

1 The utility of forest attribute maps for 2 automated Avalanche Terrain Exposure 3 Scale (ATES) modelling

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10

11 Abstract

12 The number of people affected by snow avalanches during recreational activities has increased
13 considerably over the recent years in Norway. An instrument to reduce these numbers are improved
14 terrain classification systems to provide guidance for safe route finding. One such system is the
15 Avalanche Terrain Exposure Scale (ATES) which classifies terrain into the three classes simple,
16 challenging, and complex. Forests can provide some protection from avalanches, and information on
17 forest attributes can be incorporated into avalanche hazard models such as the automated ATES
18 model (AutoATES). The objectives of this study were to i) map relevant forest attributes (stem
19 density and canopy cover) based on National Forest Inventory and remote sensing data and, ii) use
20 these forest attributes as input to the AutoATES model to improve avalanche hazard maps. We
21 predicted stem density with species-specific mixed-effects models and directly calculated canopy
22 cover using airborne laser scanning data in a 20 Mha study area ranging from the arctic circle to
23 southern Norway. The forest attributes were mapped for 16 m x 16 m pixels, which were used as
24 input for the AutoATES model. The uncertainties of the stem number and canopy cover maps were
25 30% and 31%, respectively. The overall classification accuracy of 52 ski touring routes in Western
26 Norway with a total length of 282 km increased from 55% in the model without forest information to
27 67% when utilizing canopy cover. The F1 score for the three predicted ATES classes improved by 31%,
28 9%, and 6%. The use of stem number improved the hazard maps to a slightly smaller degree. We
29 conclude that large-scale fine-resolution forest attribute maps are valuable data in the modelling and
30 mapping of avalanche hazards. Together, these maps may be valuable for precise planning of forest
31 management operations aiming at the utilization of forests as nature-based solutions for avalanche-
32 related disaster risk reduction.

33

34 **Keywords:** Airborne laser scanning, National Forest Inventory, SR16, disaster risk reduction, nature
35 based solutions

36

37 1 Introduction

38 Snow avalanches cause on average six fatalities per year in Norway (NGI 2022; Varsom 2022); these
39 deaths and other injuries are primarily associated with recreation. Likely due to the increased use of
40 the outdoors, the number of people affected by avalanches has increased remarkably in the recent
41 years (Varsom 2022). Considerable resources have therefore been invested to reduce the number of
42 casualties. Hazard maps to assist route-finding are believed to be an important tool in this context.
43 Forest cover can alter avalanche behavior by modifying the snowpack through canopy interception
44 (Bebi et al. 2001) and, albeit to a lesser extent, by increasing friction on prone slopes through the
45 mechanism of the physical barriers of tree stems (Teich et al. 2014). On the other hand, large
46 avalanches that release far above the tree line are only to a small degree affected by forests (Teich et
47 al. 2012). Snow interception is largely dependent on tree species, because of the different
48 morphology of tree crowns, and the size and number of trees in a given area, which are the factors
49 that will collectively determine canopy cover and gaps. These parameters can potentially be derived
50 from remote sensing in a way that is suited to avalanche simulation (Brožová et al. 2020) because
51 they are spatially explicit. Maps of such forest attributes allow for monitoring of forest development
52 and, subsequently, for adequate and effective forest management towards an optimized avalanche
53 protection function to reduce avalanche hazards (Brang et al. 2006). This is especially crucial under
54 the challenge of climate change that requires us to adapt forests to changing growing conditions to
55 maintain healthy and resilient forests that can fulfil their functions. Moreover, once avalanche hazard
56 zones are mapped, forest management measures could be used to reduce avalanche hazard, for
57 example by avoiding clear cuts.

58 Worldwide, various hazard maps have been developed for recreationalists using different avalanche
59 classification schemes (Barbolini et al. 2011; Schmudlach and Köhler 2016; Harvey et al. 2018; Larsen
60 et al. 2020b). In Norway, the most used classification of avalanche terrain is the Avalanche Terrain
61 Exposure Scale (ATES, Statham et al. 2006). The classification scheme divides avalanche terrain into
62 simple (class 1), challenging (class 2) and complex (class 3) terrain.

63 Originally, the ATES classification scheme was developed to provide an overall classification of an
64 entire route based on the overall exposure likely to be encountered. Recent advances including
65 modern cartographic techniques have made it more common to develop spatial maps. Making ATES
66 maps, Delparte (2008) found that slope angle and stem density were the two most important factors
67 when classifying avalanche terrain with the ATES model. Campbell and Gould (2013) developed a
68 specific model for spatial ATES including parameters for slope angle and forest density. Building on
69 the proposed model for spatial ATES mapping, Larsen et al. (2020b, a) developed an automated ATES
70 algorithm (AutoATES) for nationwide maps in Norway. However, due to limits in the spatial
71 resolution and area-coverage of forest data, this version of the algorithm was only developed for
72 non-forested terrain. The AutoATES map is consequentially likely to be inaccurate below the treeline.
73 While many recreational accidents associated with avalanches happen above the treeline, Norway is
74 not a country with particularly high mountains and the fjordic landscape means that a considerable
75 amount of avalanche prone terrain is found below the treeline. Therefore, the inclusion of forest
76 attributes in terrain exposure classification is important. Consequentially, in this study we aim to
77 integrate high spatial resolution data on forests into the spatially explicit classification of avalanche
78 exposure (AutoATES-Forest).

79 The relationship between forest attributes and remote sensing data can be quantified via regression
80 models, where the response (a forest attribute) is explained by predictors (remotely sensed
81 variables). Such models are usually established using ground reference data from field plots with
82 known locations and remote-sensing data extracted for the same locations. This is commonly known

83 as the area-based approach (Næsset 2002). In Norway, the National Forest Inventory (NFI) collects
84 extensive information about forest properties in sample plots with a size of 250 m² (Breidenbach et
85 al. 2020a), which can serve as ground reference for remote-sensing data to establish regression
86 models predicting these forest attributes. Once established, these models can be extrapolated to
87 areas beyond field-inventory plots, to obtain prediction maps for the attributes of interest. These
88 predictions are particularly useful to support operational forest management (e.g. reviewed by
89 Brosofske et al. 2014). To achieve this mapping of forest attributes, the entire area is gridded into
90 aerial units of the same size as used for model fitting on NFI plots, and the same remotely sensed
91 variables are extracted for each unit. Following this approach, various forest attributes were
92 modelled and mapped for the Norwegian forest resource map SR16 (Astrup et al. 2019; Hauglin et al.
93 2021), which is a national map at spatial resolution of 16 m x 16 m that is freely available (NIBIO
94 2022).

95 The necessary forest attributes for the AutoATES-Forest avalanche hazard model in Norway are
96 canopy cover or stem density. Canopy cover is defined as the proportion of the forest floor that is
97 obscured by tree crowns. Consequentially, airborne laser scanning (ALS) is the ideal way in which to
98 assess this variable directly for example from a surface model or as the proportion of first returns
99 above a specified height threshold (Korhonen et al. 2011). On the other hand, stem density is more
100 challenging to obtain from wide-area coverage ALS because the lasers do not penetrate the canopy
101 with sufficient spatial-resolution to directly observe the stems. Therefore, the aforementioned
102 relationships need to be quantified. Previous studies have attempted to do this in comparable forest
103 types (Næsset and Bjercknes 2001; Lindberg et al. 2010; Lindberg and Hollaus 2012; Ene et al. 2012;
104 Eysn et al. 2015). In general, the model errors are quite high compared to volume or tree height and
105 these increase with increasing complexity of the forest in terms of species and age structure. As none
106 of the currently available models are extrapolatable to the national level in Norway, this was an
107 important facilitating aim in the current study.

108 Our objectives were twofold: (I) to describe empirical models linking stem density (number of trees
109 per ha) observed at NFI sample plots to ALS metrics that are used to map this forest attribute in a
110 fine resolution of 16 m × 16 m; to map canopy cover obtained directly from ALS data; and (II) to
111 demonstrate and assess the inclusion of these in avalanche hazard classification models for
112 recreational activities. For the latter, we use expert-classified ski-touring routes in Western Norway
113 as a reference. To the best of our knowledge, this is the first study that documents the use of high-
114 resolution forest maps for the improvement of avalanche maps for recreational purposes.

115 2 Material and methods

116 2.1 Study areas

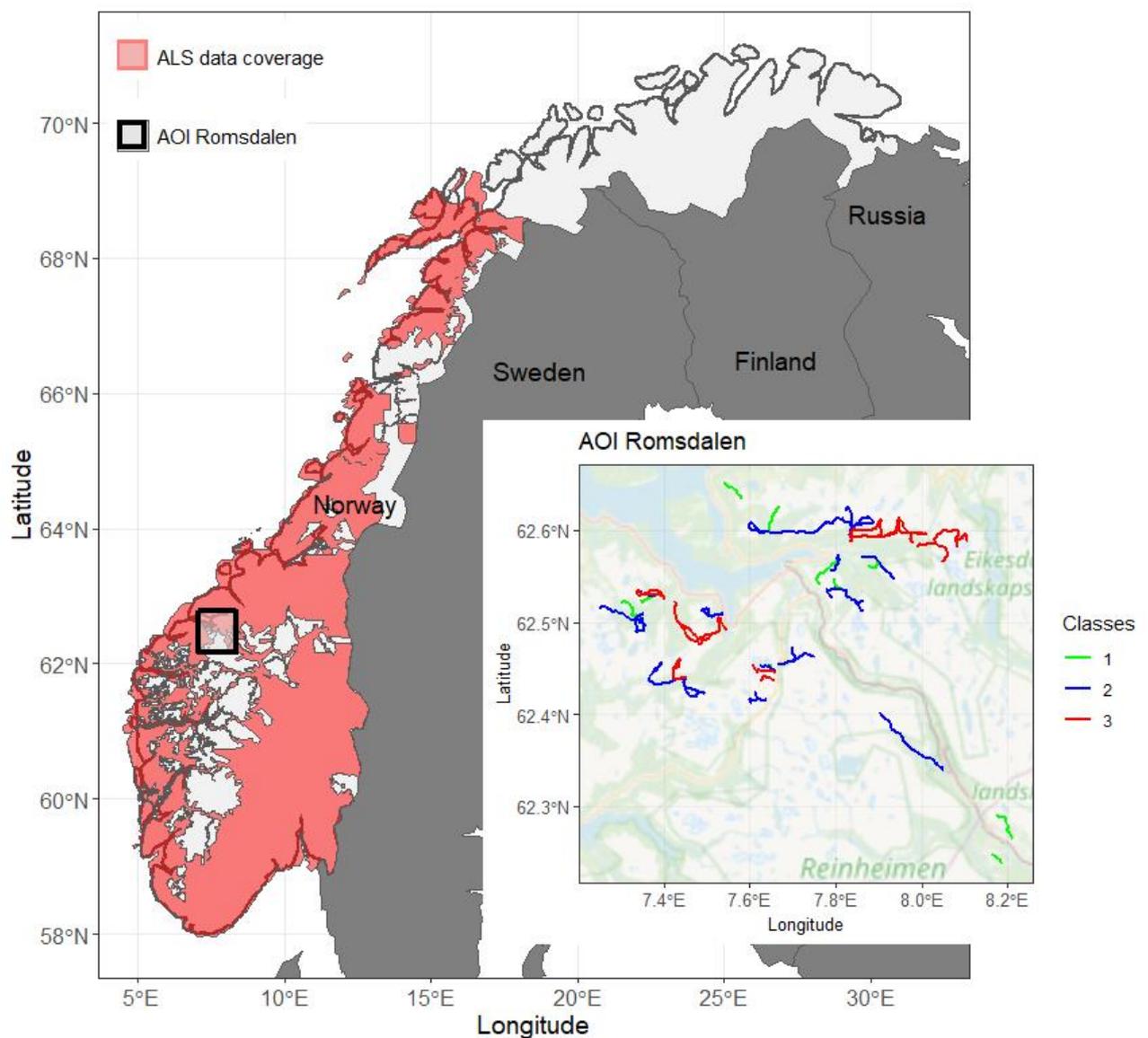
117 In this study we referred to two different areas for the different analysis levels: modelling forest
118 attributes (large part of Norway), and modelling avalanche hazard for recreational activities
119 (backcountry skiing area Romsdalen).

120 For modelling forest attributes with field reference data and auxiliary remote sensing data, we used
121 NFI data from a large part of the country covering 21.5 Mha (66% of the Norwegian mainland),
122 located in Norway between latitudes 58.0° and 69.5° N. This spatial extent was determined by the
123 availability of ALS data (Figure 1). Within the study area, forest growing conditions vary considerably
124 with latitude and elevation. The natural tree line is at around 1100 m asl in southern Norway and
125 around 130 m asl in the north. Depending on these factors, climate zones range roughly from
126 subarctic in the north and east, oceanic at the west coast, and continental in the south-east. The tree
127 species are primarily Norway spruce (*Picea abies*) and Scots pine (*Pinus sylvestris*). These make up

128 the majority of above ground biomass and standing volume. Birch (*Betula pendula* and *B. pubescens*)
129 is the most abundant species in terms of surface area and mainly occurs as early succession following
130 disturbance (including timber harvests) or in high elevation and/or latitude forests (Breidenbach et
131 al. 2020a). In this study the term broadleaves is used to represent what are mostly birch forests.
132

133 For assessing the effect of forest towards improved avalanche hazard models for recreational
134 activities we used the area of Romsdalen (Figure 1). This region is a popular destination for ski-
135 touring attracting national and international visitors. Within this area we focused on forested areas
136 on slopes that were relevant for avalanche hazard mapping along 52 documented ski-touring routes
137 (see section 2.3.1). The study area has an area of 3200 km² and the mountains reach from sea level
138 and up to 1784 m above sea level.

139



140

141 *Figure 1: Study area with airborne laser scanner (ALS) data coverage used for modelling forest characteristics,*
142 *and Romsdalen area including ski-touring routes through mountainous terrain. The terrain and touring routes*
143 *are classified according to the ATES classification scheme with classes 1 – simple (green), 2 – challenging (blue),*
144 *3 – complex (red).*

145

146 2.2 Mapping forest attributes

147 To map the forest attribute stem density, we developed a mixed-modelling regression between this
148 attribute (our response variable) and independent predictor variables calculated from remote
149 sensing data. We used field measured stem density from the Norwegian NFI (Breidenbach et al.
150 2020a) as the response variable, and remote sensing data from airborne laser scanning (ALS) and
151 Sentinel-2 satellite images (S2) as independent predictor variables (sections 2.2.2 and 2.2.3). The
152 attribute canopy cover was obtained from the ALS data directly and compared to and visually
153 assessed canopy cover in the NFI.

154

155 2.2.1 Data

156 National Forest Inventory data

157 We used the permanent sample plots of the Norwegian NFI as reference data (Breidenbach et al.
158 2020a). In the study area, the NFI is based on a systematic grid of 3 km x 3 km in the lowland region
159 and 3 km x 9 km in the low-productive, birch-dominated mountain region. For trees with a diameter
160 at breast height ≥ 5 cm (dbh, 1.3 m above ground), parameters are measured on circular plots with
161 a size of 250 m².

162 We used NFI plots located in stands dominated by spruce, pine, and broadleaved trees (defined as
163 plots with $\geq 75\%$ timber volume of each tree species, respectively). From these plots, we only
164 selected NFI plots in productive forest (yearly volume increment > 0.1 m³ / ha), and in one-layered
165 forests for stem density modelling, resulting in 1,351 spruce, 1,064 pine, and 535 broadleaved
166 dominated plots that were used for modelling stem density (Table 1). Canopy cover is only assessed
167 for unproductive forest and other wooded land in the NFI (Viken 2021, p. 69) and, therefore, the
168 number of plots used for the analysis of the ALS-based canopy cover measurement was 247, 205,
169 and 112 for spruce, pine, and broadleaved forest, respectively.

170

171 *Table 1: Summary statistics of the Norwegian national forest inventory (NFI) data used for modelling in this*
172 *study.*

	Height (m)	Volume* (m ³)	Stem density**	Canopy cover (%)
	Overall			
Min	4.9	5.2	40	0
Max	34.1	1144.7	2840	99.0
Mean	15.2	208.9	860	68.5
STD	4.4	152.2	463	23.3
	Spruce			
Min	5.7	7.6	40	3.0
Max	34.1	1144.7	2840	99.0
Mean	17.0	277.1	1030	75.8
STD	4.4	172.2	451	19.5
	Pine			
Min	7.2	12.7	40	5.0
Max	28.3	693.7	2560	99.0
Mean	14.8	176.2	652	64.4
STD	3.5	106.2	370	22.0

	Broadleaved trees			
Min	4.9	5.2	40	0.0
Max	26.4	400.7	2760	99.0
Mean	11.3	101.7	845	60.2
STD	3.5	70.9	485	28.1

173 *Volume with bark; **number of trees \geq 8 cm diameter at breast height (dbh) per ha.

174

175 Remote sensing data

176 ALS data were acquired during several measurement campaigns for the study area between 2010
 177 and 2019 with a density of 2 to 5 pulses per m². A high-resolution digital terrain model (DTM, 1 m x 1
 178 m pixel size) was produced from the last-return data by the Norwegian Mapping Authority
 179 (Kartverket 2019). The ALS point cloud was height-normalized by subtracting the DTM elevation from
 180 corresponding point cloud elevation using bi-directional interpolation. The height-normalized point
 181 cloud was used to calculate various descriptive metrics for each NFI plot based on first returns, first
 182 returns above 2 m height above ground, and last returns. The metrics included mean, variance,
 183 coefficients of variation, kurtosis and skewness of ALS return heights, 10th, 25th, 50th, 75th, 90th, and
 184 95th height percentiles, and ALS return density metrics for 10 height slices (d0 – d9). A canopy
 185 coverage metric was calculated as percentage of first returns above 2 m (pctab2f). The DTM was
 186 resampled to 16 m x 16 m, such that the cell size corresponded approximately to the area covered by
 187 an NFI plot (250 m²). From the DTM, terrain slope was computed as a raster with a cell size of 16 m x
 188 16 m. S2 bottom of atmosphere reflectance images acquired between 30 June and 31 July 2018 were
 189 mosaiced using the bands B2, B3, B4, B5, B6, B7, B8, B8A, B11, and B12, measuring reflectance in the
 190 visible, NIR and SWIR spectrum (Drusch et al. 2012). The normalized difference vegetation index
 191 (NDVI) was calculated as band 8 minus band 4 divided by band 8 plus band 4 and tested as predictor
 192 in the prediction models.

193

194 2.2.2 Modelling and mapping tree density

195 In the Norwegian forest resource mapping project SR16 (Astrup et al. 2019; Hauglin et al. 2021) linear
 196 mixed regression models were developed estimating various forest properties. These models have
 197 the structure:

$$198 \quad y = \mathbf{X}\beta + \mathbf{Z}u + \epsilon, \text{ with } u \sim N(0, \mathbf{G}) \text{ and } \epsilon \sim N(0, \mathbf{R}), \quad (\text{Equation 1})$$

199 where y is the dependent response variable, \mathbf{X} and \mathbf{Z} are the design matrices for fixed and random
 200 effects, respectively, β are the fixed effects parameters, u is a vector of random effects, and \mathbf{G} and \mathbf{R}
 201 are the covariance matrices for random effects and residual errors, respectively. We used the nlme
 202 package (Pinheiro et al. 2020) in the statistics software R (R Core Team 2020) to estimate the model
 203 parameters. A starting model was stepwise reduced by forward and backward selection of predictors
 204 based on Akaike Information Criterion as stopping rule (stepAIC function in R (Venables and Ripley
 205 2002)) and was further reduced by backward selection based on p-values ($p < 0.05$). We used the
 206 information on ALS project acquisition as random effect on the intercept in the models to account for
 207 differences in ALS data collection between the different projects. Among others, we used the
 208 predicted coefficient of determination, R^2 , for model assessment

$$209 \quad \text{Predicted } R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (\text{Equation 2})$$

210 where y_i and \hat{y}_i are observed and predicted values in unit i and the number of units is denoted by n .

211

212 We used the approach described above and the model structure in Equation (1) to fit linear-mixed
213 effects models predicting stem density (for trees ≥ 8 cm dbh) for three tree species of interest. Area
214 wide predictions of the forest attributes were made by applying the developed models to 16 m x 16
215 m pixels, which is similar to the area of the NFI plots used during model fitting. A tree species map
216 (Breidenbach et al. 2020b) was used to apply the corresponding tree species-specific model.

217

218 2.2.3 Mapping canopy cover

219 Canopy cover was calculated from the ALS data directly by analyzing the spatial distribution of laser
220 echoes with above-ground heights ≥ 5 m. The normalized laser point cloud of each 16 m x 16 m
221 pixel was divided into 64 voxels of size $2 \times 2 \times h$ m³, where h is the vertical distance from 5 m above
222 ground to the maximum above-ground echo height. Each voxel was thus defined by a 2 x 2 m² base
223 at 5 m above ground and extended upwards to the height of the highest echo, i.e., h . Note that this
224 means that the shape of the voxels where in most cases not cubical, but typically were higher than
225 the 2 m sides of the base and that forests smaller than 5 m height will have a crown cover of 0. The
226 proportion of non-empty voxels were used as a representation for canopy cover in the 16 m x 16 m
227 pixel, with non-empty voxels being voxels containing at least one laser echo. Canopy cover was then
228 compared to field-based estimates of canopy cover at NFI plots.

229

230 2.3 Avalanche hazard maps for recreational activities

231 2.3.1 Reference data generation: avalanche hazard classification for routes

232 As a basis for comparison in the case study area, we used the hazard classification of (ski-touring)
233 routes by local avalanche experts. The dataset consists of 52 routes with a total length of 282 km
234 (Figure 1, Table 2) that were manually mapped by local avalanche experts of the Norwegian Water
235 Resources and Energy Directorate (NVE) in 2018 (Larsen et al. 2020b). NVE is the government
236 authority for avalanche hazard mapping in Norway. The work was done using the ATES v1.04 defined
237 by Statham et al. (2006) presented in Table 2. Methods used included: a GIS web tool, visual
238 interpretation of aerial imagery, local expertise, and field surveys. Each route is classified according
239 to eleven different avalanche terrain factors and classified as either simple, challenging, or complex
240 terrain. If the route is within the challenging or complex definition of slope angle for a short section
241 of the trip, the whole trip will be classified as challenging or complex.

242

243 *Table 2: ATES Public Communication Model (v1.04) (Statham et al. 2006), and summary of the 52 documented ski-touring*
244 *routes in Romsdalen used in this study.*

Description	Class	Terrain Criteria for Avalanche Exposure (relevant excerpt)	# Routes	Total length (km)
Simple	1	Exposure to low angle or primarily forested terrain. Some forest openings may involve the runout zones of infrequent avalanches. Many options to reduce or eliminate exposure.	12	43

Challenging	2	Exposure to well defined avalanche paths, starting zones or terrain traps; options exist to reduce or eliminate exposure with careful route finding.	26	131
Complex	3	Exposure to multiple overlapping avalanche paths or large expanses of steep, open terrain; multiple avalanche starting zones and terrain traps below; minimal options to reduce exposure.	14	108

245

246

247 2.3.2 The AutoATES model

248 To investigate the effect of forest data on ATES maps for recreational activities, we used the
 249 AutoATES algorithms developed by Larsen et al. (2020b, a). We examined the impact of using either
 250 canopy cover or stem density and compared it to AutoATES with no forest data as input as per Larsen
 251 et al. (2020b, a). AutoATES is an automated algorithm that is made to create spatial ATES maps using
 252 a DEM and optional forest data as input. In the present study a DEM based on ALS data was used
 253 (Kartverket 2019).

254 The full methodology of the AutoATES model is described in detail in Larsen et al. (2020b), and it will
 255 therefore only be briefly presented here. The first step of the algorithm is to calculate the potential
 256 release areas (PRA) using the algorithm developed by Veitinger et al. (2016) and modified by Sharp et
 257 al. (2018). Using a fuzzy operator, they combine the input variables slope angle, terrain roughness,
 258 wind shelter, and stem density using a Cauchy membership value (Jang et al. 1997). In previous
 259 publications, stem density has not been available in high resolution. Cauchy membership values must
 260 be defined for each input variable:

$$261 \mu(x) = \frac{1}{1 + \left(\frac{x-c}{a}\right)^{2b}} \quad (\text{Equation 3})$$

262 where $\mu(x)$ is the Cauchy membership value, x is an input variable, and a , b , and c are parameters
 263 which control the weight of each input variable. We use the parameter values suggested by Sharp et
 264 al. (2018) for slope angle, roughness, wind shelter, and stem density. There are currently no
 265 parameter values documented for canopy cover, therefore we set the values as given in Table 3. A
 266 fuzzy operator is used to generate the final PRA values as a result of the four Cauchy membership
 267 values (Table 3) (Veitinger et al. 2016; Sharp et al. 2018). The PRA zone is classified as ATES class 3
 268 (complex terrain).

269

270 *Table 3: The parameters used to calculate the fuzzy membership of forest input in the PRA model.*

Parameter:	a	b	c
Slope angle (Sharp et al. 2018)	7	2	38
Roughness (Sharp et al. 2018)	0.01	5	-0.007
Wind shelter (Sharp et al. 2018)	2	3	2
Stem density (Sharp et al. 2018)	350	2.5	-150
Canopy cover	240	25	-200

271

272 In a second step, a runout model is used to calculate areas downslope of the PRAs that could be
 273 affected by an avalanche. For modelling the runout, FlowPy (D'Amboise et al. 2021) is used, which is
 274 a flow model that is limited by the angle of reach, i.e. the angle from the top pf the PRA to the
 275 lowermost point of the avalanche path (Larsen et al. 2020b). The algorithm is controlled by
 276 parameters for slope angle (SAT), cell count (CC), angle of reach (AAT), and PRA threshold (PRA THD)

277 (Table 4). Using these parameters, the AutoATES model outputs a preliminary layer with the
 278 categorical classes simple, challenging, and complex terrain.
 279

280 *Table 4: The input parameters used for AutoATES (Larsen et al. 2020b). The parameters were used in models that included*
 281 *either no forest data, stem density, or canopy cover.*

Parameter:	AAT1	AAT2	AAT3	CC1	CC2	SAT01	SAT12	SAR23	SAT34	PRA THD
Value:	20°	25°	31°	50	250	15°	25°	31°	37°	0.15

282

283 To account for forest attributes in the runout zone, the forest map information of each pixel is split
 284 into four categories given the cut points in Table 5. Using map algebra equations on each of these
 285 forest density categories, the ATES classifications are then kept the same, or altered to a lower ATES-
 286 class value (Larsen et al. 2020b). For example, if the initial ATES class is 3 (complex) but forest is
 287 dense (category 4), the final ATES class is 2 (challenging).

288 *Table 5: The parameters used in the raster calculator to account for forest density outside of the PRA.*

Parameter:	Cut point 1	Cut point 2	Cut point 3
Stem density (n/ha)	100	250	500
Canopy cover (%)	10	25	65

289

290 To compare the AutoATES classification with the manual ATES classification for skiing routes, the
 291 values of the AutoATES map were extracted every 10 m along the length of the route. The 95th
 292 percentile of the extracted AutoATES predictions was used to assign one predicted class per route.

293

294 2.4 Evaluation criteria

295 We used the evaluation criteria RMSE, and RMSE% to evaluate the modelled forest attribute stem
 296 density and the calculated canopy cover (Equations, 4, 5).

$$297 \quad RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad (\text{Equation 4})$$

$$298 \quad RMSE\% = 100 \times \frac{RMSE}{\frac{1}{n} \sum_{i=1}^n (y_i)} \quad (\text{Equation 5})$$

299 where y_i and \hat{y}_i are observed and predicted values in unit i . The number of units in data is denoted
 300 by n .

301 To evaluate the overall route classification, we used overall accuracy (OA), and to evaluate each class
 302 separately we used producers' accuracy (PA), users' accuracy (UA), and F1 score according to

$$303 \quad OA = \frac{\sum \text{True positives}}{\text{Total number of observations}} \quad (\text{Equation 6})$$

$$304 \quad PA = \frac{\text{True positive}}{\text{True positive} + \text{False negative}} \quad (\text{Equation 7})$$

$$305 \quad UA = \frac{\text{True positive}}{\text{True positive} + \text{False positive}} \quad (\text{Equation 8})$$

$$306 \quad F1 = 2 \times \frac{PA \times UA}{PA + UA} \quad (\text{Equation 9})$$

307

308 3 Results

309 3.1 Forest attribute maps

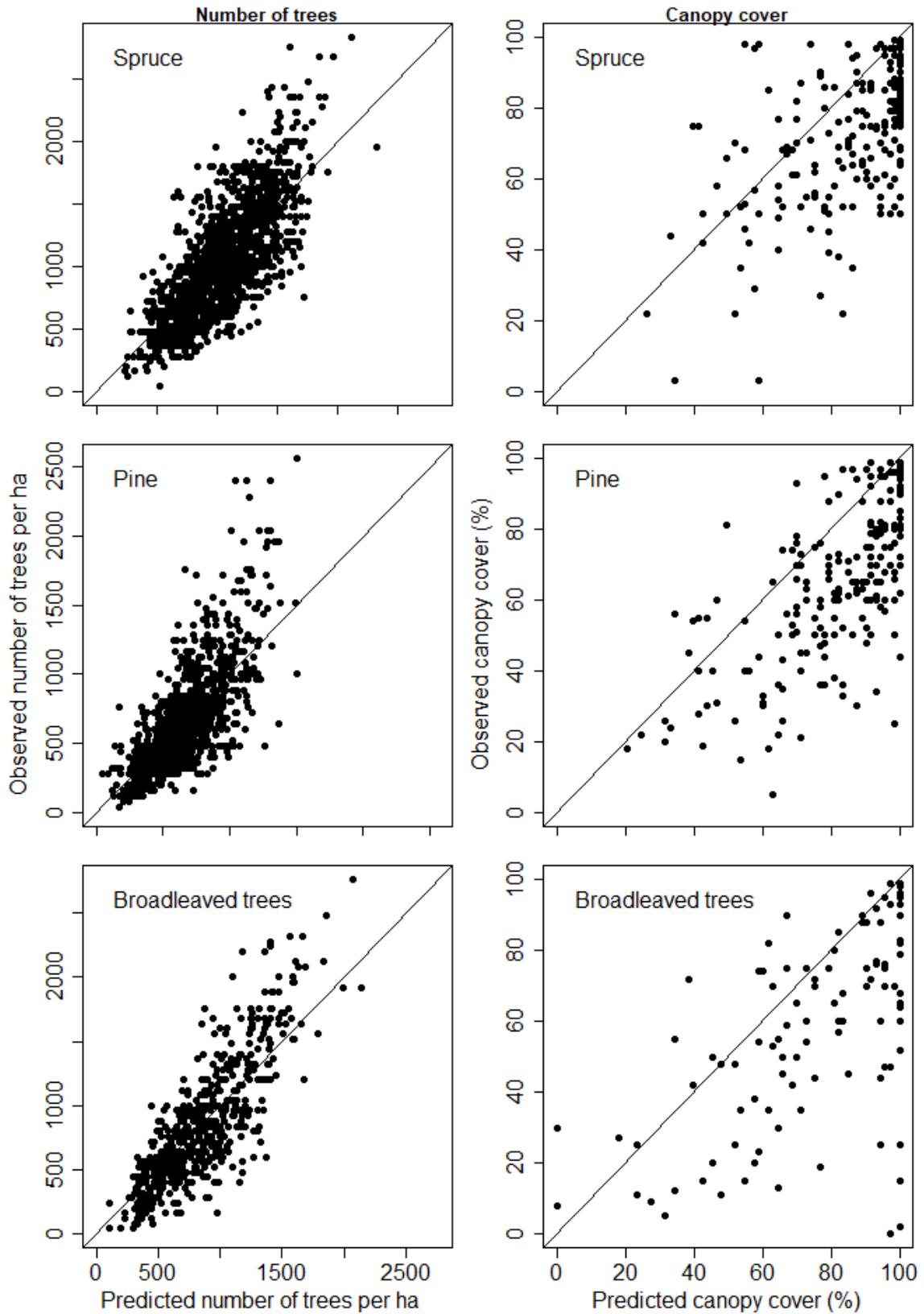
310 We modelled the stem density using linear mixed effects models, and directly calculated canopy
311 cover from ALS data for the spruce, pine, and broadleaved forests (Figure 2). The fit statistics
312 associated with the linear-mixed models for stem density showed that the results for spruce were
313 the most accurate in terms of leave-one-out cross-validated $RMSE_{cv}\%$ (Table 6). The significant
314 predictors were similar for the spruce and pine models. Both models contained the 75th percentile of
315 first ALS returns, (h75f) and its squared version (h75fsq), the percentage of first ALS returns above 2
316 m height, (pctab2f) and its squared version (pctab2fsq), the interactions between h75f and pctab2f,
317 and between h75fsq and pctab2fsq, the normalized difference vegetation index (NDVI), and terrain
318 slope. For the spruce model one additional first return density metric d6f was included, and for the
319 pine model the first return density metric d4f was included. The model for broadleaved forests only
320 included the predictors h75fsq, pctab2fsq, and d6f. Model details and variance components of the
321 stem density models are presented in Section 6 in the Appendix in Table 9 and Table 10.

322

323

324

325



327

328 *Figure 2: Observed vs. predicted stem density (number of trees per ha, left column), and canopy cover (right*
 329 *column) stratified into three tree species groups: spruce (top row), pine (middle row), and broadleaved trees*
 330 *(bottom row).*

331

332 The R^2 of the stem density models was 0.59, 0.56, 0.68, and 0.62 for spruce, pine, broadleaved, and
 333 all forest, respectively. The Pearson correlation between canopy cover directly obtained from the ALS
 334 data and canopy cover assessed at NFI plots was 0.58, 0.67, 0.62, and 0.64 for spruce, pine, and
 335 broadleaved, respectively, and all forest (Figure 2, Table 6).

336 The two plots in broadleaved forest that have zero predicted canopy cover (Figure 2, bottom right)
 337 are due to low ALS returns. Since we only used ALS returns above 5 m height, canopy cover
 338 predictions are less accurate in low forest.

339

340 *Table 6: Characteristics of the fitted models and canopy cover relationship*

	Stem density	Canopy cover*
Overall		
RMSE _{cv}	300.9	23.3
RMSE _{cv} %	35.0	34.0
Norway spruce		
RMSE _{cv}	307.9	20.2
RMSE _{cv} %	29.9	30.8
Scots pine		
RMSE _{cv}	277.4	23.6
RMSE _{cv} %	42.5	36.2
Broadleaved trees		
RMSE _{cv}	330.7	28.7
RMSE _{cv} %	39.1	38.8

341 * RMSE_{cv} in percentage points, RMSE_{cv}% in percentage to the mean

342

343 3.2 Assessment of hazard maps for recreational activities

344 Overall, including forest attributes in the AutoATES model improved terrain and, thereby, route
 345 classifications with regard to avalanche hazard (Figure 3). Using the 95th percentile of predicted
 346 values to assign one class per route, AutoATES-Forest classifications showed a considerable
 347 improvement compared to AutoATES without forest attribute (Table 7).

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358 *Table 7: Confusion matrices for 282 km manually classified routes (ATES) in Romsdalen and the automated ATES*
 359 *algorithms AutoATES, AutoATES-Forest (canopy cover) and AutoATES-Forest (stem density) on entire-route*
 360 *level. Routes were classified according to the 95th percentile of AutoATES and AutoATES-Forest predictions.*
 361 *Values represent km of routes (route count is given in parentheses).*

<u>No forest parameters included</u>		AutoATES		
		Class 1	Class 2	Class 3
Manually mapped (ATES)	Class 1 simple	10.5 (3)	21.8 (7)	10.6 (2)
	Class 2 challenging	0 (0)	59.9 (12)	71.2 (14)
	Class 3 complex	0 (0)	23.1 (3)	84.7 (11)

<u>Including canopy cover</u>		AutoATES-Forest		
		Class 1	Class 2	Class 3
Manually mapped (ATES)	Class 1 simple	23.1 (6)	13.8 (5)	6.0 (1)
	Class 2 challenging	0 (0)	90.1 (16)	41.0 (10)
	Class 3 complex	0 (0)	31.9 (4)	75.8 (10)

<u>Including stem density</u>		AutoATES-Forest		
		Class 1	Class 2	Class 3
Manually mapped (ATES)	Class 1 simple	29.2 (8)	13.7 (4)	0 (0)
	Class 2 challenging	24.7 (3)	78.9 (16)	27.5 (7)
	Class 3 complex	0 (0)	38.7 (5)	69.0 (9)

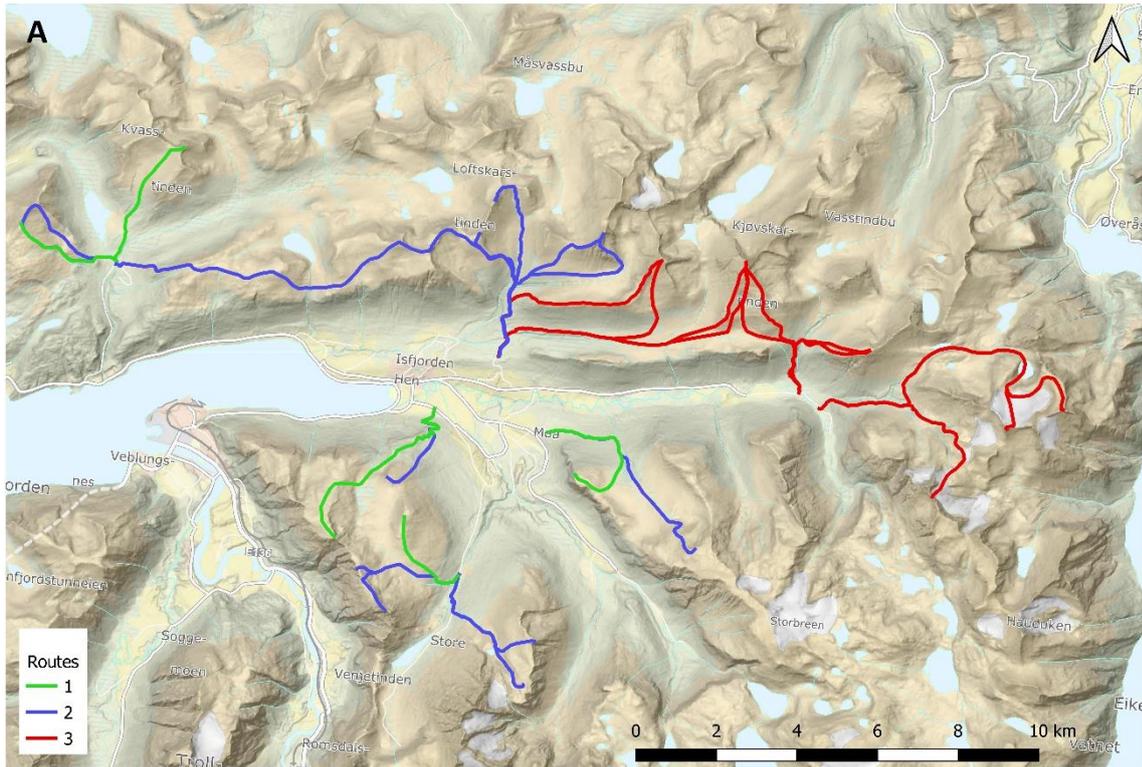
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 363 Overall accuracies weighted by route lengths increased from 0.55 for AutoATES to 0.67 for AutoATES-
 364 Forest using canopy cover and to 0.63 for AutoATES-Forest using stem density. Similarly, also the
 365 other accuracy statistics PA, UA, and F1 score improved (Table 8). Only PA of class 3 decreased when
 366 using forest properties in the model since more routes that were marked as class 3 in the reference
 367 were predicted as class 2.

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 369 *Table 8: accuracies for routes assigned to one class; routes were assigned one predicted value using the 95th percentile of*
 370 *predicted pixel values within a route; OA = Overall accuracy, PA = Producer's accuracy, UA = User's accuracy.*

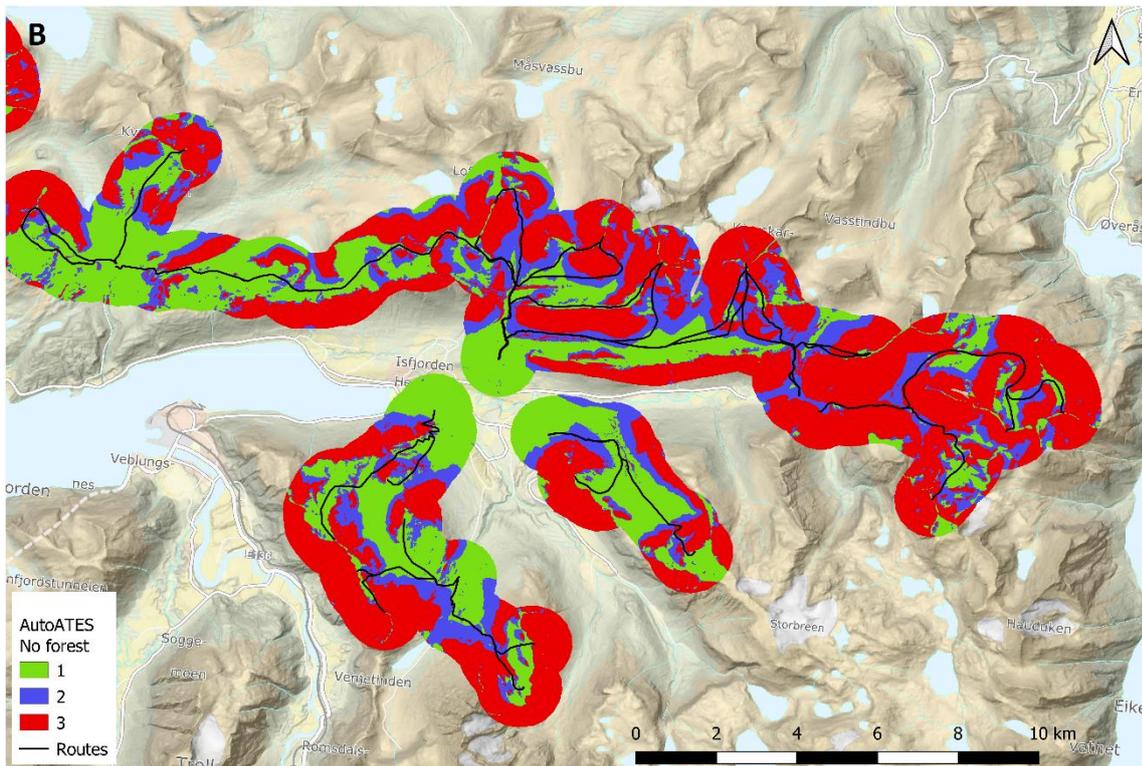
	OA	F1 score			PA			UA		
		Class 1	Class 2	Class 3	Class 1	Class 2	Class 3	Class 1	Class 2	Class 3
AutoATES No forest	0.55	0.39	0.51	0.62	0.25	0.46	0.79	1.00	0.57	0.51
AutoATES Canopy cover	0.67	0.70	0.58	0.66	0.54	0.69	0.70	1.00	0.66	0.62
AutoATES Stem density	0.63	0.60	0.60	0.68	0.68	0.60	0.64	0.54	0.60	0.72

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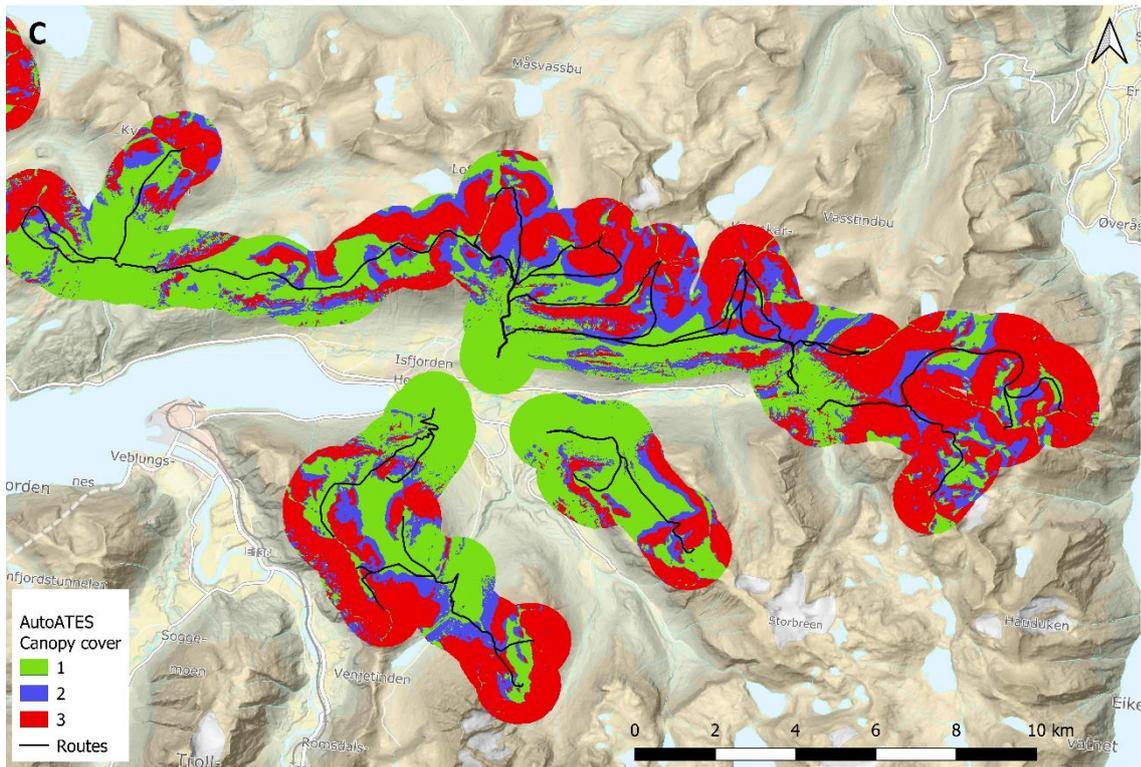
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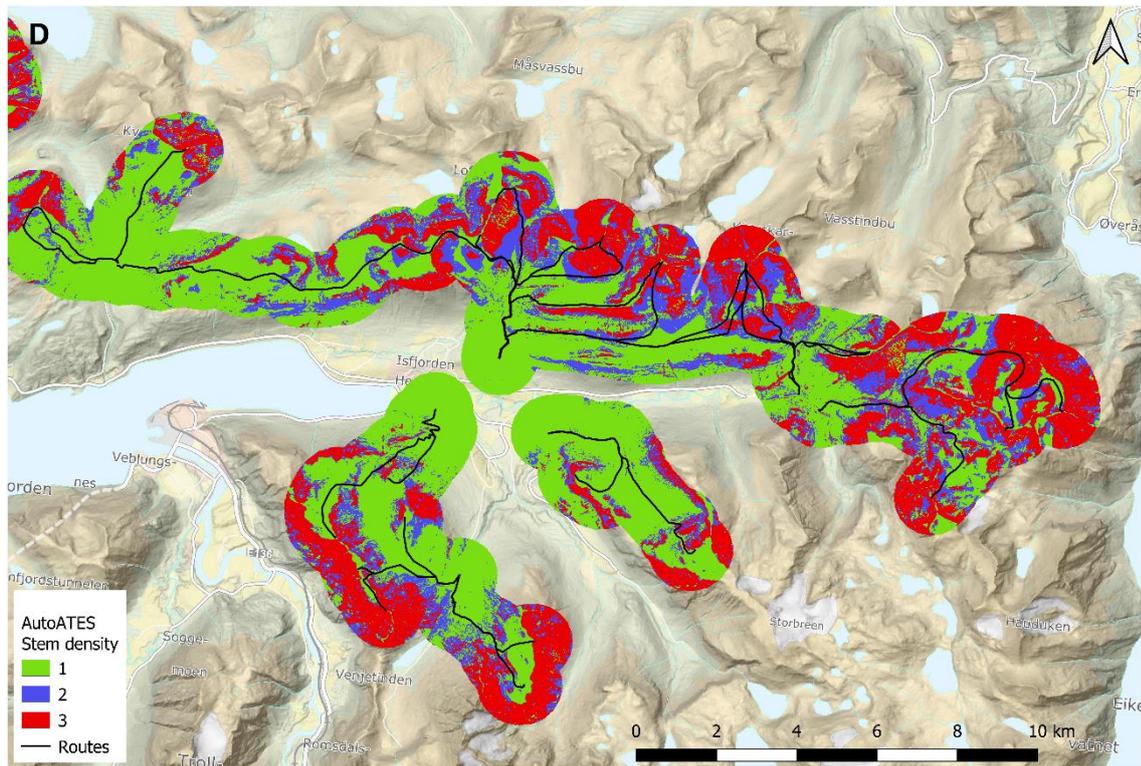
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377 *Figure 3: Area around the town Isfjorden; A) manually ATES classification of touring routes according to the part*
378 *with the greatest hazard used as reference (class 1 = simple in green, class 2 = challenging in blue, class 3 =*
379 *complex in red); B) output of AutoATES model without forest; C) output of AutoATES-Forest model with forest*
380 *canopy cover as model input; D) output of AutoATES-Forest model with forest stem density as model input.*



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383 *Figure 3 continued.*

384

385 4 Discussion

386 In this study, we modelled and mapped the forest attributes of stem density and canopy cover
 387 respectively using NFI and remote sensing data collected over a large area in Norway. We included

388 these forest attribute maps as inputs in the spatially explicit avalanche hazard model AutoATES-
389 Forest in order to improve avalanche hazard maps for recreational activities. Forest attribute and
390 avalanche hazard maps may in this way become valuable tools for informing forest management
391 decisions aiming at the utilization of forests as nature-based solutions for avalanche-related disaster
392 risk reduction (EEA 2021).

393 We predicted stem density and found an overall R^2 and cross-validated RMSE of 0.62 and 301
394 (35%), respectively. Tompalski et al. (2019) found similar results with R^2 and RMSE of 0.37 and 293
395 (42%), respectively, for modelling stem density in Canada. Lindberg and Hollaus (2012) compared
396 area-based and single tree-based approaches for estimating the number of trees and found RMSE of
397 53% (area-based) and 63-92% (single tree based). Ene et al. (2012) used the single tree-based
398 approach and reported 46-50% detection rate for stem number estimates in heterogenous boreal
399 forests. Eysn et al. (2015) reported 47% overall tree detection rate in heterogenous alpine forest.
400 Stem density is difficult to predict using the type of remote sensing data used in this study. While
401 using very high-resolution ALS or drone data (Puliti et al. 2020; Persson et al. 2022) would allow for
402 analyses on single tree trunk level that might result in higher accuracies, collecting such high-
403 resolution data on the large spatial scale used in this study is currently not feasible.

404 In an initial analysis, we also compared canopy cover calculated as proposed by Korhonen et al.
405 (2011) with canopy cover from the NFI. However, this relationship was worse than our voxel-based
406 approach and therefore not further considered in this study. The relation between predicted and
407 observed canopy cover was not as good as for stem density. This can partially be attributed to the
408 fact that canopy cover in the NFI is not measured, but visually estimated by the NFI crew.

409 Using the forest attributes stem density or canopy cover in the AutoATES-Forest models improved
410 the terrain and route hazard classification compared to the AutoATES model without forest
411 attributes. The percentage of class 1 (simple terrain) wrongly classified as class 2 (challenging) or 3
412 (complex) was reduced. When classifying ski-touring routes linearly using manual ATES, the overall
413 class is decided by the most hazardous area on a given route. This means that if the route is located
414 mostly in simple terrain (class 1), the whole route could be classified as complex terrain (class 3) if
415 there is a short section of this type of terrain along the given route. This is a deliberate design feature
416 that errs on the side of safety. A result of this is that even though the algorithm, which works on the
417 pixel level, defines a large percentage of a given route as less hazardous than the manual
418 classification class rating, it is not wrong. Therefore, the 95th percentile of pixel values from the
419 AutoATES predictions was used for assigning one hazard class to a route.

420 Using the forest attribute canopy cover resulted in slightly better classifications, but the difference
421 between the two forest metrics was not as great as the difference between the use of forest metrics
422 and the lack of forest metrics. These results indicate that adding spatially explicit information on
423 forest attributes are beneficial for terrain evaluation. Other forest properties such as diameter
424 distributions can be mapped from laser scanner data (Räty et al. 2021) and should be considered as
425 input to avalanche hazard models in the future. Furthermore, avalanche hazard models could be
426 further improved to utilize forest attributes as continuous values.

427 Brožová et al. (2020) evaluated variables extracted from ALS and photogrammetric point clouds
428 towards their influence on simulation results of avalanche runout in a case study in Switzerland.
429 Remote sensing based tree heights, canopy coverage, and DTM roughness were used for avalanche
430 simulation. They concluded that remote sensing data with a fine resolution of about 1 m x 1 m were
431 generally suitable to model relevant forest attributes used as input for avalanche simulation. The
432 simulation results using the two data sources – ALS and photogrammetric point clouds – were both

433 sufficiently accurate for numerical modelling and for real-world applications in snow avalanche
434 hazard mapping using the RAMMS model. However, simulations of only two avalanches were
435 analyzed. Bühler et al. (2022) described automated avalanche hazard mapping using the RAMMS
436 model in one Canton in Switzerland. Terrain slope and the forest properties percentage of crown
437 cover and gap width were used to predict a 'protection forest index' for each forested raster cell of 5
438 m x 5 m. Threshold values were found defining a sufficient protection forest index for two different
439 return period scenarios (frequent and rare). This way, forest was treated as a binary input variable
440 either being present and influencing an avalanche or not. This approach is similar to ours for the
441 runout zone where we define four groups of forest types that influence avalanche behavior.
442 However, Bühler et al. (2022) focus on avalanche hazard modelling for regional planning with
443 avalanche return periods of 10-30 and 100-300 years. In the present study we focus on avalanche
444 hazard modelling for backcountry ski-touring, where return periods are much shorter.

445 A wider implication of these findings is that the value of ecosystem services, such as the protection
446 function of forests, is often difficult to assess. In this respect, our study showed the positive effect of
447 forest in avalanche hazard prediction, and this is something that can be quantified, at least spatially.
448 The authors jointly consider that no price should be put on human lives and therefore we will not
449 enter into discussion of the monetary value of such protection here, though examples exist (e.g Grilli
450 et al. 2020) and it is no doubt an important subject for forest owners whose primary interests are
451 timber revenues. In this respect however, we feel that protection should influence forest
452 management decisions, but that significantly more research is required to investigate optimal forest
453 management of protective forests in a Norwegian context.

454 Finally, mapping the probability of avalanche releases is meant as an additional planning aid for route
455 choice, much like a weather forecast, and can be wrong. Avalanche conditions change dramatically
456 depending on snow conditions and these are not in any way included in the ATES system. While we
457 strive to improve the decision-making tools, these are no substitute for local evaluation of the
458 current conditions on the ground, and this requires specific training and experience. Even then,
459 avalanches pose a significant threat and safety is solely the responsibility of the individual.
460 Nonetheless, we can conclude that the inclusion of forest attributes in avalanche hazard models can
461 considerably improve their predictive performance.

462

463 5 Acknowledgements

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468 6 Appendix

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470 *Table 9: stem density models; coefficients, their standard errors, and p-values for the tree species specific linear*
471 *regression models for spruce, pine, and broadleaved trees.*

Variable	Estimate	Std. Error	p-value
Stem density model for spruce			

<i>Intercept</i>	-73.85	130.87	0.573
<i>h75f</i>	37.52	23.48	0.110
<i>h75fsq</i>	-1.37	0.65	0.034
<i>pctab2f</i>	-175.99	406.92	0.665
<i>pctab2fsq</i>	1862.63	421.25	< 0.001
<i>d6f</i>	1122.08	103.12	< 0.001
<i>NDVI</i>	414.73	113.61	< 0.001
<i>slope</i>	-1.94	0.57	< 0.001
<i>h75f_x_pctab2f</i>	-89.52	35	0.011
<i>h75fsq_x_pctab2fsq</i>	1.57	0.74	0.033
Stem density model for pine			
<i>Intercept</i>	-171.32	109.02	0.116
<i>h75f</i>	16.39	15.27	0.283
<i>h75fsq</i>	0.60	0.65	0.361
<i>pctab2f</i>	364.46	421.98	0.388
<i>pctab2fsq</i>	1491.58	375.16	< 0.001
<i>d4f</i>	986.33	140.30	< 0.001
<i>NDVI</i>	240.69	110.80	0.03
<i>Slope</i>	-1.84	0.54	0.001
<i>h75f x pctab2f</i>	-126.86	32.79	< 0.001
<i>h75fsq x pctab2fsq</i>	2.37	0.84	0.005
Stem density model for broadleaved trees			
<i>Intercept</i>	191.58	41.93	< 0.001
<i>h75fsq</i>	-2.07	0.25	< 0.001
<i>pctab2fsq</i>	1255.46	91.02	< 0.001
<i>d6f</i>	993.70	180.47	< 0.001

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474 *Table 10: Variance components for fixed and random effects and residual of the stem density models for spruce, pine, and*
475 *broadleaved forest.*

Variance (%)	
Norway spruce	
Fixed effects	50.91
Random effect	5.59
Residual	43.50
Scots pine	
Fixed effects	40.72
Random effect	10.81
Residual	48.47
Broadleaved trees	
Fixed effects	48.08
Random effect	13.99
Residual	37.93

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