

Normalized Voigt-Notation = Mandel notation

$$B_i \cdot B_j = \delta_{ij} \quad \text{with } i, j \in [1, 2, 3, 4, 5, 6]$$

with respect to orthonormal base system $e_m, m \in [1, 2, 3]$ in \mathbb{R}^3

$$B_1 = e_1 \otimes e_1$$

$$B_4 = \frac{\sqrt{2}}{2} (e_1 \otimes e_3 + e_3 \otimes e_1)$$

$$B_2 = e_2 \otimes e_1$$

$$B_5 = \frac{\sqrt{2}}{2} (e_1 \otimes e_2 + e_2 \otimes e_1)$$

$$B_3 = e_3 \otimes e_1$$

$$B_6 = \frac{\sqrt{2}}{2} (e_1 \otimes e_2 - e_2 \otimes e_1)$$

and

$$\sigma_i = \sigma \cdot B_i$$

$$\sigma = \begin{pmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ & \sigma_{22} & \sigma_{23} \\ \text{sym} & & \sigma_{33} \end{pmatrix} e_m \otimes e_n \quad m, n \in [1, 2, 3]$$

$$C_{ij} = C \cdot (B_i \otimes B_j)$$

back

$$= \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sqrt{2} \sigma_{23} \\ \sqrt{2} \sigma_{13} \\ \sqrt{2} \sigma_{12} \end{bmatrix} B_i \quad i \in [1, \dots, 6]$$

\Rightarrow Reduce required storage from 3×3 to 6 for Tensor 2 order

$$\Rightarrow EW(C_{\text{tensor}}) = EW(\sigma_{\text{matrix}})$$

$$\Rightarrow \sigma = C \cdot \epsilon$$

e.g. isotropic:

$$\sigma = 2\mu \epsilon + \lambda \text{sp}(\epsilon) \mathbb{1}$$

$$a = \text{sp}(\epsilon) = \epsilon_{11} + \epsilon_{22} + \epsilon_{33}$$

$$\begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sqrt{2} \sigma_{23} \\ \sqrt{2} \sigma_{13} \\ \sqrt{2} \sigma_{12} \end{bmatrix} = \begin{bmatrix} 2\mu \epsilon_{11} + a \lambda \\ 2\mu \epsilon_{22} + a \lambda \\ 2\mu \epsilon_{33} + a \lambda \\ 2\mu \sqrt{2} \epsilon_{23} \\ 2\mu \sqrt{2} \epsilon_{13} \\ 2\mu \sqrt{2} \epsilon_{12} \end{bmatrix}$$

Attention: If $\Gamma(\epsilon)$ is given as formula for tensorial σ ,

scale components 4, 5 and 6 of $\epsilon = [\epsilon_{11}, \epsilon_{12}, \epsilon_{13}, \sqrt{2} \epsilon_{23}, \sqrt{2} \epsilon_{13}, \sqrt{2} \epsilon_{12}]$

by $\frac{1}{\sqrt{2}}$ before calculation