

Determinant based Fully Automatic one Scan Adaptive Image Scaling Algorithm

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ABSTRACT

Image Scaling is defined as the resizing of images either by means of up-scaling or down-scaling. Various Algorithm such as Nearest-neighbor interpolation, Bilinear and bicubic algorithms, Sinc and Lanczos resampling, Box sampling, Mipmap, Fourier-transform methods, Edge-directed interpolation, hqx, Vectorization and Deep convolutional neural networks are available to perform image scaling. Carlo Arcelli et al. proposed a fully automatic one scan adaptive image scaling algorithm in which expanded pixel is found by the sum of weighted neighboring pixel. This paper proposes a same fully automatic one scan adaptive image scaling algorithm in which expanded pixel is found by the determinant of weighted neighboring pixel instead of summation. Finally both the existing and proposed algorithm is compared by means of PSNR and SSIM.

Keywords: Algorithm, PSNR, SSIM

INTRODUCTION

Image zooming algorithm plays a vital role in various application especially in medical field. For example if the doctor wants to check whether the patient is affected by ulcer then the doctor will take scan on the stomach in which affected area will be clearly viewed by the means of zooming process.

If the image is broken when the scanned image is zoomed then the doctor will not correctly predict whether the patient is affected by ulcer or not. Hence it is required to get better image quality when the image is zoomed. The better image quality can be recognized by means of PSNR and SSIM value.

The various basic algorithms used for performing image scaling are Nearest-neighbor interpolation, Bilinear and bicubic algorithms, Sinc and Lanczos

resampling, Box sampling, Mipmap, Fourier-transform methods, Edge-directed interpolation, hqx, Vectorization and Deep convolutional neural networks. In nearest neighbor interpolation, each pixel in the zoomed version is replaced by its neighboring pixel and we can preserve sharp details but introduces the jaggedness in the zoomed image.

In bilinear and bicubic algorithm, it introduces continuous transition for interpolating pixel color values into the output (zoomed image) even the original image has discrete transition. In Sinc resampling, there is a better reconstruction for zoomed image for a perfectly band-limited signal.

An approximation of the Sinc method called Lanczos resampling which produces better result compared to Sinc resampling. Also there is a computationally efficient

approximation of the Lanczos resampling method is called Bicubic interpolation.

The methods till now discussed to perform image zooming has a limitation that to sample only the limited number of pixel. To avoid this, we introduce box sampling in which the algorithm samples non adjacent pixel when the down scaling below a certain threshold value. The threshold value is the twice for all bi-sampling algorithms. The optimization technique is very hard to done for this algorithm.

To solve this problem, another method called mipmap which is a prescaled set of downscale copies. This algorithm ensures that there is no scaling happens below the threshold of bilinear scaling. To preserve the edges of the zoomed image, edge directed interpolation is used. Also, image scaling can be done using vectorization and deep convolutional neural network.

For the zooming factor of 2,

$$\begin{aligned} q(1,1) &= 4 * p + 1 * tl + 2 * t + 2 * l \\ q(1,2) &= 4 * p + 2 * t + 1 * tr + 2 * r \\ q(2,1) &= 4 * p + 2 * l + 1 * bl + 2 * b \\ q(2,2) &= 4 * p + 2 * b + 1 * br + 2 * r \end{aligned}$$

For the zooming factor of 3,

$$\begin{aligned} q(1,1) &= 9 * p + 6 * l + 6 * t + 4 * tl \\ q(1,2) &= 9 * p + 3 * l + 6 * t + 2 * tl + 2 * tr + 3 * r \\ q(1,3) &= 9 * p + 6 * t + 4 * tr + 6 * r \\ q(2,1) &= 9 * p + 6 * l + 3 * t + 2 * tl + 3 * b + 2 * bl \\ q(2,2) &= 9 * p + 3 * l + 3 * r + 3 * b + bl + br + 3 * t + tl + tr \\ q(2,3) &= 9 * p + 6 * r + 3 * b + 2 * br + 3 * t + 2 * tr \\ q(3,1) &= 9 * p + 6 * l + 4 * bl + 6 * b \\ q(3,2) &= 9 * p + 3 * l + 3 * r + 2 * bl + 6 * b + 2 * br \\ q(3,3) &= 9 * p + 6 * r + 6 * b + 4 * br \end{aligned}$$

For the zooming factor of 4,

$$\begin{aligned} q(1,1) &= 6 * l + 4 * tl + 6 * t + 9 * p \\ q(1,2) &= 3 * l + 2 * tl + 8 * t + 12 * p \\ q(1,3) &= 8 * t + 2 * tr + 3 * r + 12 * p \\ q(1,4) &= 6 * t + 4 * tr + 6 * r + 12 * p \\ q(2,1) &= 8 * l + 2 * tl + 3 * t + 12 * p \end{aligned}$$

Carlo Arcelli et al proposes the fully automatic one scan adaptive image scaling algorithm. This paper shows the WAZ algorithm is best compared to other interpolation methods such as nearest neighbor, bilinear and bicubic interpolation, etc. This WAZ algorithm is more convenient for performing image scaling compared to ALZ.[1-3]

EXISTING ALGORITHM – WEIGHTED SUM

The algorithm for the fully automatic one scan adaptive image scaling algorithm is shown below:

- Step 1: Load the input color image.
- Step 2: Separate the three color components R, G, and B plane from the color image.
- Step 3: Identify the eight neighbors of each pixel in each color components.
- Step 4: Expand each pixel for n x n matrix named it as ‘q’ using weighted sum.

$$\begin{aligned}
 q(2,2) &= 4 * l + tl + 4 * t + 16 * p \\
 q(2,3) &= 4 * t + tr + 4 * r + 16 * p \\
 q(2,4) &= 12 * p + 8 * r + 2 * tr + 3 * t \\
 q(3,1) &= 12 * p + 3 * b + 2 * bl + 8 * l \\
 q(3,2) &= 16 * p + 4 * b + bl + 4 * l \\
 q(3,3) &= 16 * p + 4 * b + br + 4 * r \\
 q(3,4) &= 12 * p + 3 * b + 2 * br + 8 * r \\
 q(4,1) &= 9 * p + 6 * l + 4 * bl + 6 * b \\
 q(4,2) &= 12 * p + 3 * l + 2 * bl + 8 * b \\
 q(4,3) &= 12 * p + 8 * b + 2 * br + 3 * r \\
 q(4,4) &= 9 * p + 6 * b + 4 * br + 6 * r
 \end{aligned}$$

where p is the value of the pixel, and l, r, t, b, tl, tr, bl, and br are the neighbors of the pixel p.

Step 5: After computing q matrix find the maximum and minimum value in the q matrix.

Step 6: Find the value of Δ by using the formula

$$\Delta = \min_{q_k \neq p} \{|q_k - p|\}$$

Step 7: Find the value of T by using the formula

$$T = \begin{cases} q_{max} + q_{min} - p & \text{if } (q_{max} + q_{min})/2 \neq p \\ p & \text{if } (q_{max} + q_{min})/2 = p \end{cases}$$

Step 8: Find the final value of the pixel in q matrix is obtained by

$$q_k = \begin{cases} q_k - \Delta & \text{if } p \leq q_{min} \text{ for any } q_k > p \\ q_k + p & \text{if } p \geq q_{max} \text{ for any } q_k < p \\ \min(255, q_k + \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k \geq T \\ \min(0, q_k - \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k < T \end{cases}$$

Step 9: Finally calculate the PSNR and SSIM between the input and zoomed algorithm.

$$PSNR = 20 \log_{10} \left(\frac{255}{\sqrt{MSE}} \right)$$

where MSE is the mean square error.

$$SSIM = \frac{(2\mu_v\mu_w + c_1)(2cov_{vw} + c_2)}{(\mu_v^2 + \mu_w^2 + c_1)(\sigma_v^2 + \sigma_w^2 + c_2)}$$

μ_v is the mean of the input image

μ_w is the mean of the zoomed image

σ_v^2 is the variance of the input image

σ_w^2 is the variance of the zoomed image

$c_1 = (k_1L)^2$ and $c_2 = (k_2L)^2$

$k_1 = 0.01$; $k_2 = 0.03$ and $L = 255$

The Pseudo code for the fully automatic one scan adaptive image scaling algorithm is shown below:

P ← Input image

Q ← Output image

N ← zooming factor

for each pixel in p do

tl=p(i-1,j-1,k);

t=p(i-1,j,k);

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tr=p(i-1,j+1,k);
l=p(i,j-1,k);
p=p(i,j,k);
r=p(i,j+1,k);
bl=p(i+1,j-1,k);
b=p(i+1,j,k);
br=p(i+1,j+1,k);
end for
for each pixel in p do
for i = 1 to n do
if N=2 do
q(1,1)=4*p+1*tl+2*t+2*l;
q(1,2)=4*p+2*t+1*tr+2*r;
q(2,1)=4*p+2*l+1*bl+2*b;
q(2,2)=4*p+2*b+1*br+2*r;
elseif N=3 do
q(1,1)=9*p+6*l+6*t+4*tl;
q(1,2)=9*p+3*l+6*t+2*tl+2*tr+3*r;
q(1,3)=9*p+6*t+4*tr+6*r;
q(2,1)=9*p+6*l+3*t+2*tl+3*b+2*bl;
q(2,2)=9*p+3*l+3*r+3*b+bl+br+3*t+tl+tr;
q(2,3)=9*p+6*r+3*b+2*br+3*t+2*tr;
q(3,1)=9*p+6*l+4*bl+6*b;
q(3,2)=9*p+3*l+3*r+2*bl+6*b+2*br;
q(3,3)=9*p+6*r+6*b+4*br;
else // N=4
q(1,1)=6*l+4*tl+6*t+9*p;
q(1,2)=3*l+2*tl+8*t+12*p;
q(1,3)=8*t+2*tr+3*r+12*p;
q(1,4)=6*t+4*tr+6*r+12*p;
q(2,1)=8*l+2*tl+3*t+12*p;
q(2,2)=4*l+tl+4*t+16*p;
q(2,3)=4*t+tr+4*r+16*p;
q(2,4)=12*p+8*r+2*tr+3*t;
q(3,1)=12*p+3*b+2*bl+8*l;
q(3,2)=16*p+4*b+bl+4*l;
q(3,3)=16*p+4*b+br+4*r;
q(3,4)=12*p+3*b+2*br+8*r;
q(4,1)=9*p+6*l+4*bl+6*b;
q(4,2)=12*p+3*l+2*bl+8*b;
q(4,3)=12*p+8*b+2*br+3*r;
q(4,4)=9*p+6*b+4*br+6*r;
end if
end for
if (qk ≠ p) do
Δ = min (|qk - p|)
end if
if (q max + qmin)/2 ≠ p do
t = q max + qmin - p
```

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else
T = P
end if
if ( p ≤ qmin && qk > p) do
qk = qk - Δ
else if (p ≥ qmax && qk < p) do
qk = qk + Δ
else if ((qmin < p < qmax) && (qk ≥ T)) do
qk = min(255, qk + Δ)
else
qk = min (0, qk - Δ)
end if
end for

```

PROPOSED ALGORITHM – DETERMINANT BASED

The algorithm for the determinant based fully automatic one scan adaptive image scaling algorithm is shown below:

Step 1: Load the input color image.

Step 2: Separate the three color components R, G, and B plane from the color image.

Step 3: Identify the eight neighbors of each pixel in each color components.

Step 4: Expand each pixel for n x n matrix named it as 'q' using determinant of weighted pixel.

For the zooming factor of 2,

$$\begin{aligned}
 q(1,1) &= \begin{vmatrix} tl & t \\ l & p \end{vmatrix} \\
 q(1,2) &= \begin{vmatrix} t & tr \\ p & r \end{vmatrix} \\
 q(2,1) &= \begin{vmatrix} l & p \\ bl & b \end{vmatrix} \\
 q(2,2) &= \begin{vmatrix} p & r \\ b & br \end{vmatrix}
 \end{aligned}$$

For the zooming factor of 3,

$$\begin{aligned}
 q(1,1) &= \begin{vmatrix} tl & t \\ l & p \end{vmatrix} \\
 q(1,2) &= \begin{vmatrix} tl & t \\ l & p \end{vmatrix} + \begin{vmatrix} t & tr \\ p & r \end{vmatrix} \\
 q(1,3) &= \begin{vmatrix} t & tr \\ p & r \end{vmatrix} \\
 q(2,1) &= \begin{vmatrix} tl & t \\ l & p \end{vmatrix} + \begin{vmatrix} l & p \\ bl & b \end{vmatrix} \\
 q(2,2) &= \begin{vmatrix} tl & t \\ l & p \end{vmatrix} + \begin{vmatrix} t & tr \\ p & r \end{vmatrix} + \begin{vmatrix} l & p \\ bl & b \end{vmatrix} + \begin{vmatrix} p & r \\ b & br \end{vmatrix} \\
 q(2,3) &= \begin{vmatrix} t & tr \\ p & r \end{vmatrix} + \begin{vmatrix} p & r \\ b & br \end{vmatrix} \\
 q(3,1) &= \begin{vmatrix} l & p \\ bl & b \end{vmatrix} \\
 q(3,2) &= \begin{vmatrix} l & p \\ bl & b \end{vmatrix} + \begin{vmatrix} p & r \\ b & br \end{vmatrix}
 \end{aligned}$$

$$q(3,3) = \begin{vmatrix} p & r \\ b & br \end{vmatrix}$$

For the zooming factor of 4,

$$q(1,1) = \begin{vmatrix} tl & t \\ l & p \end{vmatrix}$$

$$q(1,2) = \begin{vmatrix} tl & t \\ l & p \end{vmatrix}$$

$$q(1,3) = \begin{vmatrix} t & tr \\ p & r \end{vmatrix}$$

$$q(1,4) = \begin{vmatrix} t & tr \\ p & r \end{vmatrix}$$

$$q(2,1) = \begin{vmatrix} tl & t \\ l & p \end{vmatrix}$$

$$q(2,2) = \begin{vmatrix} tl & t \\ l & p \end{vmatrix}$$

$$q(2,3) = \begin{vmatrix} t & tr \\ p & r \end{vmatrix}$$

$$q(2,4) = \begin{vmatrix} t & tr \\ p & r \end{vmatrix}$$

$$q(3,1) = \begin{vmatrix} l & p \\ bl & b \end{vmatrix}$$

$$q(3,2) = \begin{vmatrix} l & p \\ bl & b \end{vmatrix}$$

$$q(3,3) = \begin{vmatrix} p & r \\ b & br \end{vmatrix}$$

$$q(3,4) = \begin{vmatrix} p & r \\ b & br \end{vmatrix}$$

$$q(4,1) = \begin{vmatrix} l & p \\ bl & b \end{vmatrix}$$

$$q(4,2) = \begin{vmatrix} l & p \\ bl & b \end{vmatrix}$$

$$q(4,3) = \begin{vmatrix} p & r \\ b & br \end{vmatrix}$$

$$q(4,4) = \begin{vmatrix} p & r \\ b & br \end{vmatrix}$$

where p is the value of the pixel, and l, r, t, b, tl, tb, bl, and br are the neighbors of the pixel p.

Step 5: After computing q matrix find the maximum and minimum value in the q matrix.

Step 6: Find the value of Δ by using the formula

$$\Delta = \min_{q_k \neq p} \{|q_k - p|\}$$

Step 7: Find the value of T by using the formula

$$T = \begin{cases} q_{max} + q_{min} - p & \text{if } (q_{max} + q_{min})/2 \neq p \\ p & \text{if } (q_{max} + q_{min})/2 = p \end{cases}$$

Step 8: Find the final value of the pixel in q matrix is obtained by

$$q_k = \begin{cases} q_k - \Delta & \text{if } p \leq q_{min} \text{ for any } q_k > p \\ q_k + p & \text{if } p \geq q_{max} \text{ for any } q_k < p \\ \min(255, q_k + \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k \geq T \\ \min(0, q_k - \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k < T \end{cases}$$

Step 9: Finally calculate the PSNR and SSIM between the input and zoomed algorithm.

$$PSNR = 20 \log_{10} \left(\frac{255}{\sqrt{MSE}} \right)$$

where MSE is the mean square error.

$$SSIM = \frac{(2\mu_v\mu_w + c_1)(2cov_{vw} + c_2)}{(\mu_v^2 + \mu_w^2 + c_1)(\sigma_v^2 + \sigma_w^2 + c_2)}$$

μ_v is the mean of the input image

μ_w is the mean of the zoomed image

σ_v^2 is the variance of the input image

σ_w^2 is the variance of the zoomed image

$c_1 = (k_1L)^2$ and $c_2 = (k_2L)^2$

$k_1 = 0.01$; $k_2 = 0.03$ and $L = 255$

The Pseudocode for the determinant based fully automatic one scan adaptive image scaling algorithm is shown below:

```

P ← Input image
Q ← Output image
N ← zooming factor
for each pixel in p do
  tl=p(i-1,j-1,k);
  t=p(i-1,j,k);
  tr=p(i-1,j+1,k);
  l=p(i,j-1,k);
  p=p(i,j,k);
  r=p(i,j+1,k);
  bl=p(i+1,j-1,k);
  b=p(i+1,j,k);
  br=p(i+1,j+1,k);
end for
for each pixel in p do
  for i = 1 to n do
    if N=2 do
      q(1,1) =  $\begin{vmatrix} tl & t \\ l & p \end{vmatrix}$ 
      q(1,2) =  $\begin{vmatrix} t & tr \\ p & r \end{vmatrix}$ 
      q(2,1) =  $\begin{vmatrix} l & p \\ bl & b \end{vmatrix}$ 
      q(2,2) =  $\begin{vmatrix} p & r \\ b & br \end{vmatrix}$ 
    elseif N=3 do
      q(1,1) =  $\begin{vmatrix} tl & t \\ l & p \end{vmatrix}$ 
      q(1,2) =  $\begin{vmatrix} tl & t \\ l & p \end{vmatrix} + \begin{vmatrix} t & tr \\ p & r \end{vmatrix}$ 
      q(1,3) =  $\begin{vmatrix} t & tr \\ p & r \end{vmatrix}$ 
      q(2,1) =  $\begin{vmatrix} tl & t \\ l & p \end{vmatrix} + \begin{vmatrix} l & p \\ bl & b \end{vmatrix}$ 
    end if
  end for
end for

```

```

q(2,2) = |tl  t| + |t  tr| + |l  p| + |p  r|
          |l  p| + |p  r| + |bl b| + |b  br|
q(2,3) = |t  tr| + |p  r|
          |p  r| + |b  br|
q(3,1) = |l  p|
          |bl b|
q(3,2) = |l  p| + |p  r|
          |bl b| + |b  br|
q(3,3) = |p  r|
          |b  br|
else // N=4
q(1,1) = |tl  t|
          |l  p|
q(1,2) = |tl  t|
          |l  p|
q(1,3) = |t  tr|
          |p  r|
q(1,4) = |t  tr|
          |p  r|
q(2,1) = |tl  t|
          |l  p|
q(2,2) = |tl  t|
          |l  p|
q(2,3) = |t  tr|
          |p  r|
q(2,4) = |t  tr|
          |p  r|
q(3,1) = |l  p|
          |bl b|
q(3,2) = |l  p|
          |bl b|
q(3,3) = |p  r|
          |b  br|
q(3,4) = |p  r|
          |b  br|
q(4,1) = |l  p|
          |bl b|
q(4,2) = |l  p|
          |bl b|
q(4,3) = |p  r|
          |b  br|
q(4,4) = |p  r|
          |b  br|
end if
end for
if (qk ≠ p) do
Δ = min (|qk - p|)
end if
if (q max + qmin)/2 ≠ p do
t = q max + qmin - p
else
T = P
end if

```



```

if ( p ≤ qmin && qk > p) do
qk = qk - Δ
else if (p ≥ qmax && qk < p) do
qk = qk + Δ
else if ((qmin < p < qmax) && (qk ≥ T)) do
qk = min(255, qk + Δ)
else
qk = min (0, qk - Δ)
end if
end for

```

**PROPOSED ALGORITHM –
WEIGHTED DETERMINANT BASED**

The algorithm for the weighted determinant based fully automatic one scan adaptive image scaling algorithm is shown below:

Step 1: Load the input color image.

Step 2: Separate the three color components R, G, and B plane from the color image.

Step 3: Identify the eight neighbors of each pixel in each color components.

Step 4: Expand each pixel for n x n matrix named it as ‘q’ using determinant of weighted pixel.

For the zooming factor of 2,

$$\begin{aligned}
 q(1,1) &= \begin{vmatrix} tl & 2t \\ 2l & 4p \end{vmatrix} \\
 q(1,2) &= \begin{vmatrix} 2t & tr \\ 4p & 2r \end{vmatrix} \\
 q(2,1) &= \begin{vmatrix} 2l & 4p \\ bl & 2b \end{vmatrix} \\
 q(2,2) &= \begin{vmatrix} 4p & 2r \\ 2b & br \end{vmatrix}
 \end{aligned}$$

For the zooming factor of 3,

$$\begin{aligned}
 q(1,1) &= \begin{vmatrix} 4tl & 6t \\ 6l & 9p \end{vmatrix} \\
 q(1,2) &= \begin{vmatrix} 2tl & 6t \\ 3l & 9p \end{vmatrix} + \begin{vmatrix} 6t & 2tr \\ 9p & 3r \end{vmatrix} \\
 q(1,3) &= \begin{vmatrix} 6t & 4tr \\ 9p & 6r \end{vmatrix} \\
 q(2,1) &= \begin{vmatrix} 2tl & 3t \\ 6l & 9p \end{vmatrix} + \begin{vmatrix} 6l & 9p \\ 2bl & 3b \end{vmatrix} \\
 q(2,2) &= \begin{vmatrix} tl & 3t \\ 3l & 9p \end{vmatrix} + \begin{vmatrix} 3t & tr \\ 9p & 3r \end{vmatrix} + \begin{vmatrix} 3l & 9p \\ bl & 3b \end{vmatrix} + \begin{vmatrix} 9p & 3r \\ 3b & br \end{vmatrix} \\
 q(2,3) &= \begin{vmatrix} 3t & 2tr \\ 9p & 6r \end{vmatrix} + \begin{vmatrix} 9p & 6r \\ 3b & 2br \end{vmatrix} \\
 q(3,1) &= \begin{vmatrix} 6l & 9p \\ 4bl & 6b \end{vmatrix} \\
 q(3,2) &= \begin{vmatrix} 3l & 9p \\ 2bl & 6b \end{vmatrix} + \begin{vmatrix} 9p & 3r \\ 6b & 2br \end{vmatrix} \\
 q(3,3) &= \begin{vmatrix} 9p & 6r \\ 6b & 4br \end{vmatrix}
 \end{aligned}$$

For the zooming factor of 4,

$$\begin{aligned}
 q(1,1) &= \begin{vmatrix} 4tl & 6t \\ 6l & 9p \end{vmatrix} \\
 q(1,2) &= \begin{vmatrix} 2tl & 8t \\ 3l & 12p \end{vmatrix} \\
 q(1,3) &= \begin{vmatrix} 8t & 2tr \\ 12p & 3r \end{vmatrix} \\
 q(1,4) &= \begin{vmatrix} 6t & 4tr \\ 12p & 6r \end{vmatrix} \\
 q(2,1) &= \begin{vmatrix} 2tl & 3t \\ 8l & 12p \end{vmatrix} \\
 q(2,2) &= \begin{vmatrix} tl & 4t \\ 4l & 16p \end{vmatrix} \\
 q(2,3) &= \begin{vmatrix} 4t & tr \\ 16p & 4r \end{vmatrix} \\
 q(2,4) &= \begin{vmatrix} 3t & 2tr \\ 12p & 8r \end{vmatrix} \\
 q(3,1) &= \begin{vmatrix} 8l & 12p \\ 2bl & 3b \end{vmatrix} \\
 q(3,2) &= \begin{vmatrix} 4l & 16p \\ bl & 4b \end{vmatrix} \\
 q(3,3) &= \begin{vmatrix} 16p & 4r \\ 4b & br \end{vmatrix} \\
 q(3,4) &= \begin{vmatrix} 12p & 8r \\ 3b & 2br \end{vmatrix} \\
 q(4,1) &= \begin{vmatrix} 6l & 9p \\ 4bl & 6b \end{vmatrix} \\
 q(4,2) &= \begin{vmatrix} 3l & 12p \\ 2bl & 8b \end{vmatrix} \\
 q(4,3) &= \begin{vmatrix} 12p & 3r \\ 8b & 2br \end{vmatrix} \\
 q(4,4) &= \begin{vmatrix} 9p & 6r \\ 6b & 4br \end{vmatrix}
 \end{aligned}$$

where p is the value of the pixel, and l, r, t, b, tl, tr, bl, and br are the neighbors of the pixel p.

Step 5: After computing q matrix find the maximum and minimum value in the q matrix.

Step 6: Find the value of Δ by using the formula

$$\Delta = \min_{q_k \neq p} \{|q_k - p|\}$$

Step 7: Find the value of T by using the formula

$$T = \begin{cases} q_{max} + q_{min} - p & \text{if } (q_{max} + q_{min})/2 \neq p \\ p & \text{if } (q_{max} + q_{min})/2 = p \end{cases}$$

Step 8: Find the final value of the pixel in q matrix is obtained by

$$q_k = \begin{cases} q_k - \Delta & \text{if } p \leq q_{min} \text{ for any } q_k > p \\ q_k + p & \text{if } p \geq q_{max} \text{ for any } q_k < p \\ \min(255, q_k + \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k \geq T \\ \min(0, q_k - \Delta) & \text{if } q_{min} < p < q_{max} \text{ for any } q_k < T \end{cases}$$

Step 9: Finally calculate the PSNR and SSIM between the input and zoomed algorithm.

$$PSNR = 20 \log_{10} \left(\frac{255}{\sqrt{MSE}} \right)$$

where MSE is the mean square error.

$$SSIM = \frac{(2\mu_v\mu_w + c_1)(2cov_{vw} + c_2)}{(\mu_v^2 + \mu_w^2 + c_1)(\sigma_v^2 + \sigma_w^2 + c_2)}$$

μ_v is the mean of the input image

μ_w is the mean of the zoomed image

σ_v^2 is the variance of the input image

σ_w^2 is the variance of the zoomed image

$c_1 = (k_1L)^2$ and $c_2 = (k_2L)^2$

$k_1 = 0.01$; $k_2 = 0.03$ and $L = 255$

The Pseudocode for the weighted determinant based fully automatic one scan adaptive image scaling algorithm is shown below:

$P \leftarrow$ Input image

$Q \leftarrow$ Output image

$N \leftarrow$ zooming factor

for each pixel in p do

$tl = p(i-1, j-1, k)$;

$t = p(i-1, j, k)$;

$tr = p(i-1, j+1, k)$;

$l = p(i, j-1, k)$;

$p = p(i, j, k)$;

$r = p(i, j+1, k)$;

$bl = p(i+1, j-1, k)$;

$b = p(i+1, j, k)$;

$br = p(i+1, j+1, k)$;

end for

for each pixel in p do

for $i = 1$ to n do

if $N=2$ do

$$q(1,1) = \begin{vmatrix} tl & 2t \\ 2l & 4p \end{vmatrix}$$

$$q(1,2) = \begin{vmatrix} 2t & tr \\ 4p & 2r \end{vmatrix}$$

$$q(2,1) = \begin{vmatrix} 2l & 4p \\ bl & 2b \end{vmatrix}$$

$$q(2,2) = \begin{vmatrix} 4p & 2r \\ 2b & br \end{vmatrix}$$

elseif $N=3$ do

$$q(1,1) = \begin{vmatrix} 4tl & 6t \\ 6l & 9p \end{vmatrix}$$

$$q(1,2) = \begin{vmatrix} 2tl & 6t \\ 3l & 9p \end{vmatrix} + \begin{vmatrix} 6t & 2tr \\ 9p & 3r \end{vmatrix}$$

$$q(1,3) = \begin{vmatrix} 6t & 4tr \\ 9p & 6r \end{vmatrix}$$

$$q(2,1) = \begin{vmatrix} 2tl & 3t \\ 6l & 9p \end{vmatrix} + \begin{vmatrix} 6l & 9p \\ 2bl & 3b \end{vmatrix}$$

$$q(2,2) = \begin{vmatrix} tl & 3t \\ 3l & 9p \end{vmatrix} + \begin{vmatrix} 3t & tr \\ 9p & 3r \end{vmatrix} + \begin{vmatrix} 3l & 9p \\ bl & 3b \end{vmatrix} + \begin{vmatrix} 9p & 3r \\ 3b & br \end{vmatrix}$$

```

q(2,3) = |3t 2tr| + |9p 6r|
          |9p 6r|   |3b 2br|
q(3,1) = |6l 9p|
          |4bl 6b|
q(3,2) = |3l 9p| + |9p 3r|
          |2bl 6b|   |6b 2br|
q(3,3) = |9p 6r|
          |6b 4br|
else // N=4
q(1,1) = |4tl 6t|
          |6l 9p|
q(1,2) = |2tl 8t|
          |3l 12p|
q(1,3) = |8t 2tr|
          |12p 3r|
q(1,4) = |6t 4tr|
          |12p 6r|
q(2,1) = |2tl 3t|
          |8l 12p|
q(2,2) = |tl 4t|
          |4l 16p|
q(2,3) = |4t tr|
          |16p 4r|
q(2,4) = |3t 2tr|
          |12p 8r|
q(3,1) = |8l 12p|
          |2bl 3b|
q(3,2) = |4l 16p|
          |bl 4b|
q(3,3) = |16p 4r|
          |4b br|
          q(3,4) = |12p 8r|
                   |3b 2br|
q(4,1) = |6l 9p|
          |4bl 6b|
q(4,2) = |3l 12p|
          |2bl 8b|
q(4,3) = |12p 3r|
          |8b 2br|
q(4,4) = |9p 6r|
          |6b 4br|
end if

end for
if (qk ≠ p) do
Δ = min (|qk - p|)
end if
if (q max + qmin)/2 ≠ p do
t = q max + qmin - p
else
T = P
end if

```

```

if ( p ≤ qmin && qk > p) do
    qk = qk - Δ
else if (p ≥ qmax && qk < p) do
    qk = qk + Δ
else if ((qmin < p < qmax) && (qk ≥ T)) do
    qk = min(255, qk + Δ)
else
    qk = min (0, qk - Δ)

end if
end for

```

RESULTS AND DISCUSSION

To evaluate the result we consider the MATLAB default image namely wpeppers.jpg. Figure 1 (a), (b) and (c) shows the input image and zoomed image with zooming factor of 2, 3, and 4 for the

existing weighted sum, and proposed determinant and weighted determinant based fully automatic one scan adaptive image scaling algorithm respectively for wpeppers.jpg.

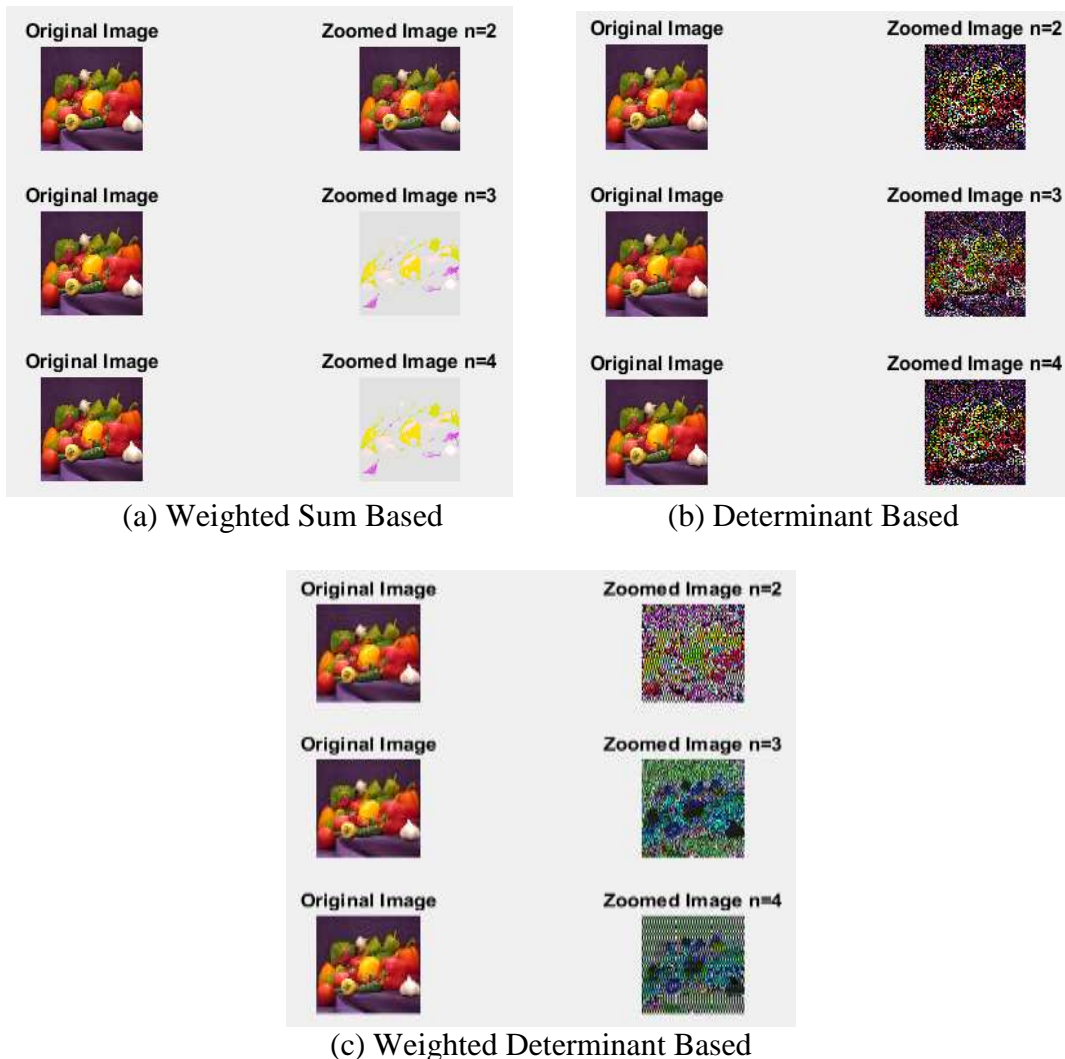


Fig. 1: Input and Output Image for Existing and Proposed Method for Wpeppers.jpg

Figure 2 (a), (b) and (c) shows the input image and zoomed image with zooming factor of 2, 3, and 4 for the existing weighted sum, and proposed determinant

and weighted determinant based fully automatic one scan adaptive image scaling algorithm respectively for football.jpg.

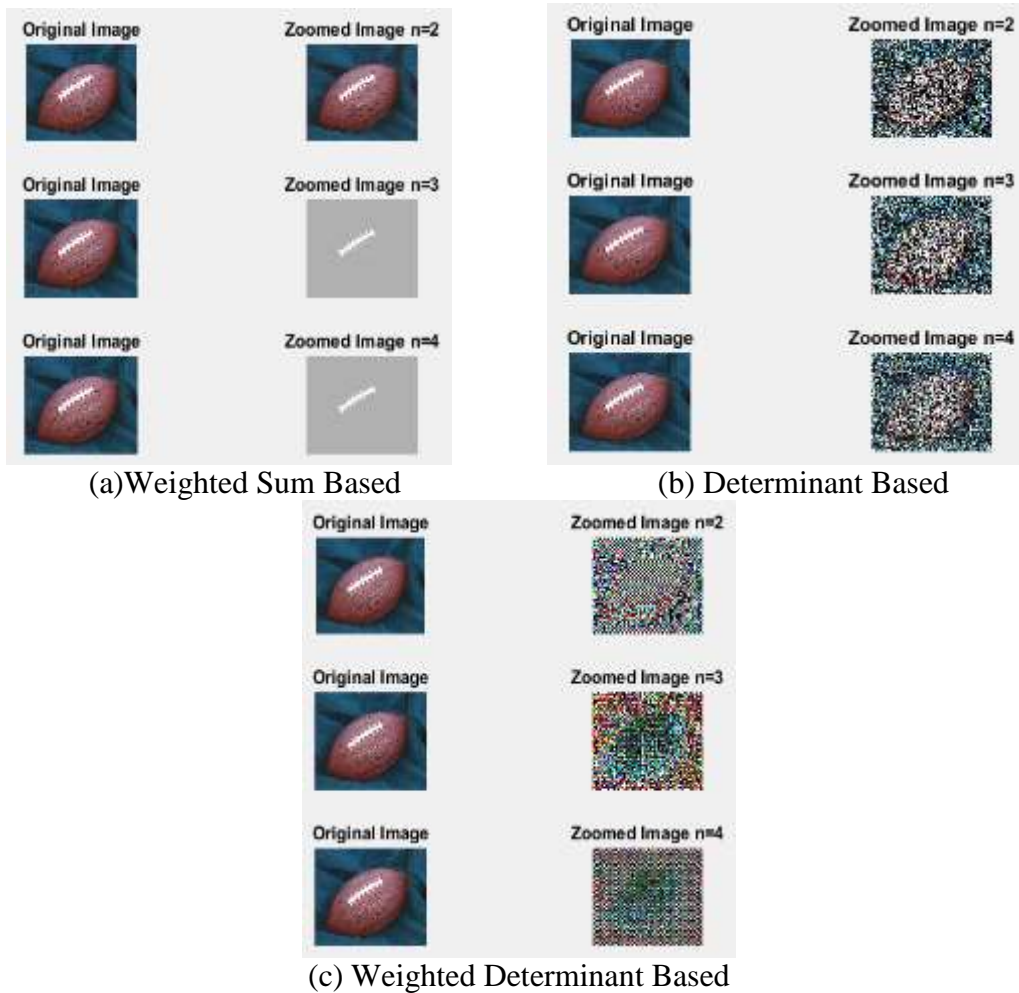


Fig. 2: Input and Output Image for Existing and Proposed Method for Football.

Table 1 shows the comparison of exiting weighted sum based and proposed determinant and weighted determinant based algorithm in terms of PSNR and SSIM.

CONCLUSION

From the table 5.1, it is concluded that the PSNR and SSIM value of the proposed determinant and weighted determinant based image scaling algorithm is worst compared to the existing weighted sum based image scaling algorithm. It is evident by seeing the figure 1 and 2 that the image quality is poor in case of

proposed system compared to existing systems. In future, we will analyze why this method is not efficient through the theoretic calculation and also will able to explain how this problem can be rectified. Also we can see from figure 1 and 2 that the information from the zoomed image with zooming factor 3 and 4 is known in case of proposed system than existing system, i.e., in existing system, information and noise both are less for zooming factor 3 and 4 and in proposed system, information and noise both are high for zooming factor 3 and 4.

Table 1: Comparison Table.

Image	Zooming Factor	Carlo Arcelli <i>et al</i>		Proposed			
		Weighted Sum based		Determinant based		Weighted Determinant based	
		PSNR	SSIM	PSNR	SSIM	PSNR	SSIM
wpeppers.jpg	2	30.0596	1.9277 $\times 10^{-19}$	-2.3702	2.5836 $\times 10^{-36}$	-0.8106	2.4314 $\times 10^{-36}$
	3	4.5864	4.5072 $\times 10^{-23}$	-1.9219	1.0881 $\times 10^{-37}$	-10.7206	-5.1015 $\times 10^{-41}$
	4	4.5882	8.1732 $\times 10^{-23}$	-2.0859	2.5661 $\times 10^{-37}$	-1.2910	-4.0028 $\times 10^{-39}$
football.jpg	2	32.5538	1.3484 $\times 10^{-21}$	-5.5334	-6.8174 $\times 10^{-39}$	-2.9893	1.1175 $\times 10^{-39}$
	3	7.5004	6.1611 $\times 10^{-22}$	-7.2121	6.8290 $\times 10^{-40}$	-17.1157	2.1201 $\times 10^{-44}$
	4	7.5005	1.0884 $\times 10^{-21}$	-4.4485	-3.4114 $\times 10^{-39}$	-1.1430	-1.1410 $\times 10^{-39}$

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