

Unified Potential Fluctuations Model for Photoluminescence Spectra at Room Temperature - Cu(In,Ga)Se₂ Thin Films

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Room temperature photoluminescence (PL) is a powerful technique to study the properties of semiconductors. However, the interpretation of the data can be cumbersome when non-ideal band edge absorption takes place, as is the case in the presence of potential fluctuations. In this study, PL measurements are modeled to quantify potential fluctuations in Cu(In,Ga)Se₂ (CIGS) absorber layers for photovoltaic applications. Previous models have attributed these variations to either band gap fluctuations (BGF) or electrostatic fluctuations (EF). In reality, these two phenomena happen simultaneously and therefore affect the PL together. Here, a new model is introduced: the unified potential fluctuations (UPF) model. This model incorporates the effect of both types of fluctuations on the absorptance of the material, and subsequently the PL spectra. The UPF model is successfully used to fit both single- and three-stage co-evaporated ultrathin (around 500 nm) CIGS samples, showing a clear improvement with respect to the previous BGF and EF models. Some PL measurements show possible interference distortions, for which an interference function is used to simultaneously correct the PL spectra of a sample measured with several laser excitation intensities. All the models used in this work are bundled into a user-friendly, open-source Python program.

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I. INTRODUCTION

The ambition of achieving a carbon-free society is paving the way for continuous developments in photovoltaics (PV). With crystalline silicon increasingly dominating the market share, thin-film technologies must continue to evolve in order to compete with this established industry, both from a performance and an economical perspective. Within thin-film PV, Cu(In,Ga)Se₂ (CIGS) is seen as one of the most promising materials,¹ already reaching a 23.4% efficiency on a cell level.^{2,3} One of the key challenges to push the efficiency further is to understand and control the electronic properties of the absorber layer,⁴ given its inherent electronic inhomogeneities that degrade the V_{oc} ,^{5,6} for instance.

Proper characterisation techniques are indispensable to evaluate the electronic quality of absorber layers and to identify opportunities for improvement. In this regard, photoluminescence (PL) is a resourceful method to investigate the optoelectronic properties of a semiconductor. The possibility of changing experimental parameters such as the temperature and excitation intensity allow the exploration of diverse material characteristics such as the band gap, defect distribution, quasi-fermi level splitting (QFLS) and potential variations,⁷ among others. There are extensive PL studies on chalcopyrite materials that examine these parameters. Measurements at low temperatures have been performed to identify the ionisation energies of defect levels^{8,9} and spatial variations of the QFLS,¹⁰ as well as absolute values of the QFLS at room temperature (RT).¹¹ Moreover, the positive effect of KF post-deposition treatments was quantified from PL measurements by noting a reduction in potential fluctuations at low temperature PL¹² and reduced sub-band gap absorption in RT PL.¹³

The inhomogeneity of CIGS has been confirmed through spatially resolved PL. With submicron lateral resolution measurements, fluctuations of the QFLS¹⁴ and local band gap¹⁵ have been identified, the last one being attributed to local changes of composition.^{16,17} To relate these electrical properties to PL spectra, the generalized Planck's law is often used, which links the energy-dependent PL emission $I_{PL}(E)$ to the external rate of spontaneous emission under non-equilibrium conditions, given by¹⁸

$$I_{PL}(E) = \frac{2\pi}{h^3 c^2} \frac{a(E)E^2}{\exp\left(\frac{E-\Delta\mu}{k_B T}\right) - 1}, \quad (1)$$

where h is Planck's constant, c the speed of light, $a(E)$ the absorptance, $\Delta\mu$ the QFLS, k_B the Boltzmann constant and T the absolute temperature. This relation holds for constant material properties and $\Delta\mu$.⁷ To compute the QFLS, it can be assumed that for E well above the band gap E_g , $a(E) = 1$, such that the equation can be simplified to obtain $\Delta\mu$ as a function of I_{PL} . This provides an upper limit for the open-circuit voltage V_{oc} .⁷ Nevertheless, it has been shown that this high-energy tail fitting procedure is very sensitive to the fitting region.¹⁹ This could lead to reasonable differences in the obtained $\Delta\mu$ and must therefore be used carefully.

Other approaches to the use of Eq. (1) involve modeling the absorptance $a(E)$ in an attempt to fit the resulting PL spectrum. Given the inhomogeneous nature of CIGS, potential fluctuations arising from band gap fluctuations (BGF) and electrostatic fluctuations (EF) are present in such polycrystalline absorbers.⁶ These two are visualized in Fig. 1. For BGF [Fig. 1(a)], the CB and VB edges vary independently, changing the local band gap throughout the material. Here, we can define a global, average band gap: \bar{E}_g . For EF [Fig. 1(b)], the CB and VB edges vary synchronously, keeping the band gap E_g constant. In both cases, the maximum QFLS $\Delta\mu_{max}$ of the material is reduced, limiting the V_{oc} of the resulting cell.⁴ Moreover, the absorptance profile is also affected, and models that deviate from the ideal, step-like absorptance must therefore be used. Some approaches that include sub-band gap absorption have been proposed. On the one hand, BGF have been modeled with a Gaussian probability distribution of local band gaps around a mean band gap to describe the absorptance²⁰ and PL spectra.²¹ On the other, EF were included in a general sub-band gap absorption model that uses exponential decays to describe band tails.¹⁹ Even though the models part from different physical principles, they both offer plausible fits to PL spectra of CIGS absorber layers. However, each type of fluctuation is treated independently, when both are expected to occur concurrently.⁶

These models assume only one PL emission peak, which is the case of CIGS at RT, corresponding to the band-to-band transition.⁷ Several peaks might hint to the presence of a secondary phase²² or deep defects,²³ but can also be attributed to interference.^{24,25} In the latter, the resulting fringes can be predicted and corrected for with an interference function (IF).²⁴

The purpose of this study is to introduce the Unified Potential Fluctuations (UPF) model, which merges the effect of band gap fluctuations and electrostatic fluctuations to describe non-ideal absorption of a semiconductor. Using this model, valuable information on potential fluctuations of the absorber layer can be obtained even before integrating it into a solar cell. The presence of these potential fluctuations is evaluated from RT PL measurements, which can

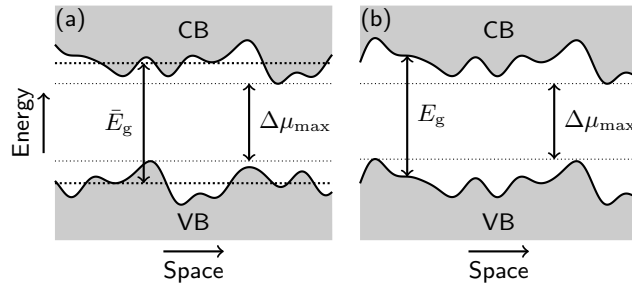


FIG. 1. Schematics of the spatial variation of the conduction band (CB) and valence band (VB) in the case of (a) band gap fluctuations and (b) electrostatic fluctuations.

be directly related to the absorption profile. The model is used to describe the PL spectra of three ultrathin CIGS absorber layers: one without band gap gradient (single-stage co-evaporated), one with a nodge band gap profile (three-stage co-evaporated) and a final single-stage co-evaporated one where interference effects were visible. In the latter, a correction with the IF is done. This work starts by elaborating on the existing models for the description of different potential fluctuations and deriving the unified approach, along with the experimental methods used in this study. The models are then applied to experimental PL data, where a possible correction for interference is also considered. Finally, we summarize the most important conclusions and provide information developed program.

II. MODELING

A. Band gap fluctuations model

Band gap fluctuations describe the spatial variations of the fundamental band gap.²¹ Independent variations of the conduction and valence band level across the material result in a spatially inhomogeneous band gap, as seen in Fig. 1(a). This can have several causes. In CIGS, it is mainly due to a compositional variation (variations in the Ga and In content change the band gap), stress (strain-induced band gap variation due to the distortion of the lattice) and stoichiometry (a change in the local Cu content affects the band gap).²⁰

A general model for the influence of BGF on the absorptance was introduced by Rau and Werner.²⁰ In order to compute the impact of BGF on the efficiency of a solar cell, a probability distribution for the band gap was used. A Gaussian distribution of local band gaps was assumed around the mean band gap of the material, expressed as:

$$P(E_g^{\text{loc}}) = \frac{1}{\sigma_g \sqrt{2\pi}} \exp \left[\frac{-(E_g^{\text{loc}} - \bar{E}_g)^2}{2\sigma_g^2} \right], \quad (2)$$

where E_g^{loc} is the local band gap, \bar{E}_g the mean band gap and σ_g the standard deviation of the distribution.²⁰ Moreover, the absorptance for a given local band gap is considered to be ideal ($a(E) = 1$ for $E \geq E_g^{\text{loc}}$ and $a(E) = 0$ for $E < E_g^{\text{loc}}$). After integration over the spectrum of possible local band gaps with Eq. (2), the absorptance on a larger scale can be described by

$$a(E) = \frac{1}{2} \text{erfc} \left(\frac{\bar{E}_g - E}{\sqrt{2}\sigma_g} \right), \quad (3)$$

where erfc is the complementary error function. Figure 2(a) shows the absorptance for different standard deviations of the Gaussian distribution. As σ_g is increased, the absorptance is symmetrically broadened around \bar{E}_g , which creates an absorption tail below the mean band gap. The impact of BGF on PL spectra was further developed by Mattheis et al.²¹ To this end, Eq. (1) is used to describe the *local* PL emission, where the band gap E_g^{loc} is well defined. Variations in the QFLS are possible, which is why this variable is also only locally defined: $\Delta\mu^{\text{loc}}$. To quantify the scale of the fluctuations in comparison to the charge carrier transport, a parameter $\beta \in [0, 1]$ is introduced.²¹ For variations occurring on small length scales ($\beta = 0$), the quasi-fermi levels flatten and $\Delta\mu^{\text{loc}}$ is constant. For large scale fluctuations ($\beta = 1$), charge carrier transport can be neglected and the quasi-fermi levels follow the local band gap. To account for all fluctuation length scales, the authors define $\Delta\mu^{\text{loc}} = \mu_0 + \beta E_g^{\text{loc}}$.²¹

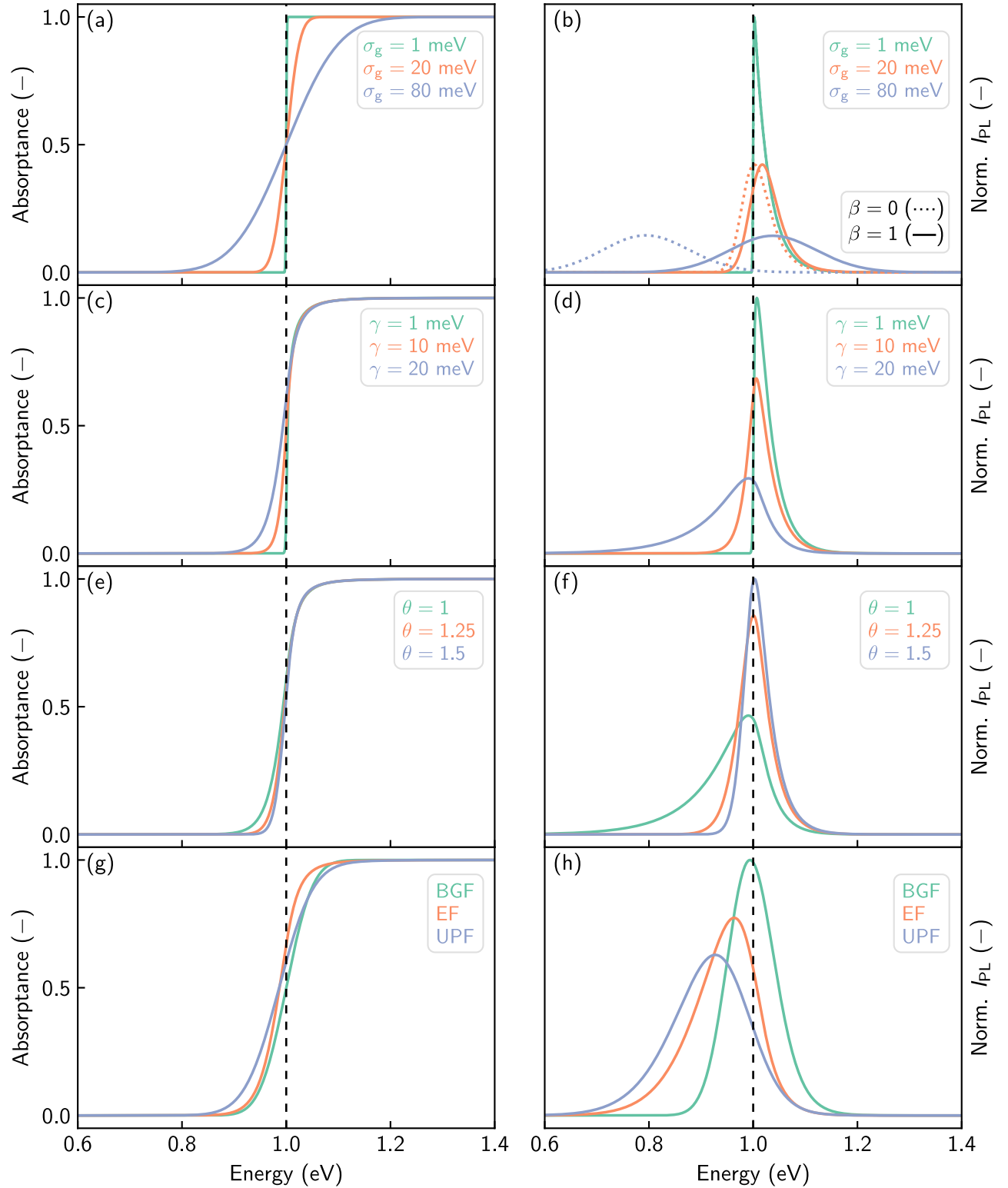


FIG. 2. Absorbance (left column) and area-normalized PL spectra (right column) for different model parameters in the BGF, EF and UPF models. (a) and (b): BGF model for $\sigma_g \in \{1, 20, 80\}$ meV and $\beta \in \{0, 1\}$. The absorbance profile is not affected by the length scale of the fluctuations. (c) and (d): EF model for $\gamma \in \{1, 10, 20\}$ meV and $\theta = 1$. (e) and (f): EF model for $\theta \in \{1, 1.25, 1.5\}$ and $\gamma = 20$ meV. (g) and (h) BGF, EF and UPF models for $\sigma_g = 40$ meV, $\beta = 0.5$ (intermediate scale fluctuations), $\theta = 1.25$ and $\gamma = 35$ meV. For all subplots, it holds (where applicable): $\bar{E}_g = E_g = 1$ eV, $T = 300$ K and $a_0d = 15$, as suggested in Katahara et al.¹⁹ The dashed line is plotted at the (average) band gap.

Using the Boltzmann approximation for the exponent in Eq. (1) (valid for $E - \Delta\mu^{\text{loc}} \gg k_{\text{B}}T$), the local contributions to the PL emission can be integrated with the Gaussian probability distribution to obtain the *global* PL emission:

$$I_{\text{PL}}(E) = \frac{\pi}{h^3 c^2} E^2 \operatorname{erfc} \left(\frac{\bar{E}_{\text{g}} - E + \beta \sigma_{\text{g}}^2 / (k_{\text{B}}T)}{\sqrt{2} \sigma_{\text{g}}} \right) \times \exp \left[-\frac{E - \mu_0 - \beta \bar{E}_{\text{g}}}{k_{\text{B}}T} + \frac{1}{2} \left(\frac{\beta \sigma_{\text{g}}}{k_{\text{B}}T} \right)^2 \right]. \quad (4)$$

Figure 2(b) shows how the area-normalized PL emission is affected by σ_{g} in the case of small and large scale fluctuations ($\beta = 0$ and $\beta = 1$, respectively). In general, it is observed that the PL peak broadens for larger fluctuations, which can be expected when considering the effect on the absorptance in Fig. 2(a). For large scale fluctuations, the peak is centred around the mean band gap of 1 eV. This peak is shifted towards lower energies for smaller scale fluctuations, and this phenomenon is intensified as σ_{g} increases. This is why the continuous and dashed green lines overlap in Fig. 2(b). These area-normalized spectra are independent of μ_0 , as this is just a scaling factor in Eq. (4).

B. Electrostatic fluctuations model

Changes in the potential also arise from *electrostatic fluctuations*, which distorts the band structure of the material.⁷ In this case, the valence and conduction band are shifted together while keeping a constant band gap, as seen in Fig. 1(b). This is a consequence of the distribution of charged states, originating from structural defects, doping atoms and impurities.⁶ In these disordered materials, states within the average band gap are introduced to form the so-called band tails, which extend the absorption to energies below the band gap.

Typical functional forms for these band tails are exponential decays from the edge of the band gap into the forbidden gap, typically called Urbach tails.²⁶ Shklovskii and Efros²⁷ noted a sharper decay for tails arising from charged defects, which results in an exponential decay to the power 1.25. Furthermore, a 1.5 power exponentially decaying absorption tail was identified by Franz²⁸ and Keldysh²⁹ when an electric field is present, possibly caused by charged impurities. As CIGS has a high degree of compensation and charged grain boundaries,⁴ exponential powers near 1.25 and 1.5 can be expected, instead of Urbach tails with a power of 1.

Generally, the functional forms of density of states G of the tail states are described as exponentials, which Katahara et al.¹⁹ bundled into an exponential function for energies below the band gap:

$$G(\Delta E) = \exp \left(- \left| \frac{\Delta E}{\gamma} \right|^{\theta} \right) \quad (E < E_{\text{g}}), \quad (5)$$

where γ and θ are the characteristic energy and power of the decay, respectively, and $\Delta E = E - E_{\text{g}}$.³⁰ To construct the density of states for all energies, this behavior under the band gap was joined with an ideal square root behavior of the density of states above the band, typical for direct semiconductor materials.³¹ This is done by means of a convolution operation, expressed as

$$G(\Delta E) = \frac{1}{2\gamma\Gamma(1 + 1/\theta)} \int_{-\infty}^{\Delta E} \exp \left(- \left| \frac{\Delta E_*}{\gamma} \right|^{\theta} \right) \times \sqrt{\Delta E - \Delta E_*} d\Delta E_*, \quad (6)$$

where Γ is the gamma function.³⁰ The prefactor of the integral is included for normalisation purposes. Based on this density of states, the absorption coefficient α can be computed with $\alpha(E) = \alpha_0 G(E)$, where α_0 is a proportionality parameter dependent on the material. The absorptance is then given by

$$a(E) = 1 - \exp[-\alpha(E)d], \quad (7)$$

where d is the characteristic length over which carriers are generated and recombined.¹⁹ The behavior of the absorptance when varying the values of γ and θ is shown in Figs. 2(c) and 2(e). As γ increases, the tail states penetrate more into the band gap, which broadens the absorptance towards lower energies. For a change in θ , the increase of

the exponential power of decay results in a reduction of the tail states. In both cases, the effect on energies above the band gap is minimal. Finally, the PL spectrum is computed with Eq. (1), to which an occupation dependent factor is subsequently added:¹⁹

$$I_{\text{PL}}(E) = \frac{2\pi}{h^3 c^2} \frac{E^2}{\exp\left(\frac{E-\Delta\mu}{k_{\text{B}}T}\right) - 1} \times \left\{ 1 - \exp\left[-G(\Delta E)\alpha_0 d \times \left(1 - \frac{2}{\exp\left(\frac{E-\Delta\mu}{2k_{\text{B}}T}\right) + 1}\right)\right]\right\}. \quad (8)$$

The resulting area-normalized PL spectra for different values of γ and θ are shown in Figs. 2(d) and 2(f). In all cases, a broader absorptance results in the widening of the PL peak. Both parameters have an impact on the energy at which the emission peaks, such that a significant presence of tail states results in a peak shift towards lower energies, as can be expected. The impact of changing $\Delta\mu$ is negligible when considering normalized spectra.

C. Unified potential fluctuations model

The previous paragraphs introduced two existing models for non-ideal absorptance in semiconductors. The physical motivation behind these two models is the possibility of compositional variations in the material (which can change the local band gap) and the random distribution of charged defects (which influences the local electrostatic potential), both of which can cause fluctuations of the potential landscape. In reality, one can expect both effects to take place simultaneously.⁶ To the extent of our knowledge, no studies are available that superimpose the contributions of BGF and EF to the absorptance, and consequently the PL spectrum. Here, an attempt is made to combine the two phenomena into the *unified potential fluctuations* model, along with the impact on the absorptance properties and PL emission.

Starting from the general expression for the *global* absorptance a^{glob} in the BGF model, we have²¹

$$a^{\text{glob}}(E) = \int_{-\infty}^{\infty} a^{\text{loc}}(E, E_{\text{g}}^{\text{loc}}) P(E_{\text{g}}^{\text{loc}}) dE_{\text{g}}^{\text{loc}}. \quad (9)$$

In the BGF model, $a^{\text{loc}}(E, E_{\text{g}}^{\text{loc}})$ is then assumed to be ideal for each local band gap. For the UPF model, we choose to include an absorptance term as described in the EF model, parting from the ideal semiconductor behavior to include a decaying tail at $E_{\text{g}}^{\text{loc}}$ in the absorptance spectrum. In this sense, $a^{\text{loc}}(E, E_{\text{g}}^{\text{loc}})$ is defined by Eq. (7), redefining ΔE as $\Delta E^{\text{loc}} = E - E_{\text{g}}^{\text{loc}}$ in Eq. (6). This approach allows for the simultaneous occurrence of a fluctuating local band gap and the presence of tail states as a consequence of charged defects. Combining all the expressions, we obtain

$$a^{\text{glob}}(E) = \int_{-\infty}^{\infty} \left\{ 1 - \exp[-G(\Delta E^{\text{loc}})\alpha_0 d] \right\} \times P(E_{\text{g}}^{\text{loc}}) dE_{\text{g}}^{\text{loc}}, \quad (10)$$

where $P(E_{\text{g}}^{\text{loc}})$ and $G(\Delta E^{\text{loc}})$ are defined by Eqs. (2) and (6), respectively. For the analysis of PL spectra, the derivation is similar to the procedure followed for the absorptance. The general expression for the global absorptance in the BGF model is²¹

$$I_{\text{PL}}(E) = \frac{2\pi}{h^3 c^2} \int_{-\infty}^{\infty} E^2 \exp\left[-\frac{E - (\mu_0 + \beta E_{\text{g}}^{\text{loc}})}{k_{\text{B}}T}\right] \times a^{\text{loc}}(E, E_{\text{g}}^{\text{loc}}) P(E_{\text{g}}^{\text{loc}}) dE_{\text{g}}^{\text{loc}}, \quad (11)$$

assuming a Boltzmann approximation. Again, we can assume a local absorption profile as in the EF model to arrive at

$$\begin{aligned}
 I_{\text{PL}}(E) = & \frac{2\pi}{h^3 c^2} \int_{-\infty}^{\infty} E^2 \exp \left[-\frac{E - (\mu_0 + \beta E_g^{\text{loc}})}{k_B T} \right] \\
 & \times \left\{ 1 - \exp[-G(\Delta E^{\text{loc}})\alpha_0 d] \right\} \\
 & \times P(E_g^{\text{loc}}) dE_g^{\text{loc}}.
 \end{aligned} \tag{12}$$

The UPF model quantifies potential fluctuations in terms of BGF (with \bar{E}_g , σ_g and β) and EF (with γ and θ). Moreover, the temperature T and the product $\alpha_0 d$ in the absorptance terms in Eqs. (10) and (12) are left as free parameters of the model. Figure 2(g) plots the absorptance of the three models for a reference set of parameters. Parting from the symmetrical BGF model for the absorptance around the band gap of 1 eV, the symmetry is broken when looking at the UPF model, given the inclusion of non-ideal absorptance from the EF. The absorptance of the energies below the band gap is increased, as a consequence of the tail states that are now present. Above the band gap, it is clear that the EF model for absorptance deviates somewhat from the ideal case, which is a consequence of the convolution operation in Eq. (6). This causes the UPF absorptance model to drop below the BGF one, which assumed a unity absorptance above the local band gap. In Fig. 2(h), the area-normalized PL intensities for each model are shown, which depicts what can be expected based on the absorptance in Fig. 2(g). The UPF model presents the broadest absorptance for the same parameters as in the BGF and EF models, which results in the broadest PL emission. The emission peaks of the BGF and EF models are around the same energy, and the combination of these two in the UPF model noticeable shifts the peak to a lower energy. Again, the impact of μ_0 and $\Delta\mu$ is neglected on these normalized spectra.

III. EXPERIMENTAL

Three CIGS absorber layers, denoted sample 1, 2 and 3, are used to evaluate the models presented in Section II. All the samples were prepared by either single- or three-stage co-evaporation process on soda lime glass/Mo substrates at 550 °C, and have a thickness of around 500 nm. XRF measurements revealed that $[\text{Cu}]/([\text{Ga}] + [\text{In}]) = \text{CGI} \approx 0.8$ and $[\text{Ga}]/([\text{Ga}] + [\text{In}]) = \text{GGI} \approx 0.3$ for all absorber layers. Single-stage sample 1 was deposited on a Mo/6 nm Al_2O_3 /5 nm NaF stack. The holes that are formed in the Al_2O_3 back layer enhances light scattering, which reduces the interference of light reflecting back into the absorber layer.³² Moreover, the front surface was passivated with Al_2O_3 to increase the PL yield. Sample 2 was deposited through a three-stage process and underwent a post-deposition treatment (PDT) with RbF, similar as the KF treatment presented by de Wild et al.¹³ The stack is finalized with a 30 nm CdS front layer grown by means of chemical bath deposition. The roughness of the three-stage absorber layer and the PDT are believed to limit the occurrence of interference. Finally, sample 3 was deposited with a single-stage process, with a front CdS layer grown through chemical bath deposition. The PL measurements of this sample showed interference, which allowed the study of a correction with the interference function for a laser power series measurement.

Regarding the PL data acquisition, two different setups were used. The spectrum gathered for sample 1 is from a photospectrometer from PicoQuant with a TimeHarp 260 single photon counter for the time resolved measurements. The laser excitation wavelength was 532 nm at an approximate intensity of 0.1 W cm^{-1} and repetition rate of 3 MHz. For the intensity dependent measurement of sample 3, a Hamamatsu spectrometer was used. The excitation wavelength is unchanged at 532 nm, now with a 15 kHz rate. This setup allowed for a variation of the laser intensity from 1 to 46 mW. Finally, the data for sample 2 were also measured with this setup, at a fixed power of 3 mW. All PL spectra are corrected for the optical path and instrumental response. No absolute intensity calibrations were possible given the unavailability of a reference light source to calibrate the setup. Therefore, all the analyses in this work were done on normalized PL spectra, which still allowed for the study of the peak widths as a consequence of potential fluctuations.

IV. RESULTS AND DISCUSSION

The BGF, EF and UPF models introduced in Section II were implemented in *Python*, followed by the development of a user-friendly interface that incorporates the models into one program. More details on the program are explained in Appendix 1 and the code can be accessed under Appendix 2. The program is used to fit experimental PL spectra

TABLE I. Subset of the fitted parameters of the BGF, EF and UPF models for the PL spectrum of sample 1 in the case of relaxed parameter bounds, along with the model errors.

| Model | E_g (eV) | θ | T (K) | ε |
|-------|------------|----------|---------|---------------|
| BGF | 1.22 | - | 250 | 0.0194 |
| EF | 1.28 | 1.75 | 350 | 0.0112 |
| UPF | 1.22 | 1.00 | 350 | 0.0077 |

of samples 1 and 2 to compare the different absorptance models in Section IV A. In Section IV B, the PL spectra of sample 3, where interference fringes are present, is touched upon. As explained in Section III, only normalized data are used.

A. Modeling of experimental data

The specifics of the preparation of samples 1 and 2 allowed for an interference-free PL measurement, such that the PL models can be applied directly. To start, fits of the PL spectrum of sample 1 were done with the BGF, EF and UPF models with relaxed limits in the parameter space of the fitting routine: $E_g \in [1, 1.4]$ eV, $\sigma \in [1, 100]$ meV, $\gamma \in [1, 100]$ meV, $\theta \in [1, 2]$ and $T \in [250, 350]$ K, with $\alpha_0 d$ fixed at 15, as suggested by Katahara et al.¹⁹ Moreover, μ_0 and $\Delta\mu$ are excluded from the analysis: the former because it does not affect normalized PL spectra, and the latter because of its negligible impact after normalization. Table I summarizes the fitted parameters worthy of consideration, along with the average fit error ε as defined in Eq. (A.1).

The errors indicate that decent fits are obtained for all models, the UPF model yielding the best results. Given the GGI ratio ($[\text{Ga}]/([\text{Ga}] + [\text{In}])$) of 0.3 for this sample, we can expect a band gap of around 1.20 eV,³³ which is below the values found for all the fitted models. This has to do with the definition of the band gap in each case. Experimentally, the high slope of the absorption coefficient tail is extrapolated and the value of the band gap is read off the intercept on the energy axis, in the form of Tauc plots.³⁴ This results in band gaps lower than the definition in the BGF case, for instance, where the *average* band gap is used and is located halfway the absorptance tail. Note how, in the absorptance plots of Fig. 2(a), the average band gap is the same for the three cases, even though different band gaps can be expected as σ_g changes. Moreover, the band gap in the EF model is defined very close to the tail start [see Figs. 2(c) and 2(e)], and is independent of the choice of γ and θ . In the BGF and UPF models, the parameter β also introduces some freedom in the choice of the average band gap when fitting normalized PL spectra, as changing this parameter merely results in an energy shift. For these reasons, a direct comparison between band gaps of the models and experimentally determined values is not possible without prior analysis.

It is worth noting that fits of the EF model often yield very high temperatures, beyond what has been measured externally.¹¹ This was also the case here, where the fitted temperature reached the upper bound of 350 K in the program. This issue also seems to be inherited by the UPF model, also reaching the maximum temperature in the fit. On the other hand, the fitted temperature in the BGF model reaches the lower bound of the program: 250 K. We do not expect a large increase in temperature during the measurement and certainly no decrease with respect to RT. Therefore, the fitted temperatures of all models appear to be unreliable for this normalized PL spectrum. Moreover, the exponential tail parameter θ also reached unanticipated values. Electrostatic fluctuations in CIGS are thought to be caused by the random distribution of charged states,⁴ which indicates that $\theta \in [1.25, 1.5]$.¹⁹ Both the fit values of the EF and UPF models are outside this range. It is clear how the freedom given to θ and T in the parameter space resulted in unexpected values. As more variables are added to a model, we might compromise its ability to discern the influence of parameters on the fit, which is particularly important for the many variables in the UPF model. A solution is therefore to fix as many parameters as known beforehand and limit the parameter ranges to physically feasible values. Fixing the band gap is not desirable, as mentioned earlier, but a sample temperature near RT (293 K) and $\theta \in [1.25, 1.5]$ are fair assumptions. Under these new conditions, the models were once again fitted to the data. The fits and relevant fit parameters are presented in Fig. 3(a), where the PL spectrum and two more shifted versions are shown to visualize the quality of the fit for each model. It is evident how the UPF model provides, once again, a better fit to the data. For this model, the error shown in the lower pane of Fig. 3(a) is the closest to 0. The BGF model correctly approaches the slope of the data in the high-energy tail of the peak, but fails to do so in the lower energy range. This is the opposite for the EF model. By superimposing these two in the UPF model, both sides of the peak are accurately matched. The average fit errors have logically increased, and now correspond to 0.0202, 0.0203 and 0.0093 for the BGF, EF and UPF models, respectively. The quality of the EF fit suffers the most from the restriction of the parameter space, evidencing the difficulty of this model to adapt to the measurement data under

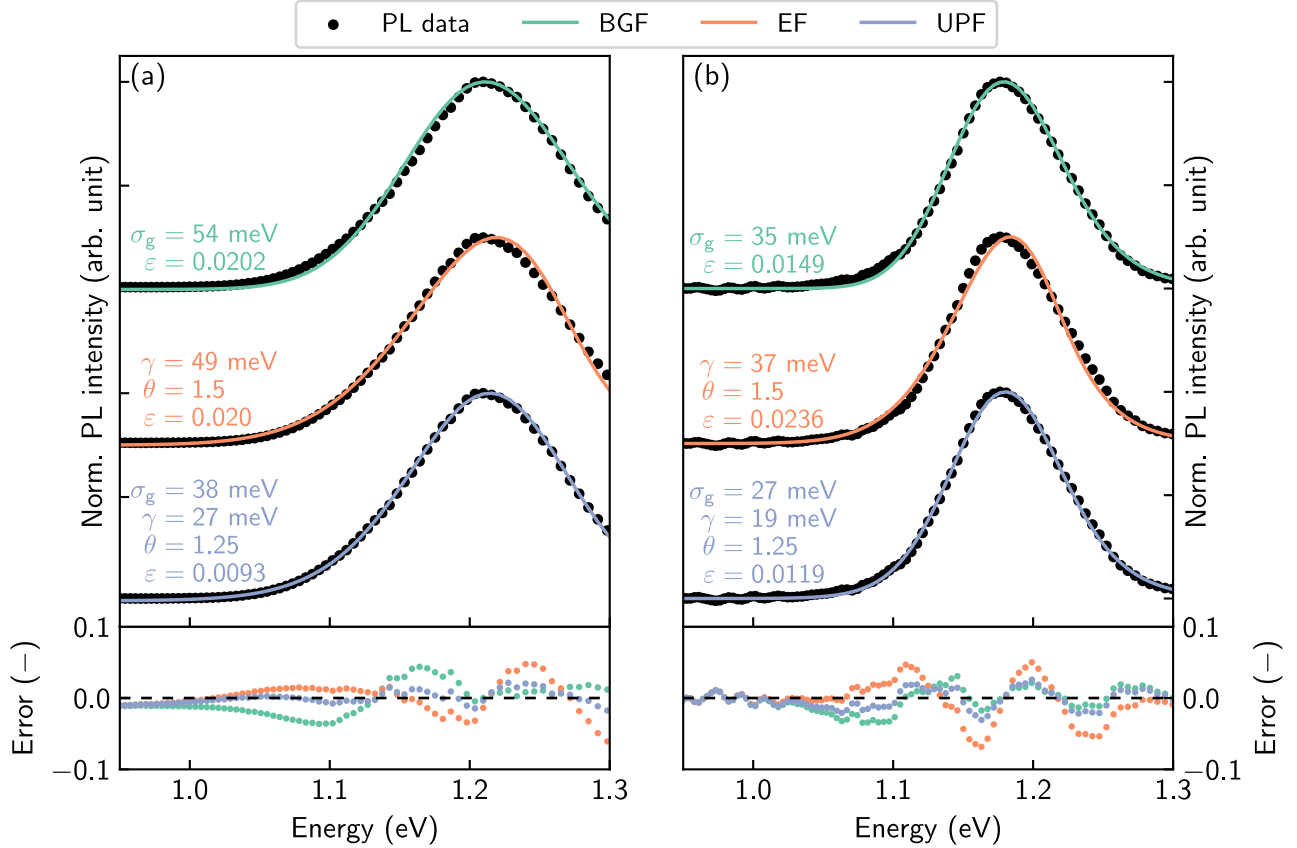


FIG. 3. Normalized PL spectrum along with two shifted copies of (a) sample 1 and (b) sample 2, fitted with the BGF, EF and UPF models with a limited parameter space: $T = 293$ K and $\theta \in [1.25, 1.5]$. The lower panes plot the difference between the data and the models.

modest assumptions. It is clear how the UPF model combines both types of fluctuations, band gap and electrostatic, to arrive at a closer match to the data. The BGF model widens the peak by including band gap fluctuations with a standard deviation of 54 meV, whereas the EF model incorporates an exponential decay with a characteristic energy of 49 meV and power of 1.5. All these values are reduced in the UPF model, since it combines the impact both potential fluctuations have on the peak width, offering a superior fit even with a constricted parameter space.

For some analysed CIGS samples, the improvement with the UPF model is less evident, as is the case for sample 2. Figure 3(b) plots the PL data and model fits for this sample, in the same way as Fig. 3(a) did for sample 1. Once again, we restrict ourselves to $T = 293$ K and $\theta \in [1.25, 1.5]$. The BGF model seems to correctly match the width of the PL spectrum, but once again fails to approximate the luminescence at the lower end of the peak (between 1.05 and 1.1 eV), i.e. where sub-band gap emission takes place. This region is, in turn, slightly overestimated by the EF model, and an overall mismatch with the data is found for this model. Given that sample 2 was co-evaporated in a three-stage process, there are intrinsic band gap variations in the depth of the sample given a Ga gradient. This can explain the dominance of BGF over EF and the resulting fit errors for each model. The UPF model again provides the closest match to the data, but the improvement from the BGF model is minimal, mainly improving the lower tail of the peak [as seen in the lower pane of Fig. 3(b)].

B. Interference correction

When analysing PL spectra, it is important to distinguish between actual PL emission and optical artefacts of the measurement, such as interference. This causes the appearance of additional peaks in the PL spectra or significant shoulders,²⁵ which makes the analysis of potential fluctuations rather cumbersome. Figure 4(a) depicts this effect for a series of measurements of sample 3 at different laser excitation intensities. The dots represent the measurement data and the lines the best fit according to the UPF model.

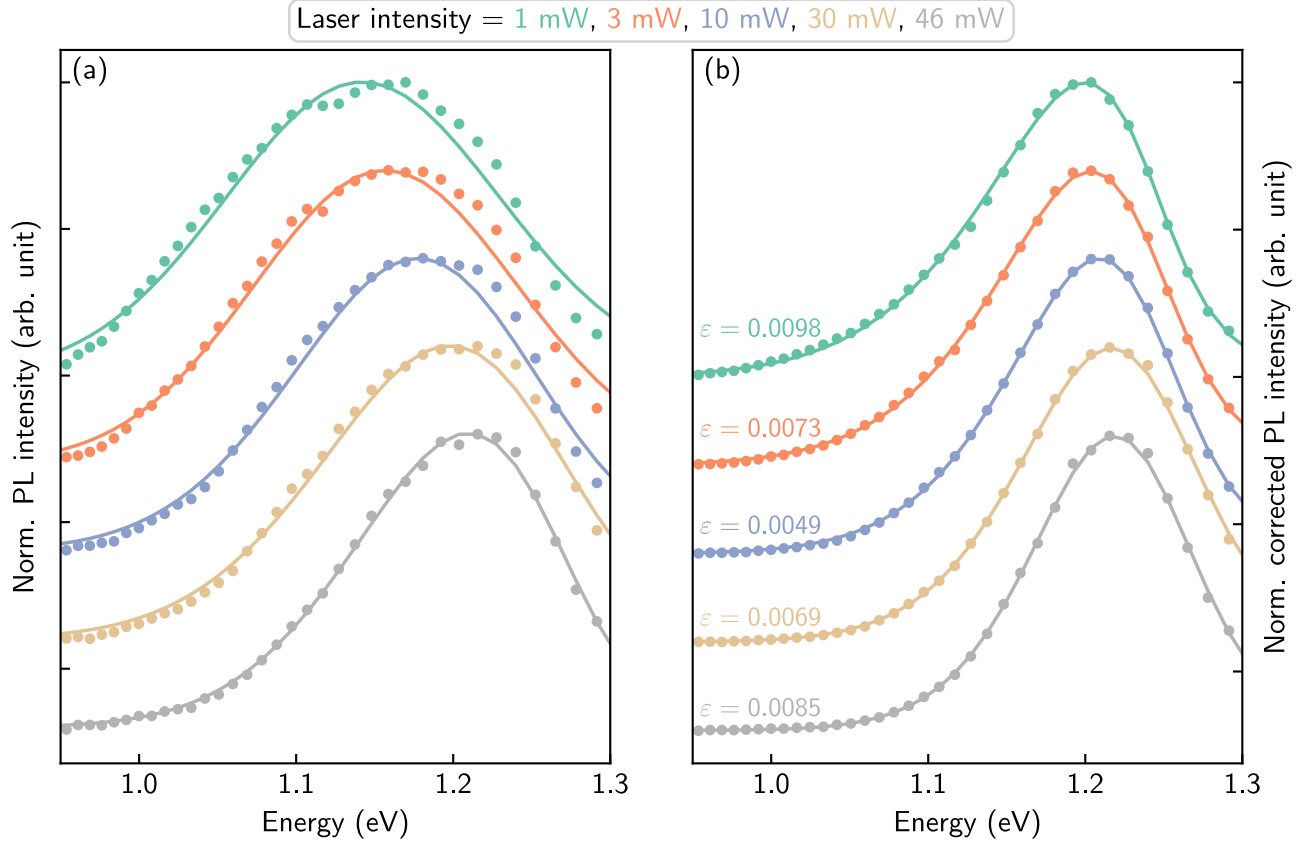


FIG. 4. (a) Normalized PL spectra measured at different laser excitation intensities and (b) normalized PL spectra after interference correction with $L(z) = \delta(z - 363 \text{ nm})$ of sample 3. In both subplots, the dots represent the measurement data and the line the best fit based on the UPF model. A fixed band gap of 1.24 eV was chosen for (b).

Depending on the sample, several peaks might actually hint to the presence of a secondary phase in the material, as can happen in CZTSe.²² However, it can also lead to the incorrect interpretation of peaks as multiple phases.^{35,36} Previous characterisations with GDOES and XRD on similar single-stage layers as in Fig. 4(a) excluded this possibility.¹³ Moreover, the thermal quenching of possible defect states at RT makes defect-related transitions improbable, given the small activation energy it would have based on the shown plot. We can therefore assume the PL emission comes from band-to-band transitions,⁷ such that interference offers a plausible explanation for the distortion of the spectra.

From the fitted UPF models in Fig. 4(a), it is visible how no proper description of the data is possible. The BGF and EF model fits were also not satisfactory (not shown here). Interference effects can be corrected for from an experimental or a modeling approach. Previous studies explore the possibility of averaging PL spectra over several excitation angles²⁵ or including a scattering layer to reduce coherent superposition of light.³⁷ Larsen et al.²⁴ conducted a comprehensive study on interference corrections for CIGS thin films. Here, we implement an interference correction by means of an interference function (IF) model and suggest how its estimation can be improved with a laser power series as the one shown in Fig. 4(a).

The IF was first derived by Holm et al.,³⁸ and it is based on the prediction of the interference fringes in a stack of thin-film layers. It includes both the effect of multiple-beam interference (caused by multiple reflections of the PL emission at the interfaces of the material, as typically seen in transmission measurements) and wide-angle interference (caused by the interference of the directly emitted beam and the one reflected at the bottom interface).²⁴ The model starts by assuming the configuration shown in Fig. 5, typical for CIGS absorber layers. The complex coefficient of each layer can be written as $N_x = n_x + ik_x$, $x \in \{1, 2, 3\}$, from which Fresnel's coefficients for reflection (r_{xy}) and transmission (t_{xy}) for light travelling from any layer x to y can be computed. These coefficients were adapted to account for the interface roughness, as described by Larsen et al.²⁴ Next, it is assumed that the spontaneous emission is caused by randomly oriented dipoles, and the contribution over the full sphere solid angle is averaged.³⁸ This results in the quantification of the emission probabilities for each light polarisation. If we assume perpendicular light

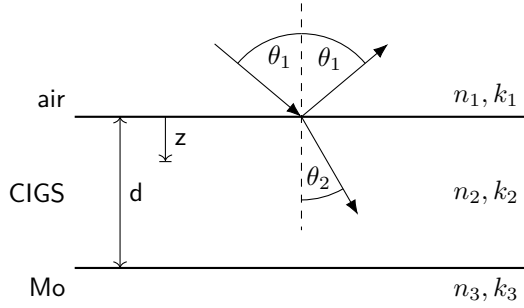


FIG. 5. Visualisation of assumed stack of layers and the relevant parameters for the computation of the IF. Inspired by Larsen et al.²⁴

incidence ($\theta_1 = 0$, such that $\theta_2 = 0$), we obtain²⁴

$$P(\lambda, z) = \frac{1}{8\pi} \frac{n_2}{n_1} |t_{21}|^2 \frac{|1 + r_{23} \exp(i\delta)|^2}{|1 - r_{21} r_{23} \exp(i\phi)|^2}, \quad (13)$$

where $\phi = 4\pi N_2 d / \lambda$ and $\delta = 4\pi N_2 (d - z) / \lambda$. All in all, the resulting interference function IF is computed as the integration of this emission probability $P(\lambda, z)$, the excitation intensity $E(z)$ and the luminescence distribution $L(z)$ over the depth of the sample:

$$\text{IF}(\lambda) = \frac{\int_0^d P(\lambda, z) L(z) E(z) dz}{\int_0^d L(z) E(z) dz}. \quad (14)$$

Typically, $E(z) = A \exp(-\alpha_{\text{laser}} z)$, where α_{laser} is the absorption coefficient at the laser wavelength, following Lambert-Beer's law. $L(z)$ quantifies the emission profile, which is not straightforward to predict, since it is dependent on the absorber layer emission characteristics. A uniform emission throughout the depth of the sample indicates that $L(z) = 1$, whereas more localized emissions can be approximated with Gaussians centred at the emission depth.²⁴ After computing the interference function, the corrected PL emission spectrum can be simply found with $I_{\text{PL}}^{\text{corr}} = I_{\text{PL}} / \text{IF}$.

Following the emission profile $L(z)$ used by de Wild et al.,³⁹ we will correct for interference by using a Dirac delta function, which removed the fringe distortion from the measurements. As in that study, the CdS layer is omitted due to the proximity of its refractive index to that of CIGS in the investigated spectral range and the fact that no sharp interface is expected.³⁹ Moreover, an rms roughness of around 50 nm was measured and used to account for scattering in Fresnel's equations.²⁴ Figure 4(b) plots the same PL spectra as in Fig. 4(a), this time with an interference correction using an IF with $L(z) = \delta(z - 363 \text{ nm})$. The choice for an emission profile at this depth is based on the minimisation of the addition of the UPF fit errors for the plotted laser intensities. This gave a total added error of 0.0374. It is also visually evident how this choice of IF removes the broad peak shoulders evident in Fig. 4(a).

When looking at only one PL spectra, it might be the case that several $L(z)$ allow for a proper interference correction. This is the case for the measurement at 46 mW, where by using $L(z) = \delta(z - 195 \text{ nm})$ the peak distortion was removed and the UPF model could be fitted with great accuracy, as seen in the bottom curve of Fig. 6. Given that the measurements are done at the same spot, it is reasonable to assume the IF to remain unchanged for other excitation intensities, since the material properties that define the function stay the same. If we were to use $L(z) = \delta(z - 195 \text{ nm})$ to correct for the measurement at 1 mW, for instance, an unsatisfactory fit with the UPF model is obtained. This points to the fact that this choice of $L(z)$ is not suitable for the sample in general, despite the encouraging fit from correcting only the 46 mW measurement.

By means of this example, we encourage the use of several PL measurements at different laser excitation intensities when the interference function is to be used to remove fringes. Under the assumption that the IF is unaffected from one measurement to the other, it allows for a better selection of the emission profile $L(z)$, given the possibility of discarding profiles that are not able to adequately correct all measurements simultaneously.

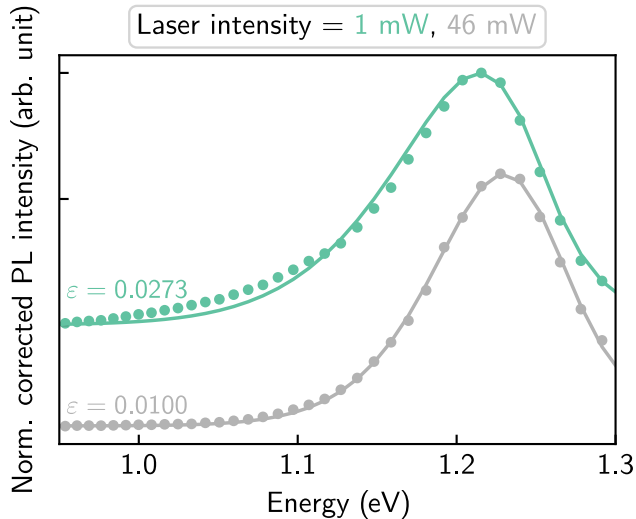


FIG. 6. Normalized PL spectra after interference correction with $L(z) = \delta(z - 195 \text{ nm})$ at laser excitation intensities of 1 mW and 46 mW of sample 3. The dots represent the measurement data and the line the best fit based on the UPF model.

V. CONCLUSION

In conclusion, a unified model for potential fluctuations (UPF) was formulated based on existing models for band gap and electrostatic fluctuations (BGF and EF, respectively). The models were fit to measured PL spectra of both ultrathin single- and three-stage co-evaporated CIGS samples, and the results show a much better fit for the UPF model compared to the BGF and EF models. The UPF introduces a new model that takes into consideration both sources of potential fluctuations, providing a more complete description of the physical phenomena involved in the absorption and consecutive emission of light involved in PL. The presence of these fluctuations in absorber layers partially explain losses in V_{oc} of the resulting solar cell. Therefore, the fitted model parameters can provide an insight into the extent of these losses as a consequence of deposition conditions, post-deposition treatments, etc., even before integrating the absorber layer into a device. The application of this model is not limited to only CIGS layers, but could be generally applied to direct band gap semiconductors. However, careful consideration of the parameter space in the model is needed to ensure realistic fitting outcomes, for which previous knowledge of the nature of the fluctuations can be useful. Moreover, the use of absolute PL spectra could increase the parameter sensitivity of the model. An extension to the analysis presented in this work could include the manufacturing of solar cells from absorber layers analysed with the UPF model in order to relate the presence of potential fluctuations to the solar cell performance. Some PL spectra were distorted by interference effects, for which an interference function (IF) was used to correct for the fringes. It was shown how the correction using several measurements on the same spot under different laser excitation intensities, can help to search for the right luminescence distribution needed in the IF.

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DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Appendix: PL modeling program

1. Program description

The PL modeling program, with the possibility of fitting the BGF, EF and UPF models and correcting for interference with the IF, was fully developed in Python. A graphical user interface based on *Tkinter* was built on top of the modeling back end to expand its accessibility, providing the user with a straightforward fitting tool. In the program, model parameters can be adjusted manually to directly visualize the impact of a variable on the PL spectrum. Here, a quick overview of the methods used in the program are presented. The code and a more in-depth explanation can be found accessed from Appendix 2.

The parameter bounds of the models can be easily configured by providing an optional configuration file to the program. All the fits are done with the `curve_fit` tool in `scipy.optimize`, which is a non-linear least square fitting routine that follows the Levenberg-Marquardt algorithm. It is wrapped around a function that enables the dynamic variation of the number of parameters to be fitted, given the user’s choice to fix model parameters. Numerical integrations use the `scipy.integrate.quad` function, which computes definite integrals based on QUADPACK. To speed up the computation of the EF model, a 2D lookup table was generated for the integral in Eq. (6) for the variables $\Delta E/\gamma$ and θ , as suggested by Katahara et al.³⁰ This also improves the computation time of the UPF model. Here, the final integration step of the model is done with `numpy.trapz` in the non-zero interval of the integrand, once again improving the computation time. Finally, the average model errors are computed with

$$\varepsilon = \sqrt{\frac{\sum_i (I_{\text{PL},i} - I_{\text{PL},i}^{\text{mod}})^2}{N}}, \quad (\text{A.1})$$

where $I_{\text{PL},i}$ and $I_{\text{PL},i}^{\text{mod}}$ are the experimental and modeled normalized PL intensity sampled according to the input data, respectively, and N the number of samples in the measurement.

2. Code availability

The Python program developed for this work, including the source code and a manual, is published in GitHub: <https://github.com/erikspaans/PL-Modeling>.

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