

Theoretical Equations for the Study of Entropy of Emotions and Enhancing Performance of Artificial Intelligence

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Basic entropy evaluation

$$\text{d}^2x + d^2\pi^x - d^2x^{1/3} - d^2\sqrt{x}$$

Equation (eq) 1

In[3]:= $d^2 \pi^x + d^2 x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}$

Out[3]= $d^2 \pi^x + d^2 x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}$

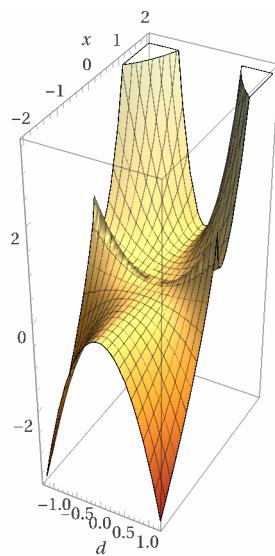
In[4]:=  $d^2x + d^2\pi^x - d^2\sqrt[3]{x} - d^2\sqrt{x}$

Input:

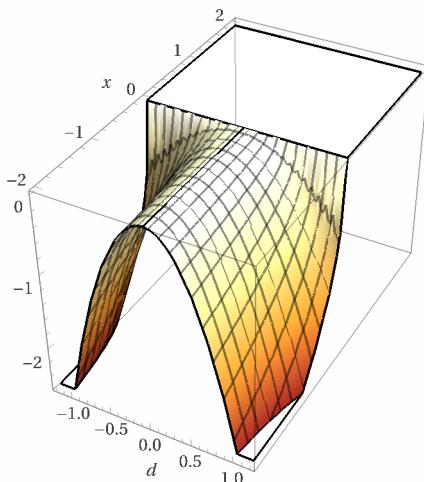
$$d^2 x + d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}$$

3D plots:

Real part:



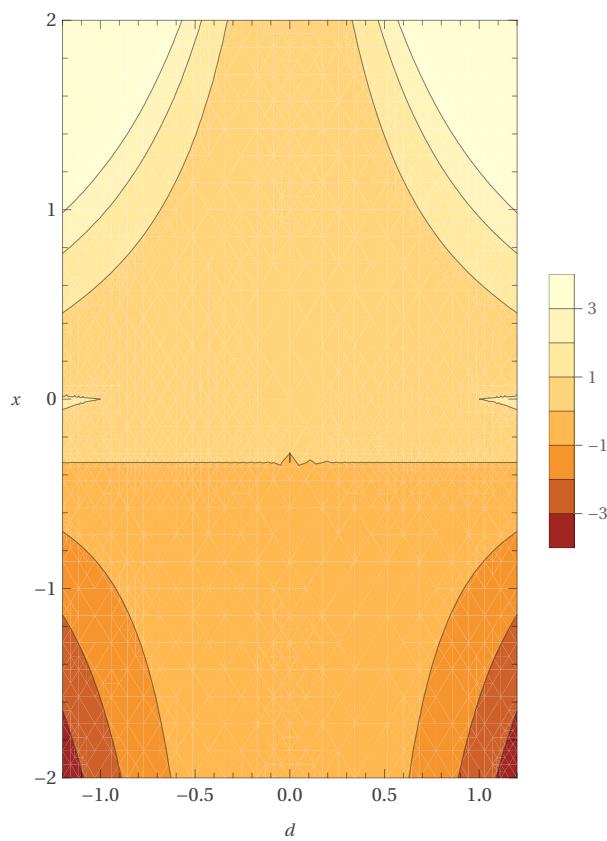
Imaginary part:



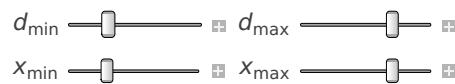
Contour plots:



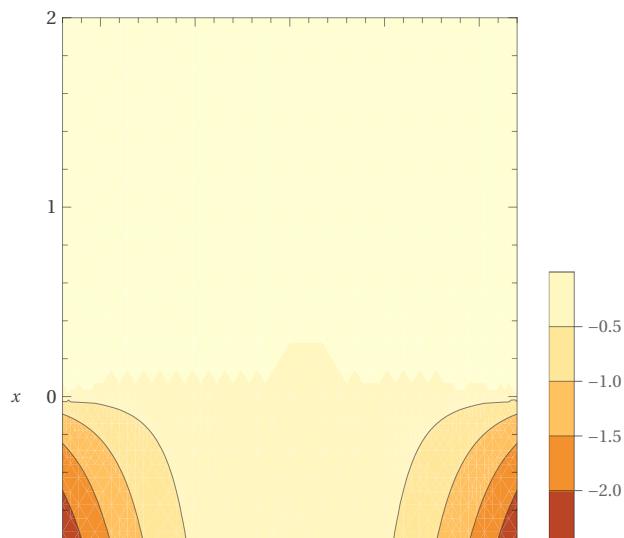
Real part:

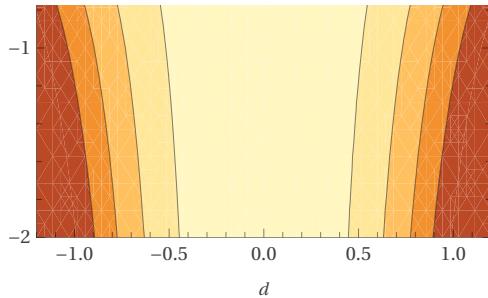


Out[4]=



Imaginary part:





d_{\min} d_{\max}
 x_{\min} x_{\max}

Alternate form:

$$d^2 \left(x - \sqrt{x} - \sqrt[3]{x} + \pi^x \right)$$

Real root:

$$d = 0, \quad x \geq 0$$

Property as a real function:

Domain:

$$\{x \in \mathbb{R} : x \geq 0\} \text{ (all non-negative real numbers)}$$

R is the set of real numbers »

Series expansion at $x = 0$:

$$\begin{aligned} & d^2 - d^2 \sqrt[3]{x} - d^2 \sqrt{x} + d^2 x (1 + \log(\pi)) + \frac{1}{2} d^2 x^2 \log^2(\pi) + \\ & \frac{1}{6} d^2 x^3 \log^3(\pi) + \frac{1}{24} d^2 x^4 \log^4(\pi) + \frac{1}{120} d^2 x^5 \log^5(\pi) + O(x^{16/3}) \end{aligned}$$

(Puiseux series)

log(x) is the natural logarithm »

Big-O notation »

Derivative:

Approximate form

Step-by-step solution



$$\frac{\partial}{\partial x} \left(d^2 x + d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x} \right) = \frac{d^2 (6 x^{2/3} (\pi^x \log(\pi) + 1) - 3 \sqrt[3]{x} - 2)}{6 x^{2/3}}$$

Indefinite integral:

Approximate form

Step-by-step solution



$$\int (d^2 x + d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}) dx = d^2 \left(-\frac{3 x^{4/3}}{4} - \frac{2 x^{3/2}}{3} + \frac{x^2}{2} + \frac{\pi^x}{\log(\pi)} \right) + \text{constant}$$

$$\blacksquare d^2x + d^2e^x - d^2x^{1/3} - d^2\sqrt{x}$$

Eq 2

In[5]:= $d^2x + d^2e^x - d^2x^{1/3} - d^2\sqrt{x}$

Out[5]= $d^2 e^x + d^2 x - d^2 \sqrt{x} - d^2 \sqrt[3]{x}$

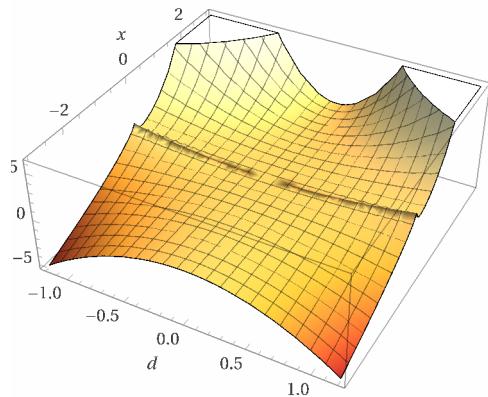
In[7]:= $\blacksquare d^2x + d^2e^x - d^2x^{1/3} - d^2\sqrt{x}$

Input:

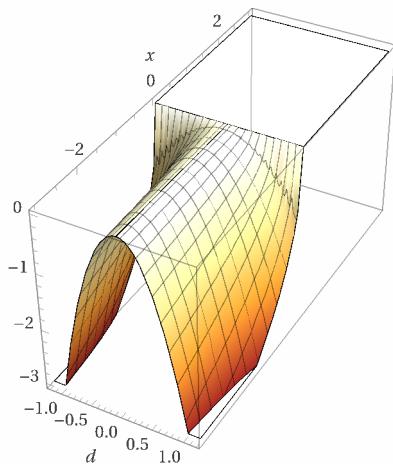
$$d^2x + d^2e^x - d^2\sqrt[3]{x} - d^2\sqrt{x}$$

3D plots:

Real part:



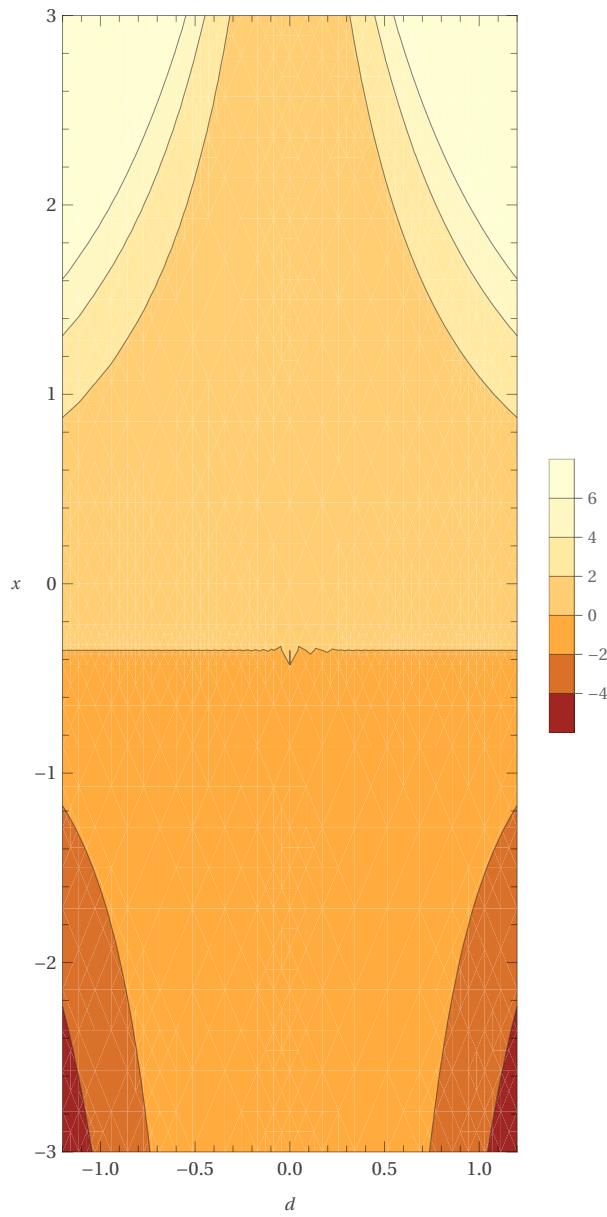
Imaginary part:



Contour plots:



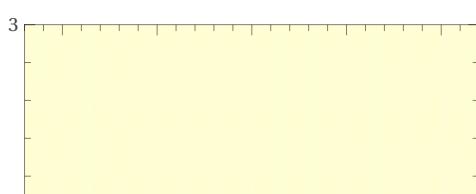
Real part:

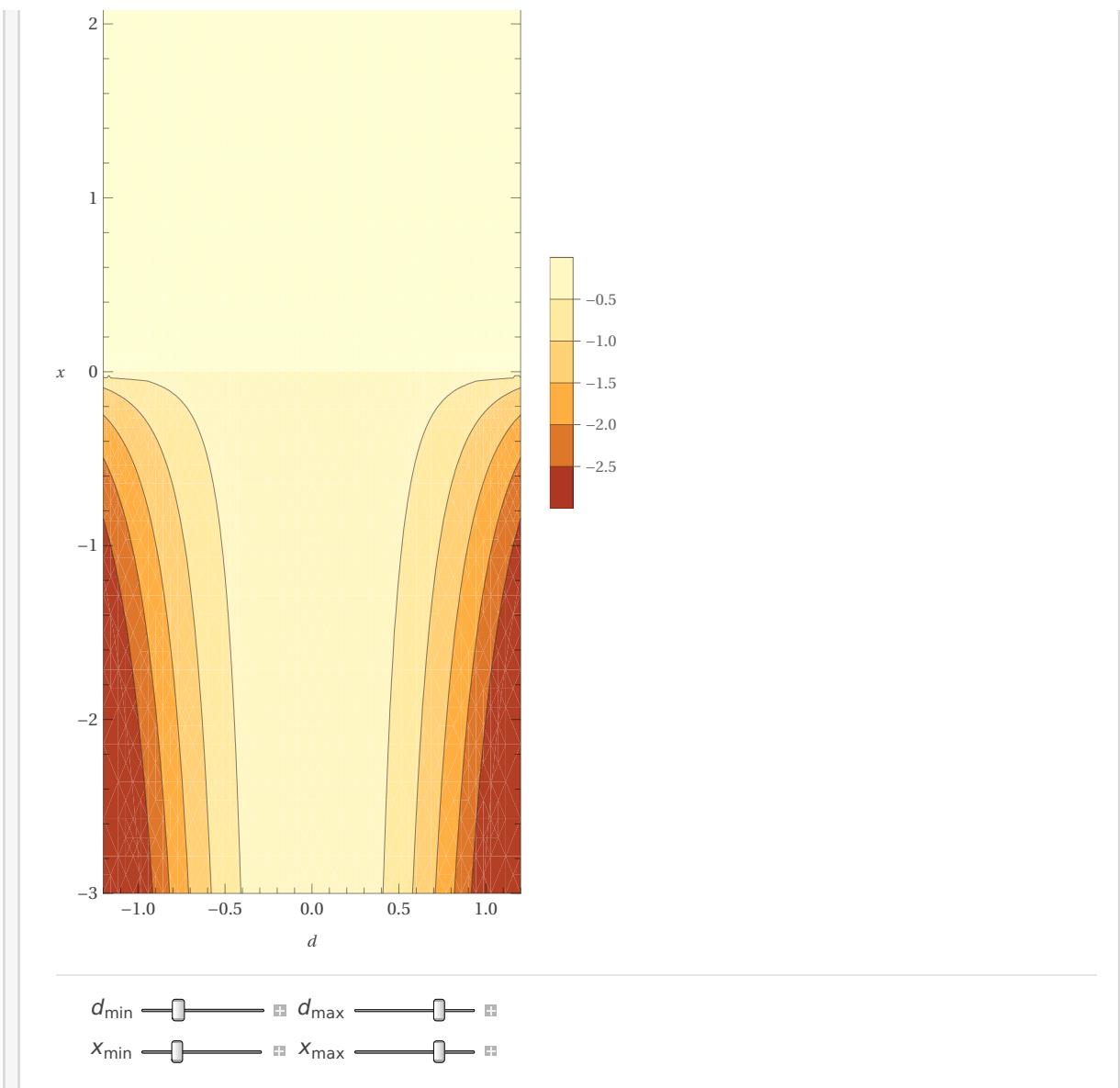


Out[7]=

d_{\min} d_{\max}
 x_{\min} x_{\max}

Imaginary part:





Alternate forms:

$$d^2(x - \sqrt{x} - \sqrt[3]{x} + e^x)$$

$$d^2(x^{2/3} - \sqrt[6]{x} - 1) \sqrt[3]{x} + d^2 e^x$$

Real root:

$$d = 0, \quad x \geq 0$$

Property as a real function:

Domain:

$$\{x \in \mathbb{R} : x \geq 0\} \text{ (all non-negative real numbers)}$$

[R is the set of real numbers >](#)

Series expansion at $x = 0$:

$$d^2 - d^2 \sqrt[3]{x} - d^2 \sqrt{x} + 2 d^2 x + \frac{d^2 x^2}{2} + \frac{d^2 x^3}{6} + \frac{d^2 x^4}{24} + O(x^5)$$

(Puiseux series)

[Big-O notation »](#)

Derivative:

[Step-by-step solution](#)

$$\frac{\partial}{\partial x} (d^2 x + d^2 e^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}) = \frac{d^2 (6 x^{2/3} (e^x + 1) - 3 \sqrt[6]{x} - 2)}{6 x^{2/3}}$$

Indefinite integral:

[Step-by-step solution](#)

$$\int (d^2 x + d^2 e^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}) dx = d^2 \left(\frac{1}{12} (-9 x^{4/3} - 8 x^{3/2} + 6 x^2) + e^x \right) + \text{constant}$$

[WolframAlpha](#)

In[6]:= Simplify[d^2 e^x - d^2 x^(1/3) - d^2 Sqrt[x] + d^2 x]

Out[6]= $d^2 (x - \sqrt{x} - \sqrt[3]{x} + e^x)$

$d^2 x - d^2 \pi^x - d^2 x^{1/3} - d^2 \sqrt{x}$

Eq 3

In[8]:= $d^2 x - d^2 \text{Pi}^x - d^2 x^{(1/3)} - d^2 \text{Sqrt}[x]$

Out[8]= $d^2 (-\pi^x) + d^2 x - d^2 \sqrt{x} - d^2 \sqrt[3]{x}$

In[10]:= $d^2 x - d^2 \pi^x - d^2 x^{1/3} - d^2 \sqrt{x}$

Out[10]=

Input:

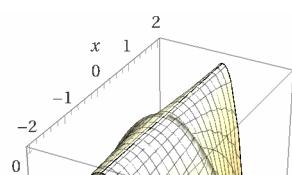
$$d^2 x - d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}$$

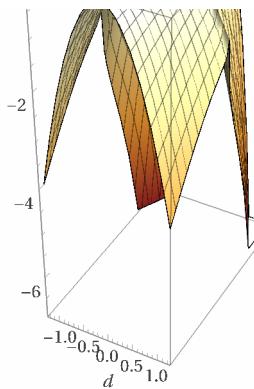
Result:

$$d^2 (-\pi^x) + d^2 x - d^2 \sqrt{x} - d^2 \sqrt[3]{x}$$

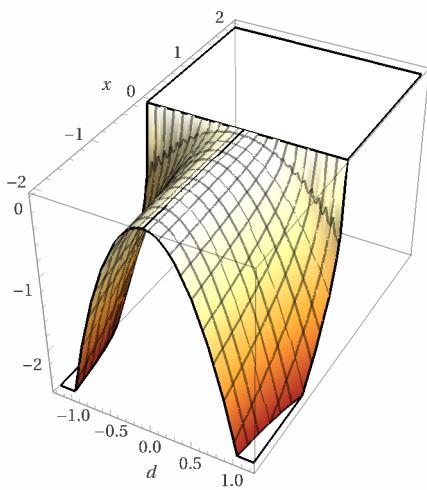
3D plots:

Real part:





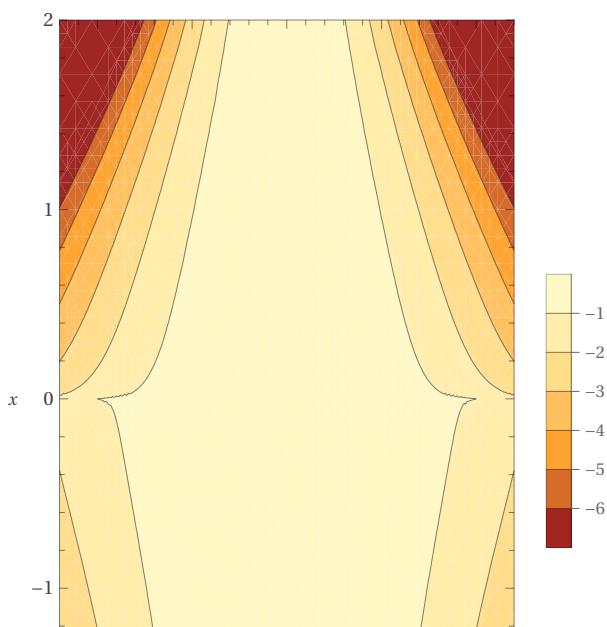
Imaginary part:

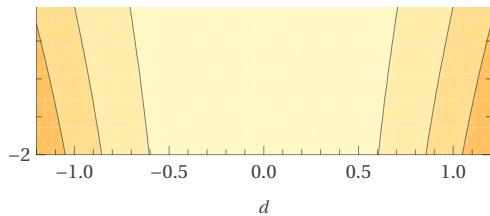


Contour plots:



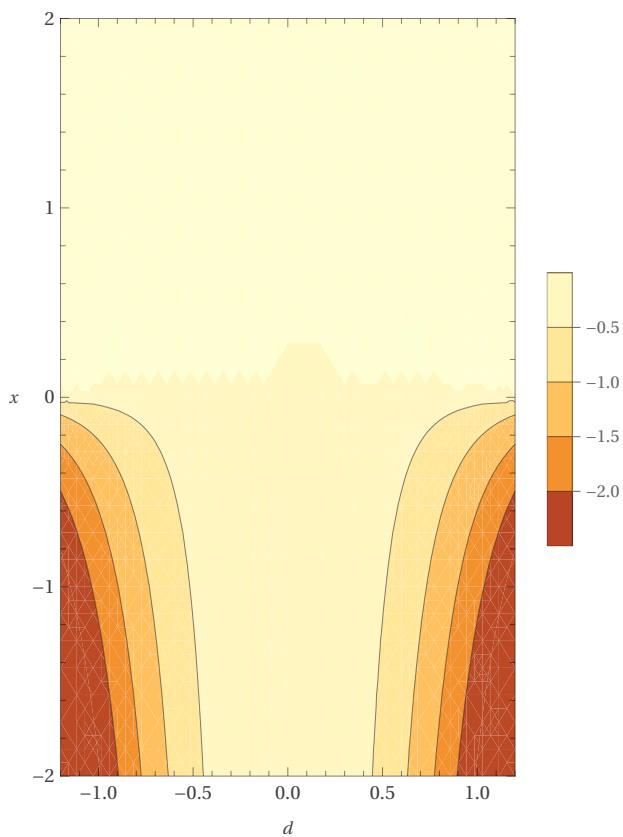
Real part:





d_{\min} d_{\max}
 x_{\min} x_{\max}

Imaginary part:



d_{\min} d_{\max}
 x_{\min} x_{\max}

Alternate forms:



$$-d^2(-x + \sqrt{x} + \sqrt[3]{x} + \pi^x)$$

$$d^2(x - \sqrt{x} - \sqrt[3]{x} - \pi^x)$$

Real root:



$$d = 0, \quad x \geq 0$$

Property as a real function:

Domain:

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R is the set of real numbers »

Series expansion at $x = 0$:

$$\begin{aligned} -d^2 - d^2 \sqrt[3]{x} - d^2 \sqrt{x} - d^2 x (\log(\pi) - 1) - \frac{1}{2} x^2 (d^2 \log^2(\pi)) - \\ \frac{1}{6} x^3 (d^2 \log^3(\pi)) - \frac{1}{24} x^4 (d^2 \log^4(\pi)) - \frac{1}{120} x^5 (d^2 \log^5(\pi)) + O(x^{16/3}) \end{aligned}$$

(Puiseux series)

log(x) is the natural logarithm »

Big-O notation »

Derivative:

Approximate form

Step-by-step solution

$$\frac{\partial}{\partial x} (d^2 x - d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}) = -\frac{d^2 (6 x^{2/3} (\pi^x \log(\pi) - 1) + 3 \sqrt[6]{x} + 2)}{6 x^{2/3}}$$

Indefinite integral:

Approximate form

Step-by-step solution

$$\int (-d^2 \pi^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x} + d^2 x) dx = -d^2 \left(\frac{3 x^{4/3}}{4} + \frac{2 x^{3/2}}{3} - \frac{x^2}{2} + \frac{\pi^x}{\log(\pi)} \right) + \text{constant}$$

WolframAlpha

In[9]:= Simplify[-d^2 π^x - d^2 x^(1/3) - d^2 √x + d^2 x]

Out[9]= $-d^2 (-x + \sqrt{x} + \sqrt[3]{x} + \pi^x)$

Eq 4

$$\blacksquare d^{2x} - d^2 e^x - d^2 x^{1/3} - d^2 \sqrt{x}$$

In[11]:= d^2 x - d^2 E^x - d^2 x^(1/3) - d^2 Sqrt[x]

Out[11]=

$$d^2 (-e^x) + d^2 x - d^2 \sqrt{x} - d^2 \sqrt[3]{x}$$

In[13]:=  d^2 x - d^2 e^x - d^2 x^(1/3) - d^2 √x

Out[13]=

Input:

$$d^2 x - d^2 e^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x}$$

Result:

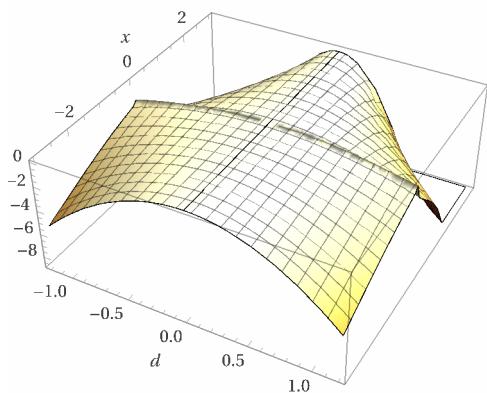
$$d^2 (-e^x) + d^2 x - d^2 \sqrt{x} - d^2 \sqrt[3]{x}$$



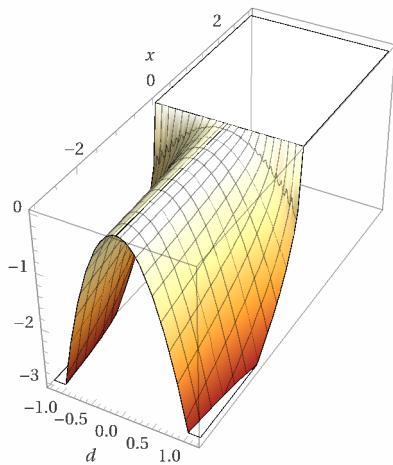
3D plots:



Real part:



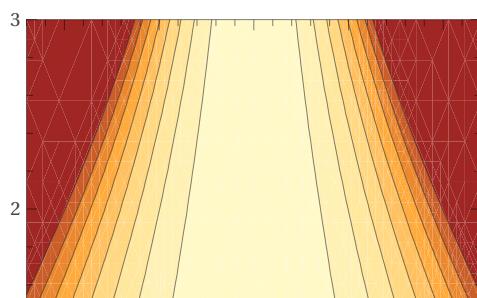
Imaginary part:

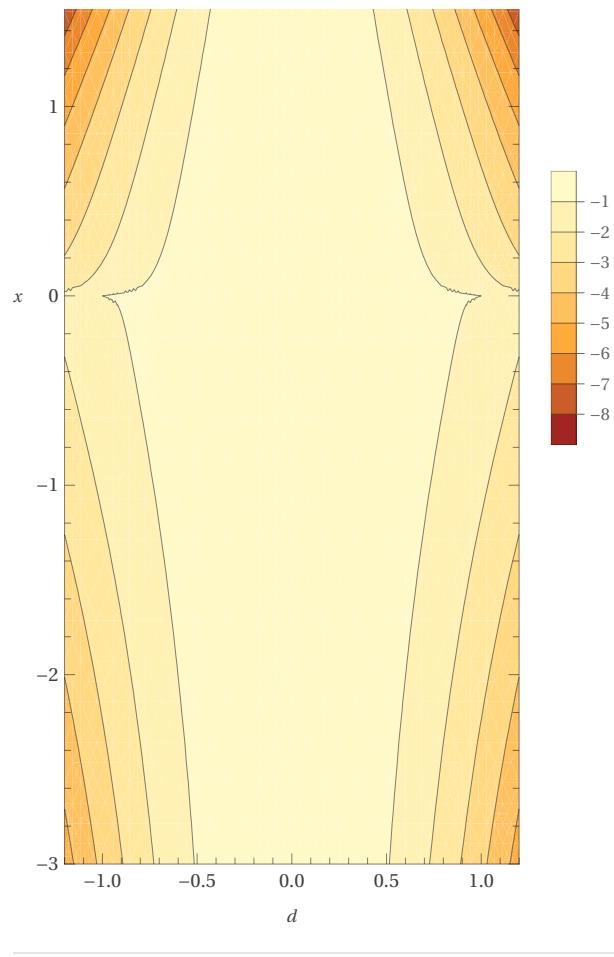


Contour plots:



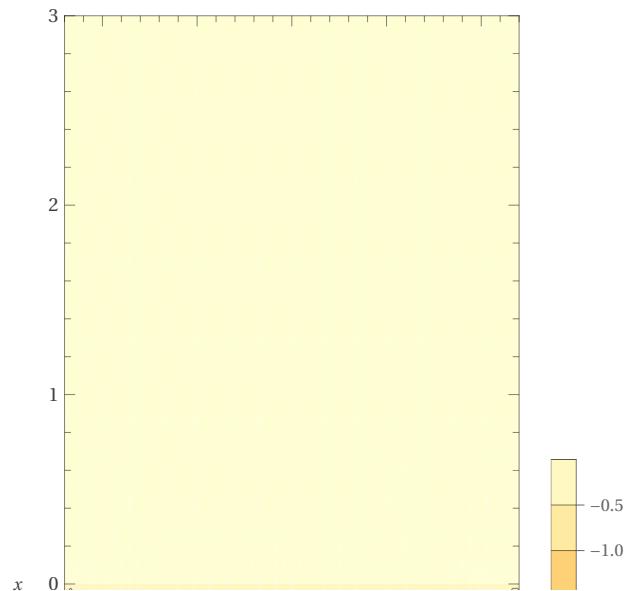
Real part:

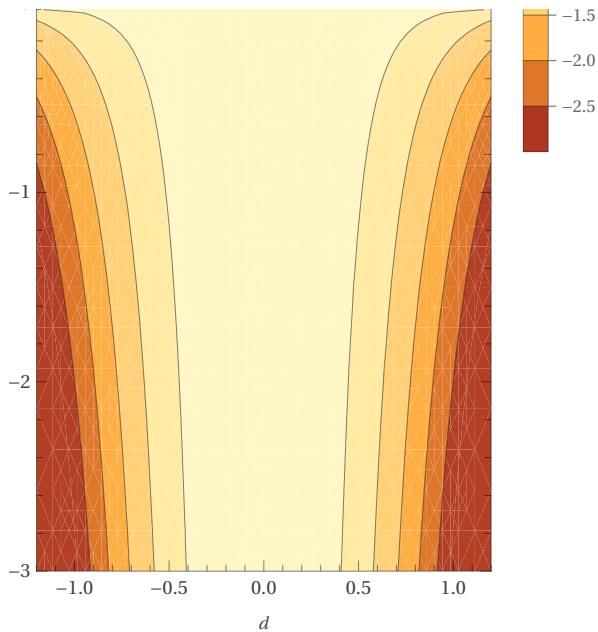




d_{\min} ————— d_{\max} x_{\min} ————— x_{\max}

Imaginary part:





$$\begin{array}{c} d_{\min} \text{---} \square \text{---} d_{\max} \\ x_{\min} \text{---} \square \text{---} x_{\max} \end{array}$$

Alternate forms:

$$-d^2(-x + \sqrt{x} + \sqrt[3]{x} + e^x)$$

$$d^2(x - \sqrt{x} - \sqrt[3]{x} - e^x)$$

$$d^2(x^{2/3} - \sqrt[6]{x} - 1) \sqrt[3]{x} - d^2 e^x$$

Real root:

$$d = 0, \quad x \geq 0$$

Property as a real function:

Domain:

$$\{x \in \mathbb{R} : x \geq 0\} \text{ (all non-negative real numbers)}$$

\mathbb{R} is the set of real numbers »

Series expansion at $x = 0$:

$$-d^2 - d^2 \sqrt[3]{x} - d^2 \sqrt{x} - \frac{d^2 x^2}{2} - \frac{d^2 x^3}{6} - \frac{d^2 x^4}{24} + O(x^5)$$

(Puiseux series)

Big-O notation »

Derivative:

$$\partial \quad \partial \quad \partial \quad \partial \quad \partial \quad \partial \quad d^2(6x^{2/3}(e^x - 1) + 3\sqrt[6]{x} + 2)$$

Step-by-step solution

$$\frac{d^2}{dx^2} \left(d^2 x - d^2 e^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x} \right) = -\frac{e^x + 2x^{1/3} + 2x^{1/2}}{6x^{2/3}}$$

Indefinite integral:

[Step-by-step solution](#)

$$\int (-d^2 e^x - d^2 \sqrt[3]{x} - d^2 \sqrt{x} + d^2 x) dx = -\frac{1}{12} d^2 (9x^{4/3} + 8x^{3/2} - 6x^2 + 12e^x) + \text{constant}$$

[WolframAlpha](#)

In[12]:= $\text{Simplify}[-d^2 e^x - d^2 x^{1/3} - d^2 \sqrt{x} + d^2 x]$

Out[12]=

$$-d^2 (-x + \sqrt{x} + \sqrt[3]{x} + e^x)$$

$d^2 x / dt^2 - d^2 e^x / dt^2 - d^2 x^{1/3} / dt^2 - d^2 \sqrt{x} / dt^2$

Eq 5

In[14]:= $D[x, \{t, 2\}] - d^2 2 * \left(E^x / D[t^2 - d^2 2 * \left(x^{1/3} / dt^2 \right) - d^2 \sqrt{x}, t]^2 \right)$

Out[14]=

$$-\frac{d^2 e^x t^{d^2 \sqrt[3]{x} (2/dt^2) + 2} d^2 \sqrt{x} - 2}{(d^2 \sqrt[3]{x} (-1/dt^2) - d^2 \sqrt{x} + 2)^2}$$

In[15]:= $d^2 x / dt^2 - d^2 e^x / dt^2 - d^2 x^{1/3} / dt^2 - d^2 \sqrt{x} / dt^2$

Out[15]=

Input interpretation:

$$x''(t) - d^2 \times \frac{e^x}{\left(\frac{\partial t^{2-d^2 \sqrt[3]{x}/(dt^2)} - d^2 \sqrt{x}}{\partial t} \right)^2}$$

Result:

$$x''(t) - \frac{d^2 e^x t^{d^2 \sqrt[3]{x} 2/dt^2 (\text{per metric deciton squared}) + 2} d^2 \sqrt{x} - 2}{(d^2 \sqrt[3]{x} - 1/dt^2 (\text{per metric deciton squared}) - d^2 \sqrt{x} + 2)^2}$$

[WolframAlpha](#)

$$\text{Eq 5}$$

$$\{d^2x/d^2t\} - \{d^2e^x/d^2t\} - \{d^2x^{1/3}/d^2t\} - \{d^2\sqrt{x}/d^2t\}$$

In[16]:= $d^2x/d^2t - d^2e^x/d^2t - d^2x^{1/3}/d^2t - d^2\sqrt{x}/d^2t$

Out[16]=

$$t(-e^x) + t x - t\sqrt{x} - t\sqrt[3]{x}$$

In[18]:= $\{d^2x/d^2t\} - \{d^2e^x/d^2t\} - \{d^2x^{1/3}/d^2t\} - \{d^2\sqrt{x}/d^2t\}$

Out[18]=

Input:

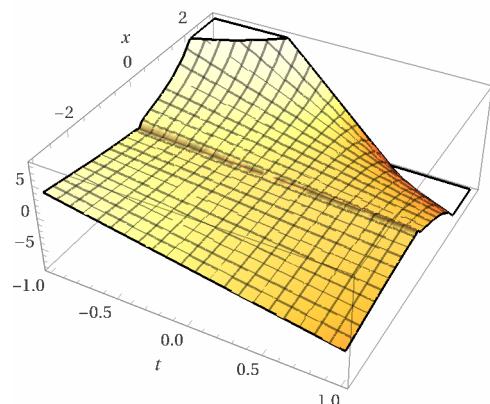
$$d^2x/d^2t - d^2e^x/d^2t - d^2x^{1/3}/d^2t - d^2\sqrt{x}/d^2t$$

Result:

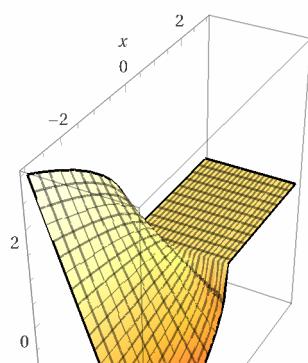
$$t(-e^x) + t x - t\sqrt{x} - t\sqrt[3]{x}$$

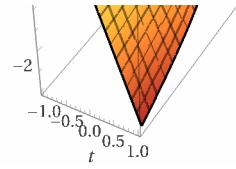
3D plots:

Real part:



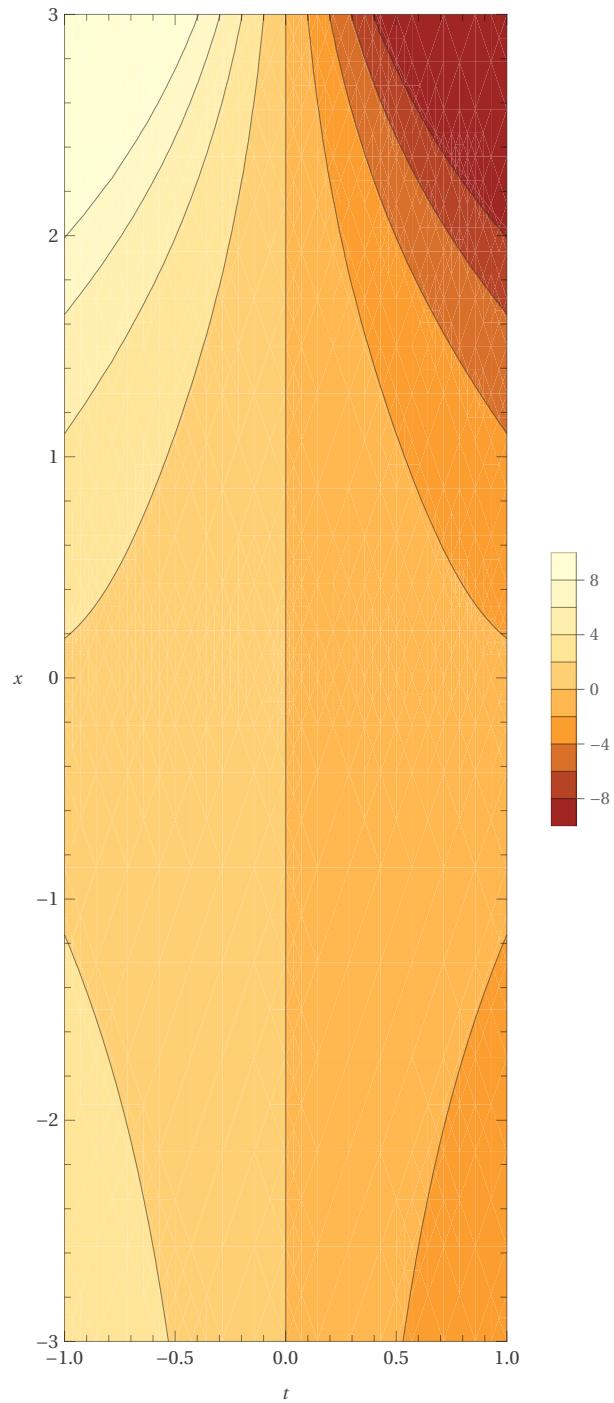
Imaginary part:

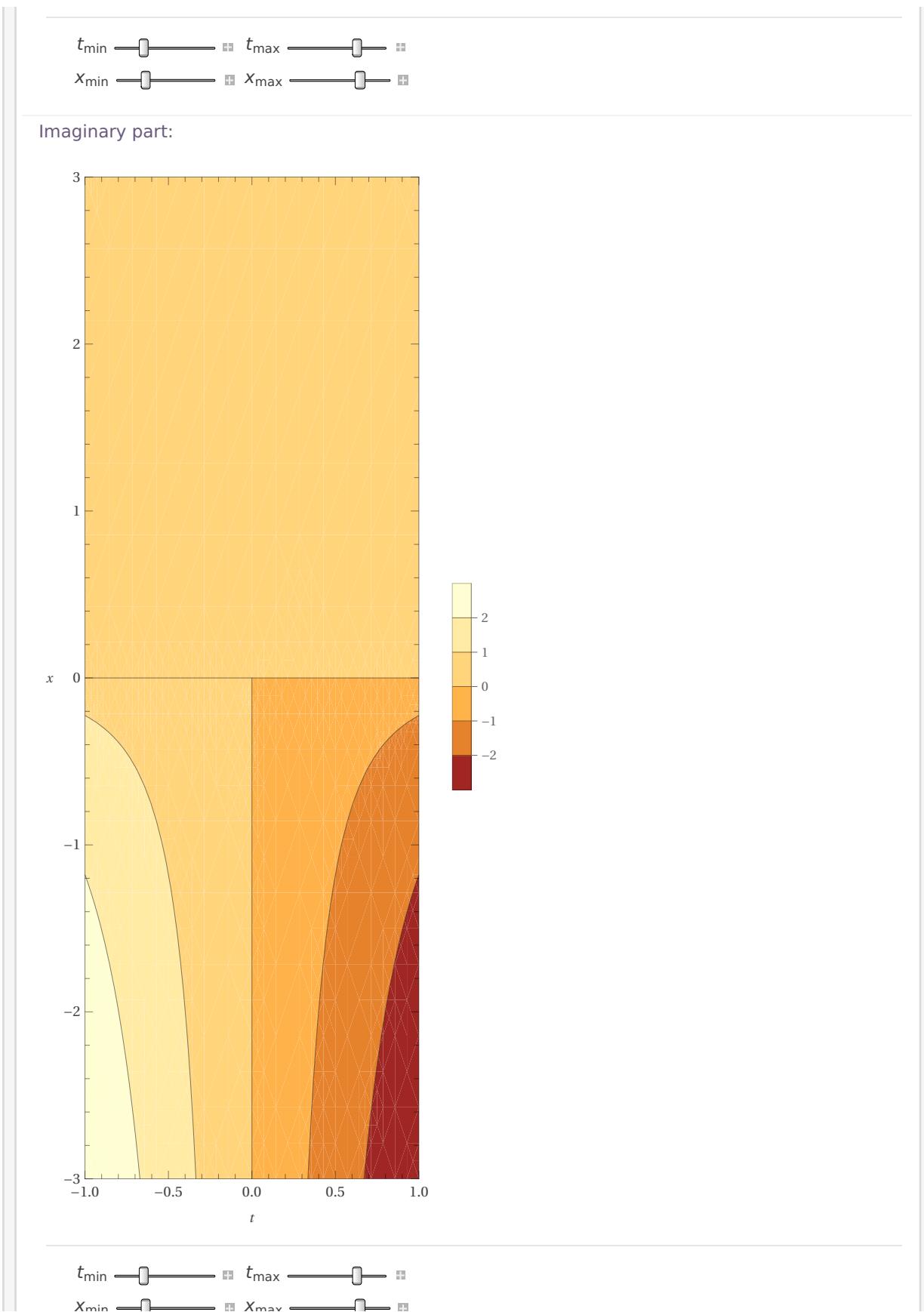




Contour plots:

Real part:





Alternate forms:

$$-t(-x + \sqrt{x} + \sqrt[3]{x} + e^x)$$

$$t(x - \sqrt{x} - \sqrt[3]{x} - e^x)$$

$$t(x^{2/3} - \sqrt[6]{x} - 1) \sqrt[3]{x} - t e^x$$

Real root:

$$t = 0, \quad x \geq 0$$

Series expansion at $x = 0$:

$$-t - t \sqrt[3]{x} - t \sqrt{x} - \frac{t x^2}{2} - \frac{t x^3}{6} - \frac{t x^4}{24} + O(x^5)$$

(Puiseux series)

[Big-O notation »](#)

Derivative:

[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{d^2 x t}{d^2} - \frac{d^2 e^x t}{d^2} - \frac{d^2 \sqrt[3]{x} t}{d^2} - \frac{d^2 \sqrt{x} t}{d^2} \right) = \frac{1}{6} t \left(-\frac{2}{x^{2/3}} - 6 e^x - \frac{3}{\sqrt{x}} + 6 \right)$$

Indefinite integral:

[Step-by-step solution](#)

$$\int (-e^x t - t \sqrt[3]{x} - t \sqrt{x} + t x) dx = -\frac{1}{12} t (9 x^{4/3} + 8 x^{3/2} - 6 x^2 + 12 e^x) + \text{constant}$$

[WolframAlpha](#)

In[17]:= **Simplify**[- $e^x t - t x^{1/3} - t \sqrt{x} + t x]$

Out[17]=

$$-t(-x + \sqrt{x} + \sqrt[3]{x} + e^x)$$

$$\blacksquare \{d^2 x/d^2 t\} - \{d^2 \pi^x/d^2 t\} - \{d^2 x^{1/3}/d^2 t\} - \{d^2 \sqrt{x}/d^2 t\}$$

Eq 6

In[1]:= $d^2 x/d^2 t - d^2 \pi^x/d^2 t - d^2 x^{1/3}/d^2 t - d^2 \sqrt{x}/d^2 t$

Out[1]= $t(-\pi^x) + t x - t \sqrt{x} - t \sqrt[3]{x}$

In[2]:= $\blacksquare \{d^2 x/d^2 t\} - \{d^2 \pi^x/d^2 t\} - \{d^2 x^{1/3}/d^2 t\} - \{d^2 \sqrt{x}/d^2 t\}$

Input:

v

π^x

$\sqrt[3]{v}$

\sqrt{v}

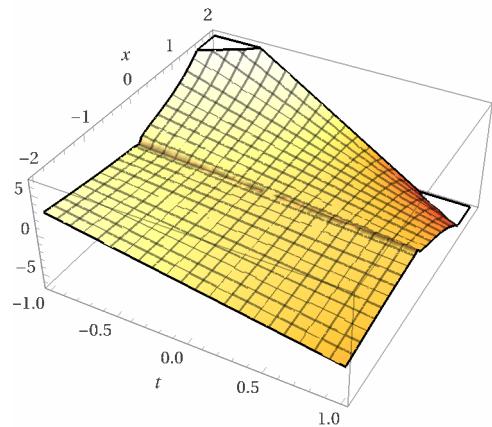
$$d^2 \times \frac{\pi}{d^2} t - d^2 \times \frac{\pi}{d^2} t - d^2 \times \frac{\pi}{d^2} t - d^2 \times \frac{\pi}{d^2} t$$

Result:

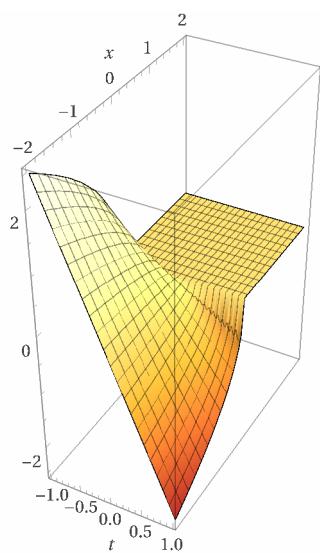
$$t(-\pi^x) + t x - t \sqrt{x} - t \sqrt[3]{x}$$

3D plots:

Real part:

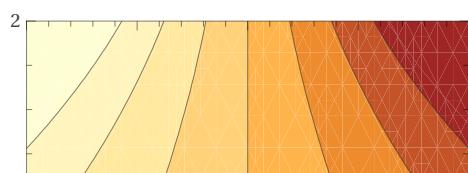


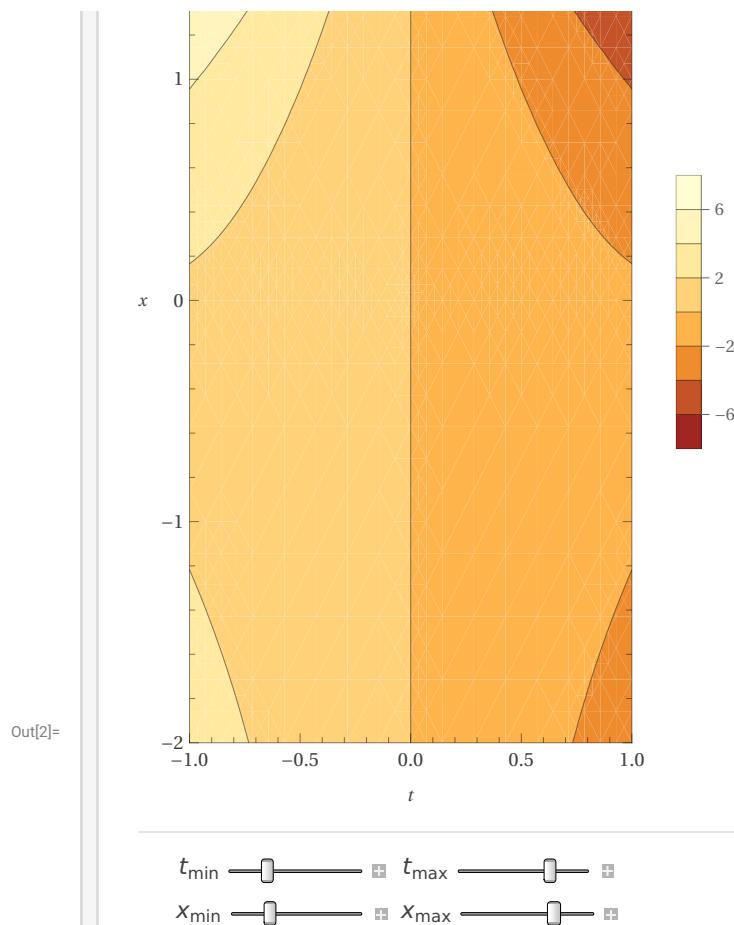
Imaginary part:



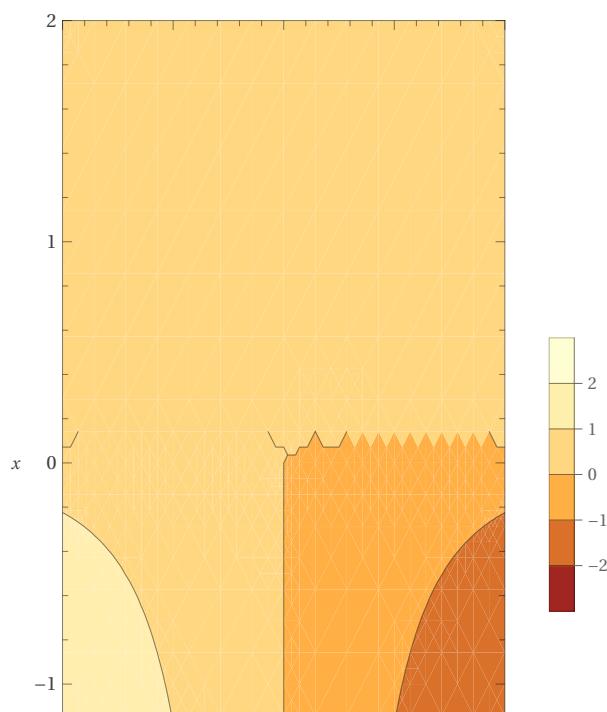
Contour plots:

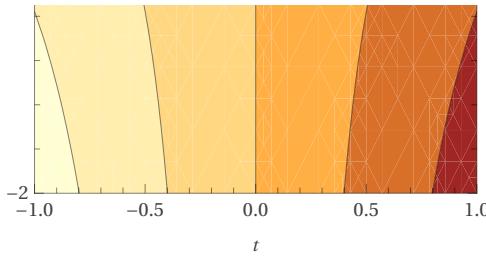
Real part:





Imaginary part:





t_{\min} t_{\max}

x_{\min} x_{\max}

Alternate forms:

$$-t(-x + \sqrt{x} + \sqrt[3]{x} + \pi^x)$$

$$t(x - \sqrt{x} - \sqrt[3]{x} - \pi^x)$$

Real root:

$$t = 0, \quad x \geq 0$$

Series expansion at $x = 0$:

$$\begin{aligned} & -t - t \sqrt[3]{x} - t \sqrt{x} + x(t - t \log(\pi)) - \frac{1}{2} x^2 (t \log^2(\pi)) - \\ & \frac{1}{6} x^3 (t \log^3(\pi)) - \frac{1}{24} x^4 (t \log^4(\pi)) - \frac{1}{120} x^5 (t \log^5(\pi)) + O(x^{16/3}) \end{aligned}$$

(Puiseux series)

log(x) is the natural logarithm [»](#)

Big-O notation [»](#)

Derivative:

[Approximate form](#)

[Step-by-step solution](#)



$$\frac{\partial}{\partial x} \left(\frac{d^2 x t}{d^2} - \frac{d^2 \pi^x t}{d^2} - \frac{d^2 \sqrt[3]{x} t}{d^2} - \frac{d^2 \sqrt{x} t}{d^2} \right) = \frac{1}{6} t \left(-\frac{2}{x^{2/3}} - \frac{3}{\sqrt{x}} - 6 \pi^x \log(\pi) + 6 \right)$$

Indefinite integral:

[Approximate form](#)

[Step-by-step solution](#)



$$\int (-\pi^x t - t \sqrt[3]{x} - t \sqrt{x} + t x) dx = -t \left(\frac{3 x^{4/3}}{4} + \frac{2 x^{3/2}}{3} - \frac{x^2}{2} + \frac{\pi^x}{\log(\pi)} \right) + \text{constant}$$

WolframAlpha [+/-](#)

$\blacksquare \{d^2 x/dt^2\} - \{d^2 \pi^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}$

Eq 7

In[3]:= $D[x, \{t, 2\}] - D[\text{Pi}^x, \{t, 2\}] - d^2 \frac{\partial^2 \pi^x}{\partial t^2} - D[\text{Sqrt}[x], \{t, 2\}]$

Out[3]= $d^2 \sqrt[3]{x} (-1/dt^2)$

In[4]:= $\boxed{\{d^2 x/dt^2\} - \{d^2 \pi^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}}$

Input interpretation:

$$x''(t) - \frac{\partial^2 \pi^x}{\partial t^2} - d^2 \times \frac{\sqrt[3]{x}}{dt^6 \text{ (metric deciton squared)}} - \frac{\partial^2 \sqrt{x}}{\partial t^2}$$

Out[4]=

Result:

$$d^2 \sqrt[3]{x} - 1/dt^6 \text{ (per metric deciton squared)} + x''(t)$$

WolframAlpha 

$\boxed{\{d^2 x/dt^2\} - \{d^2 e^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}}$ Eq 8

In[5]:= $D[x, \{t, 2\}] - D[e^x, \{t, 2\}] - d^2 \frac{\partial^2 e^x}{\partial t^2} - D[\text{Sqrt}[x], \{t, 2\}]$

Out[5]= $d^2 \sqrt[3]{x} (-1/dt^2)$

In[6]:= $\boxed{\{d^2 x/dt^2\} - \{d^2 e^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}}$

Input interpretation:

$$x''(t) - \frac{\partial^2 e^x}{\partial t^2} - d^2 \times \frac{\sqrt[3]{x}}{dt^2 \text{ (metric deciton squared)}} - \frac{\partial^2 \sqrt{x}}{\partial t^2}$$

Out[6]=

Result:

$$d^2 \sqrt[3]{x} - 1/dt^2 \text{ (per metric deciton squared)} + x''(t)$$

WolframAlpha 

$\boxed{\{d^2 x/dt^2\} + \{d^2 e^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}}$ Eq 9

In[7]:= $D[x, \{t, 2\}] + D[e^x, \{t, 2\}] - d^2 \frac{\partial^2 e^x}{\partial t^2} - D[\text{Sqrt}[x], \{t, 2\}]$

Out[7]= $d^2 \sqrt[3]{x} (-1/dt^2)$

In[10]:=  $\{d^2 x/dt^2\} + \{d^2 e^x/dt^2\} - \{d^2 x^{1/3}/dt^2\} - \{d^2 \sqrt{x}/dt^2\}$

Out[10]=

Input interpretation:

$$x''(t) + \frac{\partial^2 e^x}{\partial t^2} - d^2 \times \frac{\sqrt[3]{x}}{dt^6 \text{ (metric deciton squared)}} - \frac{\partial^2 \sqrt{x}}{\partial t^2}$$

Result:

$$d^2 \sqrt[3]{x} - 1/dt^6 \text{ (per metric deciton squared)} + x''(t)$$

WolframAlpha 

In[8]:= $\partial_U \left(d \ x / \text{Quantity}\left[-1, \frac{1}{\text{"MetricDecitons"}}\right] \right)$

$$\text{Out}[8]= \frac{d^2 \left(-\frac{1}{3} / dt^2\right)}{x^{2/3}}$$

In[9]:= $\text{Numerator}\left[\frac{d \ \text{Quantity}\left[--, \frac{1}{0BQOF@ B@FQLKP}\right]}{x /}\right]$

$$\text{Out}[9]= d^2 \left(-\frac{1}{3} / dt^2\right)$$

In[11]:= $\partial_A \left(d \ \text{Quantity}\left[-\frac{1}{3}, \frac{1}{\text{"MetricDecitons"}^2}\right] \right)$

Out[11]=

$$d \left(-\frac{2}{3} / dt^2\right)$$

In[12]:= $\text{Solve}\left[d \ \text{Quantity}\left[-\frac{2}{3}, \frac{1}{\text{"MetricDecitons"}^2}\right] == 0, d\right]$

Out[12]=

$$\{(d \rightarrow 0 \text{ kg})\}$$

In[13]:= $\{\{d \rightarrow \text{Quantity}[0, \text{"Kilograms"]}\}\} /. \text{Rule} \rightarrow \text{Equal}$

Out[13]=

$$(d = 0 \text{ kg})$$

In[14]:= $\text{Flatten}[\{\{d == \text{Quantity}[0, \text{"Kilograms"]}\}\}]$

Out[14]=

$$\{d = 0 \text{ kg}\}$$

$$\boxed{\{d^2x/dt^2\} + \{d^2e^x/dt^2\} - \{d^2x^{1/3}/dt^2\} - \{d^2\sqrt{x}/dt^2\}}$$

Eq 10

In[1]:= $d^2x/dt^2 = t e^x + t x - t \sqrt{x} - t \sqrt[3]{x}$

Out[1]= $t e^x + t x - t \sqrt{x} - t \sqrt[3]{x}$

Sum: $\{d^2x/dt^2\} + \{d^2e^x/dt^2\} - \{d^2x^{1/3}/dt^2\} - \{d^2\sqrt{x}/dt^2\}$

Input:

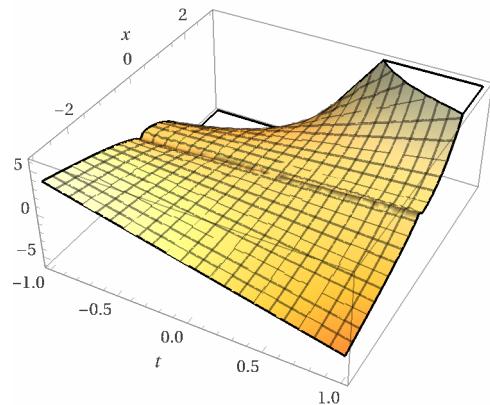
$$d^2 \times \frac{x}{d^2} t + d^2 \times \frac{e^x}{d^2} t - d^2 \times \frac{\sqrt[3]{x}}{d^2} t - d^2 \times \frac{\sqrt{x}}{d^2} t$$

Result:

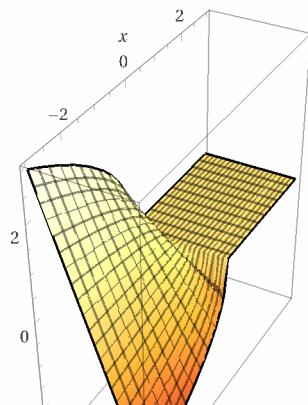
$$t e^x + t x - t \sqrt{x} - t \sqrt[3]{x}$$

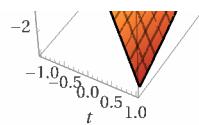
3D plots:

Real part:



Imaginary part:

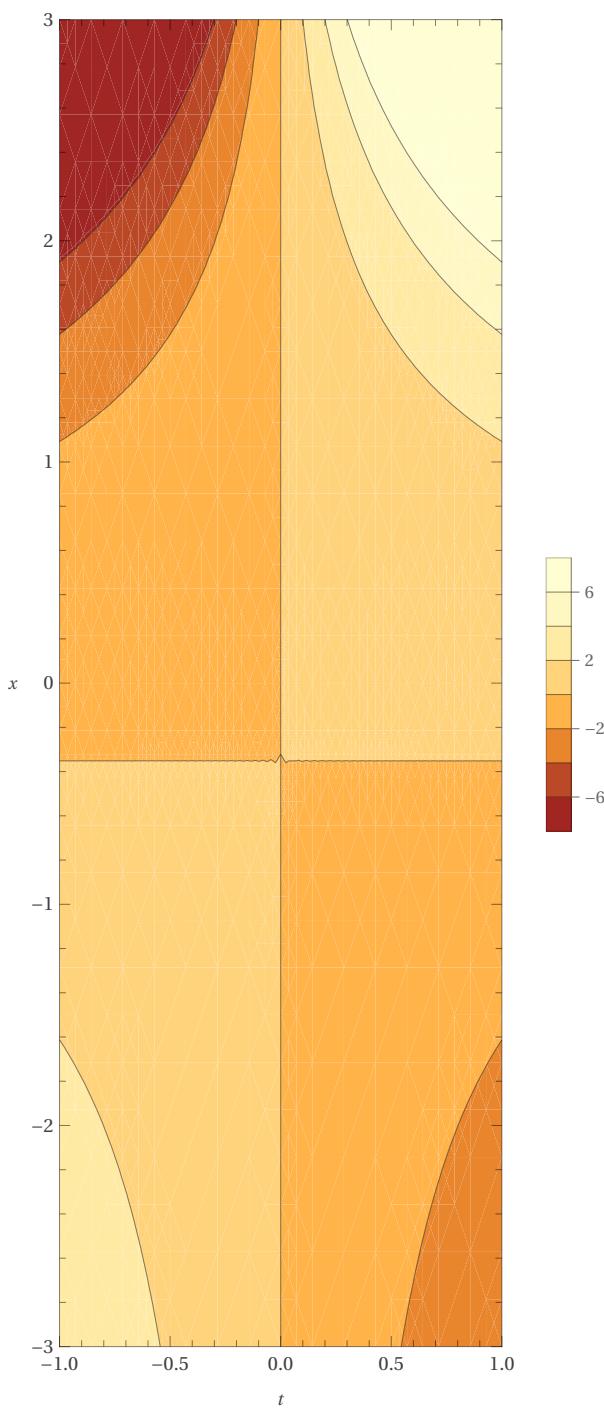




Contour plots:

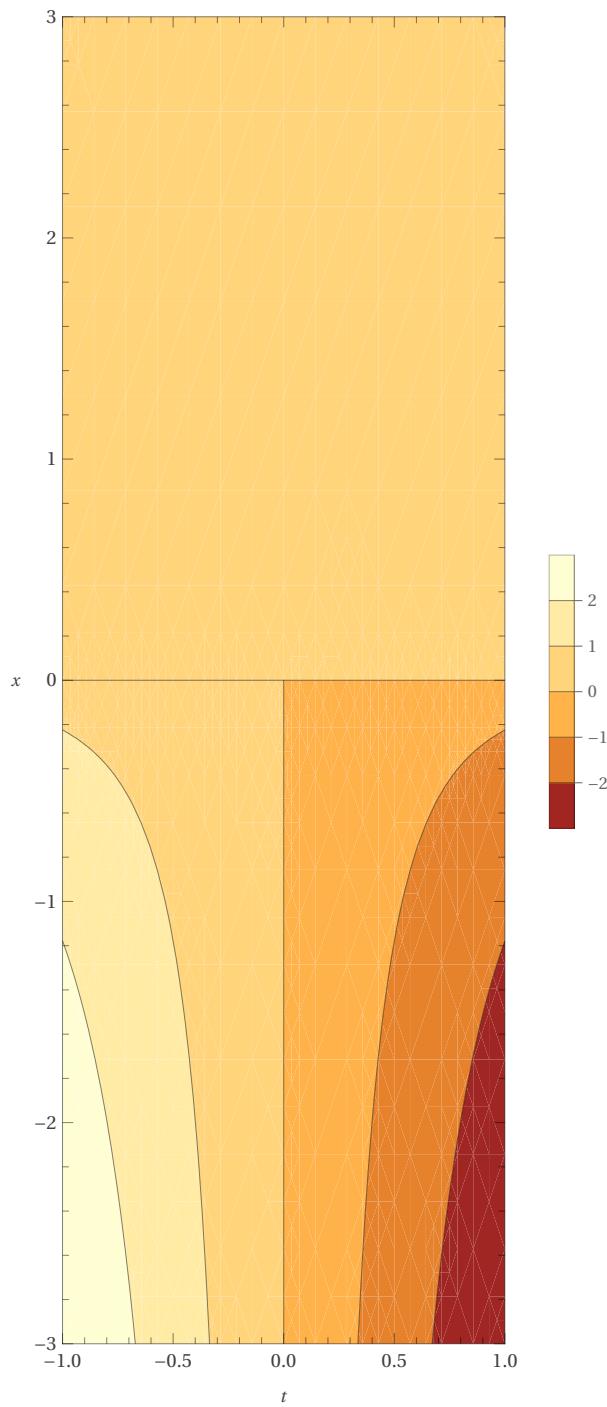


Real part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Alternate forms:

$$t(x - \sqrt{x} - \sqrt[3]{x} + e^x)$$

$$t(x^{2/3} - \sqrt[6]{x} - 1) \sqrt[3]{x} + t e^x$$



Real root:

$$t = 0, \quad x \geq 0$$



Series expansion at $x = 0$:

$$t - t \sqrt[3]{x} - t \sqrt{x} + 2 t x + \frac{t x^2}{2} + \frac{t x^3}{6} + \frac{t x^4}{24} + O(x^5)$$

(Puiseux series)



[Big-O notation »](#)

Derivative:

[Step-by-step solution](#)



$$\frac{\partial}{\partial x} \left(\frac{d^2 x t}{d^2} + \frac{d^2 e^x t}{d^2} - \frac{d^2 \sqrt[3]{x} t}{d^2} - \frac{d^2 \sqrt{x} t}{d^2} \right) = \frac{1}{6} t \left(-\frac{2}{x^{2/3}} + 6 e^x - \frac{3}{\sqrt{x}} + 6 \right)$$

Indefinite integral:

[Step-by-step solution](#)



$$\int (e^x t - t \sqrt[3]{x} - t \sqrt{x} + t x) dx = t \left(\frac{1}{12} (-9 x^{4/3} - 8 x^{3/2} + 6 x^2) + e^x \right) + \text{gs r u e r x}$$

[WolframAlpha](#)



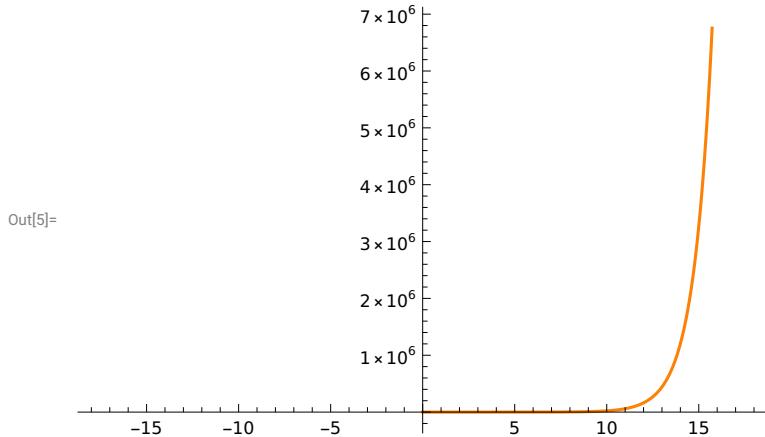
In[2]:= **Simplify**[$e^x t - t x^{1/3} - t \sqrt{x} + t x$]

Out[2]:= $t(x - \sqrt{x} - \sqrt[3]{x} + e^x)$

In[4]:= $\partial_t(t(e^x - x^{1/3} - \sqrt{x} + x))$

Out[4]:= $x - \sqrt{x} - \sqrt[3]{x} + e^x$

In[5]:= Plot[e^x - x^(1/3) - Sqrt[x] + x, {x, -18., 18.}]



$\boxed{\{d^2 x/d^2 t\} + \{d^2 \pi^x/d^2 t\} - \{d^2 x^{1/3}/d^2 t\} - \{d^2 \sqrt{x}/d^2 t\}}$

Eq 11

In[6]:= $d^2 x/(d^2 t) + d^2 \pi^x/(d^2 t) - d^2 x^{1/3}/(d^2 t) - d^2 \sqrt{x}/(d^2 t)$

Out[6]= $t \pi^x + t x - t \sqrt{x} - t \sqrt[3]{x}$

$\star \{d^2 x/d^2 t\} + \{d^2 \pi^x/d^2 t\} - \{d^2 x^{1/3}/d^2 t\} - \{d^2 \sqrt{x}/d^2 t\}$

Input:

$$d^2 \times \frac{x}{d^2} t + d^2 \times \frac{\pi^x}{d^2} t - d^2 \times \frac{\sqrt[3]{x}}{d^2} t - d^2 \times \frac{\sqrt{x}}{d^2} t$$



Result:

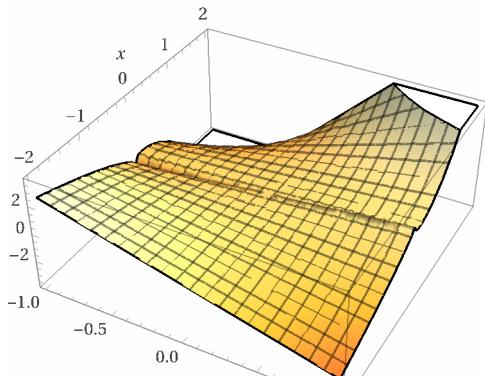
$$t \pi^x + t x - t \sqrt{x} - t \sqrt[3]{x}$$

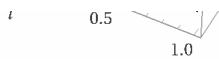


3D plots:

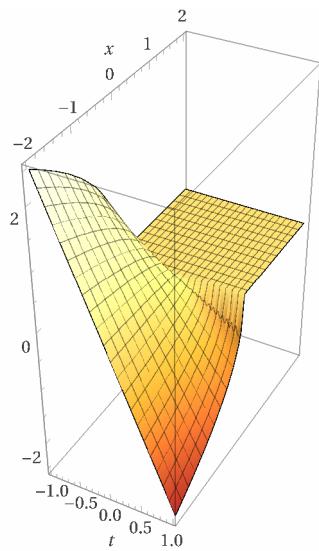


Real part:





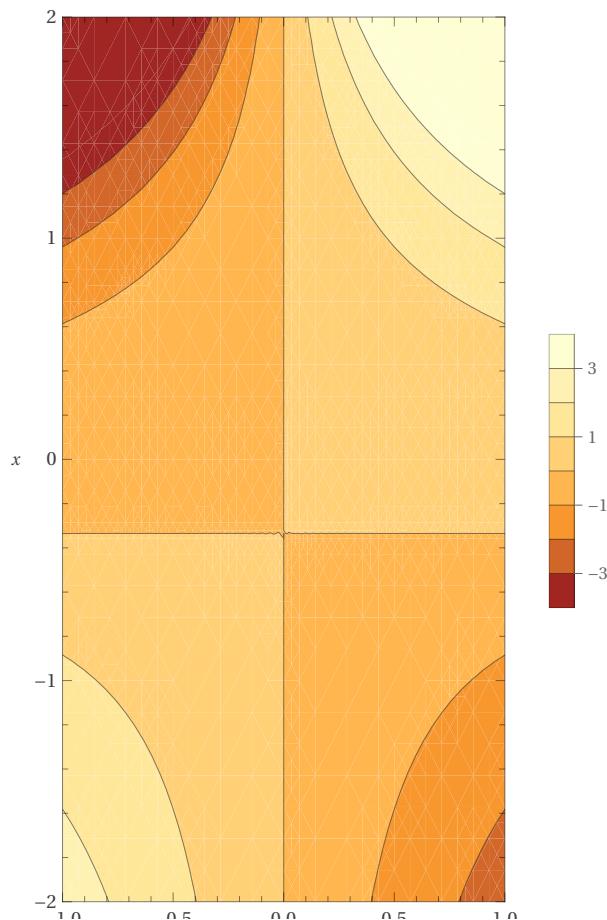
Imaginary part:

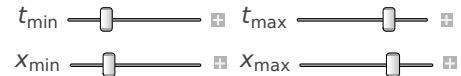
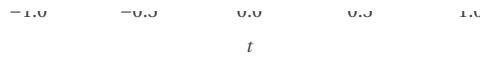


Contour plots:

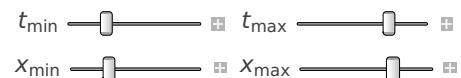
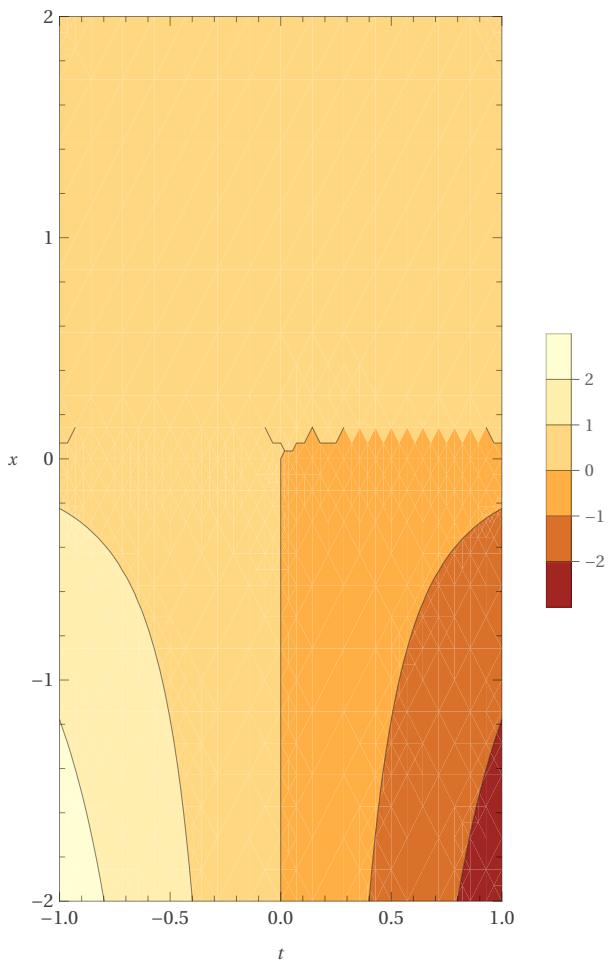


Real part:





Imaginary part:



Alternate form:

$$t(x - \sqrt{x} - \sqrt[3]{x} + \pi^x)$$



Real root:

$$t = 0, \quad x \geq 0$$



Series expansion at $x = 0$:



$$t - t \sqrt[3]{x} - t \sqrt{x} + t x (1 + \log(\pi)) + \frac{1}{2} t x^2 \log^2(\pi) + \frac{1}{6} t x^3 \log^3(\pi) + \frac{1}{24} t x^4 \log^4(\pi) + \frac{1}{120} t x^5 \log^5(\pi) + O(x^{16/3})$$

(Puiseux series)

[log\(x\) is the natural logarithm »](#)[Big-O notation »](#)

Derivative:

[Approximate form](#)[Step-by-step solution](#) +

$$\frac{\partial}{\partial x} \left(\frac{d^2 x t}{d^2} + \frac{d^2 \pi^x t}{d^2} - \frac{d^2 \sqrt[3]{x} t}{d^2} - \frac{d^2 \sqrt{x} t}{d^2} \right) = \frac{1}{6} t \left(-\frac{2}{x^{2/3}} - \frac{3}{\sqrt{x}} + 6 \pi^x \log(\pi) + 6 \right)$$

Indefinite integral:

[Approximate form](#)[Step-by-step solution](#) +

$$\int (\pi^x t - t \sqrt[3]{x} - t \sqrt{x} + t x) dx = t \left(-\frac{3 x^{4/3}}{4} - \frac{2 x^{3/2}}{3} + \frac{x^2}{2} + \frac{\pi^x}{\log(\pi)} \right) + \text{constant}$$

[WolframAlpha](#) +
✖ **simplify{d^2x/d^2t}+{d^2π^x/d^2t}-{d^2x^1/3/d^2t}-{d^2√x/d^2t}**

In[8]:= Simplify[d^2*(x/d^2)*t + d^2*(Pi^x/d^2)*t - d^2*(x^(1/3)/d^2)*t - d^2*(Sqrt[x]/d^2)*t]

Out[8]= $t (x - \sqrt{x} - \sqrt[3]{x} + \pi^x)$
✖ **simplify{d^2x/d^2t}+{d^2π^x/d^2t}-{d^2x^1/3/d^2t}-{d^2√x/d^2t}**

Out[11]=

Input interpretation:

simplify	$d^2 \times \frac{x}{d^2} t + d^2 \times \frac{\pi^x}{d^2} t - d^2 \times \frac{\sqrt[3]{x}}{d^2} t - d^2 \times \frac{\sqrt{x}}{d^2} t$
----------	--

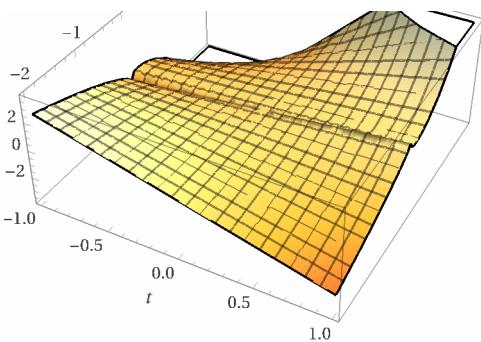
Result:

$$t (x - \sqrt{x} - \sqrt[3]{x} + \pi^x)$$

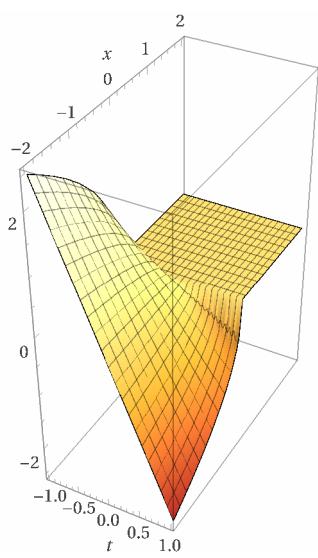
3D plots:

Real part:





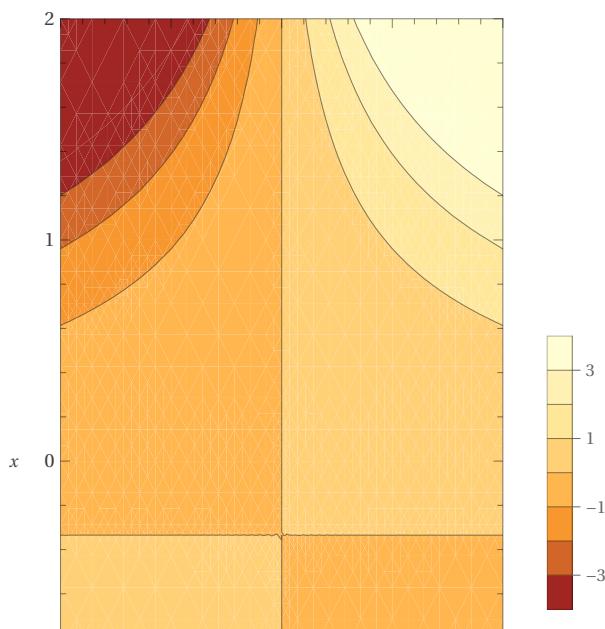
Imaginary part:

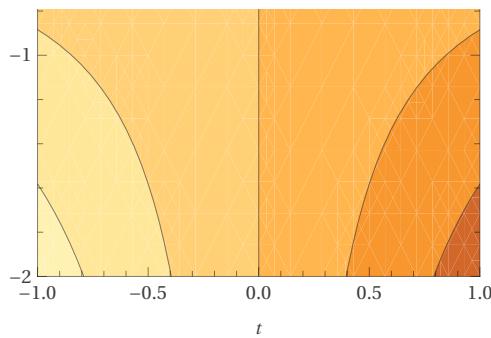


Contour plots:



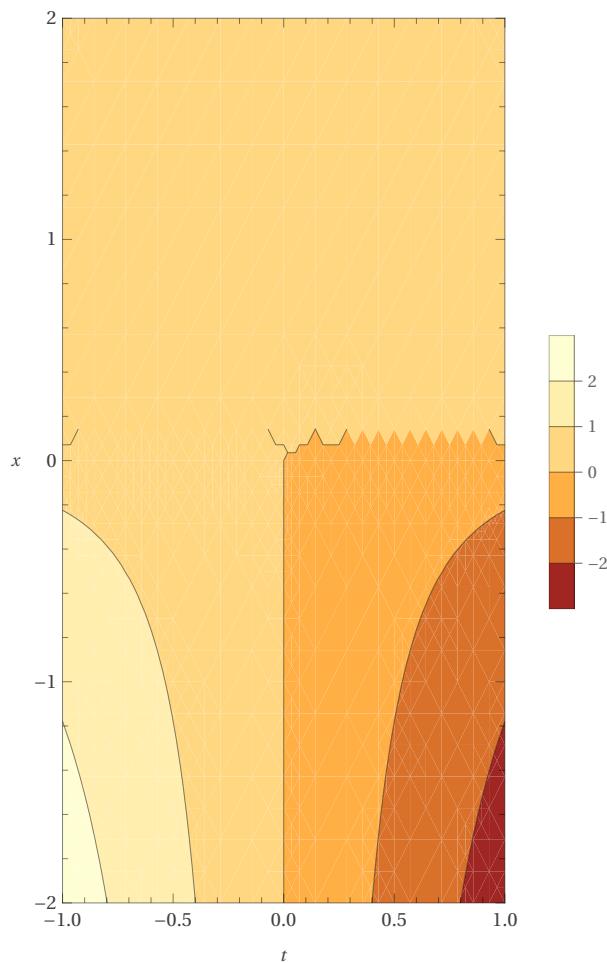
Real part:





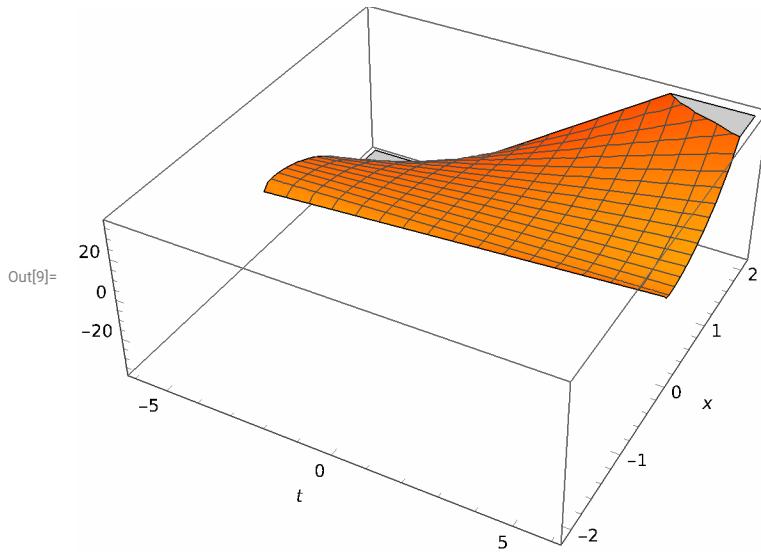
t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

In[9]:= Plot3D[t (π^x - x^{1/3} - √x + x), {t, -6., 6.}, {x, -2.10603, 2.10603}]



■ simplify{d²x/d²t}+{d²e^x/d²t}-{d²x^{1/3}/d²t}-{d²√x/d²t}

Eq 10

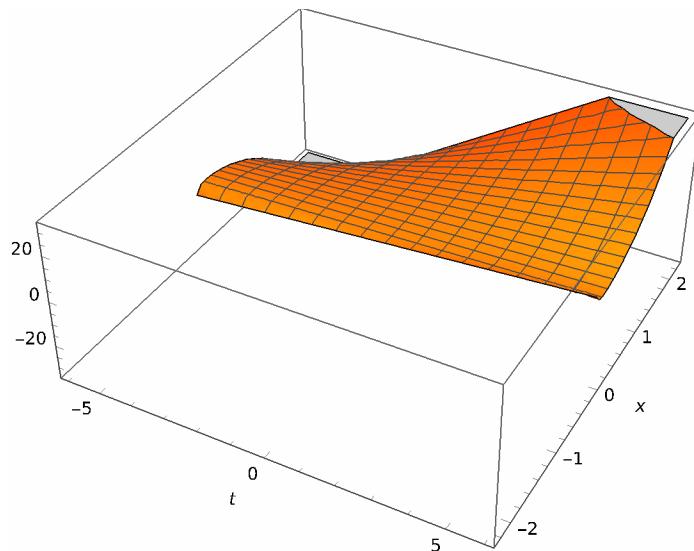
In[10]:= Simplify[d^2*(x/d^2)*t + d^2*(E^x/d^2)*t - d^2*(x^(1/3)/d^2)*t - d^2*(Sqrt[x]/d^2)*t]

Out[10]=

$$t \left(x - \sqrt{x} - \sqrt[3]{x} + e^x \right)$$

In[12]:= Plot3D[t (e^x - x^{1/3} - √x + x), {t, -6., 6.}, {x, -2.24762, 2.24762}]

Out[12]=



$$\blacksquare [\{d^2x/d^2t + \{d^2e^x/d^2t\}]/[\{d^2x^{1/3}/d^2t\} + \{d^2\sqrt{x}/d^2t\}]$$

Eq 12

In[1]:= $d^2x/d^2t + \{d^2e^x/d^2t\}/[\{d^2x^{1/3}/d^2t\} + \{d^2\sqrt{x}/d^2t\}]$

Out[1]:= $t x + \frac{t e^x}{t \sqrt{x} + t \sqrt[3]{x}}$

✗ $\blacksquare [\{d^2x/d^2t + \{d^2e^x/d^2t\}]/[\{d^2x^{1/3}/d^2t\} + \{d^2\sqrt{x}/d^2t\}]$

An attempt was made to fix mismatched parentheses, brackets, or braces.

Input:

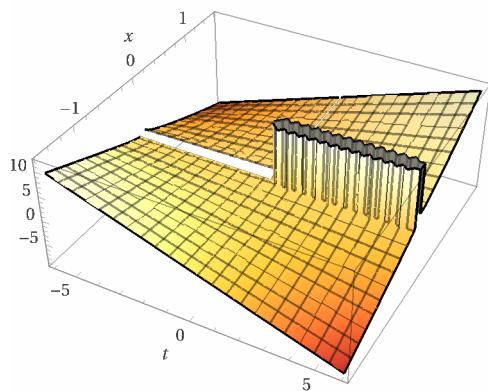
$$d^2 \times \frac{x}{d^2} t + \frac{d^2 \times \frac{e^x}{d^2} t}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + d^2 \times \frac{\sqrt{x}}{d^2} t}$$

Result:

$$t x + \frac{t e^x}{t \sqrt{x} + t \sqrt[3]{x}}$$

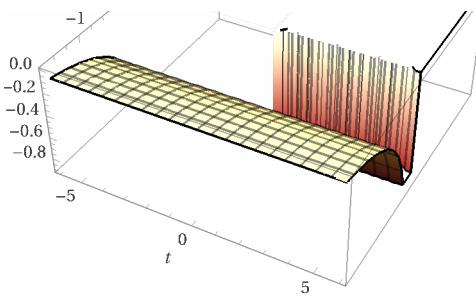
3D plots:

Real part:



Imaginary part:

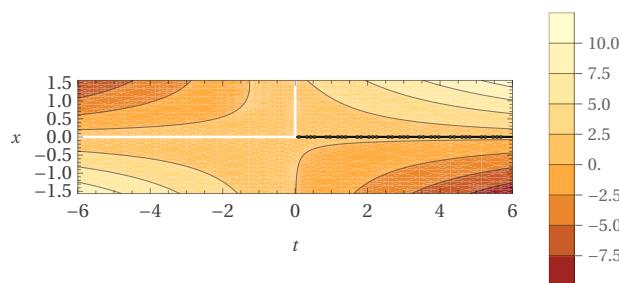




Contour plots:



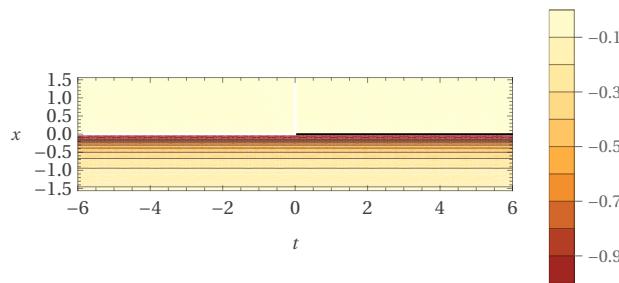
Real part:



Out[4]=

t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Alternate forms:

More

$$tx + \frac{e^x}{\sqrt{x} + \sqrt[3]{x}}$$

$$t x + \frac{e^x}{(\sqrt[6]{x} + 1) \sqrt[3]{x}}$$

$$t \left(\frac{e^x}{\sqrt[3]{x} (t \sqrt[6]{x} + t)} + x \right)$$

Series expansion at $x = 0$:

$$O\left(\frac{1}{x^7}\right)$$

(Taylor series)

[Big-O notation »](#)Series expansion at $x = \infty$:

$$\left(t x + O\left(\left(\frac{1}{x}\right)^6\right) \right) +$$

$$e^x \left(\sqrt{\frac{1}{x}} - \left(\frac{1}{x}\right)^{2/3} + \left(\frac{1}{x}\right)^{5/6} - \frac{1}{x} + \left(\frac{1}{x}\right)^{7/6} - \left(\frac{1}{x}\right)^{4/3} + \left(\frac{1}{x}\right)^{3/2} - \left(\frac{1}{x}\right)^{5/3} + \left(\frac{1}{x}\right)^{11/6} - \left(\frac{1}{x}\right)^2 + \right.$$

$$\left(\frac{1}{x} \right)^{13/6} - \left(\frac{1}{x}\right)^{7/3} + \left(\frac{1}{x}\right)^{5/2} - \left(\frac{1}{x}\right)^{8/3} + \left(\frac{1}{x}\right)^{17/6} - \left(\frac{1}{x}\right)^3 + \left(\frac{1}{x}\right)^{19/6} -$$

$$\left(\frac{1}{x} \right)^{10/3} + \left(\frac{1}{x}\right)^{7/2} - \left(\frac{1}{x}\right)^{11/3} + \left(\frac{1}{x}\right)^{23/6} - \left(\frac{1}{x}\right)^4 + \left(\frac{1}{x}\right)^{25/6} - \left(\frac{1}{x}\right)^{13/3} +$$

$$\left. \left(\frac{1}{x} \right)^{9/2} - \left(\frac{1}{x}\right)^{14/3} + \left(\frac{1}{x}\right)^{29/6} - \left(\frac{1}{x}\right)^5 + \left(\frac{1}{x}\right)^{31/6} - \left(\frac{1}{x}\right)^{16/3} + O\left(\left(\frac{1}{x}\right)^{11/2}\right) \right)$$

[Big-O notation »](#)

Derivative:

[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{d^2 x t}{d^2} + \frac{d^2 e^x t}{d^2 \left(\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{d^2 \sqrt{x} t}{d^2} \right)} \right) = t + \frac{e^x (6 x^{7/6} + 6 x - 3 \sqrt[6]{x} - 2)}{6 (\sqrt[6]{x} + 1)^2 x^{4/3}}$$

WolframAlpha

In[2]:= Simplify[$\frac{e^x t}{t x^{1/3} + t \sqrt{x}} + t x]$ Out[2]:= $t \left(\frac{e^x}{\sqrt[3]{x} (t \sqrt[6]{x} + t)} + x \right)$

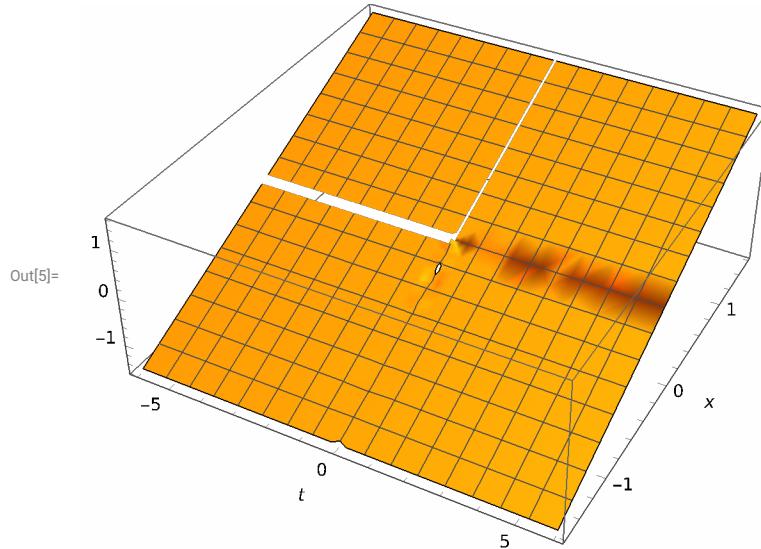
```
In[3]:= Dt t 

```
Out[3]= -\frac{t e^t (\sqrt[6]{x} + 1)}{\sqrt[3]{x} (t \sqrt[6]{x} + t)^2} + \frac{e^t}{\sqrt[3]{x} (t \sqrt[6]{x} + t)} + x
```



```
In[5]:= Plot3D[-\frac{e^t t (1 + x^t)}{(t + t x^t) x^t} + x, {t, -6., 6.}, {x, -1.56716, 1.56716}]
```


```



$$\boxed{\text{Eq 12} \quad \text{In[6]:= } \frac{d^2(x/d^2)*t + d^2*(E^x/d^2)*t}{(d^2*(x^(1/3)/d^2)*t + d^2*(Sqrt[x]/d^2)*t)}}$$

```
Out[6]= \frac{t e^x + t x}{t \sqrt{x} + t \sqrt[3]{x}}
```

=

Input:

$$\frac{d^2 \times \frac{x}{d^2} t + d^2 \times \frac{e^x}{d^2} t}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + d^2 \times \frac{\sqrt{x}}{d^2} t}$$

+

Result:

$$\frac{t e^x + t x}{t \sqrt{x} + t \sqrt[3]{x}}$$

+

Alternate forms:

$$\frac{x + e^x}{\sqrt{x} + \sqrt[3]{x}}$$

$$\frac{x + e^x}{(\sqrt[3]{x} + 1) \sqrt[3]{x}}$$

$$\frac{x^{2/3}}{\sqrt[6]{x} + 1} + \frac{e^x}{(\sqrt[6]{x} + 1) \sqrt[3]{x}}$$



Expanded form:

[Step-by-step solution](#)



$$\frac{t x}{t \sqrt{x} + t \sqrt[3]{x}} + \frac{t e^x}{t \sqrt{x} + t \sqrt[3]{x}}$$

Series expansion at $x = 0$:

$$O\left(\frac{1}{x^7}\right)$$

(Taylor series)

[Big-O notation »](#)



Series expansion at $x = \infty$:

$$\text{Out}[7]= e^x \left(\sqrt{\frac{1}{x}} - \left(\frac{1}{x}\right)^{2/3} + \left(\frac{1}{x}\right)^{5/6} - \frac{1}{x} + \left(\frac{1}{x}\right)^{7/6} - \left(\frac{1}{x}\right)^{4/3} + \left(\frac{1}{x}\right)^{3/2} - \left(\frac{1}{x}\right)^{5/3} + \left(\frac{1}{x}\right)^{11/6} - \left(\frac{1}{x}\right)^2 + \left(\frac{1}{x}\right)^{13/6} - \left(\frac{1}{x}\right)^{7/3} + \left(\frac{1}{x}\right)^{5/2} - \left(\frac{1}{x}\right)^{8/3} + \left(\frac{1}{x}\right)^{17/6} - \left(\frac{1}{x}\right)^3 + \left(\frac{1}{x}\right)^{19/6} - \left(\frac{1}{x}\right)^{10/3} + \left(\frac{1}{x}\right)^{7/2} - \left(\frac{1}{x}\right)^{11/3} + \left(\frac{1}{x}\right)^{23/6} - \left(\frac{1}{x}\right)^4 + \left(\frac{1}{x}\right)^{25/6} - \left(\frac{1}{x}\right)^{13/3} + \left(\frac{1}{x}\right)^{9/2} - \left(\frac{1}{x}\right)^{14/3} + \left(\frac{1}{x}\right)^{29/6} - \left(\frac{1}{x}\right)^5 + O\left(\left(\frac{1}{x}\right)^{31/6}\right) \right) + \left(\sqrt{x} - \sqrt[3]{x} + \sqrt[6]{x} - 1 + \sqrt[6]{\frac{1}{x}} - \sqrt[3]{\frac{1}{x}} + \sqrt{\frac{1}{x}} - \left(\frac{1}{x}\right)^{2/3} + \left(\frac{1}{x}\right)^{5/6} - \frac{1}{x} + \left(\frac{1}{x}\right)^{7/6} - \left(\frac{1}{x}\right)^{4/3} + \left(\frac{1}{x}\right)^{3/2} - \left(\frac{1}{x}\right)^{5/3} + \left(\frac{1}{x}\right)^{11/6} - \left(\frac{1}{x}\right)^2 + \left(\frac{1}{x}\right)^{13/6} - \left(\frac{1}{x}\right)^{7/3} + \left(\frac{1}{x}\right)^{5/2} - \left(\frac{1}{x}\right)^{8/3} + \left(\frac{1}{x}\right)^{17/6} - \left(\frac{1}{x}\right)^3 + \left(\frac{1}{x}\right)^{19/6} - \left(\frac{1}{x}\right)^{10/3} + \left(\frac{1}{x}\right)^{7/2} - \left(\frac{1}{x}\right)^{11/3} + \left(\frac{1}{x}\right)^{23/6} - \left(\frac{1}{x}\right)^4 + \left(\frac{1}{x}\right)^{25/6} - \left(\frac{1}{x}\right)^{13/3} + \left(\frac{1}{x}\right)^{9/2} - \left(\frac{1}{x}\right)^{14/3} + \left(\frac{1}{x}\right)^{29/6} - \left(\frac{1}{x}\right)^5 + O\left(\left(\frac{1}{x}\right)^{31/6}\right) \right)$$

[Big-O notation »](#)



Derivative:

[Step-by-step solution](#)



$$\frac{\partial}{\partial x} \left(\frac{\frac{d^2 x t}{d^2} + \frac{d^2 e^x t}{d^2}}{\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{d^2 \sqrt{x} t}{d^2}} \right) = \frac{e^x (6 x^{7/6} + 6 x - 3 \sqrt[6]{x} - 2) + (3 \sqrt[6]{x} + 4) x}{6 (\sqrt[6]{x} + 1)^2 x^{4/3}}$$

Limit:

$$\lim_{t \rightarrow -\infty} \frac{e^x t + t x}{t \sqrt[3]{x} + t \sqrt{x}} = \frac{-x - e^x}{-\sqrt{x} - \sqrt[3]{x}} \approx \frac{-x - 2.71828^x}{-\sqrt{x} - \sqrt[3]{x}}$$

$$\lim_{t \rightarrow \infty} \frac{e^x t + t x}{t \sqrt[3]{x} + t \sqrt{x}} = \frac{x + e^x}{\sqrt{x} + \sqrt[3]{x}} \approx \frac{x + 2.71828^x}{\sqrt{x} + \sqrt[3]{x}}$$

WolframAlpha 

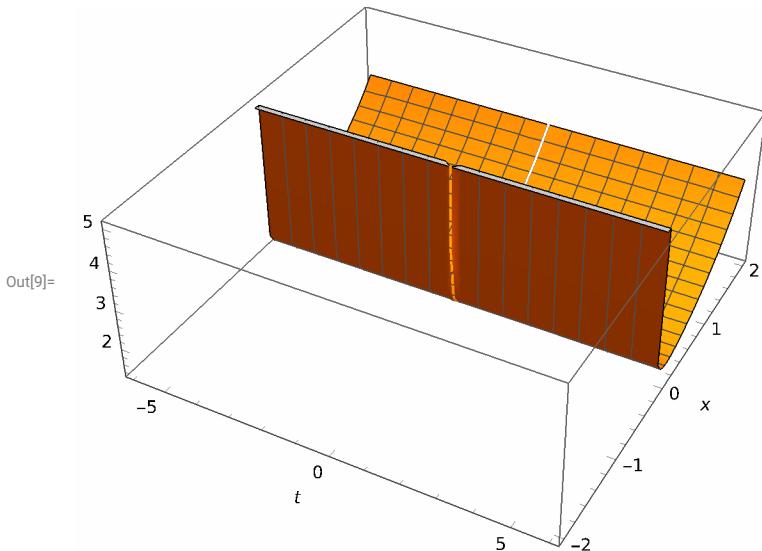
 $\text{In}[8]:= \frac{d^2 x/d^2 t + d^2 e^x/d^2 t}{[d^2 x^{1/3}/d^2 t + d^2 \sqrt{x}/d^2 t]}$

Eq 12

$\text{Out}[8]= \frac{t e^x + t x}{t \sqrt{x} + t \sqrt[3]{x}}$

$\text{Out}[8]= \frac{t e^x + t x}{t \sqrt{x} + t \sqrt[3]{x}}$

$\text{In}[9]:= \text{Plot3D}\left[\frac{e^U t + t x}{t x / + t \sqrt{x}}, \{t, -6., 6.\}, \{x, -2.00691, 2.00691\}\right]$



$$\text{In}[10]:= \frac{\{d^2 x/d^2 t\} \sin(x) + \{d^2 e^x/d^2 t\} \tan(x)}{\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin(x)}$$

$$\text{Out}[10]= \frac{\left(d^2 \times (x/d^2) \times t\right) \sin(x) + \left(d^2 \times (e^x/d^2) \times t\right) \tan(x)}{\left(d^2 \times (x^{1/3}/d^2) \times t\right) + \left(d^2 \times (\sqrt{x}/d^2) \times t\right) \sin(x)}$$

$$\text{Out}[10]= \frac{t x \sin(x) + t e^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

$$\text{In}[12]:= \frac{\{d^2 x/d^2 t\} \sin(x) + \{d^2 e^x/d^2 t\} \tan(x)}{\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin(x)}$$

Out[12]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{e^x}{d^2} t\right) \tan(x)}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$

Result:

$$\frac{t x \sin(x) + t e^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Alternate forms:

$$\begin{aligned} & \frac{(e^x + x \cos(x)) \tan(x)}{\sqrt[3]{x} + \sqrt{x} \sin(x)} \\ & \frac{(e^x + x \cos(x)) \tan(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)} \\ & \frac{x \sin(x) + e^x \tan(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)} \end{aligned}$$

More

Expanded form:

$$\frac{t x \sin(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{t e^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Series expansion at $x = 0$:

$$\begin{aligned} & x^{2/3} + 2 x^{5/3} - x^{11/6} + \frac{5 x^{8/3}}{6} - 2 x^{17/6} + x^3 + \frac{x^{11/3}}{3} - \\ & \frac{2 x^{23/6}}{3} + 2 x^4 - x^{25/6} + \frac{41 x^{14/3}}{120} + \frac{x^5}{2} - 2 x^{31/6} + x^{16/3} + O(x^{17/3}) \end{aligned}$$

(Puiseux series)

[Big-O notation »](#)

Derivative:

[Step-by-step solution](#) +

$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 e^x t) \tan(x)}{d^2}}{\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2}} \right) = \frac{1}{6 x^{4/3} (\sqrt[6]{x} \sin(x) + 1)^2}$$

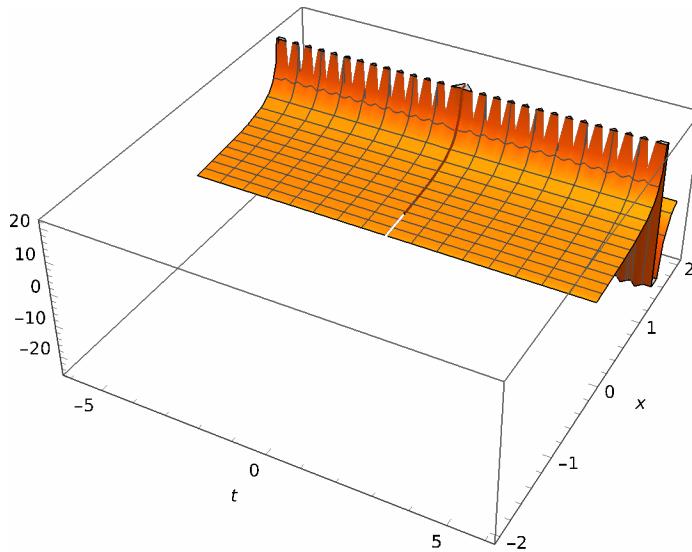
$$(6 x (\sqrt[6]{x} \sin(x) + 1) (\sin(x) + x \cos(x) + e^x \tan(x) + e^x \sec^2(x)) - (x \sin(x) + e^x \tan(x)) (6 x^{7/6} \cos(x) + 3 \sqrt[6]{x} \sin(x) + 2))$$

sec(x) is the secant function »

[WolframAlpha](#) +

```
In[11]:= Plot3D[(t x Sin[x] + e^t t Tan[x]) / (t x^1/3 + t sqrt[x] Sin[x]), {t, -6., 6.}, {x, -2.00691, 2.00691}]
```

Out[11]=



✖ $\frac{\{d^2 x/d^2 t\} \sin x + \{d^2 e^x/d^2 t\} \tan x}{[\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]}$ Eq 13

```
In[13]:= ((d^2*(x/d^2)*t)*Sin[x] + (d^2*(E^x/d^2)*t)*Tan[x])/((d^2*(x^(1/3)/d^2)*t)*(d^2*(Sqrt[x]/d^2)*t)*Sin[x])
```

Out[13]=

$$\frac{\csc(x) (t x \sin(x) + t e^x \tan(x))}{t^2 x^{5/6}}$$

✖ $\frac{\{d^2 x/d^2 t\} \sin x + \{d^2 e^x/d^2 t\} \tan x}{[\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]}$

Out[15]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{e^x}{d^2} t\right) \tan(x)}{\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$



Result:

$$\frac{\csc(x) (t x \sin(x) + t e^x \tan(x))}{t^2 x^{5/6}}$$

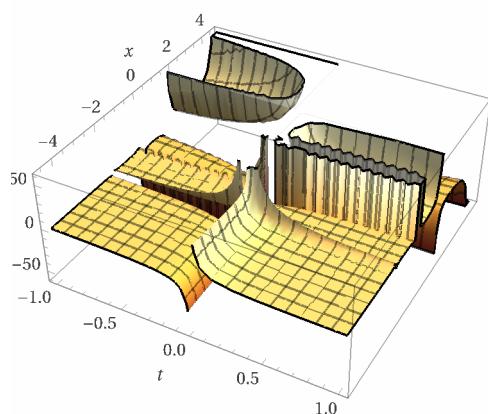


[csc\(x\) is the cosecant function >](#)

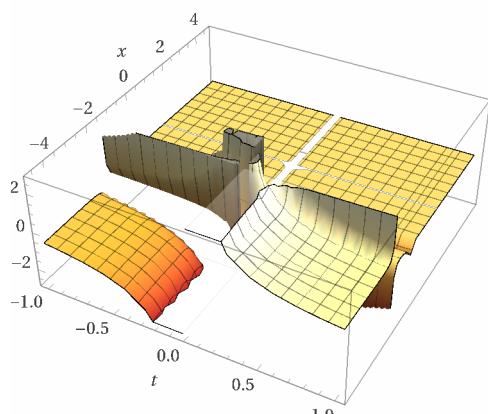
3D plots:



Real part:



Imaginary part:

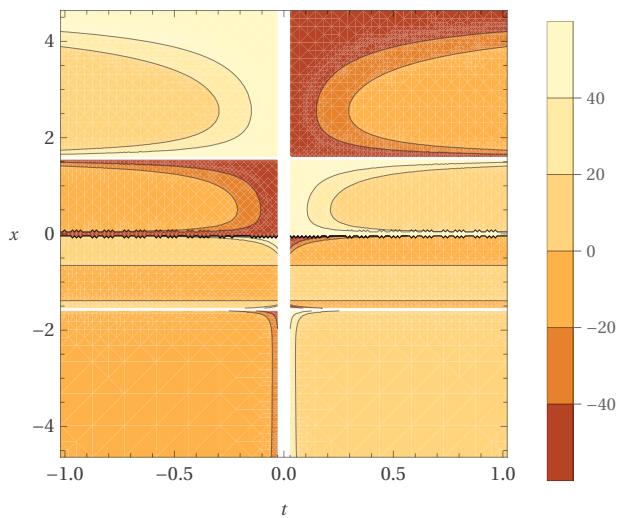


Contour plots:



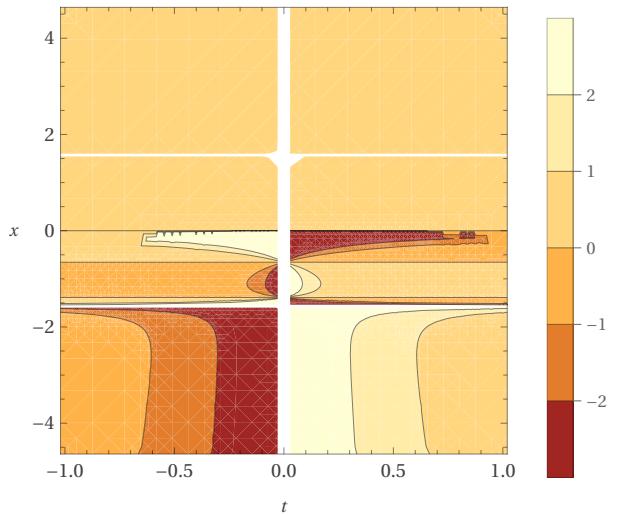
Real part:





t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Alternate forms:

$$\frac{x + e^x \sec(x)}{t x^{5/6}}$$

$$\frac{(e^x + x \cos(x)) \sec(x)}{t x^{5/6}}$$

More

$$\frac{\frac{e^x \sec(x)}{x^{5/6}} + \sqrt[6]{x}}{t}$$

[sec\(x\) is the secant function »](#)

Expanded form:

$$\frac{e^x \sec(x)}{t x^{5/6}} + \frac{\sqrt[6]{x}}{t}$$

Series expansion at $x = 0$:

$$O\left(\frac{1}{x^{25}}\right)$$

(Taylor series)

[Big-O notation »](#)

Derivative:

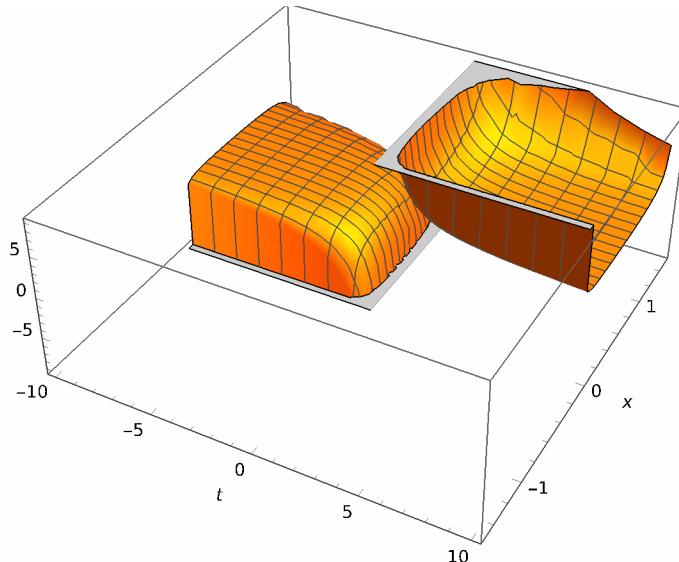
[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 e^x t) \tan(x)}{d^2}}{\frac{(d^2 \sqrt[3]{x} t)(d^2 \sqrt{x} t) \sin(x)}{d^2 d^2}} \right) = \frac{x + e^x (6 x - 5) \sec(x) + 6 e^x x \csc(x) (\sec^2(x) - 1)}{6 t x^{11/6}}$$

[WolframAlpha](#)

In[14]:= Plot3D[$\frac{\text{Csc}[x] (t x \sin[x] + e^x t \tan[x])}{t^2 x^{5/6}}$, {t, -10., 10.}, {x, -1.50958, 1.50958}]

Out[14]=



$$\blacksquare [\{d^2x/d^2t\}\sin x + \{d^2e^x/d^2t\}\tan x]^2 / [\{d^2x^{1/3}/d^2t\} * \{d^2\sqrt{x}/d^2t\}\sin x] \quad \text{Eq 13}$$

In[1]:=
$$\begin{aligned} & \left((d^2(x/d^2)*t)*\sin[x] + (d^2(e^x/d^2)*t)*\tan[x] \right)^2 \\ & ((d^2(x^{1/3}/d^2)*t)*(d^2(\sqrt{x}/d^2)*t)*\sin[x]) \end{aligned}$$

Out[1]=
$$\frac{\csc(x) (t x \sin(x) + t e^x \tan(x))^2}{t^2 x^{5/6}}$$

In[3]:=
$$\blacksquare [\{d^2x/d^2t\}\sin x + \{d^2e^x/d^2t\}\tan x]^2 / [\{d^2x^{1/3}/d^2t\} * \{d^2\sqrt{x}/d^2t\}\sin x]$$

Input:

$$\frac{\left(\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{e^x}{d^2} t\right) \tan(x)\right)^2}{\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$

Result:

$$\frac{\csc(x) (t x \sin(x) + t e^x \tan(x))^2}{t^2 x^{5/6}}$$

[csc\(x\) is the cosecant function >](#)

Alternate forms:

$$\frac{\sin(x) (x + e^x \sec(x))^2}{x^{5/6}}$$

$$\frac{(x^2 \cos^2(x) + e^{2x} + 2 e^x x \cos(x)) \tan(x) \sec(x)}{x^{5/6}}$$

$$\frac{\left(t x \sin(x) + \frac{e^x t \sin(x)}{\cos(x)}\right)^2}{t^2 x^{5/6} \sin(x)}$$

[More](#)[sec\(x\) is the secant function >](#)

Out[3]=

Expanded form:

$$x^{7/6} \sin(x) + \frac{e^{2x} \tan(x) \sec(x)}{x^{5/6}} + 2 e^x \sqrt[6]{x} \tan(x)$$

Series expansion at x = 0:

$$\sqrt[6]{x} + 4 x^{7/6} + \frac{35 x^{13/6}}{6} + O(x^{19/6})$$

(Puiseux series)

[Big-O notation >](#)

Derivative:

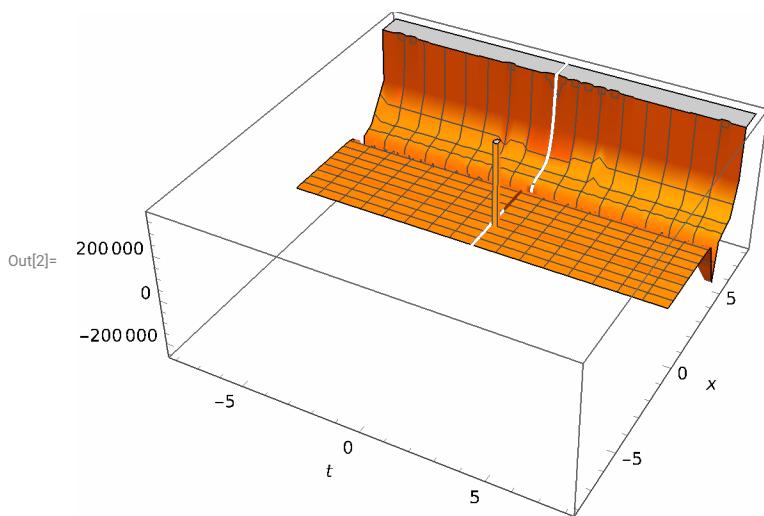
[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{\left(\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 e^x t) \tan(x)}{d^2} \right)^2}{\frac{(d^2 \sqrt[3]{x} t)(d^2 \sqrt{x} t) \sin(x)}{d^2 d^2}} \right) =$$

$$\frac{\cos(x) (x + e^x \sec(x)) (x (6 x + 7 \tan(x)) + 12 e^x x \sec^3(x) + e^x ((12 x - 5) \tan(x) - 6 x) \sec(x))}{6 x^{11/6}}$$

WolframAlpha

$$\text{In[2]:= } \text{Plot3D}\left[\frac{\csc[x] (t \sin[x] + e^x t \tan[x])^2}{t^2 x^{5/6}}, \{t, -8, 8\}, \{x, -8, 8\}\right]$$



■ $\frac{(\{d^2 x/d^2 t\} \sin x + \{d^2 e^x/d^2 t\} \tan x) / (\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x)^2}{\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x}$ Eq 14

$$\text{In[4]:= } \frac{((d^2 (x/d^2) * t) * \sin[x] + (d^2 (e^x/d^2) * t) * \tan[x]) / ((d^2 (x^{1/3}/d^2) * t) * (d^2 (\sqrt{x}/d^2) * t) * \sin[x])^2}{((d^2 (x^{1/3}/d^2) * t) * (d^2 (\sqrt{x}/d^2) * t) * \sin[x])^2}$$

$$\text{Out[4]= } \frac{\csc^2(x) (t x \sin(x) + t e^x \tan(x))}{t^4 x^{5/3}}$$

■ $\frac{(\{d^2 x/d^2 t\} \sin x + \{d^2 e^x/d^2 t\} \tan x) / (\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x)^2}{\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x}$

Input:

$$\frac{(d^2 \times \frac{x}{d^2} t) \sin(x) + (d^2 \times \frac{e^x}{d^2} t) \tan(x)}{\left((d^2 \times \frac{\sqrt[3]{x}}{d^2} t)\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)^2}$$

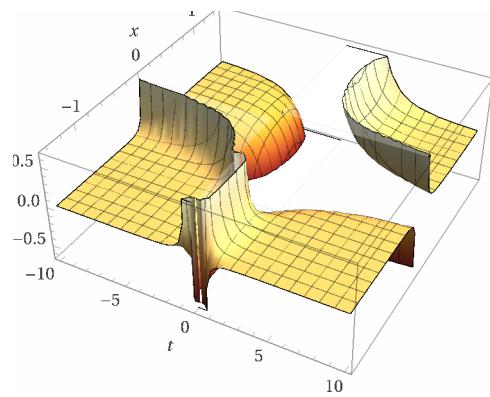
Result:

$$\frac{\csc^2(x) (t x \sin(x) + t e^x \tan(x))}{t^4 x^{5/3}}$$

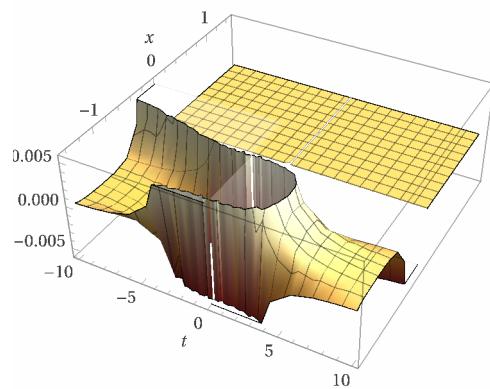
csc(x) is the cosecant function »

3D plots:

Real part:



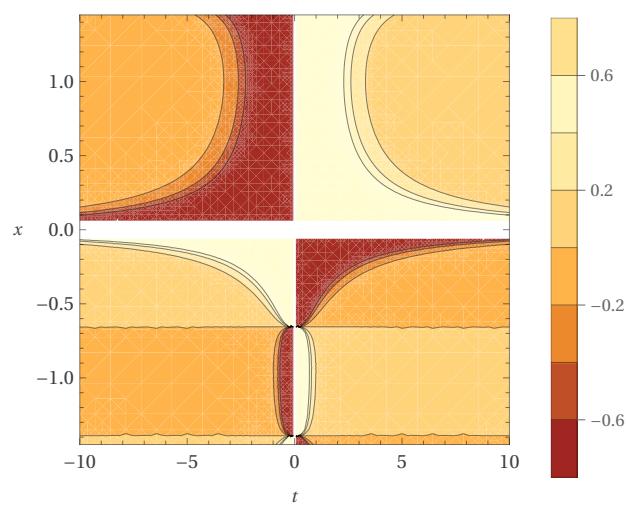
Imaginary part:



Contour plots:



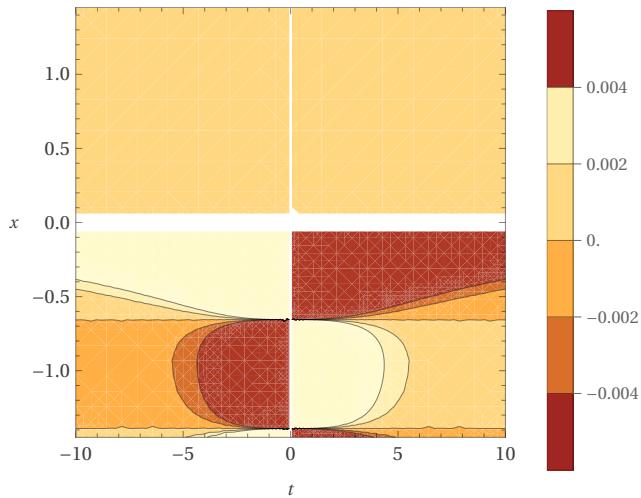
Real part:



Out[6]=



Imaginary part:



t_{\min} t_{\max}

x_{\min} x_{\max}

Alternate forms:

[More](#)

$$\frac{\csc(x)(x + e^x \sec(x))}{t^3 x^{5/3}}$$

$$\frac{(e^x + x \cos(x)) \csc(x) \sec(x)}{t^3 x^{5/3}}$$

$$\frac{\csc(x) \left(\frac{e^x \sec(x)}{x^{5/3}} + \frac{1}{x^{2/3}} \right)}{t^3}$$

[sec\(x\) is the secant function »](#)

Expanded form:

$$\frac{e^x \csc(x) \sec(x)}{t^3 x^{5/3}} + \frac{\csc(x)}{t^3 x^{2/3}}$$

Series expansion at $x = 0$:

$$O\left(\frac{1}{x^{19}}\right)$$

(Taylor series)

[Big-O notation »](#)

Derivative:

[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 e^x t) \tan(x)}{d^2}}{\left(\frac{(d^2 \sqrt[3]{x} t) (d^2 \sqrt{x} t) \sin(x)}{d^2 d^2} \right)^2} \right) = -\frac{\cot(x) (\sec(x) (2 x - e^x (3 x - 5) \sec(x)) + 3 x \csc(x) (x - e^x \sec^3(x) + 2 e^x \sec(x)))}{3 t^3 x^{8/3}}$$

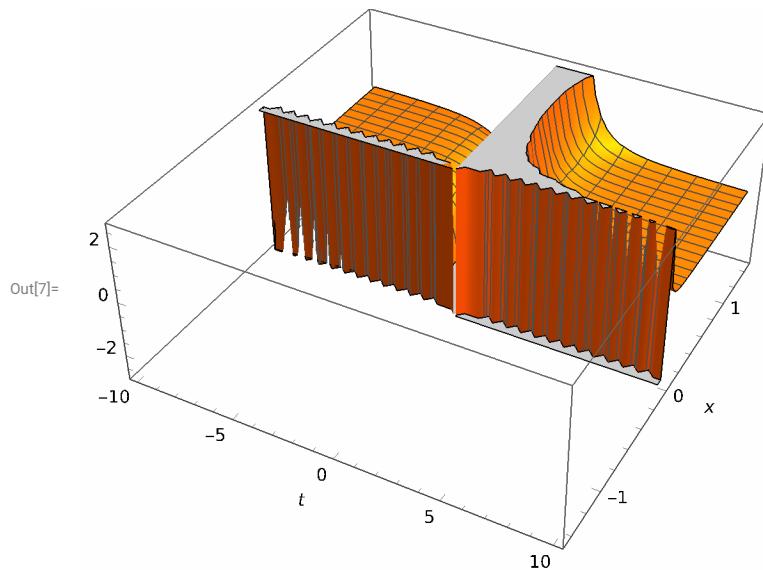
$\cot(x)$ is the cotangent function »

WolframAlpha 

$$\text{In[5]:= } \text{FullSimplify}\left[\frac{\csc[x]^2 (t x \sin[x] + e^x t \tan[x])}{t^4 x^{5/3}}\right]$$

$$\text{Out[5]= } \frac{\csc(x) (x + e^x \sec(x))}{t^3 x^{5/3}}$$

$$\text{In[7]:= } \text{Plot3D}\left[\frac{\csc[x] (x + e^x \sec[x])}{t^3 x^{5/3}}, \{t, -10., 10.\}, \{x, -1.4497, 1.4497\}\right]$$



■ $[(d^2 x/d^2 t) \sin x + (d^2 \pi^x/d^2 t) \tan x] / [(d^2 x^{1/3}/d^2 t) * (d^2 \sqrt{x}/d^2 t) \sin x]^2 \text{ Eq 15}$

$$\text{In[8]:= } \frac{((d^2 x/d^2 t) \sin x + (d^2 \pi^x/d^2 t) \tan x) / ((d^2 x^{1/3}/d^2 t) * (d^2 \sqrt{x}/d^2 t) \sin x)^2}{((d^2 x^{1/3}/d^2 t) * (d^2 \sqrt{x}/d^2 t) \sin x)^2}$$

$$\text{Out[8]= } \frac{\csc^2(x) (t x \sin(x) + t \pi^x \tan(x))}{t^4 x^{5/3}}$$

In[11]:=  $\frac{\{d^2 \times 2x/d^2 t\} \sin(x) + \{d^2 \times 2\pi^x/d^2 t\} \tan(x)}{\{\{d^2 \times 2x^{1/3}/d^2 t\} * \{d^2 \times 2\sqrt{x}/d^2 t\} \sin(x)\}^2}$

Out[11]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)}{\left(\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)\right)^2}$$



Result:

$$\frac{\csc^2(x) (t x \sin(x) + t \pi^x \tan(x))}{t^4 x^{5/3}}$$

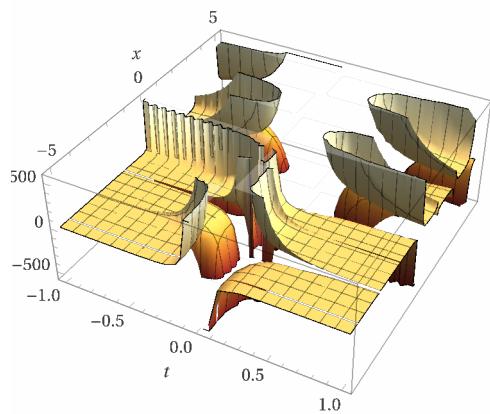


csc(x) is the cosecant function >

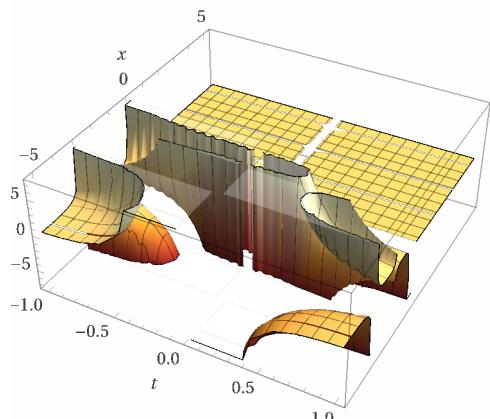
3D plots:



Real part:

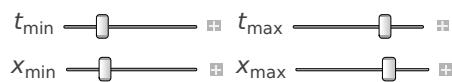
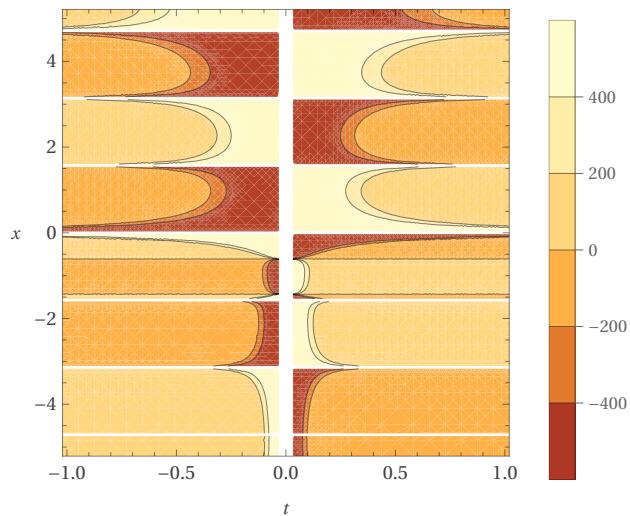


Imaginary part:

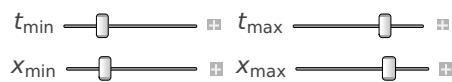
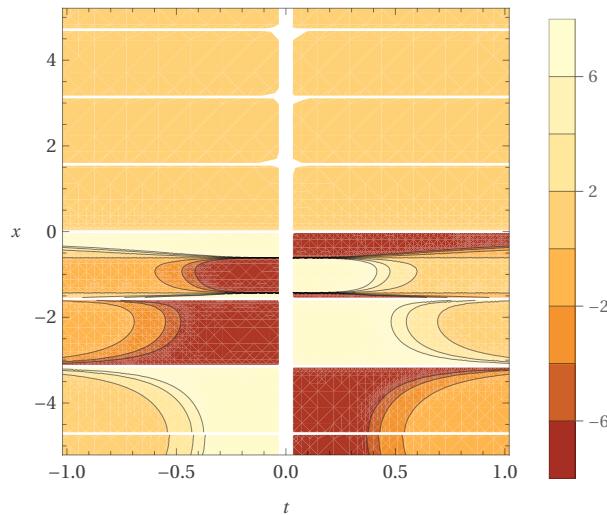


Contour plots:

Real part:



Imaginary part:



Alternate forms:

$$\frac{\csc(x)(x + \pi^x \sec(x))}{t^3 x^{5/3}}$$

More

$$\frac{(\pi^x + x \cos(x)) \csc(x) \sec(x)}{t^3 x^{5/3}}$$

$$\frac{\csc(x) \left(\frac{\pi^x \sec(x)}{x^{5/3}} + \frac{1}{x^{2/3}} \right)}{t^3}$$

[sec\(x\) is the secant function »](#)

Partial fraction expansion:

[Step-by-step solution](#)

$$\frac{\pi^x \csc(x) \sec(x)}{t^3 x^{5/3}} + \frac{\csc(x)}{t^3 x^{2/3}}$$

Series expansion at $x = 0$:

$$\begin{aligned} & \frac{1}{t^3 x^{8/3}} + \frac{1 + \log(\pi)}{t^3 x^{5/3}} + \frac{4 + 3 \log^2(\pi)}{6 t^3 x^{2/3}} + \frac{\sqrt[3]{x} (1 + \log^3(\pi) + 4 \log(\pi))}{6 t^3} + \\ & \frac{x^{4/3} (112 + 15 \log^4(\pi) + 120 \log^2(\pi))}{360 t^3} + \frac{x^{7/3} (7 + 3 \log^5(\pi) + 40 \log^3(\pi) + 112 \log(\pi))}{360 t^3} + \\ & \frac{x^{10/3} (1984 + 21 \log^6(\pi) + 420 \log^4(\pi) + 2352 \log^2(\pi))}{15120 t^3} + \\ & \frac{x^{13/3} (31 + 3 \log^7(\pi) + 84 \log^5(\pi) + 784 \log^3(\pi) + 1984 \log(\pi))}{15120 t^3} + O(x^{16/3}) \end{aligned}$$

(Puiseux series)

[log\(x\) is the natural logarithm »](#)

[Big-O notation »](#)

Derivative:

[Approximate form](#)

[Step-by-step solution](#)

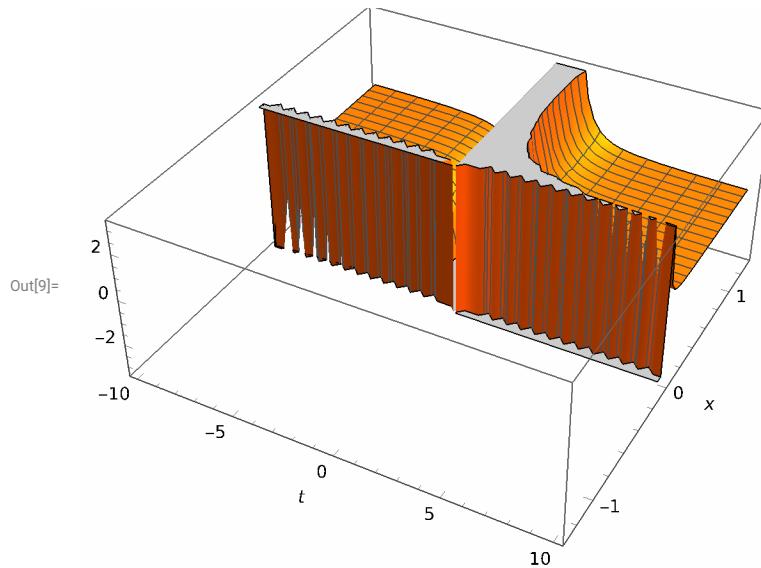
$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2}}{\left(\frac{(d^2 \sqrt[3]{x} t) (d^2 \sqrt{x} t) \sin(x)}{d^2 d^2} \right)^2} \right) =$$

$$-\frac{\cot(x) (\sec(x) (2 x - \pi^x (3 x \log(\pi) - 5) \sec(x)) + 3 x \csc(x) (x - \pi^x \sec^3(x) + 2 \pi^x \sec(x)))}{3 t^3 x^{8/3}}$$

[cot\(x\) is the cotangent function »](#)

[WolframAlpha](#)

In[9]:= Plot3D[$\frac{\csc[x]^2 (t \sin[x] + \pi^x t \tan[x])}{t^4 x^{5/3}}$, {t, -10., 10.}, {x, -1.30812, 1.30812}]



$\left[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x/d^2 t\} \tan x\right]^2 / [\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]$ Eq 16

```
In[12]:= ((d^2*(x/d^2)*t)*Sin[x] + (d^2*(Pi^x/d^2)*t)*Tan[x])^2/
((d^2*(x^(1/3)/d^2)*t)*(d^2*(Sqrt[x]/d^2)*t)*Sin[x])
```

Out[12]=

$$\frac{\csc(x) (t x \sin(x) + t \pi^x \tan(x))^2}{t^2 x^{5/6}}$$

$\left[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x/d^2 t\} \tan x\right]^2 / [\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]$

Out[14]=

Input:

$$\frac{\left(\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)\right)^2}{\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$

Result:

$$\frac{\csc(x) (t x \sin(x) + t \pi^x \tan(x))^2}{t^2 x^{5/6}}$$

[csc\(x\) is the cosecant function >](#)

Alternate forms:

$$\frac{\sin(x) (x + \pi^x \sec(x))^2}{x^{5/6}}$$

$$\frac{(x^2 \cos^2(x) + \pi^2 x + 2 \pi^x x \cos(x)) \tan(x) \sec(x)}{x^{5/6}}$$

$$\frac{\left(t x \sin(x) + \frac{\pi^x t \sin(x)}{\cos(x)}\right)^2}{t^2 x^{5/6} \sin(x)}$$

[More](#)[sec\(x\) is the secant function >](#)

Expanded form:

$$x^{7/6} \sin(x) + \frac{\pi^2 x \tan(x) \sec(x)}{x^{5/6}} + 2 \pi^x \sqrt[6]{x} \tan(x)$$

Series expansion at x = 0:

$$\sqrt[6]{x} + x^{7/6} (2 + 2 \log(\pi)) + x^{13/6} \left(\frac{11}{6} + 2 \log^2(\pi) + 2 \log(\pi) \right) + O(x^{19/6})$$

(Puiseux series)

[log\(x\) is the natural logarithm >](#)[Big-O notation >](#)

Derivative:

[Approximate form](#)[Step-by-step solution](#)

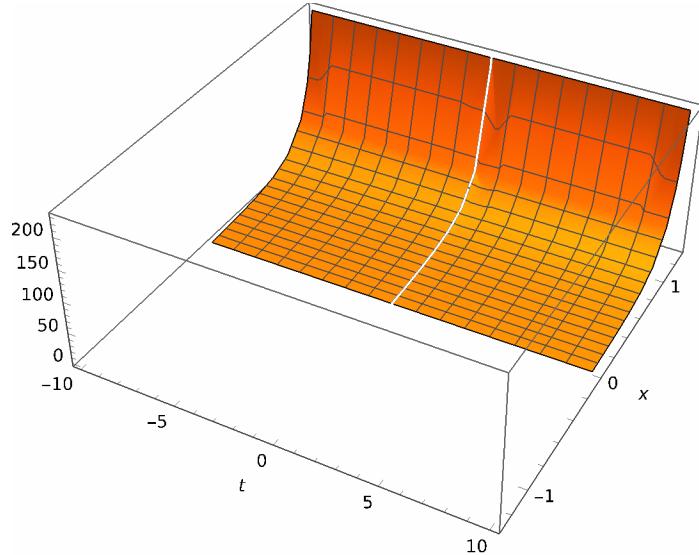
$$\frac{\partial}{\partial x} \left(\frac{\left(\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2} \right)^2}{\frac{(d^2 \sqrt[3]{x} t) (d^2 \sqrt{x} t) \sin(x)}{d^2 d^2}} \right) = \frac{1}{6 x^{11/6}} \cos(x) (x + \pi^x \sec(x))$$

$$(x (6 x + 7 \tan(x)) + 12 \pi^x x \sec^3(x) + \pi^x \sec(x) ((12 x \log(\pi) - 5) \tan(x) - 6 x))$$

WolframAlpha [+](#)

In[13]:= Plot3D[$\frac{\csc[x] (\pi^x t \tan[x] + t x \sin[x])^2}{t^2 x^{5/6}}$, {t, -10., 10.}, {x, -1.29231, 1.29231}]

Out[13]=



$\blacksquare [d^2 x/d^2 t] \sin x + [d^2 \pi^x x/d^2 t] \tan x] / [d^2 x^{1/3}/d^2 t] * [d^2 \sqrt{x}/d^2 t] \sin x]$ Eq 17

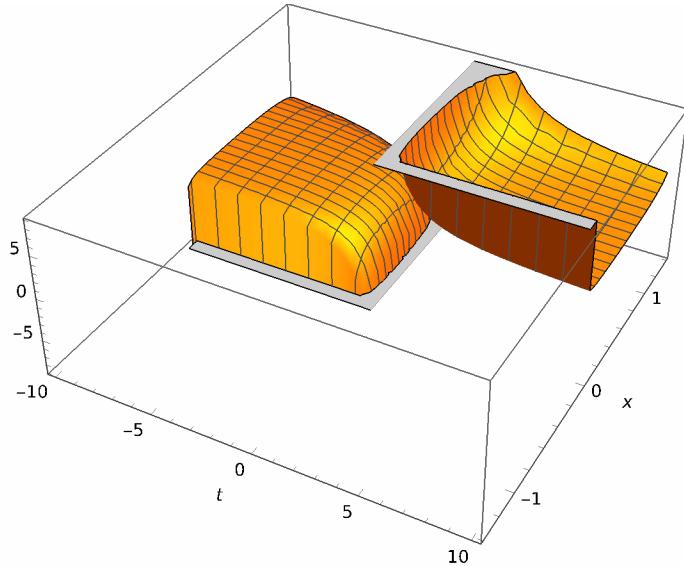
In[15]:=
$$\frac{((d^2 x/d^2 t) \sin x + (d^2 \pi^x x/d^2 t) \tan x)}{((d^2 x^{1/3}/d^2 t) * (d^2 \sqrt{x}/d^2 t) \sin x)}$$

Out[15]=

$$\frac{\csc(x) (t x \sin(x) + t \pi^x \tan(x))}{t^2 x^{5/6}}$$

In[16]:= Plot3D[$\frac{\csc[x] (t \sin[x] + \pi^x t \tan[x])}{t^2 x^{5/6}}$, {t, -10., 10.}, {x, -1.36799, 1.36799}]

Out[16]=



■ $[(d^2 x^2 / d^2 t) \sin x + (d^2 \pi^x x / d^2 t) \tan x] / [(d^2 x^{1/3} / d^2 t) * (d^2 \sqrt{x} / d^2 t) \sin x]^3$ Eq 18

In[17]:=
$$\frac{(d^2 (x/d^2) * t) \sin(x) + (d^2 (\pi^x / d^2) * t) \tan(x)}{(d^2 (x^{1/3}/d^2) * t) * (d^2 (\sqrt{x}/d^2) * t) \sin(x)^3}$$

Out[17]=

$$\frac{\csc^3(x) (t x \sin(x) + t \pi^x \tan(x))}{t^6 x^{5/2}}$$

In[19]:= **✚** $[(d^2 x^2 / d^2 t) \sin x + (d^2 \pi^x x / d^2 t) \tan x] / [(d^2 x^{1/3} / d^2 t) * (d^2 \sqrt{x} / d^2 t) \sin x]^3$

Out[19]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)}{\left(\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)\right)^3}$$



Result:

$$\frac{\csc^3(x) (t x \sin(x) + t \pi^x \tan(x))}{t^6 x^{5/2}}$$

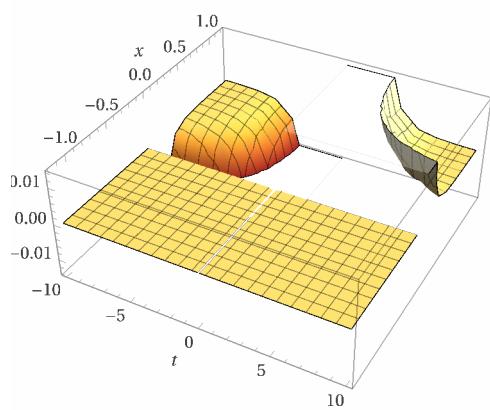


csc(x) is the cosecant function »

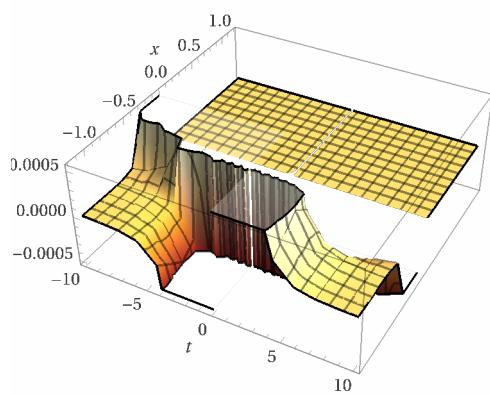
3D plots:



Real part:



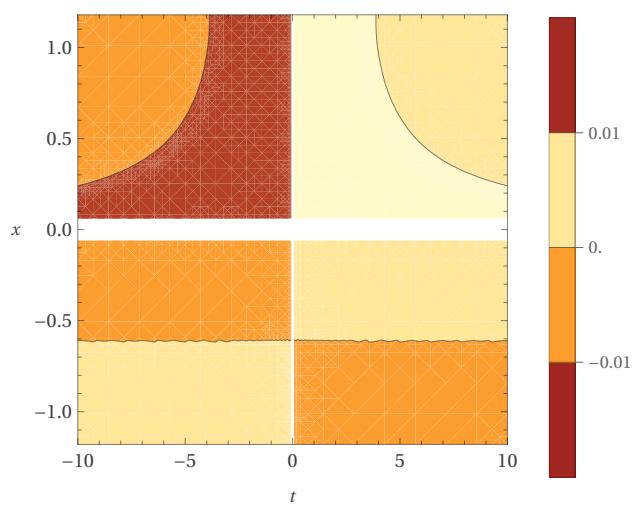
Imaginary part:

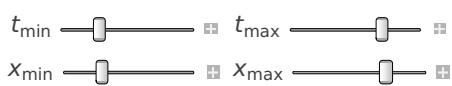


Contour plots:

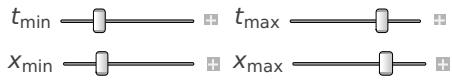
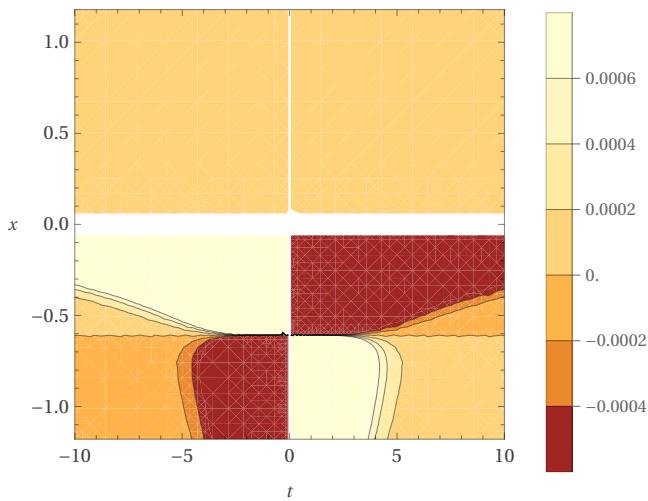


Real part:





Imaginary part:



Alternate forms:

[More](#)

$$\frac{\csc^2(x)(x + \pi^x \sec(x))}{t^5 x^{5/2}}$$

$$\frac{(\pi^x + x \cos(x)) \csc^2(x) \sec(x)}{t^5 x^{5/2}}$$

$$\frac{\csc^2(x) \left(\frac{\pi^x \sec(x)}{x^{5/2}} + \frac{1}{x^{3/2}} \right)}{t^5}$$

[sec\(x\) is the secant function](#) »

Partial fraction expansion:

[Step-by-step solution](#)

$$\frac{\pi^x \csc^2(x) \sec(x)}{t^5 x^{5/2}} + \frac{\csc^2(x)}{t^5 x^{3/2}}$$

Derivative:

[Approximate form](#)

[Step-by-step solution](#)

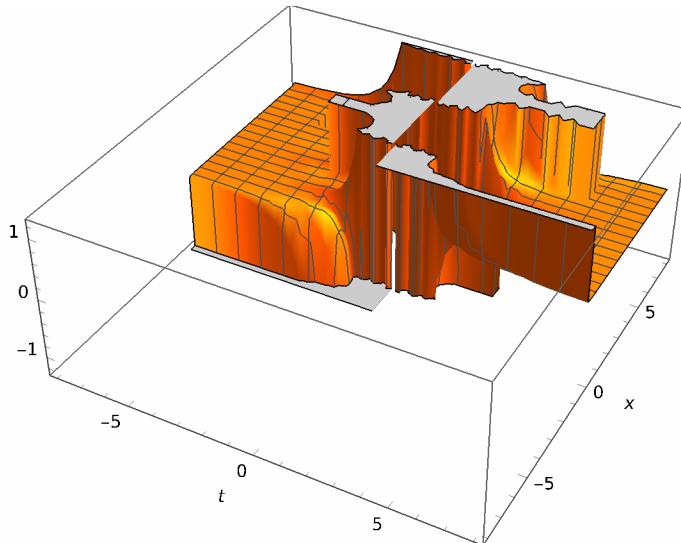
$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2}}{\left(\frac{(d^2 \sqrt[3]{x} t) (d^2 \sqrt{x} t) \sin(x)}{d^2} \right)^3} \right) = -\frac{1}{2 t^5 x^{7/2}} \cot(x) \csc(x)$$

$\text{cot}(x)$ is the cotangent function »
 $\log(x)$ is the natural logarithm »

WolframAlpha +

In[18]:= Plot3D[$\frac{\csc[x]^3(t \sin[x] + \pi^x t \tan[x])}{t^6 x^{5/2}}$, {t, -8, 8}, {x, -8, 8}]

Out[18]=



■ $[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x] / [\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]$ Eq 19

In[20]:= $\frac{(d^2 \times (x/d^2) * t) * \sin[x] + (d^2 \times (\text{Pi}^x * x/d^2) * t) * \tan[x]}{(d^2 \times (x^{1/3}/d^2) * t + (d^2 \times (\text{Sqrt}[x]/d^2) * t) * \sin[x]}$

Out[20]=

$$\frac{t x \sin(x) + t \pi^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

ln[22]:= ■ $[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x] / [\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]$

Out[22]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$

Result:

$$\frac{t x \sin(x) + t \pi^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Alternate forms:

[More](#) [+](#)

$$\frac{(\pi^x + x \cos(x)) \tan(x)}{\sqrt[3]{x} + \sqrt{x} \sin(x)}$$

$$\frac{(\pi^x + x \cos(x)) \tan(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

$$\frac{x \sin(x) + \pi^x \tan(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

Expanded form:

[+](#)

$$\frac{t x \sin(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{t \pi^x \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Series expansion at $x = 0$:[+](#)

$$\begin{aligned} & x^{2/3} + x^{5/3} (1 + \log(\pi)) - x^{11/6} + \frac{1}{6} x^{8/3} (2 + 3 \log^2(\pi)) + x^{17/6} (-1 - \log(\pi)) + \\ & x^3 + \frac{1}{6} x^{11/3} (-1 + \log^3(\pi) + 2 \log(\pi)) + \frac{1}{6} x^{23/6} (-1 - 3 \log^2(\pi)) + \\ & x^4 (1 + \log(\pi)) - x^{25/6} + \frac{1}{120} x^{14/3} (16 + 5 \log^4(\pi) + 20 \log^2(\pi)) + \\ & \frac{1}{6} x^{29/6} (2 - \log^3(\pi) - \log(\pi)) + \frac{1}{2} x^5 \log^2(\pi) + x^{31/6} (-1 - \log(\pi)) + x^{16/3} + O(x^{17/3}) \end{aligned}$$

(Puiseux series)

[log\(x\) is the natural logarithm](#) »[Big-O notation](#) »

Derivative:

[Approximate form](#)[Step-by-step solution](#)[+](#)

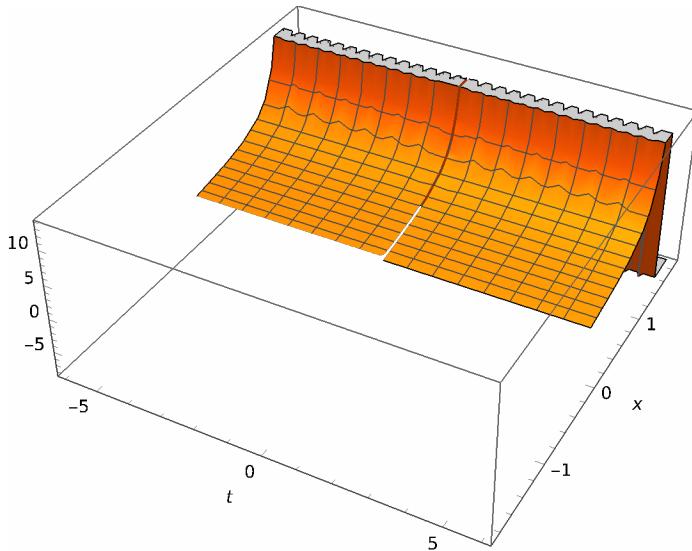
$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2}}{\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2}} \right) = \frac{1}{6 x^{4/3} (\sqrt[6]{x} \sin(x) + 1)^2}$$

$$\begin{aligned} & (6 x (\sqrt[6]{x} \sin(x) + 1) (\sin(x) + x \cos(x) + \pi^x \sec^2(x) + \pi^x \log(\pi) \tan(x)) - \\ & (x \sin(x) + \pi^x \tan(x)) (6 x^{7/6} \cos(x) + 3 \sqrt[6]{x} \sin(x) + 2)) \end{aligned}$$

[sec\(x\) is the secant function](#) »WolframAlpha [+](#)

In[21]:= Plot3D[$\frac{t x \sin[x] + \pi^x t \tan[x]}{t x^{1/3} + t \sqrt{x} \sin[x]}$, {t, -6., 6.}, {x, -1.87476, 1.87476}]

Out[21]=



$[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x]/[\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]^2$ Eq 20

In[23]:= $\frac{(d^2 \times (x/d^2) * t) * \sin(x) + (d^2 \times (\text{Pi}^x * x/d^2) * t) * \tan(x)}{(d^2 \times (x^{1/3}/d^2) * t + (d^2 \times (\text{Sqrt}[x]/d^2) * t) * \sin(x))^2}$

Out[23]=

$$\frac{t x \sin(x) + t \pi^x \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2}$$

$[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x]/[\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]^2$

Out[25]=

Input:

$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)}{\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t + \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)\right)^2}$$



Result:

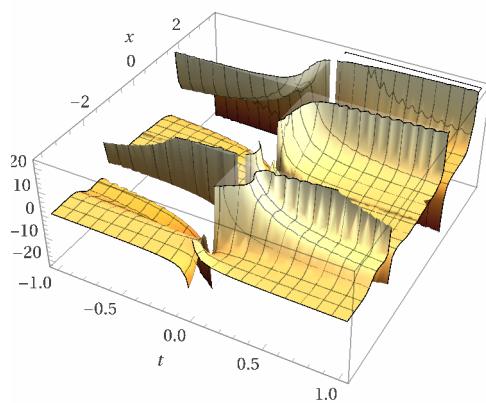
$$\frac{t x \sin(x) + t \pi^x \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2}$$



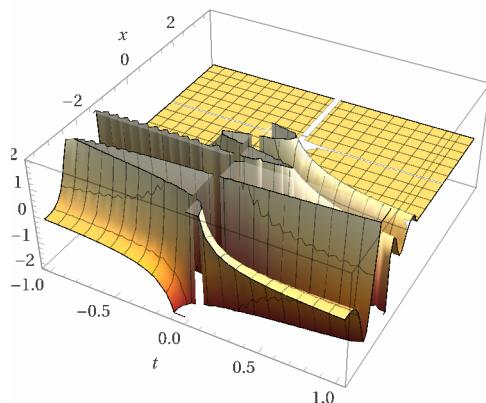
3D plots:



Real part:

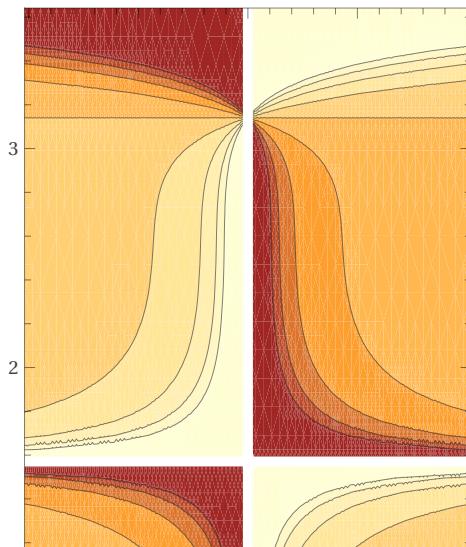


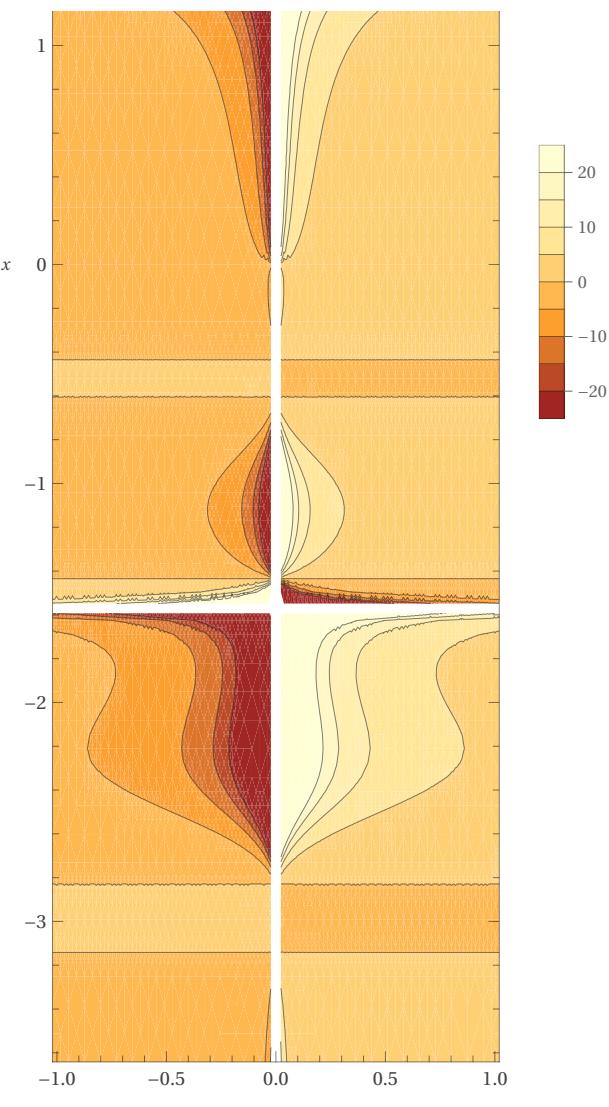
Imaginary part:



Contour plots:

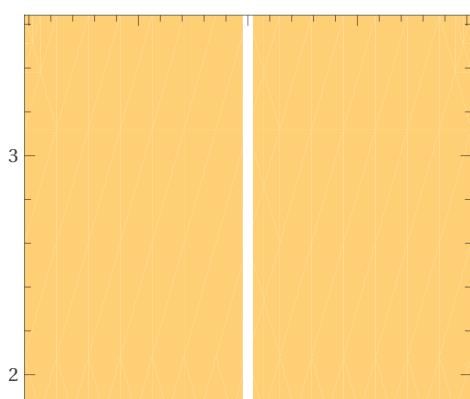
Real part:

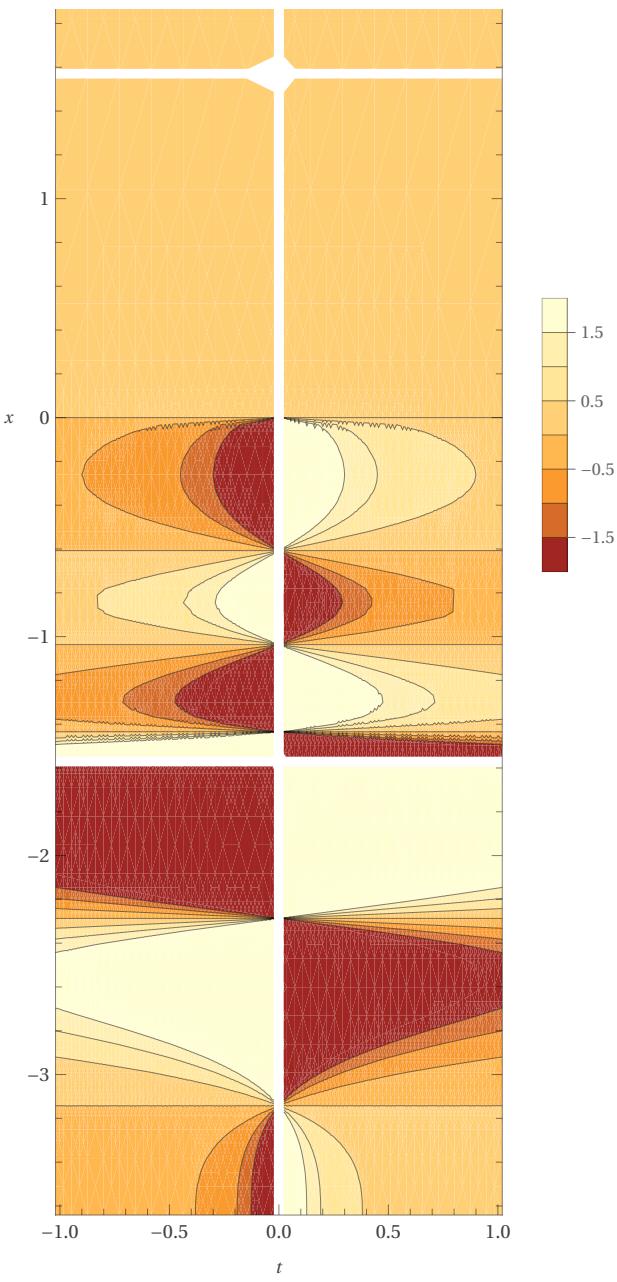




t_{\min} ————— t_{\max} —————
 x_{\min} ————— x_{\max} —————

Imaginary part:





t_{\min} t_{\max}

x_{\min} x_{\max}

Alternate forms:

$$\frac{(\pi^x + x \cos(x)) \tan(x)}{t x^{2/3} (\sqrt[6]{x} \sin(x) + 1)^2}$$

$$\frac{x \sin(x) + \pi^x \tan(x)}{t x^{2/3} (\sqrt[6]{x} \sin(x) + 1)^2}$$

More

$$\frac{t x \sin(x) + \frac{\pi^x t \sin(x)}{\cos(x)}}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2}$$

Partial fraction expansion:

[Step-by-step solution](#) +

$$\frac{\pi^x \tan(x)}{t x^{2/3} (\sqrt[6]{x} \sin(x) + 1)^2} + \frac{\sqrt[3]{x} \sin(x)}{t (\sqrt[6]{x} \sin(x) + 1)^2}$$

Expanded forms:

+

$$\begin{aligned} & \frac{t x \sin(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2} + \frac{t \pi^x \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2} \\ & \frac{t x \sin(x)}{2 t^2 x^{5/6} \sin(x) + t^2 x^{2/3} + t^2 x \sin^2(x)} + \frac{t \pi^x \tan(x)}{2 t^2 x^{5/6} \sin(x) + t^2 x^{2/3} + t^2 x \sin^2(x)} \end{aligned}$$

Derivative:

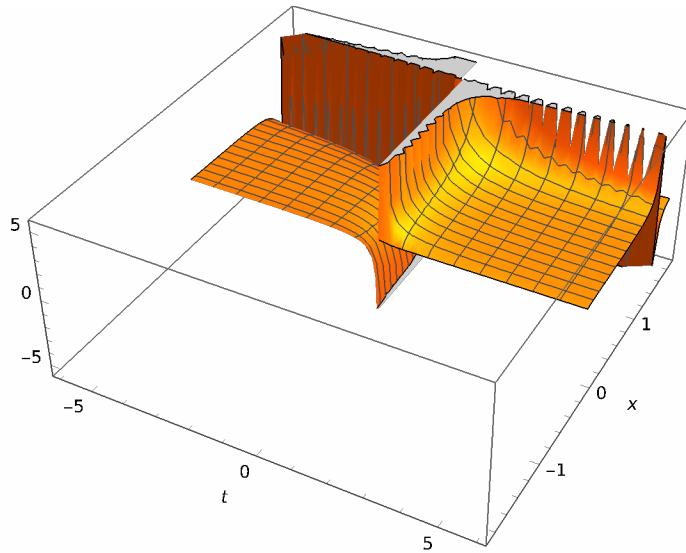
[Approximate form](#)[Step-by-step solution](#) +

$$\begin{aligned} & \frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2}}{\left(\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2} \right)^2} \right) = \\ & (3 x (\sqrt[6]{x} \sin(x) + 1) (\sin(x) + x \cos(x) + \pi^x \sec^2(x) + \pi^x \log(\pi) \tan(x)) - \\ & (x \sin(x) + \pi^x \tan(x)) (6 x^{7/6} \cos(x) + 3 \sqrt[6]{x} \sin(x) + 2)) / (3 t x^{5/3} (\sqrt[6]{x} \sin(x) + 1)^3) \end{aligned}$$

sec(x) is the secant function »log(x) is the natural logarithm »WolframAlpha +

```
In[24]:= Plot3D[(t x Sin[x] + π^x t Tan[x]) / (t x^(1/3) + t √x Sin[x])^2, {t, -6., 6.}, {x, -1.87476, 1.87476}]
```

Out[24]=



$$\boxed{\text{Eq 21}} \quad \text{[}\{d^2x/d^2t\}\sin x + \{d^2\pi^x/d^2t\}\tan x\text{]}^2 / [\{d^2x^{1/3}/d^2t\} + \{d^2\sqrt{x}/d^2t\}\sin x]$$

In[25]:=

$$\frac{\left(d^2 \times (x/d^2) \cdot t \cdot \sin(x) + (d^2 \times (\pi^x/d^2) \cdot t) \cdot \tan(x)\right)^2}{\left(d^2 \times (x^{1/3}/d^2) \cdot t + (d^2 \times (\sqrt{x}/d^2) \cdot t) \cdot \sin(x)\right)}$$

Out[26]=

$$\frac{(t x \sin(x) + t \pi^x \tan(x))^2}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

$$\boxed{\text{Eq 26}} \quad \text{[}\{d^2x/d^2t\}\sin x + \{d^2\pi^x/d^2t\}\tan x\text{]}^2 / [\{d^2x^{1/3}/d^2t\} + \{d^2\sqrt{x}/d^2t\}\sin x]$$

Out[29]=

Input:

$$\frac{\left(\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)\right)^2}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)}$$



Result:

$$\frac{(t x \sin(x) + t \pi^x \tan(x))^2}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

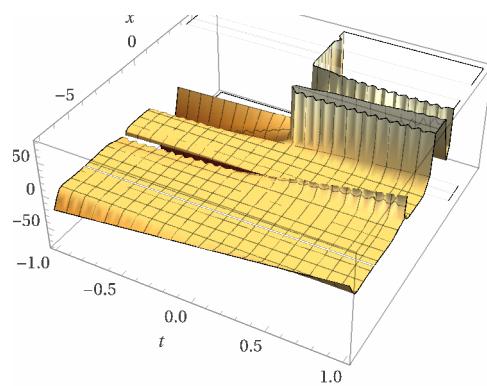


3D plots:

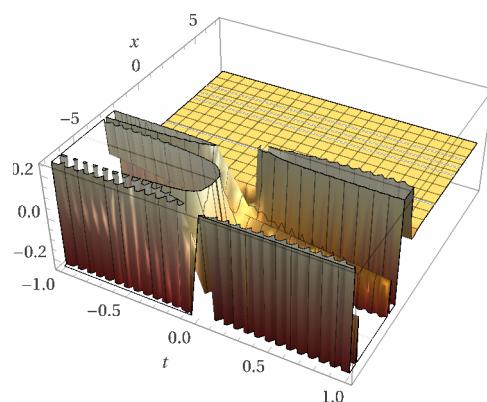


Real part:





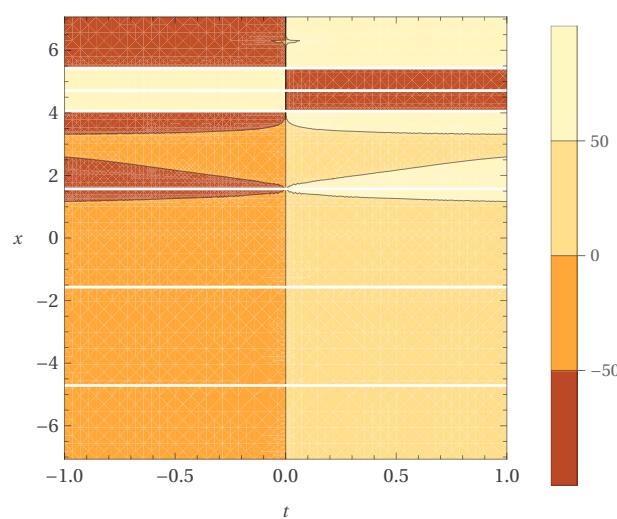
Imaginary part:



Contour plots:

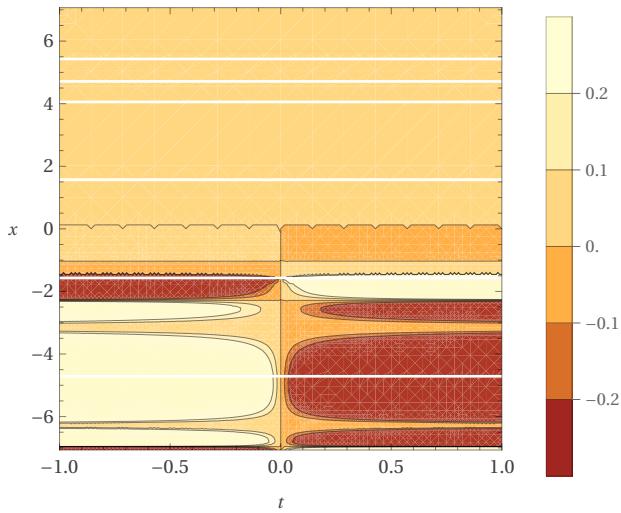


Real part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}
 x_{\min} x_{\max}

Alternate forms:

More

$$\frac{t(x \sin(x) + \pi^x \tan(x))^2}{\sqrt[3]{x} + \sqrt{x} \sin(x)}$$

$$\frac{t(x \sin(x) + \pi^x \tan(x))^2}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

$$\frac{t(\pi^x + x \cos(x))^2 \tan^2(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

Expanded form:

$$\frac{t^2 x^2 \sin^2(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{t^2 \pi^{2x} \tan^2(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{2 t^2 \pi^x x \sin(x) \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Derivative:

Approximate form

Step-by-step solution

$$\frac{\partial}{\partial x} \left(\frac{\left(\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2} \right)^2}{\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2}} \right) =$$

$$\frac{2(t x \sin(x) + t \pi^x \tan(x))(t \sin(x) + t x \cos(x) + t \pi^x \sec^2(x) + t \pi^x \log(\pi) \tan(x))}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} -$$

$$\frac{(t x \sin(x) + t \pi^x \tan(x))^2 \left(\frac{t}{3 x^{2/3}} + \frac{t \sin(x)}{2 \sqrt{x}} + t \sqrt{x} \cos(x) \right)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2}$$

$\sec(x)$ is the secant function »

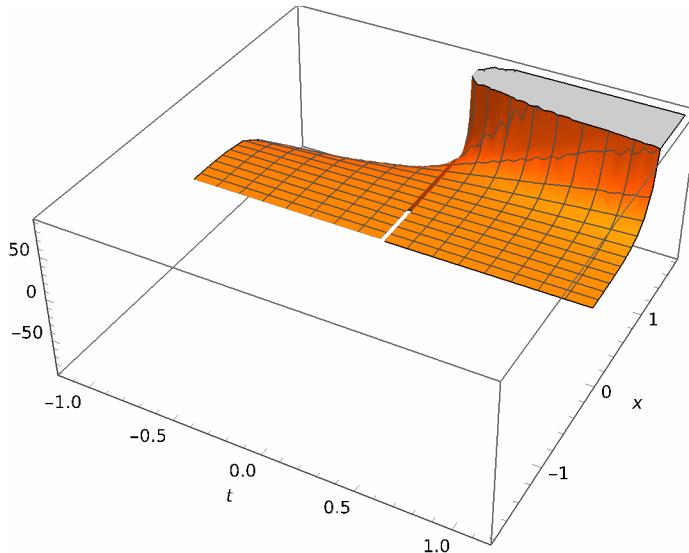
$\log(x)$ is the natural logarithm »

WolframAlpha 

$$\text{In[28]:= } \text{Plot3D}\left[\frac{(t x \sin[x] + \pi^x t \tan[x])^2}{t x^{1/3} + t \sqrt{x} \sin[x]}, \{t, -1.14412, 1.14412\}, \{x, -1.78005, 1.78005\}\right]$$

$$\text{In[27]:= } \text{Plot3D}\left[\frac{(t x \sin[x] + \pi^x t \tan[x])^2}{t x^{1/3} + t \sqrt{x} \sin[x]}, \{t, -1.14412, 1.14412\}, \{x, -1.78005, 1.78005\}\right]$$

Out[27]=



 $[(d^2 x/d^2 t) \sin x + (d^2 \pi^x x/d^2 t) \tan x]/[(d^2 x^{1/3}/d^2 t) + (d^2 \sqrt{x}/d^2 t) \sin x]^3$ Eq 22

$$\text{In[30]:= } \frac{(d^2 x/(d^2 t)) \sin x + (d^2 (\pi^x x)/(d^2 t)) \tan x}{(d^2 x^{1/3}/(d^2 t)) + (d^2 (\sqrt{x})/(d^2 t)) \sin x}$$

Out[30]=

$$\frac{t x \sin(x) + t \pi^x \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^3}$$

 $[(d^2 x/d^2 t) \sin x + (d^2 \pi^x x/d^2 t) \tan x]/[(d^2 x^{1/3}/d^2 t) + (d^2 \sqrt{x}/d^2 t) \sin x]^3$

Out[33]=

Input: 

Input:

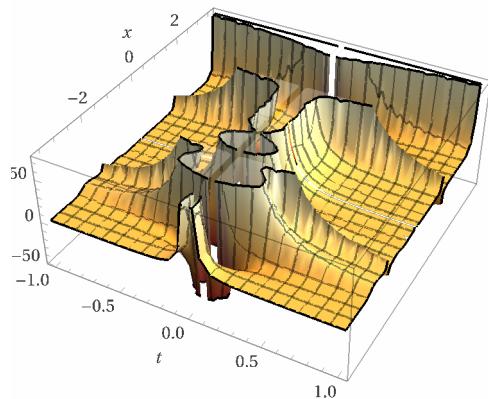
$$\frac{\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) + \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)}{\left(d^2 \times \frac{\sqrt[3]{x}}{d^2} t + \left(d^2 \times \frac{\sqrt{x}}{d^2} t\right) \sin(x)\right)^3}$$

Result:

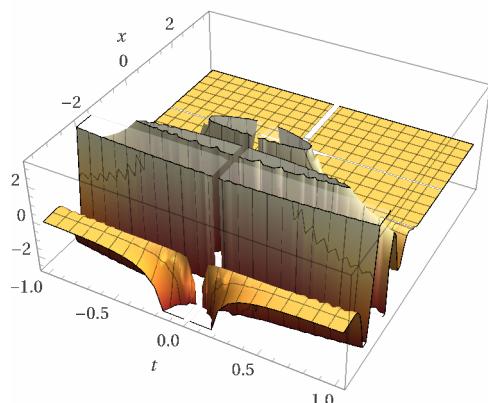
$$\frac{t x \sin(x) + t \pi^x \tan(x)}{\left(t \sqrt[3]{x} + t \sqrt{x} \sin(x)\right)^3}$$

3D plots:

Real part:

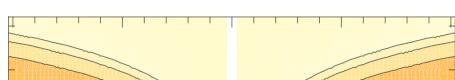


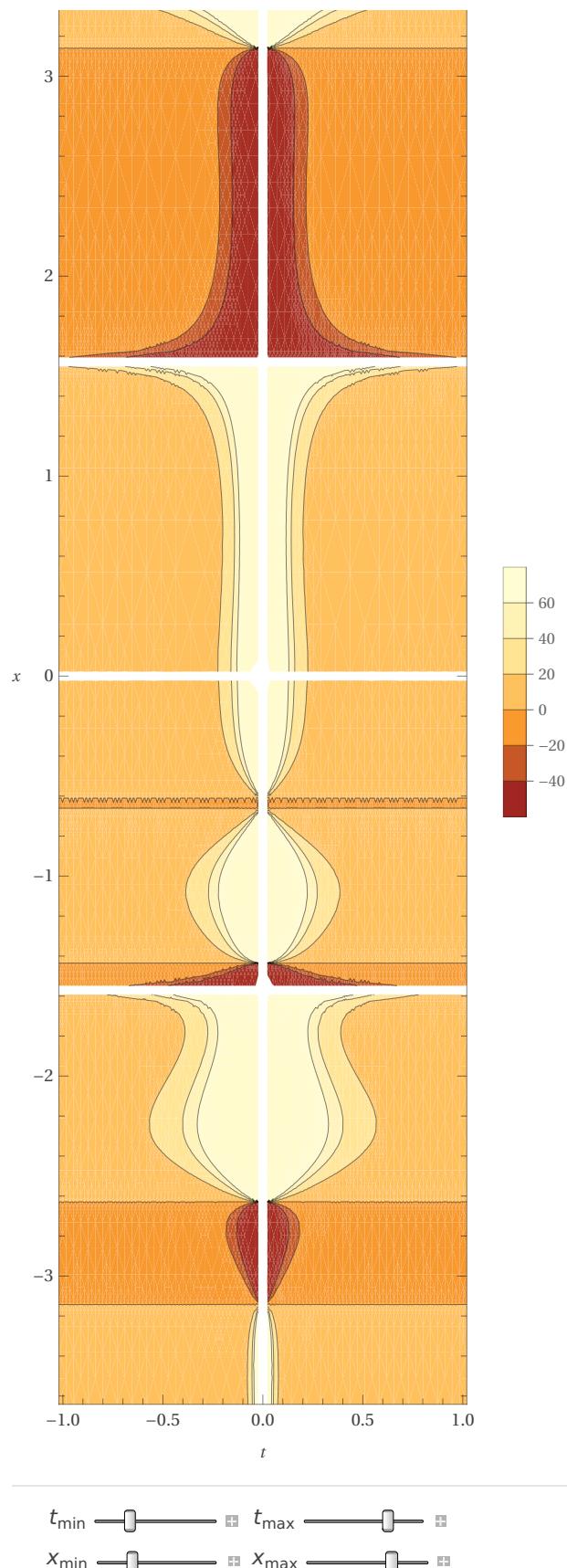
Imaginary part:



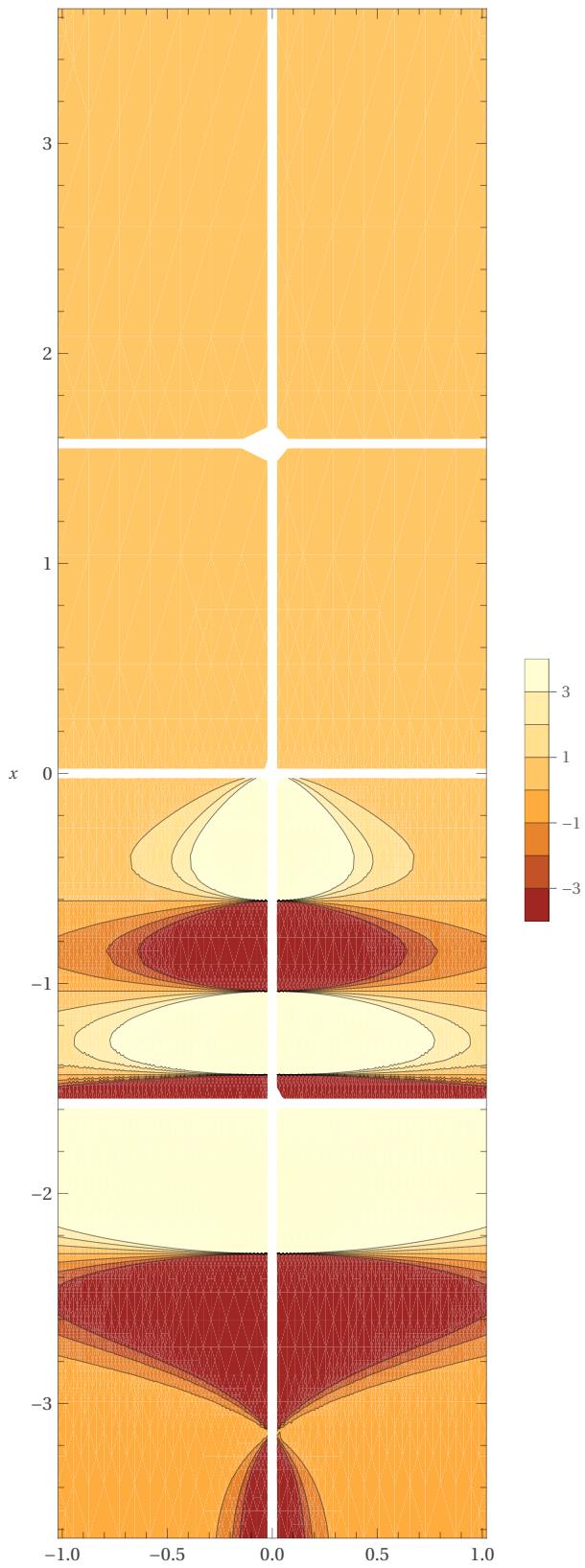
Contour plots:

Real part:





Imaginary part:



t

$$\begin{array}{c} t_{\min} \xrightarrow{\quad} t_{\max} \\ x_{\min} \xrightarrow{\quad} x_{\max} \end{array}$$

Alternate forms:

[More](#)

$$\frac{(\pi^x + x \cos(x)) \tan(x)}{t^2 x (\sqrt[6]{x} \sin(x) + 1)^3}$$

$$\frac{x \sin(x) + \pi^x \tan(x)}{t^2 x (\sqrt[6]{x} \sin(x) + 1)^3}$$

$$\frac{t x \sin(x) + \frac{\pi^x t \sin(x)}{\cos(x)}}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^3}$$

Partial fraction expansion:

[Step-by-step solution](#)

$$\frac{\sin(x)}{t^2 (\sqrt[6]{x} \sin(x) + 1)^3} + \frac{\pi^x \tan(x)}{t^2 x (\sqrt[6]{x} \sin(x) + 1)^3}$$

Expanded forms:

[+](#)

$$\frac{t x \sin(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^3} + \frac{t \pi^x \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^3}$$

$$\frac{t x \sin(x)}{3 t^3 x^{7/6} \sin(x) + 3 t^3 x^{4/3} \sin^2(x) + t^3 x^{3/2} \sin^3(x) + t^3 x} +$$

$$\frac{t \pi^x \tan(x)}{3 t^3 x^{7/6} \sin(x) + 3 t^3 x^{4/3} \sin^2(x) + t^3 x^{3/2} \sin^3(x) + t^3 x}$$

Derivative:

[Approximate form](#)[Step-by-step solution](#)[+](#)

$$\frac{\partial}{\partial x} \left(\frac{\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2}}{\left(\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2} \right)^3} \right) = \frac{t \sin(x) + t x \cos(x) + t \pi^x \sec^2(x) + t \pi^x \log(\pi) \tan(x)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^3} -$$

$$\frac{3 (t x \sin(x) + t \pi^x \tan(x)) \left(\frac{t}{3 x^{2/3}} + \frac{t \sin(x)}{2 \sqrt{x}} + t \sqrt{x} \cos(x) \right)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^4}$$

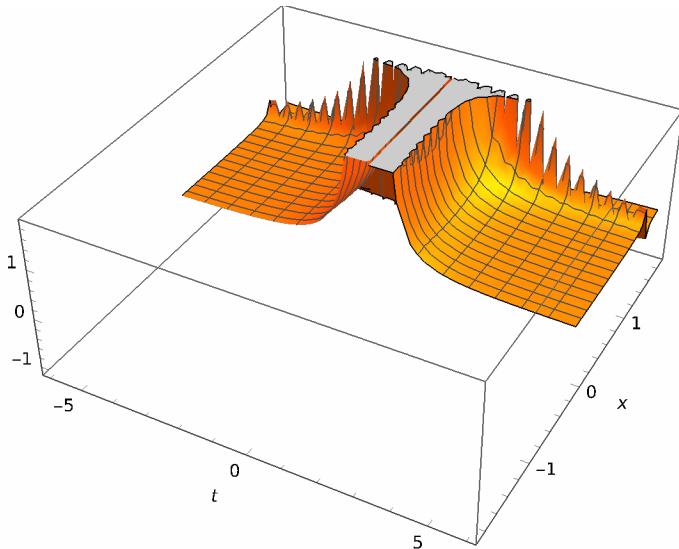
sec(x) is the secant function >

log(x) is the natural logarithm >

In[32]:= Plot3D[$\frac{t x \sin[x] + \pi^U t \tan[x]}{(t x / + t \sqrt{x} \sin[x])}$, {t, -6., 6.}, {x, -1.87476, 1.87476}]

In[31]:= Plot3D[$\frac{t x \sin[x] + \pi^U t \tan[x]}{(t x / + t \sqrt{x} \sin[x])}$, {t, -6., 6.}, {x, -1.87476, 1.87476}]

Out[31]=



$[(d^2 \times (x/d^2) * t) \sin(x) + (d^2 \times (\pi^U x/d^2) * t) \tan(x)]^3 / [(d^2 \times (x^{1/3}/d^2) * t) + (d^2 \times (\sqrt{x}/d^2) * t) \sin(x)]$ Eq 23

In[34]:= $\frac{((d^2 \times (x/d^2) * t) \sin(x) + (d^2 \times (\pi^U x/d^2) * t) \tan(x))^3}{(d^2 \times (x^{1/3}/d^2) * t) + (d^2 \times (\sqrt{x}/d^2) * t) \sin(x)}$

Out[34]=

$$\frac{(t x \sin(x) + t \pi^U \tan(x))^3}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

$[(d^2 \times (x/d^2) * t) \sin(x) + (d^2 \times (\pi^U x/d^2) * t) \tan(x)]^3 / [(d^2 \times (x^{1/3}/d^2) * t) + (d^2 \times (\sqrt{x}/d^2) * t) \sin(x)]$

Out[36]=

Input:

$$\frac{((d^2 \times \frac{x}{d^2} t) \sin(x) + (d^2 \times \frac{\pi^U}{d^2} t) \tan(x))^3}{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + (d^2 \times \frac{\sqrt{x}}{d^2} t) \sin(x)}$$



Result:

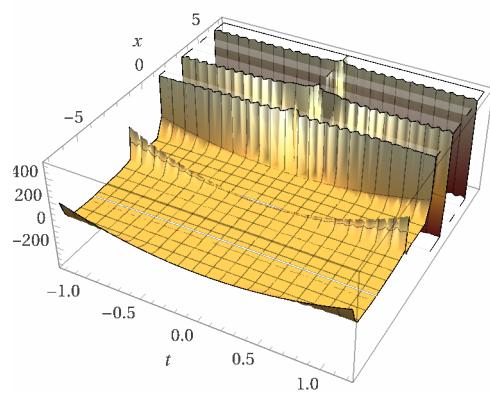
$$\frac{(t x \sin(x) + t \pi^U \tan(x))^3}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$



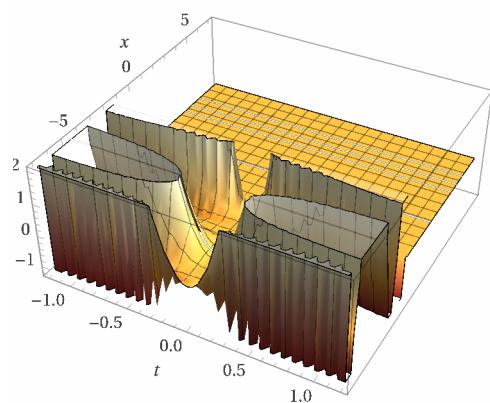
$$\nu \nabla x + \nu \nabla x \sin(x)$$

3D plots:

Real part:

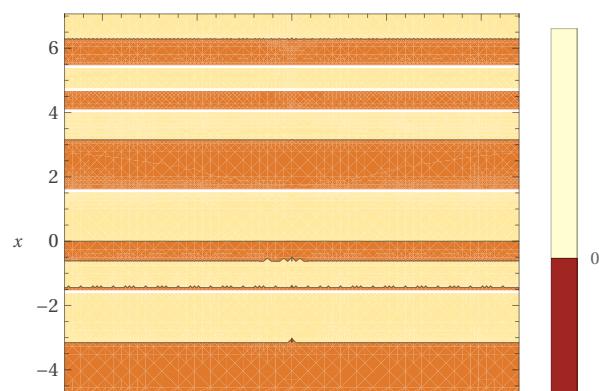


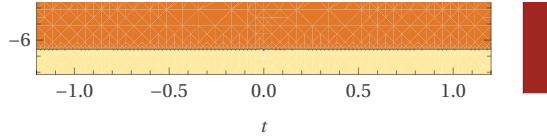
Imaginary part:



Contour plots:

Real part:

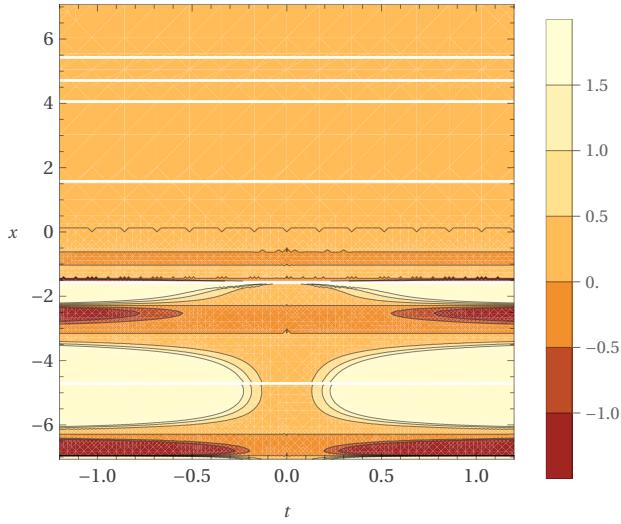




t_{\min} t_{\max}

x_{\min} x_{\max}

Imaginary part:



t_{\min} t_{\max}

x_{\min} x_{\max}

Alternate forms:

[More](#)

$$\frac{t^2 (x \sin(x) + \pi^x \tan(x))^3}{\sqrt[3]{x} + \sqrt{x} \sin(x)}$$

$$\frac{t^2 (x \sin(x) + \pi^x \tan(x))^3}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

$$\frac{t^2 (\pi^x + x \cos(x))^3 \tan^3(x)}{\sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}$$

Expanded form:

$$\frac{t^3 x^3 \sin^3(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{3 t^3 \pi^x x^2 \sin^2(x) \tan(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{t^3 \pi^{3x} \tan^3(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} + \frac{3 t^3 \pi^{2x} x \sin(x) \tan^2(x)}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

Derivative:

[Approximate form](#)

[Step-by-step solution](#)

$$\frac{\partial}{\partial x} \left(\frac{\left(\frac{(d^2 x t) \sin(x)}{d^2} + \frac{(d^2 \pi^x t) \tan(x)}{d^2} \right)^3}{\frac{d^2 \sqrt[3]{x} t}{d^2} + \frac{(d^2 \sqrt{x} t) \sin(x)}{d^2}} \right) =$$

$$\frac{3 (t x \sin(x) + t \pi^x \tan(x))^2 (t \sin(x) + t x \cos(x) + t \pi^x \sec^2(x) + t \pi^x \log(\pi) \tan(x))}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)} -$$

$$\frac{(t x \sin(x) + t \pi^x \tan(x))^3 \left(\frac{t}{3 x^{2/3}} + \frac{t \sin(x)}{2 \sqrt{x}} + t \sqrt{x} \cos(x) \right)}{(t \sqrt[3]{x} + t \sqrt{x} \sin(x))^2}$$

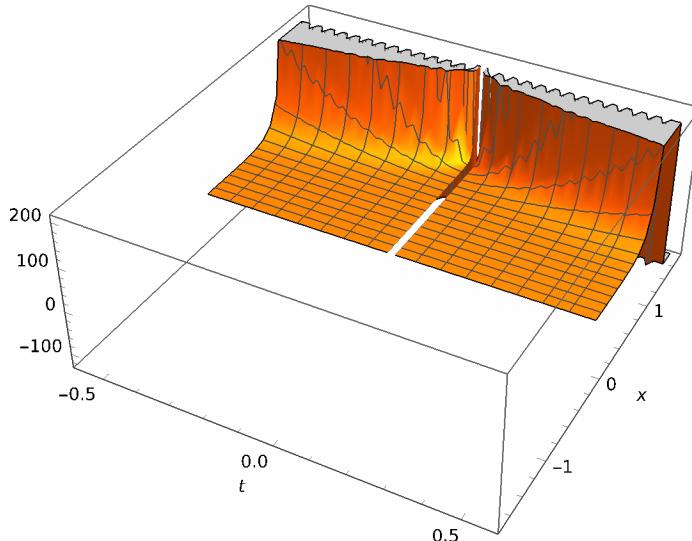
$\sec(x)$ is the secant function »

$\log(x)$ is the natural logarithm »

WolframAlpha 

In[35]:= Plot3D[$\frac{(t x \sin[x] + \pi^x t \tan[x])^3}{t x^{1/3} + t \sqrt{x} \sin[x]}$, {t, -0.569059, 0.569059}, {x, -1.72149, 1.72149}]

Out[35]=



■ $\frac{(d^2 x / d^2 t) \sin x + (d^2 \pi^x / d^2 t) \tan x}{(d^2 x^{1/3} / d^2 t) + (d^2 \sqrt{x} / d^2 t) \sin x}$ Eq 23

In[37]:= $\frac{(d^2 x / d^2 t) \sin x + (d^2 \pi^x / d^2 t) \tan x}{(d^2 x^{1/3} / d^2 t) + (d^2 \sqrt{x} / d^2 t) \sin x}$

Out[37]=

$$\frac{(t x \sin(x) + t \pi^x \tan(x))^3}{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}$$

In[38]:= Simplify[$\frac{(t x \sin[x] + \pi^x t \tan[x])^3}{t x^{1/3} + t \sqrt{x} \sin[x]}$]

Out[38]=

$$\frac{t^2 (x \sin(x) + \pi^x \tan(x))^3}{\sqrt[3]{x} + \sqrt{x} \sin(x)}$$

 $[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x]^3 / [\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]^{1/3}$ Eq 24

In[1]:= $\frac{((d^2 \times (x/d^2) * t) * \sin[x] + (d^2 \times (\text{Pi}^x * x/d^2) * t) * \tan[x])^3}{(d^2 \times (x^{1/3}/d^2) * t + (d^2 \times (\text{Sqrt}[x]/d^2) * t) * \sin[x])^{(1/3)}}$

Out[1]= $\frac{(t x \sin(x) + t \pi^x \tan(x))^3}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}}$

In[2]:=  $[\{d^2 x/d^2 t\} \sin x + \{d^2 \pi^x x/d^2 t\} \tan x]^3 / [\{d^2 x^{1/3}/d^2 t\} + \{d^2 \sqrt{x}/d^2 t\} \sin x]^{1/3}$

Input:

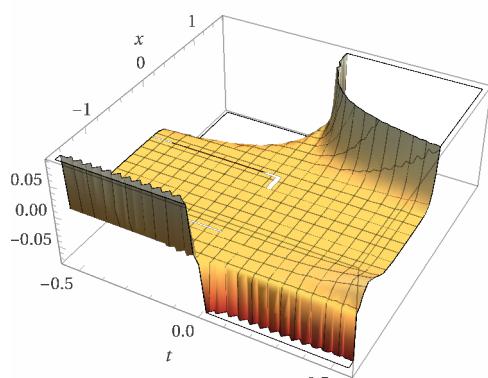
$$\frac{((d^2 \times \frac{x}{d^2} t) \sin(x) + (d^2 \times \frac{\pi^x}{d^2} t) \tan(x))^3}{\sqrt[3]{d^2 \times \frac{\sqrt[3]{x}}{d^2} t + (d^2 \times \frac{\sqrt{x}}{d^2} t) \sin(x)}}$$

Result:

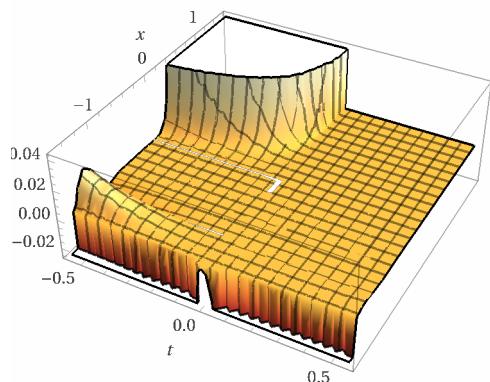
$$\frac{(t x \sin(x) + t \pi^x \tan(x))^3}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}}$$

3D plots:

Real part:

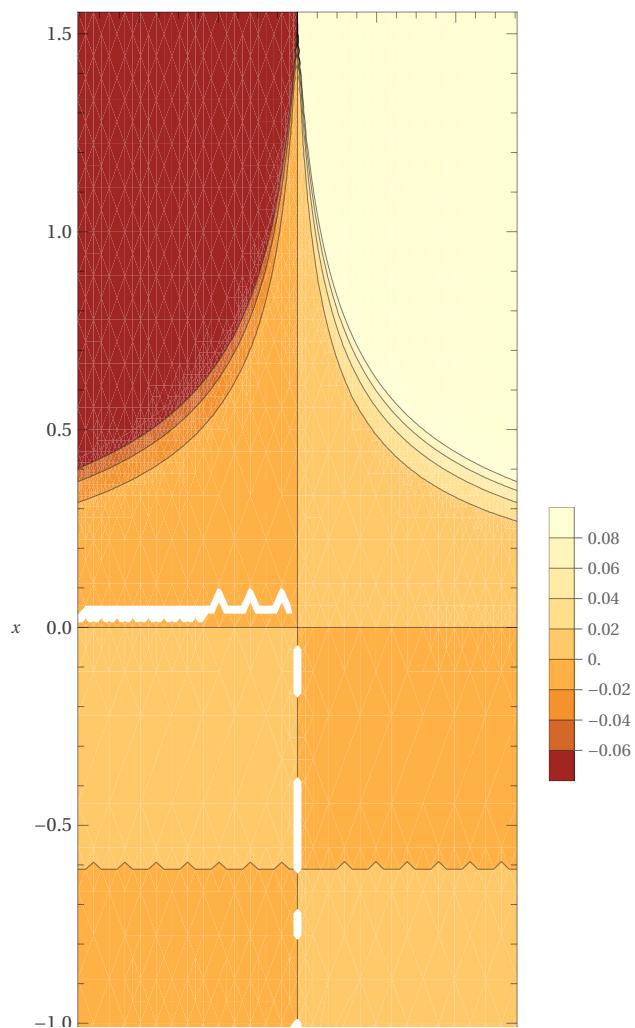


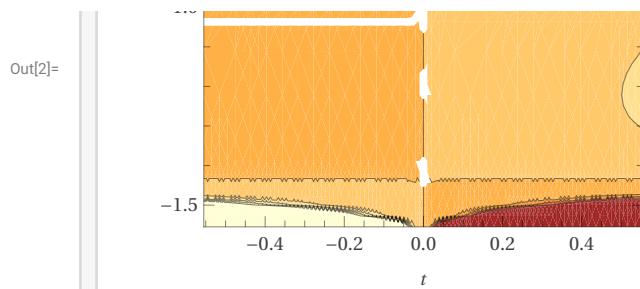
Imaginary part:



Contour plots:

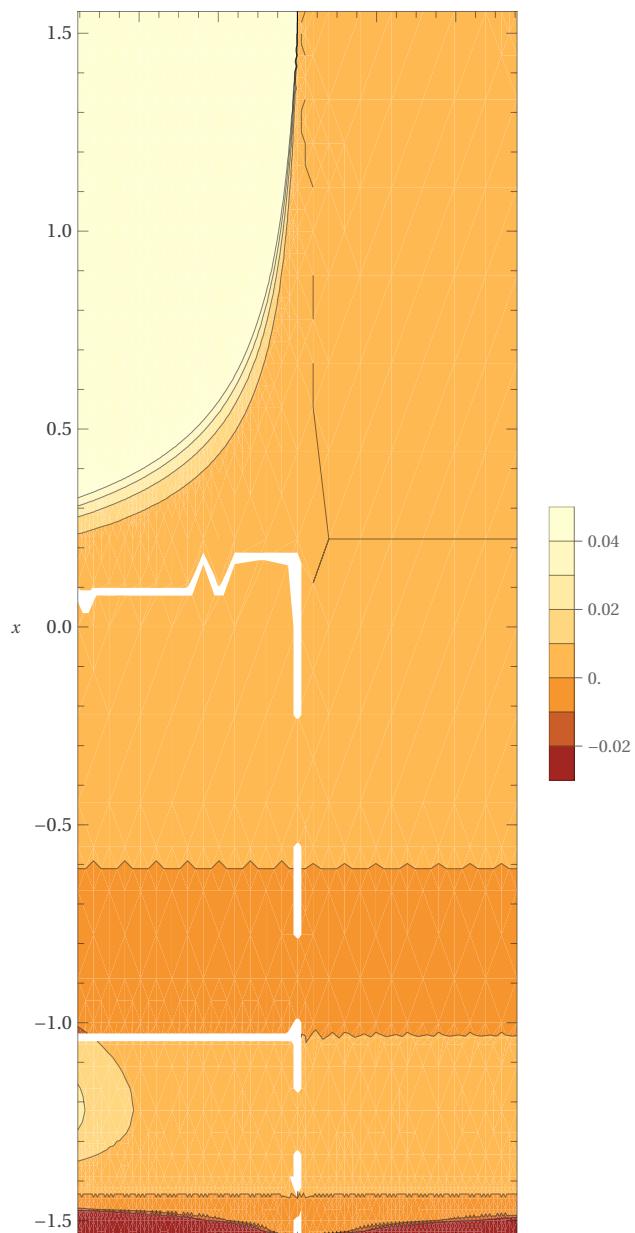
Real part:

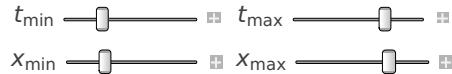
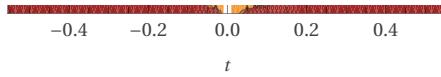




t_{\min} t_{\max}
 x_{\min} x_{\max}

Imaginary part:





Alternate forms:

More +

$$\frac{t^3 (\pi^x + x \cos(x))^3 \tan^3(x)}{\sqrt[3]{t (\sqrt[3]{x} + \sqrt{x} \sin(x))}}$$

$$\frac{t^3 (x \sin(x) + \pi^x \tan(x))^3}{\sqrt[3]{t \sqrt[3]{x} (\sqrt[6]{x} \sin(x) + 1)}}$$

$$\frac{\left(t x \sin(x) + \frac{\pi^x t \sin(x)}{\cos(x)} \right)^3}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}}$$

Expanded form:

+

$$\frac{t^3 x^3 \sin^3(x)}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}} + \frac{3 t^3 \pi^x x^2 \sin^2(x) \tan(x)}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}} +$$

$$\frac{t^3 \pi^{3x} \tan^3(x)}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}} + \frac{3 t^3 \pi^{2x} x \sin(x) \tan^2(x)}{\sqrt[3]{t \sqrt[3]{x} + t \sqrt{x} \sin(x)}}$$

WolframAlpha +

█ $[\{d^2 x/d^2 t\} \sin x * \{d^2 \pi^x x/d^2 t\} \tan x] / [\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]$ Eq 25

In[3]:= $((d^2 x/d^2 t) * \sin x * (d^2 \pi^x x/d^2 t) * \tan x) / ((d^2 x^{1/3}/d^2 t) * (d^2 \sqrt{x}/d^2 t) * \sin x)$

Out[3]= $\pi^x \sqrt[6]{x} \tan(x)$

█ $[\{d^2 x/d^2 t\} \sin x * \{d^2 \pi^x x/d^2 t\} \tan x] / [\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]$

█ $[\{d^2 x/d^2 t\} \sin x * \{d^2 \pi^x x/d^2 t\} \tan x] / [\{d^2 x^{1/3}/d^2 t\} * \{d^2 \sqrt{x}/d^2 t\} \sin x]$

Input:

+

$$\left(d^2 \times \frac{x}{d^2} t\right) \sin(x) \left(d^2 \times \frac{\pi^x}{d^2} t\right) \tan(x)$$

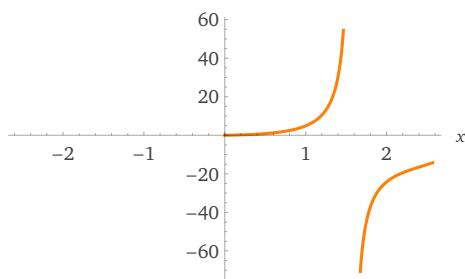
$$\frac{\left(d^2 \times \frac{\sqrt[6]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt[6]{x}}{d^2} t\right) \sin(x)}{\left(d^2 \times \frac{\sqrt[6]{x}}{d^2} t\right) \left(d^2 \times \frac{\sqrt[6]{x}}{d^2} t\right) \sin(x)}$$

Result:

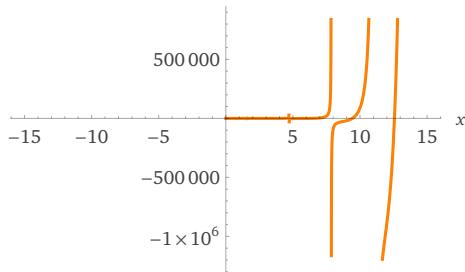
$$\pi^x \sqrt[6]{x} \tan(x)$$

Plots:

Real-valued plots | +



min — max —



min — max —

Alternate forms:

$$\frac{\pi^x \sqrt[6]{x} \sin(x)}{\cos(x)}$$

$$\frac{i(e^{-ix} - e^{ix}) \pi^x \sqrt[6]{x}}{e^{-ix} + e^{ix}}$$

Roots:

Out[5]=

(no roots exist)

Step-by-step solution +

Series expansion at x = 0:

$$x^{7/6} + x^{13/6} \log(\pi) + \frac{1}{6} x^{19/6} (2 + 3 \log^2(\pi)) + \frac{1}{6} x^{25/6} \log(\pi) (2 + \log^2(\pi)) + O(x^{31/6})$$

(Puiseux series)

[log\(x\) is the natural logarithm »](#)[Big-O notation »](#)

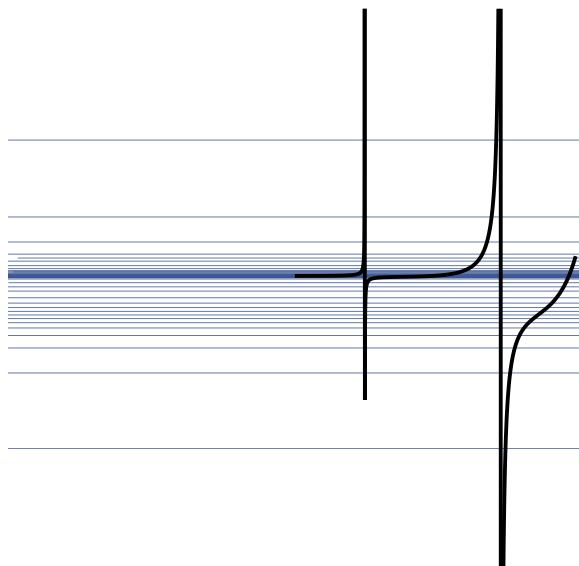
Derivative:

[Approximate form](#)[Step-by-step solution](#)

$$\frac{d}{dx} \left(\frac{(d^2 x t) \sin(x) (d^2 \pi^x t) \tan(x)}{\frac{(d^2 d^2)((d^2 \sqrt[3]{x} t)(d^2 \sqrt{x} t) \sin(x))}{d^2 d^2}} \right) = \frac{\pi^x (\tan(x) + 6 x \sec^2(x) + 6 x \log(\pi) \tan(x))}{6 x^{5/6}}$$

[sec\(x\) is the secant function »](#)

Differential geometric curves:

 $\pi^x \sqrt[3]{x} \tan(x)$

normals

Horizontal plot range:

 x_{\min}  x_{\max} 

symmetric

[More controls](#)

WolframAlpha

In[4]:= $\text{Plot}[\pi^x x^{1/6} \text{Tan}[x], \{x, -15.4248, 15.4248\}]$

