

# Block-Wise Bordered and Pandiagonal Magic Squares Multiples of 7

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## Abstract

*During past years author worked with **block-wise bordered magic squares** of even number blocks. These are based on equal sums magic squares of orders 4, 6, 8, 10, etc. This type of work is an extension of classical bordered magic squares. In case of multiples of 4, the extension is made for **pandiagonal** magic squares [23]. For multiples of order 6 refer Taneja [24]. For the first time, we are presenting here bordered magic squares of odd number blocks. Recently, author worked on multiples of 3, based on different sums magic squares of order 3 [29]. The work for the borders multiples of 5 refer [30]. It is done with two types of magic squares of order 5. One type is pandiagonal magic squares, and another as bordered magic squares. Based on same procedure we worked with multiples of 7 based on magic squares of order 7. Pandiagonal magic squares of orders 21, 28, 35 and 49 are also given. Higher order examples can be seen in **Excel file** attached with the work. The total work is up to order 140. Pandiagonal magic squares based on equal sums pandiagonal magic squares of order 7 are also included in the **Excel file**.*

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## 1 Introduction

During past years author [2, 3, 4, 5, 6, 7, 8] worked with **block-wise** magic squares from orders 12 to 47. Author [9, 10, 11, 12, 13, 14] also worked with **bordered** magic squares. The study on **bordered** magic squares is extended to **block-bordered** magic squares [15, 16, 17]. This is specially done for the magic squares of orders  $p$  and  $2p$ , where  $p$  is a prime number. This study is still extended to **block-wise bordered** magic squares [18, 19, 20, 21]. Some connection with Pythagorean triples and area-representations are also made [23, 24, 25, 26, 27]. The main property of **bordered** magic squares is that if we remove external borders, still we get **sub-bordered** magic squares, i.e., each layer in itself lead us to magic squares. In many cases, the properties of **bordered** magic square are separated by **even** and **odd** orders magic squares. In many cases, we get good properties for the **even** order **bordered** magic squares. In some cases, we have to use fractional numbers to reach minimum perfect square sum of entries. For more study on **bordered** magic squares refer H. White’s web-site [1].

The idea of bordered magic squares is already discussed by H. White’s web-site [1] where the borders are of **single digits**. Borders multiples of even numbers starting from 4 are done extensively by author [23, 24, 25, 26, 27, 28].

Recently, for the first time, we presented bordered magic squares of odd number blocks. In case of multiples of 3, we worked with different sums magic squares of order 3. In case of multiples of 5, we worked with **pandiagonal** and **bordered** magic squares of order 5. This work is for multiples of 7. Here also we worked with two types of magic squares of order 7. One **pandiagonal** and another is **bordered** magic squares of order 7. The procedure, how to get these **block-wise bordered** magic squares is also explained. **Pandiagonal** magic squares multiples of 7 are also given. This work is up to order 49. Higher orders examples can be seen in **Excel file** attached with this work. Before proceeding further, let's summarize, the idea of **block-wise bordered** magic squares:

## 1.1 Classification of Bordered Magic Squares

- **Single Digit:** Bordered magic squares based on single digit [9, 10, 1].
- **Two Digits:** Bordered magic squares based on magic rectangles multiples of 2 [58, 59, 60, 61, 61].
- **Three Digits:** Bordered magic squares based on magic squares of order 3 [29].
- **Four Digits:** Bordered magic squares based on magic squares of order 4 [23].
- **Five Digits:** Bordered magic squares based on magic squares of order 5 [30].
- **Six Digits:** Bordered magic squares based on magic squares of order 6 [24].
- **Seven Digits:** Bordered magic squares based on magic squares of order 7 (This work).

For further even number multiples refer the following works of author:

- **Eight Digits:** Bordered magic squares based on magic squares of order 8 [25].
- **Ten Digits:** Bordered magic squares based on magic squares of order 10 [26].
- **Twelve Digits:** Bordered magic squares based on magic squares of order 12 [27].
- **Fourteen Digits:** Bordered magic squares based on magic squares of order 14 [28].

Let's see below the some examples of **block-wise bordered** magic squares multiples 7, where magic squares of order 7 are considered in two different ways.

## **2 Block-Wise Bordered Magic Squares**

### **2.1 Magic Squares of Orders 42 and 49**

Let's consider bordered magic square of orders 6 and 7 given by

6							111
6	30	3	36	4	32	111	
35	17	22	11	24	2	111	
29	12	23	18	21	8	111	
27	26	13	20	15	10	111	
9	19	16	25	14	28	111	
5	7	34	1	33	31	111	
111	111	111	111	111	111	111	

7								175
44	38	40	5	4	2	42	175	
11	34	30	15	14	32	39	175	
9	19	28	21	26	31	41	175	
7	17	23	25	27	33	43	175	
47	37	24	29	22	13	3	175	
49	18	20	35	36	16	1	175	
8	12	10	45	46	48	6	175	
175	175	175	175	175	175	175	175	

The entries of above two magic squares are sequential numbers starting from 1:

$$D_{11 \times 11} := \{1, 2, \dots, 35, 36\}$$

$$D_{12 \times 12} := \{1, 2, \dots, 48, 49\}$$

These two magic squares are such that replacing the upper border still we are left with magic squares of sequential vales. Multiplying each entry by 49, we get

6							5439
294	1470	147	1764	196	1568	5439	
1715	833	1078	539	1176	98	5439	
1421	588	1127	882	1029	392	5439	
1323	1274	637	980	735	490	5439	
441	931	784	1225	686	1372	5439	
245	343	1666	49	1617	1519	5439	
5439	5439	5439	5439	5439	5439	5439	

7								8575
2156	1862	1960	245	196	98	2058	8575	
539	1666	1470	735	686	1568	1911	8575	
441	931	1372	1029	1274	1519	2009	8575	
343	833	1127	1225	1323	1617	2107	8575	
2303	1813	1176	1421	1078	637	147	8575	
2401	882	980	1715	1764	784	49	8575	
392	588	490	2205	2254	2352	294	8575	
8575	8575	8575	8575	8575	8575	8575	8575	

The distributions of these two magic squares are given by

$$D_{17 \times 7} := \{49, 98, \dots, 1715, 1764\}$$

$$D_{18 \times 8} := \{49, 98, \dots, 2352, 2401\}.$$

In both the cases the difference between entries is 25. Now in each case replace the entries by magic squares of order 5 formed by the entries as given below:

49 → 1, 2, ..., 49  
98 → 50, 51, ..., 98  
147 → 99, 100, ..., 147  
... → ...  
2352 → 2304, 2305, ..., 2352  
2401 → 2353, 2354, ..., 2401

This lead us to following two bordered magic squares of orders 42 and 49.







Below are two bordered magic squares of order 49 with blocks of magic squares of order 7:





$$D_{40 \times 40} := \{1, 2, \dots, 2400, 2401\}.$$

These four magic squares are bordered magic squares with border made by **pandiagonal** and **bordered** magic squares of order 5. If you remove the external borders, still we are left with magic squares of lower orders. Let's see how it works.

## 2.2 Magic Squares of Order 35

These magic squares are obtained from above by the application of the formula  $\frac{a^2 - b^2}{2}$ ,  $a > b$ . Removing the external border of order 7 and then subtracting  $\frac{49^2 - 35^2}{2} := 588$  from magic squares of orders 49, we get magic squares of order 35 given by





### 2.3 Magic Squares of Order 28

These magic squares are obtained from above by the application of the formula  $\frac{a^2 - b^2}{2}$ ,  $a > b$ . Removing the external border of order 7 and then subtracting  $\frac{42^2 - 28^2}{2} := 490$  from magic squares of orders 42, we get magic squares of order 28 given by

pan	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990
10990	343	335	327	319	311	303	295	588	580	572	564	556	548	540	49	41	33	25	17	9	1	686	678	670	662	654	646	638	10990	
10990	304	296	337	336	328	320	312	549	541	582	581	573	565	557	10	2	43	42	34	26	18	647	639	680	679	671	663	655	10990	
10990	321	313	305	297	338	330	329	566	558	550	542	583	575	574	27	19	11	3	44	36	35	664	656	648	640	681	673	672	10990	
10990	331	323	322	314	306	298	339	576	568	567	559	551	543	584	37	29	28	20	12	4	45	674	666	665	657	649	641	682	10990	
10990	299	340	332	324	316	315	307	544	585	577	569	561	560	552	5	46	38	30	22	21	13	642	683	675	667	659	658	650	10990	
10990	309	308	300	341	333	325	317	554	553	545	586	578	570	562	15	14	6	47	39	31	23	652	651	643	684	676	668	660	10990	
10990	326	318	310	302	301	342	334	571	563	555	547	546	587	579	32	24	16	8	7	48	40	669	661	653	645	644	685	677	10990	
10990	98	90	82	74	66	58	50	637	629	621	613	605	597	589	392	384	376	368	360	352	344	539	531	523	515	507	499	491	10990	
10990	59	51	92	91	83	75	67	598	590	631	630	622	614	606	353	345	386	385	377	369	361	500	492	533	532	524	516	508	10990	
10990	76	68	60	52	93	85	84	615	607	599	591	632	624	623	370	362	354	346	387	379	378	517	509	501	493	534	526	525	10990	
10990	86	78	77	69	61	53	94	625	617	616	608	600	592	633	380	372	371	363	355	347	388	527	519	518	510	502	494	535	10990	
10990	54	95	87	79	71	70	62	593	634	626	618	610	609	601	348	389	381	373	365	364	356	495	536	528	520	512	511	503	10990	
10990	64	63	55	96	88	80	72	603	602	594	635	627	619	611	358	357	349	390	382	374	366	505	504	496	537	529	521	513	10990	
10990	81	73	65	57	56	97	89	620	612	604	596	595	636	628	375	367	359	351	350	391	383	522	514	506	498	497	538	530	10990	
10990	784	776	768	760	752	744	736	147	139	131	123	115	107	99	490	482	474	466	458	450	442	245	237	229	221	213	205	197	10990	
10990	745	737	778	777	769	761	753	108	100	141	140	132	124	116	451	443	484	483	475	467	459	206	198	239	238	230	222	214	10990	
10990	762	754	746	738	779	771	770	125	117	109	101	142	134	133	468	460	452	444	485	477	476	223	215	207	199	240	232	231	10990	
10990	772	764	763	755	747	739	780	135	127	126	118	110	102	143	478	470	469	461	453	445	486	233	225	224	216	208	200	241	10990	
10990	740	781	773	765	757	756	748	103	144	136	128	120	119	111	446	487	479	471	463	462	454	201	242	234	226	218	217	209	10990	
10990	750	749	741	782	774	766	758	113	112	104	145	137	129	121	456	455	447	488	480	472	464	211	210	202	243	235	227	219	10990	
10990	767	759	751	743	742	783	775	130	122	114	106	105	146	138	473	465	457	449	448	489	481	228	220	212	204	203	244	236	10990	
10990	441	433	425	417	409	401	393	294	286	278	270	262	254	246	735	727	719	711	703	695	687	196	188	180	172	164	156	148	10990	
10990	402	394	435	434	426	418	410	255	247	288	287	279	271	263	696	688	729	728	720	712	704	157	149	190	189	181	173	165	10990	
10990	419	411	403	395	436	428	427	272	264	256	248	289	281	280	713	705	697	689	730	722	721	174	166	158	150	191	183	182	10990	
10990	429	421	420	412	404	396	437	282	274	273	265	257	249	290	723	715	714	706	698	690	731	184	176	175	167	159	151	192	10990	
10990	397	438	430	422	414	413	405	250	291	283	275	267	266	258	691	732	724	716	708	707	699	152	193	185	177	169	168	160	10990	
10990	407	406	398	439	431	423	415	260	259	251	292	284	276	268	701	700	692	733	725	717	709	162	161	153	194	186	178	170	10990	
10990	424	416	408	400	399	440	432	277	269	261	253	252	293	285	718	710	702	694	693	734	726	179	171	163	155	154	195	187	10990	
28	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990

28																													10990
300	306	304	339	340	342	302	545	551	549	584	585	587	547	6	12	10	45	46	48	8	643	649	647	682	683	685	645	10990	
333	310	314	329	330	312	305	578	555	559	574	575	557	550	39	16	20	35	36	18	11	676	653	657	672	673	655	648	10990	
335	325	316	323	318	313	303	580	570	561	568	563	558	548	41	31	22	29	24	19	9	678	668	659	666	661	656	646	10990	
337	327	321	319	317	311	301	582	572	566	564	562	556	546	43	33	27	25	23	17	7	680	670	664	662	660	654	644	10990	
297	307	320	315	322	331	341	542	552	565	560	567	576	586	3	13	26	21	28	37	47	640	650	663	658	665	674	684	10990	
295	326	324	309	308	328	343	540	571	569	554	553	573	588	1	32	30	15	14	34	49	638	669	667	652	651	671	686	10990	
336	332	334	299	298	296	338	581	577	579	544	543	541	583	42	38	40	5	4	2	44	679	675	677	642	641	639	681	10990	
55	61	59	94	95	97	57	594	600	598	633	634	636	596	349	355	353	388	389	391	351	496	502	500	535	536	538	498	10990	
88	65	69	84	85	67	60	627	604	608	623	624	606	599	382	359	363	378	379	361	354	529	506	510	525	526	508	501	10990	
90	80	71	78	73	68	58	629	619	610	617	612	607	597	384	374	365	372	367	362	352	531	521	512	519	514	509	499	10990	
92	82	76	74	72	66	56	631	621	615	613	611	605	595	386	376	370	368	366	360	350	533	523	517	515	513	507	497	10990	
52	62	75	70	77	86	96	591	601	614	609	616	625	635	346	356	369	364	371	380	390	493	503	516	511	518	527	537	10990	
50	81	79	64	63	83	98	589	620	618	603	602	622	637	344	375	373	358	357	377	392	491	522	520	505	504	524	539	10990	
91	87	89	54	53	51	93	630	626	628	593	592	590	632	385	381	383	348	347	345	387	532	528	530	495	494	492	534	10990	
741	747	745	780	781	783	743	104	110	108	143	144	146	106	447	453	451	486	487	489	449	202	208	206	241	242	244	204	10990	
774	751	755	770	771	753	746	137	114	118	133	134	116	109	480	457	461	476	477	459	452	235	212	216	231	232	214	207	10990	
776	766	757	764	759	754	744	139	129	120	127	122	117	107	482	472	463	470	465	460	450	237	227	218	225	220	215	205	10990	
778	768	762	760	758	752	742	141	131	125	123	121	115	105	484	474	468	466	464	458	448	239	229	223	221	219	213	203	10990	
738	748	761	756	763	772	782	101	111	124	119	126	135	145	444	454	467	462	469	478	488	199	209	222	217	224	233	243	10990	
736	767	765	750	749	769	784	99	130	128	113	112	132	147	442	473	471	456	455	475	490	197	228	226	211	210	230	245	10990	
777	773	775	740	739	737	779	140	136	138	103	102	100	142	483	479	481	446	445	443	485	238	234	236	201	200	198	240	10990	
398	404	402	437	438	440	400	251	257	255	290	291	293	253	692	698	696	731	732	734	694	153	159	157	192	193	195	155	10990	
431	408	412	427	428	410	403	284	261	265	280	281	263	256	725	702	706	721	722	704	697	186	163	167	182	183	165	158	10990	
433	423	414	421	416	411	401	286	276	267	274	269	264	254	727	717	708	715	710	705	695	188	178	169	176	171	166	156	10990	
435	425	419	417	415	409	399	288	278	272	270	268	262	252	729	719	713	711	709	703	693	190	180	174	172	170	164	154	10990	
395	405	418	413	420	429	439	248	258	271	266	273	282	292	689	699	712	707	714	723	733	150	160	173	168	175	184	194	10990	
393	424	422	407	406	426	441	246	277	275	260	259	279	294	687	718	716	701	700	720	735	148	179	177	162	161	181	196	10990	
434	430	432	397	396	394	436	287	283	285	250	249	247	289	728	724	726	691	690	688	730	189	185	187	152	151	149	191	10990	
10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	

Above two magic squares of order 28 formed by blocks of magic squares of order 7 are with sequential entries:

$$D_{25 \times 25} := \{1, 2, \dots, 783, 784\}$$

## 2.4 Magic Squares of Order 21

These magic squares are obtained from above by the application of the formula  $\frac{a^2 - b^2}{2}$ ,  $a > b$ . Removing the external border of order 7 and then subtracting  $\frac{35^2 - 21^2}{2} := 392$  from magic squares of orders 35, we get magic squares of order 21 given by



21																												4641
392	384	376	368	360	352	344	49	41	33	25	17	9	1	294	286	278	270	262	254	246	4641							
353	345	386	385	377	369	361	10	2	43	42	34	26	18	255	247	288	287	279	271	263	4641							
370	362	354	346	387	379	378	27	19	11	3	44	36	35	272	264	256	248	289	281	280	4641							
380	372	371	363	355	347	388	37	29	28	20	12	4	45	282	274	273	265	257	249	290	4641							
348	389	381	373	365	364	356	5	46	38	30	22	21	13	250	291	283	275	267	266	258	4641							
358	357	349	390	382	374	366	15	14	6	47	39	31	23	260	259	251	292	284	276	268	4641							
375	367	359	351	350	391	383	32	24	16	8	7	48	40	277	269	261	253	252	293	285	4641							
147	139	131	123	115	107	99	245	237	229	221	213	205	197	343	335	327	319	311	303	295	4641							
108	100	141	140	132	124	116	206	198	239	238	230	222	214	304	296	337	336	328	320	312	4641							
125	117	109	101	142	134	133	223	215	207	199	240	232	231	321	313	305	297	338	330	329	4641							
135	127	126	118	110	102	143	233	225	224	216	208	200	241	331	323	322	314	306	298	339	4641							
103	144	136	128	120	119	111	201	242	234	226	218	217	209	299	340	332	324	316	315	307	4641							
113	112	104	145	137	129	121	211	210	202	243	235	227	219	309	308	300	341	333	325	317	4641							
130	122	114	106	105	146	138	228	220	212	204	203	244	236	326	318	310	302	301	342	334	4641							
196	188	180	172	164	156	148	441	433	425	417	409	401	393	98	90	82	74	66	58	50	4641							
157	149	190	189	181	173	165	402	394	435	434	426	418	410	59	51	92	91	83	75	67	4641							
174	166	158	150	191	183	182	419	411	403	395	436	428	427	76	68	60	52	93	85	84	4641							
184	176	175	167	159	151	192	429	421	420	412	404	396	437	86	78	77	69	61	53	94	4641							
152	193	185	177	169	168	160	397	438	430	422	414	413	405	54	95	87	79	71	70	62	4641							
162	161	153	194	186	178	170	407	406	398	439	431	423	415	64	63	55	96	88	80	72	4641							
179	171	163	155	154	195	187	424	416	408	400	399	440	432	81	73	65	57	56	97	89	4641							
4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641						

21																					4641
349	355	353	388	389	391	351	6	12	10	45	46	48	8	251	257	255	290	291	293	253	4641
382	359	363	378	379	361	354	39	16	20	35	36	18	11	284	261	265	280	281	263	256	4641
384	374	365	372	367	362	352	41	31	22	29	24	19	9	286	276	267	274	269	264	254	4641
386	376	370	368	366	360	350	43	33	27	25	23	17	7	288	278	272	270	268	262	252	4641
346	356	369	364	371	380	390	3	13	26	21	28	37	47	248	258	271	266	273	282	292	4641
344	375	373	358	357	377	392	1	32	30	15	14	34	49	246	277	275	260	259	279	294	4641
385	381	383	348	347	345	387	42	38	40	5	4	2	44	287	283	285	250	249	247	289	4641
104	110	108	143	144	146	106	202	208	206	241	242	244	204	300	306	304	339	340	342	302	4641
137	114	118	133	134	116	109	235	212	216	231	232	214	207	333	310	314	329	330	312	305	4641
139	129	120	127	122	117	107	237	227	218	225	220	215	205	335	325	316	323	318	313	303	4641
141	131	125	123	121	115	105	239	229	223	221	219	213	203	337	327	321	319	317	311	301	4641
101	111	124	119	126	135	145	199	209	222	217	224	233	243	297	307	320	315	322	331	341	4641
99	130	128	113	112	132	147	197	228	226	211	210	230	245	295	326	324	309	308	328	343	4641
140	136	138	103	102	100	142	238	234	236	201	200	198	240	336	332	334	299	298	296	338	4641
153	159	157	192	193	195	155	398	404	402	437	438	440	400	55	61	59	94	95	97	57	4641
186	163	167	182	183	165	158	431	408	412	427	428	410	403	88	65	69	84	85	67	60	4641
188	178	169	176	171	166	156	433	423	414	421	416	411	401	90	80	71	78	73	68	58	4641
190	180	174	172	170	164	154	435	425	419	417	415	409	399	92	82	76	74	72	66	56	4641
150	160	173	168	175	184	194	395	405	418	413	420	429	439	52	62	75	70	77	86	96	4641
148	179	177	162	161	181	196	393	424	422	407	406	426	441	50	81	79	64	63	83	98	4641
189	185	187	152	151	149	191	434	430	432	397	396	394	436	91	87	89	54	53	51	93	4641
4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641

Above two magic squares of order 21 formed by blocks of magic squares of order 7 are with sequential entries:

$$D_{20 \times 20} := \{1, 2, \dots, 440, 441\}$$

### 3 Pandiagonal Magic Squares Multiples 7

This section brings pandiagonal magic squares multiples 7. It includes magic squares of orders 21, 28, 35 and 49. The details are excluded as these are studied extensively in author's previous works [5, 7, 20].

#### 3.1 Pandiagonal Magic Square of Order 21

Below is a **pandiagonal** magic squares of order 21.

	pan	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641		
4641	1	111	155	243	265	375	397	3	110	154	242	266	374	398	2	109	156	241	267	373	399	4641
4641	370	396	19	106	153	239	264	371	395	20	108	152	238	263	372	394	21	107	151	240	262	4641
4641	237	260	369	391	18	124	148	236	259	368	392	17	125	150	235	261	367	393	16	126	149	4641
4641	123	166	232	258	365	390	13	122	167	234	257	364	389	14	121	168	233	256	366	388	15	4641
4641	386	12	118	165	250	253	363	385	11	119	164	251	255	362	387	10	120	163	252	254	361	4641
4641	271	358	384	8	117	160	249	272	360	383	7	116	161	248	273	359	382	9	115	162	247	4641
4641	159	244	270	376	379	6	113	158	245	269	377	381	5	112	157	246	268	378	380	4	114	4641
4641	43	90	134	222	286	354	418	45	89	133	221	287	353	419	44	88	135	220	288	352	420	4641
4641	349	417	61	85	132	218	285	350	416	62	87	131	217	284	351	415	63	86	130	219	283	4641
4641	216	281	348	412	60	103	127	215	280	347	413	59	104	129	214	282	346	414	58	105	128	4641
4641	102	145	211	279	344	411	55	101	146	213	278	343	410	56	100	147	212	277	345	409	57	4641
4641	407	54	97	144	229	274	342	406	53	98	143	230	276	341	408	52	99	142	231	275	340	4641
4641	292	337	405	50	96	139	228	293	339	404	49	95	140	227	294	338	403	51	94	141	226	4641
4641	138	223	291	355	400	48	92	137	224	290	356	402	47	91	136	225	289	357	401	46	93	4641
4641	22	69	176	201	307	333	439	24	68	175	200	308	332	440	23	67	177	199	309	331	441	4641
4641	328	438	40	64	174	197	306	329	437	41	66	173	196	305	330	436	42	65	172	198	304	4641
4641	195	302	327	433	39	82	169	194	301	326	434	38	83	171	193	303	325	435	37	84	170	4641
4641	81	187	190	300	323	432	34	80	188	192	299	322	431	35	79	189	191	298	324	430	36	4641
4641	428	33	76	186	208	295	321	427	32	77	185	209	297	320	429	31	78	184	210	296	319	4641
4641	313	316	426	29	75	181	207	314	318	425	28	74	182	206	315	317	424	30	73	183	205	4641
4641	180	202	312	334	421	27	71	179	203	311	335	423	26	70	178	204	310	336	422	25	72	4641
	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	4641	

The blocks of order 7 are of **equal sums** magic squares, i.e.,  $M_{7 \times 7} := 1547$

### 3.2 Pandiagonal Magic Square of Order 28

Below is a **pandiagonal** magic squares of order 28.

	pan	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990			
10990	343	335	327	319	311	303	295	588	580	572	564	556	548	540	49	41	33	25	17	9	1	686	678	670	662	654	646	638	10990	
10990	304	296	337	336	328	320	312	549	541	582	581	573	565	557	10	2	43	42	34	26	18	647	639	680	679	671	663	655	10990	
10990	321	313	305	297	338	330	329	566	558	550	542	583	575	574	27	19	11	3	44	36	35	664	656	648	640	681	673	672	10990	
10990	331	323	322	314	306	298	339	576	568	567	559	551	543	584	37	29	28	20	12	4	45	674	666	665	657	649	641	682	10990	
10990	299	340	332	324	316	315	307	544	585	577	569	561	560	552	5	46	38	30	22	21	13	642	683	675	667	659	658	650	10990	
10990	309	308	300	341	333	325	317	554	553	545	586	578	570	562	15	14	6	47	39	31	23	652	651	643	684	676	668	660	10990	
10990	326	318	310	302	301	342	334	571	563	555	547	546	587	579	32	24	16	8	7	48	40	669	661	653	645	644	685	677	10990	
10990	98	90	82	74	66	58	50	637	629	621	613	605	597	589	392	384	376	368	360	352	344	539	531	523	515	507	499	491	10990	
10990	59	51	92	91	83	75	67	598	590	631	630	622	614	606	353	345	386	385	377	369	361	500	492	533	532	524	516	508	10990	
10990	76	68	60	52	93	85	84	615	607	599	591	632	624	623	370	362	354	346	387	379	378	517	509	501	493	534	526	525	10990	
10990	86	78	77	69	61	53	94	625	617	616	608	600	592	633	380	372	371	363	355	347	388	527	519	518	510	502	494	535	10990	
10990	54	95	87	79	71	70	62	593	634	626	618	610	609	601	348	389	381	373	365	364	356	495	536	528	520	512	511	503	10990	
10990	64	63	55	96	88	80	72	603	602	594	635	627	619	611	358	357	349	390	382	374	366	505	504	496	537	529	521	513	10990	
10990	81	73	65	57	56	97	89	620	612	604	596	595	636	628	375	367	359	351	350	391	383	522	514	506	498	497	538	530	10990	
10990	784	776	768	760	752	744	736	147	139	131	123	115	107	99	490	482	474	466	458	450	442	245	237	229	221	213	205	197	10990	
10990	745	737	778	777	769	761	753	108	100	141	140	132	124	116	451	443	484	483	475	467	459	206	198	239	238	230	222	214	10990	
10990	762	754	746	738	779	771	770	125	117	109	101	142	134	133	468	460	452	444	485	477	476	223	215	207	199	240	232	231	10990	
10990	772	764	763	755	747	739	780	135	127	126	118	110	102	143	478	470	469	461	453	445	486	233	225	224	216	208	200	241	10990	
10990	740	781	773	765	757	756	748	103	144	136	128	120	119	111	446	487	479	471	463	462	454	201	242	234	226	218	217	209	10990	
10990	750	749	741	782	774	766	758	113	112	104	145	137	129	121	456	455	447	488	480	472	464	211	210	202	243	235	227	219	10990	
10990	767	759	751	743	742	783	775	130	122	114	106	105	146	138	473	465	457	449	448	489	481	228	220	212	204	203	244	236	10990	
10990	441	433	425	417	409	401	393	294	286	278	270	262	254	246	735	727	719	711	703	695	687	196	188	180	172	164	156	148	10990	
10990	402	394	435	434	426	418	410	255	247	288	287	279	271	263	696	688	729	728	720	712	704	157	149	190	189	181	173	165	10990	
10990	419	411	403	395	436	428	427	272	264	256	248	289	281	280	713	705	697	689	730	722	721	174	166	158	150	191	183	182	10990	
10990	429	421	420	412	404	396	437	282	274	273	265	257	249	290	723	715	714	706	698	690	731	184	176	175	167	159	151	192	10990	
10990	397	438	430	422	414	413	405	250	291	283	275	267	266	258	691	732	724	716	708	707	699	152	193	185	177	169	168	160	10990	
10990	407	406	398	439	431	423	415	260	259	251	292	284	276	268	701	700	692	733	725	717	709	162	161	153	194	186	178	170	10990	
10990	424	416	408	400	399	440	432	277	269	261	253	252	293	285	718	710	702	694	693	734	726	179	171	163	155	154	195	187	10990	
28	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990	10990

The blocks of order 7 are with **different sums** pandiagonal magic squares. It is the same magic square given in previous section.

### 3.3 Pandiagonal Magic Square of Order 35

Below is a **pandiagonal** magic squares of order 35.



### 3.4 Pandiagonal Magic Square of Order 49

Below is a **pandiagonal** magic squares of order 49.



**Remark 1.** The *excel file* attached with this work contains only **pandiagonal** magic squares with **equal sums** of order 7 up to order 133, i.e., these are of orders 21, 35, 49, 63, 77, 91, 105, 109, and 133. It is left for the readers to check the other order multiples of 7. Whole the work in Excel file is up to order 140.

## 4 Author's Contribution to Recreation of Numbers and Magic Squares

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