
$$

This lead us to following two bordered magic squares of orders 42 and 49 .










 | 1703 | 1695 | 1694 | 1686 | 1678 | 1670 | 1711 | 821 | 813 | 812 | 804 | 796 | 788 | 829 | 1066 | 1058 | 1057 | 1049 | 1041 | 1033 | 1074 | 527 | 519 | 518 | 510 | 502 | 494 | 535 | 1164 | 1156 | 1155 | 1147 | 1139 | 1131 | 1172 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
































|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 37705 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 251 | 257 | 55 | 290 | 291 | 293 | 253 | 1427 | 1433 | 1431 | 1466 | 67 | 1469 | 1429 | 104 | 110 | 08 | 143 | 44 | 146 | 106 | 17 | 1727 | 25 | 1760 | 761 | 1763 | 1723 | 153 | 159 | 57 | 192 | 193 | 195 | 155 | 1525 | 31 | 152 | 1564 | 1565 | 1567 | 1527 |  |
| 284 | 261 | 265 | 280 | 28 | 263 | 256 | 1460 | 1437 | 1441 | 暏 | 1457 | 39 | 1432 | 137 | 114 | 118 | 133 | 134 | 116 | 109 | 1754 | 17 | 1735 | 50 | 1751 | 1733 | 1726 | 186 | 163 | 167 | 182 | 183 | 165 | 158 | 1 | 1535 | 153 | 1554 | 1555 | 1537 | 1530 | 37065 |
| 286 | 276 | 267 | 274 | 269 | 264 | 254 | 1462 | 2 | 1443 |  | 1445 | 1440 | 1430 | 139 | 129 | 120 | 127 | 122 | 117 | 107 | 1756 | 1746 | 1737 | 1744 | 173917 | 1734 | 1724 | 88 | 178 | 169 | 176 | 171 | 166 | 156 | 1560 | 1550 | 1541 | 48 | 1543 | 153 | 528 | 37065 |
| 288 | 278 | 272 | 270 | 268 | 262 | 25 | 14 | 1454 | 14 |  | 1444 | 1438 | 1428 | 141 | 131 | 125 | 123 | 121 | 115 | 05 | 175 | 1748 | 1742 |  | 1738 | 1732 | 172 | 190 | 180 | 174 | 172 | 170 | 164 | 154 | 1562 | 52 | 1546 |  | 542 | 1536 | 1526 | 37065 |
| 248 | 258 | 271 | 266 | 273 | 282 | 292 | 1424 | 1434 | 1447 | 1442 | 1449 | 1458 | 1468 | 101 | 111 | 24 | 119 | 126 | 135 | 145 | 17 | 1728 | 1741 | 1736 | 1743 | 1752 | 17 | 150 | 160 | 173 | 68 | 175 | 184 | 194 | 1522 | 32 | 15 | 40 | 447 | 1556 | 1566 | 37065 |
| 246 | 277 | 275 | 260 | 259 | 279 | 294 | 1422 | 1453 | 1451 | 1436 | 35 | 5 | 1470 | 99 | 130 | 128 | 13 | 112 | 132 | 147 | 1716 | 1747 | 1745 | 1730 | 1729 | 49 | 1764 | 48 | 179 | 177 | 162 | 161 | 181 | 196 | 1520 | 1551 | 154 | 534 | 1533 | 1553 | 568 | 37065 |
| 287 | 283 | 285 | 50 | 249 | 247 | 289 | 1463 | 1459 | 1461 | 1426 | 1425 | 1423 | 46 | 140 | 136 | 138 | 103 | 102 | 100 | 142 | 1757 | 1753 | 1755 | 1720 | 1719 | 1717 | 1759 | 189 | 185 | 87 | 152 | 151 | 149 | 191 | 1561 | 1557 | 155 | 1524 | 1523 | 1521 | 56 |  |
| 1672 | 1678 | 16 | 1711 | 17 | 1714 | 167 | 790 | 796 | 794 | 829 | 830 | 832 | 792 | 1035 | 1041 | 1039 | 1074 | 1075 | 1077 | 037 | 496 | 502 | 500 | 535 | 536 | 538 | 498 | 133 | 1139 | 137 | 172 | 173 | 1175 | 1135 | 55 | 61 | 59 | 94 | 95 | 97 | 57 | 37065 |
| 1705 | 1682 | 1686 | 1701 | 1702 | 1684 | 167 | 823 | 800 | 804 | 819 | 820 | 802 | 795 |  | 1045 | 1049 | 9 | 065 | 1047 | 1040 | 529 | 506 | 510 | 525 | 526 | 508 | 501 | 1166 | 114 | 114 | 1162 | 163 | 1145 | 1138 | 88 | 65 | 69 | 84 | 85 | 67 | 60 |  |
| 1707 | 1697 | 1688 | 1695 | 1690 |  | 1675 | 825 | 815 | 806 | 813 | 808 | 803 | 793 | 1070 | 1060 | 10 | 11058 | 1053 | 1048 | 1038 | 53 | 521 | 512 | 519 | 514 | 509 | 99 | 1168 | 1158 | 1149 | 156 | 1151 | 146 | 1136 | 90 | 80 | 71 | 78 | 73 | 68 | 58 |  |
| 1709 | 1699 | 1693 | 1691 | 1689 | 16 | 16 | 827 | 817 | 811 | 809 | 07 | 801 | 791 | 10 | 1062 | 10 | 61054 | 1052 | 1046 | 1036 | 533 | 523 | 517 | 515 | 513 | 507 | 497 | 1170 | 1160 | 1154 | 52 | 1150 | 1144 | 1134 | 92 | 82 | 76 | 74 | 72 | 66 | 56 | 37065 |
| 1669 | 167 | 16 | 1687 | 1694 | 1703 | 1713 | 787 | 797 | 810 | 805 | 812 | 821 | 831 | 1032 |  | 10 | 1050 | 057 | 1066 | 1076 | 493 | 503 | 516 | 511 | 518 | 527 | 537 | 1130 | 1140 | 1153 | 148 | 1155 | 164 |  | 52 | 62 | 75 | 70 | 77 | 86 | 96 | 7065 |
| 1667 | 169 | 16 | 1681 | 1680 | 1700 | 1715 | 785 | 816 | 814 | 799 | 798 | 818 | 833 | 1030 | 1061 | 1059 | 9104 | 1043 | 1063 | 1078 | 49 | 522 | 520 | 505 | 504 | 524 | 539 | 1128 | 15 | 1157 | 1142 | 1141 | 1161 | 1176 | 50 | 81 | 79 | 64 | 63 | 83 | 98 |  |
| 1708 | 1704 | 1706 | 1671 | 16 | 1668 | 171 | 82 | 822 | 824 | 789 | 788 | 786 | 828 | 107 | 1067 | 1069 | 1034 | 1033 | 1031 | 1073 | 532 | 528 | 530 | 495 | 494 | 492 | 534 | 1169 | 1165 | 1167 | 32 | 1131 | 1129 | 117 | 91 | 87 | 89 | 54 | 53 | 51 | 93 |  |
| 13 | 1384 | 1382 | 1417 | 1418 | 1420 | 1380 | 545 | 551 | 549 | 584 | 585 | 57 | 547 | 1084 | 1090 | 108 | 81123 | 1124 | 126 | 1086 | 83 | 845 | 843 | 78 | 879 | 881 | 841 | 986 | 992 | 990 | 1025 | 1026 | 1028 | 988 | 349 | 355 | 35 | 388 | 38 | 391 | 351 |  |
| 1411 | 1388 | 13921 |  |  | 1390 | 1383 | 578 | 555 | 559 | 574 | 75 | 557 | 550 | 1117 | 1094 | 1098 | 81113 | 111 | 1096 | 10 | 87 | 849 | 853 | 868 | 69 | 851 | 844 | 1019 | 99 | 1000 | 1015 | 1016 | 998 | 991 | 382 | 359 | 36 | 378 | 37 | 361 | 354 |  |
| 1413 | 140 | 13 | 1401 | 1396 | 1391 | 138 | 58 | 57 | 56 | 568 | 563 | 558 | 548 | 1119 | 1109 | 1100 | 1107 | 1102 | 1097 | 1087 | 87 | 864 | 855 | 862 | 857 | 852 | 842 | 1021 | 1011 | 1002 | 1009 | 1004 | 999 | 989 | 384 | 374 | 365 | 372 | 367 | 362 | 352 | 37065 |
| 1415 | 1405 | 13 |  |  | 1389 | 1379 | 582 | 572 | 566 | 564 | 562 | 556 | 546 |  |  | 1105 | 1103 | 1101 | 1095 | 1085 | 876 | 866 | 860 | 858 | 856 | 850 | 840 | 1023 | 1013 | 100 |  | 03 | 997 | 987 | 386 | 376 | 370 | 68 | 366 | 360 | 350 |  |
| 1375 | 1385 | 139 | 1393 | 1400 | 1409 | 1419 | 5 | 552 | 565 | 560 | 567 | 576 | 586 | 1081 | 1091 | 1104 | 41099 | 110 | 1115 | 1125 | 836 | 846 | 859 | 854 | 861 | 870 | 880 | 983 | 993 | 1006 | 1001 | 1008 | 10 | 10 | 346 | 356 | 369 | 364 | 371 | 380 | 390 |  |
| 1373 | 140 | 1402 | 1387 | 138 | 406 | 1421 | 54 | 571 | 569 | 554 | 553 | 573 | 588 | 1079 | 1110 | 1108 | 1093 | 1092 | 1112 | 1127 | 83 | 865 | 863 | 848 | 847 | 867 | 882 | 981 | 1012 | 1010 | 995 | 994 | 1014 | 1029 | 34 | 375 | 373 | 358 | 357 | 377 | 392 |  |
| 1414 | 1410 | 141 | 1377 | 1376 | 137 | 141 | 581 | 577 | 579 | 544 | 543 | 541 | 583 | 1120 | 1116 | 1118 | 1083 | 108 | 1080 | 112 | 875 | 871 | 873 | 838 | 837 | 835 | 877 | 102 | 101 | 1020 | 985 | 984 | 982 | 102 | 38 | 381 | 383 | 348 | 34 | 345 | 387 |  |
| 128 | 1286 | 1284 | 1319 | 1320 | 1322 | 1282 | 12 | 1237 | 1235 | 1270 | 1271 | 1273 | 1233 | 594 | 600 | 598 | 633 | 634 | 636 | 596 | 937 | 943 | 94 | 976 | 977 | 79 | 939 | 692 | 698 | 696 | 731 | 732 | 734 | 694 | 447 | 45 | 45 | 486 | 48 | 48 | 449 |  |
| 1313 | 1290 | 12941 | 1309 | 1310 | 1292 | 1285 | 1264 | 12 | 1245 | 1260 | 1261 | 1243 | 1236 | 627 | 604 | 608 | 623 | 624 | 606 | 599 | 970 | 947 | 951 | 966 | 667 | 949 | 942 | 725 | 702 | 706 | 72 | 722 | 704 | 697 | 480 | 45 | 461 | 476 | 47 | 45 | 452 |  |
| 1315 | 130 | 1296 |  | 1298 | 1293 | 1283 | 1266 | 1256 | 12 | 1254 | 1249 | 1244 | 1234 | 629 | 619 | 610 | 617 | 612 | 607 | 597 | 972 | 962 | 953 | 960 | 955 | 950 | 940 | 727 | 717 | 08 | 715 | 710 | 705 | 695 | 482 | 472 | 463 | 470 | 46 | 460 | 450 |  |
| 131 | 130 | 13 |  | 1297 | 1291 | 1281 | 1268 |  | 12 | 1250 | 1248 | 1242 | 1232 | 631 | 621 | 615 | 613 | 611 | 605 | 59 | 974 | 96 | 958 | 956 | 954 | 948 | 938 | 729 | 719 | 713 | 711 | 709 | 703 | 69 | 484 | 474 | 46 | 466 | 464 | 458 | 448 |  |
| 12 | 128 | 1300 | 1295 | 1302 | 1311 | 1321 | 1228 | 12 | 1251 | 1246 | 253 | 12 | 127 | 591 | 601 | 614 | 609 | 616 | 625 | 635 | 934 | 944 | 957 | 952 | 59 | 968 | 978 | 689 | 699 | 712 | 70 | 714 | 723 | 733 | 444 | 454 | 467 | 462 | 46 | 478 | 488 |  |
| 127 | 130 | 1304 | 289 | 1288 | 1308 | 1323 | 1226 | 1257 | 1255 | 1240 | 1239 | 1259 | 1274 | 589 | 620 | 618 | 603 | 602 | 622 | 37 | 932 | 963 | 961 | 946 | 945 | 965 | 980 | 68 | 718 | 716 | 701 | 700 | 720 | 735 | 442 | 473 | 471 | 456 | 455 | 475 | 490 |  |
| 1316 | 1312 | 1314 | 1279 | 1278 | 1276 | 1318 | 1267 | 1263 | 1265 | 123 | 1229 | 227 | 1269 | 630 | 62 | 628 | 59 | 592 | 90 | 632 | 973 | 969 | 971 | 936 | 935 | 933 | 975 | 728 | 724 | 726 | 691 | 690 | 688 | 73 | 48 | 479 | 481 | 446 | 44 | 443 | 485 |  |
| 398 | 404 | 402 | 437 | 438 | 440 | 400 | 888 | 89 | 892 | 927 | 928 | 930 | 890 | 741 | 747 | 745 | 780 | 781 | 783 | 743 | 11 | 1188 | 1186 | 122 | 122 | 122 | 1184 | 643 | 649 | 647 | 682 | 683 | 685 | 645 | 1329 | 133 | 133 | 368 | 136 | 137 | 1331 |  |
| 431 | 408 | 412 | 427 | 428 | 410 | 403 | 92 | 89 | 902 | 917 | 918 | 900 | 89 | 774 | 751 | 75 | 770 | 77 | 753 | 746 | 12 | 1192 | 1196 | 1211 | 1212 | 1194 | 1187 | 676 | 65 | 657 | 672 | 673 | 655 | 64 | 1362 | 39 | 13 | 58 | 359 | 1341 | 1334 | 37065 |
| 433 | 423 | 414 | 421 | 416 | 411 | 401 | 923 | 913 | 904 | 911 | 906 | 901 | 891 | 776 | 766 | 757 | 764 | 759 | 754 | 744 | 1217 | 1207 | 1198 | 1205 | 200 |  | 1185 | 678 | 668 | 659 | 666 | 661 | 656 | 646 | 1364 | 1354 | 134 | 52 | 347 | 1342 | 1332 | 37065 |
| 435 | 425 | 419 | 417 | 415 | 409 | 399 | 925 | 915 | 909 | 907 | 905 | 899 | 889 | 778 | 768 | 762 | 60 | 758 | 752 | 742 | 12 | 12 | 12 | 1201 | 1199 | 1193 | 1183 | 680 | 67 | 664 | 662 | 660 | 654 | 64 | 1366 | 1356 | 1350 | 348 | 1346 | 1340 | 1330 | 37065 |
| 395 | 405 | 418 | 413 | 420 | 429 | 43 | 885 | 895 | 908 | 903 | 910 | 919 | 929 | 738 | 748 | 761 | 756 | 763 | 772 | 782 | 1179 | 1189 | 1202 | 1197 | 1204 | 1213 | 1223 | 640 | 650 | 663 | 658 | 665 | 674 | 684 | 1326 | 1336 | 1349 | 344 | 1351 | 1360 | 1370 | 37065 |
| 393 | 424 | 422 | 407 | 406 | 426 | 441 | 883 | 914 | 912 | 897 | 896 | 916 | 931 | 736 | 767 | 765 | 750 | 749 | 769 | 784 | 117 | 1208 | 1206 | 1191 | 1190 | 1210 | 22 | 638 | 669 | 667 | 652 | 651 | 671 | 686 | 1324 | 1355 | 135 | 338 | 337 | 1357 | 1372 |  |
| 434 | 430 | 43 | 397 | 39 | 394 | 436 | 92 | 920 | 922 | 887 | 886 | 884 | 926 | 777 | 773 | 775 | 740 | 739 | 737 | 779 | 1218 | 1214 | 1216 | 1181 | 1180 | 1178 | 1220 | 679 | 675 | 677 | 642 | 641 | 639 | 681 | 136 | 136 | 136 | 1328 | 13 | 132 | 1367 |  |
| 202 | 208 | 206 | 241 | 242 | 244 | 204 | 300 | 306 | 304 | 339 | 340 | 342 | 302 | 1623 | 1629 | 1627 | 71662 | 63 | 1665 | 162 | 6 | 12 | 10 | 45 | 46 | 48 | 8 | 74 | 1580 | 1578 | 1613 | 1614 | 1616 | 1576 | 1476 | 1482 | 1480 | 1515 | 1516 | 1518 | 1478 | 37065 |
| 235 | 212 | 216 | 231 | 232 | 214 | 207 | 333 | 310 | 314 | 329 | 330 | 312 | 305 | 16 | 1633 | 1637 | 71652 | 1653 | 1635 | 162 | 39 | 16 | 20 | 35 | 36 | 18 | 11 | 1607 | 158 | 158 | 1603 | 1604 | 1586 | 157 | 1509 | 148 | 149 | 505 | 50 | 1488 | 1481 | 37065 |
| 237 | 22 | 218 | 22 | 22 | 21 | 205 | 335 | 32 | 316 | 323 | 318 | 313 | 303 | 16 | 1648 | 16 | 9 | 1641 | 16 | 162 | 41 | 31 | 22 | 29 | 24 | 19 | 9 | 1609 | 159 | 15 | 1597 | 1592 | 15 | 15 | 1511 | 150 | 149 | 99 | 1494 | 14 | 1479 | 37065 |
| 239 | 229 | 223 | 221 | 219 | 213 | 203 | 337 | 327 | 321 | 319 | 317 | 311 | 301 | 1660 | 1650 | 16 | 1642 | 10 | 16 | 1624 | 43 | 33 | 27 | 25 | 23 | 17 | 7 | 161 | 160 | 15 | 593 | 591 | 1585 | 157 | 1513 | 1503 | 1497 | 95 | 49 | 1487 | 1477 | 37065 |
| 199 | 209 | 222 | 217 | 224 | 233 | 243 | 297 | 307 | 320 | 315 | 322 | 331 | 341 | 1620 | 1630 | 1643 | 31638 | 1645 | 654 | 166 | 3 | 13 | 26 | 21 | 28 | 37 | 47 | 1571 | 158 | 1594 | 589 | 1596 | 1605 | 1615 | 1473 | 1483 | 1496 | 1491 | 1498 | 1507 | 1517 | 37065 |
| 197 | 228 | 226 | 211 | 210 | 230 | 245 | 295 | 326 | 324 | 309 | 308 | 328 | 343 | 1618 | 1649 | 1647 | 71632 | 1631 | 1651 | 1666 | 1 | 32 | 30 | 15 | 14 | 34 | 49 | 156 | 160 | 1598 | 1583 | 1582 | 1602 | 16 | 14 | 1502 | 1500 | 1485 | 1484 | 150 | 1519 | 37065 |
| 238 | 234 | 236 | 201 | 200 | 198 | 240 | 336 | 332 | 334 | 299 | 298 | 296 | 338 | 1659 | 1655 | 1657 | 71622 | 1621 | 1619 | 1661 | 42 | 38 | 40 | 5 | 4 | 2 | 44 | 1610 | 1606 | 1608 | 1573 | 1572 | 1570 | 1612 | 1512 | 1508 | 1510 | 1475 | 1474 | 1472 | 1514 | 37065 |
| 3706 | 3706 | 370 | 37705 | 37065 | 37065 | 37065 | 370 | 37065 | 370 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 37065 | 3706 | 37065 | 37065 | 37065 | 37065 | 37065 | 37865 |

Above two magic squares of order 42 formed by blocks of magic squares of order 7 are with sequential entries:

$$
D_{35 \times 35}:=\{1,2, \ldots, 1763,1764\}
$$

Below are two bordered magic squares of order 49 with blocks of magic squares of order 7:

































































 $\begin{array}{llllllllllllllll}337 & 327 & 321 & 319 & 317 & 311 & 301 & 827 & 817 & 811 & 809 & 807 & 801 & 791\end{array}$









 $229622922294225922582256229818061802180417691768176618081169116511671132113111291171 \mid 1414141014121377137613741416$ 1071 106710691034103310311073














Above two magic squares of order 49 formed by blocks of magic squares of order 7 are with sequential entries:

$$
D_{40 \times 40}:=\{1,2, \ldots, 2400,2401\} .
$$

These four magic squares are bordered magic squares with border made by pandiagonal and bordered magic squares of order 5 . If you remove the external borders, still we are left with magic squares of lower orders. Let's see how it works.

### 2.2 Magic Squares of Order 35

These magic squares are obtained from above by the application of the formula $\frac{a^{2}-b^{2}}{2}, a>b$. Removing the external border of order 7 and then subtracting $\frac{49^{2}-35^{2}}{2}:=588$ from magic squares of orders 49, we get magic squares of order 35 given by


| 1035 | 1041 | 1039 | 74 | 1075 | 1077 | 1037 | 839 | 845 | 8438 | 878 | 879 | 881 | 841 | 104 | 110 | 108 | 143 | 144 | 146 | 106 | 55 | 61 | 59 | 94 | 95 | 97 | 57 | 937 | 943 | 941 | 976 | 977 | 979 | 939 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1068 | 1045 | 1049 | 64 | 65 | 1047 | 1040 | 8 | 849 | 853 | 868 | 869 | 851 | 844 | 137 | 14 | 18 | 133 | 134 | 116 | 109 | 88 | 65 | 69 | 84 | 85 | 67 | 60 | 70 | 947 | 951 | 966 | 967 | 94 | 2 |  |
| 1070 | 1060 | 1051 | 58 | 1053 | 1048 | 1038 | 874 | 4 | 855 | 82 | 857 | 852 | 42 | 139 | 129 | 120 | 27 | 22 | 117 | 107 | 90 | 80 | 71 | 78 | 73 | 68 | 58 | 72 | 962 | 953 | 960 | 955 | 950 | 0 | 2145 |
| 1072 | 1062 | 1056 | 1054 | 52 | 1046 | 1036 | 876 | 866 | 8608 | 58 | 856 | 850 | 840 | 141 | 31 | 125 | 23 | 121 | 15 | 105 | 92 | 82 | 76 | 74 | 72 | 66 | 56 | 974 | 964 | 958 | 956 | 954 | 948 | 938 | 2145 |
| 1032 | 1042 | 1055 | 50 | 1057 | 1066 | 1076 | 836 | 846 | 8598 | 854 | 861 | 870 | 880 | 101 | 111 | 124 | 119 | 126 | 135 | 145 | 52 | 62 | 75 | 70 | 77 | 86 | 96 | 934 | 944 | 957 | 952 | 959 | 968 | 978 | 2145 |
| 1030 | 10611 | 1059 | 44 | 1043 | 1063 | 1078 | 83 | 865 | 8638 | 8488 | 847 | 867 | 882 | 99 | 130 | 128 | 113 | 112 | 132 | 147 | 50 | 81 | 79 | 64 | 63 | 83 | 98 | 932 | 963 | 961 | 946 | 945 | 965 | 980 | 2145 |
| 1071 | 10671 | 1069 | 1034 | 1033 | 1031 | 1073 | 875 | 871 | 873 | 8388 | 837 | 835 | 877 | 140 | 136 | 138 | 103 | 102 | 100 | 142 | 91 | 87 | 89 | 54 | 53 | 51 | 93 | 973 | 969 | 971 | 936 | 935 | 933 | 975 |  |
| 300 | 306 | 04 | 339 | 340 | 342 | 302 | 741 | 747 | 745 | 780 | 781 | 783 | 743 | 398 | 404 | 402 | 437 | 438 | 440 | 400 | 643 | 649 | 647 | 682 | 683 | 685 | 645 | 888 | 894 | 892 | 927 | 928 | 93 | 890 |  |
| 333 | 10 | 314 | 329 | 30 | 312 | 305 | 774 | 7517 | 755 | 70 | 771 | 753 | 746 | 431 | 408 | 412 | 427 | 428 | 410 | 403 | 676 | 653 | 657 | 672 | 673 | 655 | 648 | 92 | 898 | 902 | 917 | 918 | 900 | 393 |  |
| 335 | 25 | 316 | 23 | 8 | 313 | 303 | 77 | 766 | 757 | 7647 | 759 | 754 | 74 | 433 | 423 | 41 | 21 | 16 | 411 | 401 | 678 | 68 | 659 | 666 | 661 | 656 | 646 | 923 | 913 | 90 | 911 | 906 | 901 | 891 |  |
| 337 | 327 | 321 | 319 | 317 | 311 | 301 | 778 | 768 | 762 | 7607 | 758 | 752 | 742 | 435 | 425 | 419 | 417 | 15 | 409 | 399 | 680 | 670 | 664 | 662 | 660 | 654 | 64 | 925 | 915 | 909 | 907 | 905 | 899 | 889 |  |
| 297 | 307 | 320 | 315 | 322 | 331 | 341 | 738 | 748 | 7617 | 756 | 763 | 772 | 782 | 395 | 405 | 418 | 413 | 420 | 429 | 439 | 640 | 650 | 663 | 658 | 665 | 674 | 684 | 885 | 895 | 908 | 903 | 910 | 919 | 929 |  |
| 295 | 326 | 324 | 309 | 308 | 328 | 343 | 736 | 767 | 7657 | 750 | 749 | 769 | 78 | 393 | 424 | 422 | 407 | 406 | 426 | 441 | 638 | 669 | 667 | 652 | 651 | 671 | 686 | 883 | 914 | 912 | 897 | 896 | 916 | 931 |  |
| 336 | 332 | 334 | 299 | 298 | 296 | 338 | 777 | 773 | 775 | 740 | 739 | 737 | 779 | 434 | 430 | 432 | 397 | 396 | 394 | 436 | 679 | 675 | 677 | 642 | 641 | 639 | 681 | 924 | 920 | 922 | 887 | 886 | 884 | 92 |  |
| 202 | 208 | 06 | 241 | 242 | 244 | 204 | 49 | 502 | 5005 | 535 | 536 | 538 | 498 | 594 | 600 | 598 | 633 | 34 | 636 | 596 | 692 | 698 | 696 | 731 | 732 | 734 | 694 | 986 | 992 | 990 | 1025 | 1026 | 102 | 8 |  |
| 235 | 2 | 216 | 231 | 232 | 214 | 207 | 52 | 506 | 5105 | 25 | 526 | 50 | 501 | 627 | 04 | 608 | 623 | 624 | 606 | 599 | 72 | 702 | 706 | 721 | 722 | 704 | 697 | 1019 | 996 | 1000 | 1015 | 1016 | 998 | 991 |  |
| 237 | 227 | 218 | 225 | 20 | 215 | 05 | 53 | 5215 | 512 | 519 | 5 | 509 | 499 | 629 | 619 | 610 | 17 | 612 | 607 | 597 | 727 | 717 | 708 | 715 | 710 | 5 | 695 | 1021 | 1011 | 1 | 1009 | 004 | 999 | 989 |  |
| 239 | 229 | 23 | 221 | 219 | 213 | 203 | 53 | 523 | 517 | 515 | 513 | 507 | 497 | 631 | 621 | 615 | 613 | 611 | 605 | 595 | 72 | 719 | 71 | 711 | 709 | 703 | 693 | 1023 | 1013 | 100 | 05 | 003 | 997 | 987 |  |
| 199 | 209 | 222 | 217 | 224 | 33 | 243 | 49 | 503 | 516 | 511 | 518 | 527 | 537 | 591 | 601 | 614 | 609 | 616 | 625 | 635 | 689 | 699 | 712 | 707 | 714 | 723 | 733 | 983 | 993 | 1006 | 1001 | 1008 | 1017 | 1027 |  |
| 197 | 228 | 226 | 211 | 210 | 230 | 245 | 49 | 522 | 5205 | 505 | 504 | 524 | 539 | 589 | 620 | 618 | 603 | 602 | 622 | 637 | 687 | 718 | 716 | 701 | 700 | 720 | 735 | 981 | 1012 | 1010 | 995 | 994 | 101 | 1029 |  |
| 238 | 234 | 236 | 201 | 200 | 198 | 240 | 532 | 528 | 530 | 95 | 494 | 492 | 534 | 630 | 626 | 628 | 593 | 592 | 590 | 632 | 728 | 724 | 726 | 691 | 690 | 688 | 730 | 1022 | 1018 | 1020 | 985 | 984 | 982 | 02 |  |
| 1182 | 11881 | 86 | 1221 | 1222 | 1224 | 184 | 54 | 551 | 54 | 5845 | 5 | 587 | 547 | 790 | 796 | 794 | 829 | 30 | 832 | 792 | 447 | 453 | 451 | 486 | 487 | 489 | 449 | 6 | 12 | 10 | 45 | 46 | 8 | 8 |  |
| 1215 | 11921 | 196 | 1211 | 1212 | 1194 | 1187 | 57 | 55 | 5595 | 574 | 575 | 557 | 55 | 823 | 00 | 804 | 819 | 820 | 802 | 795 | 48 | 457 | 461 | 476 | 477 | 459 | 452 | 39 | 16 | 20 | 35 | 36 | 18 | 11 |  |
| 1217 | 12071 | 11 | 1205 | 1200 | 1195 | 1185 | 58 | 5 | 5615 | 5685 | 563 | 558 | 548 | 825 | 815 | 806 | 813 | 08 | 803 | 793 | 48 | 47 | 463 | 70 | 465 | 460 | 450 | 41 | 31 | 22 | 29 | 24 | 19 | 9 |  |
| 1219 | 12091 | 1203 | 20 | 9 | 1193 | 1183 | 58 | 5725 | 566 | 5645 | 562 | 55 | 546 | 827 | 817 | 811 | 809 | 307 | 01 | 791 | 484 | 474 | 468 | 466 | 464 | 458 | 448 | 43 | 33 | 27 | 25 | 23 | 17 | 7 |  |
| 1179 | 11891 | 1202 | 1197 | 1204 | 1213 | 1223 | 542 | 5525 | 565 | 5605 | 567 | 576 | 586 | 787 | 797 | 810 | 805 | 812 | 21 | 831 | 444 | 454 | 467 | 462 | 469 | 478 | 48 | 3 | 13 | 26 | 21 | 28 | 37 | 47 |  |
| 117 | 1208 | 1206 | 1191 | 1190 | 1210 | 1225 | 54 | 5715 | 5695 | 554 | 553 | 573 | 588 | 785 | 816 | 814 | 799 | 798 | 818 | 833 | 442 | 473 | 471 | 456 | 455 | 475 | 490 |  | 32 | 30 | 15 | 14 | 34 | 49 |  |
| 1218 | 12141 | 1216 | 1181 | 1180 | 1178 | 1220 | 581 | 577 | 5795 | 544 | 543 | 541 | 583 | 826 | 822 | 824 | 789 | 788 | 786 | 828 | 483 | 479 | 481 | 446 | 445 | 443 | 485 | 42 | 38 | 40 | 5 | 4 | 2 | 44 |  |
| 251 | 257 | 5 | 290 | 91 | 293 | 253 | 3 | 355 | 3533 | 388 | 389 | 391 | 351 | 10 | 1090 | 1088 | 1123 | 1124 | 1126 | 1086 | 1133 | 1139 | 1137 | 1172 | 1173 | 1175 | 1135 | 15 | 159 | 157 | 192 | 193 | 195 | 155 |  |
| 28 | 261 | 265 | 280 | 281 | 263 | 25 | 38 | 35 | 363 | 378 | 379 | 361 | 35 | 1117 | 1094 | 1098 | 1113 | 1114 | 1096 | 1089 | 1166 | 1143 | 1147 | 1162 | 1163 | 1145 | 113 | 186 | 163 | 167 | 182 | 183 | 165 | 158 |  |
| 286 | 276 | 267 | 274 | 269 | 64 | 254 | 384 | 37 | 365 | 372 | 367 | 362 | 352 | 1119 | 1109 | 1100 | 1107 | 1102 | 1097 | 1087 | 1168 | 1158 | 1149 | 56 | 1151 | 1146 | 1136 | 188 | 178 | 169 | 176 | 171 | 166 | 156 |  |
| 288 | 278 | 272 | 270 | 268 | 262 | 252 | 386 | 376 | 370 | 368 | 366 | 360 | 350 | 1121 | 1111 | 1105 | 1103 | 1101 | 1095 | 1085 | 1170 | 1160 | 1154 | 1152 | 1150 | 1144 | 1134 | 190 | 180 | 174 | 172 | 170 | 164 | 154 | 2145 |
| 248 | 258 | 271 | 266 | 273 | 282 | 292 | 346 | 356 | 3693 | 364 | 371 | 380 | 390 | 1081 | 1091 | 1104 | 1099 | 1106 | 1115 | 1125 | 1130 | 1140 | 1153 | 1148 | 1155 | 1164 | 1174 | 150 | 160 | 173 | 168 | 175 | 184 | 194 | 2145 |
| 246 | 277 | 275 | 260 | 259 | 279 | 294 | 34 | 375 | 373 | 358 | 357 | 377 | 392 | 1079 | 1110 | 1108 | 1093 | 1092 | 1112 | 1127 | 1128 | 1159 | 1157 | 1142 | 1141 | 1161 | 1176 | 148 | 179 | 177 | 162 | 161 | 181 | 196 | 2145 |
| 287 | 283 | 285 | 250 | 249 | 247 | 289 | 385 | 3813 | 383 | 348 | 347 | 345 | 387 | 1120 | 1116 | 1118 | 1083 | 1082 | 1080 | 1122 | 1169 | 1165 | 1167 | 1132 | 1131 | 1129 | 1171 | 189 | 185 | 187 | 152 | 151 | 149 | 191 | 2145 |
| 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 214 |  |  |  |  |  |  |  | 21455 | 21455 | 21455 | 21455 | 21455 | 2145 | 214 | 214 | 21455 | 21455 | 21455 | 21455 | 21455 | 214 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 |  |

Above two magic squares of order 35 formed by blocks of magic squares of order 7 are with distributions

$$
D_{30 \times 30}:=\{1,2, \ldots, 1224,1225\}
$$

### 2.3 Magic Squares of Order 28

These magic squares are obtained from above by the application of the formula $\frac{a^{2}-b^{2}}{2}, a>b$. Removing the external border of order 7 and then subtracting $\frac{42^{2}-28^{2}}{2}:=490$ from magic squares of orders 42 , we get magic squares of order 28 given by

|  | 1 | 1 | 10990 | 10 | 10990 | 1 | 10 | 10990 | 1 | 10990 |  |  | 10990 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 343 | 335 | 327 | 319 | 11 | 303 | 295 | 588 | 580 | 572 | 564 | 556 | 548 | 540 | 49 | 41 | 33 | 25 | 17 | 9 | 1 | 686 | 678 | 670 | 662 | 654 | 646 | 638 | 90 |
| 10 | 3042 | 296 | 337 | 336 | 328 | 320 | 312 | 5 | 541 | 582 | 581 | 573 | 565 | 557 | 10 | 2 | 43 | 42 | 34 | 26 | 18 | 647 | 639 | 680 | 679 | 671 | 663 | 555 | 10990 |
| 10 | 321 | 313 | 305 | 297 | 338 | 330 | 329 | 566 | 558 | 550 | 542 | 583 | 575 | 574 | 27 | 19 | 11 | 3 | 44 | 36 | 35 | 664 | 656 | 648 | 40 | 681 | 673 | 72 | 10990 |
|  | 331 | 323 | 322 | 314 | 306 | 298 | 339 | 576 | 568 | 567 | 559 | 551 | 543 | 584 | 37 | 29 | 28 | 20 | 12 | 4 | 45 | 674 | 666 | 665 | 57 | 49 | 41 | 82 | 90 |
|  | 2993 | 340 | 33 | 32 | 3 | 315 | 307 | 544 | 58 | 577 | 569 | 561 | 560 | 552 | 5 | 46 | 38 | 30 | 22 | 21 | 13 | 642 | 683 | 675 | 667 | 659 | 58 | 650 | 0990 |
|  | 309 | 308 | 300 | 341 | 333 | 325 | 317 | 554 | 553 | 545 | 586 | 578 | 570 | 562 | 15 | 14 | 6 | 47 | 39 | 31 | 3 | 652 | 65 | 643 | 684 | 676 | 668 | 60 | 0990 |
|  | 3263 | 318 | 310 | 302 | 301 | 342 | 334 | 571 | 563 | 555 | 547 | 546 | 587 | 579 | 32 | 24 | 16 | 8 | 7 | 48 | 40 | 669 | 661 | 653 | 645 | 4 | 685 | 677 | 10990 |
|  | 98 | 90 | 82 | 74 | 66 | 58 | 50 | 637 | 629 | 621 | 613 | 605 | 597 | 589 | 392 | 384 | 376 | 368 | 360 | 352 | 344 | 539 | 531 | 523 | 515 | 507 | 499 | 491 | 90 |
|  | 59 | 51 | 92 | 91 | 83 | 75 | 67 | 59 | 590 | 631 | 630 | 622 | 614 | 606 | 353 | 345 | 386 | 385 | 377 | 369 | 361 | 50 | 492 | 533 | 532 | 524 | 516 | 508 | 90 |
|  | 76 | 68 | 60 | 52 | 93 | 85 | 84 | 615 | 607 | 599 | 591 | 632 | 62 | 623 | 37 | 36 | 35 | 34 | 387 | 379 | 37 | 517 | 509 | 50 | 49 | 53 | 26 | 525 | 90 |
|  | 8 | 78 | 77 | 69 | 61 | 53 | 94 | 625 | 617 | 616 | 608 | 60 | 59 | 633 | 38 | 372 | 37 | 363 | 355 | 347 | 388 | 527 | 519 | 518 | 510 | 50 | 49 | 535 | 90 |
|  | 54 | 95 | 87 | 79 | 71 | 70 | 62 | 593 | 634 | 626 | 618 | 610 | 609 | 601 | 34 | 389 | 381 | 373 | 36 | 364 | 356 | 49 | 53 | 528 | 52 | 512 | 51 | 503 | 1099 |
|  | 64 | 63 | 55 | 96 | 88 | 80 | 72 | 603 | 602 | 594 | 635 | 627 | 619 | 611 | 358 | 357 | 349 | 390 | 382 | 37 | 366 | 505 | 50 | 496 | 537 | 529 | 521 | 513 | 90 |
|  | 81 | 73 | 65 | 57 | 56 | 97 | 89 | 620 | 612 | 604 | 596 | 595 | 636 | 628 | 375 | 367 | 359 | 351 | 350 | 391 | 383 | 522 | 514 | 506 | 498 | 497 | 538 | 53 | 90 |
|  | 7847 | 77 | 768 | 760 | 75 | 74 | 736 | 147 | 139 | 131 | 123 | 115 | 107 | 99 | 49 | 48 | 47 | 466 | 45 | 450 | 2 | 24 | 23 | 229 | 22 | 213 | 205 | 197 | 9 |
|  | 7457 | 737 | 778 | 777 | 769 | 761 | 753 | 108 | 100 | 141 | 140 | 132 | 124 | 116 | 45 | 443 | 48 | 483 | 475 | 467 | 459 | 20 | 198 | 239 | 238 | 23 | 222 | 214 | 90 |
|  | 7627 | 75 | 7 | 738 | 779 | 771 | 770 | 125 | 117 | 109 | 101 | 142 | 134 | 133 | 46 | 460 | 45 | 44 | 485 | 47 | 47 | 22 | 215 | 207 | 199 | 24 | 23 | 231 | 90 |
|  | 7727 | 764 | 763 | 755 | 74 | 739 | 780 | 135 | 127 | 126 | 118 | 110 | 102 | 143 | 47 | 470 | 46 | 46 | 453 | 44 | 48 | 233 | 22 | 22 | 21 | 208 | 200 | 241 | 90 |
|  | 7407 | 781 | 773 | 765 | 757 | 756 | 748 | 103 | 144 | 136 | 128 | 120 | 119 | 111 | 44 | 48 | 47 | 47 | 46 | 46 | 45 | 20 | 24 | 23 | 226 | 218 | 21 | 209 | 10990 |
|  | 7507 | 749 | 741 | 782 | 774 | 766 | 758 | 113 | 112 | 104 | 145 | 137 | 129 | 121 | 45 | 45 | 447 | 48 | 480 | 472 | 464 | 21 | 21 | 20 | 24 | 23 | 22 | 219 | 10990 |
|  | 7677 | 759 | 751 | 743 | 742 | 783 | 775 | 130 | 122 | 114 | 106 | 105 | 146 | 138 | 473 | 465 | 457 | 449 | 448 | 489 | 481 | 228 | 220 | 212 | 204 | 203 | 24 | 23 | 0990 |
|  | 4414 | 33 | 425 | 417 | 409 | 401 | 393 | 29 | 286 | 278 | 270 | 262 | 254 | 246 | 73 | 727 | 719 | 711 | 703 | 695 | 687 | 19 | 18 | 180 | 172 | 16 | 156 | 148 | 90 |
| 1 | 4023 | 394 | 435 | 434 | 426 | 418 | 410 | 255 | 247 | 288 | 287 | 279 | 271 | 263 | 696 | 688 | 729 | 728 | 720 | 712 | 704 | 15 | 149 | 190 | 189 | 18 | 173 | 16 | 10990 |
| 10 | 419 | 411 | 403 | 395 | 436 | 428 | 427 | 272 | 264 | 256 | 248 | 289 | 281 | 280 | 713 | 705 | 697 | 689 | 730 | 722 | 721 | 17 | 166 | 158 | 150 | 19 | 183 | 182 | 90 |
| 10 | 429 | 421 | 420 | 412 | 404 | 396 | 437 | 282 | 27 | 273 | 265 | 257 | 249 | 290 | 723 | 715 | 714 | 706 | 698 | 690 | 731 | 18 | 176 | 175 | 167 | 159 | 151 | 192 | 10990 |
| 1092 | 397 | 438 | 430 | 422 | 414 | 413 | 405 | 250 | 291 | 283 | 275 | 267 | 266 | 258 | 691 | 732 | 724 | 716 | 708 | 707 | 699 | 152 | 193 | 185 | 177 | 169 | 168 | 160 | 109 |
| Tor90 | 4074 | 406 | 398 | 439 | 431 | 423 | 415 | 260 | 259 | 251 | 292 | 284 | 276 | 268 | 701 | 700 | 692 | 733 | 725 | 717 | 709 | 162 | 161 | 153 | 194 | 186 | 178 | 170 | 09 |
|  | 424 | 416 | 408 | 400 | 399 | 440 | 432 | 277 | 269 | 261 | 253 | 252 | 293 | 285 | 718 | 710 | 702 | 694 | 693 | 734 | 726 | 179 | 171 | 163 | 155 | 154 | 195 | 187 | 10990 |
| 28 | 1099010 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 0 | 10990 | 10990 | 10990 | 10990 | 10990 | 10990 | 90 | 10990 | 10990 | 0990 | 0990 | 10990 | 0990 | 90 | 10 |



Above two magic squares of order 28 formed by blocks of magic squares of order 7 are with sequential entries:

$$
D_{25 \times 25}:=\{1,2, \ldots, 783,784\}
$$

### 2.4 Magic Squares of Order 21

These magic squares are obtained from above by the application of the formula $\frac{a^{2}-b^{2}}{2}, a>b$. Removing the external border of order 7 and then subtracting $\frac{35^{2}-21^{2}}{2}:=392$ from magic squares of orders 35 , we get magic squares of order 21 given by
21

| 392 | 384 | 376 | 368 | 360 | 352 | 344 | 49 | 41 | 33 | 25 | 17 | 9 | 1 | 294 | 286 | 278 | 270 | 262 | 254 | 246 | 4641 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 353 | 345 | 386 | 385 | 377 | 369 | 361 | 10 | 2 | 43 | 42 | 34 | 26 | 18 | 255 | 247 | 288 | 287 | 279 | 271 | 263 | 4641 |
| 370 | 362 | 354 | 346 | 387 | 379 | 378 | 27 | 19 | 11 | 3 | 44 | 36 | 35 | 272 | 264 | 256 | 248 | 289 | 281 | 280 | 4641 |
| 380 | 372 | 371 | 363 | 355 | 347 | 388 | 37 | 29 | 28 | 20 | 12 | 4 | 45 | 282 | 274 | 273 | 265 | 257 | 249 | 290 | 4641 |
| 348 | 389 | 381 | 373 | 365 | 364 | 356 | 5 | 46 | 38 | 30 | 22 | 21 | 13 | 250 | 291 | 283 | 275 | 267 | 266 | 258 | 4641 |
| 358 | 357 | 349 | 390 | 382 | 374 | 366 | 15 | 14 | 6 | 47 | 39 | 31 | 23 | 260 | 259 | 251 | 292 | 284 | 276 | 268 | 4641 |
| 375 | 367 | 359 | 351 | 350 | 391 | 383 | 32 | 24 | 16 | 8 | 7 | 48 | 40 | 277 | 269 | 261 | 253 | 252 | 293 | 285 | 4641 |
| 147 | 139 | 131 | 123 | 115 | 107 | 99 | 245 | 237 | 229 | 221 | 213 | 205 | 197 | 343 | 335 | 327 | 319 | 311 | 303 | 295 | 4641 |
| 108 | 100 | 141 | 140 | 132 | 124 | 116 | 206 | 198 | 239 | 238 | 230 | 222 | 214 | 304 | 296 | 337 | 336 | 328 | 320 | 312 | 4641 |
| 125 | 117 | 109 | 101 | 142 | 134 | 133 | 223 | 215 | 207 | 199 | 240 | 232 | 231 | 321 | 313 | 305 | 297 | 338 | 330 | 329 | 4641 |
| 135 | 127 | 126 | 118 | 110 | 102 | 143 | 233 | 225 | 224 | 216 | 208 | 200 | 241 | 331 | 323 | 322 | 314 | 306 | 298 | 339 | 4641 |
| 103 | 144 | 136 | 128 | 120 | 119 | 111 | 201 | 242 | 234 | 226 | 218 | 217 | 209 | 299 | 340 | 332 | 324 | 316 | 315 | 307 | 4641 |
| 113 | 112 | 104 | 145 | 137 | 129 | 121 | 211 | 210 | 202 | 243 | 235 | 227 | 219 | 309 | 308 | 300 | 341 | 333 | 325 | 317 | 4641 |
| 130 | 122 | 114 | 106 | 105 | 146 | 138 | 228 | 220 | 212 | 204 | 203 | 244 | 236 | 326 | 318 | 310 | 302 | 301 | 342 | 334 | 4641 |
| 196 | 188 | 180 | 172 | 164 | 156 | 148 | 441 | 433 | 425 | 417 | 409 | 401 | 393 | 98 | 90 | 82 | 74 | 66 | 58 | 50 | 4641 |
| 157 | 149 | 190 | 189 | 181 | 173 | 165 | 402 | 394 | 435 | 434 | 426 | 418 | 410 | 59 | 51 | 92 | 91 | 83 | 75 | 67 | 4641 |
| 174 | 166 | 158 | 150 | 191 | 183 | 182 | 419 | 411 | 403 | 395 | 436 | 428 | 427 | 76 | 68 | 60 | 52 | 93 | 85 | 84 | 4641 |
| 184 | 176 | 175 | 167 | 159 | 151 | 192 | 429 | 421 | 420 | 412 | 404 | 396 | 437 | 86 | 78 | 77 | 69 | 61 | 53 | 94 | 4641 |
| 152 | 193 | 185 | 177 | 169 | 168 | 160 | 397 | 438 | 430 | 422 | 414 | 413 | 405 | 54 | 95 | 87 | 79 | 71 | 70 | 62 | 4641 |
| 162 | 161 | 153 | 194 | 186 | 178 | 170 | 407 | 406 | 398 | 439 | 431 | 423 | 415 | 64 | 63 | 55 | 96 | 88 | 80 | 72 | 4641 |
| 179 | 171 | 163 | 155 | 154 | 195 | 187 | 424 | 416 | 408 | 400 | 399 | 440 | 432 | 81 | 73 | 65 | 57 | 56 | 97 | 89 | 4641 |
| 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 464 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 |


| 21 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 4641 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 349 | 355 | 353388 | 389 | 391 | 351 | 6 | 12 | 10 | 45 | 46 | 48 | 8 | 251 | 257 | 255 | 290 | 291 | 293 | 253 | 4641 |
| 382 | 3593 | 363378 | 379 | 361 | 354 | 39 | 16 | 20 | 35 | 36 | 18 | 11 | 284 | 261 | 265 | 280 | 281 | 263 | 256 | 1 |
| 384 | 374 | 365372 | 367 | 362 | 352 | 41 | 31 | 22 | 29 | 24 | 19 | 9 | 286 | 276 | 267 | 274 | 269 | 264 | 254 | 4641 |
| 386 | 376 | 370368 | 366 | 360 | 350 | 43 | 33 | 27 | 25 | 23 | 17 | 7 | 288 | 278 | 272 | 270 | 268 | 262 | 252 | 4641 |
| 346 | 356 | 369364 | 371 | 380 | 390 | 3 | 13 | 26 | 21 | 28 | 37 | 47 | 248 | 258 | 271 | 266 | 273 | 282 | 292 | 4641 |
| 344 | 375 | 373358 | 357 | 377 | 392 | 1 | 32 | 30 | 15 | 14 | 34 | 49 | 246 | 277 | 275 | 260 | 259 | 279 | 294 | 4641 |
| 385 | 3813 | 383348 | 347 | 345 | 387 | 42 | 38 | 40 | 5 | 4 | 2 | 44 | 287 | 283 | 285 | 250 | 249 | 247 | 289 |  |
| 104 | 11010 | 108143 | 144 | 146 | 106 | 202 | 208 | 206 | 241 | 242 | 244 | 204 | 300 | 306 | 304 | 339 | 340 | 342 | 302 |  |
| 137 | 1141 | 118133 | 134 | 116 | 109 | 235 | 212 | 216 | 231 | 232 | 214 | 207 | 333 | 310 | 314 | 329 | 330 | 312 | 305 | 4641 |
| 139 | $1 2 9 \longdiv { 1 2 0 }$ | 120127 | 122 | 117 | 107 | 237 | 227 | 218 | 225 | 220 | 215 | 205 | 335 | 325 | 316 | 323 | 318 | 313 | 303 | 4641 |
| 141 | 13112 | 125123 | 121 | 115 | 105 | 239 | 229 | 223 | 221 | 219 | 213 | 203 | 337 | 327 | 321 | 319 | 317 | 311 | 301 | 4641 |
| 101 | 11112 | 124119 | 126 | 135 | 145 | 199 | 209 | 222 | 217 | 224 | 233 | 243 | 297 | 307 | 320 | 315 | 322 | 331 | 341 | 4641 |
| 99 | 13012 | 128113 | 112 | 132 | 147 | 197 | 228 | 226 | 211 | 210 | 230 | 245 | 295 | 326 | 324 | 309 | 308 | 328 | 343 | 46 |
| 140 | 13613 | 138103 | 102 | 100 | 142 | 238 | 234 | 236 | 201 | 200 | 198 | 240 | 336 | 332 | 334 | 299 | 298 | 296 | 338 | 4641 |
| 153 | 15915 | 157192 | 193 | 195 | 155 | 398 | 404 | 402 | 437 | 438 | 440 | 400 | 55 | 61 | 59 | 94 | 95 | 97 | 57 | 4641 |
| 186 | 163167 | 167182 | 183 | 165 | 158 | 431 | 408 | 412 | 427 | 428 | 410 | 403 | 88 | 65 | 69 | 84 | 85 | 67 | 60 |  |
| 188 | 17816 | 169176 | 171 | 166 | 156 | 433 | 423 | 414 | 421 | 416 | 411 | 401 | 90 | 80 | 71 | 78 | 73 | 68 | 58 |  |
| 190 | 180 | 174172 | 170 | 164 | 154 | 435 | 425 | 419 | 417 | 415 | 409 | 399 | 92 | 82 | 76 | 74 | 72 | 66 | 56 | 4641 |
| 150 | 16017 | 173168 | 175 | 184 | 194 | 395 | 405 | 418 | 413 | 420 | 429 | 439 | 52 | 62 | 75 | 70 | 77 | 86 | 96 | I |
| 148 | 17917 | 177162 | 161 | 181 | 196 | 393 | 424 | 422 | 407 | 406 | 426 | 441 | 50 | 81 | 79 | 64 | 63 | 83 | 98 | 4641 |
| 189 | 18518 | 187152 | 151 | 149 | 191 | 434 | 430 | 432 | 397 | 396 | 394 | 436 | 91 | 87 | 89 | 54 | 53 | 51 | 93 | 4641 |
| 4641 | 46414 | 46414641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 |

Above two magic squares of order 21 formed by blocks of magic squares of order 7 are with sequential entries:

$$
D_{20 \times 20}:=\{1,2, \ldots, 440,441\}
$$

## 3 Pandiagonal Magic Squares Multiples 7

This section brings pandiagonal magic squares multiples 7. It includes magic squares of orders $21,28,35$ and 49 . The details are excluded as these are studied extensively in author's previous works [5, 7, 20].

### 3.1 Pandiagonal Magic Square of Order 21

Below is a pandiagonal magic squares of order 21.

|  | pan | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 46 | 46 | 4641 | 4641 | 46 | , | 46 | 46 |  |  |  | 4641 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 111 | 155 | 243 | 265 | 375 | 397 | 3 | 110 | 154 | 242 | 266 | 374 | 398 | 2 | 109 | 156 | 241 | 267 | 373 | 399 | 4641 |
| 4641 | 370 | 396 | 619 | 106 | 153 | 239 | 264 | 371 | 395 | 520 | 108 | 152 | 238 | 263 | 372 | 394 | 21 | 107 | 151 | 240 | 262 | 4641 |
| 4641 | 237 | 260 | 369 | 391 | 18 | 124 | 148 | 236 | 259 | 368 | 392 | 17 | 125 | 150 | 235 | 261 | 367 | 393 | 16 | 126 | 149 |  |
|  | 123 | 166 | 232 | 258 | 365 | 390 | 13 | 122 | 167 | 234 | 257 | 364 | 389 | 14 | 121 | 168 | 233 | 256 | 366 | 388 | 15 |  |
|  | 386 | 12 | 118 | 165 | 250 | 253 | 363 | 385 | 11 | 119 | 164 | 251 | 255 | 362 | 387 | 10 | 120 | 163 | 252 | 254 | 361 |  |
|  | 271 | 358 | 384 | 8 | 117 | 160 | 249 | 272 | 360 | 383 | 7 | 116 | 161 | 248 | 273 | 359 | 382 | 9 | 115 | 162 | 247 | 4641 |
|  | 159 | 244 | 270 | 376 | 379 | 6 | 113 | 158 | 245 | 269 | 377 | 381 | 5 | 112 | 157 | 246 | 268 | 378 | 380 | 4 | 114 |  |
|  | 43 | 90 | 134 | 222 | 286 | 354 | 418 | 45 | 89 | 133 | 221 | 287 | 353 | 419 | 44 | 88 | 135 | 220 | 28 | 352 | 420 |  |
|  | 349 | 417 | 61 | 85 | 132 | 218 | 285 | 350 | 416 | 62 | 87 | 131 | 217 | 284 | 35 | 415 | 63 | 86 | 130 | 219 | 283 |  |
|  | 216 | 281 | 348 | 412 | 60 | 103 | 127 | 215 | 280 | 347 | 413 | 59 | 104 | 129 | 21 | 282 | 346 | 41 | 58 | 105 | 128 |  |
|  | 102 | 145 | 211 | 279 | 344 | 411 | 55 | 101 | 146 | 213 | 278 | 343 | 410 | 56 | 100 | 147 | 212 | 277 | 34 | 409 | 57 |  |
|  | 407 | 54 | 97 | 144 | 229 | 274 | 342 | 406 | 53 | 98 | 143 | 230 | 276 | 341 | 408 | 52 | 99 | 142 | 231 | 275 | 340 |  |
|  | 292 | 337 | 405 | 50 | 96 | 139 | 228 | 293 | 339 | 404 | 49 | 95 | 140 | 227 | 29 | 338 | 403 | 51 | 94 | 141 | 226 |  |
|  | 138 | 223 | 291 | 355 | 400 | 48 | 92 | 137 | 224 | 290 | 356 | 402 | 47 | 91 | 136 | 225 | 289 | 357 | 401 | 46 | 93 |  |
|  | 22 | 69 | 176 | 201 | 307 | 333 | 439 | 24 | 68 | 175 | 200 | 308 | 332 | 440 | 23 | 67 | 177 | 199 | 30 | 331 | 441 |  |
| 40 | 328 | 438 | 40 | 64 | 174 | 197 | 306 | 329 | 437 | 41 | 66 | 173 | 196 | 305 | 330 | 436 | 42 | 65 | 172 | 198 | 304 | 4641 |
|  | 195 | 302 | 327 | 433 | 39 | 82 | 169 | 194 | 301 | 326 | 434 | 38 | 83 | 171 | 193 | 303 | 325 | 435 | 37 | 84 | 170 |  |
|  | 81 | 187 | 190 | 300 | 323 | 432 | 34 | 80 | 188 | 192 | 299 | 322 | 431 | 35 | 79 | 189 | 191 | 298 | 32 | 430 | 36 |  |
| 4641 | 428 | 33 | 76 | 186 | 208 | 295 | 321 | 427 | 32 | 77 | 185 | 209 | 297 | 320 | 429 | 31 | 78 | 184 | 210 | 296 | 319 | 4641 |
| 1 | 313 | 316 | 6426 | 29 | 75 | 181 | 207 | 314 | 318 | 425 | 28 | 74 | 182 | 206 | 315 | 317 | 424 | 30 | 73 | 183 | 205 | 4641 |
|  | 180 | 202 | 2312 | 334 | 421 | 27 | 71 | 179 | 203 | 311 | 335 | 423 | 26 | 70 | 178 | 204 | 310 | 336 | 422 | 25 | 72 |  |
|  | 4641 | 4641 | 14641 | 4641 | 46 | 4641 | 464 | 4641 | 4641 | 4641 | 46 | 4641 | 46 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 | 4641 |  |

The blocks of order 7 are of equal sums magic squares, i.e., $M_{7 \times 7}:=1547$

### 3.2 Pandiagonal Magic Square of Order 28

Below is a pandiagonal magic squares of order 28.

|  | pan | 10 | 10990 | 10990 |  | 10990 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10990 | 343 | 335 | 327 | 319 | 311 | 303 | 295 | 588 | 580 | 572 | 564 | 556 | 548 | 540 | 49 | 41 | 33 | 25 | 17 | 9 | 1 | 686 | 678 | 670 | 662 | 654 | 646 | 638 | 10990 |
| 10990 | 30 | 29 | 337 | 336 | 328 | 32 | 312 | 54 | 541 | 582 | 581 | 57 | 565 | 557 | 10 | 2 | 43 | 42 | 34 | 26 | 18 | 647 | 39 | 680 | 67 | 67 | 663 | 55 | 10990 |
|  | 321 | 313 | 305 | 297 | 338 | 33 | 329 | 566 | 558 | 550 | 5 | 583 | 57 | 74 | 27 | 19 | 11 | 3 | 44 | 36 | 35 | 664 | 56 | 48 | 640 | 681 | 73 | 672 | 10990 |
|  | 331 | 323 | 322 | 314 | 30 | 29 | 339 | 576 | 568 | 567 | 559 | 551 | 543 | 584 | 37 | 29 | 28 | 20 | 12 |  | 45 | 674 | 66 | 65 | 657 | 649 | 641 | 682 | 109 |
|  | 29 | 340 | 332 | 324 | 316 | 315 | 307 | 5 | 585 | 577 | 569 | 561 | 560 | 552 | 5 | 46 | 38 | 30 | 22 | 21 | 13 | 642 | 683 | 675 | 667 | 659 | 58 | 50 | 10990 |
|  | 30 | 308 | 300 | 341 | 333 | 325 | 317 | 554 | 553 | 545 | 586 | 578 | 570 | 562 | 15 | 14 | 6 | 47 | 39 | 31 | 23 | 652 | 651 | 643 | 684 | 76 | 668 | 60 | 10990 |
|  | 32 | 318 | 310 | 302 | 301 | 342 | 334 | 571 | 563 | 555 | 547 | 546 | 587 | 579 | 32 | 24 | 16 | 8 | 7 | 48 | 40 | 669 | 661 | 653 | 64 | 64 | 685 | 67 | 10990 |
|  | 98 | 90 | 82 | 74 | 66 | 58 | 50 | 63 | 629 | 621 | 613 | 60 | 597 | 589 | 392 | 384 | 376 | 368 | 360 | 35 | 344 | 539 | 53 | 523 | 515 | 50 | 49 | 491 | 10990 |
|  | 59 | 51 | 92 | 91 | 83 | 75 | 67 | 5 | 590 | 631 | 63 | 622 |  | 06 | 35 | 345 | 386 | 385 | 377 | 369 | 361 | 500 | 492 | 53 | 53 | 52 | 51 | 508 |  |
|  | 76 | 68 | 60 | 52 | 93 | 85 | 84 | 615 | 607 | 599 | 59 | 632 | 624 | 23 | 370 | 362 | 35 | 346 | 387 | 379 | 378 | 517 | 509 | 50 | 49 | 53 | 526 | 5 | 10990 |
|  | 86 | 78 | 77 | 69 | 61 | 53 | 94 | 62 | 617 | 616 | 60 | 600 | 592 | 33 | 380 | 372 | 371 | 363 | 355 | 347 | 388 | 527 | 519 | 518 | 510 | 50 | 49 | 5 | 10990 |
|  | 54 | 95 | 87 | 79 | 71 | 70 | 62 | 593 | 63 | 626 | 618 | 610 | 609 | 601 | 348 | 389 | 381 | 373 | 365 | 364 | 356 | 495 | 536 | 528 | 520 | 512 | 511 | 503 | 10990 |
|  | 64 | 63 | 55 | 96 | 88 | 80 | 72 | 603 | 602 | 594 | 635 | 627 | 619 | 611 | 358 | 357 | 349 | 390 | 0382 | 374 | 366 | 505 | 50 | 496 | 537 | 529 | 521 | 513 | 10990 |
|  | 81 | 73 | 65 | 57 | 56 | 97 | 89 | 620 | 612 | 604 | 596 | 595 | 636 | 628 | 375 | 367 | 359 | 351 | 1350 | 391 | 383 | 522 | 514 | 506 | 498 | 497 | 538 | 53 |  |
|  | 78 | 776 | 768 | 760 | 752 | 74 | 736 | 14 | 139 | 131 | 12 | 115 | 107 | 99 | 49 | 482 | 47 | 466 | 458 | 45 | 442 | 245 | 237 | 22 | 22 | 213 | 205 | 197 |  |
|  | 74 | 73 | 778 | 777 | 769 | 76 | 753 | 108 | 100 | 141 | 140 | 13 | 124 | 116 | 451 | 443 | 48 | 483 | 475 | 467 | 45 | 206 | 19 | 23 | 23 | 230 | 222 | 214 | 10990 |
|  | 76 | 75 | 746 | 738 | 779 | 77 | 770 | 125 | 117 | 109 | 101 | 142 | 4 | 133 | 468 | 460 | 45 | 244 | 485 | 47 | 476 | 223 | 21 | 20 | 19 | 240 | 2 | 231 |  |
|  | 77 | 76 | 763 | 75 | 747 | 73 | 78 | 135 | 127 | 126 | 118 | 110 | 2 | 143 | 478 | 470 | 46 | 46 | 453 | 445 | 486 | 23 | 22 | 22 | 216 | 208 | 200 | 241 | 10990 |
|  | 74 | 78 | 77 | 765 | 75 | 75 | 74 | 103 | 144 | 136 | 128 | 120 | 119 | 111 | 446 | 487 | 479 | 471 | 463 | 62 | 454 | 20 | 242 | 23 | 22 | 21 | 21 | 209 | 109 |
|  | 750 | 749 | 74 | 782 | 77 | 766 | 758 | 113 | 112 | 104 | 145 | 137 | 129 | 121 | 456 | 455 | 44 | 488 | 480 | 472 | 464 | 211 | 210 | 20 | 243 | 235 | 227 | 21 | 10990 |
|  | 767 | 759 | 751 | 743 | 742 | 783 | 775 | 130 | 122 | 114 | 106 | 105 | 146 | 138 | 473 | 465 | 457 | 449 | 9448 | 489 | 481 | 228 | 220 | 212 | 20 | 203 | 24 | 23 | 10990 |
|  | 4 | 43 | 425 | 17 | 409 | 401 | 39 | 29 | 286 | 278 | 270 | 262 | 254 | 246 | 73 | 72 | 719 | 711 | 703 | 695 | 687 | 19 | 188 | 180 | 172 | 164 | 156 | 148 | 10990 |
|  | 4 | 39 | 435 | 434 | 426 | 418 | 410 | 255 | 247 | 288 | 87 | 279 | 71 | 263 | 696 | 688 | 729 | 728 | 720 | 712 | 704 | 157 | 149 | 19 | 189 | 18 | 173 | 165 | 109 |
|  | 41 | 411 | 403 | 395 | 36 | 428 | 42 | 27 | 264 | 256 | 248 | 289 | 1 | 280 | 713 | 705 | 69 | 789 | 730 | 72 | 72 | 17 | 166 | 158 | 150 | 191 | 18 | 182 | 109 |
|  | 429 | 421 | 420 | 412 | 404 | 39 | 437 | 282 | 274 | 273 | 265 | 257 | 249 | 290 | 723 | 715 | 714 | 706 | 698 | 690 | 731 | 184 | 176 | 175 | 167 | 159 | 15 | 19 | 10990 |
| 10 | 39 | 438 | 430 | 422 | 414 | 413 | 405 | 250 | 291 | 283 | 275 | 267 | 266 | 258 | 691 | 732 | 72 | 716 | 708 | 707 | 699 | 152 | 193 | 185 | 177 | 169 | 168 | 16 | 10 |
| 10 | 40 | 406 | 398 | 439 | 431 | 423 | 415 | 260 | 259 | 251 | 292 | 284 | 276 | 268 | 701 | 700 | 692 | 2733 | 725 | 717 | 709 | 162 | 161 | 153 | 194 | 186 | 178 | 17 | 10 |
|  | 424 | 416 | 408 | 400 | 399 | 440 | 432 | 277 | 269 | 261 | 253 | 252 | 293 | 285 | 718 | 710 | 702 | 294 | 4693 | 734 | 726 | 179 | 171 | 163 | 155 | 154 | 195 | 187 | 109 |
| 28 | 1099 | 10 | 109 | 109 | 10 |  |  | 0 | 10990 | 10 |  |  |  |  | 10990 | 010990 | 0 | 0 10990 | 010990 |  |  |  |  |  |  |  |  |  |  |

The blocks of order 7 are with different sums pandiagonal magic squares. It is the same magic square given in previous section.

### 3.3 Pandiagonal Magic Square of Order 35

Below is a pandiagonal magic squares of order 35.

|  |  |  | 21455 | 21455 | 21455 | 21455 | 1455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 901 | 649 | 253 | 1081 | 865 | 433 | 109 | 685 | 181 | 1189 | 829 | 469 | 1 | 937 | 73 | 217 | 505 | 613 | 721 | 1009 | 1153 | 289 | 1225 | 75 | 39 | 37 | 1045 | 541 | 1117 | 793 | 361 | 145 | 973 | 577 | 325 | 21455 |
| 2 m 55 | 44 | 118 | 879 | 656 | 264 | 1058 | 871 | 14 | 911 | 692 | 195 | 1161 | 839 | 479 | 1001 | 1149 | 103 | 213 | 497 | 610 | 718 | 1017 | 555 | 296 | 119 | 770 | 407 | 47 | 588 | 332 | 109 | 802 | 373 | 151 | 950 |  |
|  | 1069 | 848 | 451 | 130 | 888 | 634 | 271 | 811 | 489 | 24 | 924 | 666 | 202 | 1175 | 602 | 715 | 998 | 1141 | 99 | 243 | 493 | 420 | 57 | 1027 | 27 | 310 | 1206 | 74 | 163 | 956 | 565 | 343 | 1102 | 780 | 382 |  |
|  | 643 | 249 | 1076 | 859 | 428 | 136 | 900 | 176 | 1182 | 25 | 461 | 34 | 934 | 679 | 239 | 52 | 598 | 707 | 995 | 1138 | 91 | 1220 | 51 | 394 | 70 | 1037 | 537 | 82 | 787 | 360 | 172 | 968 | 571 | 320 | 113 |  |
|  | 113 | 906 | 655 | 258 | 105 | 866 | 439 | 94 | 689 | 189 | 1156 | 832 | 475 | 6 | 1135 | 88 | 231 | 519 | 628 | 03 | 987 | 54 | 292 | 1192 | 65 | 401 | 44 | 1050 | 326 | 1090 | 798 | 367 | 150 | 977 | 83 |  |
| 2 m 45 | 84 | 446 | 124 | 883 | 661 | 270 | 106 | 48 | 20 | 916 | 699 | 199 | 1169 | 806 | 733 | 983 | 1127 | 85 | 228 | 511 | 624 | 51 | 1024 | 560 | 302 | 1202 | 737 | 15 | 955 | 592 | 33 | 096 | 775 | 78 | 157 |  |
| 2 m 45 | 276 | 1075 | 853 | 424 | 131 | 894 | 638 | 1179 | 819 | 456 | 27 | 930 | 67 | 209 | 508 | 616 | 729 | 1013 | 1123 | 77 | 225 | 747 | 387 | 65 | 1031 | 534 | 315 | 1212 | 355 | 168 | 962 | 570 | 347 | 1108 | 781 |  |
|  | 283 | 1197 | 750 | 403 | 56 | 104 | 558 | 109 | 805 | 372 | 152 | 947 | 590 | 331 | 907 | 653 | 256 | 1055 | 868 | 437 | 115 | 691 | 194 | 1163 | 836 | 480 | 13 | 914 | 90 | 216 | 524 | 619 | 714 | 81 | 1147 |  |
|  | 1036 | 554 | 313 | 1193 | 742 | 400 | 53 | 562 | 345 | 101 | 779 | 385 | 162 | 957 | 448 | 122 | 885 | 662 | 268 | 1061 | 845 | 25 | 923 | 669 | 20 | 1174 | 813 | 486 | 94 | 112 | 97 | 230 | 496 | 29 | 724 | 1455 |
|  | 392 | 50 | 1033 | 546 | 309 | 1223 | 738 | 175 | 96 | 572 | 317 | 1115 | 786 | 359 | 1073 | 851 | 425 | 133 | 392 | 640 | 277 | 82 | 46 | 31 | 93 | 678 | 17 | 1181 | 601 | 73 | 100 | 113 | 71 | 237 | 510 | 21455 |
|  | 1219 | 768 | 388 | 42 | 1030 | 543 | 301 | 800 | 366 | 149 | 980 | 58 | 327 | 1087 | 647 | 255 | 1082 | 863 | 431 | 110 | 903 | 188 | 115 | 83 | 47 | 8 | 941 | 69 | 211 | 517 | 615 | 706 | 101 | 1144 | 84 | 2145 |
|  | 540 | 298 | 121 | 764 | 418 | 38 | 1022 | 337 | 1097 | 772 | 380 | 156 | 954 | 595 | 116 | 88 | 65 | 262 | 1060 | 872 | 443 | 918 | 69 | 20 | 116 | 80 | 48 | 19 | 1154 | 94 | 224 | 491 | 622 | 720 | 986 |  |
|  | 68 | 1018 | 532 | 29 | 1208 | 756 | 414 | 96 | 56 | 350 | 1107 | 78 | 352 | 170 | 85 | 45 | 128 | 886 | 635 | 273 | 106 | 459 | 26 | 92 | 67 | 206 | 118 | 81 | 727 | 1000 | 1126 | 104 | 234 | 504 | 596 |  |
|  | 753 | 406 | 64 | 1048 | 528 | 287 | 1205 | 362 | 142 | 975 | 576 | 324 | 1120 | 792 | 250 | 1078 | 85 | 430 | 137 | 898 | 641 | 1186 | 83 | 46 | 4 | 93 | 68 | 18 | 514 | 609 | 701 | 1007 | 1140 | 76 | 244 |  |
|  | 69 | 198 | 1166 | 810 | 483 | 17 | 920 | 96 | 229 | 498 | 626 | 725 | 993 | 12 | 300 | 119 | 769 | 409 | 49 | 101 | 552 | 108 | 777 | 365 | 158 | 966 | 589 | 348 | 884 | 665 | 267 | 1062 | 842 | 450 | 121 |  |
|  | 28 | 927 | 675 | 207 | 1178 | 816 | 460 | 100 | 1133 | 74 | 23 | 509 | 603 | 731 | 102 | 52 | 307 | 121 | 741 | 419 | 59 | 581 | 344 | 118 | 773 | 357 | 155 | 963 | 422 | 135 | 891 | 639 | 280 | 1072 | 852 |  |
|  | 828 | 466 | 5 | 938 | 682 | 185 | 118 | 614 | 708 | 101 | 114 | 83 | 214 | 16 | 391 | 69 | 1039 | 53 | 28 | 121 | 75 | 147 | 960 | 578 | 33 | 1114 | 80 | 353 | 08 | 862 | 432 | 107 | 905 | 646 | 254 |  |
|  | 192 | 1165 | 837 | 478 | 11 | 915 | 693 | 22 | 49 | 621 | 719 | 988 | 115 | 95 | 119 | 762 | 405 | 41 | 104 | 54 | 29 | 799 | 38 | 143 | 95 | 57 | 33 | 1106 | 660 | 26 | 105 | 875 | 442 | 117 | 877 |  |
|  | 92 | 670 | 203 | 1172 | 815 | 487 | 23 | 112 | 101 | 235 | 503 | 599 | 726 | 999 | 559 | 304 | 1204 | 736 | 412 | 55 | 102 | 330 | 110 | 79 | 379 | 173 | 948 | 56 | 127 | 887 | 632 | 275 | 066 | 849 | 455 |  |
|  | 465 | 32 | 933 | 676 | 180 | 1183 | 822 | 704 | 1006 | 1139 | 78 | 241 | 515 | 608 | 62 | 1035 | 531 | 314 | 121 | 749 | 386 | 978 | 563 | 322 | 1100 | 788 | 371 | 169 | 85 | 429 | 140 | 897 | 642 | 247 | 08 |  |
|  | 1160 | 833 | 472 | 10 | 942 | 688 | 186 | 521 | 620 | 713 | 984 | 1146 | 89 | 218 | 759 | 399 | 36 | 1042 | 545 | 286 | 122 | 368 | 161 | 97 | 593 | 318 | 1092 | 785 | 257 | 1052 | 870 | 436 | 114 | 910 | 652 |  |
|  | 1105 | 776 | 384 | 164 | 959 | 56 | 342 | 878 | 637 | 60 | 1068 | 861 | 49 | 138 | 674 | 210 | 1177 | 817 | 45 | 30 | 926 | 102 | 233 | 501 | 60 | 72 | 997 | 1130 | 30 | 1209 | 743 | 416 | 60 | 1028 | 529 |  |
|  | 574 | 316 | 1112 | 790 | 356 |  | 69 | 44 | 134 | 908 | 33 | 52 | 1065 | 858 | 2 | 940 | 681 | 184 | 1190 | 82 | 467 | 1008 | 1137 | 80 | 24 | 513 | 60 | 705 | 1040 | 538 | 284 | 1216 | 75 | 39 | 66 |  |
|  | 146 | 979 | 584 | 329 | 1086 | 797 | 370 | 1057 | 855 | 438 | 126 | 904 | 63 | 248 | 840 | 477 | 12 | 912 | 695 | 191 | 116 | 618 | 711 | 985 | 1148 | 87 | 220 | 522 | 40 | 43 | 1046 | 550 | 293 | 119 | 76 |  |
|  | 771 | 377 | 160 | 951 | 594 | 339 | 1099 | 659 | 78 | 1053 | 847 | 435 | 123 | 896 | 205 | 1171 | 814 | 490 | 22 | 922 | 667 | 227 | 500 | 627 | 723 | 991 | 1125 | 98 | 1203 | 739 | 41 | 54 | 1023 | 556 | 305 |  |
|  | 349 | 1109 | 784 | 351 | 167 | 965 | 566 | 120 | 93 | 651 | 74 | 1083 | 843 | 427 | 932 | 67 | 177 | 1185 | 82 | 46 | 35 | 1131 | 75 | 238 | 507 | 60 | 732 | 1003 | 533 | 31 | 1215 | 74 | 389 | 61 | 103 |  |
|  | 972 | 580 | 321 | 11 | 794 | 364 | 141 | 873 | 423 | 112 | 90 | 648 | 266 | 1079 | 47 | 9 | 94 | 687 | 187 | 1157 | 835 | 710 | 1012 | 1143 | 81 | 215 | 518 | 612 | 39 | 104 | 544 | 288 | 122 | 760 | 398 |  |
| 21455 | 374 | 154 | 946 | 587 | 335 | 1091 | 804 | 263 | 1071 | 869 | 453 | 108 | 882 | 645 | 1167 | 807 | 485 | 16 | 919 | 700 | 197 | 495 | 623 | 717 | 990 | 1152 | 93 | 221 | 766 | 410 | 48 | 1019 | 55 | 299 | 1198 |  |
|  | 79 | 245 | 512 | 607 | 702 | 10 | 1136 | 312 | 1213 | 746 | 390 | 63 | 1032 | 535 | 111 | 789 | 358 | 171 | 970 | 573 | 319 | 895 | 636 | 279 | 107 | 854 | 421 | 132 | 66 | 18 | 117 | 823 | 476 | 29 | 943 | 245 |
|  | 982 | 1150 | 86 | 219 | 525 | 617 | 712 | 1043 | 542 | 290 | 1222 | 758 | 396 | 40 | 58 | 328 | 1089 | 796 | 369 | 148 | 976 | 43 | 106 | 90 | 650 | 251 | 108 | 86 | 21 | 93 | 698 | 178 | 116 | 820 | 473 | 145 |
|  | 630 | 722 | 992 | 1122 | 100 | 226 | 499 | 408 | 46 | 1020 | 553 | 297 | 1200 | 767 | 159 | 95 | 591 | 340 | 1098 | 774 | 376 | 1056 | 874 | 44 | 119 | 87 | 657 | 265 | 81 | 470 | 18 | 93 | 694 | 208 | 115 |  |
|  | 240 | 506 | 604 | 735 | 1002 | 1132 | 72 | 1207 | 745 | 417 | 58 | 1026 | 530 | 308 | 783 | 35 | 166 | 964 | 568 | 346 | 1110 | 631 | 272 | 1070 | 846 | 454 | 129 | 889 | 20 | 1188 | 808 | 462 | 15 | 928 | 88 | 2145 |
| 21455 | 1142 | 82 | 212 | 520 | 611 | 709 | 1015 | 536 | 285 | 1218 | 752 | 395 | 67 | 1038 | 323 | 1116 | 795 | 363 | 144 | 971 | 579 | 139 | 899 | 644 | 246 | 1077 | 860 | 426 | 92 | 683 | 196 | 118 | 838 | 458 | 7 | 245 |
| 2145 | 716 | 989 | 1155 | 92 | 222 | 492 | 625 | 45 | 1047 | 548 | 291 | 1195 | 763 | 402 | 949 | 586 | 334 | 1093 | 801 | 375 | 153 | 867 | 440 | 111 | 909 | 654 | 259 | 1051 | 488 | 3 | 917 | 680 | 193 | 1176 | 834 |  |
|  | 502 | 597 | 730 | 996 | 1129 | 105 | 232 | 740 | 413 | 52 | 1025 | 557 | 303 | 1201 | 381 | 165 | 958 | 564 | 341 | 1104 | 778 | 269 | 1064 | 841 | 447 | 125 | 881 | 664 | 1173 | 826 | 484 | 33 | 913 | 672 | 190 |  |
|  | 21455 | 21455 | 214 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 21455 | 214 | 214 | 214 | 214 | 214 | 21455 | 21455 | 214 | 214 | 21455 | 21455 | 21455 | 21455 | 21455 |

The blocks of order 7 are equal sums pandiagonal magic squares, i.e., $M_{7 \times 7}:=4291$.
It is constructed based on magic rectangle of order $5 \times 7$. blocks of order 5 given in previous work [30] is also constructed with same procedures. See the author's work [20].

### 3.4 Pandiagonal Magic Square of Order 49

Below is a pandiagonal magic squares of order 49.


|  | pm | 5889 | 5844 | 58849 |  |  | 5849 | 5849 | 58 |  |  | 8849 | 5849 | 5884 | 5884 | 5849 | 5884 | 5884 | 5849 | 5849 | 5849 | 5884 | 5848 | 5884 | 5844 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 584 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5849 | 5889 | 5849 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 401 | 801 | 1201 | 1601 | 2001 | 2401 | 334 | 391 | 742 | 1135 | 1535 | 1935 | 2335 | 268 | 668 | 725 | 1125 | 1476 | 1876 | 2269 | 209 | 609 | 1002 | 1059 | 1459 | 1859 | 2210 | 192 | 543 | 943 | 1343 | 1400 | 1793 | 2193 | 133 | 526 | 926 | 1277 | 1677 | 1734 | 2134 | 67 | 467 | 867 | 1267 | 1660 | 2011 | 2068 | 134 |
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|  | 1185 | 1585 | 1985 | 2385 | 41 | 441 | 785 | 1175 | 1526 | 1919 | 2319 | 318 | 375 | 775 | 1109 | 1509 | 1909 | 2260 | 259 | 652 | 709 | 1050 | 1443 | 1843 | 2243 | 242 | 593 | 993 | 1327 | 1384 | 1784 | 2184 | 176 | 576 | 976 | 1310 | 1710 | 1718 | 2118 | 117 | 517 | 917 | 1251 | 1651 | 2051 | 2101 | 51 | 451 | 851 |  |
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|  | 1703 | 1760 | 2111 | 110 | 510 | 910 | 1303 | 1644 | 2044 | 2094 | 93 | 444 | 84 | 1244 | 1578 | 1978 | 2378 | 34 | 434 | 827 | 1178 | 1568 | 1912 | 2312 | 311 | 368 | 768 | 1168 | 1502 | 1902 | 2302 | 252 | 645 | 702 | 1102 | 1436 | 1836 | 2236 | 235 | 63 | 986 | 1043 | 137 | 1777 | 2177 | 169 | 569 | 969 | 1369 | 588 |
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|  | 236 | 636 | 987 | 1037 | 1437 | 1837 | 2237 | 170 | 570 | 970 | 1370 | 1378 | 1778 | 2171 |  | 511 | 904 | 1304 | 1704 | 1761 | 2112 | 94 | 445 | 845 | 1245 | 1645 | 2038 | 2095 | 35 | 428 | 828 | 1179 | 1579 | 979 | 2379 | 312 | 369 | 769 | 1169 | 1562 | 1913 | 2313 | 246 | 646 | 703 | 103 | 503 | 903 | 2303 |  |
|  | 1829 | 2229 | 228 | 628 | 1028 | 1036 | 1429 | 1770 | 2170 | 162 | 562 | 962 | 1362 | 1419 | 1753 | 2153 | 103 | 503 | 903 | 1296 | 1696 | 2037 | 2087 | 86 | 486 | 837 | 1237 | 1637 | 1971 | 2371 | 27 | 427 | 820 | 1220 | 1571 | 1954 | 2305 | 304 | 361 | 761 | 1161 | 1561 | 1895 | 2295 | 294 | 638 | 695 | 1095 | 1495 |  |
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|  | 988 | 1045 | 1445 | 1845 | 224 | 244 | 595 | 978 | 1329 | 1386 | 1779 | 2179 | 178 | 578 | 912 | 1312 | 1772 | 1720 | 2120 | 119 | 512 | 853 | 1253 | 1646 | 2046 | 2103 | 53 | 453 | 787 | 1187 | 1587 | 1987 | 2387 | 36 | 436 | 777 | 1170 | 1521 | 1921 | 2321 | 320 | 377 | 711 | 1111 | 1511 | 1911 | 2255 | 254 | 654 |  |
|  | 329 | 379 | 779 | 1130 | 1530 | 1930 | 2330 | 263 | 663 | 720 | 1120 | 1513 | 1864 | 2264 | 197 | 597 | 997 | 1054 | 1454 | 1854 | 2254 | 187 | 587 | 938 | 1331 | 1388 | 1788 | 2188 | 121 | 521 | 921 | 1321 | 1672 | 1729 | 2122 | 62 | 462 | 855 | 125 | 1655 | 2055 | 2063 | 45 | 396 | 796 | 1196 | 1596 | 1989 | 2389 |  |
|  | 1922 | 2322 | 321 | 378 | 77 | 1171 | 1522 | 1905 | 2256 | 255 | 655 | 712 | 1112 | 1512 | 1846 | 2246 | 245 | 589 | 989 | 1046 | 1446 | 1780 | 2180 | 179 | 579 | 979 | 1330 | 1380 | 1721 | 2121 | 113 | 513 | 13 | 1313 | 1713 | 2047 | 2104 | 54 | 454 | 854 | 1247 | 1641 | 1988 | 2381 |  | 437 | 788 | 1188 | 588 |  |
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|  | 72 | 472 | 872 | 1272 | 1623 | 2023 | 2073 | 13 | 413 | 806 | 1206 | 1606 | 2006 | 2357 | 339 | 347 | 747 | 1147 | 1547 | 1940 | 2340 | 280 | 673 | 730 | 1081 | 1481 | 1881 | 228 | 214 | 614 | 1014 | 1071 | 1464 | 1815 | 2215 | 148 | 548 | 948 | 1348 | 1405 | 1805 |  | 38 | 538 |  | 1282 | 1682 |  | 139 |  |
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|  | 25 | 658 | 708 | 1108 | 1508 | 1908 | 2259 | 241 | 592 | 992 | 1049 | 1449 | 1842 | 2242 | 182 | 575 | 975 | 1326 | 1383 | 1783 | 2183 | ${ }^{116}$ | 516 | 916 | 1316 | 1709 | 1717 | 2117 | 50 | 450 | 850 | 1250 | 165 | 2050 | 210 | 40 | 440 | 791 | 118 | 1584 | 198 | 2384 | 317 | 374 | 774 | 1174 | 1525 | 1925 | 8 | 884 |
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|  | 683 | 691 | 109 | 1491 | 188 | 2284 | 283 | 617 | 1017 | 1074 | 1425 | 1825 | 2225 | 224 | 558 | 958 | 1358 | 1408 | 1808 | 2159 | 158 | 492 | 892 | 1292 | 1692 | 1749 | 2149 | 141 | 482 | 882 | 122 | 1626 | 202 | 2083 | 82 | 416 | 816 | 1216 | 1616 | 196 | 2360 | 16 | 357 | 750 | 1150 | 1550 | 1950 | 2350 | 300 | 884 |
|  | 2276 | 275 | 675 | 732 | 1083 | 1483 | 1883 | 221 | 216 | 616 | 1009 | 066 | 1466 | 1817 | 2200 | 150 | 550 | 950 | 1350 | 1407 | 1800 | 214 | 140 | 53 | 884 | 1284 | 684 | 1741 | 2075 | 74 | 474 | 874 | 1274 | 1618 | 2018 | 235 | 8 | 408 | 808 | 120 | 1608 | 2008 | 234 | 341 | 349 | 749 | 1142 | 1542 | 1942 | 5884 |
|  | 1475 | 875 | 2275 | 267 | 667 | 724 | 1124 | 1458 | 858 | 209 | 208 | 608 | D08 | 1058 | 1399 | 799 | 192 | 191 | 542 | 942 | 1342 | 676 | 1733 | 2133 | 132 | 532 | 925 | 1276 | 166 | 2010 | 2067 | 66 | 466 | 866 | 1266 | 160 | 2000 | 2400 | 7 | 400 | 800 | 1200 | 1534 | 1934 | 2334 | 333 | 39 | 741 | 1141 | 584 |
|  | 716 | 1116 | 1516 | 1867 | 226 | 266 | 659 | 1000 | 1057 | 450 | 1850 | 250 | 200 | 600 | 934 | 1334 | 391 | 1791 | 219 | 183 | 583 | 924 | 1317 | 1668 | 1725 | 2125 | 124 | 524 | 858 | 1258 | 1658 | 2058 | 205 | 58 | 458 | 792 | 1192 | 1592 | 1992 | 2392 | 48 | 399 | 782 | 1133 | 1533 | 1926 | 2326 | 325 | 382 |  |
|  | 5884 | 5849 | 5849 | 5844 | 5884 | 5844 | 5844 | 5844 | 5844 | 5844 | 5849 | 5844 | 5844 | 5844 | 5844 | 5849 | 5849 | 5844 | 5849 | 5889 | 5849 | 5844 | 5844 | 5884 | 5884 | 5844 | 5844 | 5884 | 5884 | 5844 | 5889 | 5849 | 5894 | 5884 | 5844 | 5889 | 5844 | 5849 | 5884 | 5889 | 5849 | 5844 | 5844 | 5849 | 5884 | 5844 | 5884 | 5889 | 5884 | S004 |

The blocks of order 7 are equal sums pandiagonal magic squares with sum $M_{7 \times 7}:=8407$. Moreover it is bimagic squares with bimagic sum $S b_{49 \times 49}:=94220679$.

Remark 1. The excel file attached with this work contains only pandiagonal magic squares with equal sums of order 7 up to order 133 , i.e., these are of orders $21,35,49,63,77,91,105,109$, and 133. It is left for the readers to check the other order multiples of 7 . Whole the work in Excel file is up to order 140.

## 4 Author's Contribution to Recreation of Numbers and Magic Squares

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[^0]:    ${ }^{1}$ Formerly, Professor of Mathematics, Federal University of Santa Catarina, Florianópolis, SC, Brazil (1978-2012) Also worked at Delhi University, India (1976-1978).
    E-mail: ijtaneja@gmail.com;
    Web-sites: http://inderjtaneja.com; http://numbers-magic.com;
    Twitter: @IJTANEJA; Instagram: @crazynumbers.

