

Integrating singular spectrum analysis and nonlinear autoregressive neural network for stock price forecasting

Asmaa Y. Fathi¹, Ihab A. El-Khodary¹, Muhammad Saafan²

¹Department of Operations Research and Decision Support, Faculty of Computers and Information, Cairo University, Giza, Egypt

²Department of Petroleum Engineering, Universiti Teknologi PETRONAS, Seri Iskandar, Malaysia

Article Info

Article history:

Received Sep 11, 2021

Revised Mar 10, 2022

Accepted Apr 6, 2022

Keywords:

Data preprocessing

Nonlinear autoregressive neural network

Singular spectrum analysis

Stock market

Stock price prediction

ABSTRACT

The main objective of stock market investors is to maximize their gains. As a result, stock price forecasting has not lost interest in recent decades. Nevertheless, stock prices are influenced by news, rumor, and various economic factors. Moreover, the characteristics of specific stock markets can differ significantly between countries and regions, based on size, liquidity, and regulations. Accordingly, it is difficult to predict stock prices that are volatile and noisy. This paper presents a hybrid model combining singular spectrum analysis (SSA) and nonlinear autoregressive neural network (NARNN) to forecast close prices of stocks. The model starts by applying the SSA to decompose the price series into various components. Each component is then used to train a NARNN for future price forecasting. In comparison to the autoregressive integrated moving average (ARIMA) and NARNN models, the SSA-NARNN model performs better, demonstrating the effectiveness of SSA in extracting hidden information and reducing the noise of price series.

This is an open access article under the [CC BY-SA](https://creativecommons.org/licenses/by-sa/4.0/) license.



Corresponding Author:

Asmaa Y. Fathi

Department of Operations Research and Decision Support, Faculty of Computers and Information, Cairo University

12613 Orman, Giza, Egypt

Email: a.fathi@fci-cu.edu.eg

1. INTRODUCTION

A stock exchange is a legitimate organization that provides chances for investing in firms by purchasing or selling their listed shares [1]. The stock market functions similar to other economic markets, i.e., buyers aim to pay the lowest possible price for the stock, while sellers aim for higher prices. Investing in stock markets yields considerable gains, making it more appealing than low-yielding assets such as government bonds. Moreover, the high liquidity present in the stock market allows the investors to transfer the assets into cash quickly [2]. Nevertheless, only a few people engage in stock trading due to the challenges of forecasting stock prices, which increases investment risk.

During the last decade, analytical and computational methods have advanced and given rise to several innovative new approaches to analysis financial-time series based on nonlinear and nonstationary models [3]. Machine learning models have been effectively employed in various sectors, including the stock market. According to the literature, artificial neural network models (ANNs) are the main machine learning method used in forecasting various financial markets [4]–[7]. ANN is a proper tool in forecasting stock prices because it does not imply any prior assumptions and can grasp nonlinear functions regarding the data properties [6]. ANNs are classified as static or dynamic networks. For instance, dynamic neural networks, e.g., the nonlinear autoregressive neural network (NARNN), assess the output utilizing a number of its

preceding inputs. Thus, dynamic networks possess a memory that supports recognizing time-varying characteristics [8]. Unfortunately, the high noise level and interaction between hidden features in the price series decrease the ANNs prediction efficiency [9]–[11]. Therefore, a data preprocessing technique, e.g., singular spectrum analysis or multicomponent amplitude and frequency modulated (AM–FM) models [12]–[15], is needed to improve the prediction accuracy via noise reduction and extracting underlying information hidden in the price series.

The singular spectrum analysis (SSA) has a variety of applications, including signal denoising, trend extraction, and forecasting [16]. Hassani *et al.* [17] employed the SSA to forecast the GBP/USD exchange rates. The authors found that the SSA model performed better than the random walk model. Fenghua *et al.* [18] employed the SSA for decomposing stock prices into a trend, fluctuation, and noise terms. Then, the support vector machine (SVM) is used to predict each term. Afterward, Abdollahzade *et al.* [19] proposed a model integrating the neuro-fuzzy with SSA to predict nonlinear chaotic time series. The authors concluded that the SSA improved the prediction performance due to noise reduction in the original time series. Lahmiri [20] presented a hybrid forecasting that integrates SSA and SVM optimized by particle swarm. The performance of the proposed model was evaluated with intraday stock prices, and results indicated its promise for predicting noisy time series. Later, Xiao *et al.* [21] forecasted the Shanghai composite index using the SSA-SVM model established by [18]. The authors compared the SSA with the empirical mode decomposition and found that the former yields better forecasts. Recently, Sulandari *et al.* [22] integrated the SSA and ANN to forecast time series and found that the SSA-ANN model outperformed the ANN model.

This paper presents a hybrid model combining SSA and NARNN for stock price forecasting. First, the model divides the weekly stock closing prices into training and testing sets. Second, the SSA decomposes the training set into various components to extract hidden features and decrease the noise. Third, a NARNN is constructed and trained for each decomposed component. Forth, the model predicts the future values of various components by decomposing the preceding available prices. Finally, the SSA-NARNN model aggregates the predicted values to obtain the final output. Therefore, these procedures simulate the real trading process and avoid inserting any information regarding the stock future performance in the training process. The suggested model's reliability is demonstrated using the weekly closing prices of twenty-four stocks listed on the Egyptian Exchange. Additionally, the superiority of the SSA-NARNN model is demonstrated by comparison to the autoregressive integrated moving average (ARIMA) and the single NARNN model.

2. RESEARCH METHODS

2.1. Singular spectrum analysis (SSA)

The SSA decomposes signals using singular value decomposition (SVD) and generates singular values containing information regarding the original time series [23]. The SSA approach is divided into two stages, decomposition and reconstruction, each of which consists of two steps [24]. This section outlines the SSA's stages.

2.1.1. Decomposition

The decomposition is performed in two steps: embedding and SVD. Embedding is the first step in which the price series is converted to a lagged trajectory matrix [24]. If $s_t = [s_1, s_2, \dots, s_N]^T$ is a time series of length N , the mapped trajectory matrix, M , is defined as [25], [26]:

$$M = [M_1 \cdot M_2 \cdot \dots \cdot M_K] = \begin{pmatrix} s_1 & s_2 & \dots & s_K \\ s_2 & s_3 & \dots & s_{K+1} \\ \vdots & \vdots & \ddots & \vdots \\ s_L & s_{L+1} & \dots & s_N \end{pmatrix} \quad (1)$$

where L is the embedding dimension and satisfies $2 \leq L \leq N$. M is a Hankel matrix. For instance, a trajectory matrix of a price series, $S_t = [1.90, 1.62, 1.55, 1.60, 1.56, 1.47, 1.51, 1.48, 1.66]$, for $L=5$ is formulated as:

$$M = \begin{pmatrix} 1.90 & 1.62 & 1.55 & 1.60 & 1.56 \\ 1.62 & 1.55 & 1.60 & 1.56 & 1.47 \\ 1.55 & 1.60 & 1.56 & 1.47 & 1.51 \\ 1.60 & 1.56 & 1.47 & 1.51 & 1.48 \\ 1.56 & 1.47 & 1.51 & 1.48 & 1.66 \end{pmatrix}$$

The SVD is used after the embedding step for factorizing the trajectory matrix into biorthogonal elementary matrices [24]. This procedure is denoted by [27]:

$$M = \sum_{r=1}^R M_r = U \Sigma V^T = \sum_{r=1}^R \sigma_r u_r v_r^T \tag{2}$$

where M_r is the r^{th} elementary matrix, U and V are orthonormal system, Σ is a diagonal matrix whose diagonal elements, σ_r , are the singular values of MM^T .

2.1.2. Reconstruction

The second stage of the SSA is reconstruction, which involves projecting the time series onto data-adaptive eigenvectors to decrease the dataset dimensionality and express it in an optimum subspace [28]. The reconstruction stage includes two processes: grouping and diagonal averaging. Grouping is the process of categorizing elementary matrices into groups based on their eigentriples. Then, the matrices within each group are then added together [16], [24]. Let $g = \{i_1, i_2, \dots, i_n\}$ represents a group of n chosen eigentriples; then, the matrix M_g for group g is written:

$$M_g = M_{i_1} + M_{i_2} + \dots + M_{i_r} \tag{3}$$

Splitting of indices set, $r = 1, \dots, R$, into m subsets, g_1, g_2, \dots, g_m , renders the original mapped trajectory matrix as:

$$M = M_{g_1} + M_{g_2} + \dots + M_{g_m} \tag{4}$$

The contribution of a component, M_g , in the trajectory matrix is represented by the ratio of its eigenvalues as $\sum_{i \in g} \lambda_i / \sum_{r=1}^R \lambda_r$.

The second step in the reconstruction process is the diagonal averaging along the N antidiagonal of the matrix M_g , also known as the Hankelization process $H(M_g)$. This process converts the matrix into a time series that is a component of the original series s_t . If $x_{g_{ij}}$ is an element of M_g , then the k^{th} term of the reconstructed time-series is obtained through averaging the elements $x_{g_{ij}}$ that satisfies $i+j=k+1$, where $1 \leq k \leq N$. The reconstructed time-series will have a length N . The application of the diagonal averaging process to all the terms of (4) renders the decomposed components of the original series as:

$$s_t = H(M_{g_1}) + H(M_{g_2}) + \dots + H(M_{g_m}) \tag{5}$$

2.2. Nonlinear autoregressive neural network (NARNN)

The NARNN is a feed-forward dynamic network that forecasts future values of a time series by using its previous d values [29]. Hence, the NARNN utilizes the time series' past behavior to predict its future behavior. Figure 1 illustrates the NARNN's structure utilized in our work. The network includes an input layer with a time delay line (TDL), two hidden layers, and an output layer. The TDL is configured with an eight-week feedback delay, which means that the previous eight closing prices are utilized to forecast the ninth closing price. The first and second hidden layers' activation functions are tan-sigmoid and log-sigmoid, respectively. Additionally, the output layer has a single neuron with linear activation. The levenberg-marquardt backpropagation (LMBP) algorithm is used in the network learning process.

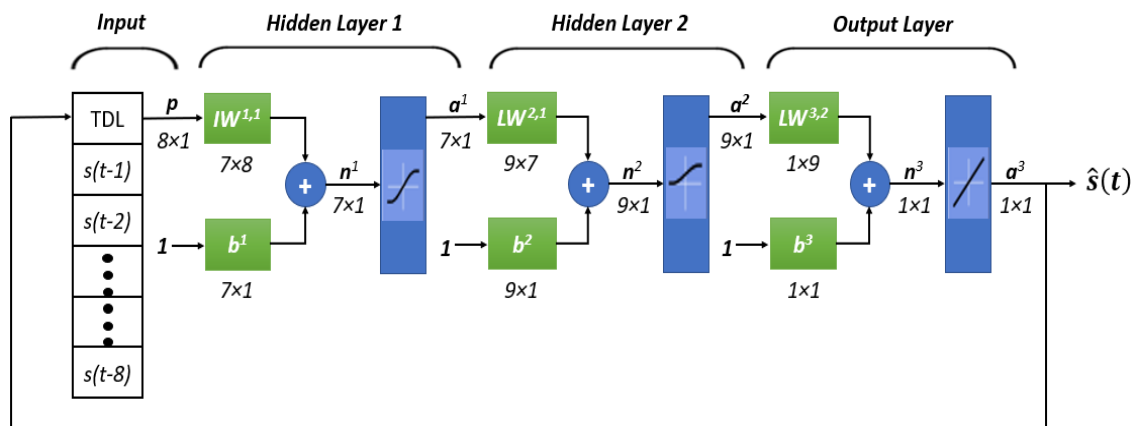


Figure 1. A typical NARNN structure

2.3. The hybrid SSA-NARNN model

The SSA-NARNN model combines the SSA and NARNN models to forecast stock prices. First, the model employs the SSA to decompose the price series into separate components, as discussed in section 2.1. Then, the increment of singular entropy, ΔE represented by (6), is utilized to separate the noise component. When ΔE reaches an asymptotic value, the information in the time series is extracted, and the remaining components represents the noise term.

$$\Delta E = - \left(\frac{\lambda_i}{\sum_{r=1}^p \lambda_r} \right) \log \left(\frac{\lambda_i}{\sum_{r=1}^p \lambda_r} \right) \quad (6)$$

The covariance and standard deviation, σ , of two components M_{g_1} and M_{g_2} , is utilized to calculate the correlation coefficient, ρ , as:

$$\rho = \frac{\text{cov}(M_{g_1}, M_{g_2})}{\sigma_1 \sigma_2} \quad (7)$$

components with $\rho \geq 0.4$ are considered linearly dependent and aggregated. The hybrid SSA-NARNN model's steps are summarized:

- a) Divide the stock prices into a training and testing sets, 70% and 30%, respectively.
- b) Decompose the training set using SSA with $L=14$ [30].
- c) Calculate ΔE for all singular values.
- d) Determine the number of orders at which ΔE attains an asymptotic value, then group the following elementary matrices into the noise term.
- e) Reconstruct the different components.
- f) Aggregate components with $\rho \geq 0.4$.
- g) Create and train a NARNN for each with the structure illustrated in Figure 1.
- h) Predict the price of each point in the testing dataset:
 - Decompose the previous prices in the manner described in steps 2-7.
 - Predict one step of each component.
 - Add the predicted values to obtain the final price.

3. RESULTS AND DISCUSSION

The stock market data used in this research involves twenty-four stocks listed on the EGX-30 index with five-year historical data from January 2016 to December 2020. The following are the seven economic sectors of the twenty-four stocks involved in our analysis: i) basic resources, ii) non-bank financial services, iii) banks, iv) textile and durables, v) real estate, vi) food, beverages and tobacco, and vii) industrial goods, services & automobiles. The proposed SSA-NARNN model is utilized to forecast the weekly closing prices of the twenty-four stocks involved in our analysis. First, a sensitivity analysis is carried to determine the optimum number of neurons in hidden layers of the NARNN. Figure 2 shows the average calculated mean absolute error (MAPE) of the predicted stocks versus the number of neurons in NARNN hidden layers. The lowest average MAPE is obtained using seven and nine neurons in the first and second hidden layers.

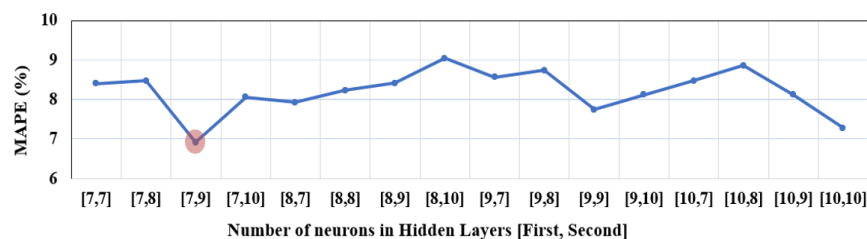


Figure 2. Sensitivity analysis of the model performance to the number of neurons in NARNN hidden layers

For demonstration, the SSA decomposition process of the COMI, the heaviest constituent of the EGX-30, is detailed. The first 70% of the available 260 trading weeks are chosen for training. The training data is decomposed into 14 elementary matrices, then the increment of singular entropy is determined. As

illustrated in Figure 3, the increment of singular entropy saturates at the sixth order. Thus, the noise term is formed by combining elementary matrices from 7 to 14.

The next step is to reconstruct the various matrices and calculate the correlation coefficient, as indicated in Table 1. The first and second reconstructed components have a correlation coefficient of 0.298, showing that they are separable. Likewise, components six and seven are separable. On the other hand, components two through six have higher correlation coefficients, $\rho \geq 0.4$, and are thus integrated into the one component. Figure 4 shows the reconstructed components, COMI's training set. RC1, RC2, and RC3 represent the market trend, fluctuation, and noise, respectively.



Figure 3. Increment of the singular entropy

Table 1. Correlation coefficients matrix of the seven reconstructed matrices

Reconstructed Matrix	1	2	3	4	5	6	7
1	1	0.298	-0.025	0.014	-0.001	-0.026	-0.012
2	0.298	1	0.421	0.057	0.067	0.009	0.005
3	-0.025	0.421	1	0.549	0.092	0.125	0.032
4	0.014	0.057	0.549	1	0.552	0.146	0.024
5	-0.001	0.067	0.092	0.552	1	0.489	0.090
6	-0.026	0.009	0.125	0.146	0.489	1	0.289
7	-0.012	0.005	0.032	0.024	0.090	0.289	1

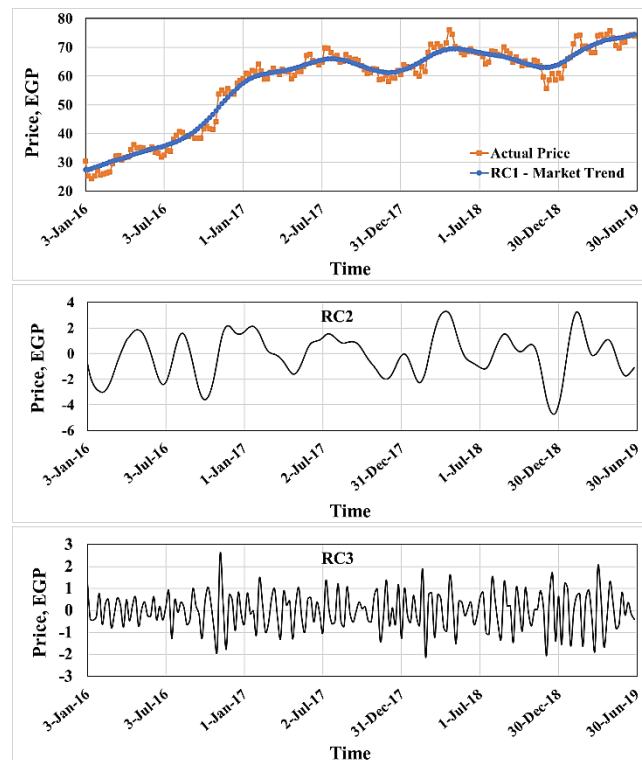


Figure 4. COMI training prices and the three reconstructed components using SSA

Each reconstructed component is utilized for training a NARNN. Then, the latest eight decomposed points are then supplied to the trained NARNNs in order to forecast the components of the first point in the testing dataset. To predict the components of the second point, the SSA is used to decompose all previous prices, i.e., the training set plus the first testing point. The NARNNs are then fed the most recent eight weeks' decomposed data. This procedure is repeated until all of the points in the testing set have been predicted. Finally, the predicted decomposed components are then aggregated to obtain the weekly closing price using the SSA-NARNN model. Figure 5 compares the predicted versus actual weekly closing prices of the COMI's testing dataset.

In order to analyze the new SSA-NARNN model's performance and prove its effectiveness, we compared it with the ARIMA and single NARNN models. Table 2 shows each model's measured evaluation criteria, with the best results bolded. The results demonstrated that the suggested SSA-NARNN outperforms the ARIMA model and the single NARNN without data preprocessing. Owing to noise and nonstationary reduction in the price data, the SSA increased the system's learning and generalization abilities. From this analysis, the proposed SSA-NARNN model proved its ability to predict stock prices in financial markets.

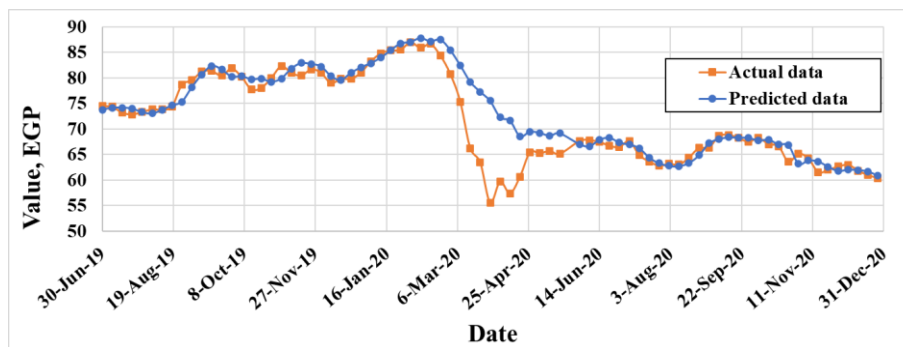


Figure 5. SSA-NARNN model's predicted weekly closing prices of the COMI stock

Table 2. Evaluation of SSA-NARNN and NARNN performance for the twenty-four stocks

Stock	RMSE			MAPE		
	ARIMA	NARNN	SSA-NARNN	ARIMA	NARNN	SSA-NARNN
ABUK	2.45	2.95	1.51	10.2	12.3	6.8
AMOC	0.52	0.43	0.29	13.2	10.4	7.5
ESRS	0.97	1.92	0.89	8.8	19.7	8
SKPC	1.34	3.47	1.04	12.2	43.5	10.1
CCAP	0.29	0.36	0.22	12.1	15.5	8.8
EKHO	0.07	0.06	0.05	4.3	3.6	3.1
HRHO	1.26	1.21	0.94	6.8	6.5	5.2
OIH	0.08	0.13	0.06	14.1	23.1	10.5
PIOH	0.53	1.92	0.41	11.8	44.3	8.5
COMI	5.21	6.25	3.73	5.2	6.2	3.6
CIEB	2.73	4.12	2.31	6.3	11.1	4.8
EXPA	0.75	0.75	0.73	5.8	5.8	4.8
ORWE	0.41	0.52	0.33	4.8	6.8	3.4
EMFD	0.18	0.12	0.11	4.3	3.3	3.2
HELI	0.56	0.46	0.45	7.8	6	5.9
MNHD	1.12	1.09	0.73	27.6	27	18.5
OCDI	1.23	1	0.92	7.7	6.5	5.9
ORHD	0.59	0.51	0.5	12.5	9.4	9.3
PHDC	0.31	0.79	0.19	16.6	52.1	11.4
TMGH	0.63	0.52	0.44	6.9	6	5.1
EAST	0.86	0.79	0.73	5.9	4.9	4
EFID	0.73	0.68	0.62	5.6	5	4.1
AUTO	0.37	0.33	0.26	10.4	9.3	7.7
SWDY	0.81	0.74	0.66	7.3	5.9	5.7

4. CONCLUSION

With regards to the importance of stock market prediction and the difficulties associated with it, researchers are constantly attempting new methods to examine these markets. NARNN is a machine learning model that contains a TDL, which lessens short-term volatility. Also, the SSA is among the effective data

preprocessing techniques that have recently been considered to reduce the noise and extract hidden information from time series. Therefore, this paper introduces a new model, i.e., the SSA-NARNN model, to forecast stock prices. Using SSA, the model first decomposes the financial time series into various components. The decomposed components are then supplied into the NARNN, which fades the short-term volatility using the eight preceding timesteps. The model performance is validated with twenty-four stocks listed on the Egyptian Exchange. Results indicate that the SSA increased the NARNN's learning and generalization, and the SSA-NARNN model outperforms the ARIMA and NARNN models. This study recommends the following for future research: i) developing a decision-based trading strategy using the proposed SSA-NARNN model to provide buy and sell signals and ii) integrating the price prediction model with other intelligent models to build portfolios with higher returns.




REFERENCES

- [1] M. Göçken, M. Özçalıcı, A. Boru, and A. T. Dosdoğru, "Integrating metaheuristics and artificial neural networks for improved stock price prediction," *Expert Systems with Applications*, vol. 44, pp. 320–331, Feb. 2016, doi: 10.1016/j.eswa.2015.09.029.
- [2] P. Sugunil and S. Somhom, "Short term stock prediction using SOM," in *Lecture Notes in Business Information Processing*, vol. 20, 2009, pp. 262–267., doi: 10.1007/978-3-642-01112-2_27.
- [3] C.-H. Cheng and L.-Y. Wei, "A novel time-series model based on empirical mode decomposition for forecasting TAIEX," *Economic Modelling*, vol. 36, pp. 136–141, Jan. 2014, doi: 10.1016/j.econmod.2013.09.033.
- [4] Y. Wang and H. Xing, "Time interval analysis on price prediction in stock market based on general regression neural networks," in *Communications in Computer and Information Science*, 2011, vol. 144, no. 2, pp. 160–166., doi: 10.1007/978-3-642-20370-1_27.
- [5] J.-F. Jerier, V. Richefeu, D. Imbault, and F.-V. Donzé, "Packing spherical discrete elements for large scale simulations," *Computer Methods in Applied Mechanics and Engineering*, vol. 199, no. 25–28, pp. 1668–1676, May 2010, doi: 10.1016/j.cma.2010.01.016.
- [6] X. Lin, Z. Yang, and Y. Song, "Short-term stock price prediction based on echo state networks," *Expert Systems with Applications*, vol. 36, no. 3, pp. 7313–7317, Apr. 2009, doi: 10.1016/j.eswa.2008.09.049.
- [7] M. R. Senapati, S. Das, and S. Mishra, "A novel model for stock price prediction using hybrid neural network," *Journal of The Institution of Engineers (India): Series B*, vol. 99, no. 6, pp. 555–563, Dec. 2018, doi: 10.1007/s40031-018-0343-7.
- [8] A. Safari and M. Davallou, "Oil price forecasting using a hybrid model," *Energy*, vol. 148, pp. 49–58, Apr. 2018, doi: 10.1016/j.energy.2018.01.007.
- [9] H. Rezaei, H. Faaljou, and G. Mansourfar, "Stock price prediction using deep learning and frequency decomposition," *Expert Systems with Applications*, vol. 169, p. 114332, May 2021, doi: 10.1016/j.eswa.2020.114332.
- [10] F. Zhou, H. Zhou, Z. Yang, and L. Yang, "EMD2FNN: a strategy combining empirical mode decomposition and factorization machine based neural network for stock market trend prediction," *Expert Systems with Applications*, vol. 115, pp. 136–151, Jan. 2019, doi: 10.1016/j.eswa.2018.07.065.
- [11] L.-Y. Wei, "A hybrid ANFIS model based on empirical mode decomposition for stock time series forecasting," *Applied Soft Computing*, vol. 42, pp. 368–376, May 2016, doi: 10.1016/j.asoc.2016.01.027.
- [12] F. Gianfelici, C. Turchetti, and P. Crippa, "Multicomponent AM-FM demodulation: the state of the art after the development of the iterated hilbert transform," in *2007 IEEE International Conference on Signal Processing and Communications*, 2007, pp. 1471–1474., doi: 10.1109/ICSPC.2007.4728608.
- [13] M. Feldman, "Analytical basics of the EMD: Two harmonics decomposition," *Mechanical Systems and Signal Processing*, vol. 23, no. 7, pp. 2059–2071, Oct. 2009, doi: 10.1016/j.ymsp.2009.04.002.
- [14] S. C. Pei and K. W. Chang, "The mystery curve: a signal processing point of view," *IEEE Signal Processing Magazine*, vol. 34, no. 6, pp. 158–163, Nov. 2017, doi: 10.1109/MSP.2017.2740457.
- [15] F. Gianfelici, G. Biagetti, P. Crippa, and C. Turchetti, "AM-FM decomposition of speech signals: an asymptotically exact approach based on the iterated hilbert transform," in *IEEE/SP 13th Workshop on Statistical Signal Processing, 2005*, 2005, no. 2, pp. 333–338., doi: 10.1109/SSP.2005.1628616.
- [16] Y. Lin, B. W.-K. Ling, N. Xu, R. W.-K. Lam, and C. Y.-F. Ho, "Effectiveness analysis of bio-electronic stimulation therapy to Parkinson's diseases via joint singular spectrum analysis and discrete fourier transform approach," *Biomedical Signal Processing and Control*, vol. 62, p. 102131, Sep. 2020, doi: 10.1016/j.bspc.2020.102131.
- [17] H. Hassani, A. S. Soofi, and A. A. Zhigljavsky, "Predicting daily exchange rate with singular spectrum analysis," *Nonlinear Analysis: Real World Applications*, vol. 11, no. 3, pp. 2023–2034, Jun. 2010, doi: 10.1016/j.nonrwa.2009.05.008.
- [18] W. Fenghua, X. Jihong, H. Zhifang, and G. Xu, "Stock price prediction based on SSA and SVM," *Procedia Computer Science*, vol. 31, pp. 625–631, 2014, doi: 10.1016/j.procs.2014.05.309.
- [19] M. Abdollahzade, A. Miranian, H. Hassani, and H. Iranmanesh, "A new hybrid enhanced local linear neuro-fuzzy model based on the optimized singular spectrum analysis and its application for nonlinear and chaotic time series forecasting," *Information Sciences*, vol. 295, no. 65, pp. 107–125, Feb. 2015, doi: 10.1016/j.ins.2014.09.002.
- [20] S. Lahmiri, "Minute-ahead stock price forecasting based on singular spectrum analysis and support vector regression," *Applied Mathematics and Computation*, vol. 320, pp. 444–451, Mar. 2018, doi: 10.1016/j.amc.2017.09.049.
- [21] J. Xiao, X. Zhu, C. Huang, X. Yang, F. Wen, and M. Zhong, "A new approach for stock price analysis and prediction based on SSA and SVM," *International Journal of Information Technology and Decision Making*, vol. 18, no. 1, pp. 35–63, Jan. 2019, doi: 10.1142/S021962201841002X.
- [22] W. Sulandari, S. Subanar, M. H. Lee, and P. C. Rodrigues, "Time series forecasting using singular spectrum analysis, fuzzy systems and neural networks," *MethodsX*, vol. 7, 2020, doi: 10.1016/j.mex.2020.101015.
- [23] A. Y. Fathi, I. A. El-Khodary, and M. Saafan, "A hybrid model integrating singular spectrum analysis and backpropagation neural network for stock price forecasting," *Revue d'Intelligence Artificielle*, vol. 35, no. 6, pp. 483–488, Dec. 2021, doi: 10.18280/ria.350606.
- [24] H. Hassani, "Singular spectrum analysis: methodology and comparison," *Journal of Data Science*, vol. 5, no. 2, pp. 239–257, Jul. 2021, doi: 10.6339/JDS.2007.05(2).396.
- [25] C. M. Rocco S, "Singular spectrum analysis and forecasting of failure time series," *Reliability Engineering and System Safety*,




- vol. 114, no. 1, pp. 126–136, Jun. 2013, doi: 10.1016/j.ress.2013.01.007.
- [26] M. de Carvalho and A. Rua, “Real-time nowcasting the US output gap: singular spectrum analysis at work,” *International Journal of Forecasting*, vol. 33, no. 1, pp. 185–198, Jan. 2017, doi: 10.1016/j.ijforecast.2015.09.004.
- [27] M. C. R. Leles, J. P. H. Sansão, L. A. Mozelli, and H. N. Guimarães, “Improving reconstruction of time-series based in singular spectrum analysis: a segmentation approach,” *Digital Signal Processing*, vol. 77, pp. 63–76, Jun. 2018, doi: 10.1016/j.dsp.2017.10.025.
- [28] A. Groth and M. Ghil, “Monte carlo singular spectrum analysis (SSA) revisited: detecting oscillator clusters in multivariate datasets,” *Journal of Climate*, vol. 28, no. 19, pp. 7873–7893, Oct. 2015, doi: 10.1175/JCLI-D-15-0100.1.
- [29] S. Lahmiri, “Wavelet low- and high-frequency components as features for predicting stock prices with backpropagation neural networks,” *Journal of King Saud University - Computer and Information Sciences*, vol. 26, no. 2, pp. 218–227, Jul. 2014, doi: 10.1016/j.jksuci.2013.12.001.
- [30] H. Hassani, Z. Ghodsi, E. S. Silva, and S. Heravi, “From nature to maths: Improving forecasting performance in subspace-based methods using genetics colonial theory,” *Digital Signal Processing*, vol. 51, pp. 101–109, Apr. 2016, doi: 10.1016/j.dsp.2016.01.002.

BIOGRAPHIES OF AUTHORS






Asmaa Y. Fathi    is a demonstrator at the Department of Operations Research and Decision Support, Faculty of Computers and Information, Cairo University, Giza, Egypt. She received her B.Sc. degree in Operations Research and Decision Support from Cairo University, Egypt, in 2015. She has been intensively involved in artificial intelligence research like neural networks, genetic algorithms, and hybrid intelligent systems. Recently, she has focused on applications of AI in predicting price behavior in financial markets. She can be contacted at email: a.fathi@fci-cu.edu.eg.



Ihab A. El-Khodary    is a professor of Operations Research and Decision Support (Data Analysis) at the Faculty of Computers and Artificial Intelligence, Cairo University. He obtained his bachelor's degree in Civil Engineering from Kuwait University, and his masters and Ph.D. degrees in Transportation Planning from the University of Waterloo, Canada. His research interests include mathematical modeling, decision support, and data analytics. His research activities have resulted in over 50 peer-reviewed articles in academic journals and conference proceedings. He has supervised over 20 Ph.D. and M.Sc. theses in mathematical modeling with applications in many disciplines including finance, medicine, sports, and archeology. He has over 25 years of teaching experience in Canada and Egypt, teaching courses in mathematical modeling, forecasting, statistics, software applications in operations research, analytics, and transportation engineering at all program levels. He can be contacted at email: e.elkhodary@fci-cu.edu.eg.



Muhammad Saafan    is a Ph.D. candidate at the Department of Petroleum Engineering, Universiti Teknologi PETRONAS (UTP), Perak Darul Ridzuan, Malaysia. He holds a master's degree in petroleum engineering in the area (production history matching using intelligent algorithms). Besides his main work in petroleum engineering, he is interested in applying artificial intelligence in predicting financial markets and portfolio optimization. He can be contacted at email: muhammad.saafan@yahoo.com.