

MOS-AK

Analytical Modeling of double channel
GaN HEMTs

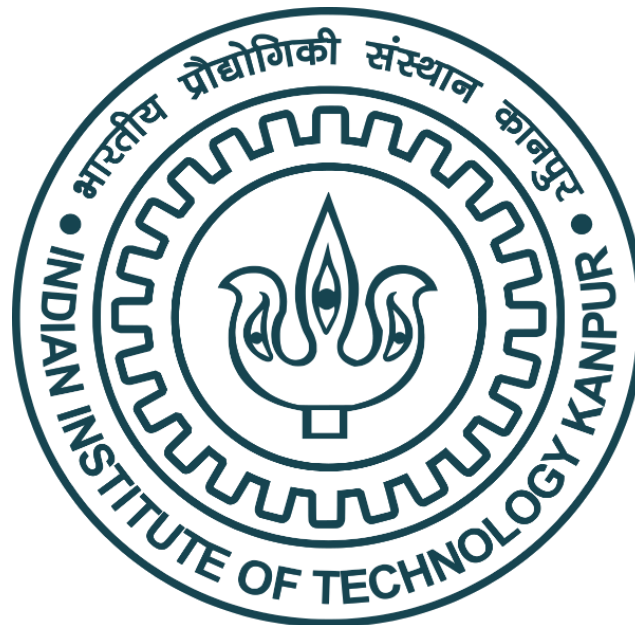
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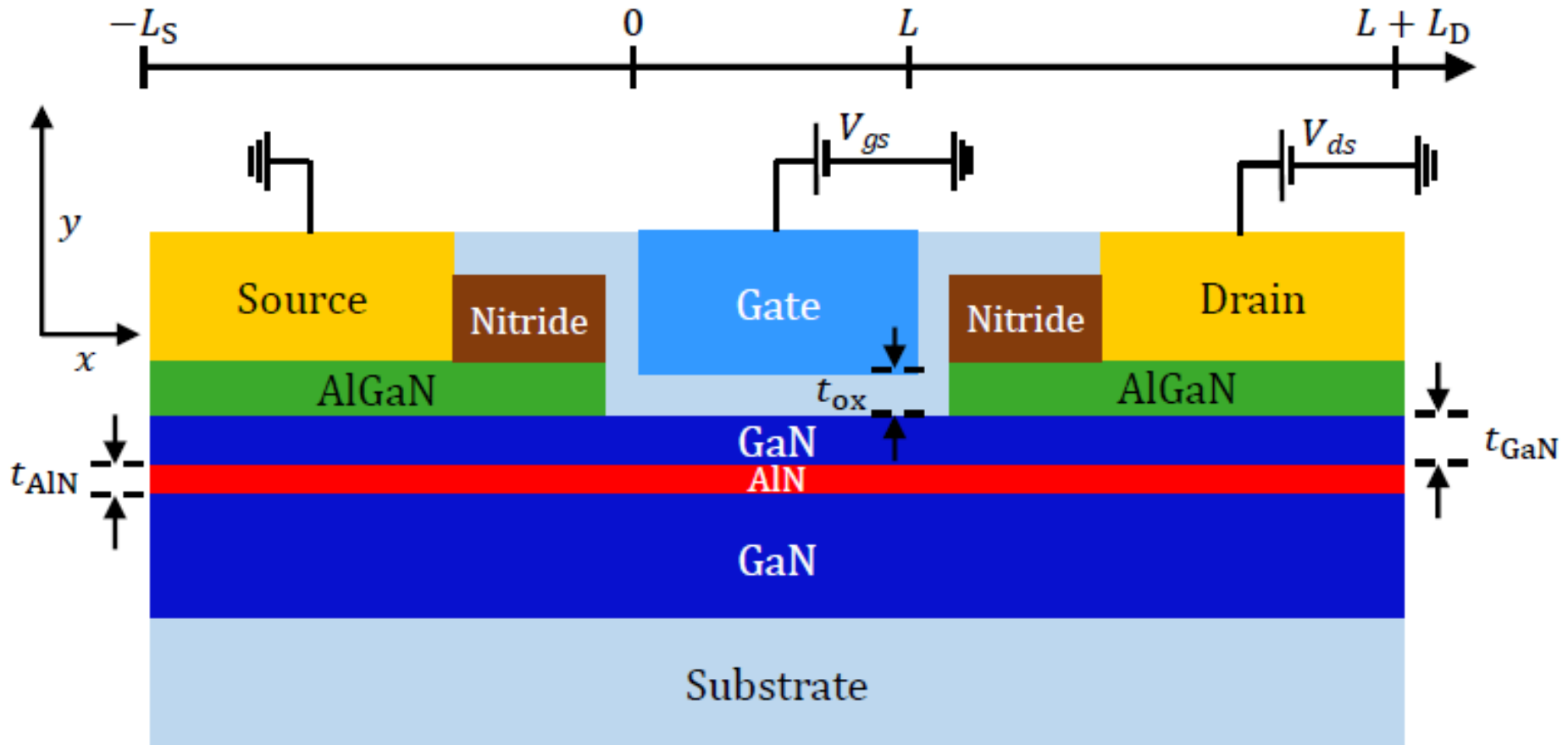
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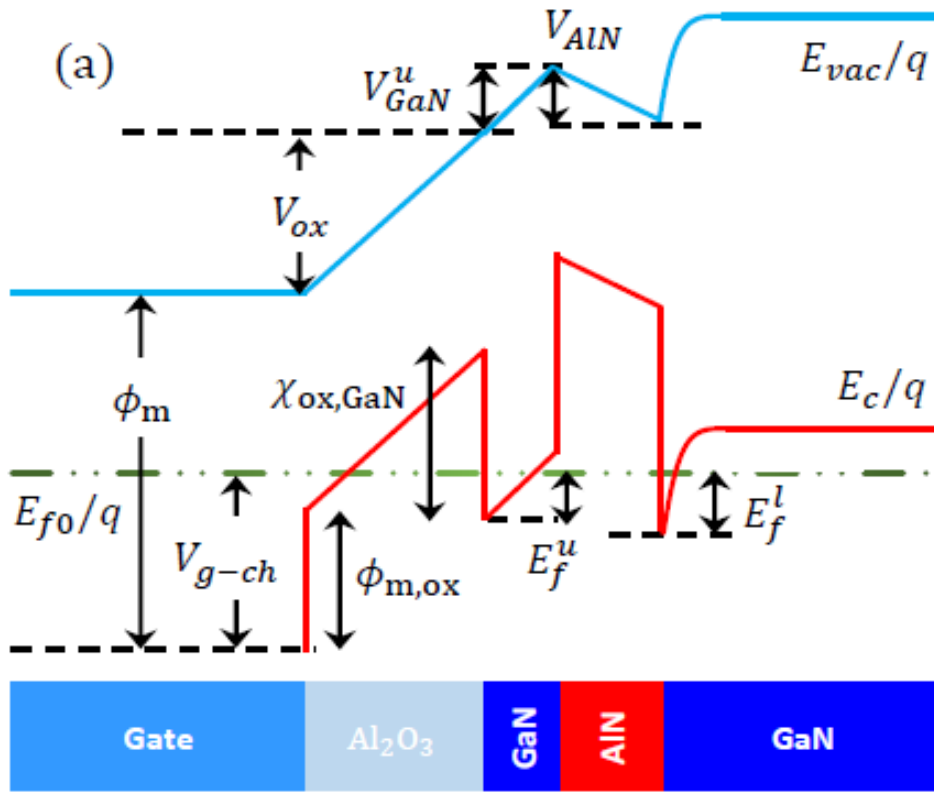
Acknowledgements



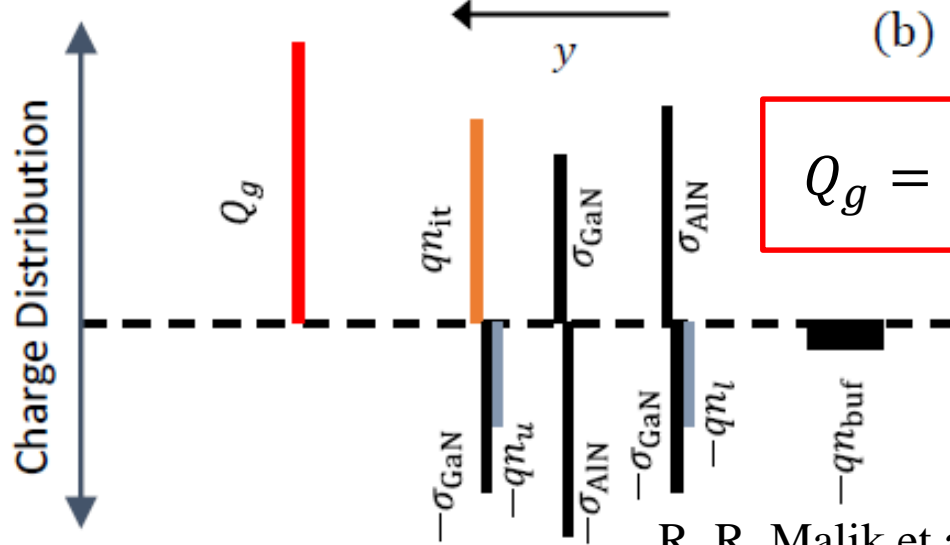
Device Schematic



Band diagram

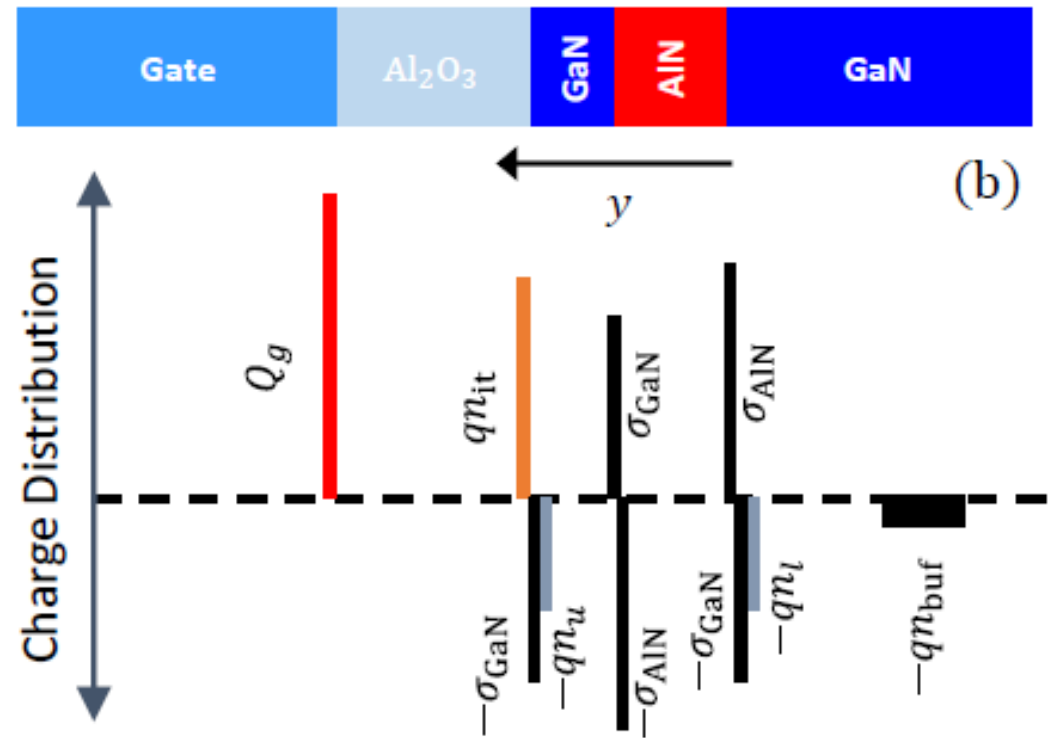


Charge neutrality



$$Q_g = -(qn_{it} - qn_u - \sigma_{\text{GaN}} - qn_l - qn_{\text{buf}})$$

1D Poisson Eq

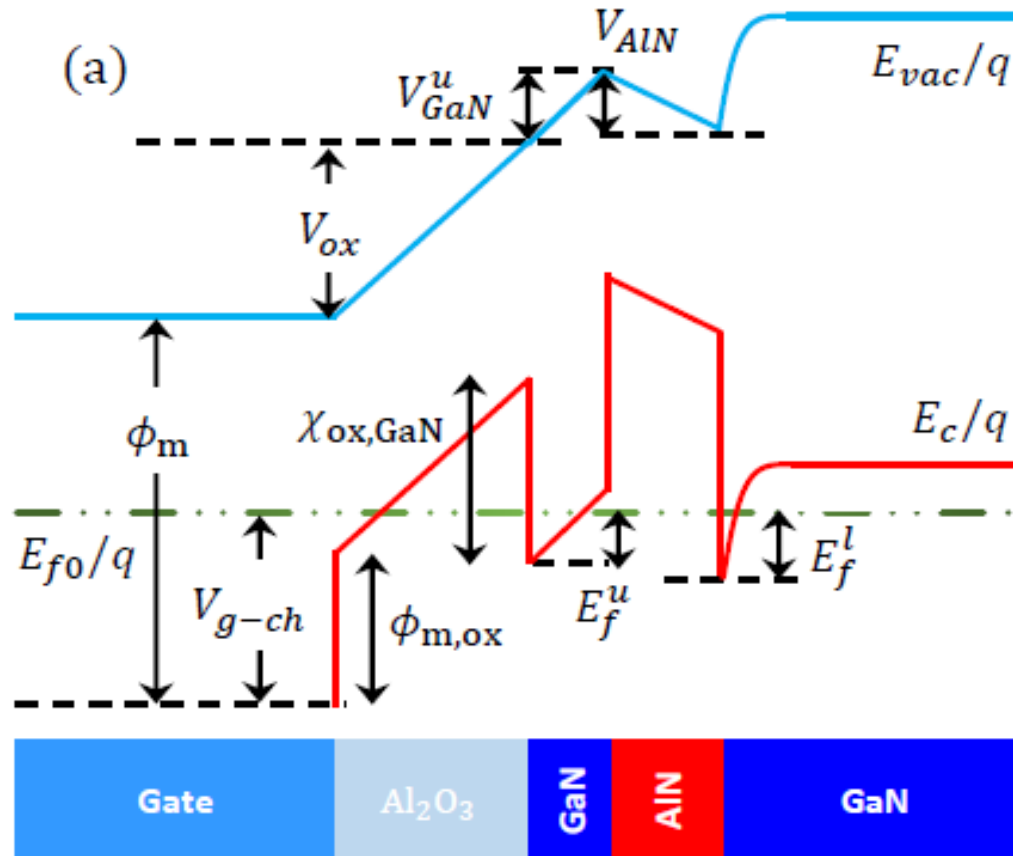


$$V_{ox} = \frac{Q_g}{C_{ox}} \quad (2)$$

$$V_{GaN}^u = \frac{Q_g + qn_{it} - \sigma_{GaN} - qn_u}{C_{GaN}} \quad (3)$$

$$V_{AlN} = -\frac{Q_g + qn_{it} - qn_u - \sigma_{AlN}}{C_{AlN}} \quad (4)$$

Potential balance – upper channel



$$\phi_{m,ox} - V_{g-ch} + V_{ox} - \chi_{GaN,ox} + \frac{E_f^u}{q} = 0 \quad (7)$$

$$E_f^u = qV_{gov}^u + \frac{q(qn_{it} - qn_u - \sigma_{\text{GaN}} - qn_l - qn_{\text{buf}})}{C_{\text{ox}}} \quad (8)$$

where $V_{gov}^u = V_{g-ch} - \phi_{m,ox} + \chi_{\text{GaN},ox}$ (9)

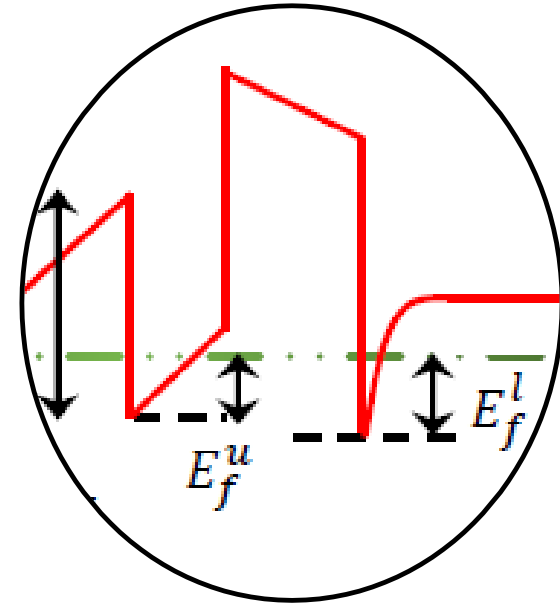
Redo the potential balance for lower channel

$$E_f^l = qV_{gov}^l + \frac{q(qn_{it} - qn_u - \sigma_{\text{GaN}} - qn_l - qn_{\text{buf}})}{C_{\text{ox}}} + q(qn_{it} - \sigma_{\text{GaN}} - qn_l - qn_{\text{buf}}) \left(\frac{1}{C_{\text{GaN}}} + \frac{1}{C_{\text{AIN}}} \right) \quad (10)$$

where $V_{gov}^l = V_{g-ch} - \phi_{m,ox} + \chi_{\text{GaN},ox} + \frac{\sigma_{\text{AIN}}}{C_{\text{AIN}}} + \frac{\sigma_{\text{GaN}}}{C_{\text{GaN}}} - qn_{it} \left(\frac{1}{C_{\text{GaN}}} + \frac{1}{C_{\text{AIN}}} \right)$ (11)

Sub-bands in triangular quantum wells

$$E_j = q \left(\frac{\hbar^2}{2m^*} \right)^{\frac{1}{3}} \left(\frac{3}{2} \pi q \mathcal{E} \right)^{\frac{2}{3}} \left(j + \frac{3}{4} \right)^{\frac{2}{3}} \quad (12)$$



$$E_{c1}^{u(l)} = \alpha \left(\mathcal{E}_{GaN}^{u(l)} \right)^{\frac{2}{3}} \quad (13)$$

where

$2.1920 \times 10^{-25} \text{ Kg}^{\frac{1}{3}} \text{ m}^{\frac{4}{3}} \text{ A}^{\frac{2}{3}}$ for GaN effective mass of $0.22m_0$

Fermi Dirac Statistics

$$n_{u(l)} = D_n kT \ln \left[1 + \exp \left(\frac{E_f^{u(l)} - E_{c1}^{u(l)}}{kT} \right) \right] \quad (14)$$

where $D_n = m^* / \pi \hbar^2$ is the 2-D DOS

$$n_u = D_n kT \ln \left[1 + \exp \left(\frac{qV_{gov}^u}{kT} + \frac{q(qn_{it} - qn_u - \sigma_{GaN} - qn_l - qn_{buf})}{C_{ox}kT} - \frac{\alpha}{kT} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{\frac{2}{3}} \right) \right] \quad (15)$$

$$n_l = D_n kT \ln \left[1 + \exp \left(\frac{qV_{gov}^l}{kT} + \frac{q(qn_{it} - qn_u - \sigma_{GaN} - qn_l - qn_{buf})}{C_{ox}kT} + \frac{q(qn_{it} - \sigma_{GaN} - qn_l - qn_{buf})}{kT} \left(\frac{1}{C_{GaN}} + \frac{1}{C_{AIN}} \right) - \frac{\alpha}{kT} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{\frac{2}{3}} \right) \right] \quad (16)$$

System of two non-linear equations with unknowns n_l and n_u

Drift-diffusion transport

$$J = J_u + J_l = -\mu_{nu}n_u \frac{dE_f}{dn_u} \frac{dn_u}{dx} - \mu_{nl}n_l \frac{dE_f}{dn_l} \frac{dn_l}{dx} \quad (20)$$

Integrate with limits

$$x : 0 \rightarrow L, n_u : n_{u,s} \rightarrow n_{u,d} \quad n_l : n_{l,s} \rightarrow n_{l,d},$$

$$I \frac{L}{W} = -\mu_{nu} \int_{n_{u,s}}^{n_{u,d}} \left(n_u \frac{dE_f}{dn_u} \right) dn_u - \mu_{nl} \int_{n_{l,s}}^{n_{l,d}} \left(n_l \frac{dE_f}{dn_l} \right) dn_l \quad (21)$$

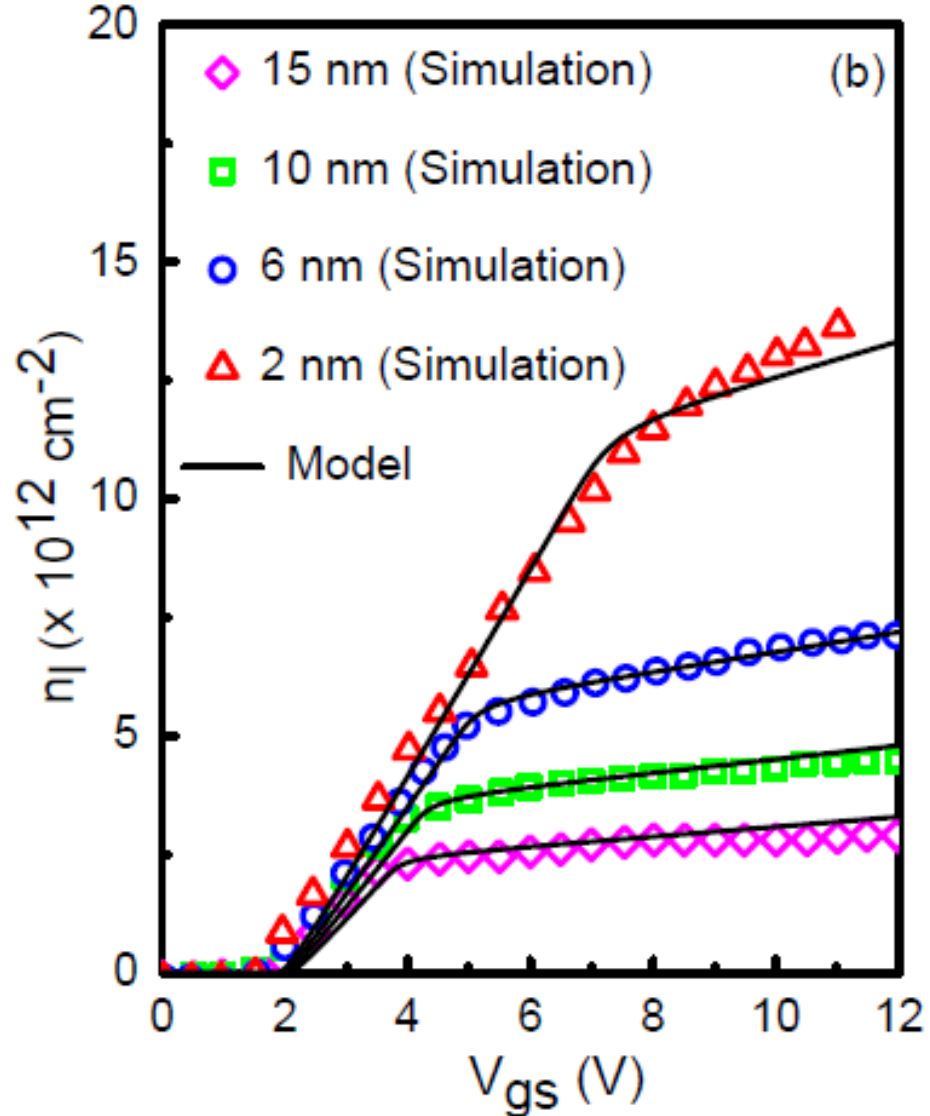
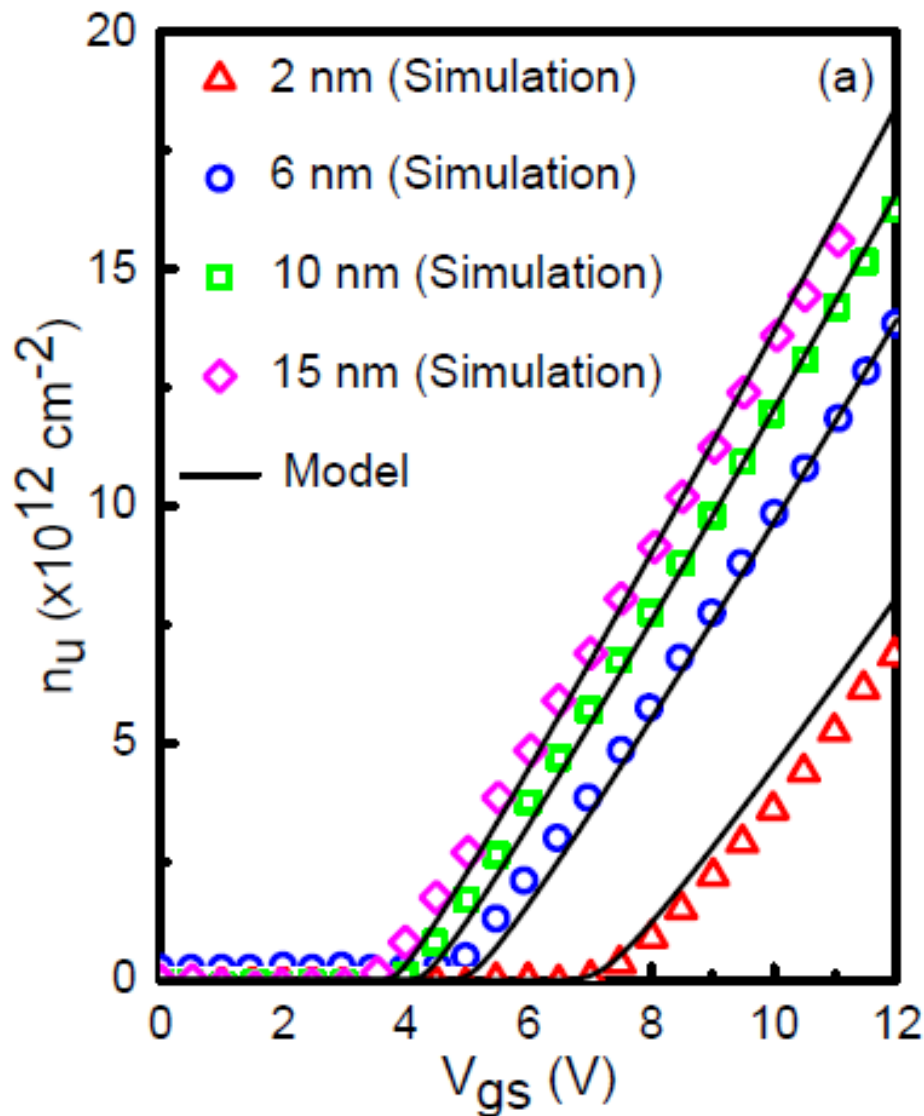
$$\begin{aligned} \frac{dE_f}{dn_u} = & \frac{q^2}{C_{ox}} \left(1 + \frac{dn_l}{dn_u} \right) + \frac{kT}{n_q} \frac{e^{n_u/n_q}}{e^{n_u/n_q} - 1} \\ & + \frac{2q\alpha}{3\epsilon_{GaN}} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{-\frac{1}{3}} \frac{dn_l}{dn_u} \quad (23) \end{aligned}$$

$$\begin{aligned} \frac{dE_f}{dn_l} = & \frac{q^2}{C_{ox}} \left(1 + \frac{dn_u}{dn_l} \right) + \frac{kT}{n_q} \frac{e^{n_l/n_q}}{e^{n_l/n_q} - 1} \\ & + \frac{2q\alpha}{3\epsilon_{GaN}} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{-\frac{1}{3}} + q^2 \left(\frac{1}{C_{GaN}} + \frac{1}{C_{AlN}} \right) \end{aligned} \quad (24)$$

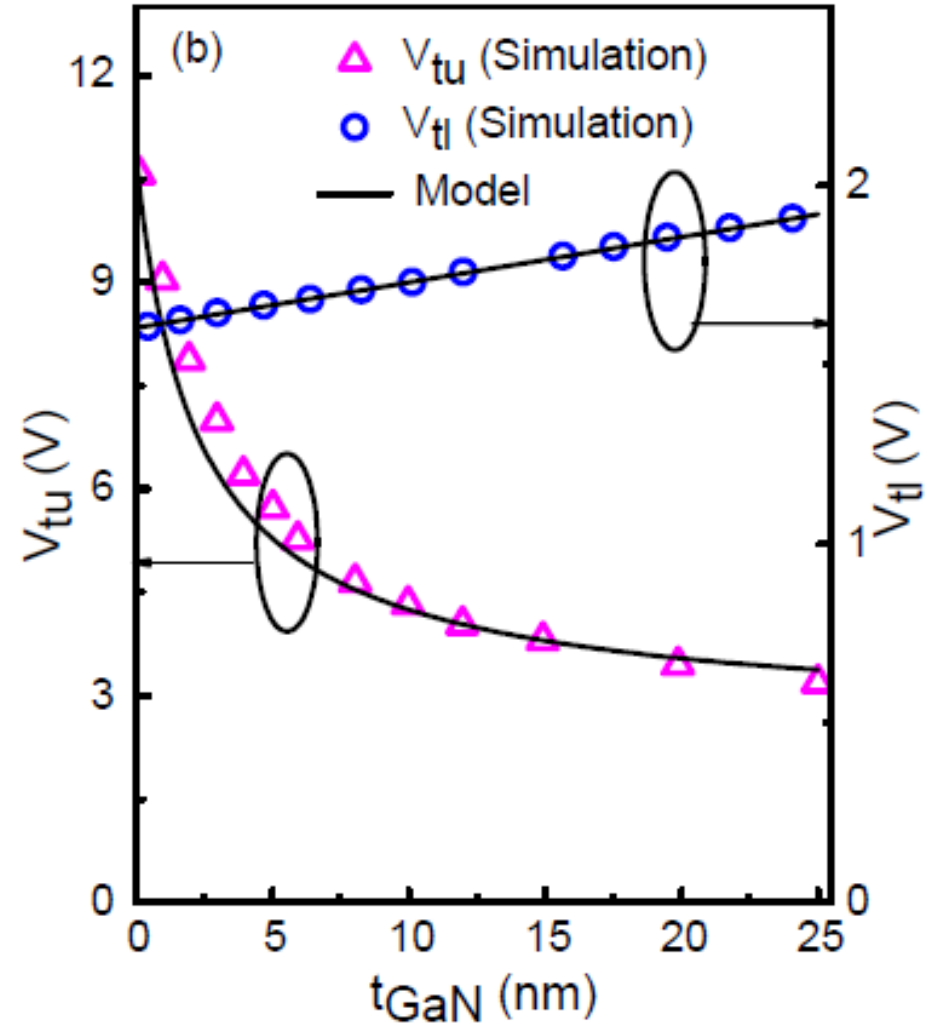
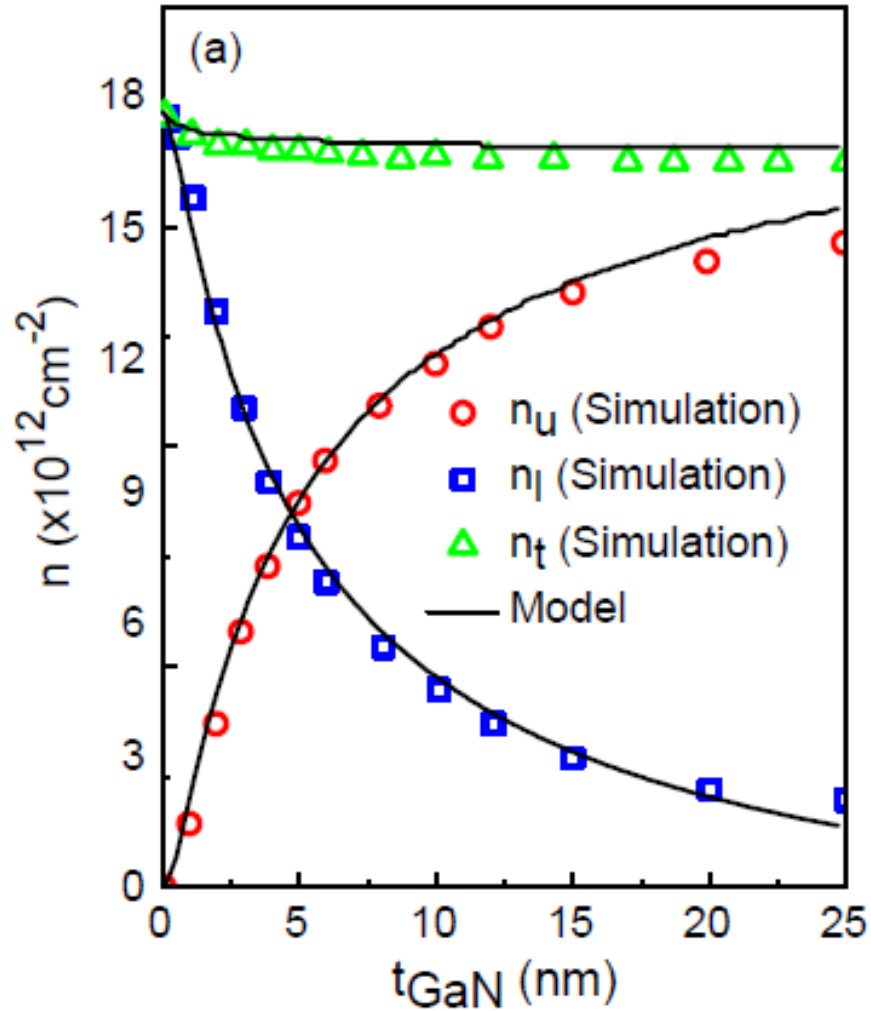
Final drift diffusion current

$$\begin{aligned} J = & \underbrace{-\frac{\mu_{nu}}{L} \frac{q^2}{C_{ox}} \int_{n_{u,s}}^{n_{u,d}} n_u dn_u}_{J_I} - \underbrace{\frac{\mu_{nl}}{L} q^2 \left(\frac{1}{C_{ox}} + \frac{1}{C_{GaN}} + \frac{1}{C_{AlN}} \right) \int_{n_{l,s}}^{n_{l,d}} n_l dn_l}_{J_{II}} - \underbrace{\frac{2\mu_{nl}q\alpha}{3\epsilon_{GaN}L} \int_{n_{l,s}}^{n_{l,d}} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{-\frac{1}{3}} n_l dn_l}_{J_{III}} \\ & - \underbrace{\frac{\mu_{nu}}{L} \frac{kT}{n_q} \int_{n_{u,s}}^{n_{u,d}} \left(\frac{e^{n_u/n_q}}{e^{n_u/n_q} - 1} \right) n_u dn_u}_{J_{IV}} - \underbrace{\frac{\mu_{nl}}{L} \frac{kT}{n_q} \int_{n_{l,s}}^{n_{l,d}} \left(\frac{e^{n_l/n_q}}{e^{n_l/n_q} - 1} \right) n_l dn_l}_{J_V} \\ & - \underbrace{\frac{\mu_{nl}}{L} \frac{q^2}{C_{ox}} \int_{n_{u,s}}^{n_{u,d}} n_l dn_u}_{J_{VI}} - \underbrace{\frac{\mu_{nu}}{L} \frac{q^2}{C_{ox}} \int_{n_{l,s}}^{n_{l,d}} n_u dn_l}_{J_{VII}} - \underbrace{\frac{2\mu_{nu}q\alpha}{3\epsilon_{GaN}L} \int_{n_{l,s}}^{n_{l,d}} \left(\frac{qn_l + qn_{buf}}{\epsilon_{GaN}} \right)^{-\frac{1}{3}} n_u dn_l}_{J_{VIII}} \end{aligned} \quad (25)$$

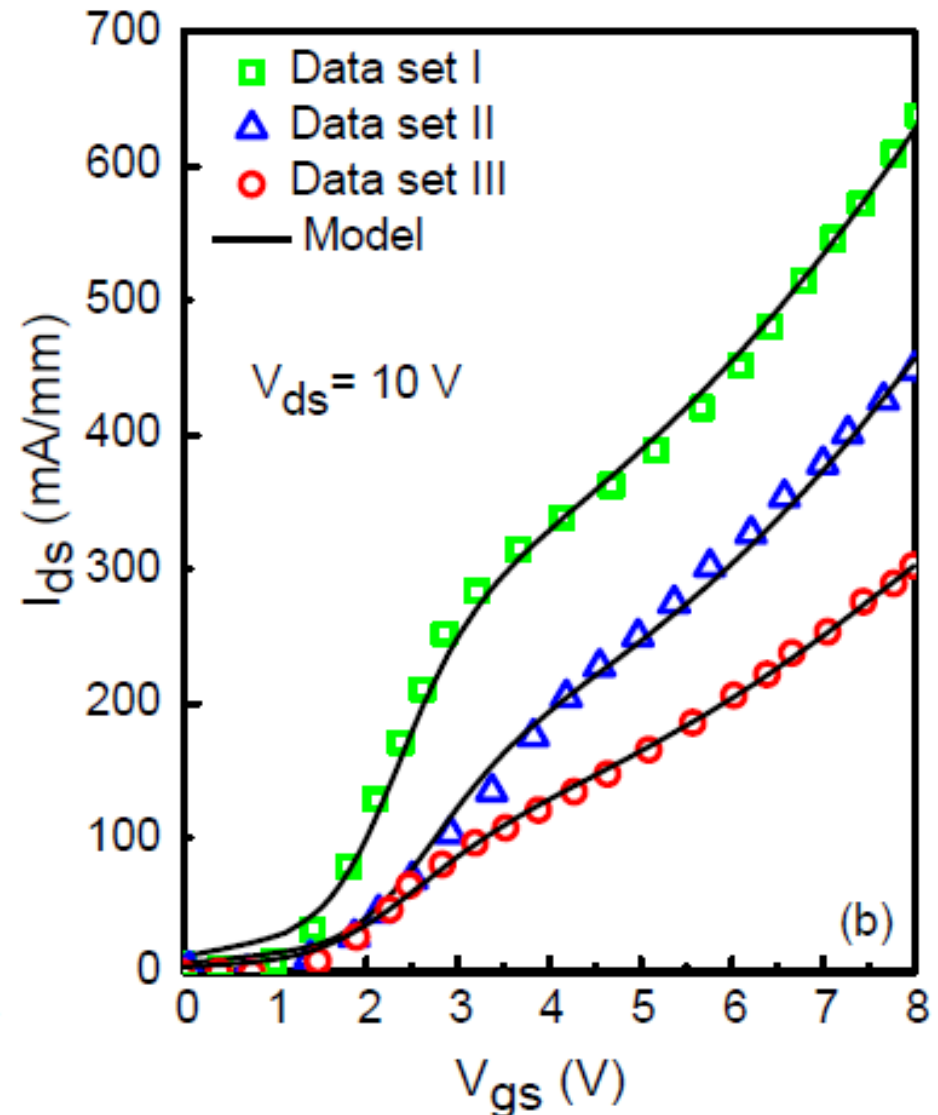
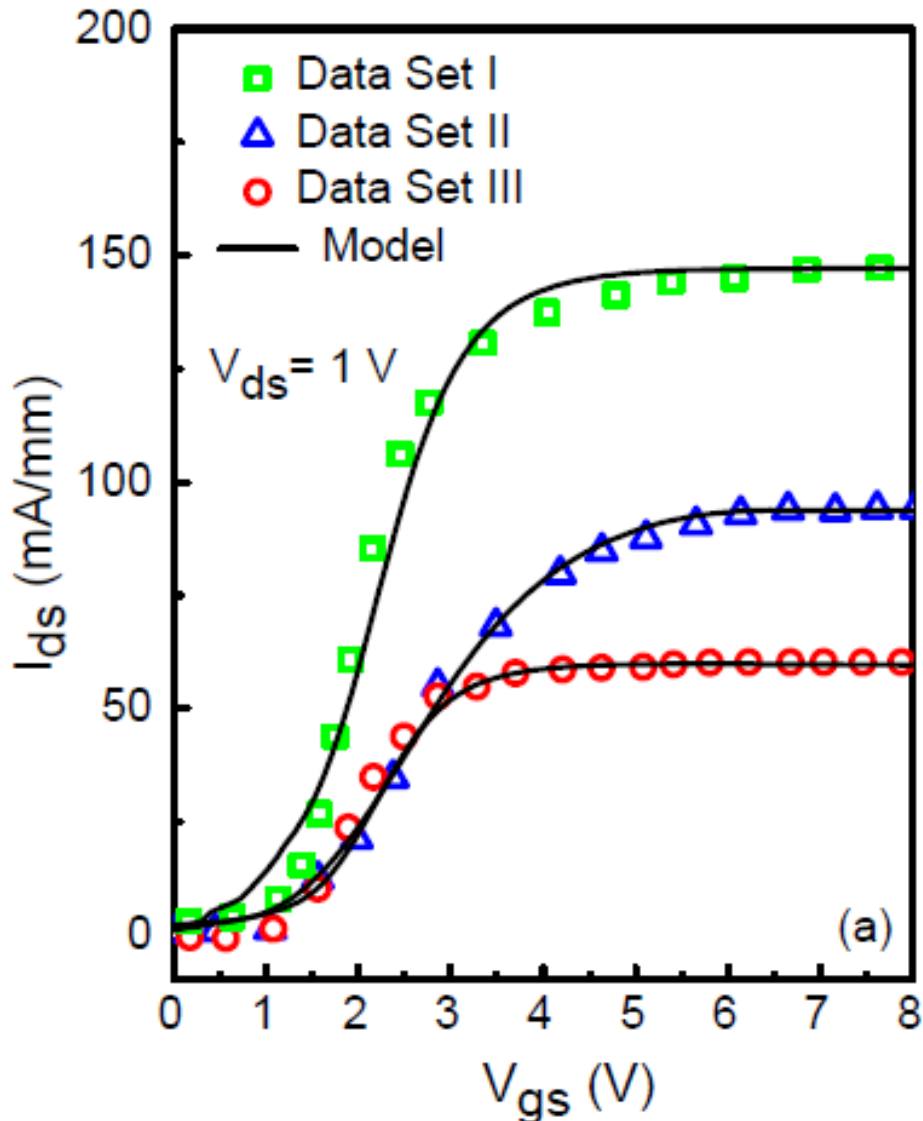
Validation against TCAD



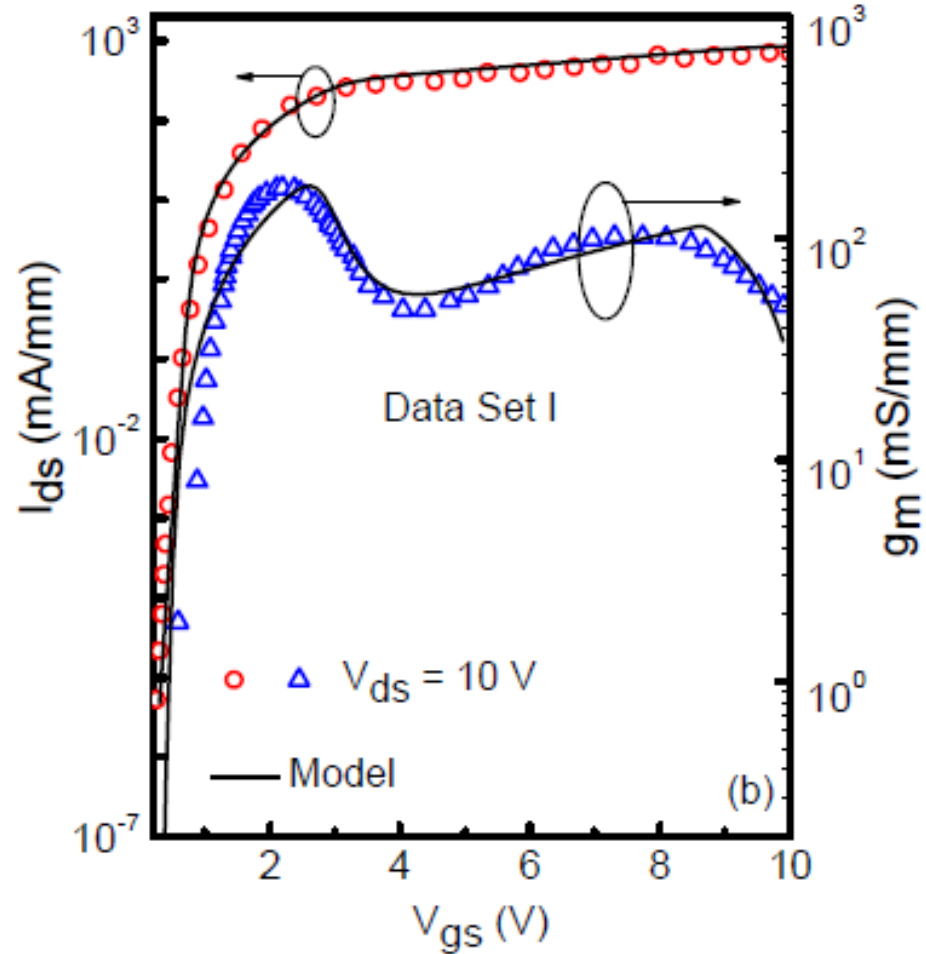
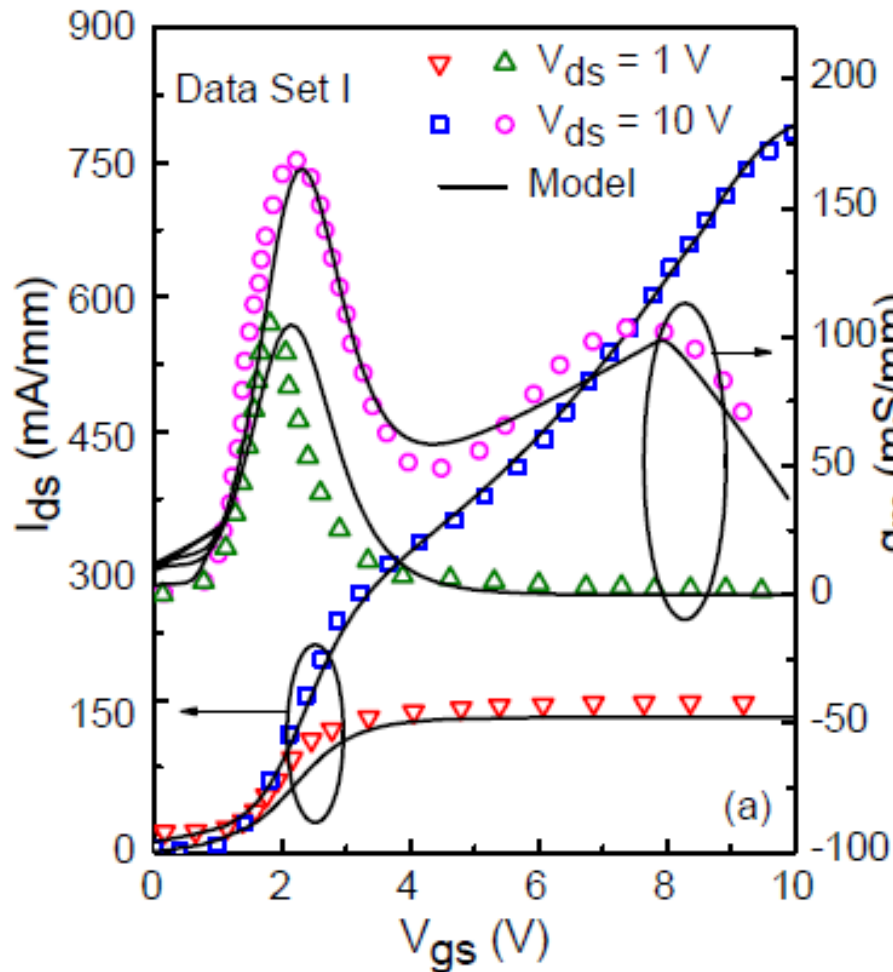
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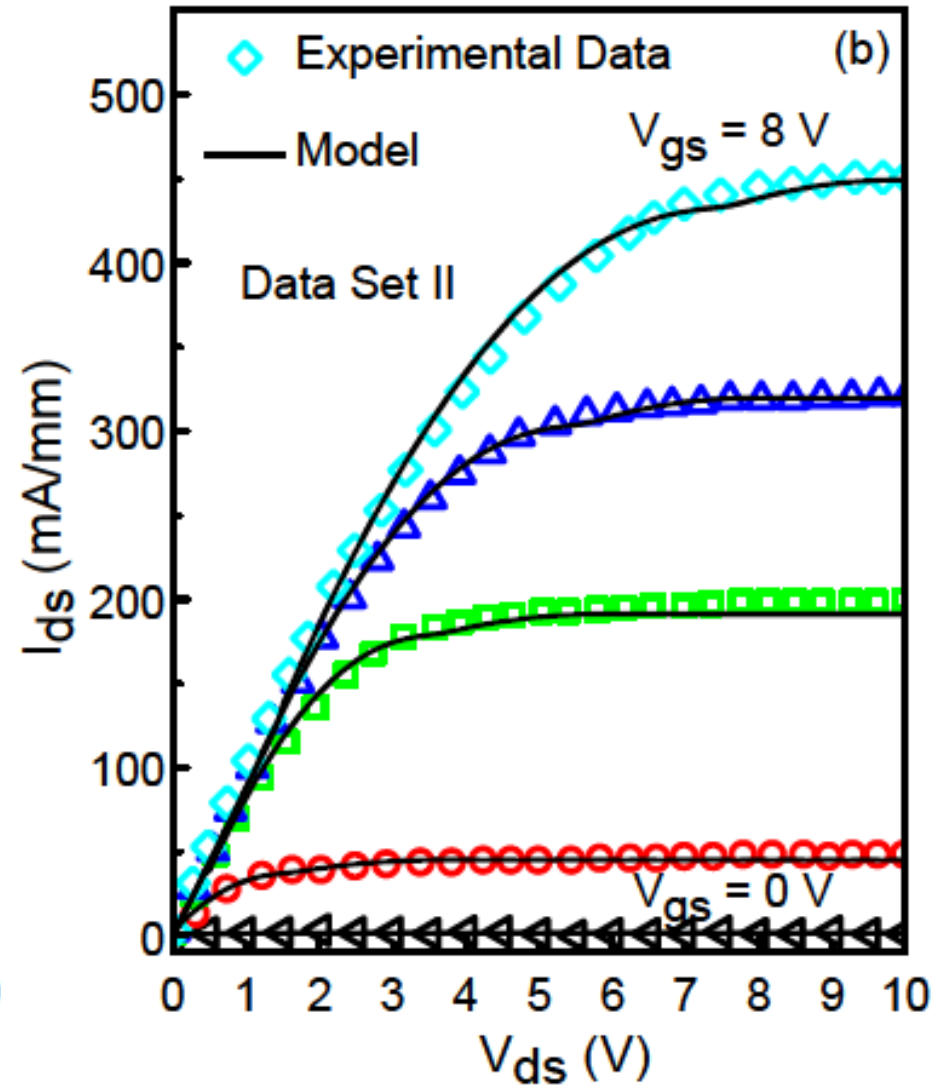
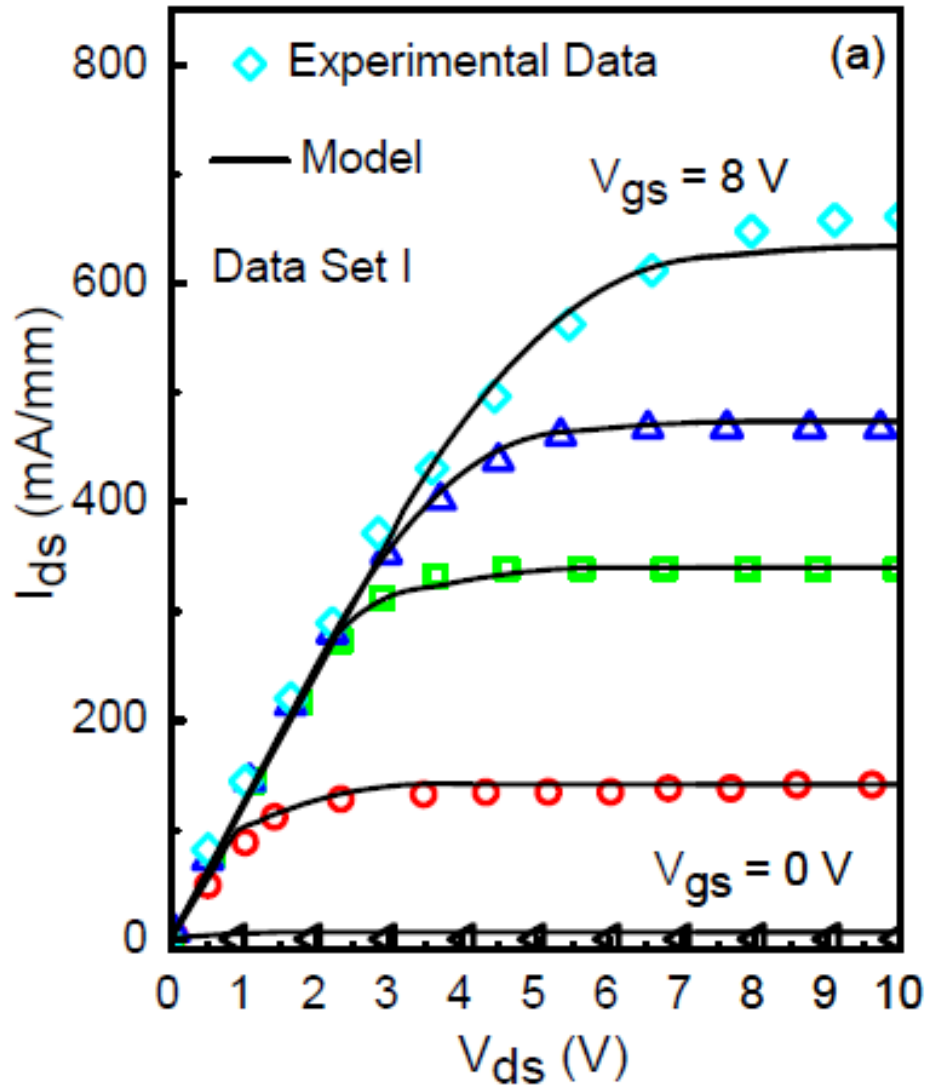
Validation against experimental



Validation against experimental



Validation against experimental



Conclusion

- A physics-based compact model for double channel GaN HEMTs was presented
- The model is analytical
- Includes the essential physics of 2D density of states, double-channel electrostatics
- Fits TCAD and experimental data reported in literature

Thank You!