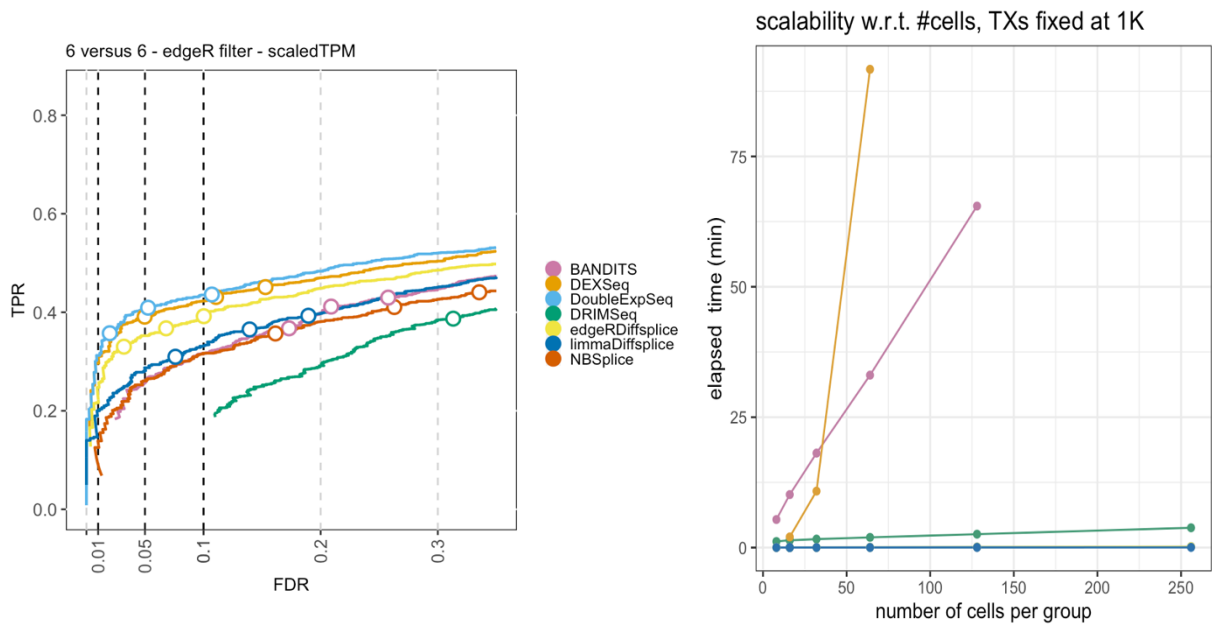


# 1 Supplementary Figures

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5 **Figure S1: Performance and scalability evaluation on a subset of the Love *et al.* dataset.** To allow for a  
6 performance and scalability evaluation of BANDITS, which does not scale to datasets with many transcripts, we  
7 here perform a DTU analysis for the *6 versus 6* samples dataset of Love *et al.* with only 1000 transcripts. **Left**  
8 **panel: performance evaluation.** The results are in line with those of Figure 1A. The performance of BANDITS is  
9 indicated in pink. **Right panel: Scalability evaluation.** BANDITS scales linearly with respect to the number of cells  
10 (or samples) in the dataset. The slope of the linear trend, however, is considerably larger than those of the other  
11 DTU methods that scale linearly. Note that the profiles of limma diffsplice, edgeR diffsplice and DoubleExpSeq  
12 overlap in this figure.

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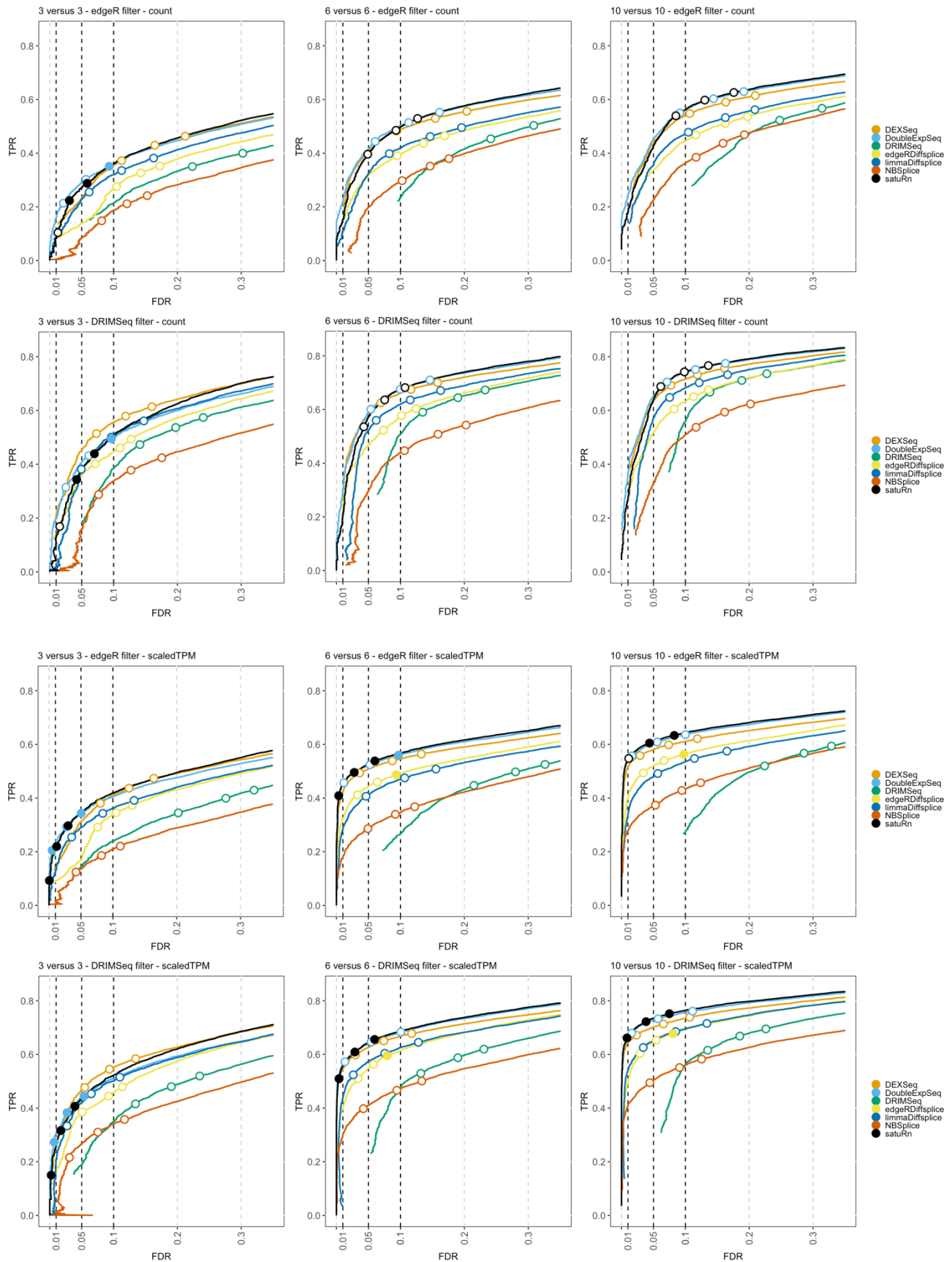
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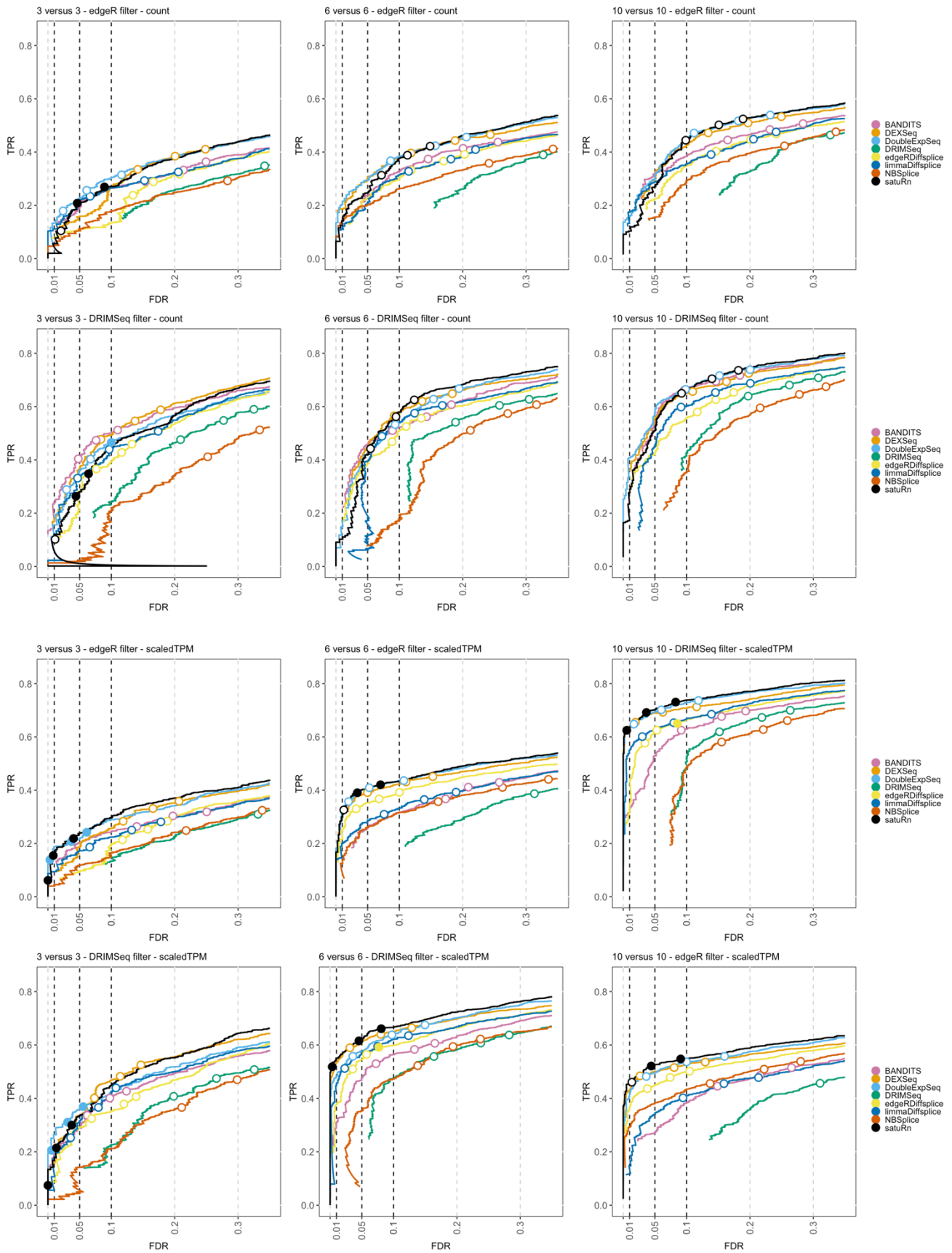
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36 **Figure S2: Performance evaluation of satuRn on different subsamples of the simulated bulk RNA-seq dataset**  
 37 **by Love *et al.*** FDR-TPR curves visualize the performance of each method by displaying the sensitivity of the  
 38 method (TPR) with respect to the false discovery rate (FDR). The three circles on each curve represent working  
 39 points when the FDR level is set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the

40 empirical FDR is equal or below the imposed FDR threshold. We subsampled two-group comparisons according  
41 to three different samples sizes; a *3 versus 3*, *6 versus 6* and *10 versus 10* comparison, as denoted in the panel  
42 titles. The benchmark was performed both on the raw counts (**rows 1 and 2**) or on scaled transcripts-per-million  
43 (TPM) (**rows 3 and 4**) as imported with the Bioconductor R package tximport<sup>1</sup>. We additionally adopted two  
44 different filtering strategies: an edgeR-based filtering (**rows 1 and 3**) and a DRIMSeq-based filtering (**rows 2 and**  
45 **4**). Overall, the performance of satuRn is on par with those of the best tools in the literature, DEXSeq and  
46 DoubleExpSeq. In addition, satuRn achieves a better control of the FDR on all datasets. For extremely small  
47 sample size, i.e. the *3 versus 3* comparison, the performance is slightly below that of DEXSeq, and inference does  
48 become slightly too conservative. Note that, as expected, the performances increase with increasing sample  
49 size, and a higher performance is achieved with the more stringent DRIMSeq filtering criterion (see Methods),  
50 which goes at the cost of retaining fewer transcripts for DTU analysis. Finally, we note that the performances  
51 and FDR control are consistently better for the scaled TPM data as compared to the raw counts. Note that this  
52 was only observed for this particular dataset.

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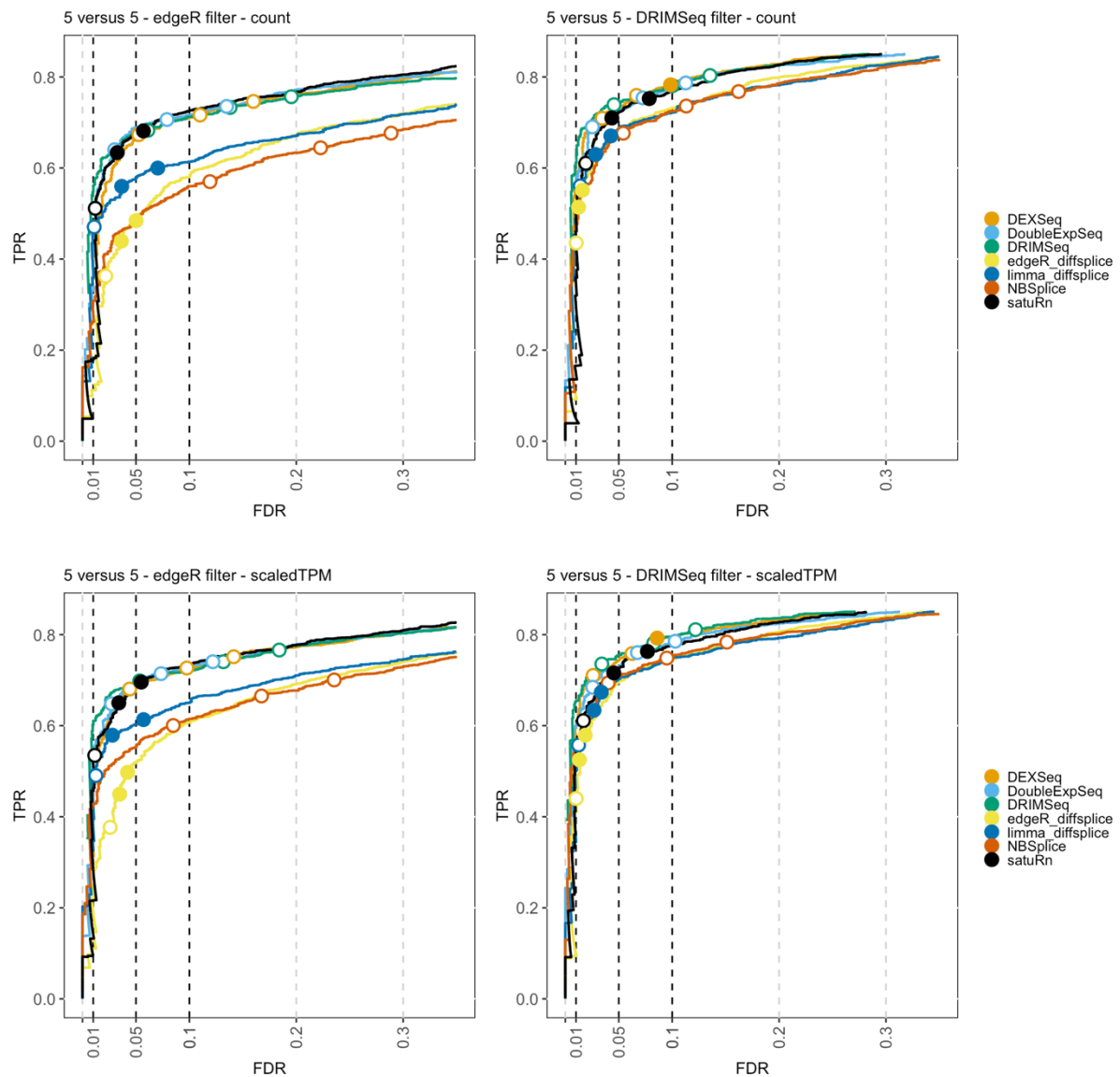
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**Figure S3: Performance evaluation on different subsamples of the simulated bulk RNA-seq dataset by Love *et al.* with a reduced number of transcripts to allow for a comparison with BANDITS. FDR-TPR curves visualize the performance of each method by displaying the sensitivity of the method (TPR) with respect to the**

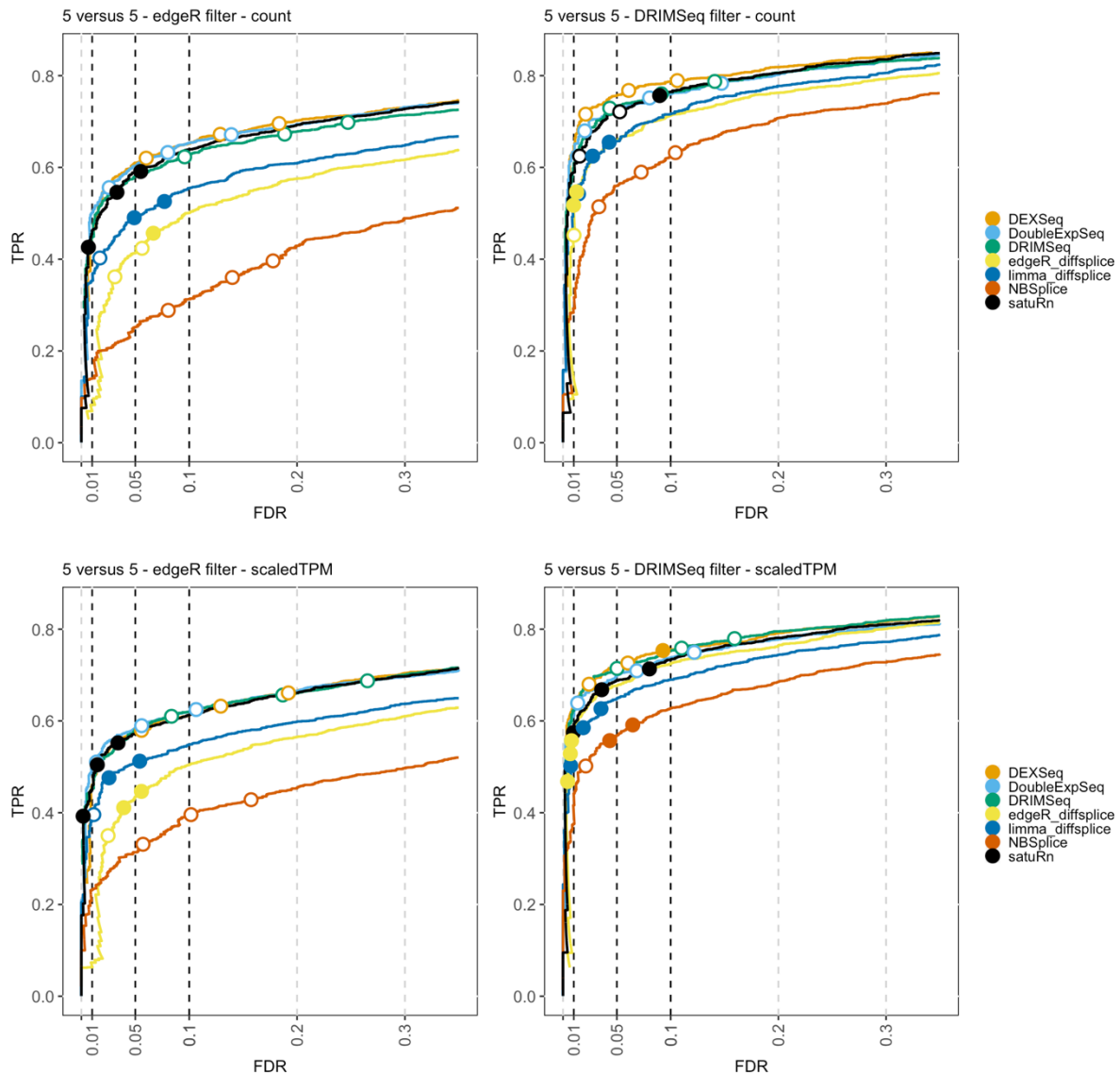


96 false discovery rate (FDR). The three circles on each curve represent working points when the FDR level is set  
97 at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the empirical FDR is equal or below  
98 the imposed FDR threshold. We subsampled two-group comparisons according to three different samples  
99 sizes; a *3 versus 3*, *6 versus 6* and *10 versus 10* comparison, as denoted on top of the panels. The benchmark  
100 was performed both on the raw counts (**rows 1 and 2**) or on scaled transcripts-per-million (TPM) (**rows 3 and**  
101 **4**) as imported with the Bioconductor R package tximport<sup>1</sup>. We additionally adopted two different filtering  
102 strategies: an edgeR-based filtering (**rows 1 and 3**) and a DRIMSeq-based filtering (**rows 2 and 4**). Note that, in  
103 contrast to Figure S2, we additionally randomly subsampled 1000 genes (~3000-5000 transcripts) after  
104 filtering, in order to reduce the number of transcripts in the data and thereby allowing for a DTU analysis with  
105 BANDITS. In concordance with Figure S2, the performance of satuRn is on par with the best tools of the  
106 literature with a better control of the FDR in general. While the performance of BANDITS is good for the  
107 settings for which it was originally developed, (i.e., small datasets with a stringent filtering criterium), its  
108 performance is reduced in larger, more leniently filtered datasets and inference is also overly liberal in these  
109 settings. In addition, while all other methods perform much better on the scaledTPM data (rows 3 and 4) than  
110 on the raw count data (rows 1 and 2), BANDITS has a similar performance on both input data types. This can  
111 be explained by the fact that BANDITS inherently corrects for differences in transcript length, even when raw  
112 counts are used as an input.

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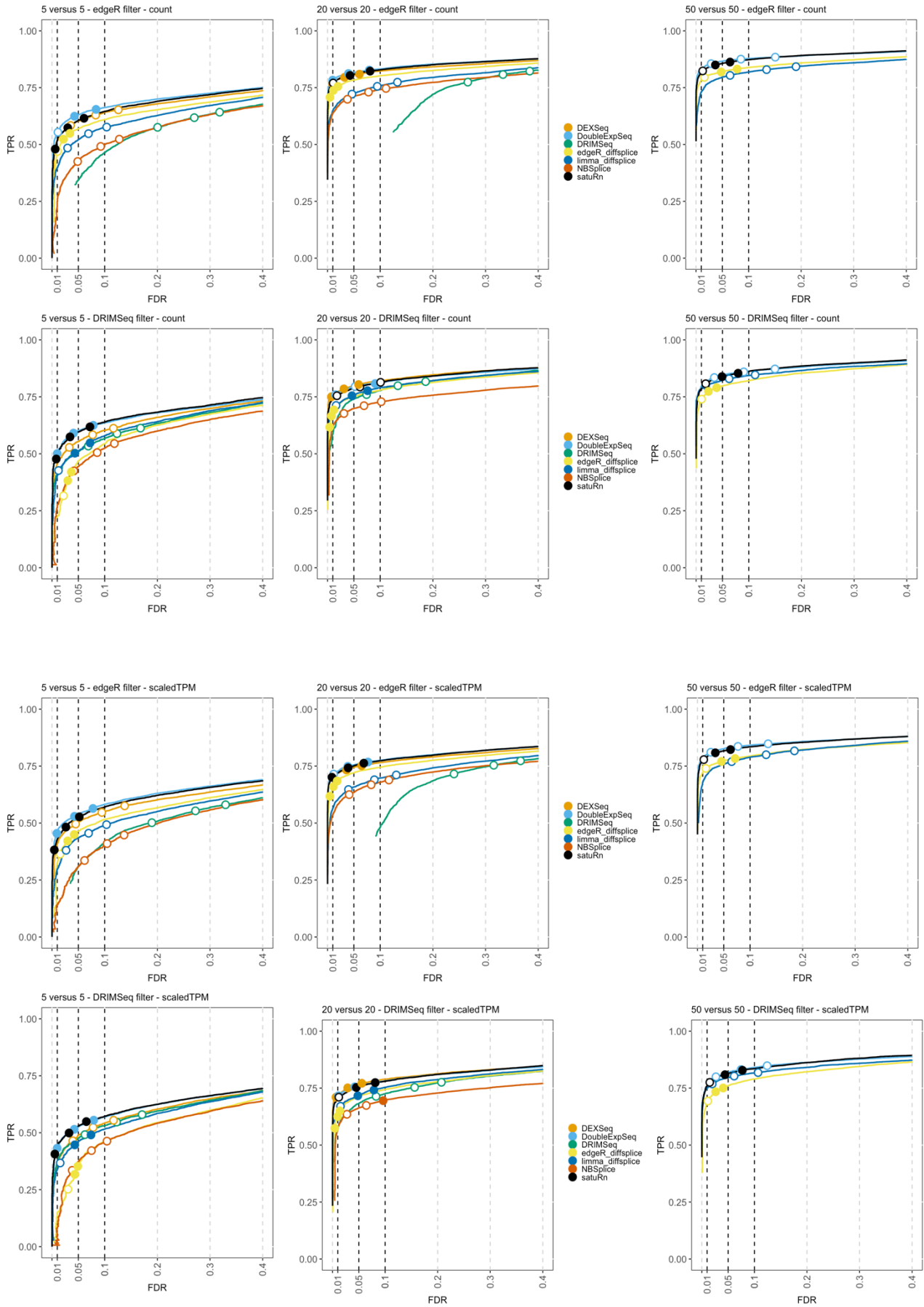


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 142 **Figure S4: Performance evaluation of DTU methods on the “Drosophila” simulated bulk RNA-seq dataset**  
 143 **by Van den Berge *et al.*** FDR-TPR curves visualize the performance of each method by displaying the sensitivity  
 144 of the method (TPR) with respect to the false discovery rate (FDR). The three circles on each curve represent  
 145 working points when the FDR level is set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled  
 146 if the empirical FDR is equal or below the imposed FDR threshold. The benchmark was performed both on the  
 147 raw counts (**row 1**) and on scaled TPM (**row 2**) as obtained with the Bioconductor R package tximport<sup>1</sup>. We  
 148 additionally adopted two different filtering strategies; an edgeR-based filtering (**column 1**) and a DRIMSeq-based  
 149 filtering (**column 2**). Overall, the performance of satuRn is on par with those of the best tools in the literature,  
 150 DEXSeq and DoubleExpSeq. In contrast to the performance evaluation on the dataset by Love *et al.* (Figures 1A  
 151 and S2), there is a limited difference in performances based on the data input type (i.e., counts versus scaled  
 152 TPM), and DRIMSeq also performs well on these datasets.  
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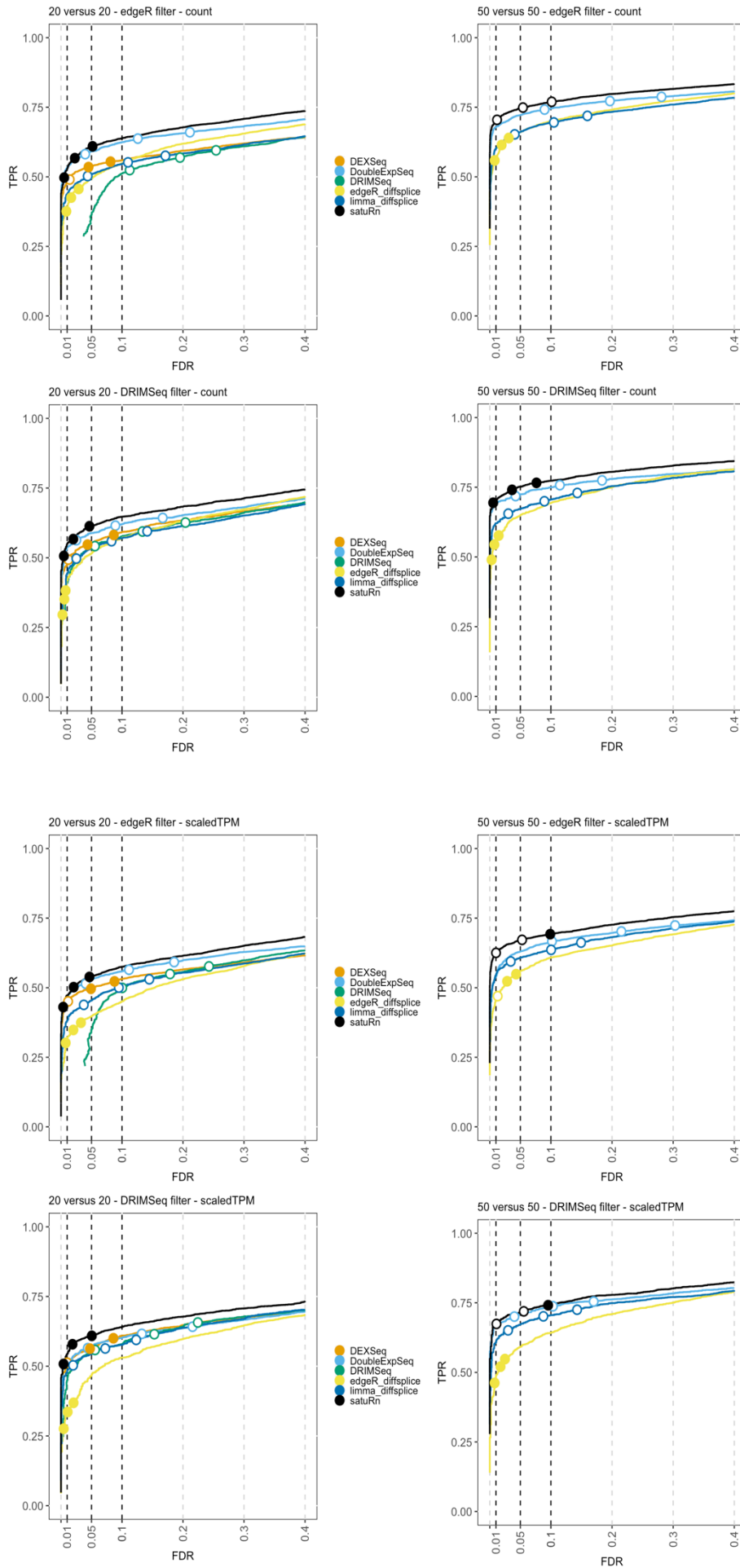
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 163 **Figure S5: Performance evaluation of DTU methods on the “Hsapiens” simulated bulk RNA-seq dataset by Van**  
 164 **den Berge *et al.*** FDR-TPR curves visualize the performance of each method by displaying the sensitivity of the  
 165 method (TPR) with respect to the false discovery rate (FDR). The three circles on each curve represent working  
 166 points when the FDR level is set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the  
 167 empirical FDR is equal or below the imposed FDR threshold. The benchmark was performed both on the raw  
 168 counts (**row 1**) and on scaled TPM (**row 2**) as obtained with the Bioconductor R package tximport<sup>1</sup>. We  
 169 additionally adopted two different filtering strategies; an edgeR-based filtering (**column 1**) and a DRIMSeq-based  
 170 filtering (**column 2**). Overall, the performance of satuRn is on par with those of the best tools in the literature,  
 171 DEXSeq and DoubleExpSeq. In contrast to the performance evaluation on the dataset by Love *et al.* (Figures 1A  
 172 and S2), there is a limited difference in performances based on the data input type (i.e., counts versus scaled  
 173 TPM), and DRIMSeq also performs well on these datasets.

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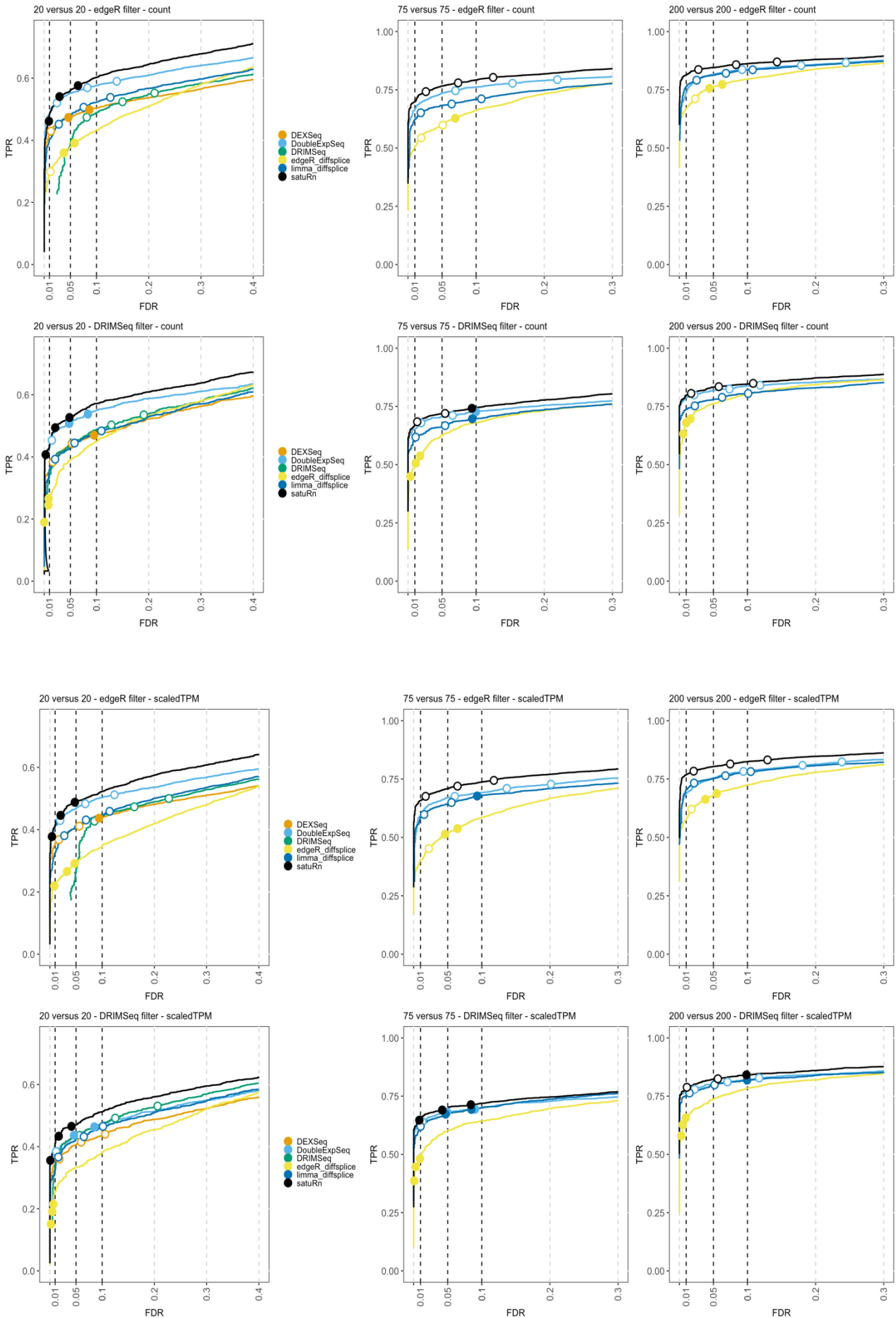
183 **Figure S6: Performance evaluation of DTU methods on the GTEx bulk RNA-seq dataset.** FDR-TPR curves  
184 visualize the performance of each method by displaying the sensitivity (TPR) with respect to the false discovery  
185 rate (FDR). The three circles on each curve represent working points when the FDR level is set at nominal levels  
186 of 1%, 5% and 10%, respectively. The circles are filled if the empirical FDR is equal or below the imposed FDR  
187 threshold. The benchmark was performed both on the raw counts (**rows 1 and 2**) or on scaled transcripts-per-  
188 million (TPM) (**rows 3 and 4**) as obtained with the Bioconductor R package tximport<sup>1</sup>. We additionally adopted  
189 two different filtering strategies; an edgeR-based filtering (**rows 1 and 3**) and a DRIMSeq-based filtering (**rows 2**  
190 **and 4**). The performance of satuRn is on par with the best tools from the literature, DEXSeq and DoubleExpSeq.  
191 In addition, satuRn consistently provides a stringent control of the FDR, while DoubleExpSeq becomes more  
192 liberal with increasing sample sizes. Note that DEXSeq, DRIMSeq and NBSplice were omitted from the largest  
193 comparison, as these methods do not scale to large datasets (Figure1).

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243 **Figure S7: Performance evaluation of DTU methods on the real scRNA-seq dataset by Chen *et al.*** FDR-TPR  
244 curves visualize the performance of each method by displaying the sensitivity of the method (TPR) with respect  
245 to the false discovery rate (FDR). The three circles on each curve represent working points when the FDR level is  
246 set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the empirical FDR is equal or below  
247 the imposed FDR threshold. The benchmark was performed both on the raw counts (**rows 1 and 2**) or on scaled  
248 transcripts-per-million (TPM) (**rows 3 and 4**) as obtained with the Bioconductor R package tximport<sup>1</sup>. We  
249 additionally adopted two different filtering strategies; an edgeR-based filtering (**rows 1 and 3**) and a DRIMSeq-  
250 based filtering (**rows 2 and 4**). The performance of satuRn is at least on par with the best tools from the  
251 literature. Note that the performance of DEXSeq is clearly lower. In addition, our method consistently controls  
252 the FDR close to its imposed nominal FDR threshold, while DoubleExpSeq becomes more liberal with increasing  
253 sample sizes. DEXSeq and DRIMSeq were omitted from the largest comparison (two groups with 50 cells each),  
254 as these methods do not scale to large datasets (Figure 1). NBSplice was omitted from all comparisons, as it does  
255 not converge on datasets with many zeros, such as scRNA-seq datasets.

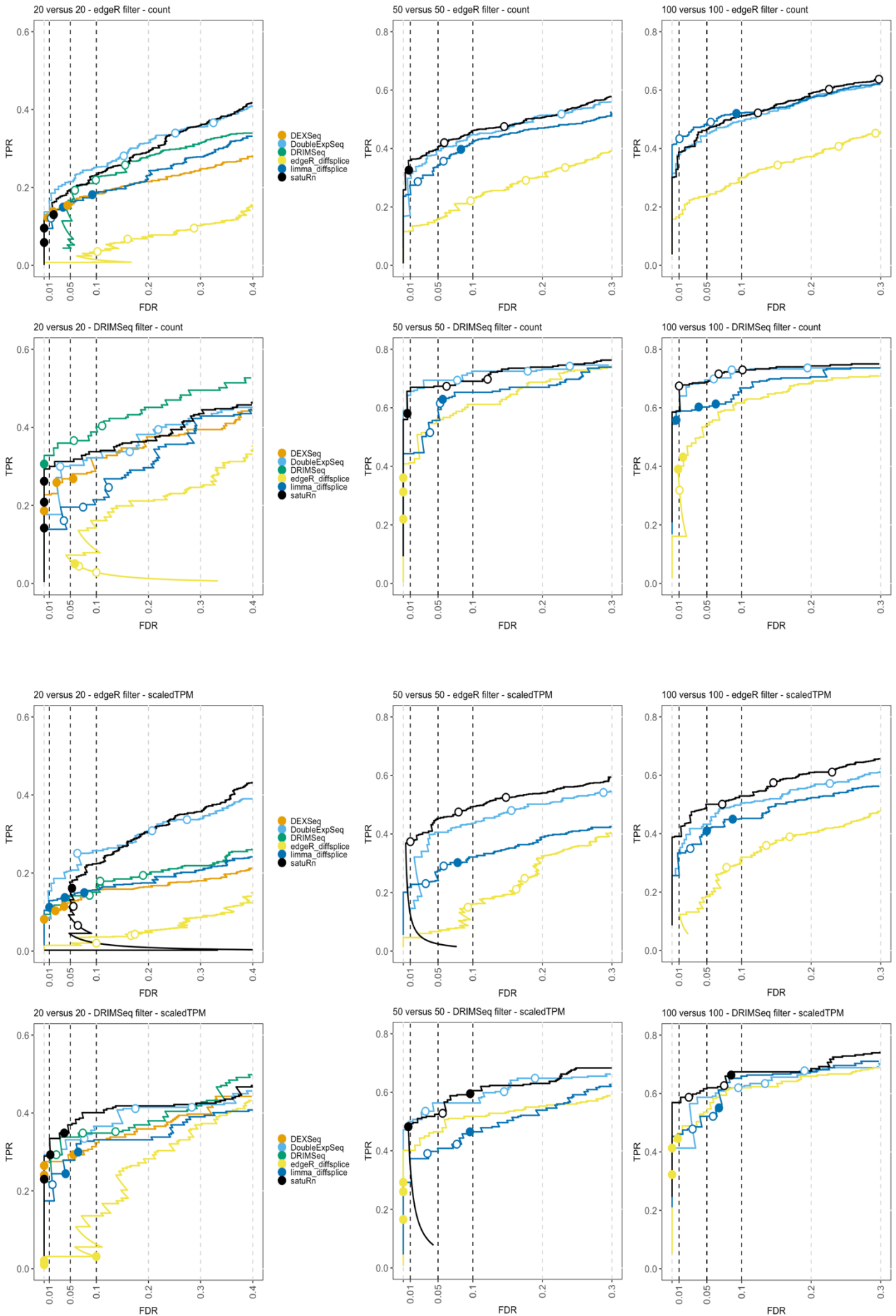
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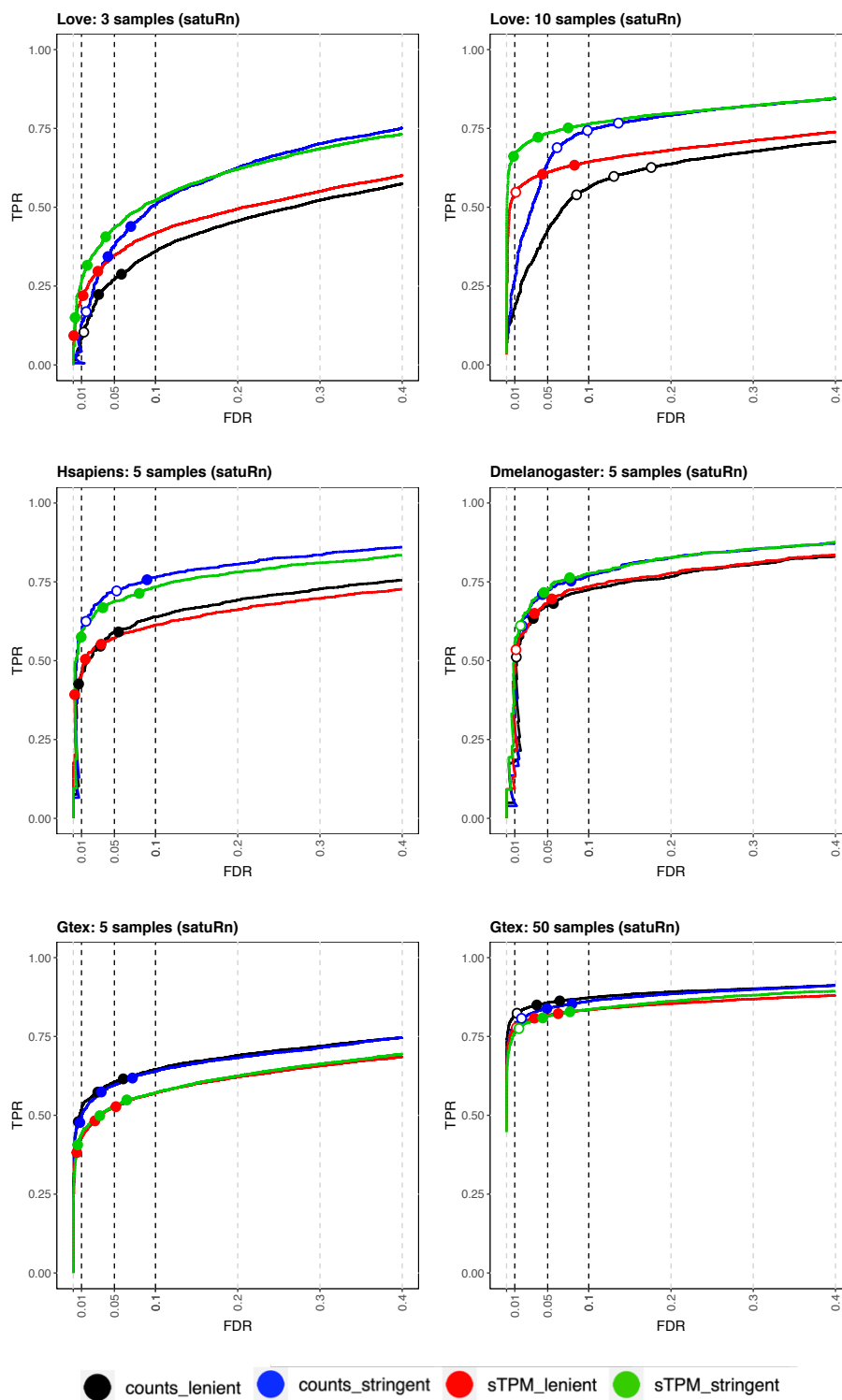
300 **Figure S8: Performance evaluation of DTU methods on the real scRNA-seq dataset by Tasic *et al.*** FDR-TPR  
301 curves visualize the performance of each method by displaying the sensitivity of the method (TPR) with respect  
302 to the false discovery rate (FDR). The three circles on each curve represent working points when the FDR level is  
303 set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the empirical FDR is equal or below  
304 the imposed FDR threshold. We generated three two-group comparisons of 20, 75 and 200 cells each (left,  
305 middle and right panel, respectively). The benchmark was performed both on the raw counts (**rows 1 and 2**) or  
306 on scaled transcripts-per-million (TPM) (**rows 3 and 4**) as obtained with the Bioconductor R package tximport<sup>1</sup>.  
307 We additionally adopted two different filtering strategies; an edgeR-based filtering (**rows 1 and 3**) and a  
308 DRIMSeq-based filtering (**rows 2 and 4**). Overall, satuRn slightly outperforms DoubleExpSeq, the best tools from  
309 the literature. Note that the performance of DEXSeq is clearly lower. In addition, our method consistently  
310 controls the FDR close to its imposed nominal FDR threshold, while DoubleExpSeq becomes more liberal with  
311 increasing sample sizes. DEXSeq and DRIMSeq were omitted from the largest comparison (two groups with 75  
312 cells and 200 cells each, respectively), as these methods do not scale to large datasets (Figure 1). NBSplice was  
313 omitted from all comparisons, as it does not converge on datasets with many zeros, such as scRNA-seq datasets.

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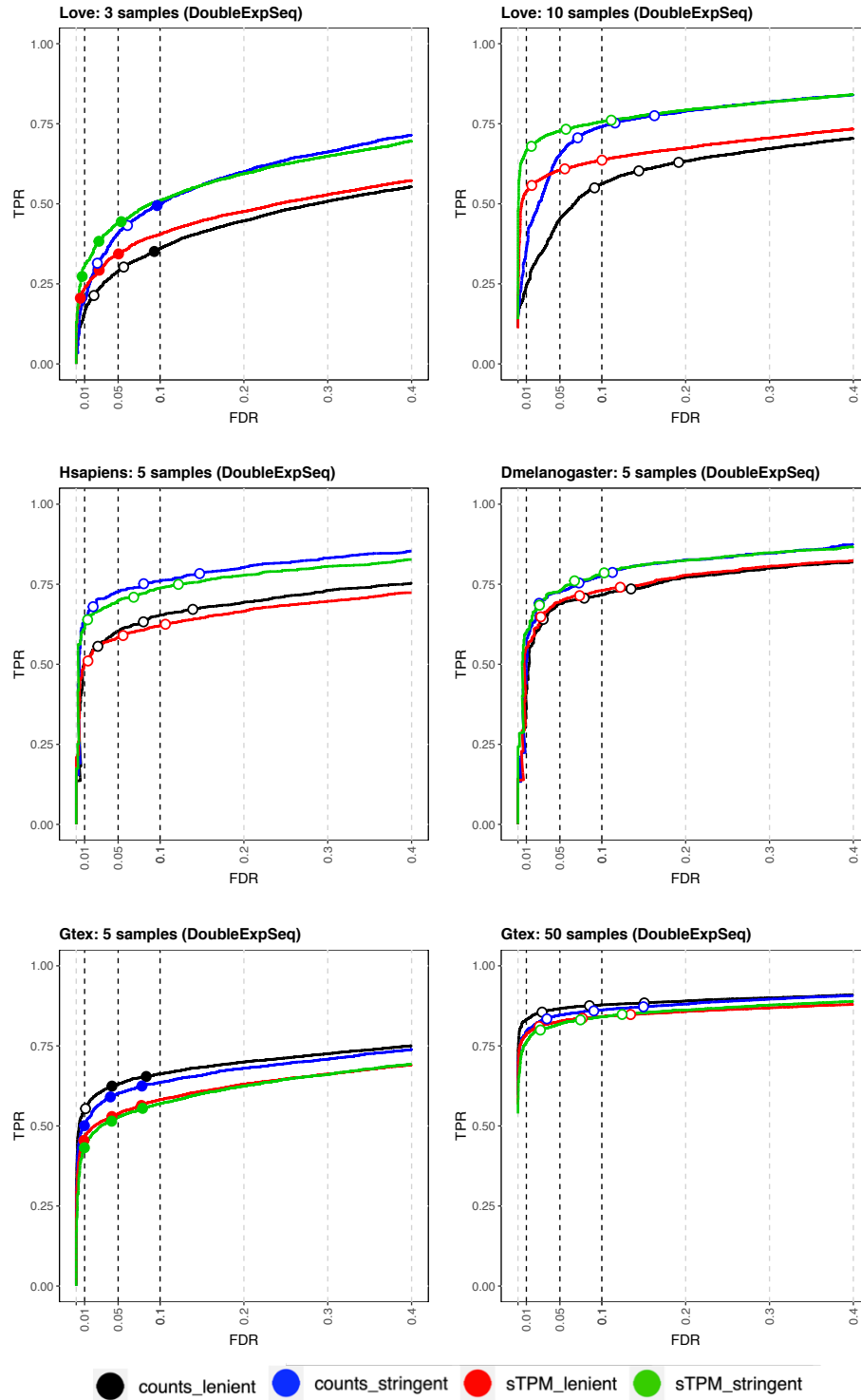
353 **Figure S9: Performance evaluation of DTU methods on the real scRNA-seq dataset by Darmanis *et al.*** FDR-TPR  
354 curves visualize the performance of each method by displaying the sensitivity of the method (TPR) with respect  
355 to the false discovery rate (FDR). The three circles on each curve represent working points when the FDR level is  
356 set at nominal levels of 1%, 5% and 10%, respectively. The circles are filled if the empirical FDR is equal or below  
357 the imposed FDR threshold. We generated three two-group comparisons of 20, 50 and 100 cells each (left,  
358 middle and right panel, respectively). The benchmark was performed both on the raw counts (**rows 1 and 2**) or  
359 on scaled transcripts-per-million (TPM) (**rows 3 and 4**) as obtained with the Bioconductor R package tximport<sup>1</sup>.  
360 We additionally adopted two different filtering strategies; an edgeR-based filtering (**rows 1 and 3**) and a  
361 DRIMSeq-based filtering (**rows 2 and 4**). Overall, the performance of *satuRn* is similar to DoubleExpSeq, the best  
362 tools from the literature. In addition, our method consistently controls the FDR close to its imposed nominal FDR  
363 threshold, while DoubleExpSeq becomes more liberal with increasing sample sizes. On the dataset with the  
364 smallest sample size, the FDR control of *satuRn* does become too strict.

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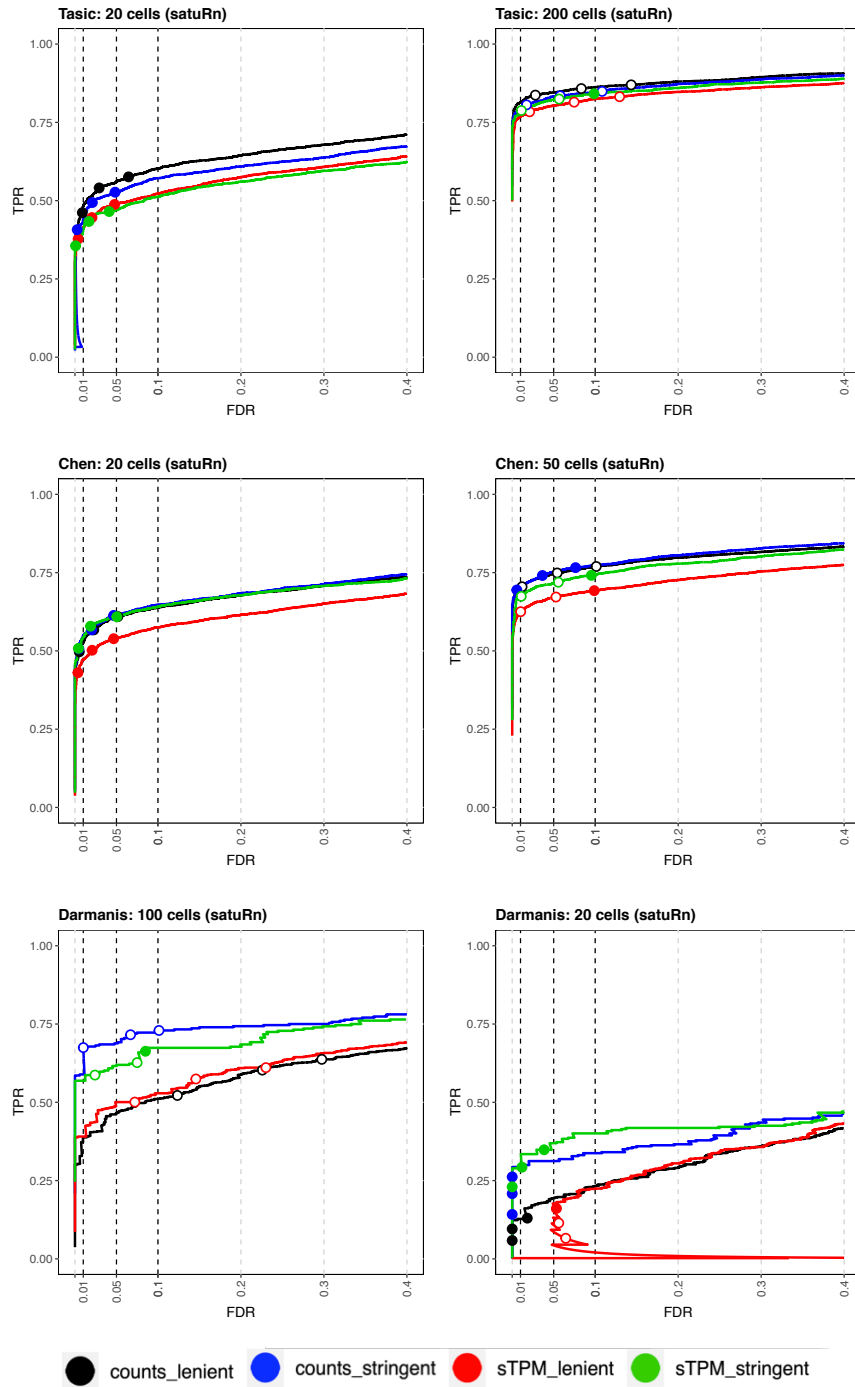
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**Figure S10: The effect of filtering and abundance metrics on the performance of satuRn in the different bulk RNA-seq benchmark datasets.** The effect of filtering and abundance metric differs between the different datasets. **Top row:** For the dataset by Love *et al.*, filtering more stringently improves performance. In addition, both performance and FDR control are much better when using scaledTPM abundances, as compared to using counts. **Middle row:** For the simulated bulk datasets by Van den Berge *et al.*<sup>40</sup>, we also observe a positive effect of stringent filtering, however, the difference between scaledTPM and raw count abundances is negligible. **Bottom row:** For GTEX bulk dataset, the effect of filtering is limited. However, using counts performs considerably better than using scaledTPM abundances.



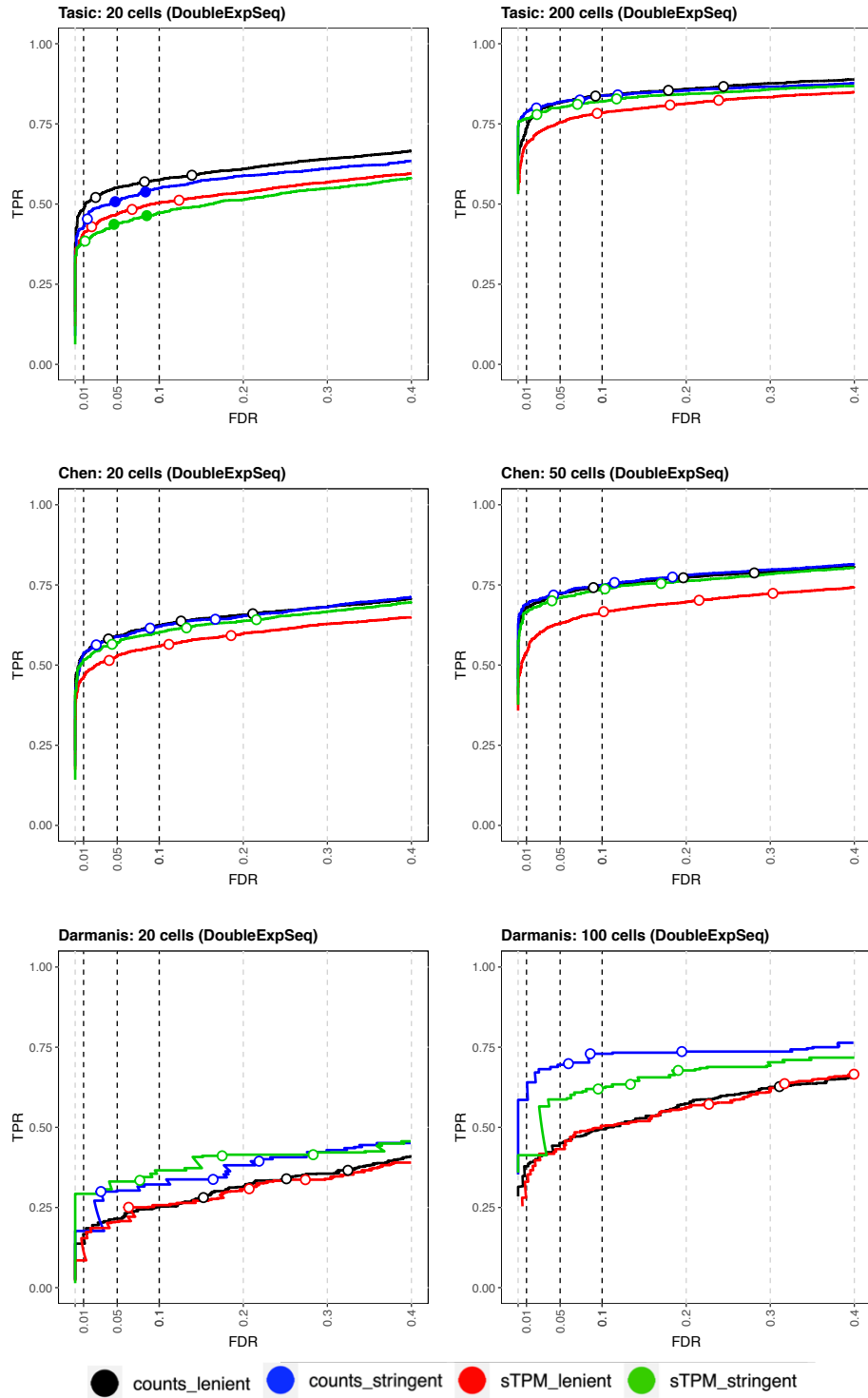
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**Figure S11: The effect of filtering and abundance metrics on the performance of DoubleExpSeq in the different bulk RNA-seq benchmark datasets.** The effect of filtering and abundance metric differs between the different datasets. The observed effects correspond strongly with the effects of filtering and abundance metrics on satuRn (figure S10) and limma diffsplice (not shown). **Top row:** For the dataset by Love *et al.*, filtering more stringently improves performance. In addition, both performance and FDR control are much better when using scaledTPM abundances, as compared to using counts. **Middle row:** For the simulated bulk datasets by Van den Berge *et al.*<sup>40</sup>, we also observe a positive effect of stringent filtering, however, the difference between scaledTPM and raw count abundances is negligible. **Bottom row:** For GTEx bulk dataset, the effect of filtering is limited. However, using counts performs considerably better than using scaledTPM abundances.



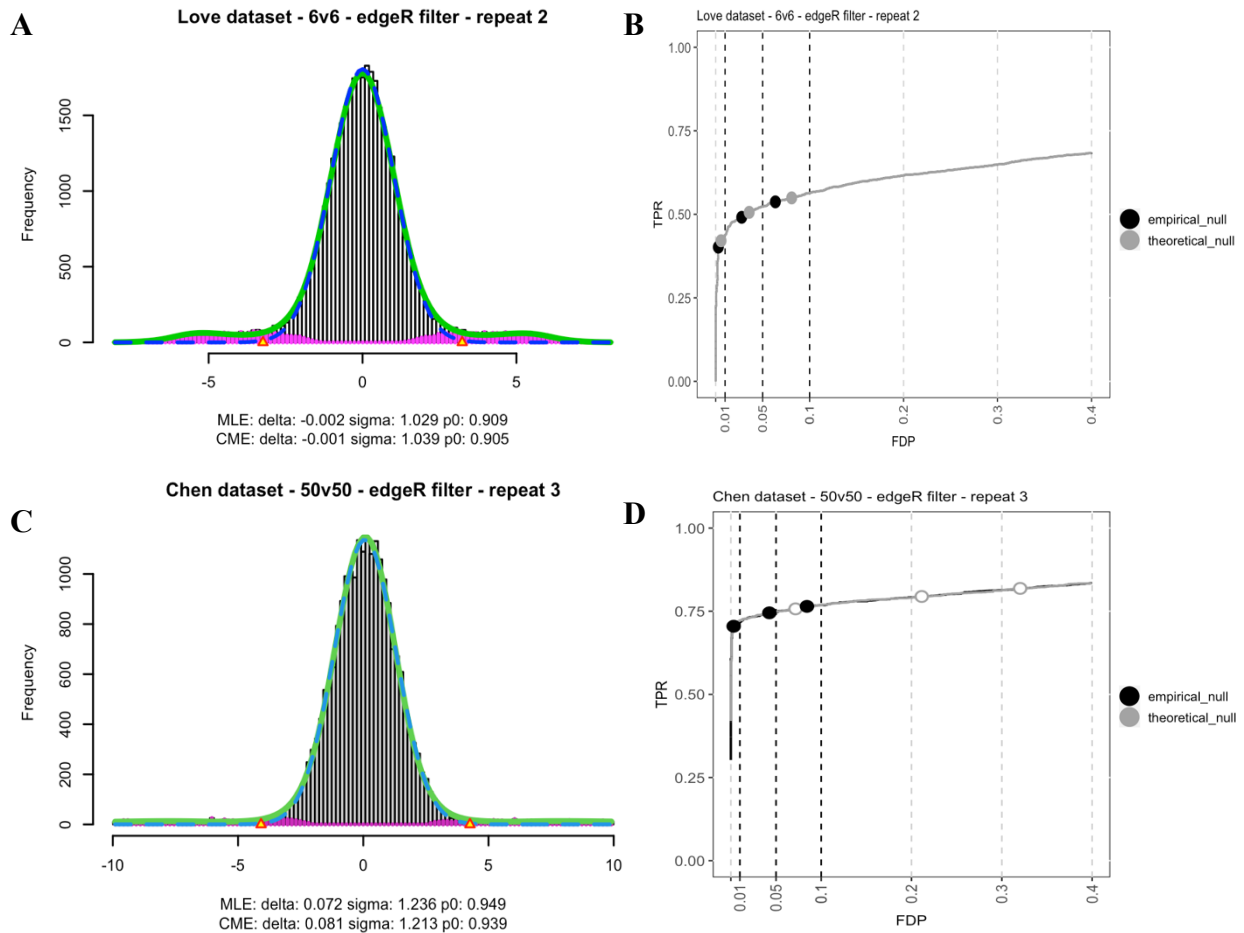
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**Figure S12: The effect of filtering and abundance metrics on the performance of satuRn in the different single-cell RNA-seq benchmark datasets.** For the Tasic (**top row**) and Chen (**middle row**) datasets, the effects of filtering are limited and using counts performs slightly better than using *scaledTPM* abundances. For the Darmanis dataset (**bottom row**), which is the sparsest dataset (see Figure S30 and table S1), a positive impact of the more stringent DRIMSeq filtering criterion is observed.



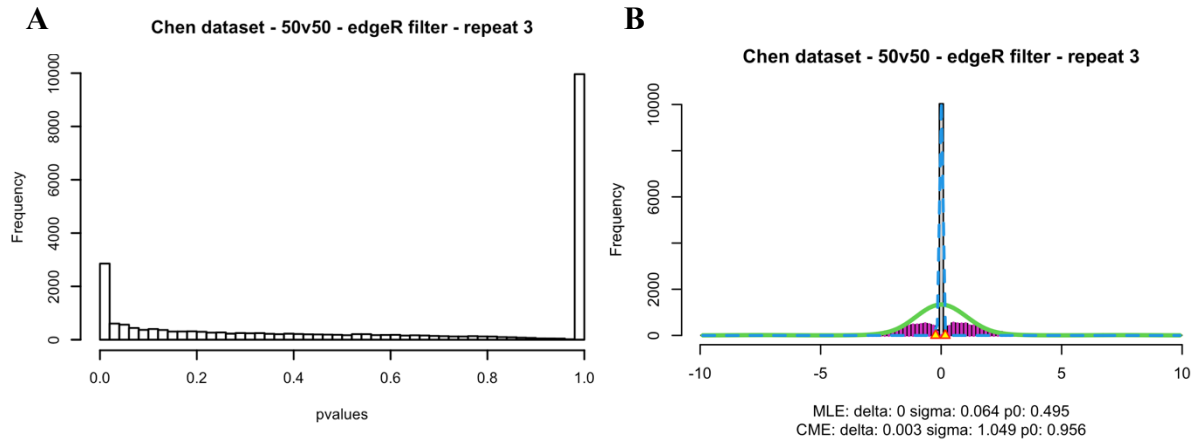
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**Figure S13: The effect of filtering and abundance metrics on the performance of DoubleExpSeq in the different single-cell RNA-seq benchmark datasets.** The observed effects of filtering and abundance metric correspond strongly with the effects observed for on satuRn (figure S12) and limma diffsplice (not shown). For the Tasic (**top row**) and Chen (**middle row**) datasets, the effects of filtering are limited and using counts performs slightly better than using *scaledTPM* abundances. For the Darmanis dataset (**bottom row**), which is the sparsest dataset (see Figure S30 and table S1), a positive impact of the more stringent DRIMSeq filtering criterion is observed.

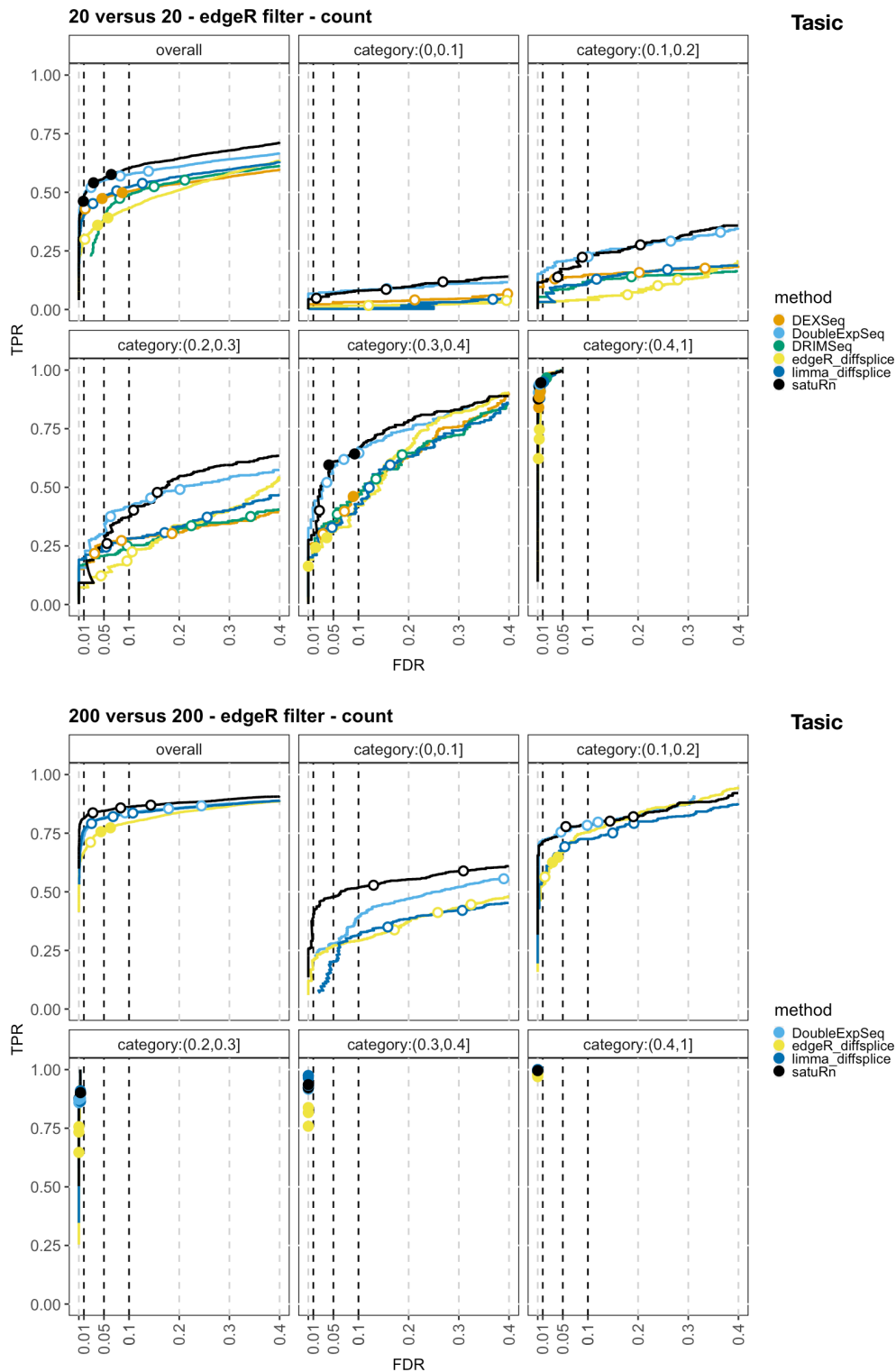


444 **Figure S14: The effect of using an empirical null distribution on the false discovery control of satuRn.** **Panel A:**  
 445 Empirical distribution of the satuRn test statistics in one of the bulk transcriptomics benchmark datasets adapted  
 446 from Love *et al.* The test statistics are z-scores, calculated from satuRn p-values as described in formula 5 (see  
 447 Methods). This benchmark dataset is constructed to have 15% DTU transcripts and thus 85% non-DTU or null  
 448 transcripts. The z-scores corresponding to the null transcripts are expected to follow a standard normal  
 449 distribution (mean = 0, standard deviation = 1). This corresponds well with the maximum likelihood estimates  
 450 (MLE) for the mean and variance of the empirical null distribution (mean = -0.002, standard deviation = 1.029)  
 451 as obtained with the *locfdr* package<sup>2</sup>. In brief, these estimates are obtained by assuming that the z-scores of all  
 452 transcripts follow a mixture distribution, where the z-scores of the null transcripts are expected to follow a  
 453 normal distribution and the z-scores of the DTU transcripts follow some other distribution. Two models are fitted  
 454 to the z-scores. The blue dashed curve is a normal distribution that is fitted to the mid 50% of the z-scores, which  
 455 are assumed to originate from null genes, thus representing the estimated empirical null component densities.  
 456 The MLE and central matching estimates (CME) for the mean and standard deviation of the estimated empirical  
 457 null distribution are provided in the caption at the bottom of the plot. Finally, the green solid curve represents  
 458 the estimated marginal density across all z-scores and is obtained by fitting a spline model to the histogram  
 459 counts. **Panel B:** FDP-TPR curve for the bulk transcriptomics benchmark dataset. As the theoretical null  
 460 distribution and the empirical null distribution are virtually identical, we observe a negligible difference between  
 461 both strategies, both in terms of performance and FDR control. **Panel C:** Empirical distribution of the satuRn test  
 462 statistics in one of the single-cell benchmark datasets adapted from Chen *et al.* Again, most of these z-scores are  
 463 expected to follow a standard normal distribution as this benchmark dataset is also constructed to have 15%  
 464 DTU transcripts. However, the empirical distribution is considerably wider than expected (standard deviation =  
 465 1.236). We additionally observe a small shift of the distribution (mean = 0.072). **Panel D:** FDP-TPR curve for the  
 466 single-cell benchmark dataset. While the inference for satuRn is overly liberal when working under the  
 467 theoretical null, FDR control is restored by adopting the wider empirical null distribution. Note that the  
 468 performance (the ranking of the transcripts according to their p-values) will only be affected when the empirical  
 469 null distribution is shifted with respect to the theoretical null (i.e., when the MLE for the mean is clearly different  
 470 from zero), which was not the case in this example nor in any other dataset from our analyses.



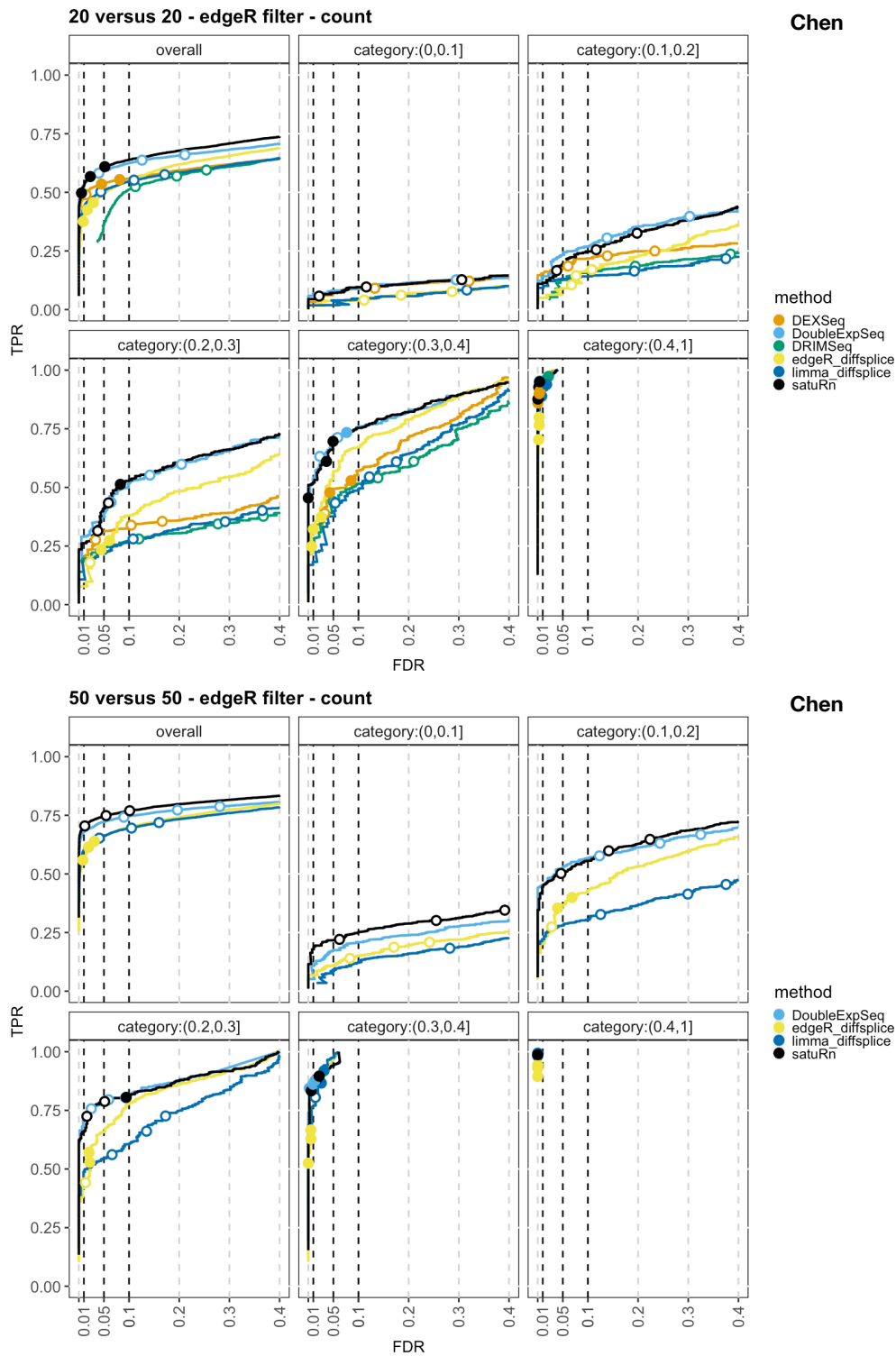


471 **Figure S15: Adopting an empirical null distribution to improve FDR control is infeasible for DoubleExpSeq.**  
 472 **Panel A:** Distribution of the p-values from a DoubleExpSeq analysis in one of the single-cell benchmark datasets  
 473 adapted from Chen *et al.* We immediately observe the large spike of p-values equal to 1, which distorts the p-  
 474 value distribution. In addition, the p-values in the mid-range (e.g., from 0.1 to 0.9), which are expected to be  
 475 uniformly distributed, are skewed towards smaller values, which underlies the overly liberal results of  
 476 DoubleExpSeq in our single-cell benchmarks. **Panel B:** The corresponding empirical distribution of the  
 477 DoubleExpSeq test statistics. The test statistics are z-scores, calculated from the original DoubleExpSeq p-values  
 478 as described in formula 5 (see Methods). As all our benchmark datasets are constructed to have 15% DTU  
 479 transcripts and thus 85% non-DTU or null transcripts, most of these z-scores are expected to follow a standard  
 480 normal distribution (mean = 0, standard deviation = 1). However, given the pathological distribution of the p-  
 481 values it is not feasible to properly estimate the empirical null distribution, as also clearly shown by the widely  
 482 different parameter estimates obtained using the two estimation frameworks implemented in the *locfdr* R  
 483 package<sup>2</sup>; compare the estimates between MLE (maximum likelihood estimation) and CME (central matching  
 484 estimation). For more details on the *locfdr* figures we refer to the caption of figure S10.  
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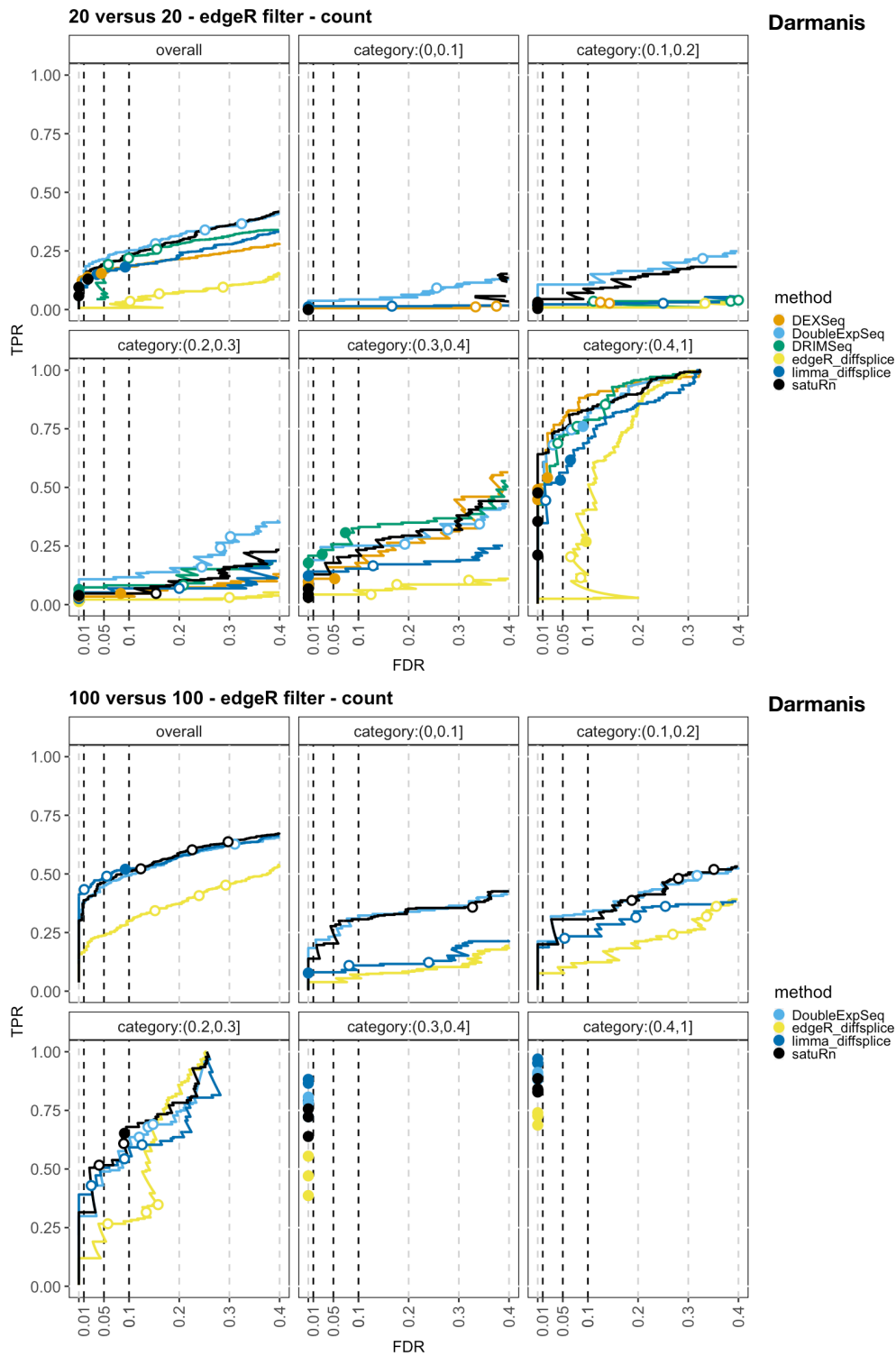
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**Figure S16: Performance evaluation on the real scRNA-seq dataset by Tasic *et al.*, stratified by the magnitude of the DTU signal.** The FDR-TPR curves are stratified on the difference in the observed average transcript usage between the two groups of cells. The difference in the fraction of transcript usage between the two groups is indicated in the panel headers. **Panel A: Dataset with 20 cells per group.** The ability of all methods to detect DTU decreases when the strength of the DTU signal decreases. Notably, satuRn and DoubleExpSeq are more successful in detecting small differences as compared to the other methods. **Panel B: Dataset with 200 cells per group.** Given the larger number of cells, the performance of all methods is increased compared to panel A. Again, satuRn and DoubleExpSeq are the most successful in detecting small differences in transcript usage.



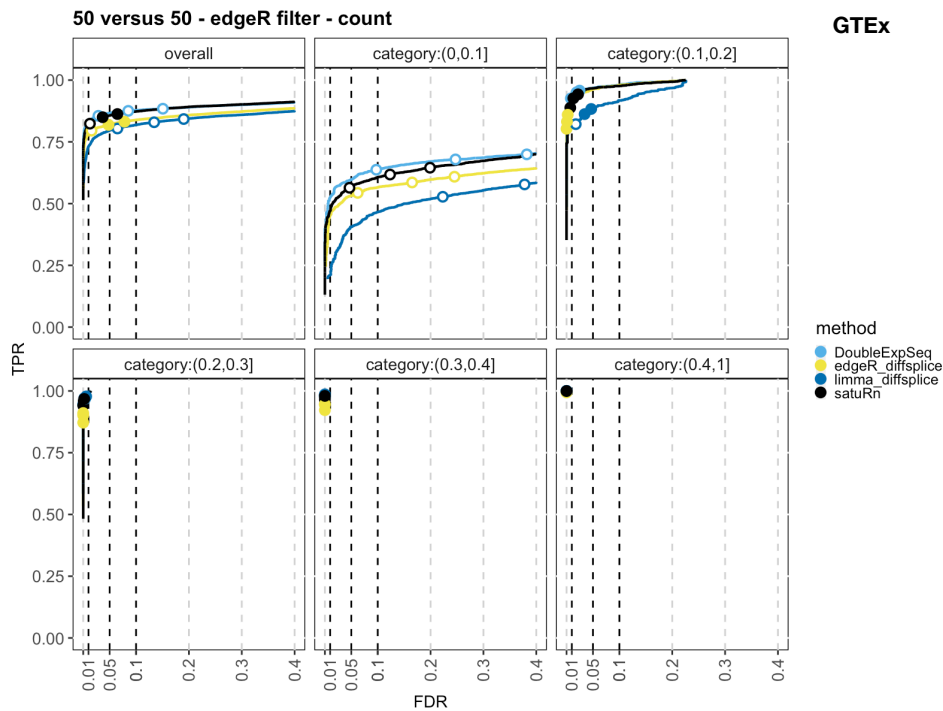
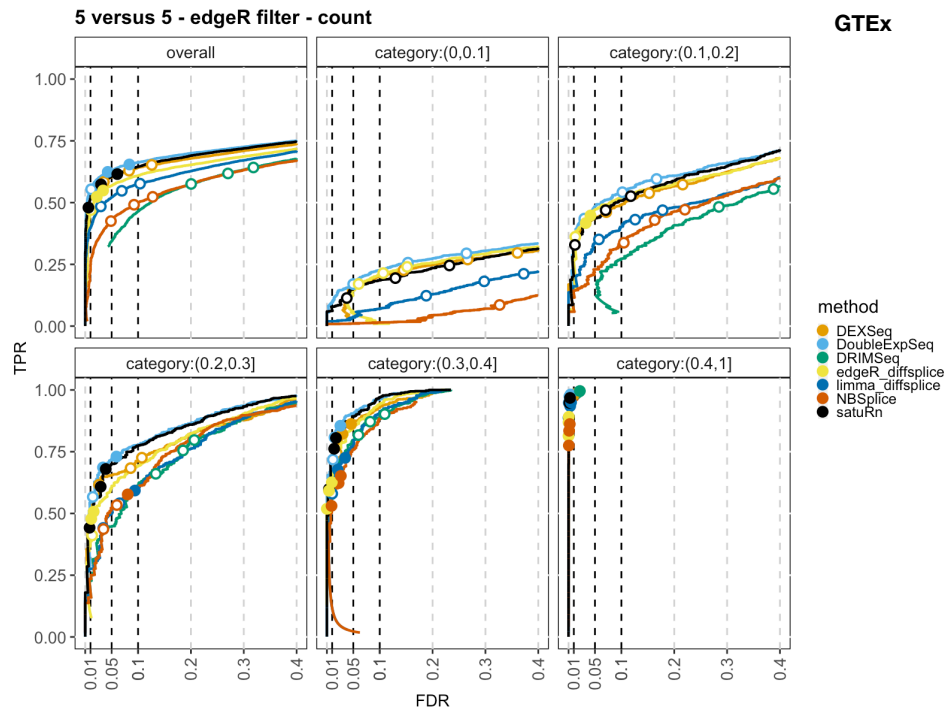
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**Figure S17: Performance evaluation on the real scRNA-seq dataset by Chen *et al.*, stratified by the magnitude of the DTU signal.** The FDR-TPR curves are stratified on the difference in the observed average transcript usage between the two groups of cells. The difference in the fraction of transcript usage between the two groups is indicated in the panel headers. The same patterns are observed as for the Tasic *et al.* dataset from Figure S16. **Panel A: Dataset with 20 cells per group.** The ability of all methods to detect DTU decreases when the strength of the DTU signal decreases. Notably, satuRn and DoubleExpSeq are more successful in detecting small differences as compared to the other methods. **Panel B: Dataset with 50 cells per group.** Given the larger number of cells, the performance of all methods is increased compared to panel A. Again, satuRn and DoubleExpSeq are the most successful in detecting small differences in transcript usage.



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**Figure S18: Performance evaluation on the real scRNA-seq dataset by Darmanis *et al.*, stratified by the magnitude of the DTU signal.** The FDR-TPR curves are stratified on the difference in the observed average transcript usage between the two groups of cells. The difference in the fraction of transcript usage between the two groups is indicated in the panel headers. The same patterns are observed as for the Tasic *et al.* and Chen *et al.* datasets from Figures S16 and S17. **Panel A: Dataset with 20 cells per group.** The ability of all methods to detect DTU decreases when the strength of the DTU signal decreases. Notably, satuRn and DoubleExpSeq are more successful in detecting small differences as compared to the other methods. **Panel B: Dataset with 100 cells per group.** Given the larger number of cells, the performance of all methods is increased compared to panel A. Again, satuRn and DoubleExpSeq are the most successful in detecting small differences in transcript usage.



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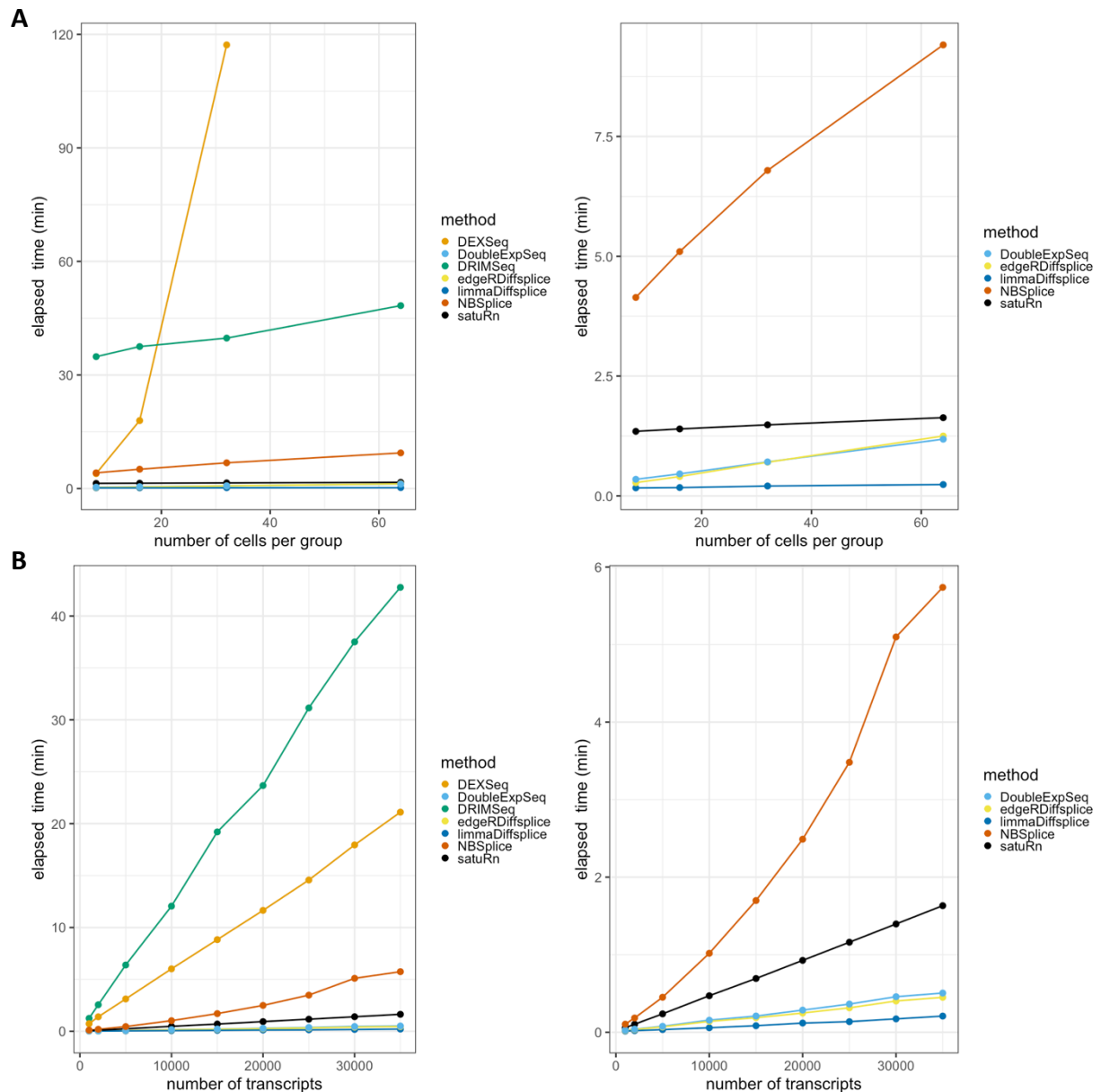
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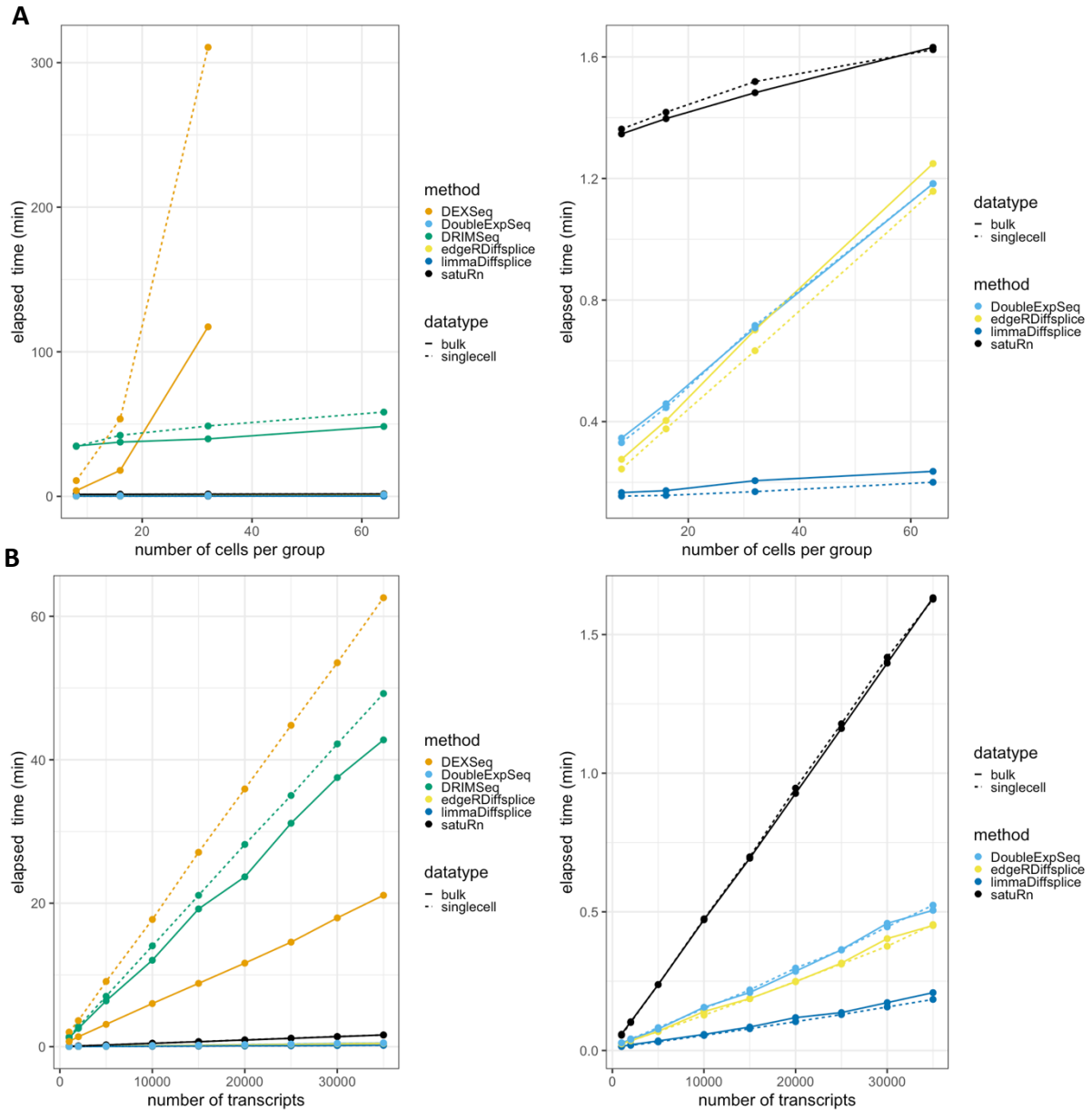
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**Figure S19: Performance evaluation on the GTEx bulk RNA-seq dataset, stratified by the magnitude of the DTU signal.** The FDR-TPR curves are stratified on the difference in the observed average transcript usage between the two groups of cells. The difference in the fraction of transcript usage between the two groups is indicated in the panel headers. The same patterns are observed as for the single-cell datasets from Figures S16-S18. **Panel A: Dataset with 5 samples per group.** The ability of all methods to detect DTU decreases when the strength of the DTU signal decreases. satuRn and DoubleExpSeq are more successful in detecting small differences as compared to the other methods. **Panel B: Dataset with 50 samples per group.** Given the larger number of cells, the performance of all methods is increased compared to panel A. Again, satuRn and DoubleExpSeq are the most successful in detecting small differences in transcript usage. Given the larger sequencing depth of bulk RNA-seq data, fewer observations per group are required to detect small differences in transcript usage as compared to single-cell datasets.



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**Figure S20: Scalability evaluation on bulk RNA-seq data. A: Runtime with respect to the number of samples in a bulk RNA-Seq dataset. Left panel:** DRIMSeq and especially DEXSeq scale poorly with the number of cells in the dataset. **Right panel:** Detailed plot of the fastest methods. satuRn scales linearly with increasing numbers of samples, with a slope that is comparable to that of limma diffsplice. As such, satuRn can perform a DTU analysis on a dataset with two groups of 64 samples each and 30,000 transcripts in less than three minutes. For all sample sizes, the number of transcripts in the datasets were set at 30,000. Note that BANDITS was not included in this analysis as we did not obtain equivalence class counts for the GTEx bulk dataset. NBSplice, which was not included in the single-cell scalability benchmark of Figure 5 because it fails to converge on datasets with a large proportion of zero counts, is included here. **B: Runtime with respect to the number of transcripts in a bulk RNA-seq dataset. Left panel:** DEXSeq and DRIMSeq scale poorly to the number of transcripts in the dataset. **Right panel:** Detailed plot of the remaining methods. satuRn scales linearly with increasing numbers of transcripts, but with a steeper slope than edgeR diffsplice, DoubleExpSeq and limma diffsplice. The number of samples in the dataset was set fixed to two groups of 16 samples. All scalability benchmarks were run on a single core.



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 543 **Figure S21: Comparison of the scalability profiles between bulk RNA-seq and scRNA-seq data. A: Runtime with**  
 544 **respect to the number of cells/samples in the dataset. Left panel:** The scalability of the different DTU tools on  
 545 bulk data is indicated with a full line, while the scalability on single-cell data is displayed with a dashed line. A  
 546 large effect between both data types was only observed for DEXSeq, which scales considerably worse on single-  
 547 cell data, suggesting that the estimation of the GLM parameters is slower with sparse data. However, as the  
 548 scalability profile of DEXSeq is quadratic with respect to the number of cells/samples in the data, it is still  
 549 infeasible to adopt DEXSeq in datasets with many cells/samples, e.g., an analysis with 32 cells in each group  
 550 takes approximately two hours. **Right panel:** detailed plot of the fastest methods. **B: Runtime with respect to**  
 551 **the number of transcripts in the dataset.** The scalability of the different DTU tools on bulk data is indicated with  
 552 a full line, while the scalability on single-cell data is displayed with a dashed line. Again, the largest difference in  
 553 scalability between bulk and single-cell data was observed for DEXSeq. **Right panel:** detailed plot of the fastest  
 554 methods.

Comparison	Cell type 1 (ALM)	Cell type 2 (VlSp)	DoubleExpSeq FDR	Limma FDR	Limma Empirical FDR
1	Cpa6 Gpr88	Batf3	2142	3602	169
2	Cbln4 Fezf2	Col27a1	644	468	297
3	Cpa6 Gpr88	Col6a1 Fezf2	335	1029	77
4	Gkn1 Pcdh19	Col6a1 Fezf2	1878	2861	58
5	Lypd1 Gpr88	Hsd11b1 Endou	829	1411	249
6	Tnc	Hsd11b1 Endou	4580	4819	341
7	Tmem163 Dmrtb1	Hsd11b1 Endou	3388	5603	176
8	Tmem163 Arhgap25	Whrn Tox2	455	1387	166

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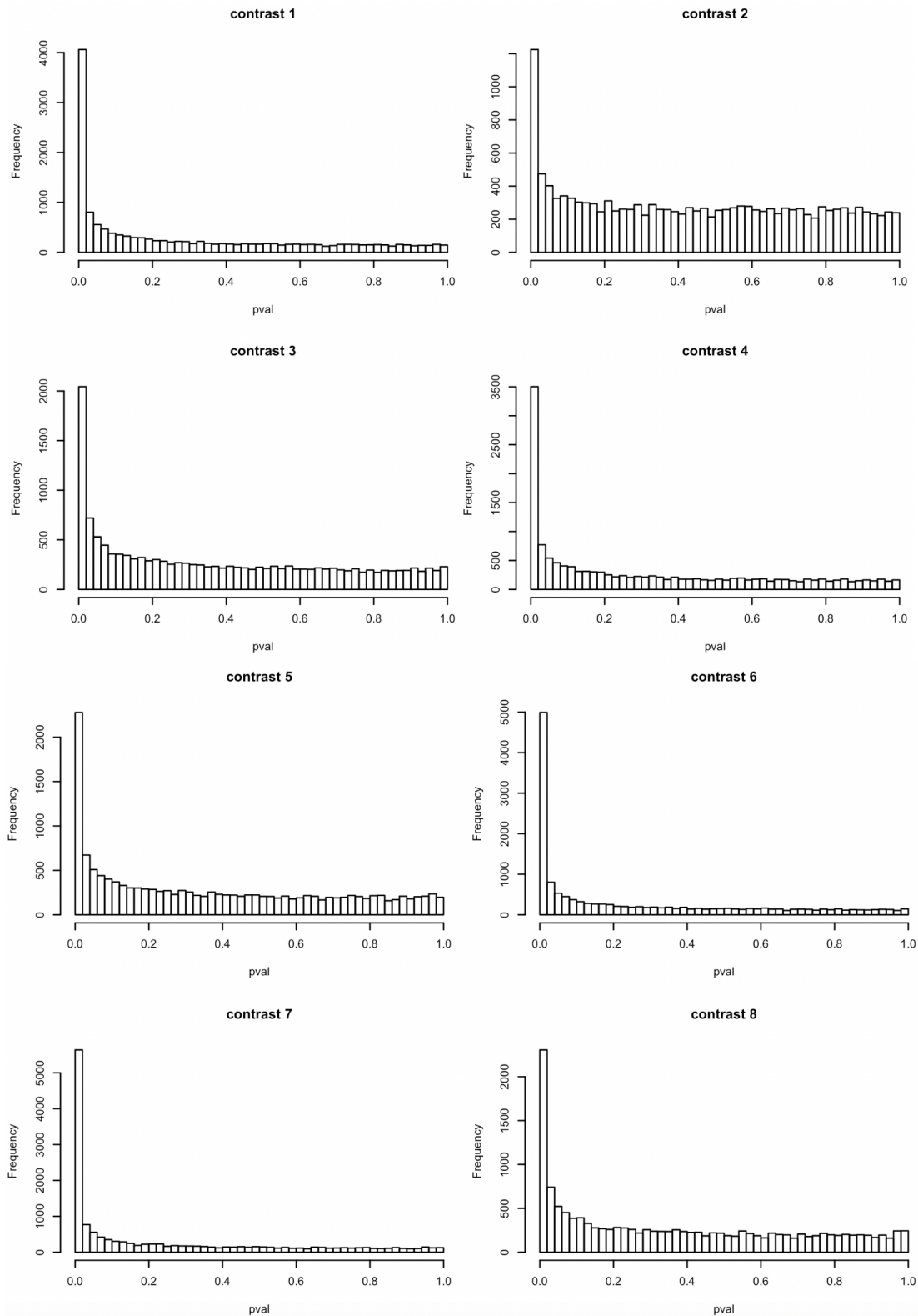
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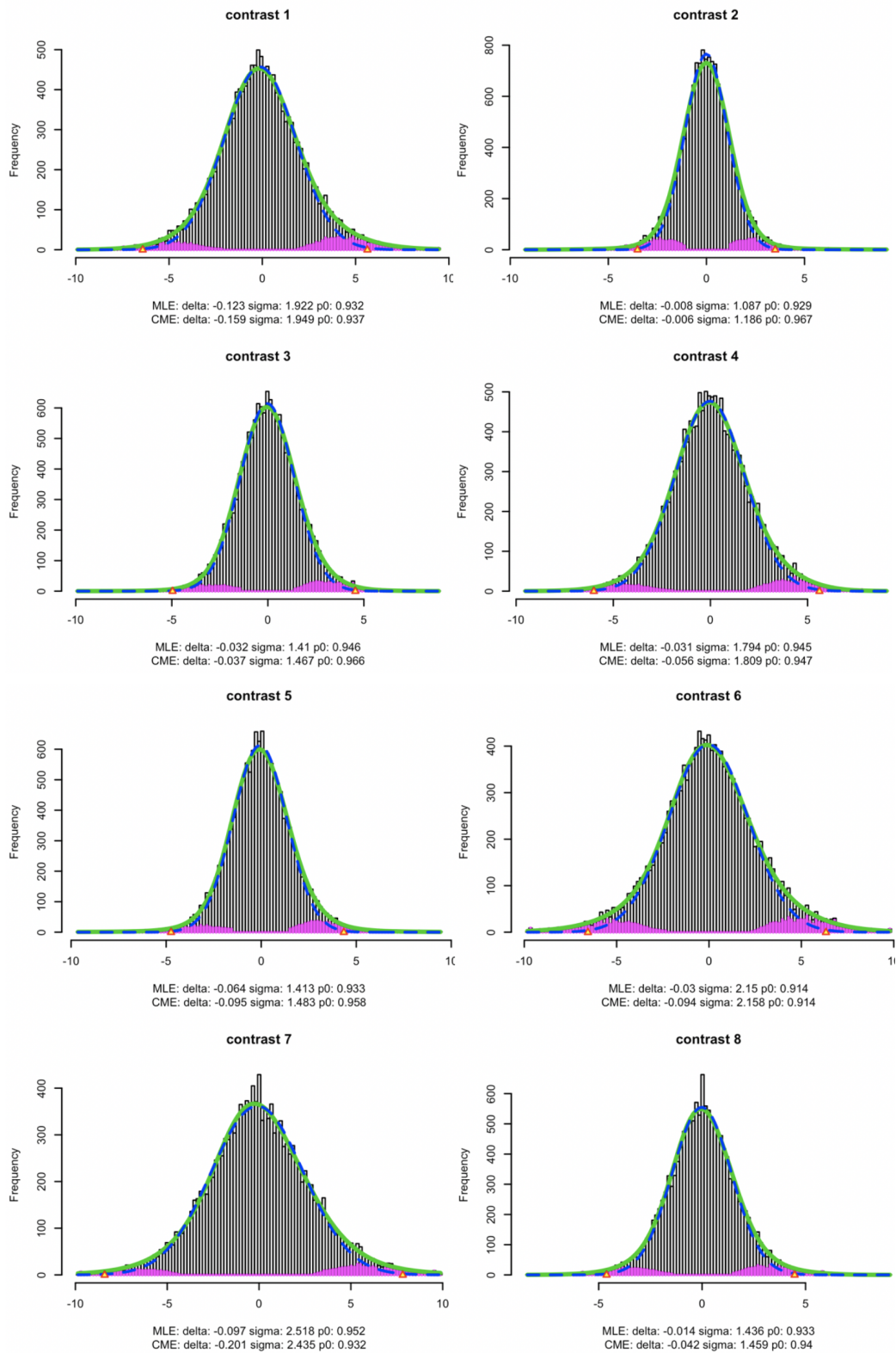
**Figure S22: Number of differentially used transcripts as identified by DoubleExpSeq and limma diffsplice.** The first three columns indicate the comparisons between ALM cell types (column 2) and VlSp cell types (column 3), respectively. Column 4 indicates the number of differentially used transcripts as identified by DoubleExpSeq. Column 5 indicates the number of differentially used transcripts as identified by a limma diffsplice analysis with default settings. Column 6 displays the number of differentially used transcripts found by limma diffsplice after correcting for deviations between the theoretical and empirical null distributions.



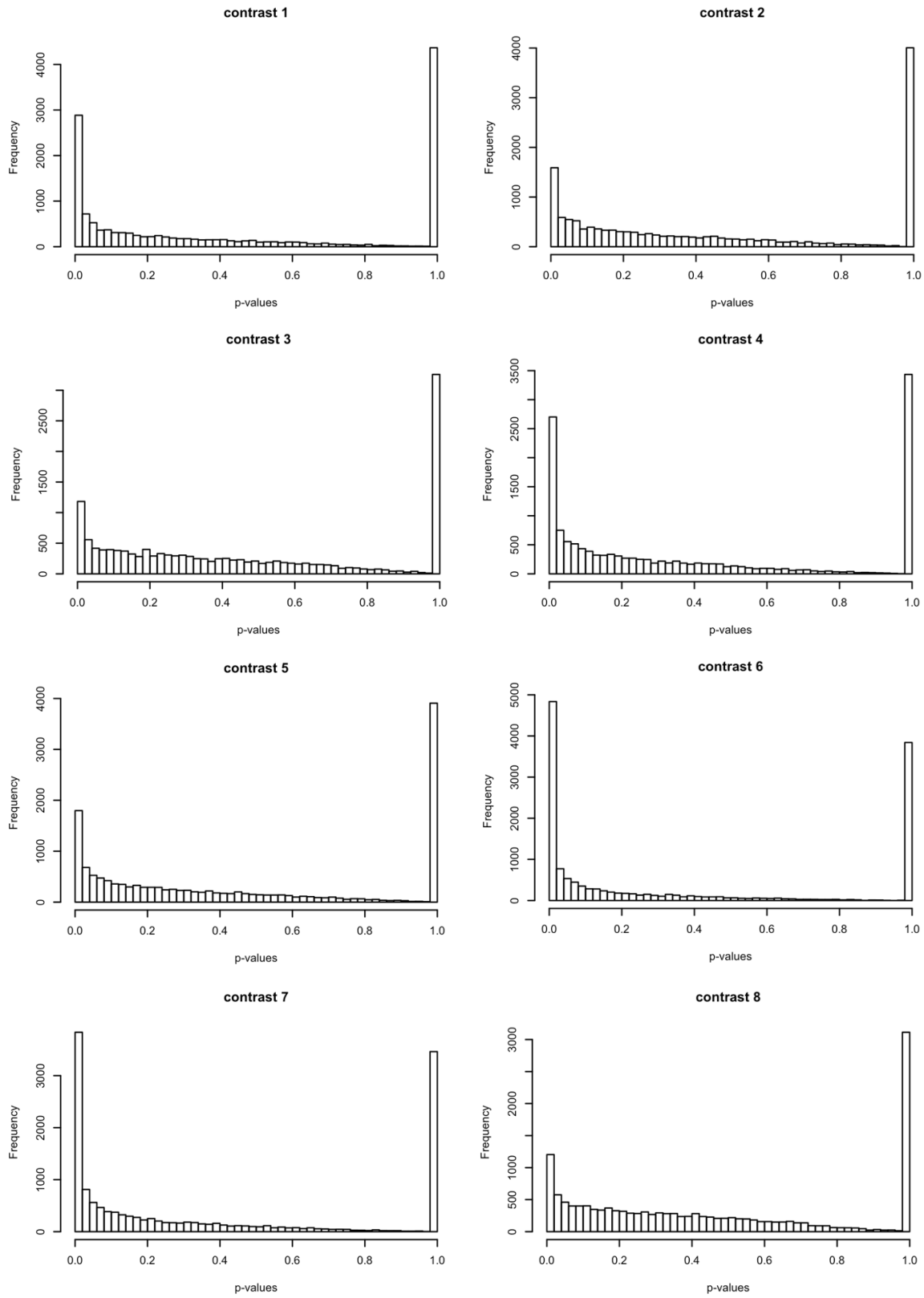


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**Figure S23: Histograms of the p-values from limma diffsplice.** From these histograms, the huge number of DTU transcripts identified by limma diffsplice become apparent. Note that the general tendency of limma diffsplice for smaller p-values is better visible when converting the p-values into z-scores (see Figure S13).

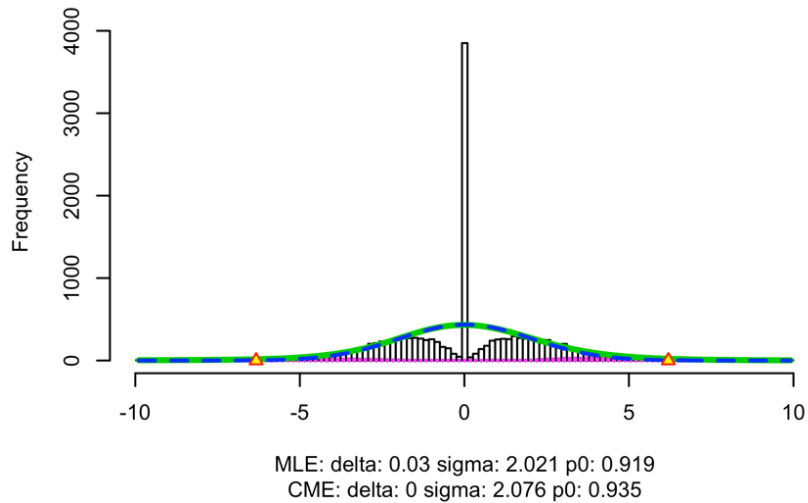


588 **Figure S24: Empirical distribution of the limma diffsplice test statistics.** The test statistics are z-scores,  
589 calculated from limma diffsplice p-values as described in formula 5. Theoretically, these z-scores are expected  
590 to follow a standard normal distribution (mean = 0, standard deviation =1). Here, however, the empirical  
591 distributions are considerably wider (standard deviation > 1), as indicated underneath the plots. This indicates  
592 that the results returned by limma diffsplice in this case study are overly liberal. For more details on the *locfdr*  
593 figures we refer to the caption of figure S14.



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**Figure S25: Histograms of the p-values from DoubleExpSeq.** From these histograms, the huge number of DTU transcripts identified by limma diffsplice become apparent. In addition, we observe a gradual decrease of p-values over the interval  $[0.05 < p < 0.95]$ , with a very large spike of p-values that are exactly 1 in all comparisons or contrasts of interest.



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**Figure S26: Empirical distribution of the test statistics in comparison #6 of the case study with DoubleExpSeq.**

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The test statistics are z-scores, calculated from DoubleExpSeq p-values as described in formula 5 (see Methods).

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Theoretically, the bulk of these z-scores are expected to follow a standard normal distribution (mean = 0,

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standard deviation =1), i.e., assuming that most transcripts are not differentially used. However, the large spike

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of p-values equal to 1 (See Figure S14) results spike of z-scores equal to zero, which poses a problem when

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estimating the empirical null distribution (blue dashed curve). For more details on the *locfdr* figures we refer to

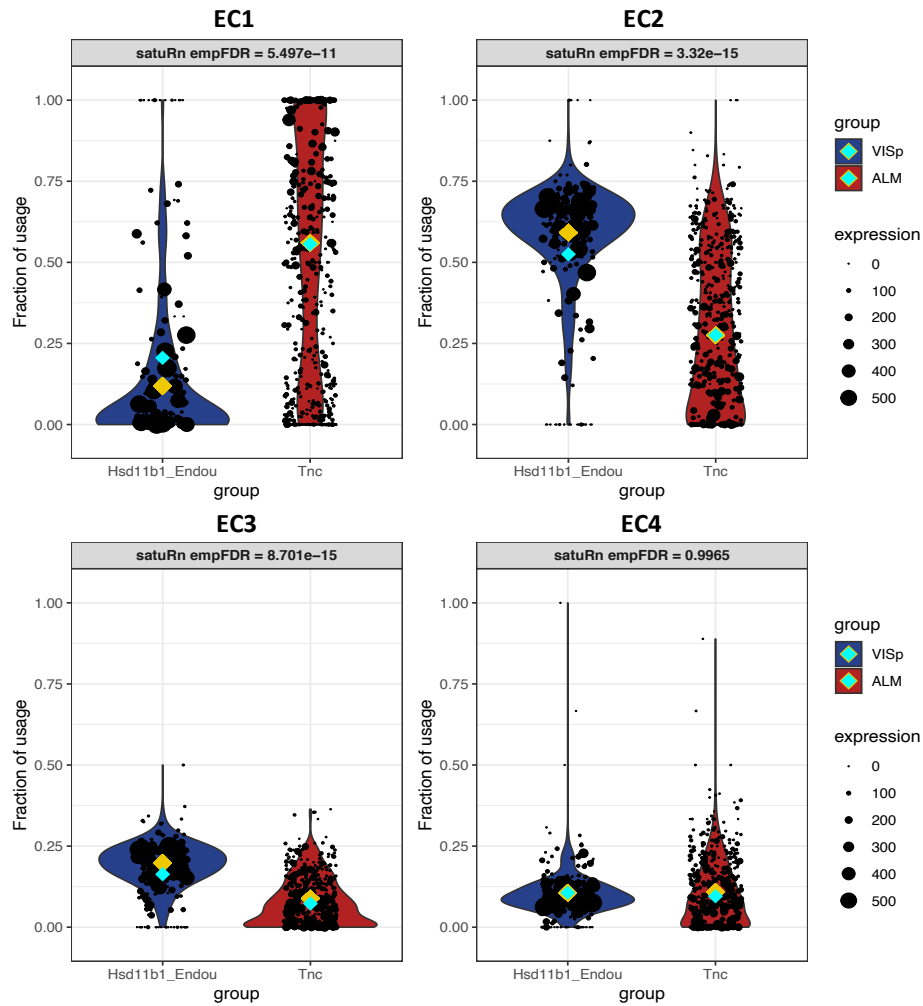
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the caption of figure S14.

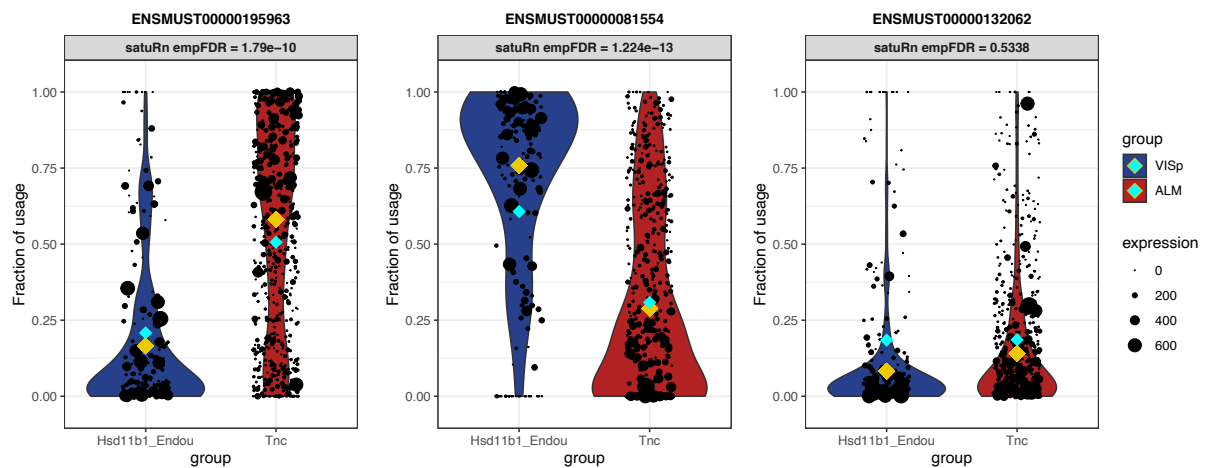
**A**

	EC 1	EC 2	EC 3	EC 4
ENSMUST00000195963	X			
ENSMUST00000031429		X	X	X
ENSMUST00000081554		X	X	X
ENSMUST00000139712			X	
ENSMUST00000139631				X
ENSMUST00000142664				X
ENSMUST00000132062				

**B**



**C**



608 **Figure S27: Differential usage analysis at the EC level and the transcript level for gene P2rx4. Panel A: Link**  
609 **between equivalence classes and transcripts.** Four equivalence classes (ECs) of gene P2rx4 passed feature-level  
610 filtering. EC1 is compatible only with transcript ENSMUST00000195963. Equivalence classes two three and four  
611 are compatible with multiple transcripts. Transcripts that passed feature-level filtering in the transcript-level  
612 DTU analysis are colored green. Note that none of equivalence classes in the filtered data are compatible with  
613 the bottom transcript ENSMUST00000132062. **Panel B: Visualization of DU in the equivalence class analysis.**  
614 Evidence for differential usage is found in EC1, EC2 and EC3. **Panel C: Visualization of DTU in the transcript-level**  
615 **analysis.** Evidence for differential usage is found in transcript ENSMUST00000195963 and transcript  
616 ENSMUST00000081554. The DTU signal ENSMUST00000195963 corresponds directly with the DU signal in EC1,  
617 since EC1 is only compatible with ENSMUST00000195963 and vice versa (panel A). For EC2 and EC3, we cannot  
618 directly make a link with the transcript-level profiles. Because here we performed both types of analyses, we  
619 can infer that while EC2, EC3 and EC4 are compatible with multiple transcripts, the EM algorithm assigned the  
620 majority of reads to transcripts ENSMUST00000081544. If we had to rely only on the EC-level analysis, it would  
621 not be possible to unambiguously assign the differential EC usage to transcript ENSMUST00000081544, as all  
622 equivalence classes are also compatible with transcript ENSMUST00000031429.

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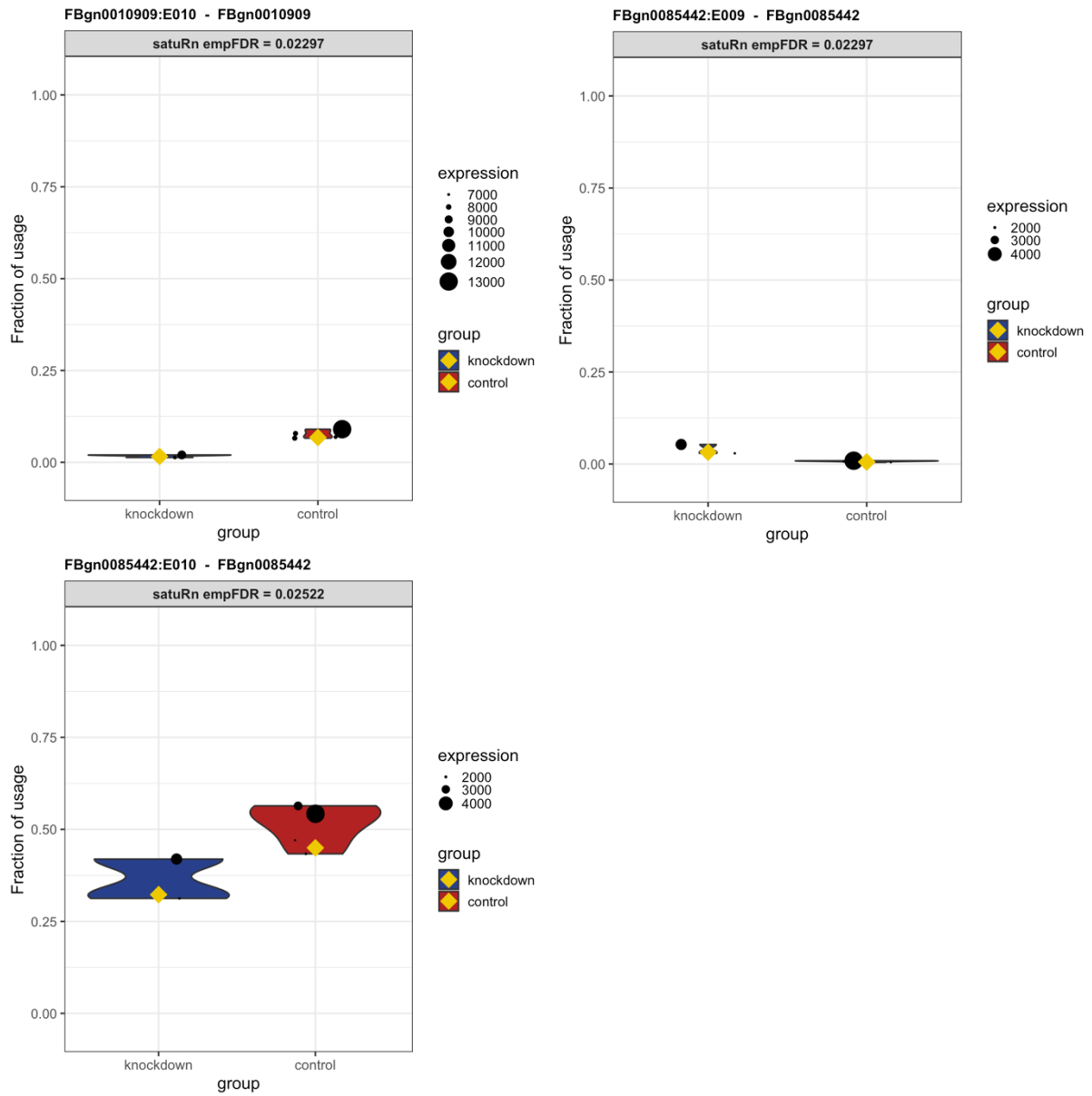
	exon_id	gene_id	rank_satuRn	rank_DEXSeq
114	FBgn0010909:E010	FBgn0010909	1	1
425	FBgn0085442:E009	FBgn0085442	2	2
426	FBgn0085442:E010	FBgn0085442	3	3
9	FBgn0000256:E009	FBgn0000256	4	4
454	FBgn0261573:E010	FBgn0261573	8	5
26	FBgn0000578:E009	FBgn0000578	5	6
177	FBgn0020309:E007	FBgn0020309	6	7
55	FBgn0002921:E015	FBgn0002921	13	8
203	FBgn0027579:E002	FBgn0027579	7	9
202	FBgn0027579:E001	FBgn0027579	9	10
420	FBgn0085442:E004	FBgn0085442	11	11
250	FBgn0032979:E004	FBgn0032979	12	12
52	FBgn0002921:E012	FBgn0002921	18	13
10	FBgn0000256:E010	FBgn0000256	10	14
455	FBgn0261573:E011	FBgn0261573	23	15
46	FBgn0002921:E006	FBgn0002921	15	16
406	FBgn0051352:E017	FBgn0051352	24	17
13	FBgn0000256:E013	FBgn0000256	34	18
388	FBgn0050460:E016	FBgn0050460	29	19
261	FBgn0034158:E006	FBgn0034158	14	20

**B**

	exon_id	gene_id	rank_satuRn	rank_DEXSeq
114	FBgn0010909:E010	FBgn0010909	1	1
425	FBgn0085442:E009	FBgn0085442	2	2
426	FBgn0085442:E010	FBgn0085442	3	3
9	FBgn0000256:E009	FBgn0000256	4	4
26	FBgn0000578:E009	FBgn0000578	5	6
177	FBgn0020309:E007	FBgn0020309	6	7
203	FBgn0027579:E002	FBgn0027579	7	9
454	FBgn0261573:E010	FBgn0261573	8	5
202	FBgn0027579:E001	FBgn0027579	9	10
10	FBgn0000256:E010	FBgn0000256	10	14
420	FBgn0085442:E004	FBgn0085442	11	11
250	FBgn0032979:E004	FBgn0032979	12	12
55	FBgn0002921:E015	FBgn0002921	13	8
261	FBgn0034158:E006	FBgn0034158	14	20
46	FBgn0002921:E006	FBgn0002921	15	16
458	FBgn0261573:E014	FBgn0261573	16	22
401	FBgn0051352:E009	FBgn0051352	17	32
52	FBgn0002921:E012	FBgn0002921	18	13
272	FBgn0034180:E007	FBgn0034180	19	30
31	FBgn0000578:E014	FBgn0000578	20	21

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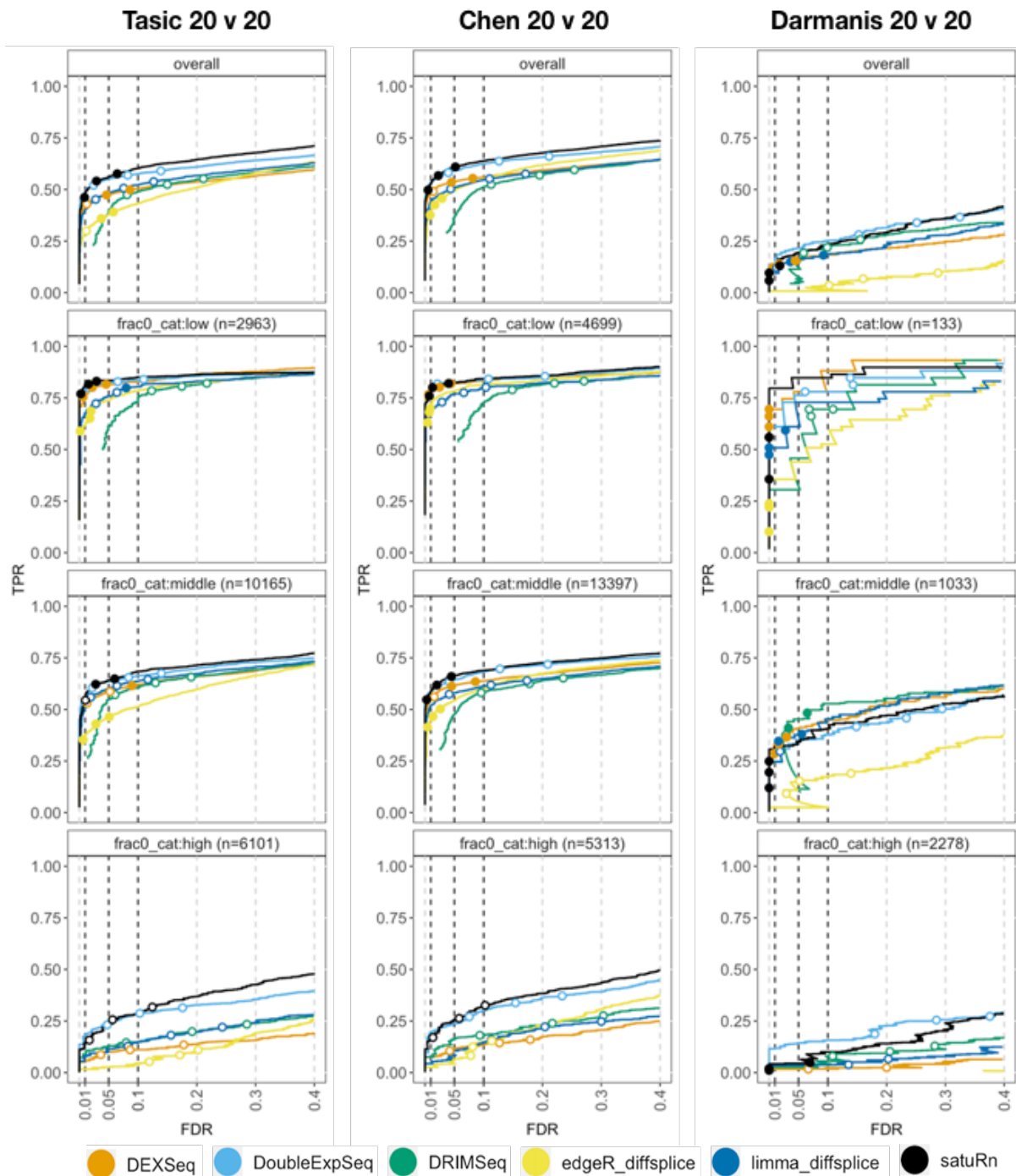
**Figure S28: Comparison of the exons ranked according to p-values between the DEXSeq and satuRn differential exon usage analysis. Panel A:** Top 20 exons for DEXSeq and corresponding rankings for satuRn. **Panel B:** Top 20 exons for satuRn and corresponding rankings for DEXSeq. For both panels, we observe a very strong concordance between the rankings obtained with the DEXSeq analysis and the satuRn analysis.



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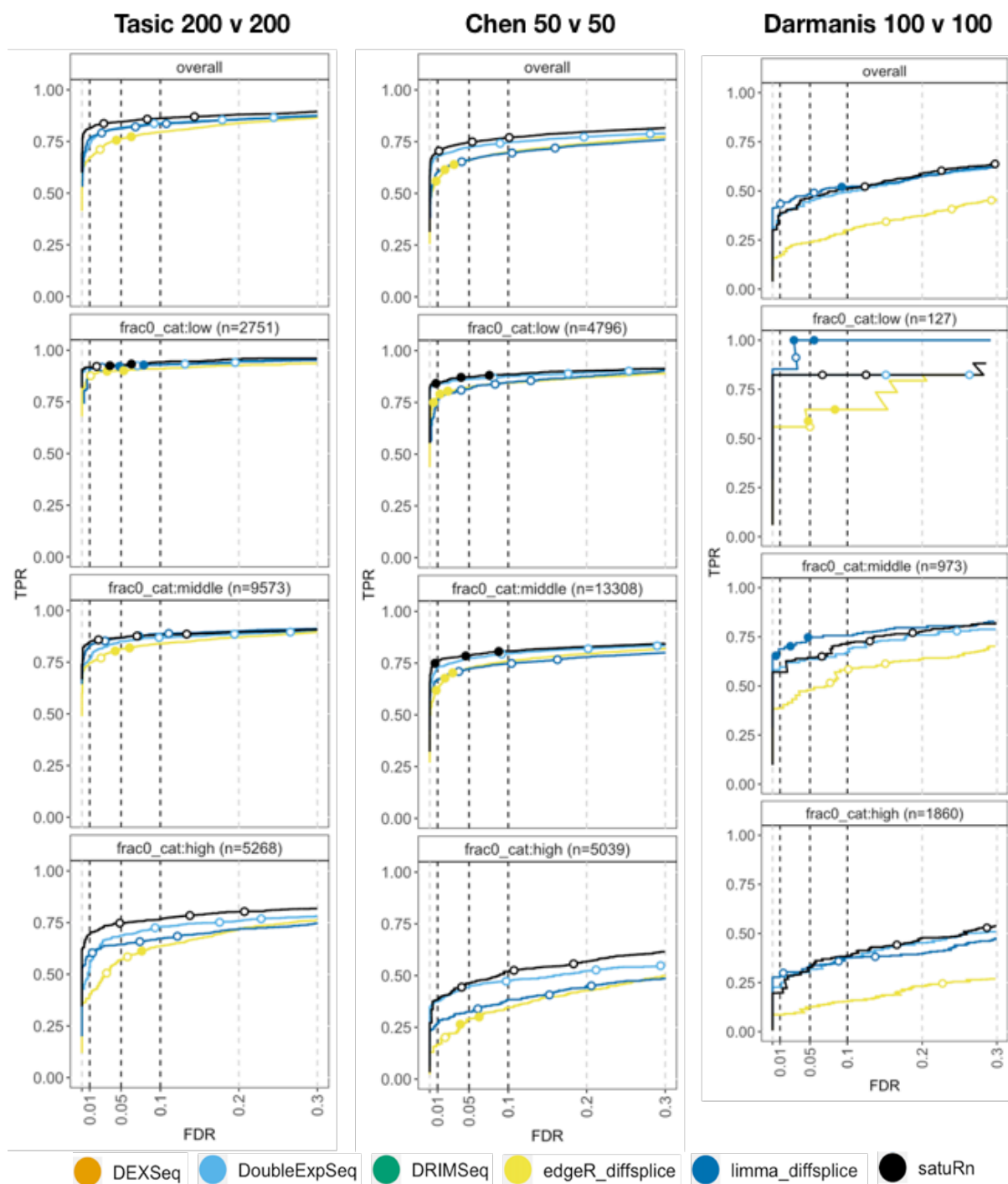
**Figure S29: Visualization of differential exon usage with satuRn.** satuRn visualization of the three exons with an FDR below 5% in the demonstrational differential exon analysis.





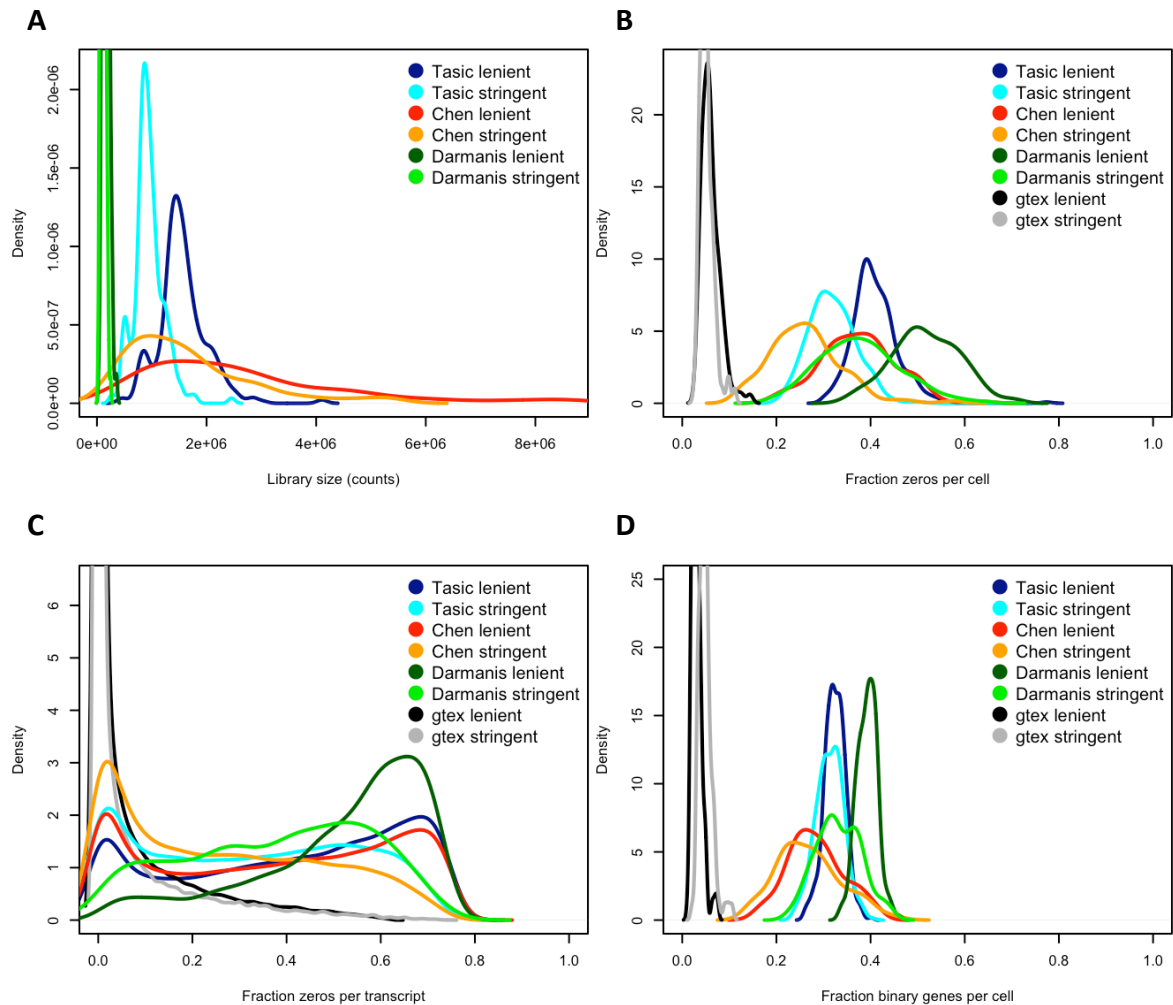
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**Figure S30: Performance evaluation on the smallest subset of the three scRNA-seq datasets, stratified by the percentage of zero counts.** Performances are shown for datasets filtered with edgeR and using raw counts data. The top panels display the performances on the different datasets for all transcripts, as previously displayed in figures 4, S8 and S9. The other panels display the performances on different subsets of transcripts. The three strata correspond to transcripts of genes that have a low (< 25%), middle (25-50%) or high (> 50%) percentage of zero counts in their corresponding transcript-level count matrices. The number of transcripts in each stratum is indicated in the header of each panel. The performances are relatively similar between the different datasets within the same stratum. However, given that the number of transcripts in the stratum with the highest percentage zero counts is proportionally much higher in for the Darmanis dataset, the overall performances (top panel) on this dataset are markedly lower than for the other datasets.



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**Figure S31: Performance evaluation on the largest subsets of the three scRNA-seq datasets stratified by the percentage of zero counts.** Performances are shown for datasets filtered with edgeR and using raw counts data. The top panels display the performances on the different datasets for all transcripts, as previously displayed in figures 4, S8 and S9. The other panels display the performances on different subsets of transcripts. The three strata correspond to transcripts of genes that have a low (< 25%), middle (25-50%) or high (> 50%) percentage of zero counts in their corresponding transcript-level count matrices. The number of transcripts in each stratum is indicated in the header of each panel. The performances are relatively similar between the different datasets within the same stratum. However, given that the number of transcripts in the stratum with the highest percentage zero counts is proportionally much higher in for the Darmanis dataset, the overall performances (top panel) on this dataset are markedly lower than for the other datasets.



661 **Figure S32: Properties of the three different scRNA-seq datasets.** Datasets included are the largest subset of  
 662 the Tasic dataset (400 cells), the Chen dataset (100 cells) and the Darmanis dataset (200 cells). The datasets  
 663 were either filtered using edgeR (lenient) or DRIMSeq (stringent). **Panel A:** Density plot of the library sizes. The  
 664 densities are obtained as the total sum of the counts per cell in each dataset. Library sizes are smallest for the  
 665 Darmanis dataset. The mode of the densities for the Tasic dataset and the Chen dataset are similar, however,  
 666 the spread is considerably larger for the Chen dataset. **Panel B:** Density plot of the fraction of zero counts per  
 667 cell. The fraction of zero counts per cell is largest for the Darmanis dataset (modes of around 55% and 35%),  
 668 followed by the Tasic dataset (modes of around 40% and 30%) and the Chen dataset (modes of around 35% and  
 669 25%). Adopting the more stringent transcript-level filtering criterion of DRIMSeq naturally reduces the  
 670 percentage of zero counts. As a comparison, the fraction of zero counts on the bulk RNA-seq GTEx dataset (100  
 671 samples) was included as a reference (modes of around 5%). **Panel C:** Density plot of the fraction of zero counts  
 672 per transcript. Similar to panel B, the percentage zero counts per transcript is highest for the Darmanis dataset,  
 673 followed by the Tasic dataset, the Chen dataset and the GTEx dataset. **Panel D:** Fraction of binary genes per cell.  
 674 A gene is called binary in a cell if only 1 isoform of that gene is expressed in that cell. Again, the highest fraction  
 675 of fraction of binary genes is observed of cells from the Darmanis dataset, followed by the Tasic dataset, the  
 676 Chen dataset and the GTEx dataset.

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Tasic	20 v 20 lenient	200 v 200 lenient	20 v 20 stringent	200 v 200 stringent	raw
<b>n_transcripts</b>	19229	17591	9881	9074	99436
<b>overall_zero (%)</b>	41,66	41,01	32,44	32,01	83,34
<b>binary (%)</b>	32,1	32,41	31,19	31,33	24,86
<b>all_zero (%)</b>	11,17	11,46	9,11	9,24	51,7
Chen	20 v 20 lenient	50 v 50 lenient	20 v 20 stringent	50 v 50 stringent	raw
<b>n_transcripts</b>	23409	23143	11277	11209	99280
<b>overall_zero (%)</b>	38,29	37,58	26,46	26,07	78,26
<b>binary (%)</b>	29,21	28,76	27,65	27,2	25,15
<b>all_zero (%)</b>	8,94	8,75	5,86	5,83	42,82
Darmanis	20 v 20 lenient	100 v 100 lenient	20 v 20 stringent	100 v 100 stringent	raw
<b>n_transcripts</b>	3444	2961	844	769	175100
<b>overall_zero (%)</b>	53,41	51,85	39,2	37,61	95,36
<b>binary (%)</b>	39,62	39,34	33,88	32,79	15,69
<b>all_zero (%)</b>	27,99	26,97	17,91	16,87	77,55
GTEX	5 v 5 lenient	50 v 50 lenient	5 v 5 stringent	50 v 50 stringent	raw
<b>n_transcripts</b>	54019	55435	26630	26945	162972
<b>overall_zero (%)</b>	4,81	6,13	4,91	5,21	46,22
<b>binary (%)</b>	2,49	3,15	4,71	4,98	14,62
<b>all_zero (%)</b>	0,05	0,09	0,2	0,21	15,48

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		Cell 1	Cell 2
<b>Gene A</b>	Transcript 1	0	0
<b>Gene A</b>	Transcript 2	5	0
<b>Gene A</b>	Transcript 3	0	0
<b>Category</b>		Binary	All_zero

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**Table S1: Summary statistics for the GTEx bulk dataset and the three scRNA-seq datasets. Panel A:** Dataset identifiers are indicated in the top-left cell. The column headers specify the number of samples/cells of each subset and the adopted filtering strategy (lenient for edgeR, stringent for DRIMSeq). The column “raw” indicates the unfiltered count matrix including all cells and all samples, i.e., the raw output of the quantification procedures. The row “**N\_transcripts**” indicates the number of transcripts retained in the dataset. “**Overall\_zero**” is the percentage of zero values in the count matrix. “**Binary**” is computed on the gene level. For each gene, the fraction of cells that have a binary transcript usage pattern where only a single transcript of the gene is expressed (as indicated in panel B) is computed. Next, the mean of these fractions (over the genes) is taken. Such binary count profiles are less informative than profiles with counts for multiple transcripts within the same gene<sup>3</sup>. The transcript usage fractions will be zero and infinity, respectively, regardless of the count value of the expressed transcript. The computation of “**All\_zero**” is similar to that of “**Binary**”, however, here the fraction of cells that have only zero count values is computed for each gene and averaged over the genes, as indicated in panel B.

699 **References**

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