

[illegible]

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56 % User inputs of parameters
57 alpha = input('Enter parameter alpha ');
58 beta = input('Enter parameter beta ');
59 gamma = input('Enter parameter gamma ');
60 delta = input('Enter parameter delta ');
61 T = input('Enter maximum time T ');
62 delt = input('Enter time-step Delta t ');
63 % User inputs of initial data
64 u0_str = input('Enter initial data function u0(x,y) ','s');
65 u0_anon = @(x,y)eval(u0_str); % create anonymous function
66 u = arrayfun(u0_anon,x,y)';
67 v0_str = input('Enter initial data function v0(x,y) ','s');
68 v0_anon = @(x,y)eval(v0_str); % create anonymous function
69 v = arrayfun(v0_anon,x,y)';
70 % Enter the boundary conditions
71 k1 = input('Enter the parameter k1 in the Robin b.c. for u ');
72 k2 = input('Enter the parameter k2 in the Robin b.c. for v ');
73 g2u_str = input('Enter the Neumann b.c. g2u(x,y,t) for u ','s');
74 g2u = @(x,y,t)eval(g2u_str); % create anonymous function
75 g2v_str = input('Enter the Neumann b.c. g2v(x,y,t) for v ','s');
76 g2v = @(x,y,t)eval(g2v_str); % create anonymous function
77 % Calculate and assign some constants
78 N=round(T/delt);
79 % Degrees of freedom per variable (n)
80 [junk,n]=size(p);
81 % Number of elements (no_elems)
82 [junk,no_elems]=size(t);
83 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
84 %                               Assembly
85 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
86 m_hat=zeros(n,1);
87 K=sparse(n,n);
88 for elem = 1:no_elems
89     % Identify nodes ni, nj and nk in element 'elem'
90     ni = t(1,elem);
91     nj = t(2,elem);
92     nk = t(3,elem);
93     % Identify coordinates of nodes ni, nj and nk
94     xi = p(1,ni);
95     xj = p(1,nj);
96     xk = p(1,nk);
97     yi = p(2,ni);
98     yj = p(2,nj);
99     yk = p(2,nk);
100    % Calculate the area of element 'elem'
101    triangle_area = abs(xj*yk-xk*yj-xi*yk+xk*yi+xi*yj-xj*yi)/2;
102    % Calculate some quantities needed to construct elements in K
103    h1 = (xi-xj)*(yk-yj)-(xk-xj)*(yi-yj);
104    h2 = (xj-xk)*(yi-yk)-(xi-xk)*(yj-yk);
105    h3 = (xk-xi)*(yj-yi)-(xj-xi)*(yk-yi);
106    s1 = (yj-yi)*(yk-yj)+(xi-xj)*(xj-xk);
107    s2 = (yj-yi)*(yi-yk)+(xi-xj)*(xk-xi);
108    s3 = (yk-yj)*(yi-yk)+(xj-xk)*(xk-xi);
109    t1 = (yj-yi)^2+(xi-xj)^2; % g* changed to t*
110    t2 = (yk-yj)^2+(xj-xk)^2;
111    t3 = (yi-yk)^2+(xk-xi)^2;
112    % Calculate local contributions to m_hat

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113     m_hat_i = triangle_area/3;
114     m_hat_j = m_hat_i;
115     m_hat_k = m_hat_i;
116     % calculate local contributions to K
117     K_ki = triangle_area*s1/(h3*h1);
118     K_ik = K_ki;
119     K_kj = triangle_area*s2/(h3*h2);
120     K_jk = K_kj;
121     K_kk = triangle_area*t1/(h3^2);
122     K_ij = triangle_area*s3/(h1*h2);
123     K_ji = K_ij;
124     K_ii = triangle_area*t2/(h1^2);
125     K_jj = triangle_area*t3/(h2^2);
126     % Add contributions to vector m_hat
127     m_hat(nk)=m_hat(nk)+m_hat_k;
128     m_hat(nj)=m_hat(nj)+m_hat_j;
129     m_hat(ni)=m_hat(ni)+m_hat_i;
130     % Add contributions to K
131     K=K+sparse(nk,ni,K_ki,n,n);
132     K=K+sparse(ni,nk,K_ik,n,n);
133     K=K+sparse(nk,nj,K_kj,n,n);
134     K=K+sparse(nj,nk,K_jk,n,n);
135     K=K+sparse(nk,nk,K_kk,n,n);
136     K=K+sparse(ni,nj,K_ij,n,n);
137     K=K+sparse(nj,ni,K_ji,n,n);
138     K=K+sparse(ni,ni,K_ii,n,n);
139     K=K+sparse(nj,nj,K_jj,n,n);
140 end
141 % Construct matrix L
142 ivec=1:n;
143 IM_hat=sparse(ivec,ivec,1./m_hat,n,n);
144 L=delt*IM_hat*K;
145 % Construct matrices B1 & B2
146 B1=sparse(1:n,1:n,1,n,n)+L;
147 B2=sparse(1:n,1:n,1,n,n)+delta*L;
148 % Do the incomplete LU factorization of B1 and B2
149 [LB1,UB1] = ilu(B1,struct('type','ilutp','droptol',1e-5));
150 [LB2,UB2] = ilu(B2,struct('type','ilutp','droptol',1e-5));
151 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
152 %                               Time-stepping procedure
153 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
154 for nt=1:N
155     tn = nt*delt;
156     % Evaluate modified functional response
157     hhat = u./(alpha + abs(u));
158     % Update right-hand-side of linear system
159     F = u - u.*abs(u) - v.*hhat;
160     G = beta*v.*hhat - gamma*v;
161     rhs_u = u + delt*F;
162     rhs_v = v + delt*G;
163     % Impose Robin boundary conditions on Gamma1
164     for i = 1:el
165         node1 = cpp1(i,1);
166         node2 = cpp1(i,2);
167         x1 = p(1,node1);
168         y1 = p(2,node1);
169         x2 = p(1,node2);

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170     y2 = p(2,node2);
171     im_hat1 = 1/m_hat(node1);
172     im_hat2 = 1/m_hat(node2);
173     gamma12 = sqrt((x1-x2)^2 + (y1-y2)^2);
174     rhs_u(node1) = rhs_u(node1) + deltt*k1*u(node1)*im_hat1*gamma12/2;
175     rhs_u(node2) = rhs_u(node2) + deltt*k1*u(node2)*im_hat2*gamma12/2;
176     rhs_v(node1) = rhs_v(node1) + deltt*k2*v(node1)*im_hat1*gamma12/2;
177     rhs_v(node2) = rhs_v(node2) + deltt*k2*v(node2)*im_hat2*gamma12/2;
178 end
179 % Impose Neumann boundary condition on Gamma2
180 for i = 1:e2
181     node1 = cpp2(i,1);
182     node2 = cpp2(i,2);
183     x1 = p(1,node1);
184     y1 = p(2,node1);
185     x2 = p(1,node2);
186     y2 = p(2,node2);
187     im_hat1 = 1/m_hat(node1);
188     im_hat2 = 1/m_hat(node2);
189     gamma12 = sqrt((x1-x2)^2 + (y1-y2)^2);
190     rhs_u(node1) = rhs_u(node1) + deltt*g2u(x1,y1,tn)*im_hat1*gamma12/2;
191     rhs_u(node2) = rhs_u(node2) + deltt*g2u(x2,y2,tn)*im_hat2*gamma12/2;
192     rhs_v(node1) = rhs_v(node1) + deltt*g2v(x1,y1,tn)*im_hat1*gamma12/2;
193     rhs_v(node2) = rhs_v(node2) + deltt*g2v(x2,y2,tn)*im_hat2*gamma12/2;
194 end
195 % Solve for u and v using GMRES
196 [u,flagu,relresu,iteru]=gmres(B1,rhs_u,[],1e-6,[],LB1,UB1,u);
197 if flagu~=0 flagu,relresu,iteru,error('GMRES did not converge'),end
198 [v,flagv,relresv,iterv]=gmres(B2,rhs_v,[],1e-6,[],LB2,UB2,v);
199 if flagv~=0 flagv,relresv,iterv,error('GMRES did not converge'),end
200 end
201 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
202 %                                     Plot solutions
203 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
204 % Plot solution for u
205 figure;
206 set(gcf,'Renderer','zbuffer');
207 trisurf(t',x,y,u,'FaceColor','interp','EdgeColor','interp');
208 colorbar;axis off;title('u');
209 view ( 2 );
210 axis equal on tight;
211 % Plot solution for v
212 figure;
213 set(gcf,'Renderer','zbuffer');
214 trisurf(t',x,y,v,'FaceColor','interp','EdgeColor','interp');
215 colorbar;axis off;title('v');
216 view ( 2 );
217 axis equal on tight;

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