# WORDMARKOV: A NEW PASSWORD PROBABILITY MODEL OF SEMANTICS 

<br>${ }^{4}$ Peking University<br>\{xjhshare, zhurong, hbcheng, pwang\} @pku.edu.cn<br>${ }^{\S}$ Delft University of Technology<br>kaitai.liang@tudelft.nl


#### Abstract

To date there are few researches on the semantic information of passwords, which leaves a gap preventing us from fully understanding the passwords characteristic and security. We propose a new password probability model for semantic information based on Markov Chain, called WordMarkov, that can capture the semantic essence of password samples. Further, we evaluate our design via password guessing attacks, on six real-world datasets, and we show that WordMarkov obtains $24.29 \%-67.37 \%$ improvement over the state-of-the-art password probability models. We also reveal some interesting password habits from the semantics on "long" passwords. Based on those findings, WordMarkov achieves 75.35\%$96.34 \%$ attack improvement.


Index Terms- Markov Chain, password probability model, word segmentation, semantic information of password

## 1. INTRODUCTION

Password probability model is one of the cornerstones for password systems, and academia and industry have drawn their attentions to yield practical and secure designs over a decade, e.g., $[1,2,3,4,5,6]$. The model has been widely investigated under the umbrella of password security, such as password guessing attack [1, 2, 7], password-strength meters [4, 8], honeywords [9], honeyvaults [10]. To provide strong password security one should fully capture a throughout and structural understanding on passwords [11]. Some research works may be only limited to superficial investigations on patterns [8, 12]. For example, they mainly focus on password length and the presence of printable characters via such as PCFG [1], Markov [2] and LSTM [4]. However, the "in-depth patterns", in particular the ones associated with the semantic information, should be further explored.

[^0]To address the problem, a few studies have been proposed in the literature, e.g., [3, 6]. But the most recent semantic password probability models may suffer from some practical shortcomings. In [3], Veras et al. used external corpus to investigate the semantic information. Unlike natural languages, passwords do not have a regular grammatical structure [13]. And this makes one difficult to accurately describe the semantic information of passwords from natural language dictionary. As for [6], Cheng et al. extracted password semantic information by a Chinese word extraction approach. Although they did not use external corpus, their PCFG model still cannot provide generalization [2]. It is impossible to calculate or sample structures that are not included in the training set.

### 1.1. Our Contributions

We propose a new password probability model based on the Markov Chain, called WordMarkov. The Markov model (hereafter we call it Markov) is one of the mainstream tools used to study password distribution in the context of password security. In the design of Markov, a password is treated as a whole, in which we only consider the association between characters. With the help of the word extraction method proposed in [6], we divide the password into independent semantic segments (also called words) and regard a password as multiple words connected. Due to the special features of Markov, our WordMarkov can identify the semantic information in the passwords more accurately (than the current research works), but also inherit the advantages of the Markov to provide superior generalization.

We further find some interesting password habits. Language words or names (e.g., "swan","4ever", "Carlos") are more frequently used in long passwords, than keyboard patterns (e.g., "qwer", "1q2w3e"). Note by long passwords we here mean those with the length $>12$ characters. This indicates that using words/names pattern may help one to perform password guessing attacks. But the phenomenon for short passwords is the other way round.

Then we perform an empirical evaluation of the WordMarkov under the password guessing attack on six practical
datasets, and the experimental results show that the WordMarkov is able to achieve $24.29 \%-67.37 \%$ improvement over the current models. In particular, for long password guessing, its improvement can reach $75.35 \%-96.34 \%$.

## 2. PASSWORD PROBABILITY MODEL

Password probability models usually assign a probability value to each string [2]. They may help one to understand what makes users choose strong or weak passwords. And well-design models can further be applied in password strength meters [4], password cracking utilities [1] and honey encryption [14]. Generally speaking, there are two types of models to describe password distribution: one is char-based model [2, 4, 12, 14] and the other is template-based model [1, 3, 5, 10].

The char-based model is built on an intuitive idea that the probability of a user entering the current character only depends on his/her historical inputs (e.g., previously input characters). The password probability is calculated as the product of the probabilities on all the characters from a given password. Narayanan et al. [12] first used Markov to guess passwords in the char-based model. And later Ma et al. [2] proposed a more comprehensive study. A series of improvements have been proposed to optimize Markov, such as Length normalization, End-symbol normalization and Laplace smoothing. In 2016, Melicher et al. [4] applied deep learning to the password probability model and proposed LSTM of password. The overall framework is still based on Markov Chain. The difference is that when calculating the character probability, the model obtains the probability of the next character by inputting the prefix into the neural network, rather than simply counting the frequency of the string in the training set. The char-based model can provide good generalization, and it is possible to generate any passwords in the password space. However, because char-based model only focuses on characters, it is hard to reveal the semantics from passwords in the model.

The core assumption of template-based model is users habitually choose several different meaning segments and group them together as a password [6]. A password's probability is now the probability of its structure multiplied by those of its segments. Weir et al. [1] propose the first PCFG model for passwords, which divides a password into three types (namely letter, digit, special-symbol) of segments and marks the length for each segment. Cheng et al. [6] proposed WordPCFG in 2021, introducing the concept of word in PCFG by a Chinese word extraction approach. More specifically, the words are independent semantic segments of passwords. They introduced a new type of segments, word, to the original PCFG, which significantly improves the accuracy of capturing password distributions. The template-based model assumes that the each segment and template in the password are independent, and it is unable to generate those segments and tem-
plates which do not exist in the training set.
To get rid of this shortcoming, we investigate the semantic information in passwords based on Markov Chain, and further propose a semantic password probability model with both generalization and accuracy.


Fig. 1. The training process by WordMarkov

## 3. OUR APPROACH

### 3.1. Word Segmentation Method

Passwords do not have a regular grammatical structure [13] and thus, the word extraction method in natural language is not applicable here. We leverage the word extraction method proposed in [6] to extract the word dictionary from passwords. The words of a password are multiple independent semantic segments. We use the default configuration in the research [6], but we set the maximum and minimum length of each word in order to achieve practical performance (after several attempts): min_length $=3$, and max_length $=8$. In word segmentation, we recognize words in a password by Positive Maximum Matching, and the rest parts are also regarded as words even if they are not extracted into words.

### 3.2. The Design of WordMarkov

We first segment password into multiple independent semantic segments, calculate the probability of each segment, and finally multiply them to obtain the probability of password. Recall that the probability of a user entering the current character only depends on the historical characters, in the Markov Chain [12, 2]. The core assumption of Markov Chain is defined as:

$$
\begin{equation*}
\operatorname{Pr}\left(x_{i} \mid x_{i-1}, \ldots, x_{1}\right)=\operatorname{Pr}\left(x_{i} \mid x_{i-1}, \ldots, x_{i-k}\right) \tag{1}
\end{equation*}
$$

For example, 2-order Markov calculates the probability of string $c_{1} c_{2} \ldots c_{n-1} c_{n}$ as:

$$
\begin{equation*}
\operatorname{Pr}(s)=\operatorname{Pr}\left(c_{2} \mid c_{1}\right) \cdot \operatorname{Pr}\left(c_{3} \mid c_{1} c_{2}\right) \ldots \operatorname{Pr}\left(c_{n} \mid c_{n-2} c_{n-1}\right) \tag{2}
\end{equation*}
$$

We use the Laplace Smoothing method to compensate for overfitting and improve the generalization. Then the transition probability of the Markov Chain is defined as follows:

$$
\begin{align*}
& \operatorname{Pr}\left(c_{k+1} \mid c_{1} c_{2} \ldots c_{k}\right)= \\
& \frac{\operatorname{count}\left(c_{1} \ldots c_{k} c_{k+1}\right)+\sigma}{\sum_{c_{k+1}^{\prime} \in \Omega}\left(\operatorname{count}\left(c_{1} \ldots c_{k} c_{k+1}^{\prime}\right)+\sigma\right)} \tag{3}
\end{align*}
$$

where $\Omega$ is the set of all characters, and $\sigma$ is the parameter for Laplace Smooth.

However, Markov does not consider the semantics of the password [3]. For example, for the password "password123", it is easy to recognize that the password is composed of two segments. But Markov believes that the probability of character " 1 " is strongly related to its previous three characters "ord". This clearly contradicts to common sense.

To solve this problem, we introduce a Split-Symbol which divides password into independent semantic segmentswords. The Split-Symbol clears the historical information of the previous word, and the new word can be generated from the Split-Symbol without relying on the historical information. We then have the core idea of WordMarkov:

$$
\begin{equation*}
\operatorname{Pr}_{\mathrm{pw}}(\text { password })=\prod_{1}^{n} \operatorname{Pr}_{\mathrm{w}}\left(\text { word }_{i}\right) \tag{4}
\end{equation*}
$$

As shown in Fig. 1, in the training phase of WordMarkov, we add a Begin-Symbol to the head and a End-Symbol to the tail of each password. The Begin-Symbol, End-Symbol and Split-Symbol are regarded as ordinary characters. For readers' convenience, we use the " $c_{b}, c_{s}, c_{e}$ " to represent the BeginSymbol, Split-Symbol and End-Symbol in the following.


Fig. 2. An example of WordMarkov processing password
In Fig. 2, the password "John@1996" is divided into three words "John", "@" and "1996", and the WordMarkov can be regarded as a chain of multiple independent sub-chains. The probability of "John@1996" is calculated by 1-order WordMarkov as follows (for demonstration purposes, the order here is 1 ):

$$
\begin{aligned}
& \operatorname{Pr}_{\mathrm{pw}}(\mathrm{John} 1996)=\operatorname{Pr}_{\mathrm{w}}(\mathrm{John}) \cdot \operatorname{Pr}_{\mathrm{w}}(@) \cdot \operatorname{Pr}_{\mathrm{w}}(1996) \\
& \operatorname{Pr}_{\mathrm{w}}(\mathrm{John})=\mathrm{P}\left(\mathrm{~J} \mid c_{b}\right) \mathrm{P}(\mathrm{o} \mid \mathrm{J}) \mathrm{P}(\mathrm{~h} \mid \mathrm{o}) \mathrm{P}(\mathrm{n} \mid \mathrm{h}) \mathrm{P}\left(c_{s} \mid \mathrm{n}\right) \\
& \operatorname{Pr}_{\mathrm{w}}(@)=\mathrm{P}\left(@ \mid c_{s}\right) \mathrm{P}\left(c_{s} \mid @\right) \\
& \operatorname{Pr}_{\mathrm{w}}(1996)=\mathrm{P}\left(1 \mid c_{s}\right) \mathrm{P}(9 \mid 1) \mathrm{P}(9 \mid 9) \mathrm{P}(6 \mid 9) \mathrm{P}\left(c_{e} \mid 6\right)
\end{aligned}
$$

Table 1. Information of the leaked password datasets

| Dataset | Language | Total | $>12$ chars | Percentage |
| :--- | :--- | ---: | ---: | ---: |
| Rockyou | English | $32,581,870$ | $1,143,282$ | $3.50 \%$ |
| 000Webhost | English | $15,250,725$ | $2,512,525$ | $16.47 \%$ |
| Clixsense | English | $2,222,046$ | 150,631 | $6.77 \%$ |
| Tianya | Chinese | $30,901,241$ | $1,272,043$ | $4.11 \%$ |
| Dodonew | Chinese | $16,258,891$ | 371,830 | $2.28 \%$ |
| CSDN | Chinese | $6,428,277$ | 467,985 | $7.28 \%$ |

Table 2. Word count of the datasets

| Dataset | Total | $>12$ chars | Percentage |
| :--- | ---: | ---: | ---: |
| Rockyou | $7,510,232$ | 754,568 | $10.04 \%$ |
| 000Webhost | $5,932,846$ | $1,839,758$ | $31.01 \%$ |
| Clixsense | 948,363 | 126,135 | $13.30 \%$ |
| Tianya | $6,362,217$ | 886,940 | $13.94 \%$ |
| Dodonew | $4,929,769$ | 210,781 | $4.27 \%$ |
| CSDN | $2,122,924$ | 358,838 | $16.90 \%$ |

Table 3. Cracking rate under the guesses

| Dataset | Model | Total |  | $>12$ chars |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $10^{9}$ | $10^{12}$ | $10^{9}$ | $10^{12}$ |
| 000Webhost | WordMarkov | 42.17\% | 68.22\% | 21.03\% | 34.04\% |
|  | Markov | 27.84\% | 55.36\% | 2.84\% | 10.69\% |
|  | LSTM | 21.29\% | 49.93\% | 2.39\% | 6.55\% |
|  | WordPCFG | 36.21\% | 53.78\% | 3.72\% | 12.73\% |
|  | PCFG | 38.19\% | 53.47\% | 16.82\% | 25.94\% |
| CSDN | WordMarkov | 64.31\% | 88.04\% | 35.42\% | 58.38\% |
|  | Markov | 51.74\% | 82.50\% | 9.15\% | 31.91\% |
|  | LSTM | 48.49\% | 80.47\% | 8.72\% | 26.26\% |
|  | WordPCFG | 51.40\% | 77.49\% | 8.44\% | 26.17\% |
|  | PCFG | 46.89\% | 53.27\% | 18.04\% | 24.43\% |
| Rockyou | WordMarkov | 76.10\% | 93.15\% | 28.52\% | 47.89\% |
|  | Markov | 70.20\% | 90.68\% | 4.81\% | 22.11\% |
|  | LSTM | 65.58\% | 88.68\% | 6.12\% | 18.82\% |
|  | WordPCFG | 73.68\% | 88.33\% | 11.07\% | 27.31\% |
|  | PCFG | 70.69\% | 75.15\% | 19.50\% | 24.00\% |
| Dodonew | WordMarkov | 68.73\% | $\mathbf{9 4 . 7 3 \%}$ | 42.92\% | 70.84\% |
|  | Markov | 58.16\% | 92.66\% | 25.52\% | 56.49\% |
|  | LSTM | 52.52\% | 91.15\% | 22.96\% | 51.39\% |
|  | WordPCFG | 58.15\% | 85.83\% | 16.24\% | 45.06\% |
|  | PCFG | 56.73\% | 64.14\% | 28.45\% | 32.81\% |
| Clixsense | WordMarkov | 64.90\% | 85.63\% | 31.82\% | 47.06\% |
|  | Markov | 51.84\% | 78.44\% | 3.86\% | 14.97\% |
|  | LSTM | 49.19\% | 82.33\% | 6.09\% | 22.17\% |
|  | WordPCFG | 45.40\% | 67.32\% | 7.98\% | 23.57\% |
|  | PCFG | 36.74\% | 52.27\% | 16.44\% | 20.43\% |
| Tianya | WordMarkov | 77.96\% | 93.75\% | 32.26\% | 56.05\% |
|  | Markov | 71.73\% | 90.97\% | 7.24\% | 29.42\% |
|  | LSTM | 63.82\% | 86.78\% | 7.02\% | 20.28\% |
|  | WordPCFG | 69.71\% | 82.13\% | 12.97\% | 26.55\% |
|  | PCFG | 69.88\% | 73.50\% | 17.25\% | 23.33\% |

## 4. EXPERIMENTS AND RESULTS

### 4.1. Datasets

As is shown in Table 1, we collect over 103 million plaintext passwords from the public datasets [5,15, 16] to simulate password guessing attacks. Our experiments thus can present


Fig. 3. The performance of WordMarkov on password guessing attack


Fig. 4. The performance of WordMarkov on long password guessing attack
a scalable and comprehensive view of password habits in the real-world applications. In Table 2, the distribution of words in passwords is not uniform. The proportion of words in long passwords is relatively high, which indicates that long passwords contain more semantic information (i.e. more words). We state that the datasets have been widely used and studied in the previous works [4, 2, 6, 5, 15, 17]. And our research does not violate any ethical practice and privacy guidance, because we only exploit attacks on the public known datasets, which does not harm user privacy and application security.

### 4.2. Experiment Setup

We evaluate the efficiency of WordMarkov via offline guessing on the datasets given in Table 1. It is generally accepted that the more precise probability a password model can provide, the more efficient the attack can be $[1,2,4,6]$. To preclude the impact of non-uniformly training data, we employ a random sampling; and then we adopt a cross-validation approach of $k$-fold (where $k=4$ ). Specifically, we randomly split passwords into four-folds, and adopt any three of them as the training data and the last one for the testing data. In the evaluation, we use the Monte Carlo method [17] to show the results for the large number of guesses.

### 4.3. Evaluation of WordMarkov

We use the curve of cracking rate vs. guesses to show the performance of the WordMarkov model. As Fig. 3 and Table 3 shown, in the large-scale datasets (e.g., Dodonew, Rockyou), the performances of other models are close, and WordMarkov obtains $8.99 \%-24.29 \%$ improvement over others. For the small-scale sets (e.g., CSDN, 000Webhost), our improvement can reach $31.22 \%-67.30 \%$, as compared to others. We further perform a series of experiments on long passwords in Fig. 4 and Table 3. The WordMarkov obtains $75.35 \%-96.34 \%$ improvement, outperforming other models in long password guessing.

## 5. CONCLUSION

We propose WordMarkov that is a novel semantic password probability model. We perform the experiments on the real-world datasets and the results show that WordMarkov achieves a significant improvement on password guessing and outperforms the state-of-the-art models' accuracy and generalization. And WordMarkov performs particularly excellent under long password guessing. We state that WordMarkov may be used in other models which are based on Markov Chain. The improvement for the word segmentation approach could be left as an interesting open problem.

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[^0]:    *Corresponding author.
    This research is supported by National Natural Science Foundation of China (6207071129) and by National Key R\&D Program of China (2020YFB1806400).

