

# Efficient Training of Volterra Series-based Pre-distortion Filter Using Neural Networks

M1H.3, OFC 2022

V. Bajaj<sup>1,2\*</sup>, M. Chagnon<sup>2</sup>, S. Wahls<sup>1</sup>, V. Aref<sup>2</sup>

1 Delft University of Technology, The Netherlands

2 Nokia Solutions and Networks GmbH und Co KG, Stuttgart, Germany

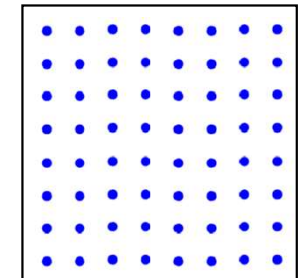
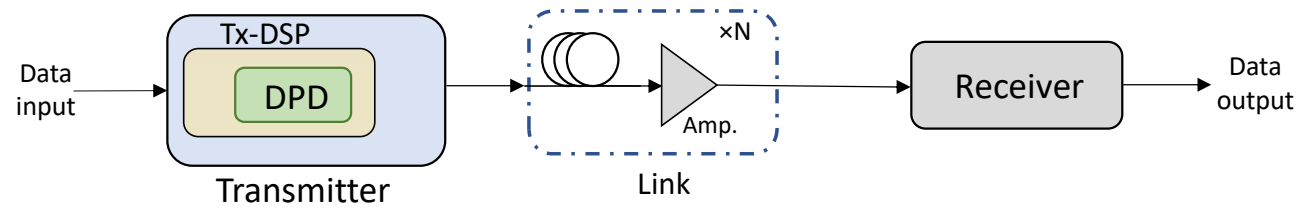
[v.bajaj-1@tudelft.nl](mailto:v.bajaj-1@tudelft.nl)



This work has received funding from the European Union H2020 research and innovation program under MSCA GA 766115.



# Digital Pre-Distortion (DPD)



64-QAM

## Common DPD techniques

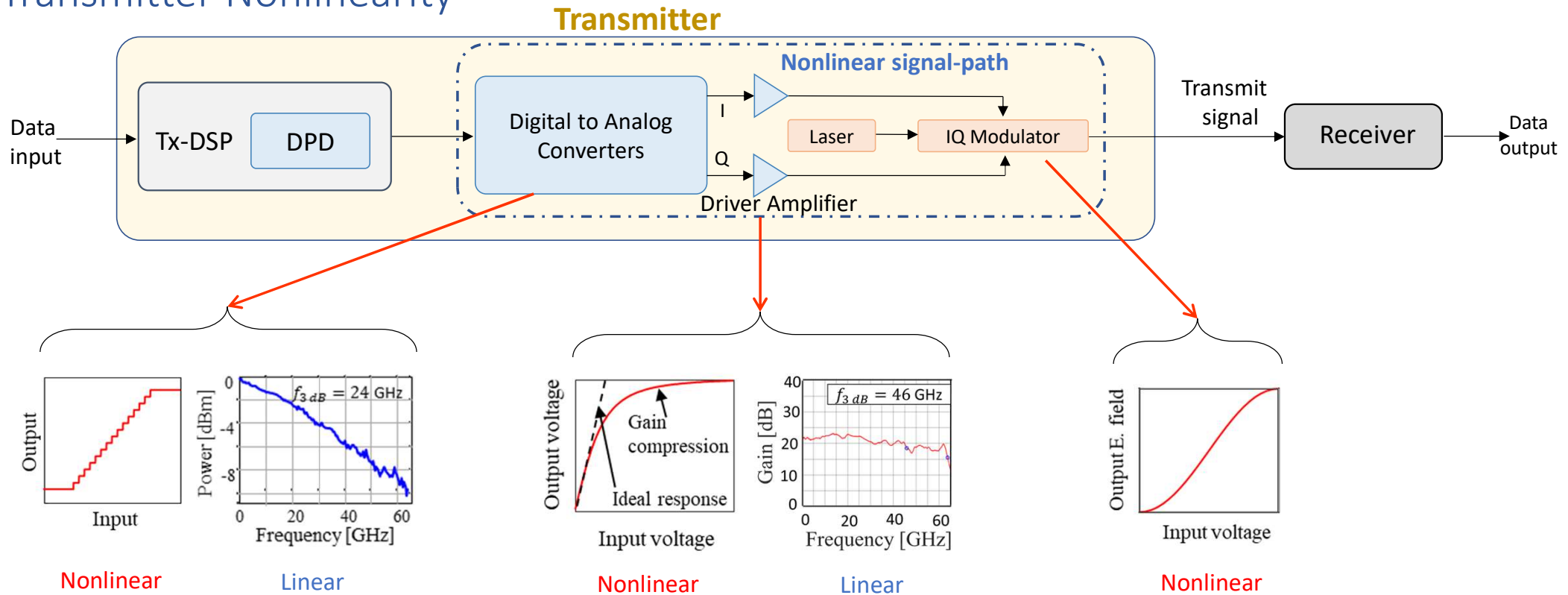
- Linear
- Look-up tables
- Volterra series-based
- Memory polynomials (MPs)
- Generalized MPs
- NN-based

# Outline

- Distortions in a Coherent Optical Transmitter
- Volterra series-based DPD and Training
- Proposed Efficient Training of Volterra-DPD
- Simulation Setup and Results
- Conclusion

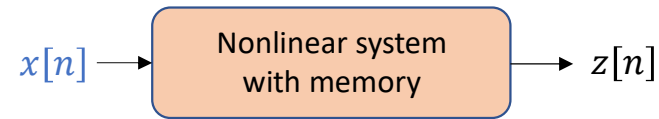
# Coherent Optical Transmitter

## Transmitter Nonlinearity



- [1] A. Napoli, et al., "Digital pre-compensation techniques enabling high-capacity bandwidth variable transponders", *Optics Communications*, 409, 52-65, 2018.
- [2] P. W. Berenguer, et al., "Nonlinear digital pre-distortion of transmitter components," *Journal of lightwave technology*, vol. 34, no. 8, pp. 1739–1745, 2015.
- [3] V. Bajaj, et al. "Deep Neural Network-Based Digital Pre-Distortion for High Baudrate Optical Coherent Transmission," *J. Lightwave Technol.* 40, 597-606 (2022)

## Volterra series-based DPD



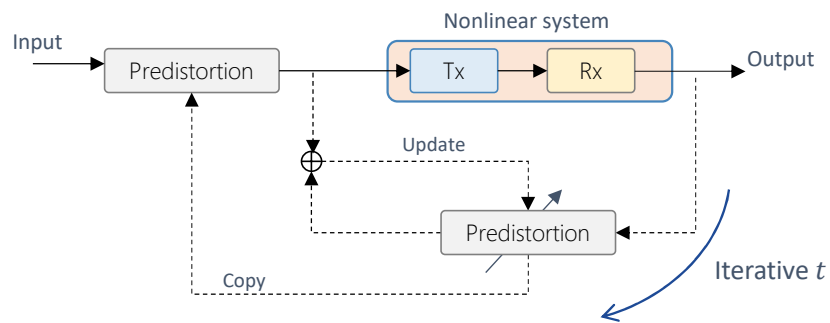
$$z[n] = H x[n]; \quad H = \text{Volterra kernels}$$

$$z[n] = h_0 + \sum_{\tau_1=-M_1}^{M_1} h_1[\tau_1]x[n - \tau_1] + \sum_{\tau_2=-M_2}^{M_2} \sum_{d_2=0}^{D_2} h_2[\tau_2, d_2]x[n - \tau_2]x[n - \tau_2 - d_2] + \dots \text{higher order terms} \dots$$

- Volterra series direct extension of the impulse response concept.

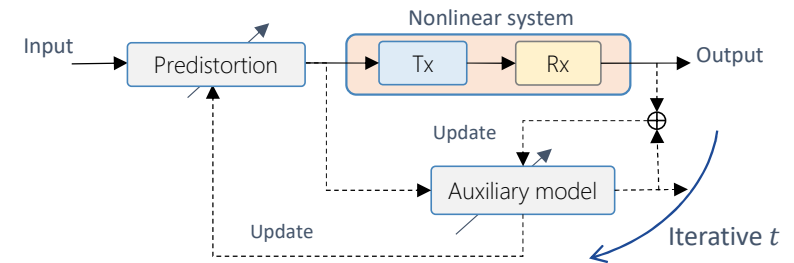
Interpretable  $\rightarrow$  Volterra series

# Training of DPDs



**Indirect learning architecture (ILA)**

- Simpler [5, 6]
- Noise offset [7]
- Nonlinear operations are not commutative [7]



**Direct learning architecture (DLA)**

- Pre-inverse
- No Noise offset
- Requires an auxiliary model (differentiable)

Accurate DPD → Direct learning

[5] C. Eun and E. J. Powers, "A new Volterra predistorter based on the indirect learning architecture," IEEE trans. on signal proc., vol. 45, no. 1, pp. 223–227, 1997.

[6] G. Khanna, et al., "A robust adaptive pre-distortion method for optical communication transmitters," IEEE Photonics Technology Letters, vol. 28, no. 7, 752–755, 2015.

[7] H. Paaso and A. Mammela, "Comparison of direct learning and indirect learning predistortion architectures," in IEEE Int. Symp. on Wireless Comm. systems, 309–313, 2008.

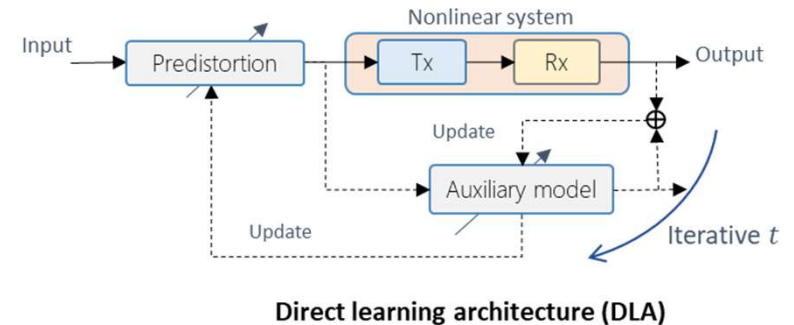
[8] Y. H. Lim, et al., "An adaptive nonlinear prefilter for compensation of distortion in nonlinear systems," IEEE Trans. on Signal Proc., 46, 6, pp. 1726–1730, 1998.

[9] D. Zhou, V. E. DeBrunner, "Novel adaptive nonlinear predistorters based on the direct learning algorithm", IEEE Trans. on Signal Proc., 55, 1, pp. 120–133, 2007.

# Training

## Direct learning

- Nonlinear Filtered x-LMS
  - Predistortion and Auxiliary model: Volterra series-based
  - Back-propagation to update pre-distortion model is difficult.
  
- Direct learning → NN-based.
  - Modular, back-propagation is easier.
  
- But NN-based DPDs are kind of black box. Very difficult to interpret.



Simpler direct learning → NN as auxiliary model

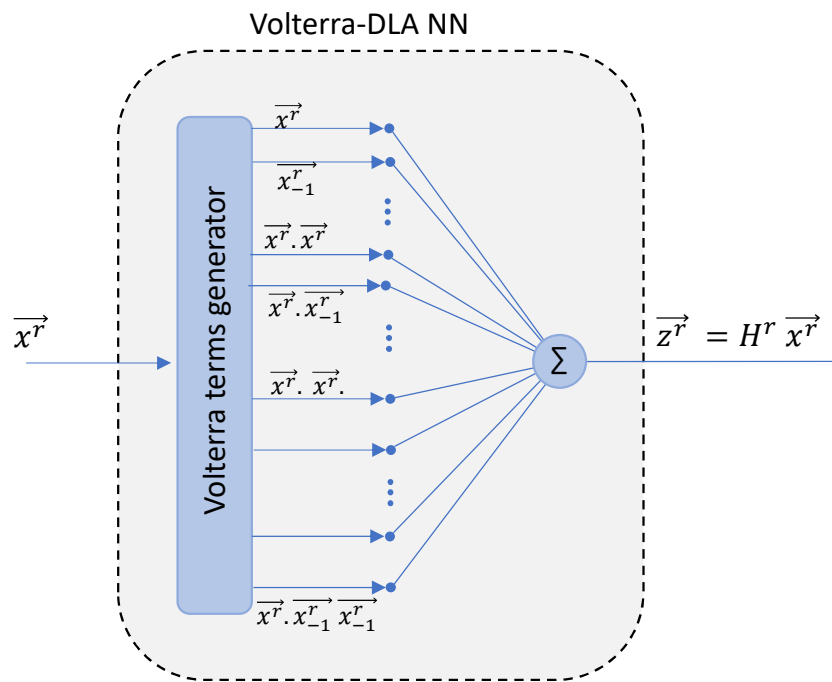
[8] Y. H. Lim, et.al., "An adaptive nonlinear prefilter for compensation of distortion in nonlinear systems", IEEE Transactions on Signal Processing, 46(6):1726–1730, 1998

[10] G. Paryanti, et. al., "A direct learning approach for neural network based pre-distortion for coherent nonlinear optical transmitter", J. Lightw. Technol., 2020.

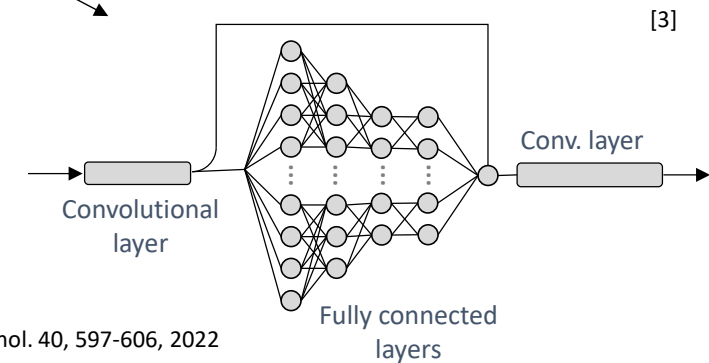
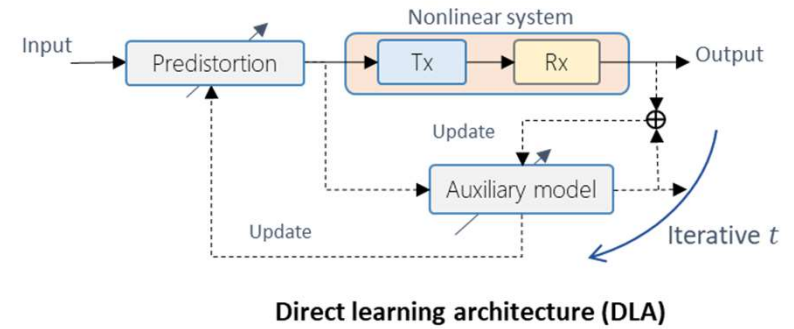
[3] V. Bajaj, et. al. "Deep Neural Network-Based Digital Pre-Distortion for High Baudrate Optical Coherent Transmission," J. Lightwave Technol. 40, 597-606, 2022

# Proposed Volterra-DLA DPD

- Direct learning of Volterra DPD by using neural networks



For Quadrature phase, similar architecture was used.

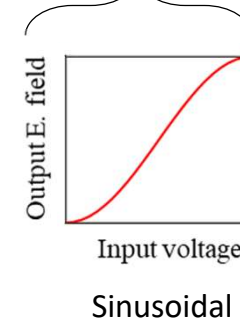
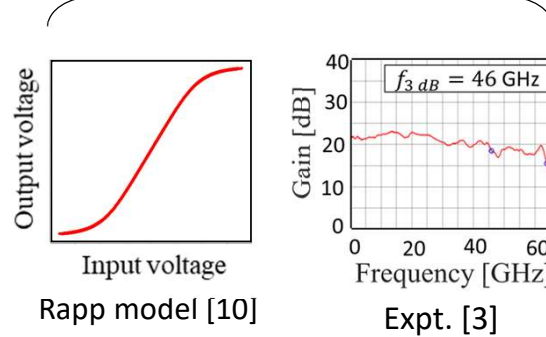
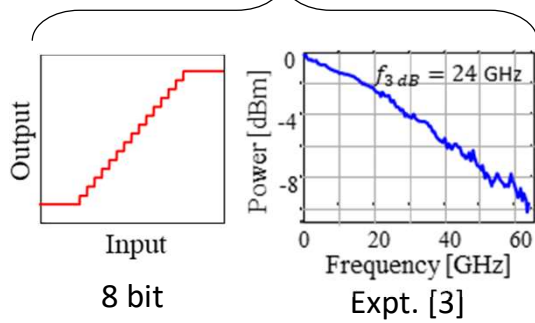
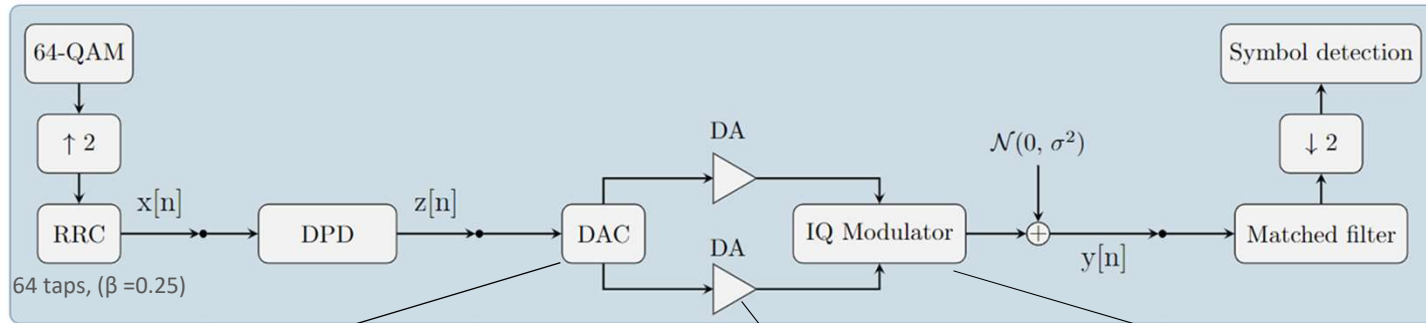


[3] V. Bajaj, et. al. "Deep Neural Network-Based Digital Pre-Distortion for High Baudrate Optical Coherent Transmission," J. Lightwave Technol. 40, 597-606, 2022



# Simulation setup

64 GBaud, back-to-back conf.



$$Back - Off [dB] = -20 \log_{10} \left( \frac{V_{rms}}{V_{sat}} \right)$$

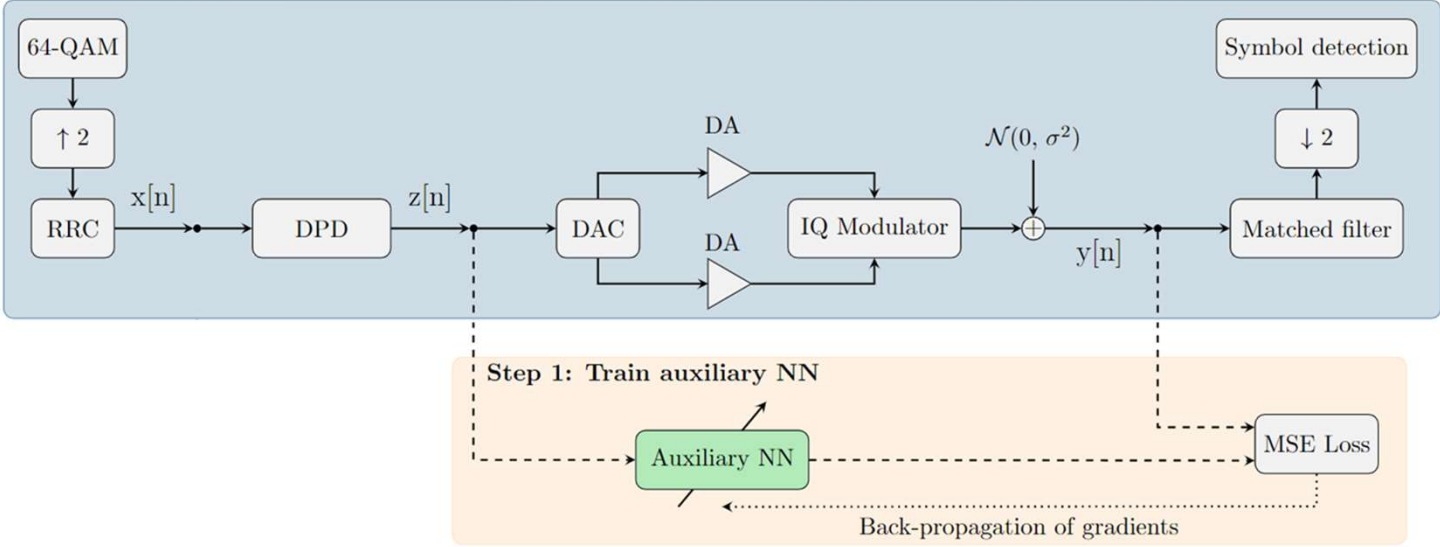
Smaller BO  $\rightarrow$  stronger nonlinearity

	Back-off [dB]
DAC	10
IQ mod	20
DA	7, 5, 3

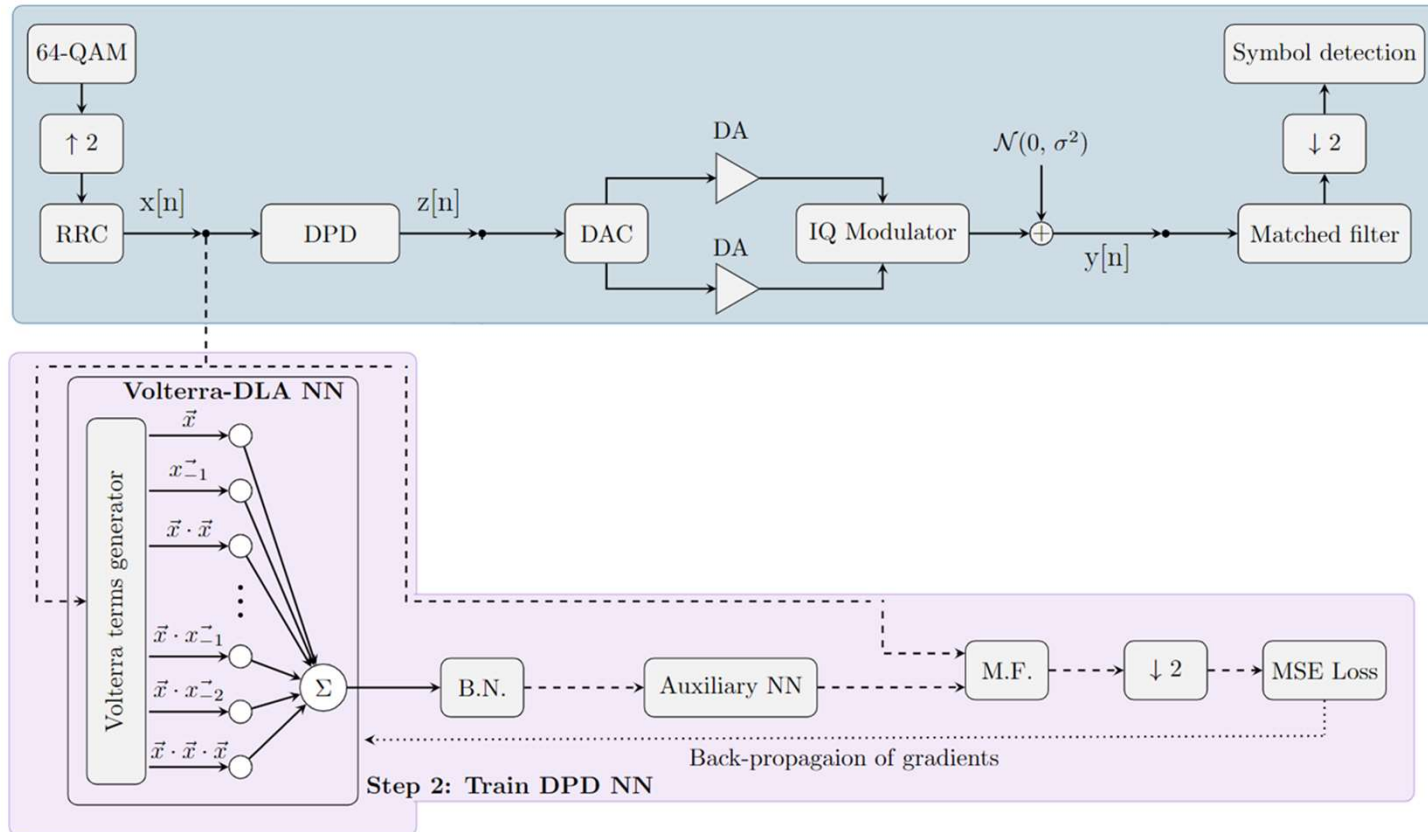
[10] G. Paryanti, et al., "A direct learning approach for neural network based pre-distortion for coherent nonlinear optical transmitter", J. Lightwave Technol., 2020.

[3] V. Bajaj, et. al. "Deep Neural Network-Based Digital Pre-Distortion for High Baudrate Optical Coherent Transmission," J. Lightwave Technol. 40, 597-606, 2022

# Training Volterra-DLA DPD

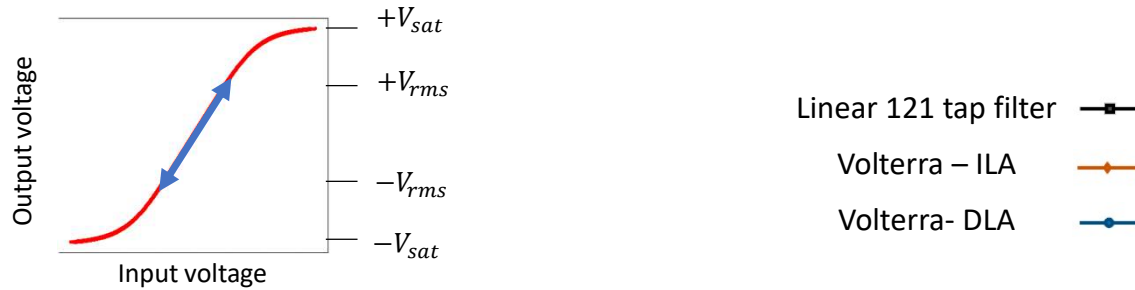


# Training Volterra-DLA DPD



# Results

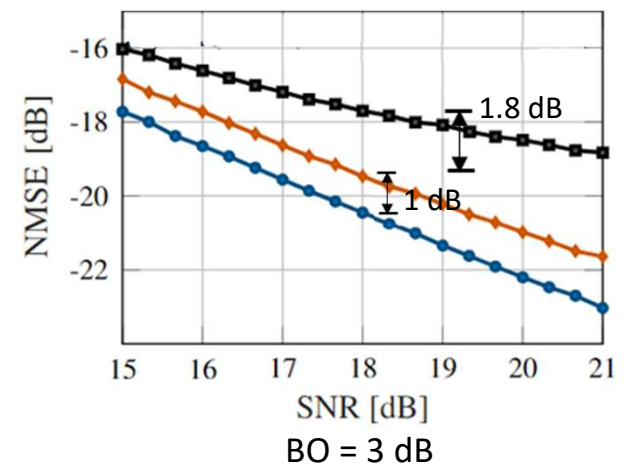
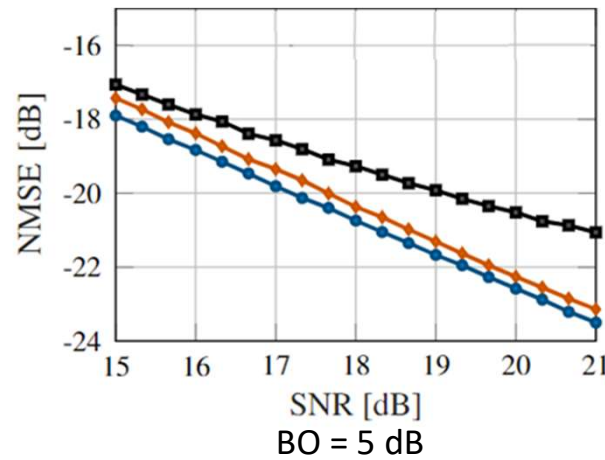
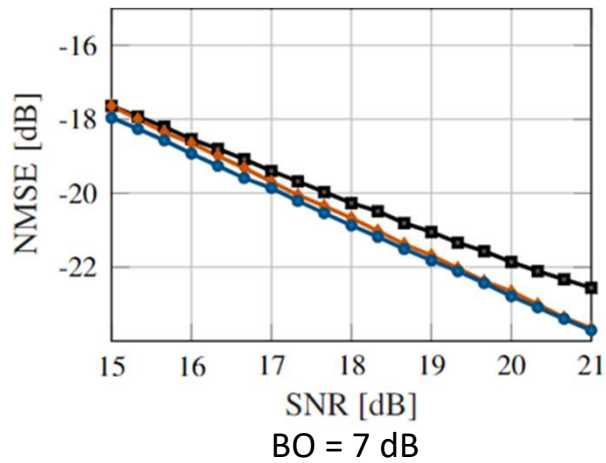
## Varying DA nonlinearity



Volterra up to 5<sup>th</sup> order

Order	Memory	Depths
1 <sup>st</sup>	121	-
3 <sup>rd</sup>	10	4
2 <sup>nd</sup> , 4 <sup>th</sup> , 5 <sup>th</sup>	3	0

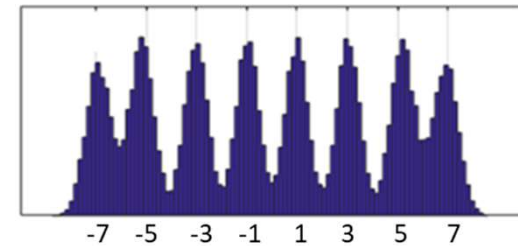
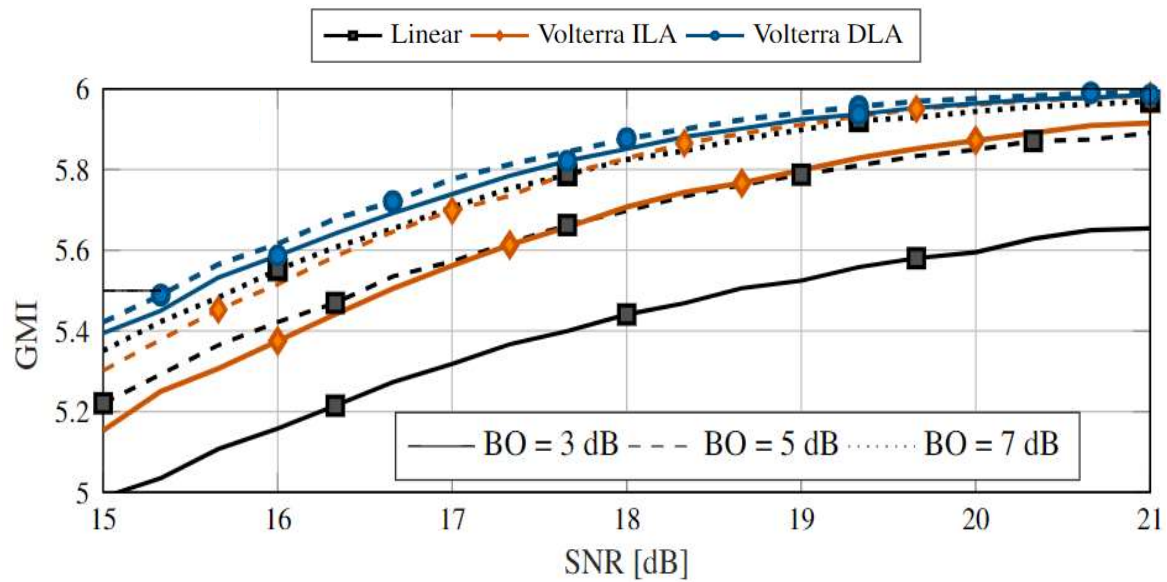
$$\text{Back - Off [dB]} = -20 \log_{10} \left( \frac{V_{rms}}{V_{sat}} \right)$$



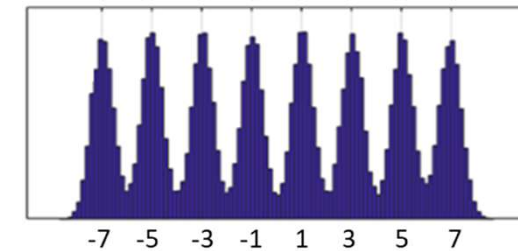
Increasing nonlinearity

# Results

## GMI and histograms



Volterra-ILA



Volterra-DLA

Histograms of the real part of received signal

# Conclusion

- NNs have nice properties to be an auxiliary model
  - Modular, easier back-propagation.
- We proposed an efficient direct learning of Volterra series-based DPD by leveraging advantages of NNs.
- We compared the performance of proposed Volterra-DLA DPD with a Volterra-ILA and a linear DPD for varying nonlinearity condition in simulations.
- The proposed method can be used for training other DPDs like memory polynomials as well.

Email: V.Bajaj-1@tudelft.nl