

Shear and reverse shear testing

AA 6016-T4

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Equipment:



- ❑ Bi-axial machine (Built in ULiège) ([Fig 1](#))
- ❑ Optical system (2 cameras) ([Fig 2](#))
- ❑ Computer 1: Command the pistons
- ❑ Computer 2: Image acquisition (from the optical system)+ Force and displacement acquisition (from the Bi-axial machine)



Fig 1: Bi-axial machine

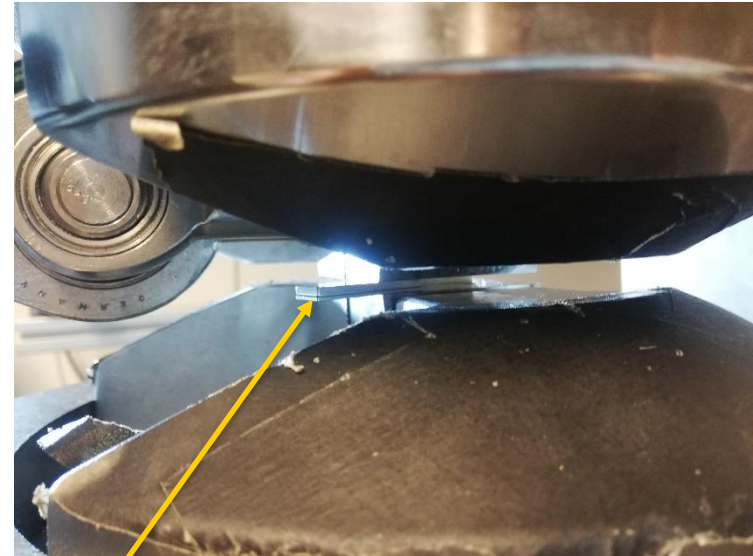
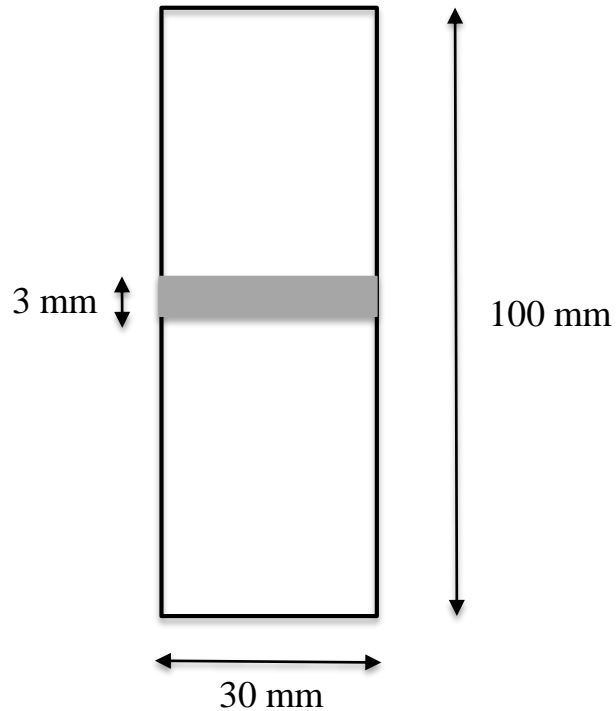


Fig 2: Optical system



Test conditions:

- ❑ Constant crosshead speed 1mm/min
- ❑ Room temperature
- ❑ The deformation zone is 30mm X 3mm (Fig 3)



Hold of 3 mm



Used software:

- ❑ “Tema” installed in computer 1 to command the horizontal piston (Fig 4)
- ❑ “VIC 3D” installed in computer 2 for the image acquisition (Fig 5)

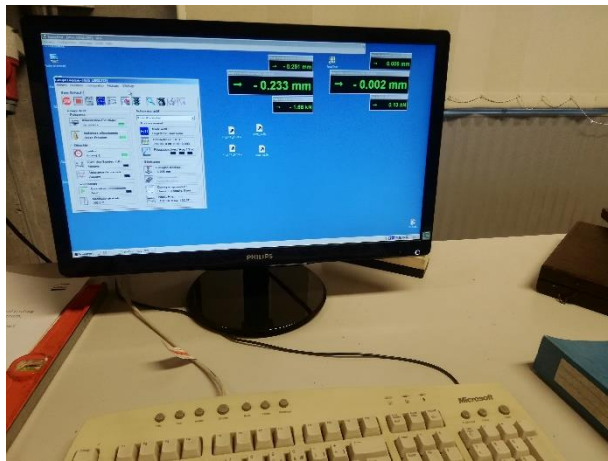


Fig 4: Tema software

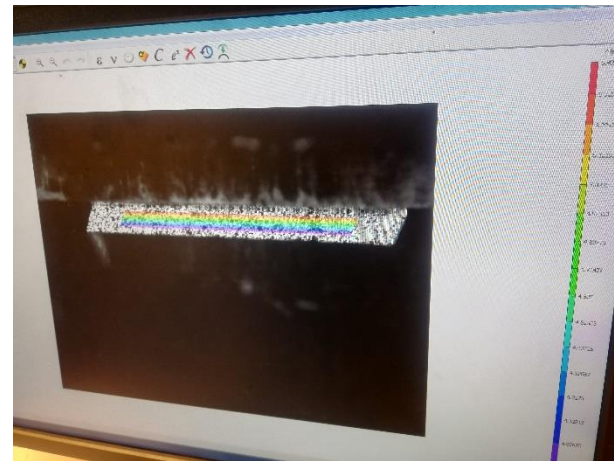


Fig 5: VIC 3D

Different types of strain tensor in VIC 3D:

Lagrange – Hencky – EulerAlmansi – Logarithmic EulerAlmansi - Engineering

The chosen type (seen its simple relation with the shear strain that Aaramis gives)

Lagrange strain:



Simple shear

$$\begin{aligned}x &= X + \tan \gamma \cdot Y \\y &= Y \\z &= Z\end{aligned}$$

Displacements field

$$\begin{aligned}u &= \tan \gamma \cdot Y \\v &= 0 \\w &= 0\end{aligned}$$

Transformation tensor

$$\mathbf{F} = \frac{\partial \mathbf{x}}{\partial \mathbf{X}} = \begin{bmatrix} 1 & \tan \gamma & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Cauchy-Green and Green-Lagrange

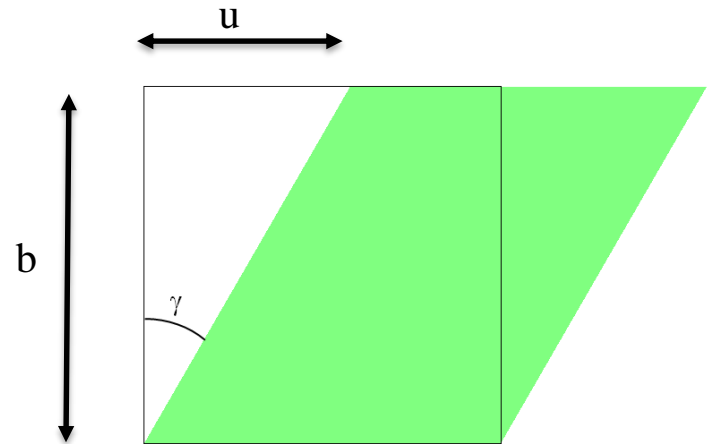
$$\mathbf{C} = \mathbf{F}^T \mathbf{F} = \begin{bmatrix} 1 & \tan \gamma & 0 \\ \tan \gamma & 1 + \tan^2 \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{E} = \frac{1}{2}(\mathbf{C} - \mathbf{I}) = \frac{1}{2} \begin{bmatrix} 0 & \tan \gamma & 0 \\ \tan \gamma & \tan^2 \gamma & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

For small angles/deformations

$$\varepsilon = \frac{1}{2} \begin{bmatrix} 0 & \gamma & 0 \\ \gamma & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

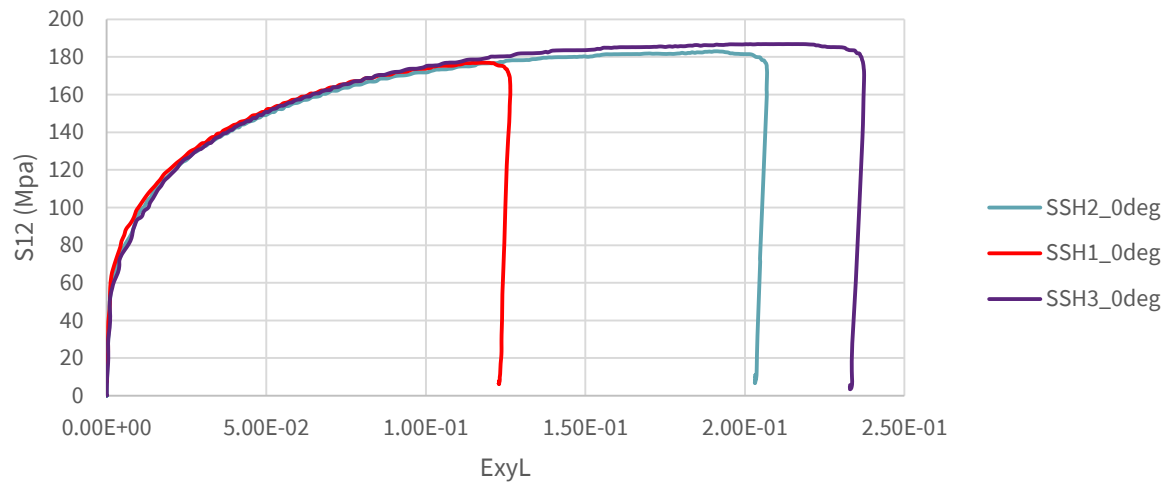
$$\gamma = u/b$$



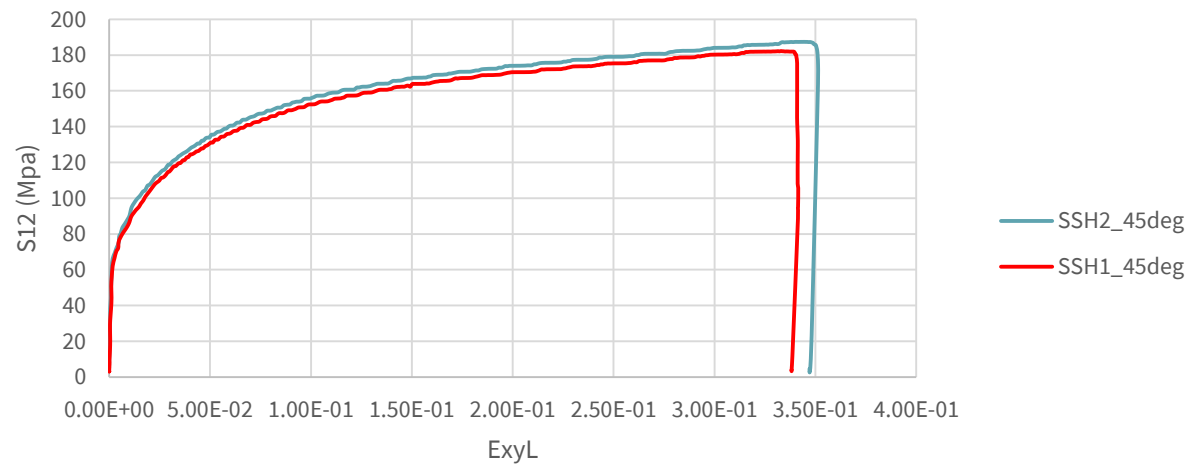
Simple shear:



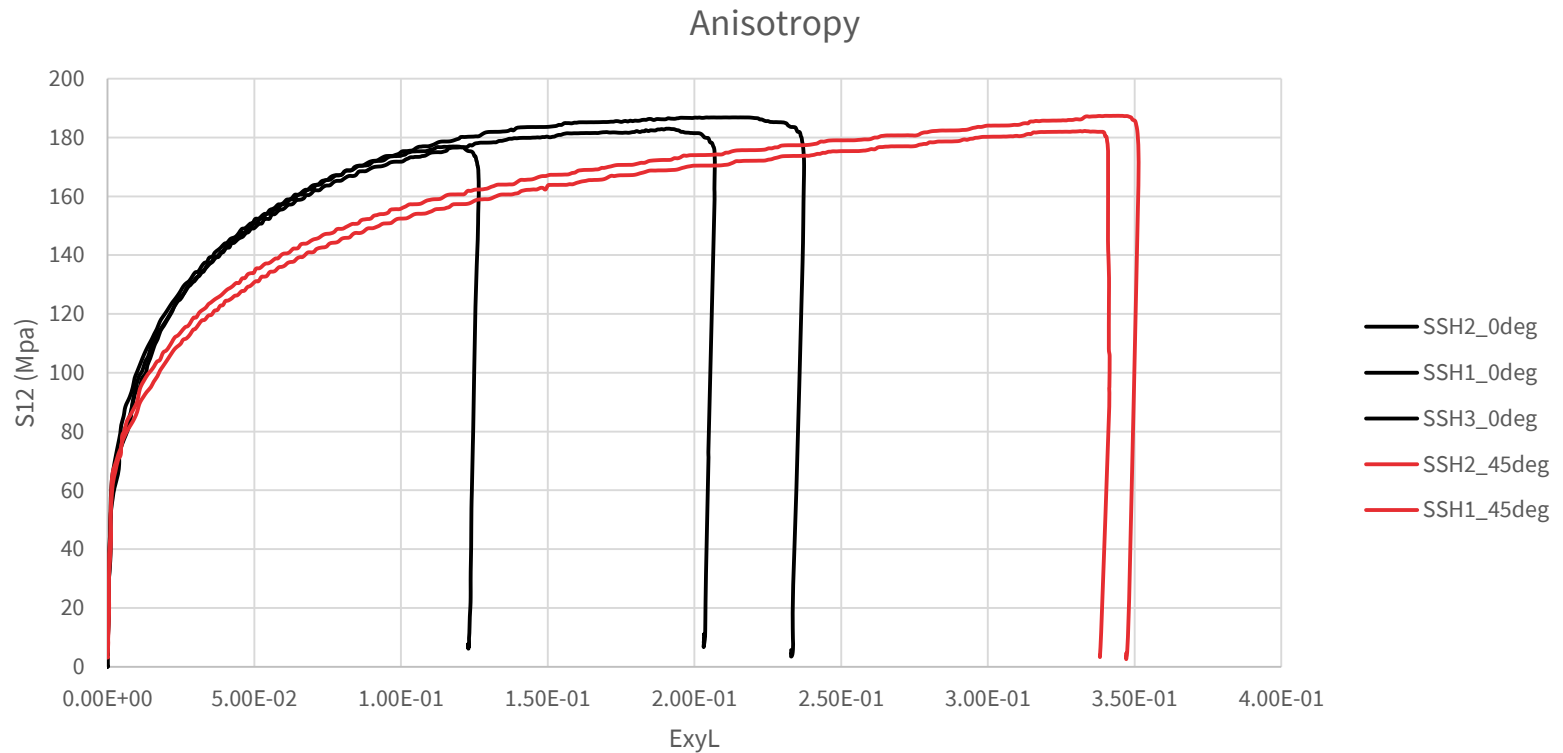
Simple Shear (0 deg)



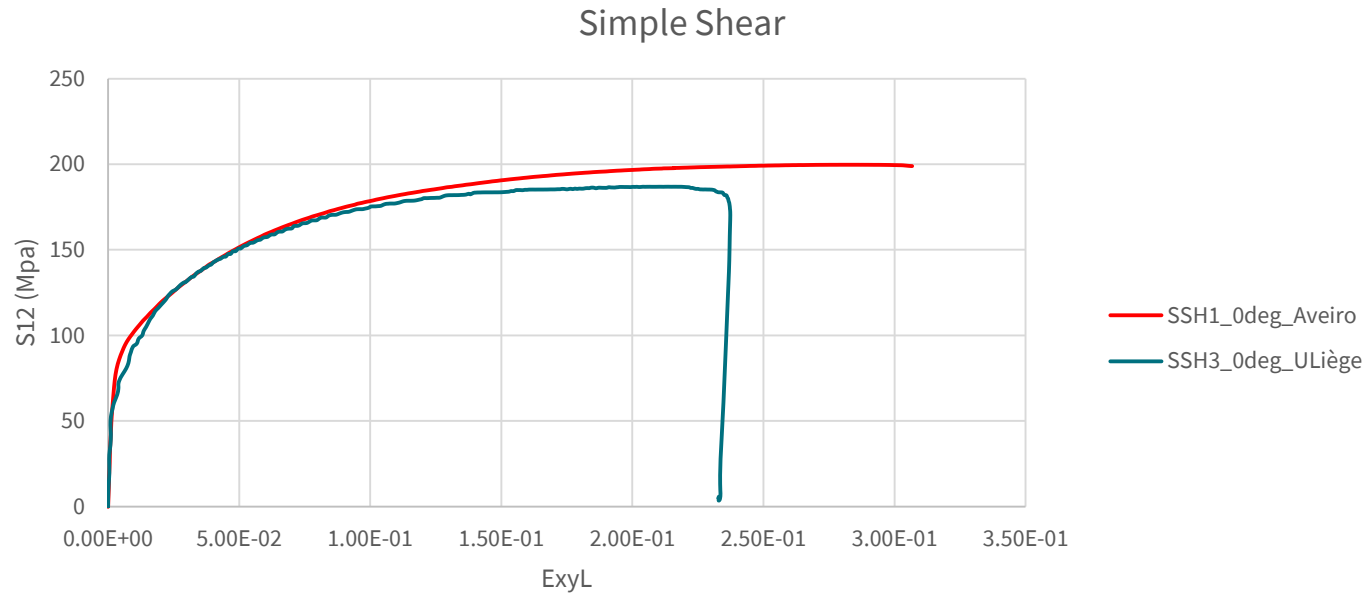
Simple Shear (45 deg)



Simple shear: Anisotropy



Simple shear: ULiège vs Aveiro

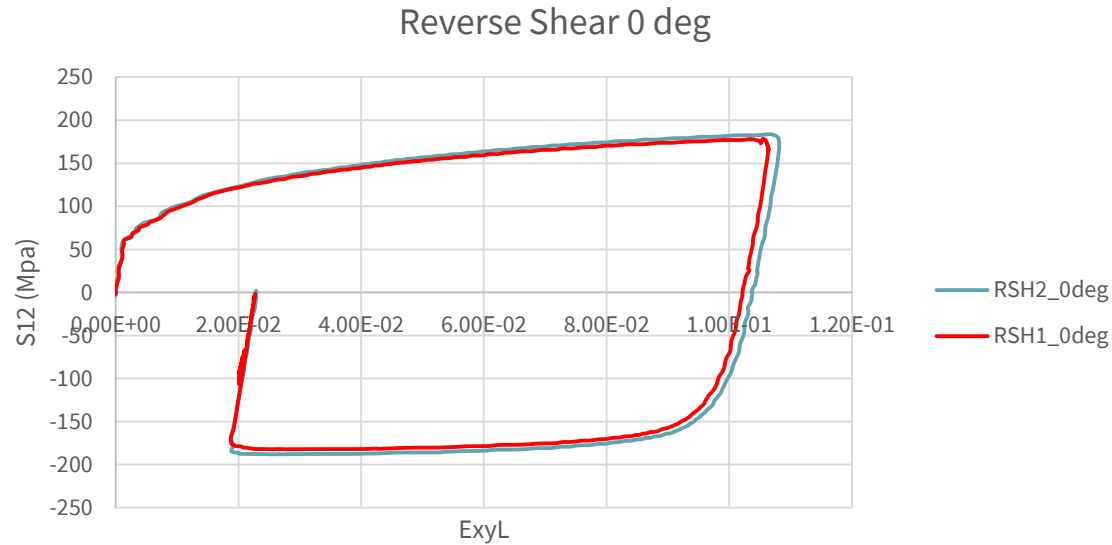


$$\varepsilon_{xy} = \frac{1}{2} \gamma$$



Reverse shear ($E_{xy} = 10\%$ (ULiège); $\Gamma = 20\%$ (Aveiro)):

$E_{xy_R} = 10,2\%$



$E_{xy_R} = 11,1\%$

