

Estimation of BDS-3 Differential Code Biases with Satellite Antenna PCO Corrections Applied

Ningbo Wang^{*1}, Yang LI¹, Zishen LI¹, Liang WANG¹, and Zongyi LI¹

¹ Aerospace Information Research Institute (AIR), Chinese Academy of Sciences (CAS)

*E-mail: wangningbo@aoe.ac.cn

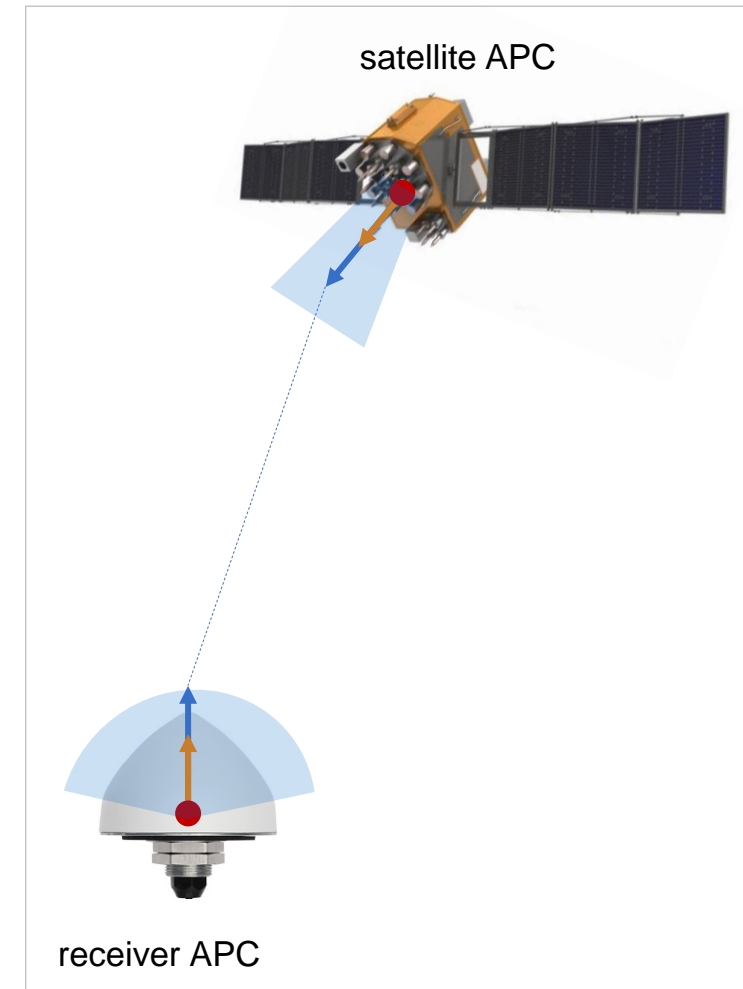
- ▶ PCO corrections in DCB estimation
- ▶ Estimated BDS-3 DCBs with/without modeled PCOs
- ▶ Effects of estimated DCBs on stand/precise positioning
- ▶ Summary and conclusions

Satellite APC corrections in DCB estimation

- ▶ z-PCO mapping on LOS: 0.97-1.0
- ▶ Z-PCO differences up to several decimeters
- ▶ satellite antenna PCOs **requires to be modelled/corrected**
- ▶ satellite phase center variations (PCV) can be ignored

Receiver APC corrections in DCB estimation

- ▶ z-PCO mapping on LOS: 0.0-1.0
- ▶ Z-PCO differences limited to several centimeter
- ▶ receiver PCO/PCV can be ignored in DCB estimation



APC: Antenna Phase Center

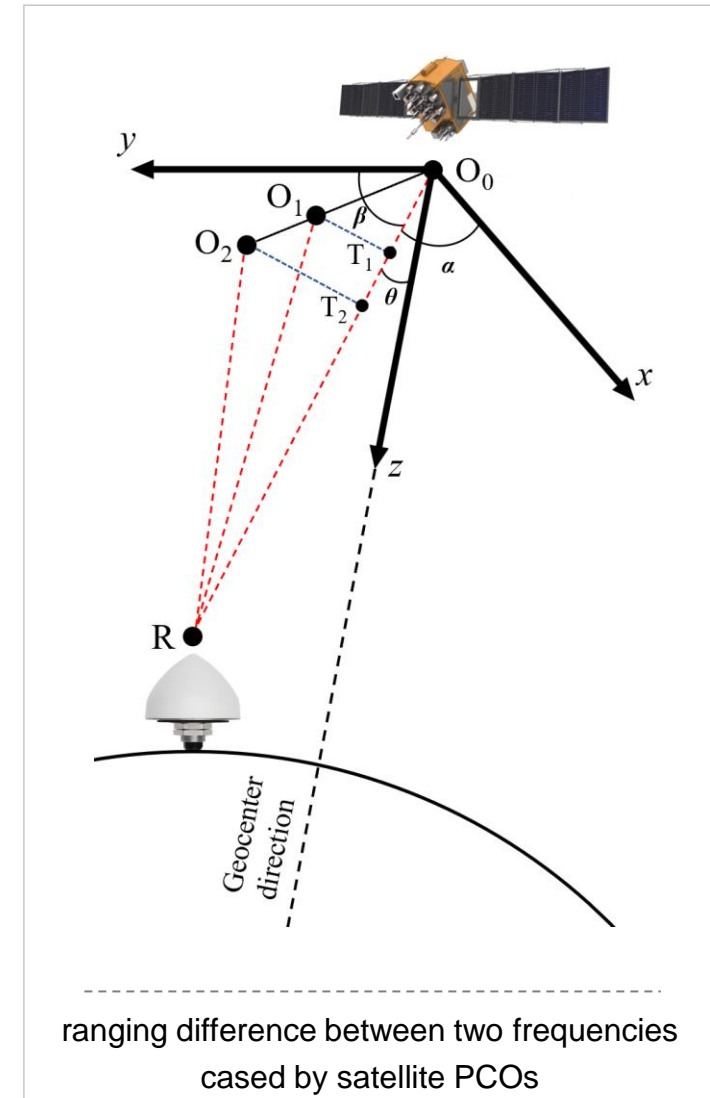
DCB estimation with satellite PCO modeled/corrected

$$\begin{aligned} \Delta PCO_{f_1-f_2}^{sat} &= PCO_{f_1}^{sat} - PCO_{f_2}^{sat} \approx \left| \overrightarrow{T_1 T_2} \right| \\ &= \cos \alpha \cdot (PCO_{x,f_1} - PCO_{x,f_2}) + \cos \beta \cdot (PCO_{y,f_1} - PCO_{y,f_2}) \\ &\quad + \cos \theta \cdot (PCO_{z,f_1} - PCO_{z,f_2}) \\ &= \cos \theta \cdot (PCO_{z,f_1} - PCO_{z,f_2}) \end{aligned}$$

↓
nearly zero

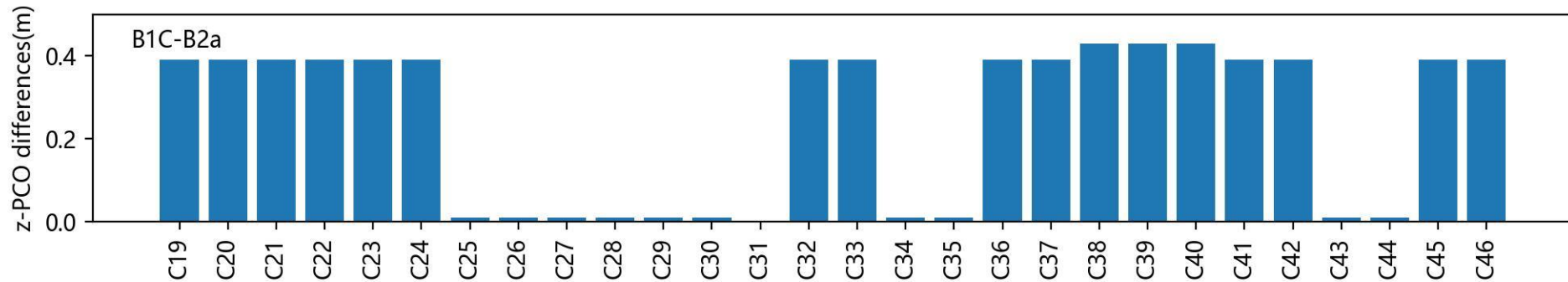
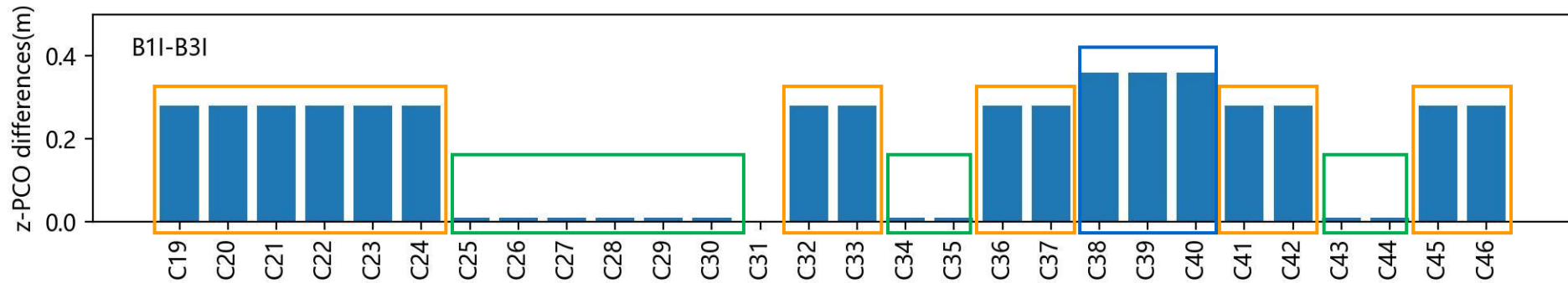
- ▶ The LOS distance is notably larger than satellite PCOs
- ▶ **xy-PCO** difference ~0.0
- ▶ **z-PCO** difference considered (smallest for Galileo, largest for QZSS)

CAST_C19	x-PCO	y-PCO	z-PCO	SECM_C25	x-PCO	y-PCO	z-PCO
B1I	-200.0	0.0	1460.0	B1I	40.0	-10.0	1100.0
B3I	-200.0	0.0	1180.0	B3I	40.0	-10.0	1090.0



DCB estimation with satellite PCO modeled/corrected

- ▶ BDS-3 z-PCO differences of B1I-B3I and B1C-B2a GF combinations (from igs14_2196.atx)



 CASC_MEO
 CASC_IGSO
 SECM_MEO

CASC: China Academy of Space Technology
 SECM: Shanghai Engineering Center for Microsatellites, CAS

DCB estimation with satellite PCO modeled (PCO-modeled DCB¹)

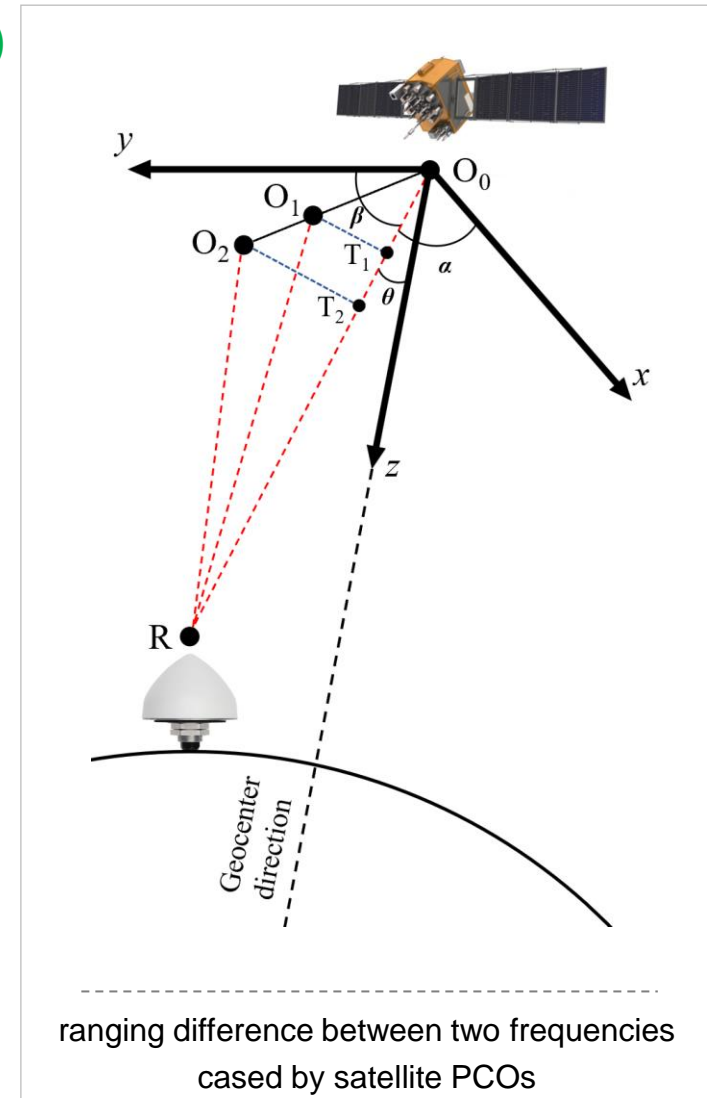
$$P_4 = (I_{f_1} - I_{f_2}) + (B_{f_1} - B_{f_2}) + (\varepsilon_{f_1} - \varepsilon_{f_2}) + (PCO_{f_1}^{sat} - PCO_{f_2}^{sat})$$

$$\approx 40.3 \cdot \left(\frac{1}{f_1^2} - \frac{1}{f_2^2} \right) \cdot sTEC + DCB_{f_1-f_2}^{sat+rec} + \Delta PCO_{f_1-f_2}^{sat}$$

$$\Delta PCO_{f_1-f_2}^{sat} \approx \left| \overrightarrow{T_1 T_2} \right|$$

- ▶ forming GF combination with satellite PCO modeled.
- ▶ using a local ionospheric VTEC modeling method for the jointly estimation of ionospheric and satellite-plus-receiver DCB parameters.
- ▶ applying a zero-constellation-mean constraint for the generation of satellite- and receiver-specific DCBs.

(Wang et al. JoGE, 2016, 2020)



DCB estimation with satellite PCO modeled (PCO-modeled DCB¹)

- ▶ CASDCB method for jointly local ionosphere and bias estimation

$$\begin{cases} P_{r,4}^{*,s} = c \cdot \mathbf{SPR}_r^s + 40.3 \cdot (f_2^2 - f_1^2) \cdot \mathbf{STEC}_r^s / f_1^2 f_2^2 \\ P_{r,4}^{*,s} = P_{r,4}^s - \cos \theta \cdot \Delta \mathbf{PCO}_z, \quad \cos \theta \in [0.97, 1.00] \\ \mathbf{SPR}_r^s = b_{r,4} - b_4^s \end{cases}$$

VTEC model $\mathbf{VTEC}_r^s(\varphi_d, \lambda_d, h) = \sum_{n=0}^{n_{\max}} \sum_{m=0}^{m_{\max}} \{E_{nm} \cdot \varphi_d^n \cdot \lambda_d^m\}$

$+ \sum_{k=0}^{k_{\max}} \{C_k \cos(k \cdot h) + S_k \sin(k \cdot h)\}$

satellite- and receiver-specific DCBs

$\hat{\mathbf{X}}_{dcb} = (\mathbf{F}^T \mathbf{F} + \mathbf{H}^T \mathbf{H})^{-1} \mathbf{F}^T \mathbf{Z}_{\mathbf{SPR}}$

$\Delta \mathbf{PCO}$ absorbed in the estimated DCBs

$$\Delta \mathbf{DCB}_{pco} = (\mathbf{F}^T \mathbf{F} + \mathbf{H}^T \mathbf{H})^{-1} \mathbf{F}^T \cdot \Delta \mathbf{PCO}_z$$

(Wang et al. JoGE, 2016, 2020)

DCB estimation with satellite PCO corrected (PCO-corrected DCB²)

- ▶ ignoring the time-varying z-PCO ($\cos\theta=1$)

$$DCB_{f_1-f_2}^{*,sat} = DCB_{f_1-f_2}^{sat} - \Delta DCB_{pco,f_1-f_2}^{sat} \quad (\text{Eq. 1})$$

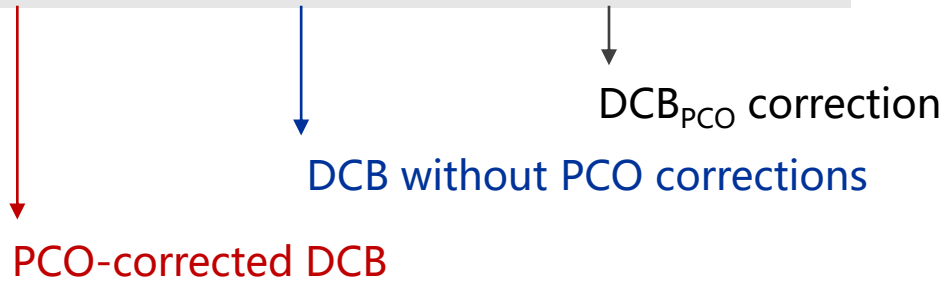
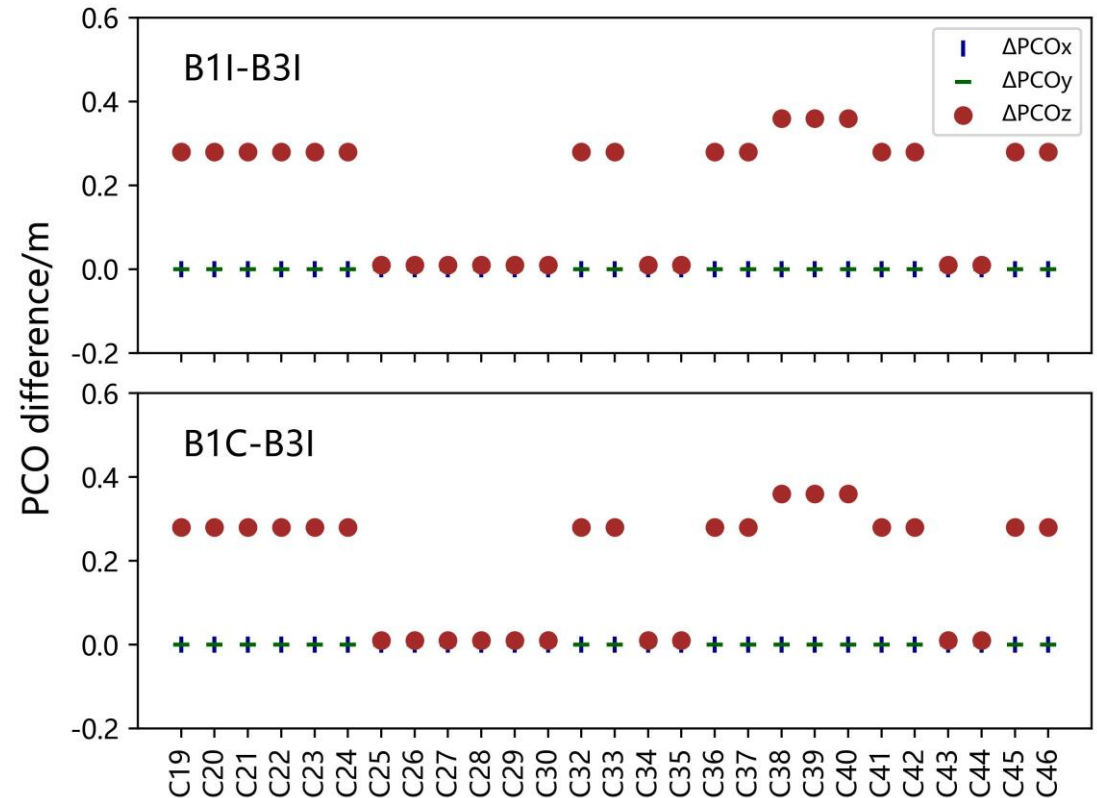


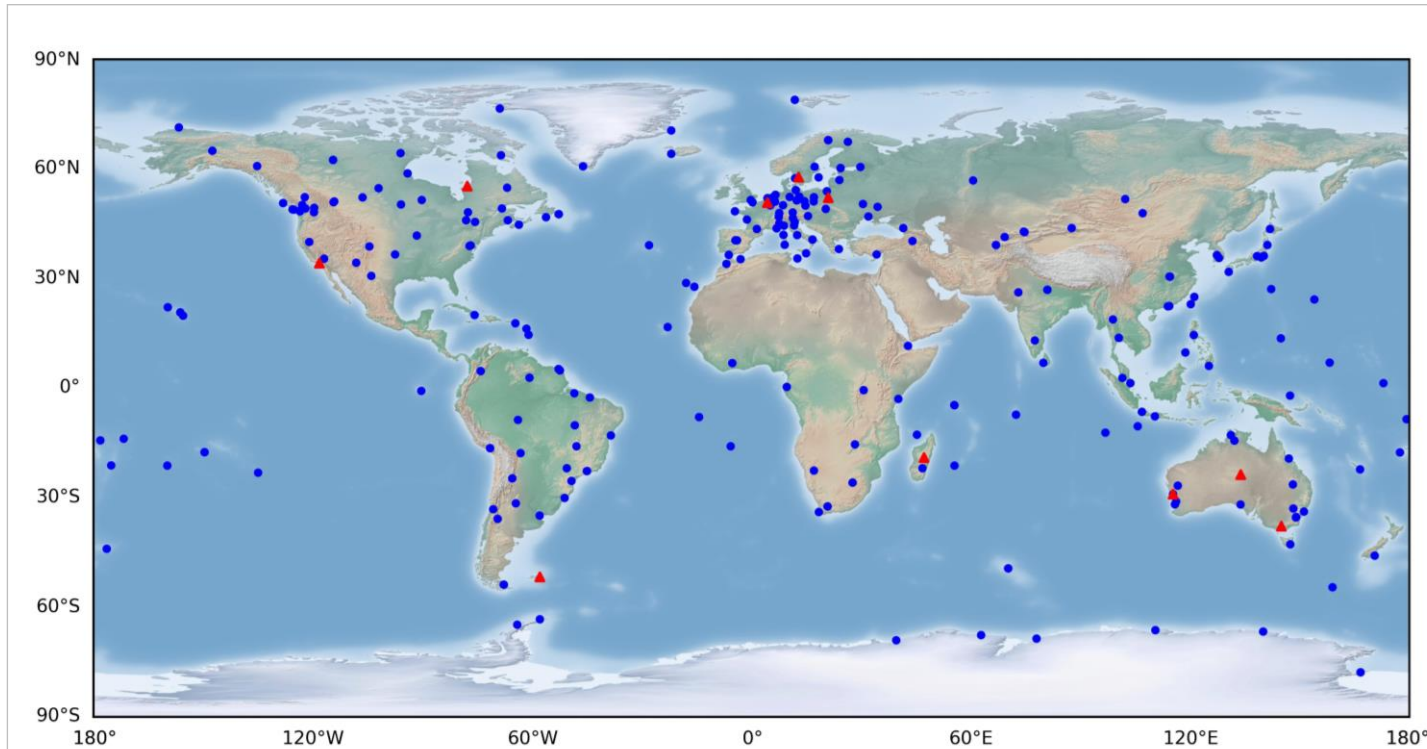
Table 1 theoretical PCO corrections for B1I/B1C-B3I DCBs

Satellite type	ΔDCB_{PCO} (ns)
CASC_MEO	-0.304
CASC_IGSO	-0.571
SECM_MEO	0.597



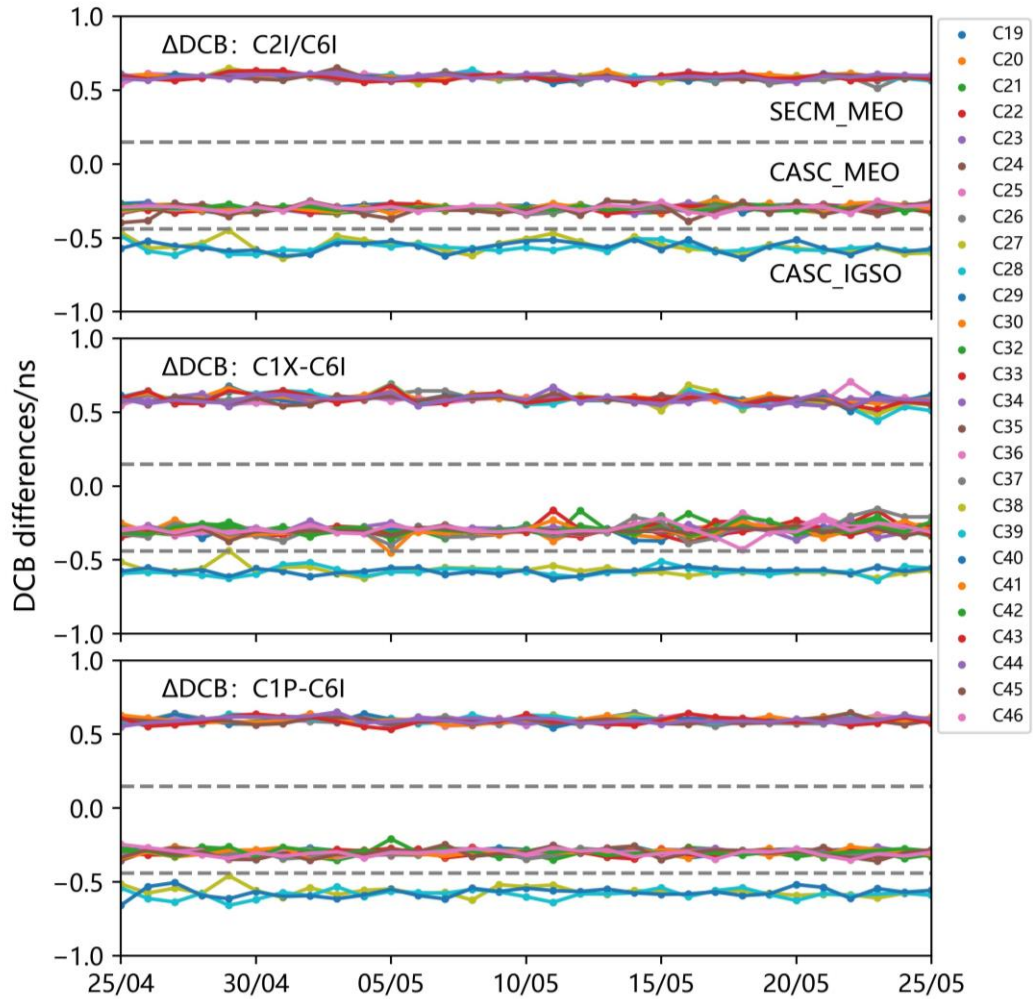
PCO differences for BDS-3 B1I-B3I and B1C-B3I GF combination (from igs14_2196.atx)

DCB estimation using IGS-MGEX observation data



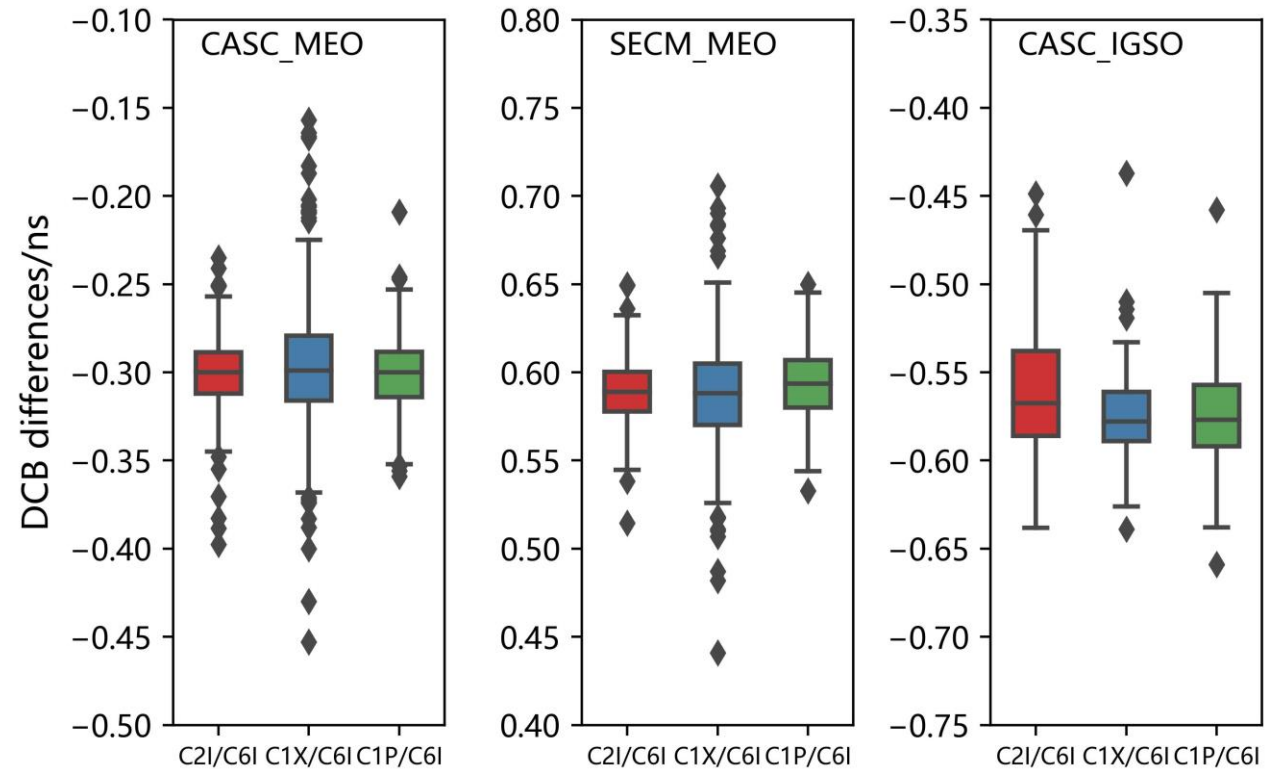
blue circles for DCB estimation with/without PCO corrections
red triangles for DCB validation in positioning

DCB	Station number	
	25/04	25/05
C2I-C6I	174	193
C1P-C6I	83	97
C1X-C6I	51	51

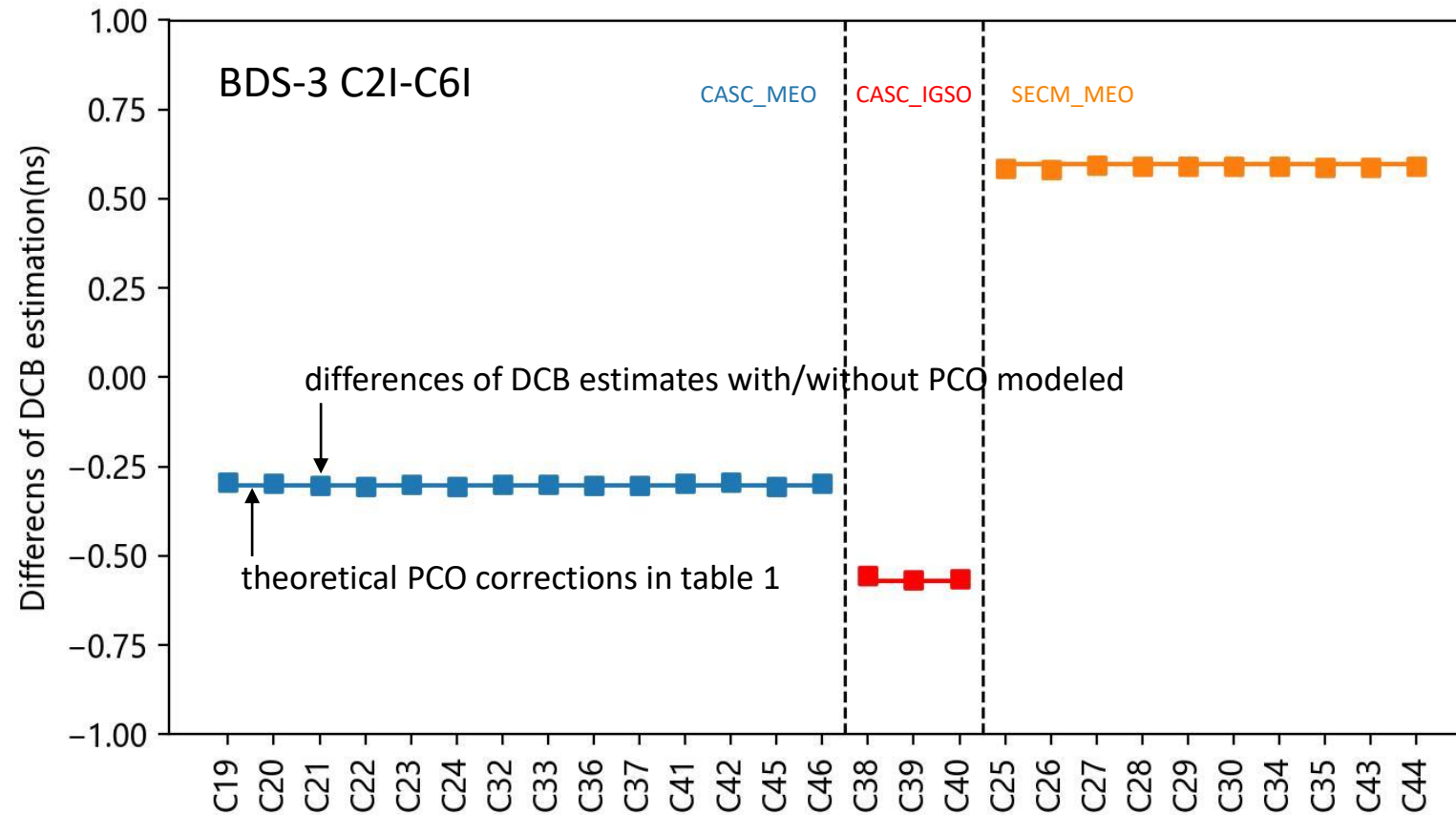


STD of DCB difference series: 0.02-0.04 ns

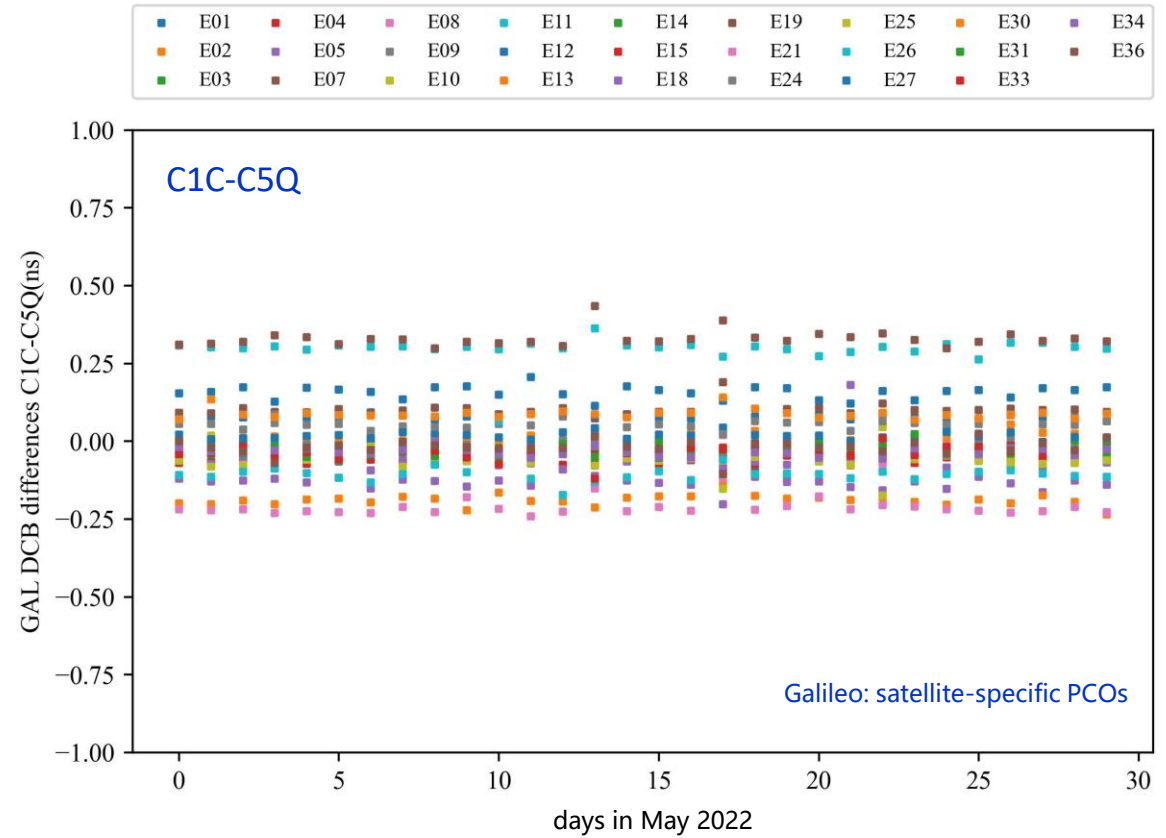
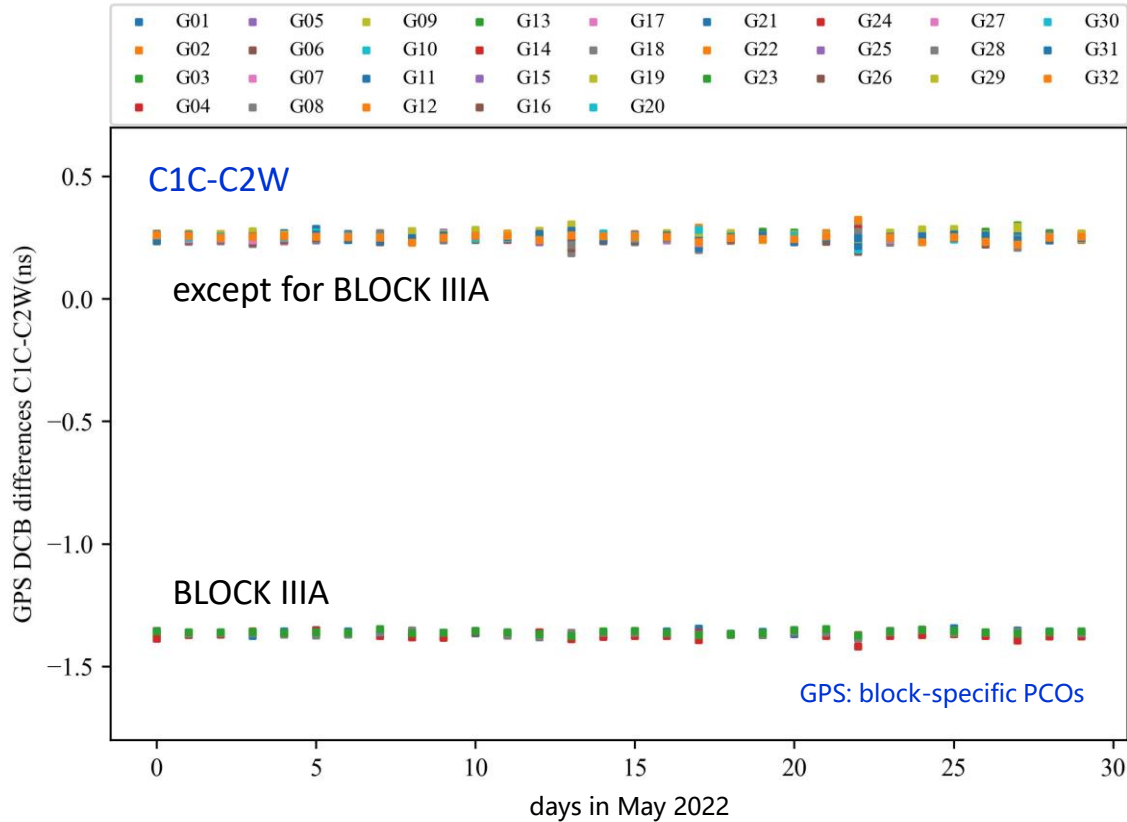
Compared to theoretical PCO corrections in Table 1
mean difference is within the range of 0.003-0.01 ns



Differences of estimated DCBs with/without PCO modeled (May 2022)



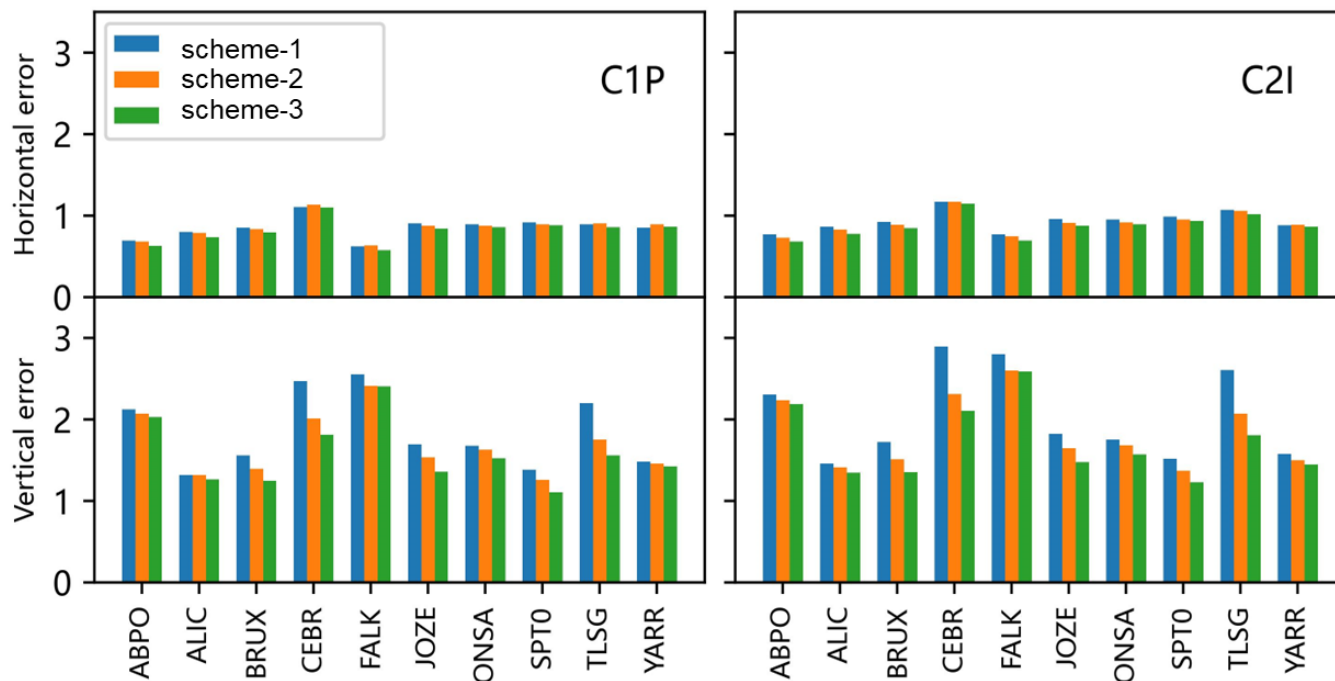
Differences of estimated GPS/GAL DCBs with/without PCO modeled (May 2022)



items	DCB/OSB without modeled PCOs	DCB/OSB with modeled PCOs
DCB file name	CAS0MGXRAP_yyyyddd0000_01D_01D_DCB.BSX	CAS1MGXRAP_yyyyddd0000_01D_01D_DCB.BSX
OSB file name	CAS0MGXRAP_yyyyddd0000_01D_01D_OSB.BIA	CAS1MGXRAP_yyyyddd0000_01D_01D_OSB.BIA
Satellite orbits	IGS combined broadcast ephemeris data	GBM rapid products
BDS-2 GDV model	Not applied	Not applied
Time latency	2 days	4 days
Data coverage	2013-now	August/2022-Now (January/2022)
Data archive	CAS/IGN/CDDIS	CAS (ftp.gipp.org.cn/product/dcb/mgex/yyyy/)

BDS-3 C1P/C2I “precise” single-frequency positioning (GFZ rapid orbits and clocks)

- ▶ **scheme-1**: estimated DCBs without PCO correction applied (i.e. CAS MGEX DCBs)
- ▶ **scheme-2**: PCO-corrected DCBs² following Eq. (1)
- ▶ **scheme-3**: PCO-modeled DCBs¹

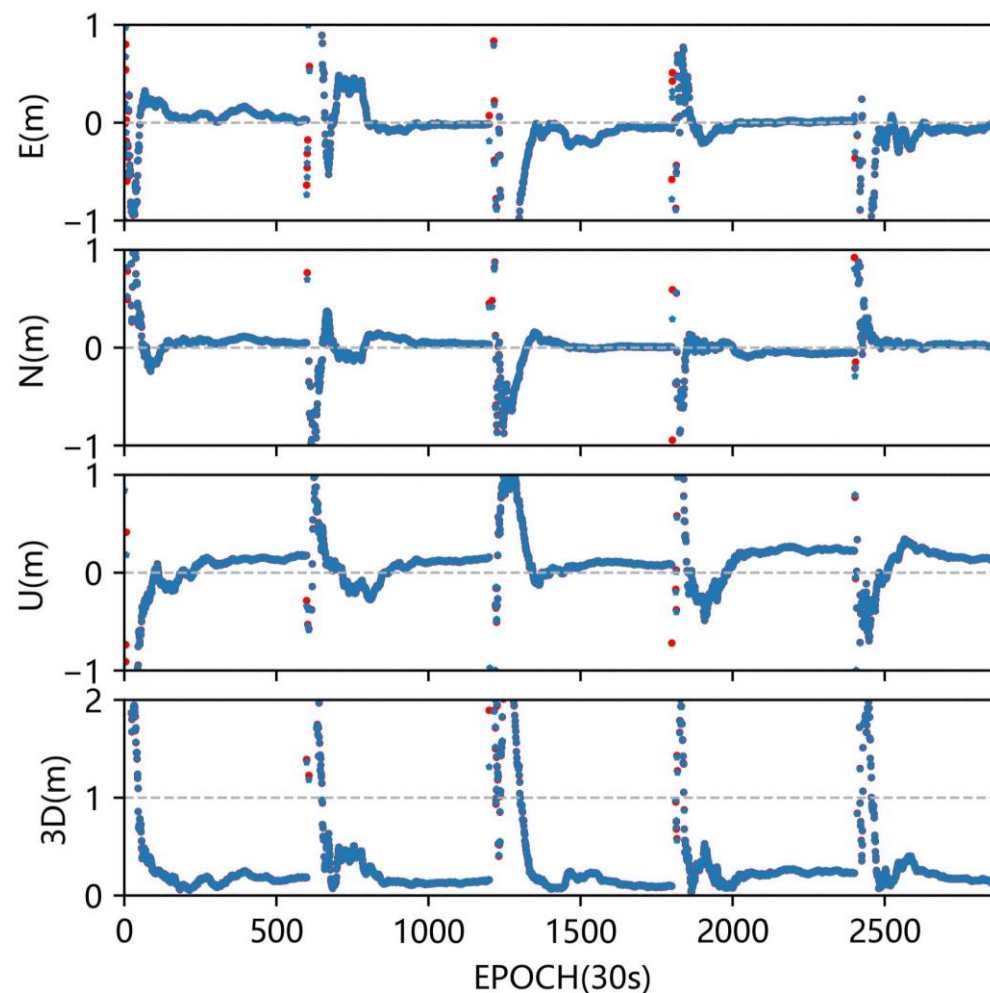


positioning improvement compared to scheme-1 (S-1, 95% percentile)

		C1P	C2I
S-2	H_95%	0.2%	3.0%
	V_95%	8.0%	9.5%
S-3	H_95%	4.8%	6.8%
	V_95%	14.2%	15.6%

BDS-3 B1I single-frequency PPP (GFZ rapid orbits and clocks)

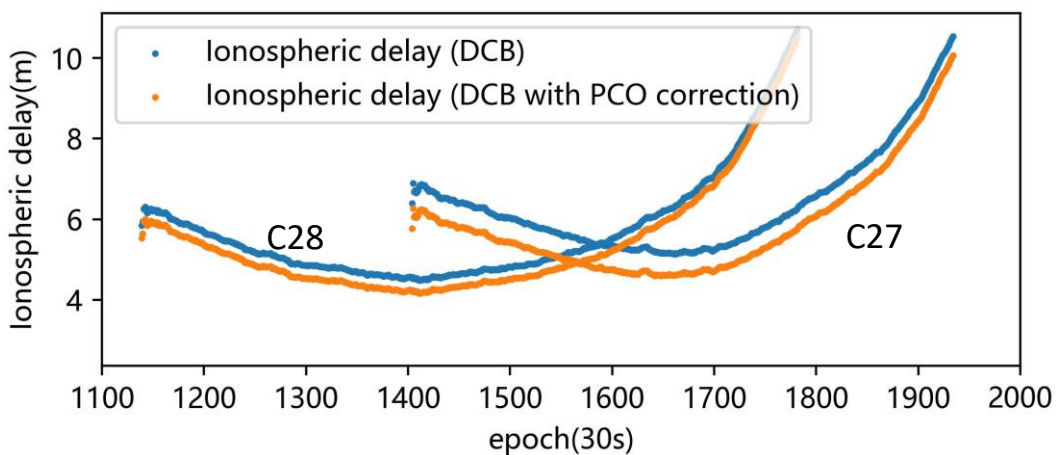
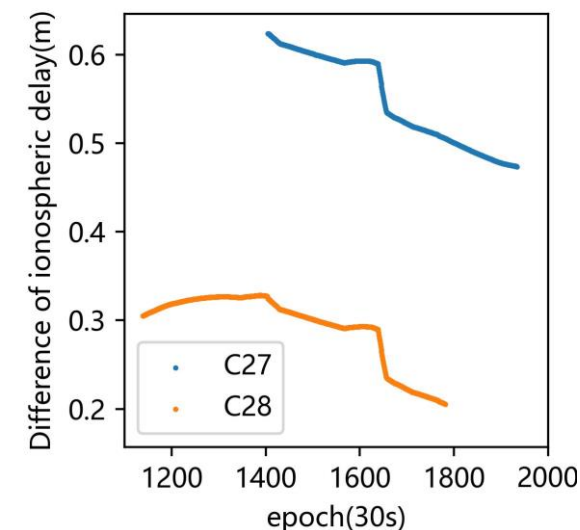
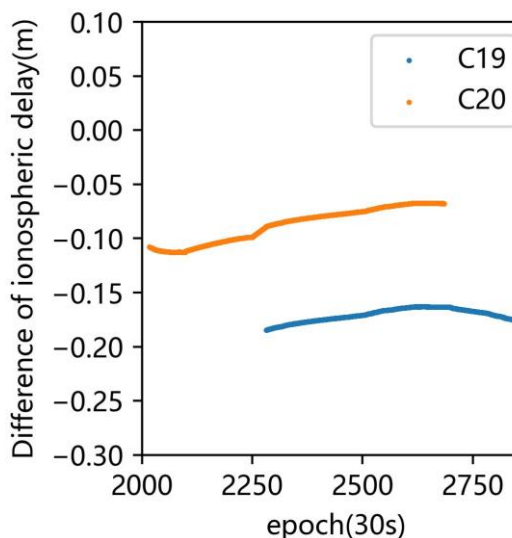
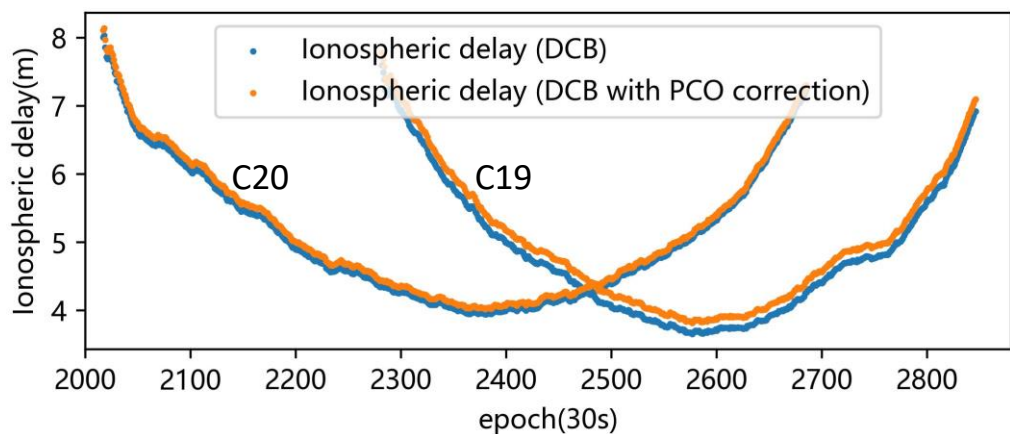
station : FFMJ
year : 2022
doy : 220
signal : BDS-3 B1I



- ▶ For SF-PPP, **positioning parameters not affected** by PCO errors in DCBs (i.e., ΔDCB_{pco})
- ▶ Such errors absorbed in receiver clock (common part), ambiguity and **ionosphere parameters** (satellite-specific part)

- DCB estimates without modeled PCOs
- DCB estimates with modeled PCOs

BDS-3 B1I single-frequency PPP (GFZ rapid orbits and clocks)



selected satellites	mean difference(m)
C19 (CASC_MEO)	-0.169
C20 (CASC_MEO)	-0.087
C27 (SECM_MEO)	0.532
C28 (SECM_MEO)	0.263

- ▶ Effects of satellite PCOs on the estimated DCBs were analyzed for BDS, GPS and Galileo (PCO-modeled DCBs vs. PCO-corrected DCBs).
- ▶ The analysis of BDS-3 B1I/B1C-B3I DCB estimates with/without modeled PCOs proves the consistent modeling of PCOs in the estimated DCBs.
- ▶ BDS-3 C1P/C2I “precise” standard positioning further verifies the good consistency between the estimated DCBs with modeled PCOs and precise orbit/clock products.
- ▶ When extracting ionosphere information from SF-PPP, the largest difference caused by DCBs with/without modeled PCOs reaches ~0.5 m (from BDS-3 B1I SF-PPP analysis) .
- ▶ Multi-GNSS DCB/OSB products with modeled PCOs are publicly accessible from CAS ftp site (data coverage: August/2022-now, <ftp://ftp.gipp.org.cn/product/dcb/mgex/yyyy/>)