



For more details and formulas see[2]. In this paper, we present an interesting sequence which play the same role of Rowland sequence composite by a prime number or 1.

## 2. The sequence of $b(n)$ and $a(n)$

The sequence  $b(n)$  satisfy the following recursive formula

$$b(n) = (n - 1)b(n - 1) - nb(n - 2); n \geq 4$$

With the starting conditions  $b(2) = -1$ , and  $b(3) = 1$ .

The first few values of  $b(n)$ .

$b(n) = \{-1, 1, 7, 23, 73, 277, 1355, 8347, 61573, 523913, 5024167, 53479135, 624890417, 7946278813, \dots\}$

Other formula of  $b(n)$  as continued fraction

$$\frac{b(n)}{n^2 - n - 1} = \frac{1}{2 - \frac{3}{3 - \frac{4}{4 - \frac{5}{\dots \frac{n}{(n-1) - \frac{n}{n-(n+1)}}}}}}}; \text{ for } n \geq 2$$

In this section, we present our sequence of prime numbers defined in the conjecture as follows.

**Conjecture .** The sequence  $a(n)$  satisfy the following formula

$$a(n) = \frac{n^2 - n - 1}{\gcd(b(n), n^2 - n - 1)} ; \text{ for } n \geq 2$$

Where  $\gcd(x, y)$  denotes the greatest common divisor of  $x$  and  $y$ .

The values of  $a(n)$ .

1, 5, 11, 19, 29, 41, 11, 71, 89, 109, 131, 31, 181, 19, 239, 271, 61, 31, 379, 419, 461, 101, 29, 599, 59, 701, 151, 811, 79, 929, 991, 211, 59, 41, 1259, 1, 281, 1481, 1559, 149, 1721, 1, 61, 1979, 2069, 2161, 1, 2351, 79, 2549, 241, 1, 2861, 2969, 3079, 3191,...

Every term of this sequence is either a prime number or equal to 1.

## References

- [1] Richard Guy, Unsolved Problems in Number Theory, Springer science (2004).
- [2] Eric S. Rowland, A Natural Prime-Generating Recurrence, Journal of Integer Sequences, Vol. 11 (2008).
- [3] N. J. A. Sloane et al., The On-line Encyclopedia of integers sequences, <https://oeis.org> (Concerned with the sequence A132199)