# Three Fog Computing Based Variants of Congestion Control in ITS 

Ananya Paul, Kiton Ghosh, Sulata Mitra


#### Abstract

The growth of vehicles and inadequate road capacity in the urban area trigger traffic congestion and raise the frequency of road accident. Therefore the need of drastically reducing traffic congestion is a significant concern. Advancement in the technology like fog computing, Internet of Things (IoT)in Intelligent Transportation Systems (ITS) aid in the more constructive management of traffic congestion. Three IoT basedFog computing oriented models are designed in the present work for mitigating traffic congestion. The first two schemes are vehicledependent as they control traffic congestion depending upon the number of vehicles and their direction of movement across the intersections. The third scheme is environment dependent as theagent senses the environment and controls the sequence of green signal at different routes dynamically. The performances of thethree schemes in ITS are analyzed along with the comparison of storage, communication and computation overhead. The efficacy of the schemes is studied theoretically and quantitatively. The quantitative performance of the three schemes is compared with five existing schemes. On the basis of the result of thecomparison, it can be concluded that the proposed schemes are capable of alleviating congestion more optimally than existing schemes due to the substantial reduction in vehicle waiting time. Index Terms-Traffic signal control, VANET, Congestion con-trol Keywords: The performances of thethree schemes in ITS are analyzed along with the comparison of storage, communication and computation overhead.


## I. INTRODUCTION

$\mathbf{V}$ ehicular transportation is one of the crucial means of transportation around the world. In urban areas, where the number of vehicles continuously escalates faster than the available traffic infrastructure, the traffic management becomes more inefficient and cumbersome [1], [2]. This inefficient and disorganized management has led to severe traffic congestion which has become a troublesome issue of late. Controlling or reducing traffic congestion has become one of the major important tasks around the world [3], [4]. As of late, fog computing with IoT plays an important role in the development of a sustainable traffic flow in ITS to mitigate the ever increasing traffic congestion [5].

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Many works reported so far provide solutions for reducing traffic congestion in ITS. The vehicle flow rate at different lanes across an intersection is considered as fixed in [6]. The duration of green signal in the incoming lanes of anintersection is considered as fixed in [7], [8]. But the flowof traffic varies throughout the day and hence the green signal duration needs to be calculated dynamically. The green signal duration to the incoming lanes is decided dynamically in [9] unlike [7], [8] but the total duration of green signal of all the four incoming lanes is considered as fixed. So the increase in green signal duration of one lane reduces the green signal duration of the other lanes which in turn increases the waiting time of vehicles in the lanes having less green signal duration. A routing algorithm is proposed in [10] to reduce traffic congestion. But the selected route is not verified as a least congested route among all the other routes during simulation. The congestion of such a selected route is measured in [11] depending upon the number of vehicles in that route at aparticular time. In [1] a lane is considered as congested if a vehicle is found in that lane for a prolonged period of time. No other parameters (e.g. waiting time, average speed of vehicles) are considered to measure the congestion in [1], [11]. The duration of green signal is not calculated in [12]. Moreover, in [12] the green signal is set to a lane as soon as the waiting time of vehicles in that lane crosses a predefined threshold. The performance of [13] is tested in a single intersection by varying the number of vehicles from 5-200 only which is not valid in real network.

All the schemes described above do not cope up with real time network. This motivates us to propose three advanced variants (Var 1, Var $\underline{2}$ and Var 3) based on fog computing for controlling traffic congestion of an intersection (Fig. 1) in ITS. The intersection consists of 4 incoming lanes (lane ${ }_{2}$, lane $_{4}$, lane ${ }_{6}$, lane ${ }_{8}$ ) and 4 outgoing lanes (lane ${ }_{1}$, lane $_{3}$, lane $_{5}$, lane $_{7}$ ). The intersection has 4 straight routes $(2->5,4->7,6->1,8->3), 4$ left turn routes ( $2->7,4->1,6->3,8->5$ ) and 4 right turn routes (2->3, 4->5, 6->7, 8->1). The vehicles can take right turn from the intersection without considering the signal, whereas the vehicles should consider the signal while going straight by crossing the intersection distance (d1 in Fig. 1) and taking left turn by crossing the arc distance ( d 2 in Fig. 1). The arc distance d 2 is calculated as $2 * \pi * \mathrm{~d} 1 *$ $(\theta / 360)$, where $\theta$ is 90 . The number of vehicles in each row of a lane isassumed as two for all the three variants. In Var 1 and Var 2 an intersection controller is maintained at the intersection for controlling traffic congestion.


Four Fog devices are present both in Var 1 and Var 2. Fog 12 is associated with lane $_{1}$ and lane ${ }_{2}$, Fog 34 is associated with lane $3_{3}$ and lane $e_{4}$, Fog 56 is associated with lane $_{5}$ and lane ${ }_{6}$, Fog 78 is associated with lane ${ }_{7}$ and lane ${ }_{8}$. In Var 3 an agent at the intersection controls traffic congestion.


Fig. 1. Routes of an intersection
Var_1 is an extension of [14]. In Var 1_the intersection controller and Fogs maintain Table I to determine the fixed sequence of green signal for the routes as ( $2->7,6->3$ ), $(4->7,8->3),(2->5,6->1),(4->1,8->5)$. So the green signal is not on in all the straight and left turn routes corresponding to a particular incoming lane simultaneously. Let, at $t^{\text {th }}$ instantof time, green signal is on in the routes $4->7$ and $8->3$. Thedesired route for the vehicles which are in front of lane $_{8}$ is $8->5$ which is not in the green signal at $t^{\text {th }}$ instant of time. Hence, such vehicles cannot cross the intersection. As a result, all the vehicles which are present behind such vehicles in/ane ${ }_{8}$ have to wait until the green signal is on in the route 8 $>5$, which increases the waiting time of vehicles in lane $8_{8}$.
In Var_2, three scheduling algorithms are proposed to control the congestion of the intersection. In Var 2 at $t^{\text {th }}$ instant of time, green signal is on in straight and left routes of a particular incoming lane. So, green signal is on in both $8->5$ and $8->3$ simultaneously unlike Var_1.
Var 1 and Var 2 are vehicle dependent dynamic approaches where the traffic is controlled depending on the number of vehicles and the direction of movement of the vehicles. Each time the duration of green signal is decided based on these two factors. To cope up with this randomness and fluctuation, environment dependent Q-learning approach is used in Var 3 where the agent senses the traffic environment at the intersec- tion for controlling traffic congestion.

In the present work, the vehicle flow rate and maximum waiting time of vehicles are considered as random unlike [6], [15], [16]. Both Var 2 and Var 3 determine the sequence of green signal dynamically in contrast to the fixed sequence of green signal in Var 1. The duration of green signal to the lanesare computed appropriately for all the three variants unlike [8], [9], [17]-[19]. The effect of such dynamic variation of the green signal duration is studied during simulation by observing the waiting time unlike [10]. The performance of the proposed variants is studied qualitatively, theoretically (using queuing system) and quantitatively. The qualitative performance is
evaluated in terms of communication, storage and computationoverhead. Both the theoretical and quantitative performance are assessed based on the waiting time of vehicles. The sim- ulation experiments are conducted for observing the variation of waiting time of the vehicles in multiple intersections under 5 to 2600 vehicles unlike [13].

## II. EXISTING WORK

Several schemes [7], [15], [16], [18]-[24] for controlling traffic congestion have already been proposed. The schemes [7], [15], [16], [20]-[22], [24] are vehicle dependent whereas the schemes [18], [19], [23] are environment dependent. Traffic Light Controller (TLC) receives all the information from the vehicles through inductive loop detectors [24], cam-eras [7], [21] or radars for controlling the traffic light dynam- ically. But this approach is expensive, has high computational complexity and latency [22]. Moreover, the camera or video recorder installed in the road might not work in bad weather.In [20], road belts are setup at each entrance and each exit of the road to detect the entering vehicles and to inform the Road Side Unit (RSU) about it. RSU counts the number of vehicles and broadcasts message for vehicles. It inserts a record of the data (speed, direction) in the database for each new vehicle.All the RSUs calculate the total load of each road and send this to TLC. TLC determines the maximum load of a roadand compares the load value of other roads with the maximumload value. TLC chooses the road having maximum load value and the road whose load value has the least difference with maximum load value for sharing green signal in the next phase. The vehicles in the road having less load value are not getting a chance to cross the road which increases the waiting time.Moreover the road belt needs to be setup at the entrance and exit of each road which incurs a high cost.

In [15], TLC calculates the waiting time of each vehicle in a road in the current phase and changes the signal to green in case the waiting time of the vehicles crosses a static threshold. Moreover, TLC calculates the traffic flow data of the roads and exchanges this value with its neighbor TLCs to predict the traffic flow at the beginning of the next phase. TLC sets green signal to the pair of roads which have the largest traffic flow and sets a red signal for the other roads. The exchange of information with the neighbor TLCs increases the communication overhead. The static threshold for the maximum waiting time of vehicles might not be appropriate as the traffic flow will not be the same throughout the day.

One vehicle among the vehicles which are reaching the intersection is picked up as the leader vehicle [16]. The driver sends whether to change the traffic light or keep the green light longer to the leader vehicle. The leader vehicle estimates the priority of each route depending upon the traffic flow. If the waiting time of vehicles in a route exceeds the constant threshold value for red light duration, green light is assigned tothat route.


If the time of green light of any route crosses the constant threshold value for the green light duration, traffic light is assigned to that route according to the traffic flow calculated by the leader vehicle. The use of such constant threshold is not suitable for fast changing traffic in urbanareas. If all vehicles on the green light route have passed the intersection, green light will be shifted from the current route to the route with the highest priority. So, the vehicles waiting in the route with less priority are not getting a chance to cross the intersection which increases the waiting time of such vehicle.
In [23], the agent captures the images of the intersection via web camera, determines the edges of the intersection using edge detection method and captures the current objects that are present on the edges to determine the vehicle density. The agent checks the current state, performs an action and receivesreward or penalty. The state is changed if the agent receives reward. But the current state needs to be changed into a new state in case the agent receives a penalty as it helps the agentto know the action which is to be performed in the next state for receiving reward to minimize the penalty.
In [18] the agent identifies the current state in the environment, performs a selected action and updates the Q table after receiving reward or penalty. After performing the action, the agent checks if the queue length in the next state has reduced from the previous state. If it is not reduced the process starts from the beginning. In [18], the states of the Q- learning algorithm are the number of vehicles at each lane of the intersection. The actions are distribution of green signals, with fixed duration to the lanes. Since, the traffic flow is unpredictable and fast changing, the fixed duration of green signal is unable to mitigate the traffic congestion efficiently.
In [19] a lane is segmented in cells. The state is composed of presence of a vehicle or not in the cell, the speed of the vehicle and the current traffic signal phase. The possible actions are the distribution of traffic signal in different lanes. The agent observes the state of the environment chooses an action and receives a reward or penalty after performing the action. But in [19], the duration of the green signal is not considered asa part of the action.

## III. PRESENT WORK

All the three Fog-based variants are elaborated in this section.

Table I Four Different States

| Current state | Green Signal Route (GSR) | Next state <br> State 1 <br> RSR) | Red Signal Route |
| :---: | :---: | :---: | :---: |
| State 2 | $2->7,6->3$ | $(4->7,8->3)$ <br> $(2->5,6->1)$ <br> $(4->1,8->5)$ | State 2 |
| State 3 | $4->7,8->3$ | $(2->5,6->1)$ <br> $(4->1,8->5)$ <br> $(2->7,6->3)$ | State 3 |
| State 4 | $2->5,6->1$ | $(4->1,8->5)$ <br> $(2->7,6->3)$ <br> $(4->7,8->3)$ | State 4 |

A. Var 1

Var_1 considers four states as shown in Table I. The sequential execution of these four states creates a cycle. Each vehicle after entering into an incoming lane sends a message ( M V) to the Fog associated with that lane in the form (type id, route id), where type id and route id are message type identification and route identification
respectively. Fogs keep receiving M Vs from the beginning to the end of aparticular state.

Each Fog searches Table I at the end of the current state to identify the route that enters into green signal (GSR) and red signal (RSR) in the next state. Let Route 1(IL1->OL1) is GSR and Route 2 (IL2->OL2) is RSR. IL1/(IL2) and OL1/(OL2) are the incoming lane and outgoing lane respectively whichare associated with Route $1 /($ Route 2 ).

Fog which is associated with OL1/(OL2) computes the capacity of OL1/ (OL2) as $C V_{1} /\left(C V_{2}\right) . C V_{1} /\left(C V_{2}\right)$ is defined as how many more number of vehicles can enter into OL1/(OL2) and is estimated as the difference of the maximum capacity (MAX CAP) and the number of vehicles present in OL1/(OL2). Fog sends $C V_{1} /\left(C V_{2}\right)$ to the Fog which is associated with IL1/(IL2) in the form of a message ( $\mathrm{M} \mathrm{Fog}_{1}$ ) to prevent the entry of vehicles more than $C V_{1} /\left(C V_{2}\right)$ into OL1/(OL2) for avoiding congestion in Route 1/ (Route 2).

Fog which is associated with IL1/(IL2) determines whether Route 1/ (Route 2) is congested using Algorithm
1 (CONGESTION DETERMINATION). The Fog counts the number of waiting vehicles in IL1/(IL2) as Count ${ }_{\angle L 1} /\left(\right.$ Count $\left._{/ \angle 2}\right)$ that are willing to enter into OL1/(OL2) using the information of the route id field of M V . Route 1/ (Route 2) is congested if Count ${ }_{/ \angle 1} /\left(\right.$ Count $\left._{/ \angle 2}\right)$ is greater than $\mathrm{CV}_{1} /\left(\mathrm{CV}_{2}\right)$.

Fog which is associated with IL1
Allows $C V_{1} /\left(\right.$ Count $\left._{\boldsymbol{I L} 1}\right)$ number of vehicles to enter into OL1 when Route 1 becomes green in the next state if Route 1 is congested/(not congested)

Computes the time which is required for $C V_{1} /\left(\right.$ Count $\left._{\boldsymbol{I L} 1}\right)$ number of vehicles to cross the intersection as normal duration of_ green signal (Normal ${ }_{\text {green }}$ ) in Route 1

Assumes that $N_{I L 1}$ number of vehicles will enter into IL1 when Route 1 becomes green in the next state. $N_{I L 1}$ is considered as same as Count ${ }_{I L 1}$
.Computes the time which is required for (CountIL1 + NIL1) number of vehicles to cross the intersection as maximum duration of green signal (Thresholdgreen) which is also the maximum waiting time of vehicles in red signal in Route_2

Computes Normal $_{\text {green }}$ and Threshold $_{\text {green }}$ using Algo- rithm 2 (Computation Normal green Thresholdgreen)

Sends (Normal green Threshold $_{\text {green }}$ ) to the intersection controller in the form of a message ( M Fog2) for determining the actual duration of green signal in Route 1

Fog which is associated with IL2 sends a message (M Fog3) to the intersection controller to inform whether congestion occurs (Occurrence of congestion) in Route 2.

The intersection controller reads the green signal routes in the current state (current GSRs) and in the next state (next GSRs) from Table I. current GSRs enter into red signal in the next state.


The intersection controller computes the actual duration of green signal for next GSRs and the maxi- mum waiting time of vehicles in current GSRs after receiving M Fog2 and M Fog3 from the Fogs using Algorithm 3.

Var 1 uses the parameters as shown in Table II.
Table II Parameters Used In Var 1

| Parameter | Definition |
| :---: | :---: |
| Count2, Count4, Count $_{6}$, Count ${ }_{8}$ | Number of waiting vehicles in incoming lane lane ${ }_{2}{\text {, } \text { lane }_{4}, \text { lane }_{6} \text {, } \text { lane }_{8} \text { respectively }}^{\text {a }}$ |
| $\begin{array}{ll} C V_{1}, & C V_{3}, \\ C V_{5}, & C V_{7} \end{array}$ | Capacity of vehicles in outgoing lane lane $_{1}$, lane ${ }_{3}$, lane 5 , lane $_{7}$ respectively |
| $\begin{array}{lll} \hline \text { Normal green } & 47, \text { Normal green } & 83 \\ \text { Normal green }^{25} & \text { Normal green } & 61, \\ \text { Normal green }^{41} \text {, Normal green } 85, \\ \text { Normal green } & 27, & \text { Normal green } \\ \hline \end{array}$ | $\begin{gathered} \text { Normal duration of green signal in the route } \\ 4->7,8->3,2->5,6->1,4->1,8->5,2->7,6- \\ >3 \\ \text { respectively } \\ \hline \end{gathered}$ |
| Threshold $_{\text {green } 47}$, Threshold green $_{\text {83 }}$, Threshold $_{\text {green } 25}$, Threshold $_{\text {green }}^{61}$, Threshold ${ }_{\text {green } 41}$, Threshold green ${ }^{55}$, Threshold ${ }_{\text {green } 27}$, Threshold ${ }_{\text {green }} 63$ | Maximum duration of green signal in the route $4->7,8->3,2->5$, respectively |

State_1: It can be observed from Table I that the routes $4->7$ and $8->3$ enter into green signal (GSR) whereas theroute $2->7$ and $6->3$ enter into red signal (RSR) when the state changes from State 1 to State 2. lane $_{4} /\left(\right.$ lane $\left._{8}\right)$ isIL1 and lane $_{7} /\left(\bar{l}_{\text {ane }}^{3} 3\right)$ is OL 1 for the route 4$>7 /(8->3)$. lane $_{2} /\left(\right.$ lane $\left._{6}\right)$ is IL2 and lane $7 /\left(\right.$ lane $\left._{3}\right)$ is OL2 for the route $2->7 /(6->3)$.

Count $_{4} /\left(\right.$ Count $\left._{8}\right)$ is Count $_{\boldsymbol{I L} 1}$ for the route $4->7 /(8-$ $>3)$. Fog $34 /(\operatorname{Fog} 78)$ is associated with the route $4->7 /(8-$ >3) whereas $\overline{\text { Fog }}$ 12/(Fog 56) is associated with the route 2-
$>7 /(6->3)$. The functions of all these Fogs are elaborated below.

## Functions of Fog 34/ (Fog 78):

Calls Algorithm 1 (CONGESTION DETERMINATION (State 1, lane $3_{3}$ 4->7))/ ( CONGESTION DETERMINATION
(State 1, lane $\left._{7}, 8->3\right)$ ) to determine whether the route $4->7 /(8->3)$ is congested -State 1 is the current state, lane $3_{3}$ is the outgoing lane which is associated with Fog 34 and lane $_{7}$ is the outgoing lane which is associated with Fog 78

Sets the returned value as Count $_{4}=$ Count $_{a}$, $C V_{3}=C V_{a}{ }^{\prime}, C V_{7}=C V_{b}$, occ cong $=$ Occurrence of congestion/ $\left(\right.$ Count $_{8}=$ Count $_{a}, C V_{7}=C V_{a}{ }^{\overline{ }}, \overline{C V}_{3}=C V_{b}$, occ cong $=$ Oc- currence of congestion)

Sends M Fog1 in the form (Fog 34, $\mathrm{CV}_{3}$ )/(Fog 78, $C V_{7}$ ) to (Fog 56 associated with $6->3$, Fog 78 associated with $8->3) /($ Fog 12 associated with 2->7, Fog 34 associated with 4->7) Calls

Algorithm
$\begin{array}{cl}2 & \\ \text { Threshold }_{\text {green }} & \text { (Computation } \\ \left(4->7, \quad \text { d1,Count } H_{4},\right. & \text { Normal }_{\text {green }} \\ \mathrm{CV}_{7},\end{array}$ $\begin{array}{ccc}\text { Threshold }_{\text {green }} & (4->7, & \mathrm{d} 1, \text { Count }_{4}, \\ & \text { occ cong))/ } & \mathrm{CV}_{7}, \\ \text { (Computation }\end{array}$ Normal $_{\text {green }} \quad$ Threshold $_{\text {green }}\left(8->3\right.$, d1, Count $_{8}$, $C V_{3}$, occ cong)) to compute Normal ${ }_{\text {green }} 47$, Threshold $_{\text {green } 47} /\left(\right.$ Normal $_{\text {green } 83}$, Threshold green 83 $)$ for the route $4->7 /(8->3)$

- Here d1 is used as both $4->7$ and $8->3$ are straight routesSets the returned value as Normal $_{\text {green }}{ }^{47}=$ Normal ${ }_{\text {green ab }}$
/ $\left(\right.$ Normal green $_{83}=$ Normal $\left._{\text {green ab }}\right)$, Threshold ${ }_{\text {green }}$ ${ }_{47}=$ Threshold $_{\text {green ab }} /\left(\text { Threshold }_{\text {green }}^{83} \text { }=\text { Threshold }_{\text {green ab }}\right)^{-}$

Sends M Fog2 in the form (Fog 34, Normal ${ }_{\text {green }} 47$, Threshold green $^{47}$ )/ (Fog 78, Normal green 83 , Threshold green ${ }_{83}$ ) to the intersection controller

## Function of Fog 12/ (Fog 56):

Calls Algorithm 1 (CONGESTION DETERMINATION (State 1, lane $_{1}$, 2->7))/ (CONGESTION DETERMINA-

TION (State 1, lane $_{5}, 6->3$ )) to determine whether the route $2->7 /(\overline{6}->3)$ is congested

- lane ${ }_{1}$ is the outgoing lane which is associated with Fog 12 and lane $_{5}$ is the outgoing lane which is associated with Fog 56

Seets occ cong= Occurrence of congestion
Sends M Fog3 in the form (Fog 12, occ cong) $/(($ Fog 56, occ cong)) to the intersection controller

```
Algorithm 1 the Congestion Determination Algorithm
1: procedure CONGESTION DETERMINATION (State, lanea',
a->b)
2: if State \(=\) State 1 then
                            Out \(\mathrm{Ln}=\) lane \(_{3}{\text {, } \text { lane }_{7} / * \text { Out }^{2} \mathrm{Ln} \text { is the }}^{2}\)
outgoinglanes of GSR and RSR in the current state */
        end if
        if \((\) State \(==\) State 2\()\) or \((\) State \(=\) State 4\()\) then
```



```
        end if
        if State==State 3 then
                            Out \(\mathrm{Ln}=\) lane \(_{1}{\text {, } \text { lane }_{5}}\)
        end if
        Estimates the number of waiting vehicles in lane \({ }_{a}\) as
Count \(_{a}\) that are willing to enter into lane \(_{b}\)
12: \(\quad\) if lane \(_{a}{ }^{\prime} \in\) Out Ln then
            Estimates the capacity of lane \({ }_{a}{ }^{\prime}\) as \(C V_{a}{ }^{\prime}\)
        end if
                            Reads \(C V_{b}\) from M Fog1 after receiving it
from theFog associated with \(\operatorname{lan} \bar{e}_{b}\)
16: \(\quad\) if Count \(_{a}>C V_{b}\) then
17: Occurrence of congestion=1/*Route a->b is
con-gested */
18: else
19: Occurrence of congestion \(=0 / *\) Route \(a->b\) is
notcongested */
20: end if
21: return \(\left(\right.\) Count \(_{a}, C V_{a}{ }^{\prime}, C V_{b}\), Occurrence of
conges-tion)
    : end procedure
```

All the Fogs maintain a static database (Table III) to store Range of number of vehicles and Range of speed $(\mathrm{Km} / \mathrm{hr})$. Each Range of number of vehicles is in the form (veh min- veh max), where veh min is the lowest number of vehicles and veh max is the highest number of vehicles in that range. Similarly, each Range of speed corresponding to a particular range of number of vehicles is in the form (speed min- speed max), where speed min is the lowest speed of vehicles and speed max is the highest speed of vehicles in that range.

For example, (41-60)\% is a range of the number of vehicles and ( $37-42$ ) $\mathrm{Km} / \mathrm{hr}$ is the corresponding range of speed. So, veh min, veh max, speed min, speed max are $41 \%, 60 \%, 37 \mathrm{Km} / \mathrm{hr}, 42 \mathrm{Km} / \mathrm{hr}$ respectively.


So, $37 \mathrm{Km} / \mathrm{hr}$ is the speed when the number of vehicles in the lane is $60 \%$ of MAX CAP and $42 \mathrm{Km} / \mathrm{hr}$ is the speed when the number of vehicles in the lane is $41 \%$ of MAX CAP.

Table III Relation Between Number of Vehicles And Range of Speed

| Range of number of vehicles | Range of speed (Km/hr) |
| :---: | :---: |
| $(0-20) \%$ of MAX CAP | $65-70$ |
| $(21-40) \%$ of MAX CAP | $51-56$ |
| $(41-60) \%$ of MAX CAP | $37-42$ |
| $(61-80) \%$ of MAX CAP | $23-28$ |
| $(81-100) \%$ of MAX CAP | $9-14$ |

Let the route IL1-> OL1 is green and $N_{I L 1}$ number of vehicles enter into IL1. Fog which is associated with IL1 searches Table III to
Find the range of vehicles corresponding to $N_{I L 1}$
Read the value of veh min, veh max, speed min, speed $\max$ to calculate the average speed $\left(\right.$ speed $\left._{I L 1}\right)$ for $N_{I L 1}$ number of vehicles in IL1
For example, let $N_{I L 1}=70$. So $61-80 \%$ is the range of number of vehicles for $N_{I L 1}$ and $23-28 \mathrm{Km} / \mathrm{hr}$ is the range of speed corresponding to the range of number of vehicles $61-80 \%$. Hence, for $N_{\boldsymbol{I L 1}}$, veh $\min =61 \%$, veh $\max =80 \%$, speed $\min =23 \mathrm{Km} / \mathrm{hr}$, speed_ $\max =2 \overline{8} \mathrm{Km} / \mathrm{hr}$. So,

$$
\text { speed }_{I L 1}=23+\frac{(80-70)}{(80-61)}(28-23)
$$

Algorithm 2 uses the following parameters. The definition of these parameters is elaborated for IL1.
start_speed $\rightarrow$ The starting speed of the waiting vehicles in IL1 when the signal of IL1 changes from red to green

T1/(T2) $\rightarrow$
Time which is required for all Count $\boldsymbol{I L}_{1} /\left(N_{\boldsymbol{I L} 1}\right)$ number of waiting vehicles in IL1 to go straight from the intersection for the straight routes after crossing distance d 1 ( $\mathrm{d}^{\prime}=\mathrm{d} 1$ in Fig. 1) or to take left turn from the intersection for the left turn routes after crossing distance d2 (d'=d2 in Fig.1)

T3/(T5) Time which is required for the first row of Count $_{\boldsymbol{I L} 1} /\left(N_{I L 1}\right)$ number of vehicles in IL1 to cross the distance d 1 (for going straight from the intersection) or d2 (for taking left turn from the intersection) with start speed/ $\left(\right.$ speed $\left._{\text {IL } 1}\right)$

T4/(T6) Time which is required for the rest of the rows (except the first row) of $\operatorname{Count}_{\boldsymbol{I L} 1} /\left(N_{\boldsymbol{I L 1}}\right)$ number of vehicles in IL1 to cross the inter vehicle distance and the length of the vehicle in its front row with start speed/(speed ${ }_{\text {IL } 1}$ )
Algorithm 2: T 3 is computed for the vehicles in the front row of lane ${ }_{a}$ to cross distance d' from the intersection (Line 2). T1 is computed for Count $_{a}$ number of waiting vehicles
i.e $\left\lceil\frac{\text { Count }_{a}}{2}\right\rceil^{\text {th }}$ row of vehicles for entering into lane $_{b}$

Line 4). The value of $N_{a}$ is assumed as same as Count ${ }_{a}$
(Line 8). T2 is computed for $N_{a}$ vehicles i.e. $\left\lceil\left.\frac{N_{a}}{2}\right|^{\text {th }}\right.$

```
Algorithm 2 Computation of Normal green and Threshold \({ }_{\text {green }}\)
    procedure COMPUTATION _ NORMAL \(_{\text {GREPN }}\)
    THRESHOLD Gremv \(\left(\mathrm{a}->\mathrm{b}, \mathrm{d}\right.\) ', Count \({ }_{a}, C V_{b}\), occ _cong)
        T3 = (d'/start_speed)
    \(T 4=(\) vehicle length + inter vehicle distance)/(start_speed)
                \(T 1=T 3+T 4 *\left(\left\lceil\frac{\text { Count }_{a}}{2}\right\rceil-1\right)\)
    : Calculate average speed of lane \({ }_{a}\) (speed \(d_{a}\) ) using TableIII and Equ. 1
        \(\mathrm{T} 5=\left(\right.\) total lane \(_{a}\) distance \(\left.^{+} \mathrm{d}^{\prime}\right) /\) speed \(_{a}\)
        T6 \(=\) vehicle lenath+inter vehicle distance
    8: \(N_{o}=\) Count \(_{a}\) speed \(_{a}\)
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```
\(T 2=T 5+T 6 *\left(\left\lceil\frac{N_{a}}{2}\right\rceil-1\right)\)
        if (occ cong \(==1\) ) then
            Normal green_ab \(=\mathrm{T} 3+\mathrm{T} 4^{*}\left(\begin{array}{ll}\frac{C V_{b}}{2} & -1\end{array}\right)\)
        else
            Normal \(_{\text {green_ab }}=\mathrm{T} 1\)
        end if
        Threshold \({ }_{\text {green } \_ \text {ab }}=\mathrm{T} 1+\mathrm{T} 2\)
        return (Normal green_ab, Threshold \({ }_{\text {green_ab }}\) )
    end procedure
```

row of vehicles for crossing lanea and entering into laneb (Line 9). If the value of occ cong is 1 then the route $a->b$ is congested. Hence, only CVb number of vehicles are allowed to enter into laneb and Normalgreen_ab is calculated for $\frac{\mathrm{CV}_{b}}{2}$ row of vehicles (Line 10, 11). Otherwise, Count
number of vehicles are allowed to enter into lane $_{b}$ and

Normal ${ }_{\text {green_ab }}$ is calculated for $\left\lceil\frac{\text { Count }_{a}}{2}\right\rceil^{\text {th }}$ row of vehicles which is equivalent to T 1 (Line 12, 13). Threshold ${ }_{\text {green }}$ ab
depends on the time which is required for Count $_{a}+$ $N_{a}$ ) number of waiting vehicles in lane ${ }_{a}$ to enter into lane ${ }_{b}$ when the route $\mathrm{a}->\mathrm{b}$ is in green signal. Hence,
Threshold $_{\text {green }}$ ab is the summation of T 1 and T 2 (Line 15).
State 2: It can be observed from Table I that the routes 2 - $>5$ and $6->1$ enter into green signal (GSR) whereas the routes $4->7$ and $8->3$ enter into red signal (RSR) when the state _ changes from State 2 to State 3. lane $_{2} /\left(\right.$ lane $\left._{6}\right)$ isIL1 and lane $_{5} /\left(\right.$ lane $\left._{1}\right)$ is OL1 for the route $2->5 /(6->1)$. lane $4_{4} /\left(\right.$ lane $\left._{8}\right)$ is IL2 and lane $_{7} /\left(\right.$ lane $\left._{3}\right)$ is OL2 for the route $4->7 /(8->3)$. Count $_{2} /\left(\right.$ Count $\left._{6}\right)$ is Count $_{\boldsymbol{I L} 1}$ for the route $2->5 /(6-$ $>1)$. Fog $12 /(\operatorname{Fog} 56)$ is associated with the route $2->5 /(6-$ $>1)$ whereas $\operatorname{Fog} 34 /\left(\mathrm{Fog}^{-78)}\right.$ is associated with the route $4->7 /(8->3)$. The functions of all these Fogs are elaborated below.


Function of Fog 12/(Fog 56):

| Calls | Algorithm | 1 | (CONGESTION |
| :--- | :---: | :---: | ---: |
| DETERMINATION(State | 2, | lane $_{1}$, | $2-$ | $>5)$ )/(CONGESTION DETERMINATION(State 2,

lane $_{5}, 6->1$ ) to determine whether the route $2->5 /(6-$ $>1$ ) is congested
-State 2 is the current state, lane $_{1}$ is the outgoing lane which is associated with Fog 12 and lane is the outgoing lane which is associated with Fōg_56.

- Sets Count ${ }_{2}=$ Count $_{a}, C V_{1}=C V_{a^{\prime}}, C V_{5}=$
$C V_{b}$, occ cong=Occurrence of congestion/ ( Count $_{6}=$ Count $_{a},{ }^{-} C V_{5}=C V_{a}{ }^{\prime},{ }^{-} C V_{1}=C V_{b}$, occ cong $=$ Occurrence of congestion)
. Sends $\mathrm{V}^{2} \mathrm{Fog} 1$ in the form (Fog 12, $C V_{1}$ ) / (Fog 56, $C V_{5}$ ) to Fog $5 \overline{6}$ associated with 6->1/ (Fog 12 associated with 2->5)
. Calls Algorithm 2 (Computation_Normal ${ }_{\text {green }}$ Threshold green $\left(2->5\right.$, d1, Count ${ }_{2}, C V_{5}$, occ cong)) / (Computation Normal green Threshold $_{\text {green }}(6->1$,
d 1, Count $_{6}, C V_{1}, \quad \overline{\text { occ }}$ cong)) to compute Normal $_{\text {green }-25}$, Threshold ${ }_{\text {green }} 25 /$ Normal $_{\text {green }}{ }_{61}$, Threshold $_{\text {green 61 }}$ ) for the
route 2->5 / (6->1)
- Here d1 is used as $2->5$ and $6->1$ are straight routes. Sets Normal $_{\text {green } 25}=$ Normal $_{\text {green ab }} /\left(\right.$ Normal $_{\text {green } 61}=$ Normal $\left._{\text {green ab }}\right)$, $\quad$ Threshold green $25={ }^{-}$Threshold green ab $^{-}$ $/\left(\right.$ Threshold $_{\text {green } 61}=$ Threshold $_{\text {green ab. }}$.)
. Sends M Fog2 in the form (Fog 12, Normal ${ }_{\text {green }} 25$,
Threshold green 25 ) / (Fog_56, Normal green_ $_{\text {61 }}$, Threshold green $^{-}$ ${ }_{61}$ ) to the intersection controller
Function of Fog 34/(Fog 78):
. Calls Algorithm 1 _ (CONGESTION DETERMINATION (State - - 2,lane $3,4->7$ ))


## /(CONGESTION_DETERMINATI

ON (State 2, lane $_{7}, 8->3$ )) to determine whether the route $4->7 /(8->3)$ is congested
. Sets $C V_{3}=C V_{a}{ }^{\prime}$, _ occ cong= Occurrence of congestion /
( $C V_{7}=C V_{a}{ }^{\prime}$, occ cong =Occurrence_of_congestion)
. Sends M Fog1 in the form (Fog 34, $C V_{3}$ ) / (Fog 7ㅛ, $C V_{7}$ ) to Fog $7 \underline{8}$ associated with $8->3 /$ (Fog $3 \underline{4}$ associated with 4->7)
. Sends M Fog3 in the form (Fog 34, occ cong) / (Fog 78, occ cong) to the intersection controller.

State_3: It can be observed from Table I that the routes $4->1$ and $8->5$ enter into green signal (GSR) whereas the routes $2->5$ and $6->1$ enter into red signal (RSR) when the state changes from State 3 to State 4. lane $_{4} /\left(\right.$ lane $\left._{8}\right)$ isIL1 and lane $1 /\left(\right.$ lane $\left._{5}\right)$ is OL 1 for the route 4$>1 /(8->5)$. lane $_{2} /\left(\right.$ lane $\left._{6}\right)$ is IL2 and lane $_{5} /\left(\right.$ lane $\left._{1}\right)$ is OL2 for the route $2->5 /(6->1)$. Count $_{4} /\left(\right.$ Count $\left._{8}\right)$ is Count $_{\text {IL1 }}$ for the route $4->1 /(8->5)$. Fog $34 /($ Fog 78$)$ is associated with the route $4->1 /(8->5)$ whereas Fog $12 /($ Fog 56) is associated $\bar{w}$ ith the route $2->5 /(6->1)$. The functions of all these Fogs areelaborated below.

## Function of Fog 12/(Fog 56):

. Calls Algorithm 1 (CONGESTION DETERMINATION (State 3, lane $\left.{ }_{\underline{1},}^{-} \quad 2->5\right)$ ) / (CONḠESTION DETERMINATION
(State _3, lane ${ }_{5}, 6->1$ )) to determine whether the route 2 -

## $>5$

/ (6->1) is congested
-State 3 is the current state, lane $_{1}$ is the outgoing lane which is associated with Fog 12 and lane $_{5}$ is the outgoing lane which is associated with Fog 56
Sets $\mathrm{CV}_{1}=\mathrm{CV}_{\mathrm{a}}{ }^{\prime}$, occ cong $=$ Occurrence of congestion / $\left(\mathrm{CV}_{5}=\mathrm{CV}_{\mathrm{a}}{ }^{\prime}\right.$, occ cong=Occurrence of congestion)
Sends M Fog1 in the form (Fog 12, $\mathrm{CV}_{1}$ ) / (Fog 56,
$\mathrm{CV}_{5}$ ) to (Fog 34 associated with 4->1, Fog 56 associated
with 6->1) / (Fog 12 associated with 2->5, Fog 78 associated
with 8->5)
Sends M Fog3 in the form (Fog_12, occ_cong) / (Fog 56 ,occ cong) to the intersection controller

## Function of Fog 34/(Fog 78):

. Calls Algorithm 1 (CONGESTION DETERMINATION (State 3, lane $3,4->1$ )) / (congestion determination(State 3 , lane ${ }_{7}, 8->5$ )) to determine whether the route $4->1 /(8->5)$ is congested

- lane ${ }_{3}$ is the outgoing lane which is associated with Fog 34 and lane $_{7}$ is the outgoing lane which is associated with Fog 78
Sets. Count ${ }_{4}=$ Count $_{\mathrm{a}}, \quad \mathrm{CV}_{3}=\mathrm{CV}_{\mathrm{a}}{ }^{\prime}, \quad \mathrm{CV}_{1}=\mathrm{CV}_{\mathrm{b}}$, occ cong= Occurrence _of congestion / (Count ${ }_{8}=$ Count $_{\mathrm{a}}, \mathrm{CV}_{7}=\mathrm{CV}_{\mathrm{a}}{ }^{\prime}, \mathrm{CV}_{5}=\mathrm{CV}_{\mathrm{b}}$, occ cong $=$ Occurrence of congestion)
. Calls Ālgorithm 2 (Computation Normal green Threshold $_{\text {green }}\left(4->1\right.$, d2, Count $_{4}, \mathrm{CV}_{1}$, occ cong $)$ ) / (Computation Normal $_{\text {green }} \quad$ Threshold $_{\text {green }}(8->5$,
d 2 , Count $\overline{8}_{8}, \quad \mathrm{CV}_{5}, \quad$ occ cong)) to compute Normal $_{\text {green }} 41$, Threshold green $^{41} /$ Normal $_{\text {green }}{ }_{85}{ }^{-}$ Threshold ${ }_{\text {green }} 85$ ) for the route $4->1 /(8->5)$
-Here d2 is used as $4->1$ and $8->5$ are left turn routes.
.Sets Normal ${ }_{\text {green } 41}=$ Normal $_{\text {green ab }} /\left(\right.$ Normal $_{\text {green }} 85=$ Normal $\left._{\text {green }} \quad \mathrm{ab}\right)$, Threshold green $^{41}=$ Threshold green $_{\text {ab }} \overline{/}$ (Threshold green $_{85}=$ Threshold $_{\text {green }}{ }^{-}$ab $)$
.Sends M Fog2 in the form (Fog 34, Normal ${ }_{\text {green }}{ }^{41}$, Threshold $_{\text {green 41 }}$ ) / (Fog 78, Normal green _ $^{25}$, Threshold green_ ${ }_{85}$ ) to the intersection controller

State 4: It can be observed from Table I that the routes $2->7$ and $6->3$ enter into green signal (GSR) whereas the routes $4->1$ and $8->5$ enter into red signal (RSR) when the state changes from State 4 to State 1 . lane $_{2} /\left(\right.$ lane $\left._{6}\right)$ isIL1 and lane $_{7} /\left(\right.$ lane $\left._{3}\right)$ is $\mathrm{OL}_{1}$ for the route 2$>7 /(6->3)$. lane $_{4} /\left(\right.$ lane $\left._{8}\right)$ is IL2 and lane $1 /\left(\right.$ lane $\left._{5}\right)$ is OL2 for the route $4->1 /(8->5)$. Count $_{2} /\left(\right.$ Count $\left._{6}\right)$ is Count $_{\text {IL1 }}$ for the route $2->7 /(6->3)$. Fog $12 /($ Fog 56$)$ is associated with the route ${ }^{-} 2->7 /(6->3)$ whereas Fog $34 /(\operatorname{Fog} 78)$ is associated with the route $4->1 /(8->5)$. The functions of all these Fogs areelaborated below.

## Function of Fog 12/(Fog 56): <br> Calls Algorithm (CONGESTION

DETERMINATION(State 4,lane ${ }_{1}$, 2->7))/ (CONGESTION_DETERMINATION(State 4, lane $_{5}$,6>3))

to determine whether the route $2->7 /(6->3)$ is congested
-State 4 is the current state, lane ${ }_{1}$ is the outgoing lane which is associated with Fog 12 and lane $_{5}$ is the outgoing lane which is associated with Fog 56

Sets Count $_{2}=$ Count $_{a}, \quad C V_{1}=\quad C V_{a}{ }^{\prime}, \quad C V_{7}=$ $C V_{b}$, occ cong= Occurrence of $\overline{\text { congestion / }}$ $\left(\right.$ Count $_{6}=$ Count $_{a}, C V_{5}=C V_{a}{ }^{\prime}, C V_{3}=C V_{b}$, occ cong $=$ Occurrence of congestion)

Sends M Fog1 in the form_(Fog 12, CV $V_{1}$ ) / (Fog 56, $C V_{5}$ ) to Fog 34 associated with 4->1 / (Fog 78 associated with 8->5)

Calls Algorithm 2 (Computation Normal green Threshold $_{\text {green }}\left(2->7, \quad \mathrm{~d} 2, \quad\right.$ Count $_{2}, \quad C V_{7}^{-}, \quad$ occ cong))/(Computation Normal green Threshold $_{\text {green }}(6$ $>3$, $\quad \mathbb{d} 2$, Count $_{6}, C V_{3}$, occ cong)) to compute Normal $_{\text {green } 27}$, Thres old $_{\text {green } 27} /\left(\right.$ Normal $_{\text {green } 63}$, Threshold $_{\text {green 63 }}$ ) for the
route $2->7 /(6->3)$

- Here d2 is used as $2->7$ and $6->3$ are straight routes.
. Sets Normal ${ }_{\text {green }}^{27} 7^{2}=$ Normal $_{\text {green }} \underline{\underline{a b}} /\left(\right.$ Normal $_{\text {green }}^{63}=$ Normal $_{\text {green_ab }}$ ), Threshold green $_{-27}=$ Threshold green $^{\text {ab }}{ }^{-/}$ (Threshold green_ $_{-}^{-}=$Threshold $_{\text {green_ab }}$ a
. Sends M Fog2 in the form (Fog 12, Normal green 27, Threshold green 27 $^{27}$ ) / (Fog_56, Normal green_ $_{\text {63 }}$, Threshold green $^{2}$ ${ }_{63}$ ) to the intersection controller


## Function of Fog 34/(Fog 78):

. Calls Algorithm 1 (CONGESTION DETERMINATION ( State 4, lane $\left._{3}, 4->1\right)$ ) / (CONGESTION DETERMINATION(
State 4, lane $_{7}, 8->5$ )) to determine whether the route $4->1 /$ (8->5) is congested
-lane $3_{3}$ is the outgoing lane which is associated with Fog 34 and lane $_{7}$ is the outgoing lane which is associated with Fog 78
. $\overline{\text { Sets }} C V_{3}=C V_{a}{ }^{\prime}$, occ cong $=$ Occurrence of congestion $/\left(C V_{7}=C V_{a}{ }^{\prime}\right.$, occ_cong=Occurrence_ of congestion)
. Sends M Fog 1 in the form ( $\operatorname{Fog} 34, C V_{3}$ )/ (Fog 78, $C V_{7}$ )to Fog $5 \overline{6}$ associated with 6->3/(Fog 12 associated with 2-
>7)
. Sends M Fog3 in the form (Fog 34, occ cong) / (Fog 78, occ cong) to the intersection controller

Function of intersection controller: It is elaborated in Algorithm 3.

```
Algorithm 3 Function of intersection controller
    Input Two M_ Fog2 and two M Fog3
    Output Actual duration of green signal in next
GSRs,maximum waiting time of the vehicles in çurrent
GSRs
    procedure
        Reads Threshold green and Normalgreen from the two
    received M Fog2
        Reads occ cong from the two received M Fog3
        if value of the two received occ cong == 0 then
    /*current GSRs are not congested*/
            Sets the maximum waiting time of the
    vehicles as the maximum of the two Threshold}\mp@subsup{|}{\mathrm{ green }}{
    values_in current GSRs for the next state
        else
            Sets the maximum waiting time of the
```

vehicles as the minimum of the two Threshold ${ }_{\text {green }}$ values in current GSRs for the next state end if

Sets the actual duration of green signal as the average of the two Normal green ${ }^{\text {values in next GSRs }}$ end procedure

Size of messages: The type id field in M V indicates that vehicle is the sender of this message and its value is 1 . The size of the route id field is 4 bits as intersection has 12 routes. The maximum vehicle speed is assumed as 120 $\mathrm{Km} / \mathrm{hr}$ and hence the size of the veh speed is 7 bits. So, the size of the message M V (Size M V) is 12 bits.
The size of the Fog identification field in M_Fog1 is 2 bits as the intersection has 4 Fogs. The size of CV value in M Fog 1 depends on the MAX CAP. During simulation MAX CAP is assumed as 200 . Hence, the size of CV value is 8 bits and the size of M Fog1 (Size M Fog1) is 10 bits.

The size of both the Normal green and Threshold ${ }_{\text {green }}$ fields in M Fog2 is assumed as 2 bytes. Hence, the size of M Fog2 (Size M Fog2) is 34 bits.

The occ_cong field in_M Fog3 indicates whether congestion occurs in the route or not. The value of this field is 1 ifcongestion occurs, otherwise it is 0 . Hence, the size of M Fog3(Size M Fog3) is 3 bits.

## B. Var-2:

Three scheduling algorithms are illustrated in Var 2. These three approaches are priority scheduling ( $\mathrm{Pr} \overline{\mathrm{S} c h}$ ), shortest job first scheduling (SJ Sch) and round robin scheduling (RR Sch). Each approach has four phases corresponding to the green signal in the four incoming lanes. The sequence of execution of these four phases is determined dynamically in all the three scheduling approaches and the execution of the four phases creates a cycle. The vehicles in a lane can go straight (d1 in Fig. 1) or left (d2 in Fig. 1) when the lane gets green signal.

## Function of a vehicle:

The function of $v^{\text {th }}$ vehicle $\left(V_{v}\right)$ after entering into an incoming lane in $k^{\text {th }}$ cycle is elaborated in this section. The On Board Unit (OBU) of $V_{v}$ determines its position usingGPS, executes Algorithm 4 to generate a message M V.

```
Algorithm 4 Function of }\mp@subsup{V}{V}{
    Input Position of }\mp@subsup{V}{v}{
    Output M_V
    procedure
        Computes its distance (d) from the intersection
        Adds d1 or d2 with d to compute the distance Dist
        Compute the time (Time v) required to cross Dist as
        Dist
        Generates M_V in the form (Time v
        Sends M_V to Fog associated with its current lane
    end procedure
```

Function of Fogs in $k^{\text {th }}$ cycle: Fog 12, Fog 34, Fog 56, Fog 78

- Receive M Vs from the vehicles in lane $_{2}$, lane $_{4}$, lane $_{6}$, lane $_{8}$
- Store the received M Vs in Queue 2 , Queue ${ }_{4}$, Queue $_{6}$, Queue $_{8}$
- Execute Algorithm 5 to determine the sequence and duration of green signal for the lanes for $(k+1)^{\text {th }}$ cycle.

```
Algorithm 5 Function of Fog_12, Fog_34, Fog_56, Fog_78
in \(k^{\text {th }}\) cycle
    Input M_Vs
    Output Sequence and duration of green signal
    procedure
        Count the number of M Vs in Queue \(_{2}\), Queue \(_{4}\),
    Queue \(_{6}\), Queue \(_{8}\) as \(V_{2}, V_{4}, V_{6}, V_{8}\) respectively
        Read time from \(V_{2}, V_{4}, V_{6}, V_{8}\) M_Vs respectively
    . Compute the maximum time \(G_{2}\) by comparing \(V_{2}\)
    number of time values, \(G_{4}\) by comparing \(V_{4}\) number of
    time values, \(G_{6}\) by comparing \(V_{6}\) number of time values,
    \(G_{8}\) by comparing \(V_{8}\) number of time values respectively
        Send a message (M Fog4) in the form [Fog_12, \(V_{2}\),
    \(\left.G_{2}\right]\), \(\left[F_{0} g_{-} 34, V_{4}, G_{4}\right]\), [Fog_56, \(\left.V_{6}, G_{6}\right]\), [Fog_78, \(V_{8}\),
    \(G_{8}\) ] to the other three fogs
        Call procedure \(\operatorname{PR}\) for \(P R\) Sch, procedure \(\operatorname{SJ}\) for
    SJ_Sch, procedure_RR for RR_Sch
    end procedure
```

```
Algorithm 6 procedure PR
    1: procedure
        Calculate the priority of lane \({ }_{2}\) (Pric lane \({ }_{2}\) ), lane \(_{4}\)
        (Prio_lane \({ }_{4}\) ), lane \({ }_{6}\) (Prio_lane \({ }_{6}\) ) and lane \({ }_{8}\) (Prio_lane \({ }_{8}\) )
        as \(\frac{V_{2}}{V_{2}+V_{4}+V_{6}+V_{8}}, \frac{V_{4}}{V_{2+}+V_{4}+V_{6}+V_{2}}, \frac{V_{6}}{V_{2}+V_{4} \pm V_{6}+V_{8}}, \frac{V_{8}}{V_{2}+V_{4}+V_{6}+V_{8}}\).
    Arrange the lanes in the descending order of their
        priority in a list to determine the sequence of green signal
        of the four lanes for \((k+1)^{\text {th }}\) cycle
            Compute cycle duration as \(G_{2}+G_{4}+G_{6}+G_{8}\)
    end procedure
```

For example, let the list in Procedure $\underline{P R}$ is (Prio lane ${ }_{2}$, Prio lane ${ }_{8}$, Prio $\underline{\text { lane }}_{4}$, Prio lane ${ }_{6}$ ). So first Fog $1 \underline{2}$ schedules green signal for the routes $2->5$ and $2->7$ for the duration $G_{2}$, then Fog 78 schedules green signal for the routes $8->3$ and $8->5$ for the duration $G_{8}$, then Fog 34 schedules green signal for the routes $4->7$ and $4->1$ for the duration $G_{4}$, then Fog 56 schedules green signal for the routes $6->1$ and $6->3$ for the duration $G_{6}$.

```
Algorithm 7 procedure_SJ
    1: procedure
        Arrange the lanes in the ascending order of green
        signal duration \(G_{2}, G_{4}, G_{6}, G_{8}\) in a list to determine the
        sequence of green signal of the four lanes for \((k+1)^{\text {th }}\)
        cycle
            Compute cycle duration as \(G_{2}+G_{4}+G_{6}+G_{8}\)
    end procedure
```

For example, let the list in Procedure SJ is $\left(G_{2}, G_{8}\right.$, $G_{4}, G_{6}$ ). So first Fog 12 schedules green signal for the routes $2->5$ and $2->7$ for the duration $G_{2}$, then Fog 78 schedules green signal for the routes $8->3$ and $8->5$ for the duration $G_{8}$, then Fog 34 schedules green signal
for the routes $4->7$ and $4->1$ for the duration $G_{4}$, then $\operatorname{Fog}$ 56 schedules green signal for the routes $6->1$ and $6->3$ for the duration $G_{6}$.

```
Algorithm 8 procedure_RR
    1: procedure
    2: Arrange the lanes in the descending order of their
        priority in a list to determine the sequence of green signal
        of the four lanes in (k+1)
            Calculate time quantum }\mp@subsup{T}{\mathrm{ avg }}{}\mathrm{ as }\frac{\mp@subsup{G}{2}{}+\mp@subsup{G}{4}{}+\mp@subsup{G}{6}{}+\mp@subsup{G}{8}{}}{4
            Compute cycle duration as 4* }\mp@subsup{T}{\mathrm{ avg }}{
    end procedure
```

For example, let the list in Procedure RR is (Prio lane ${ }_{2}$, Prio lane ${ }_{8}$, Prio lane 4 , Prio lane ${ }_{6}$ ). So first Fog 12 schedules green signal_for the routes $2->5$ and $2->7$ for the duration $T_{\text {avg }}$, then Fog 78 schedules green signal for the routes $8->3$ and $\_8->5$ for the duration $T_{\text {avg }}$, then Fog 34 schedules green signal for the routes $4->7$ and $4->1$ for the duration $T_{\text {avg }}$, then Fog_ 56 schedules green signal for the routes $6->1$ and $6->3$ for the duration $T_{\text {avg }}$.

In PR Sch, the green signal is given to the lane which has the highest priority. So, even if there is less number of vehiclesin the less priority lanes, they have to wait until the lanes receive the green signal which increases the waiting time. In SJ_Sch, instead of priority, the green signal is given to the lane which requires less duration of green signal. It increases the waiting time of vehicles in the lanes where the green signal duration is high. Waiting time decreases in RR_Sch since it considers both priority and green signal duration.

Size of messages: The size of the Time $_{v}$ field in M $-V$ of $V_{v}$ is assumed as 2 bytes. Hence, the size of M_V (Size_M_ V ) is 16 bits. The size of $V_{2}, V_{4}, V_{6}$ and $V_{8}$ is assumed as 8 bits. The size of $G_{2}, G_{4}, G_{6}$ and $G_{8}$ is assumed as 2 bytes. Hence, the size of M Fog4 (Size M Fog4) is ( $2+8+16$ ) bits.

The agent knows the sets of possible states and actions. Each lane is in a particular level of vehicles depending upon the number of vehicles at any instant of time. Five levels such as - very low (VL), low (L), medium (M), high (H) and very high (VH) are considered in Var 3. The level of vehicles in a lane is VL,L,M,H,VH if the number of vehicles in that lane is $(0-20) \%$, $(21-40) \%$, $(41-60) \%$, (61$80) \%,(81-100) \%$ of the
total number of vehicles respectively across the intersection.

A state is a tuple of four levels corresponding to four incoming lanes. For example, let the current state is s1 $<\mathrm{L}, \mathrm{M}, \mathrm{L}, \mathrm{L}>$ i.e. the level of vehicles in lane ${ }_{2}$, lane ${ }_{4}$, lane $_{6}$, lane $_{8}$ are $\mathrm{L}, \mathrm{M}, \mathrm{L}, \mathrm{L}$ respectively. Now for a particular level of vehicles in lane ${ }_{2}$, the number of level of vehicle in lane $_{4}$, lane ${ }_{6}$, lane 8 is $5^{3}$ and the number of possible states is $5^{3}$. So for five different level of vehicle in lane ${ }_{2}$, the number of possible states is $5 \times 5^{3}(=625)$.


Var 3 considers four actions - green signal in lane ${ }_{2}$, lane $_{4}$, lane $_{6}$ and lane ${ }_{8}$ as ( $\mathrm{g} 2, \mathrm{~g} 4, \mathrm{~g} 6, \mathrm{~g} 8$ ). The sequence of execution of these four actions is determined dynamically by the agent.

The execution of any four actions one after another creates a cycle. For example, the sequence ( $\mathrm{g} 2, \mathrm{~g} 4, \mathrm{~g} 6, \mathrm{~g} 8$ ) creates a cycle. The agent maintains a Q-table (Fig. 2) to store the records corresponding to 625 number of states. So the Q-table has 625 number of records. Each record in Q-table has four pair of attributes corresponding to four possible actions. These attributes are $G_{2}, G_{4}, G_{6}, G_{8}$, $Q_{2}, Q_{4}, Q_{6}, Q_{8}$ where $G_{2}, G_{4}, G_{6}, G_{8}$ are the duration of action $\mathrm{g} 2, \mathrm{~g} 4, \mathrm{~g} 6, \mathrm{~g} 8$ and $Q_{2}, Q_{4}, Q_{6}, Q_{8}$ are Q -value of action $\mathrm{g} 2, \mathrm{~g} 4, \mathrm{~g} 6, \mathrm{~g} 8$.

| State | $\mathrm{G}_{2}$ | $\mathrm{Q}_{2}$ | $\mathrm{G}_{4}$ | $\mathrm{Q}_{4}$ | $\mathrm{G}_{6}$ | $\mathrm{Q}_{6}$ | $\mathrm{G}_{8}$ | $\mathrm{Q}_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Fig. 2. Q-table

```
Algorithm 9 Congestion Control Algorithm
Input Current state s1
Output Updated Q-table
    procedure
                Calculates total waiting time of vehicles in each
lane
3: Calculates the average waiting time (avg wt) of
the
    vehicles in each lane as total waiting time of vehicles in a lane
        Calculates current waiting time as the average
of
avg wt of the four lanes
5: \(\quad\) Searches Q-table for the record (Rec s1)
correspond-ing to the current state s1
6: Reads the attributes \(\left(G_{2}, Q_{2}\right),\left(G_{4}, Q_{4}\right),\left(G_{6}\right.\),
\(\left.Q_{6}\right),\left(G_{8}, Q_{8}\right)\) from Rec s1
7: \(\quad\) Sets \(i=2\) and \(p=0\)
\(8: \quad\) if \(i_{\leq} 8\) then
9: \(\quad\) if \(\left(G_{i}, Q_{i}\right)\) pair in Rec_s1 is empty then
10: \(\quad\) Performs the action \(g_{i}(\mathrm{~g})\) for duration \(\delta_{i}\)
(D) 11: Calls Algorithm10 FUNC(g,D) at the end
of D12: \(\quad\) Sets \(G_{i}=\operatorname{New} D\) and \(Q_{i}=\) New \(Q\)
13: \(\quad\) Inserts \(\left(G_{i}, Q_{i}\right)\) in the position of \(i^{\text {th }}\) pair
in Rec s1
14: \(\quad \mathrm{p}=\mathrm{p}+1\)
                    Break
                    else
                        \(\mathrm{i}=\mathrm{i}+2\)
                            Go to step 7
            end if
        end if
        if \(p=0\) then
            Compares \(Q_{2}, Q_{4}, Q_{6}, Q_{8}\) to find the
maximumQ-value_(max Q )
23: \(\quad\) Reads the duration (D) from the pair of
attribute corresponding to max Q
24: Performs the action (g) corresponding to the
pair
25:
D
26: \(\quad\) Sets \(D=\operatorname{New} D\) and max \(Q=N e w \underline{Q}\)
27: \(\quad\) Updates ( \(\mathrm{D}, \max \mathrm{Q}\) ) pair of attribute in Rec
s1
28: end if
```

29: end procedure
The agent senses the environment to determine the number of vehicles in each lane across the intersection, computes the current state, executes the congestion control algorithm (Algorithm 9) and computes the next state.

```
Algorithm 10 Calculation of duration and Q-value
    procedure \(\mathrm{FUNC}(\mathrm{g}, \mathrm{D})\)
        Reads the number of vehicles in each lane across the
        intersection to compute next state (s2)
            Calculates avg_wt of the vehicles in each lane in s2
            Calculates next waiting time as the average of avg_wt
    of the four lanes
        if next waiting time > current waiting time then
                Receives penalty from environment
                Decreases D
                Calculates D (New_D) using Equ. 2
                Calculates Q -value (New_Q) corresponding to ac-
    tion g in s 1 using Equ. 4
                return (New_D, New_Q)
            else
                Receives reward from environment
                Increases D
                Calculates D (New_D) using Equ. 3
                Calculates Q-value (New_Q) corresponding to ac-
    tion \(g\) in sl using Equ. 4
                return (New_D, New_Q)
            end if
    end procedure
```

Calculation of New D: The value of $D$ increases in case of reward and decreases in case of penalty. The difference between the next waiting time and current waiting time is considered as diff. In case of penalty, diff is positive and hence D is reduced (diff/3) as there are three red signal lanes at a time.

$$
\begin{equation*}
N e w_{D}=D-\frac{d i f f}{3} \tag{2}
\end{equation*}
$$

In case of reward, diff is negative. New_D is calculated depending on the number of vehicles and the distance (Dist)to be covered by the vehicles in the lanes for crossing the intersection in green signal. T7 is the time taken by the first row of vehicles in an incoming lane to cross Dist. So,T7 is (Dist/ start speed). T4 is the time to cross the inter vehicle distance and the length of the vehicle in the front row as discussed in section 3.1. For example, let the number of vehicles in lane $_{2}$ is $V_{2}$ and so the number of rows of vehicles in lane ${ }_{2}$ is $\left\lceil\frac{V_{2}}{2}\right\rceil$. New_D is the new duration of green signal in lane $_{2}\left(G_{2}\right)$ and it is the time which is required by the vehicles $\left\lceil\frac{V_{2}}{2}\right\rceil^{\text {th }}$ row of lane $_{2}$ to cross the intersection when
lane $_{2}$ gets green signal. New D is calculated using Equ. 3.

Calculation of Q-value: The agent calculates the Q-value [25] corresponding to the action g in s1 using Equ 4.
New $Q \equiv(1-\alpha) Q(s 1, g)+\alpha\left[R+\gamma * Q\left(s 2, g_{\max } Q\right)\right](4)$ where,
$\alpha=$ learning rate $(0<\alpha<1), \mathrm{Q}(\mathrm{s} 1, \mathrm{~g})=\mathrm{Q}$-value of the action g corresponding to $\mathrm{s} 1, R=$ reward or penalty, $\gamma=$ discounting factor $(0<\gamma<1) g_{\max } Q=$ action g which has the maximum Q -value, $Q\left(\bar{s} 2, g_{\max } Q\right)=\mathrm{Q}$-value of the action, $g_{\max } Q$ corresponding to s2

## IV. PERFORMANCE ANALYSIS

The performance of Var 1, Var 2 and Var 3 is studied qualitatively, theoretically ${ }^{-}$and ${ }^{-}$quantitativēly. The qualitative performance is studied in terms of communication overhead (COMM OH), storage overhead (STO OH) and computation overhead ${ }^{-}(\mathrm{COMP} \mathrm{OH})$. The theoretical and quantitative per- formances are studied in terms of waiting time. Waiting time isthe time during which the vehicles are waiting in the red signal. The increase in number of vehicles causes an increase inwaiting time which in turn escalates traffic congestion. Hence the variation of waiting time is studied by varying the number of vehicles. SUMO (Simulation of Urban MObility) is used toconstruct the road network, to generate traffic flows, mobility of the vehicles and to control the traffic lights whereas NS3 is used as a discrete-event network simulator. Traffic Control Interface is used in SUMO which allows to access vehicle speed, current traffic light etc. during the simulation.
A. Qualitative performance:

In this section COMM OH, STO OH and COMP OH ofall the three variants are ${ }^{-}$studied.

1) $\mathrm{COMM}_{1} \mathrm{OH}:$ Var_1: COMM OH in a state includes transmission of M_V from vehicles to Fogs, transmission ofM Fog1 to Fogs, - transmission of M Fog2 and M Fog3 to the intersection controllers to decide the green signal duration of the routes in the next state.

Fog 12, Fog $\underline{3} 4$, Fog $\underline{5} 6$ and Fog 78 receive M V_from $\mathrm{V}_{2}, \mathrm{~V}_{4}, \mathrm{~V}_{6}$ and $\mathrm{V}_{8}$ number of vehicles respectively. Hence, COMM _OH due to the transmission of $\mathrm{M}_{-} \mathrm{V}$ is Size_M_ V

$$
*\left(\mathrm{~V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right) \text { bits. }
$$

Four M_Fog1 are transmitted by Fogs. So, the COMM OH due to the transmission of M Fog1 is (Size $\bar{M}$ Fog 1*4) bits. Two Fogs send M Fog2 and other two Fogs send M Fog3 to the intersection controller. So, the COMM OH due to the transmission of M Fog2 is (Size M Fog2*2) and M Fog3 is
(Size M Fog3*2) bits.
COMM $\overline{\mathrm{OH}}$ of all the four states (per cycle) in Var 1 is $4^{*}\left(\right.$ Size $\underline{M} \underline{\bar{V}} *\left(\mathrm{~V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)+($ Size MFog $1 * 4) \overline{+}$ (Size $\underline{M}$ Fog $2 * 2$ ) $+($ Size $\underline{M}$ Fog3*2) bits.
Var 2: COMM_OH per cycle includes transmission of M V from vehicles to Fogs, transmission of M Fog4 to the Fogs to decide the green signal duration of the routes. COMM OH due to the transmission of $\mathrm{M}_{-} \mathrm{V}$ is Size_M V
$*\left(\mathrm{~V}_{2}+{ }^{-} \mathrm{V}_{4}+\mathrm{V}_{6}+{ }^{-} \mathrm{V}_{8}\right)$ bits. Each Fog sends three M Fog4 to the other three Fogs. COMM OH due to the transmission ofM_Fog4 is (Size M Fog4*3*4) bits.

So, in Var 2 COMM OH per cycle is Size $\mathrm{M} \mathrm{V} *\left(\mathrm{~V}_{2}+\right.$ $\left.\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)+($ Size M Fog4 * $3 * 4$ ) bits.

Var 3: COMM OH is zero as the agent is not communicating with the other entities of the network.
2) STO $\mathrm{OH}:$ Var_1: STO_OH includes storage of M V and M Fog1 at Fogs, storage of M_Fog2 and M_Fog3 at the intersection controller.

Fog 12, Fog 34, Fog $5 \underline{6}$ and Fog 78 store Table III. Table III has five records, each has two àttributes- Range of number of vehicles and Range of speed. Both Range of number of vehicles and Range of speed attribute contain two integer elements as veh min, veh max and speed min, speed max respectively. So the size of each record in Table III is $4 *$ sizeOf(int) bits and STO OH to store at four Fogs is $4 * 5 * 4 *$ sizeOf(int) bits.

Fog 12, Fog 34, Fog 56 and Fog_ 78 store $V_{2}, V_{4}, V_{6}$ and $\mathrm{V}_{8}$ number of M Vs respectively. So, STO OH to store M V is Size $M V^{*}\left(V_{2}+V_{4}+V+V_{8}\right)$ bits.

Each Fog stores four M Fog1. The intersection controller stores two M Fog2 and two M Fog3.

In Var $1, \overline{\text { STO }} \mathrm{OH}$ per cycle is $(4 * 5 * 4 * \operatorname{sizeOf}(\mathrm{int})+$ Size $\underline{M}_{\underline{V}}^{*}\left(\bar{V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)+\left(\right.$ Size M Fog_ $\left.{ }_{-} 4\right)+$
(Size_ $\bar{M}$ Fog $2 * 2)+($ Size_ M Fog3*2) bits.
Var 2: STO OH per cycle includes storage of M_V and쏘 Fog4 at Fogs. Fog 12, Fog 34, Fog 56 and Fog 78 store $\mathrm{V}_{2}, \mathrm{~V}_{4}, \mathrm{~V}_{6}$ and $\mathrm{V}_{8}$ number _of M Vs. Each Fog stores threeM Fog4.
In ${ }^{-}$Var 2 STO OH per cycle is Size $\mathrm{M}_{-} \mathrm{V}_{-}^{*}\left(\mathrm{~V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\right.$ $\left.\mathrm{V}_{8}\right)+($ Size M Fog $4 * 3 * 4)$ bits.

Var 3: STO $\overline{\mathrm{O}} \underline{H}$ is due to the maintenance of Q-table (Fig. 2). The level in a state is represented either by using a single (like L, M, H) or two characters (like VL, VH). So the size of each level is considered as $2 *$ sizeOf(char) and the size of each state is $4 * 2 *$ sizeOf(char) bits. For storing duration and Q -value of 4 actions, 8 integer elements are required. The size of the 8 integer elements is 8 * sizeOf(int) bits. So, STO OH is 625 * $(4 * 2 *$ sizeOf(char) $+8 *$ sizeOf(int) $)$ bits or $1,20,000$ bits. STO OH is constant as it is independent of the number of vehicles.
3) $\mathrm{COMP} O \underline{H}$ : Var 1: $\underline{\mathrm{COMP}} \mathrm{OH}$ of a state is as follows

- Counts the number of vehicles in lane $2_{2}$ lane $_{4}$, lane $_{6}$, lane $_{8}$ with COMP $\mathrm{OH} \mathrm{O}\left(\mathrm{V}_{2}\right), \mathrm{O}\left(\mathrm{V}_{4}\right), \mathrm{O}\left(\mathrm{V}_{6}\right), \mathrm{O}\left(\mathrm{V}_{8}\right)$ respectively
- Estimates the capacity of lanes with COMP OH $\mathrm{O}(1)$
- Predicts whether the routes are congested with COMP_OH O(1)
- Estimates Normalgreen, Threshold ${ }_{\text {green }}$ with COMP OH O(1)
- Estimates final duration of green signal for the green signal routes and maximum waiting time of vehicles in the red signal routes in the next state with COMP OH O(1)

In Var 1 COMP OH per cycle is $4^{*}\left(\mathrm{O}\left(\mathrm{V}_{2}\right)+\mathrm{O}\left(\mathrm{V}_{4}\right)+\right.$ $\left.\mathrm{O}\left(\mathrm{V}_{6}\right)+\mathrm{O}\left(\mathrm{V}_{8}\right)+\mathrm{O}(1)\right)$

Var 2 : COMP_OH per cycle is as follows:

- Computes distance from the intersection and Dist with COMP OH O(1)
- Computes the time required by the vehicles to enter tothe desired route after crossing d 1 or d 2 with COMP OH O(1)
- Count the number of $\underline{\mathrm{M}}$ Vs in the queue with COMP $\mathrm{OHO}\left(\mathrm{V}_{2}\right), \mathrm{O}\left(\mathrm{V}_{4}\right), \mathrm{O}\left(\mathrm{V}_{6}\right), \mathrm{O}\left(\mathrm{V}_{8}\right)$
- Reads time values from M_Vs with COMP $\mathrm{OH} \mathrm{O}\left(\mathrm{V}_{2}\right)$, $\mathrm{O}\left(\mathrm{V}_{4}\right), \mathrm{O}\left(\mathrm{V}_{6}\right), \mathrm{O}\left(\mathrm{V}_{8}\right)$
- Compares $V_{2}, V_{4}, V_{6}, V_{8}$ to find $G_{2}, G_{4}, G_{6}, G_{8}$ with COMP OH O( $\left.\mathrm{V}_{2}\right), \mathrm{O}\left(\mathrm{V}_{4}\right), \mathrm{O}\left(\mathrm{V}_{6}\right), \mathrm{O}\left(\mathrm{V}_{8}\right)$
- Calculates the priority of each lane and arrange the lanes in descending order of their priority with COMP OH $\mathrm{O}(1)$ in PR Sch
- Arranges the lanes in ascending order of $G_{2}, G_{4}$, $G_{6}, G_{8}$
values with COMP $\underline{O H} \mathrm{O}(1)$ in SJ Sch
- Arranges the lanes in descending order of their priorityand calculates $T_{\text {avg }}$ as the time quantum with COMP OH O(1) in RR Sch

So, COMP $\overline{\mathrm{O}} \mathrm{H}$ in PR Sch, $\underline{\mathrm{SJ}}$ Sch and RR Sch per cycleis $\mathrm{O}\left(\mathrm{V}_{2}\right)+\mathrm{O}\left(\mathrm{V}_{4}\right)+\mathrm{O}\left(\mathrm{V}_{6}\right)+\mathrm{O}\left(\mathrm{V}_{8}\right)+\mathrm{O}(1)$.

## COMP OH in Var 3: The agent

Reads the number of vehicles as $\mathrm{V}_{2}, \mathrm{~V}_{4}, \mathrm{~V}_{6}, \mathrm{~V}_{8}$ for cal- culating the current state _with COMP OH $\mathrm{O}\left(\mathrm{V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)$ Calculates avg wt of each lane in the current state with

COMP OH O(1)
Calculates current waiting time with COMP $\underline{\mathrm{OH}} \mathrm{O}(1)$
Searches the Q-table for the current state among 625 statesto find_Rec s1 with COMP OH O(1)

Reads four pair of attributes from Rec s $\underline{1}$ with COMP _OH O(1)
.Chooses an action from the Q-table with COMP OH $\mathrm{O}(1$.$) Calculates the next state with COMP$ OH
$\mathrm{O}\left(\mathrm{V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)$
Calculates avg wt of each lane with COMP_OH O(1) Calculates next waiting time with COMP $\overline{\mathrm{OH}} \mathrm{O}(1)$ Compares current waiting time and next waiting time with

COMP OH O(1)
Calculates duration of action (New D) and Q-value (New _Q) with COMP _OH O(1)

Inserts or updates (New _D, New_ Q) in the Qtable
corresponding to state s1 with COMP $\mathrm{OH} \mathrm{O}(1)$
In Var 3 COMP OH per action is $\mathrm{O}\left(\mathrm{V}_{2}+\mathrm{V}_{4}+\mathrm{V}_{6}+\right.$ $\left.\mathrm{V}_{8}\right)+$
$\mathrm{O}(1)$ and for four actions in a cycle is $4^{*}\left(\mathrm{O}\left(\mathrm{V}_{2}+\right.\right.$ $\left.\left.\mathrm{V}_{4}+\mathrm{V}_{6}+\mathrm{V}_{8}\right)+\mathrm{O}(1)\right)$.

The comparison of COMM OH, STO OH and COMP OHof the three variants is depicted in Table IV.

COMM OH is less in Var 2 than Var 1 as observed from

Table IV and zero in Var 3 as discussed in section IV.STO OH is less in Var 1 than Var 2 but constant in Var $\overline{3}$

Table Iv Comparison Of Comm Oh, Sto Oh And Comp Oh

| Number of <br> vehicles | COMM <br> Var 1 | OH <br> (bits) <br> Var 2 | STO_OF <br> Var 1 | (bits) <br> Var 2 | Var 1 | MP_OF <br> Var 2 | Var 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10056 | 2712 | 10376 | 2712 | 199 | 46 | 39 |
| 250 | 12456 | 3312 | 12776 | 3312 | 197 | 48 | 45 |
| 300 | 14856 | 3912 | 29576 | 3912 | 198 | 69 | 47 |
| 600 | 29256 | 7512 | 29576 | 7512 | 192 | 120 | 79 |
| 750 | 36456 | 9312 | 36776 | 9312 | 196 | 131 | 83 |

( $1,00,000$ bits) as discussed in section IV. COMP $\underline{\mathrm{OH}}$ inVar_ 1 is more than Var 2 and Var 3.

## B. Theoretical Analysis :

Queuing system is a study of long waiting lines or queues. It is denoted by Kendall's notation [26] which is representedas $\mathrm{A} / \mathrm{B} / \mathrm{C} / \mathrm{D} / \mathrm{E} / \mathrm{F}$, where,
. A is arrival time distribution
. B is the service time distribution C is the number of
. servers
. D is the maximum number of customers allowed in the system including those in service
. E is size of population from which the customers . come F represents the queuing discipline that is followed
Queuing system is used to estimate the waiting time of the queues [26]. The vehicles in the lanes form queues in red signals to cross the intersection. In Var 1, $\underline{\text { Var }} 2$ and Var 3
. A is poisson or markov (random) arrival time distributionas the arrival time of vehicles is random

- B is also markov service time distribution as the durationof green signal is dynamic
. C is the number of intersection controller
- D is the maximum number of vehicles that can be allowedto enter into the lanes of an intersection
- E is the size of vehicle population from where vehicles can come and enter into the lanes of an intersection. So, It is assumed as infinite.
F is queuing discipline. It is First Come First Serve (FCFS) as the vehicle which enters into a green signal lane first, goes out from that lane first.

The average waiting time $\left(W_{q}\right)$ of vehicles is calculated (Equ. 5) by considering the three variants as M/M/C FCFS system. The variation of $W_{q}$ with the number of vehicles for Var 1, PR Sch, SJ Sch, RR Sch and Var 3 is estimated in three different scenarios.

$$
W_{q}=\frac{p^{C+1} *(1-p)}{(C-1)!(C-p)^{2} * \lambda}
$$

where p is $\frac{\lambda}{\mu * C}, \lambda$ is arrival rate and $\mu$ is service rate (Equ. 6).
The simulation experiment is conducted to determine the variation of $\mu$ depending upon the three different values of $\lambda$ and the number of vehicles in each scenario.
total simulation time
$\mu=\overline{\text { number of vehicles across the intersection }}$



In the first scenario the network has a single intersection. The intersection has 4 pair of lanes $(\mathrm{C}=4)$. The variation of $\mu$ is 1.6 to 4.93 for $\lambda$ equal to $0.5,1,1.5$ and for the variation of the number of vehicles from 200 to 750 as in [16].

Fig 3a- Fig 3c show the variation of $W_{q}$ vs. vehicles for $\lambda=0.5,1,1.5$ respectively. It can be observed that ${ }^{-} W_{q}$ is lessin $\underline{R} R$ Sch than $\underline{V}$ ar 1, $\underline{P} R$ Sch, SJ Sch and Var 3.

In the second scenario the network has 6 intersections. Each intersection has 4 pair of lanes ( $\mathrm{C}=4$ ). The 6 intersections are comprised of 34 lanes. The variation of $\mu$ is 8.64 to 22.38 for $\lambda$ equal to $5.5,6,7.5$ and for the variation of the number of vehicles from 1200 to 2600 as in [27].

Fig 3d- Fig 3f show the variation of $W_{q}$ vs. vehicles for $\lambda=$
$5.5,6,7.5$ respectively. It can be observed that $W_{q}$ is less inVar 1 than PR Sch, SJ Sch, RR Sch and Var 3.

In the third scenario the network has 7 intersections. Each intersection has 4 bi-directional lanes ( $\mathrm{C}=4$ ). The 7 intersections are comprised of 40 lanes. The variation of $\mu$ is 11.22 to 90 for $\lambda$ equal to $7,9,11$ and for the variation of the
numberof vehicles from 5 to 40 as in [28].
Fig 3g-Fig 3i variation of $W_{q}$ vs. vehicles for $\lambda=7,9,11$ respectively. It can be observed that $\mathrm{W}_{\mathrm{q}}$ is less in Var 3 than Var 1, PR Sch, SJ Sch and RR Sch.

## C. Quantitative Performance :

In this section, the quantitative performance of Var 1, Var 2and Var 3 is elaborated.

1) Simulation environments and result: The simulation ex- periment is conducted to observe the variation of waiting time ( Wt ) by varying the number of vehicles and compare with the existing schemes [16], [27], [28]. The total simulation time is divided into some intervals. The arrival rate of vehicles in each interval is random and hence the waiting time of vehicles in the intervals increases or decreases randomly.


Hence the simulation experiment is also conducted to observe the variation of waiting time with intervals and compare with the existing schemes [29], [30]. In Var 3, Dist is assumed as $(\mathrm{d} 1+\mathrm{d} 2) / 2$.

First experiment is conducted for observing the variation of Wt with the number of vehicles for Var 1, $\underline{P R}$ Sch, $\underline{S} J$ Sch, RR Sch,_Var 3 and [16].

Second experiment is conducted for observing the variation of Wt with the number of vehicles for Var 1, PR Sch,SJ Sch, RR Sch, Var 3 and [27].
Third experiment is conducted for observing the variation of Wt with the number of vehicles for Var 1, PR Sch, SJ Sch, RR Sch, Var 3 and [28].

Fourth experiment is conducted for observing the variationof Wt with interval for Var 3 and [29].

Fifth experiment is conducted for observing the variation of Wt with interval for Var_3 and [30].
First experiment: It is conducted in an intersection with

4 pair of lanes in the presence of 200 to 750 vehicles asconsidered in [16]. The length of each lane is 1 Km . The length of the intersection is 200 meter. The maximum speed limit of vehicles is $60 \mathrm{Km} / \mathrm{hr}$ and inter vehicle distance is assumed as 2.5 m .
Fig 4a shows the plot of Wt vs. the number of vehicles for $\underline{P R}$ Sch, $\underline{S} J$ Sch and ŔR Sch. Fig 4b shows the plot of Wt vs. the number of vehicles for_Var 1,RR Sch,Var 3 and [16].
Second experiment: It is conducted in 6 intersections comprised of 34 lanes in the presence of 1200 to 2600 vehicles as considered in [27]. The speed of the vehicles varies between $10 \mathrm{Km} / \mathrm{hr}$ to $45 \mathrm{Km} / \mathrm{hr}$ and the length of lanes varies between 500 m to 1500 m as considered in [27].
Fig 4c shows the plot of Wt vs. the number of vehicles for $\underline{P R}$ Sch, $\underline{S} J$ Sch and R자 Sch. Fig 4d shows the plot of Wt vs. the number of vehicles for $\underline{V}$ ar $1, \underline{R} R$ Sch, $\underline{\text { Var }} 3$ and [27].

Third experiment: It is conducted in 7 intersections with bi-directional lanes in the presence of 5 to 40 vehicles as considered in [28]. The speed of the vehicles varies between the range $8.5 \mathrm{~m} / \mathrm{s}$ to $14 \mathrm{~m} / \mathrm{s}$ and the length of the intersectionis 20 m as considered in [28].

Fig 4 e shows the plot of Wt vs. the number of vehicles for $\underline{P R}$ Sch, SJ Sch and RR Sch. Fig 4f shows the plot of Wt vs. the number of vehicles for Var 1, RR Sch and, Var 3 and [28].

Fourth experiment: It is conducted in two intersections in the presence of 3200 and 6000 vehicles as considered in [29].

Fig 4 g and Fig 4 h show the plot of Wt vs. interval for Var 3 and [29] for 3200 and 6000 number of vehicles respectively. Fifth experiment: It is conducted in one intersection with four 1000 feet bi-directional lanes and the numbers of vehiclesentering each lane per hour is almost 1000 as considered in
[30].
Fig 4i shows the plot of Wt vs. interval for Var 3 and [30]. Observation from simulation results: It can be observedfrom Fig 4a, Fig 4c, Fig 4e that Wt in RR Sch is much less
than PR Sch and SJ Sch as discussed in section III(b).
It can be observed from Fig 4b that Wt increases with the number of vehicles for Var 1, RR Sch,Var 3 and [16] but Wtin Var 3 is much less than [16],Var 1 and RR Sch.
It can be observed from Fig 4d that Wt increases with the number of vehicles for Var 1,RR Sch,Var 3 and [27] but it is less in Var 3 than [27],Var 1 and RR Sch.
It can be observed from Fig 4f that Wt increases with the number of vehicles for Var $\underline{1}$, RR Sch, Var $\underline{3}$ and [28] but it is less in RR_Sch than [28], Var_1 and Var_ 3.

It can be observed from both Fig 4 g and Fig 4 h that Wt is less in Var $\underline{3}$ than [29].

It can be observed from Fig 4i that Wt is less in Var 3 than [30].
Discussion of results The waiting time in theoretical result (Fig 3a-Fig 3i) is much less than the waiting time in simulation result (Fig 4a, Fig 4b-Fig 4e, Fig 4f). In the theoretical result, the service rate of each vehicle is more or less same. But,in simulation scenario, the service rate of each vehicle is not same. Some vehicles can pass the green signal at one go, but some vehicles have to wait in the red signal. Thus, the service rate of vehicles differs.

In [16] the distribution of vehicles is assumed as same in theopposite pair of routes and the number of vehicles going fromsouth to north and north to south is assumed as much higher when the total number of vehicles is 600 . Such assumptionsreduce Wt to 13 secs for 600 vehicles. When Wt of vehiclesin a lane reaches the threshold, green signal is set to that lane. If the number of vehicles is more, all waiting vehicles cannot pass the lane at one go. Hence, some vehicles have to waitagain for the next green signal which increases Wt of vehicles. Both in [27], [28] traffic congestion is controlled by forming cluster of vehicles. In [27] the vehicles which are waiting in alane form standing cluster whereas the new vehicles entering into the same lane in red signal form moving cluster. Hencethe number of vehicles waiting in red signal increases whichcauses an increase in Wt in [27]. In [28], the duration of greensignal in a lane depends upon the size of cluster. If the size ofthe cluster in one lane is large, the vehicles in the other lanes
have to wait in the red signal which increases Wt in [28].

In Var 1, the upper bound of Wt i.e. the threshold value is calculated dynamically for the waiting vehicles. While calculating this threshold, both the number of vehicles present in the red signal lane and the occurrence of congestion in the green signal lane are considered. Thus, the threshold maintains a balance between the green signal lane and red signal lane, so that no vehicles have to wait for a long time. This allows


Fig. 4. Wt vs Number of vehicles
sufficient number of vehicles to pass the lane which helps to decrease Wt than [16].

In Var 1, the green signal is not on in all the routes corresponding to a particular incoming lane simultaneously as discussed in section III.1. This increases Wt in Var 1. In RR Sch, green signal is on in all the routes of an incoming lane simultaneously unlike Var 1 which decreases Wt in RR Sch than Var 1. RR Sch schedules green signal to the Tanes as per their priority and maintains a fixed time quantum which may not be sufficient for the lane having more number of vehicles to cross the intersection or the arc distance in one go. Var 3 schedules green signal
to the lanes dynamically in contrast to [29] and [30] depending upon the number of vehicles and the action in the current state. So, the scheduling criterion is much more realistic in Var 3 than RR Sch, [29] and [30]. It helps to mitigate Wt in Var 3 than RR Sch, [29] and [30].


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## V. CONCLUSION AND FUTURE WORK

Two vehicle dependent and one environment dependent Fog computing oriented schemes for controlling traffic congestion in ITS are analyzed in the present work.

The robustness and efficacy of the schemes are compared with each other qual- itatively and quantitatively. All the three proposed schemes outperform the existing schemes in terms of waiting time of vehicles.

The simulation experiment may be conducted in real time environment to compare the performance of the three proposedschemes.

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