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1 function fe2d_n
2 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
3 %                                     Discussion
4 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
5 % 'fe2d_n.m'    2D finite element Matlab code for Scheme 2 applied
6 % to the predator-prey system with Kinetics 1. The nodes and elements
7 % of the unstructured grid are loaded from external files 't_triang.dat'
8 % and 'p_coord.dat'.
9 %
10 % Boundary conditions:
11 %   Gamma: Neumann
12 %
13 % (C) 2009 Marcus R. Garvie. See 'mycopyright.txt' for details.
14 %
15 % Modified April 7, 2014
16 %
17 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
18 %                                     Enter data for mesh geometry
19 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
20 % Read in 'p(2,n)', the 'n' coordinates of the nodes
21 load p_coord.dat -ascii
22 p = (p_coord)';
23 % Read in 't(3,no_elems)', the list of nodes for 'no_elems' elements
24 load t_triang.dat -ascii
25 t = (round(t_triang))';
26 % Construct the connectivity for the nodes on Gamma
27 edges = boundedges (p',t');
28 % Number of edges on Gamma
29 [e,junk] = size(edges);
30 % Degrees of freedom per variable (n)
31 [junk,n]=size(p);
32 % Number of elements (no_elems)
33 [junk,no_elems]=size(t);
34 % Extract vector of 'x' and 'y' values
35 x = p(1,:); y = p(2,:);
36 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
37 %                                     Enter data for model
38 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
39 % User inputs of parameters
40 alpha = input('Enter parameter alpha ');
41 beta = input('Enter parameter beta ');
42 gamma = input('Enter parameter gamma ');
43 delta = input('Enter parameter delta ');
44 T = input('Enter maximum time T ');
45 delt = input('Enter time-step Delta t ');
46 % User inputs of initial data
47 u0_str = input('Enter initial data function u0(x,y) ','s');
48 u0_anon = @(x,y)eval(u0_str); % create anonymous function
49 u = arrayfun(u0_anon,x,y)';
50 v0_str = input('Enter initial data function v0(x,y) ','s');
51 v0_anon = @(x,y)eval(v0_str); % create anonymous function
52 v = arrayfun(v0_anon,x,y)';
53 % Enter the boundary conditions
54 gu_str = input('Enter the Neumann b.c. gu(x,y,t) for u ','s');
55 gu = @(x,y,t)eval(gu_str); % create anonymous function

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56 gv_str = input('Enter the Neumann b.c. gv(x,y,t) for v ', 's');
57 gv = @(x,y,t)eval(gv_str); % create anonymous function
58 % Calculate and assign some constants
59 N=round(T/delt);
60 % Degrees of freedom per variable (n)
61 [junk,n]=size(p);
62 % Number of elements (no_elems)
63 [junk,no_elems]=size(t);
64 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
65 %                                     Assembly
66 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
67 m_hat=zeros(n,1);
68 K=sparse(n,n);
69 for elem = 1:no_elems
70     % Identify nodes ni, nj and nk in element 'elem'
71     ni = t(1,elem);
72     nj = t(2,elem);
73     nk = t(3,elem);
74     % Identify coordinates of nodes ni, nj and nk
75     xi = p(1,ni);
76     xj = p(1,nj);
77     xk = p(1,nk);
78     yi = p(2,ni);
79     yj = p(2,nj);
80     yk = p(2,nk);
81     % Calculate the area of element 'elem'
82     triangle_area = abs(xj*yk-xk*yj-xi*yk+xk*yi+xi*yj-xj*yi)/2;
83     % Calculate some quantities needed to construct elements in K
84     h1 = (xi-xj)*(yk-yj)-(xk-xj)*(yi-yj);
85     h2 = (xj-xk)*(yi-yk)-(xi-xk)*(yj-yk);
86     h3 = (xk-xi)*(yj-yi)-(xj-xi)*(yk-yi);
87     s1 = (yj-yi)*(yk-yj)+(xi-xj)*(xj-xk);
88     s2 = (yj-yi)*(yi-yk)+(xi-xj)*(xk-xi);
89     s3 = (yk-yj)*(yi-yk)+(xj-xk)*(xk-xi);
90     t1 = (yj-yi)^2+(xi-xj)^2; % g* changed to t*
91     t2 = (yk-yj)^2+(xj-xk)^2;
92     t3 = (yi-yk)^2+(xk-xi)^2;
93     % Calculate local contributions to m_hat
94     m_hat_i = triangle_area/3;
95     m_hat_j = m_hat_i;
96     m_hat_k = m_hat_i;
97     % calculate local contributions to K
98     K_ki = triangle_area*s1/(h3*h1);
99     K_ik = K_ki;
100    K_kj = triangle_area*s2/(h3*h2);
101    K_jk = K_kj;
102    K_kk = triangle_area*t1/(h3^2);
103    K_ij = triangle_area*s3/(h1*h2);
104    K_ji = K_ij;
105    K_ii = triangle_area*t2/(h1^2);
106    K_jj = triangle_area*t3/(h2^2);
107    % Add contributions to vector m_hat
108    m_hat(nk)=m_hat(nk)+m_hat_k;
109    m_hat(nj)=m_hat(nj)+m_hat_j;
110    m_hat(ni)=m_hat(ni)+m_hat_i;
111    % Add contributions to K
112    K=K+sparse(nk,ni,K_ki,n,n);

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[illegible]

```
170 figure;
171 set(gcf,'Renderer','zbuffer');
172 trisurf(t',x,y,u,'FaceColor','interp','EdgeColor','interp');
173 colorbar,axis off;title('u');
174 view ( 2 );
175 axis equal on tight;
176 % Plot solution for v
177 figure;
178 set(gcf,'Renderer','zbuffer');
179 trisurf(t',x,y,v,'FaceColor','interp','EdgeColor','interp');
180 colorbar,axis off;title('v');
181 view ( 2 );
182 axis equal on tight;
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