

# Mysteries of a Variable Star:

## $\beta$ Cas, a Time-series Spectroscopical Analysis

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# Beta Cas

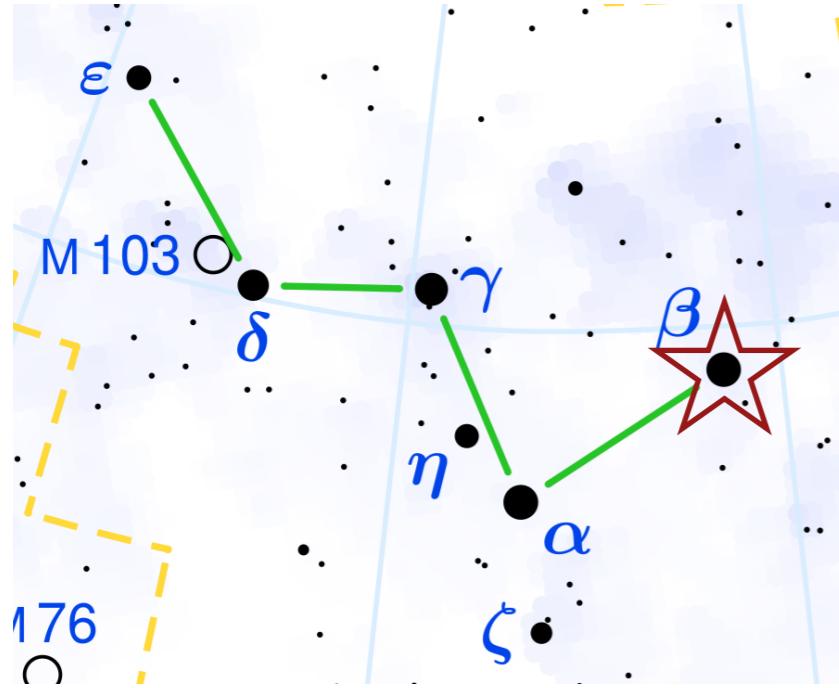


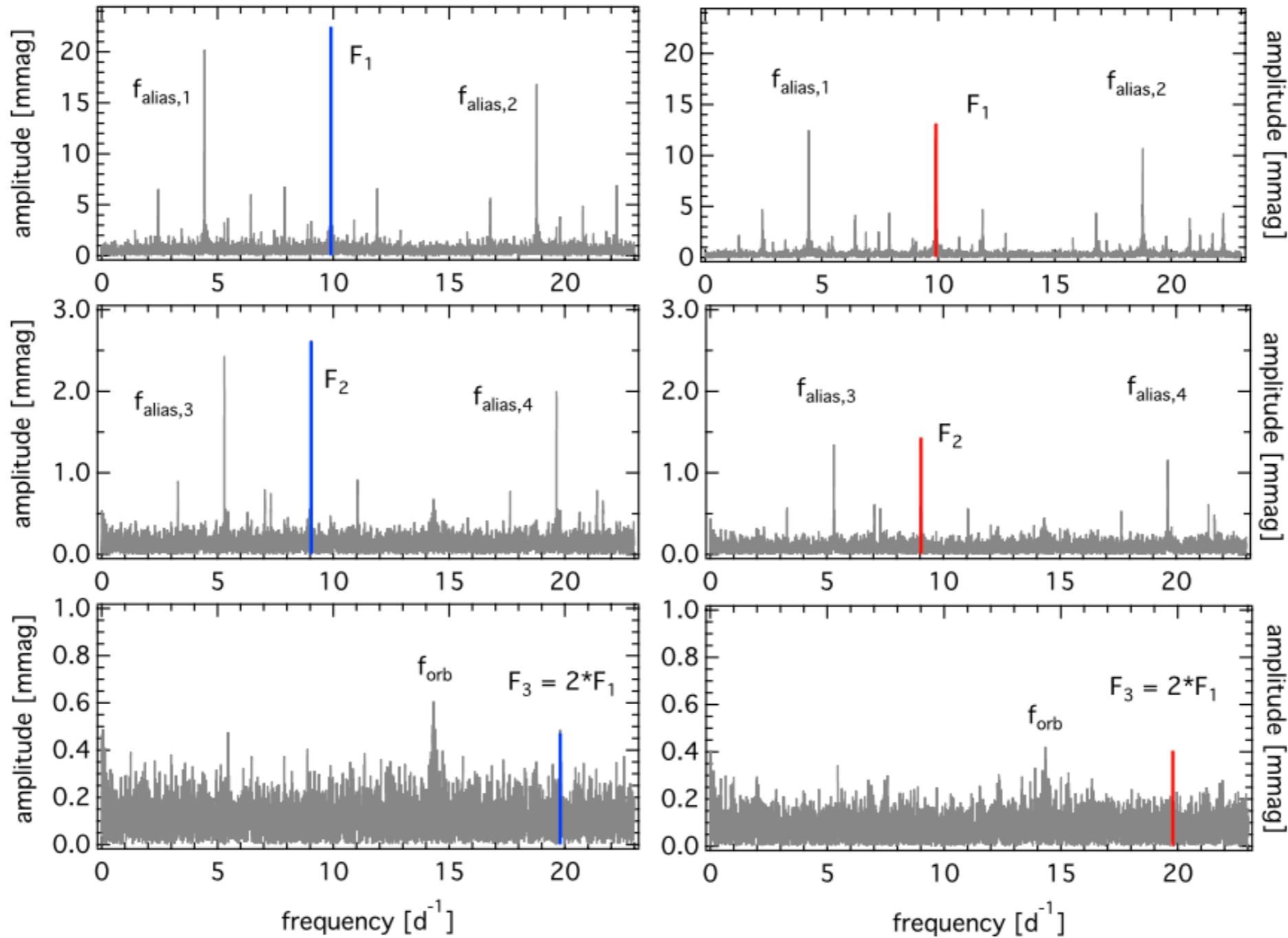
Fig. 1: Cassiopeia constellation

- Spectral type: F2 (end of main sequence lifetime);
- Retired main sequence A type star;
- Initially: monoperiodic pulsator;
- Extremely fast rotator: 92% of critical speed

Parameter	err <sub>1</sub>	err <sub>2</sub>	Che et al. (2011)		Gray et al. (2003)
			Model 1	Model 2	
$T_{\text{eff}}$ [K]	6920	35	140	6825	6897
$\log g$ [dex]	3.53	0.16	0.58	3.57	3.59
[M/H]	-0.11	0.04	0.12		-0.02
$v_{\text{e}} \sin i$ [km s <sup>-1</sup> ]	73.6	8.1	7.0	72.4	79.8
$v_{\text{mic}}$ [km s <sup>-1</sup> ]	4.1	0.4	0.5		3.1

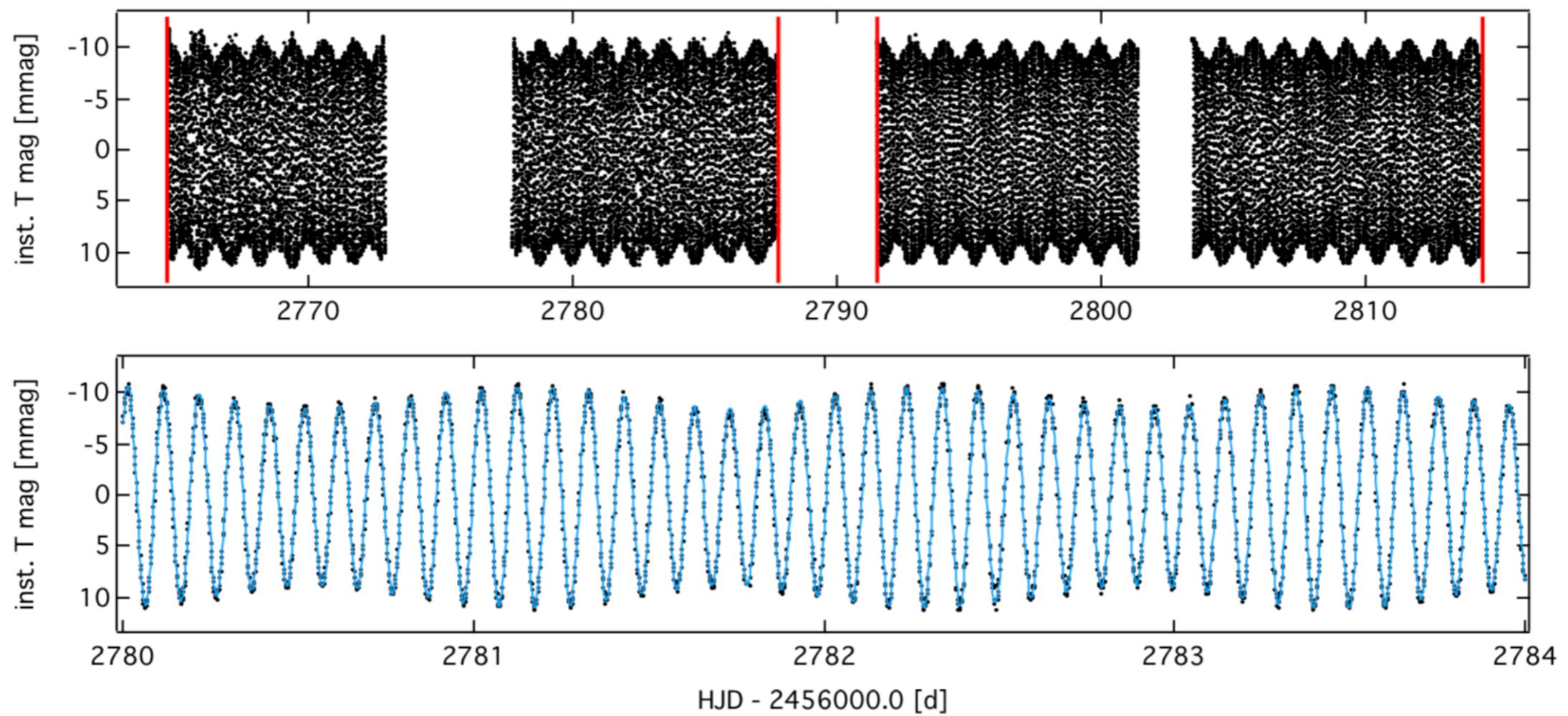
Fig. 2: Beta Cas stellar parameters, Zwintz et al., 2020

# Beta Cas



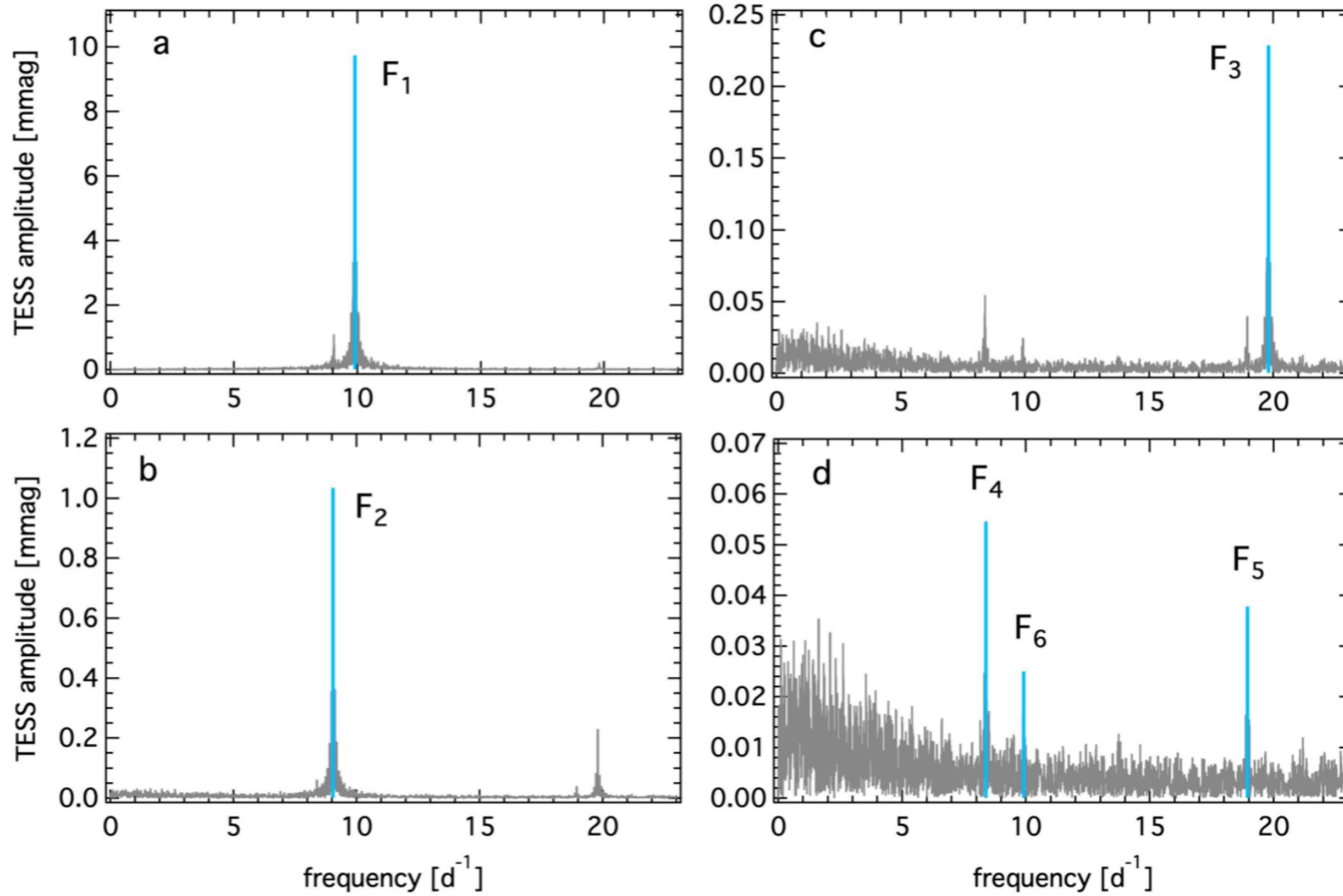
**Fig. 3:** BRITE frequencies of Beta Cas, Zwintz et al., 2020

# Beta Cas



**Fig. 4:** TESS light curve of Beta Cas, Zwintz et al., 2020

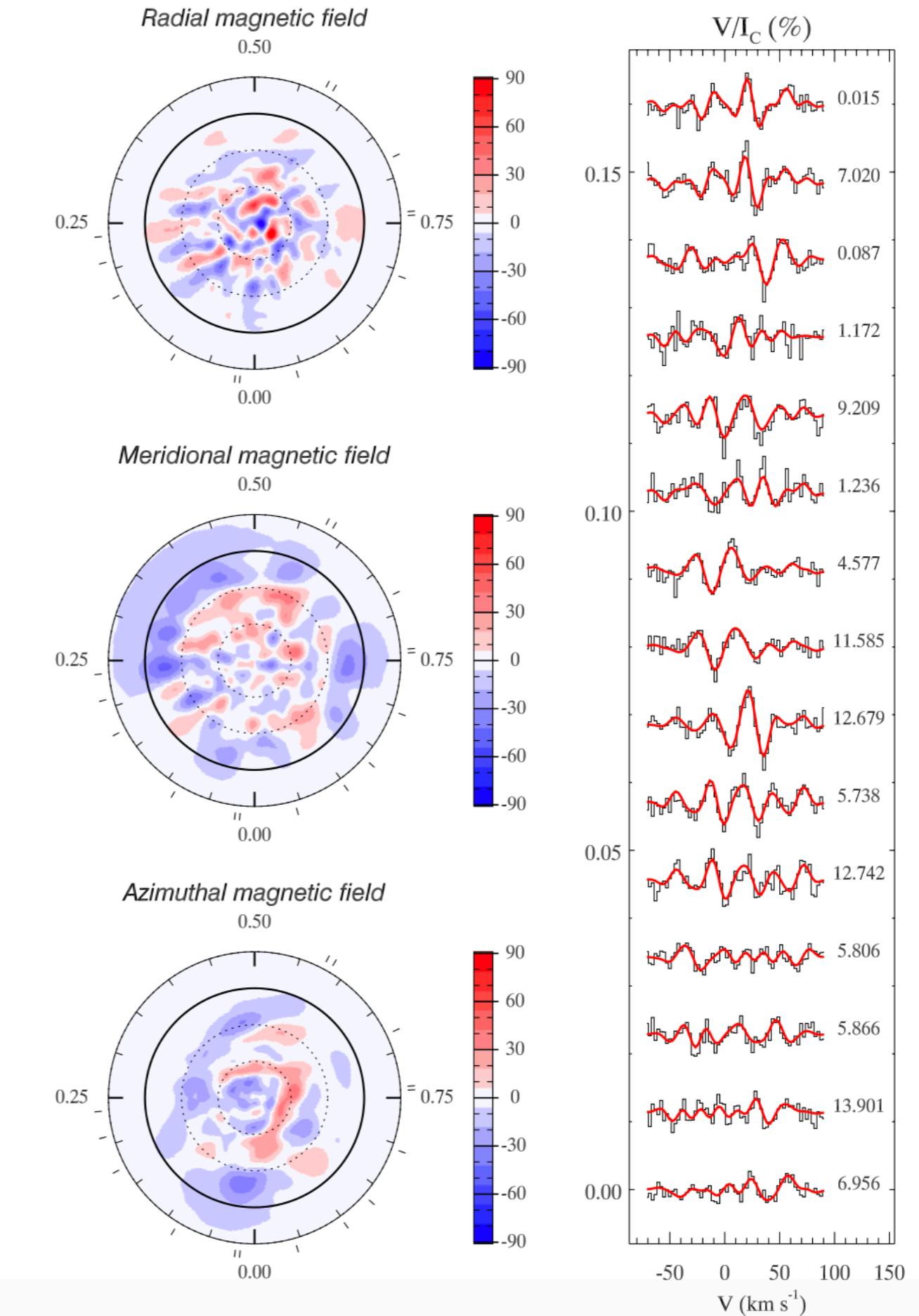
# Beta Cas



**Fig. 5:** TESS frequencies of Beta Cas, Zwintz et al., 2020

# Beta Cas

- Data obtained through the BRITE spectropolarimetry survey;
- Zeeman-Doppler Imaging technique, on data from Narval;
- Poloidal magnetic field (65% of the energy is in poloidal modes);
- Rotational period: 0.868 d.



# SONG observations

- SONG telescope @ Tenerife  
(Proposal by Beck, Zwintz et al. 2018)
- 497 spectra obtained from Nov. 16th to Nov. 30, 2018
- Total time base: 15 days;
- Range of observations: 4350 Å to 6850 Å.



# Spectroscopical Point of View

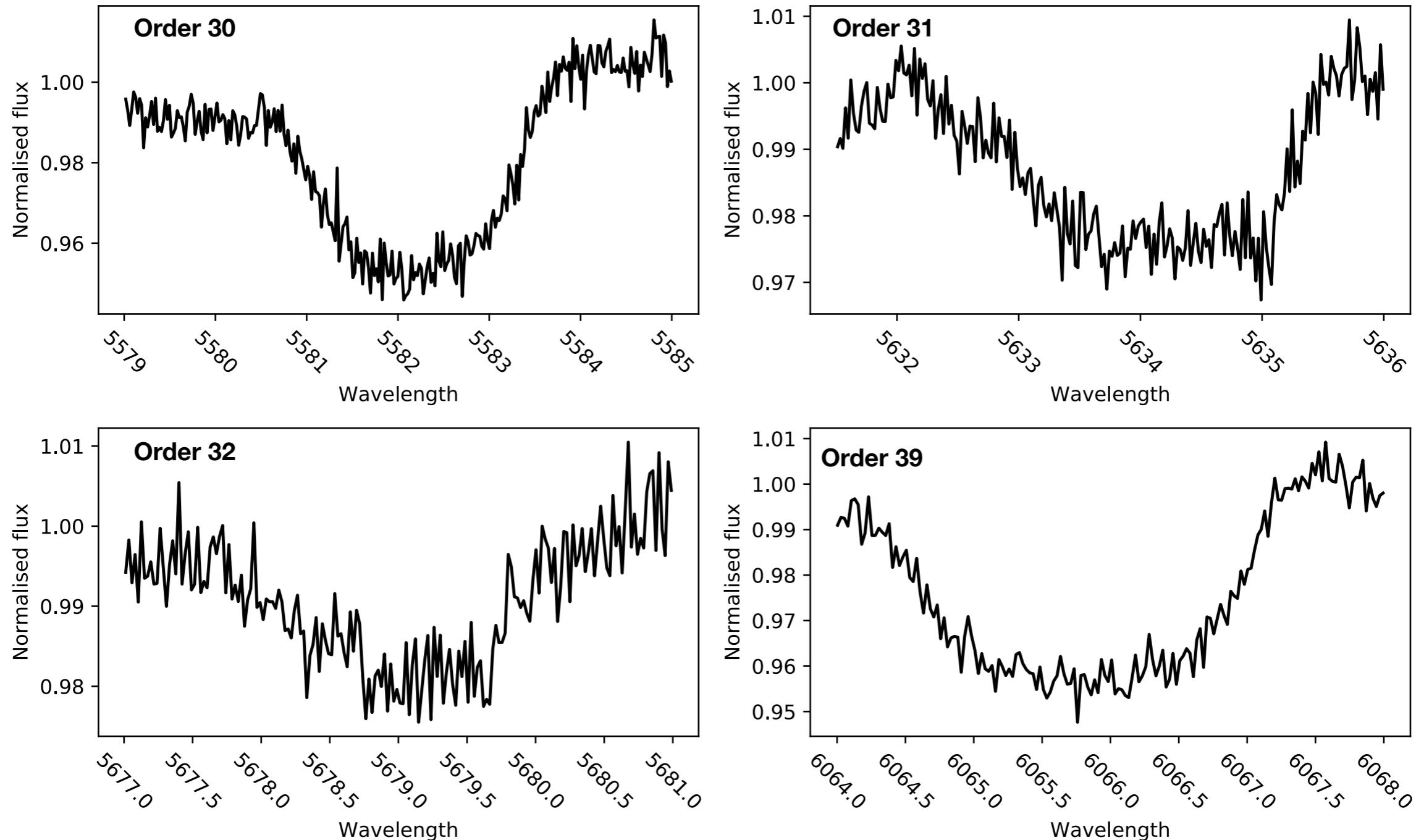
Mode ID, ideal scenario:

- Deep, narrow lines;
- Unblended lines, but no H or He;
- SNR > 200;
- R > 40000.

Mode ID,  $\beta$  Cas scenario:

- Wide, shallow lines;
- Unblended Ca I & Fe I;
- SNR > 200;
- R > 40000.

# Spectroscopical Point of View



**Fig. 7:** Cut-out spectral lines

# FAMIAS Analysis

- Search for periodicities: Fourier Parameter Fit method (Zima, 2006) and Moment method (Aerts & Briquet, 2003);
- FPF - moderate to fast rotators ( $v\sin i > 40 \text{ kms}^{-1}$ );
- MM - slow rotators ( $v\sin i < 40 \text{ kms}^{-1}$ );
- Frequencies are taken into account ONLY if the  $\text{SNR} > 4$ , for each of the found peaks (3.5 for harmonics or combinations);
- The found prominent frequency peaks will then be subjected to a LSF algorithm, which allows the improvement of amplitude, phase and, for the line profiles, the frequency, as well.

# FAMIAS Analysis - MM

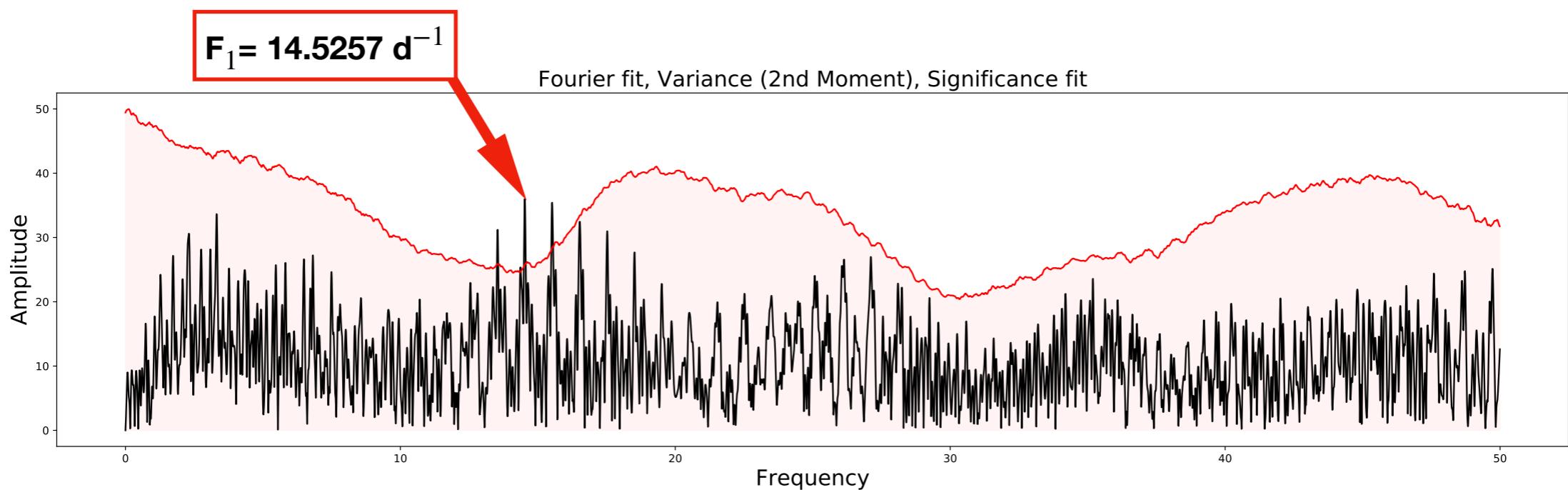
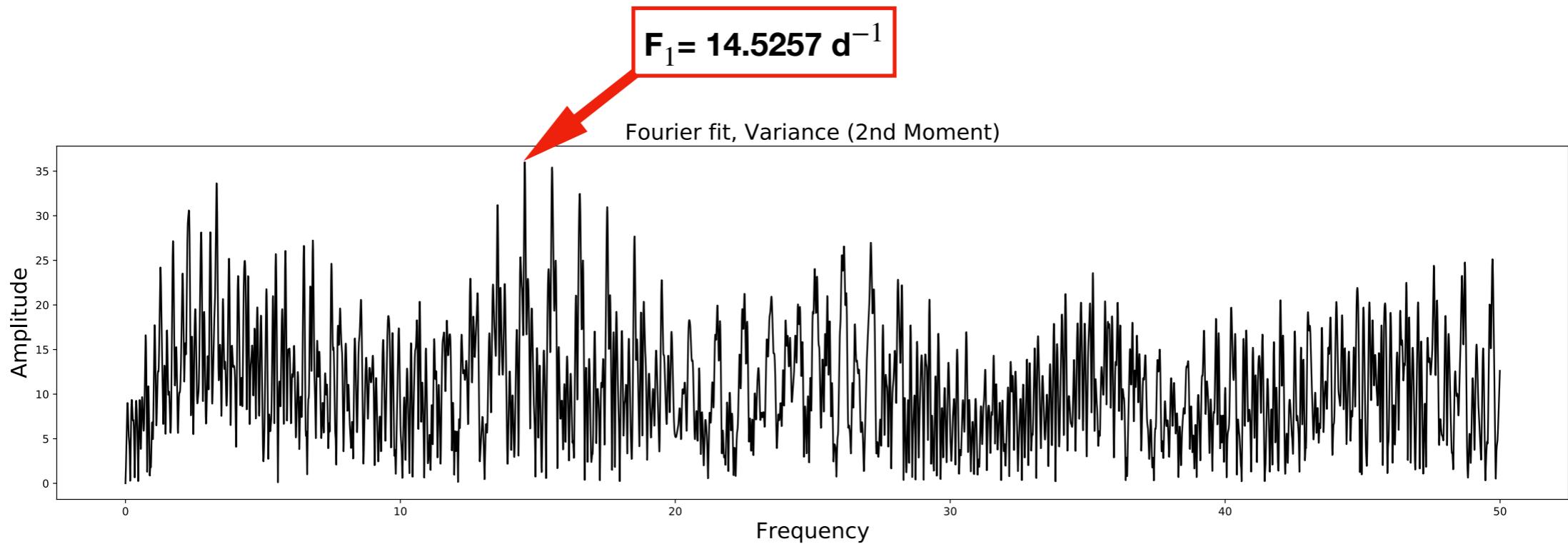


Fig. 8&9: Line moments Fourier fit, order 32

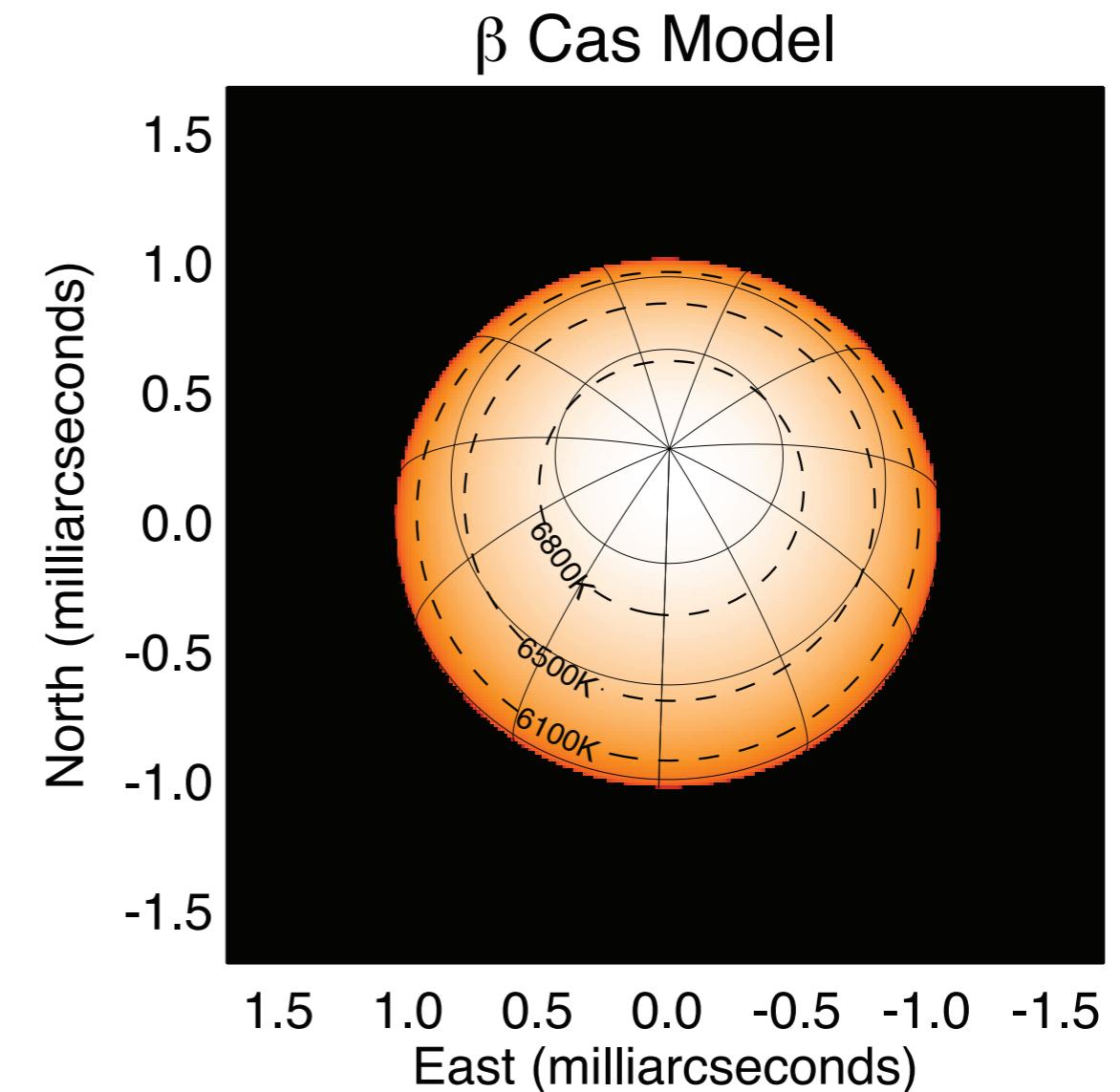
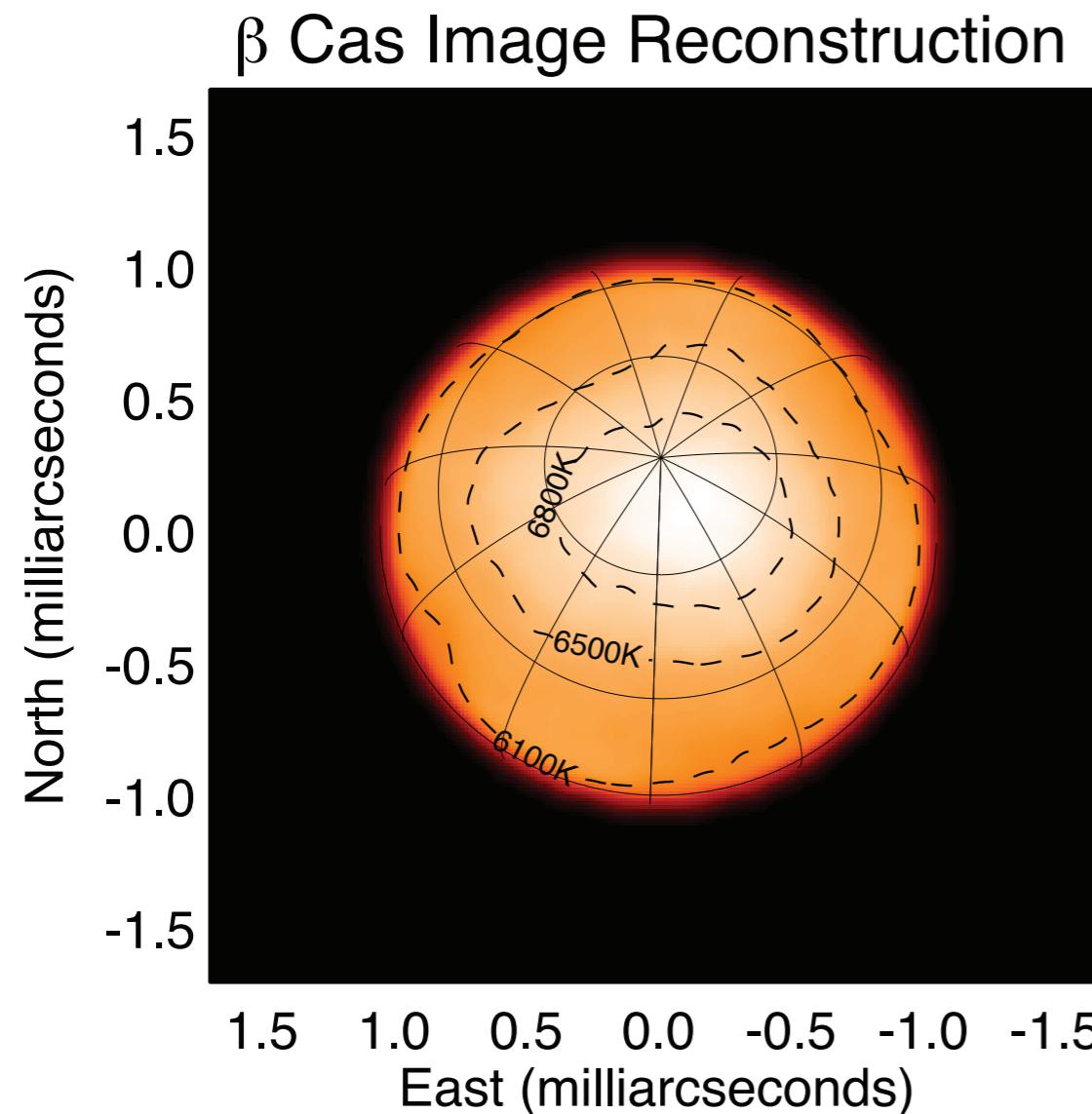
# FAMIAS Analysis - Mode ID

Line	Frequency		m
Ca I ( $\lambda_c = 5581,965\text{\AA}$ )	$16.5026\text{d}^{-1}$	0,1,2,3	-2,-1,0,3
Fe I ( $\lambda_c = 5579,023\text{\AA}$ )	$38.9769\text{d}^{-1}$	0,1,2,3	[-3,3]
Fe I ( $\lambda_c = 5579,023\text{\AA}$ )	$14.5257^*\text{d}^{-1}$	0,1,2,3	[-3,3]
Fe I ( $\lambda_c = 6065,48\text{\AA}$ )	-	-	-

# FAMIAS Analysis - Conclusions

- Che et al. (2011) determined the inclination angle of  $\beta$  Cas as  $19.9^{+1.9}_{-1.9}$  degrees;
  - Beta Cas is seen nearly pole-on;
  - Rotational broadening complicates spectroscopic analysis of pulsation frequencies;
  - A longer data set might expose more of the star's behaviour (?).

# FAMIAS Analysis - Conclusions



**Fig. 10:** Beta Cas, interferometry imaging (Che et al., 2011)

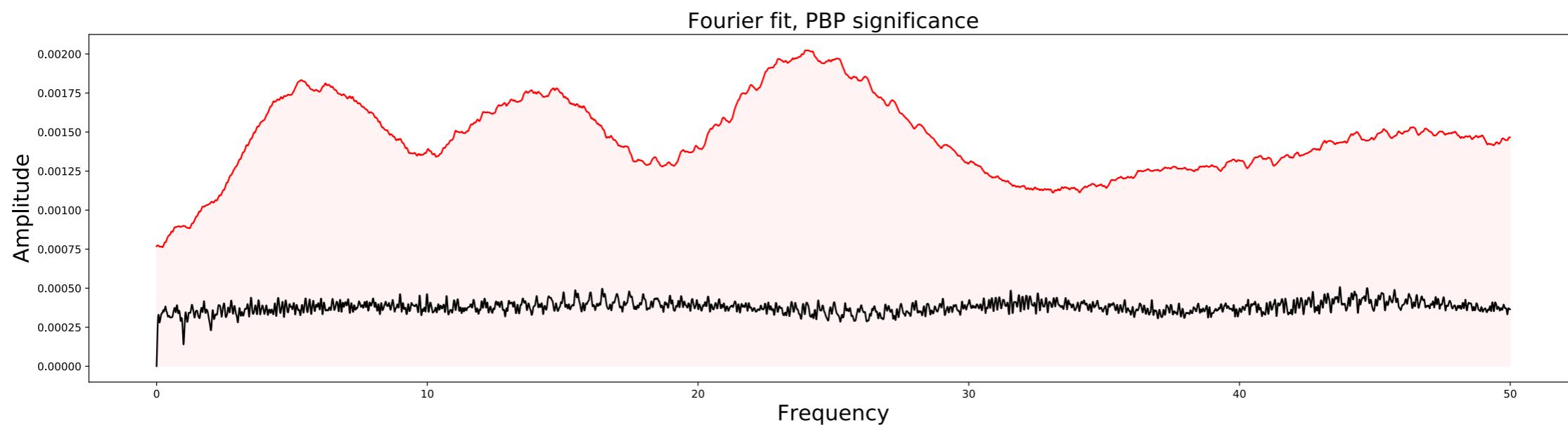
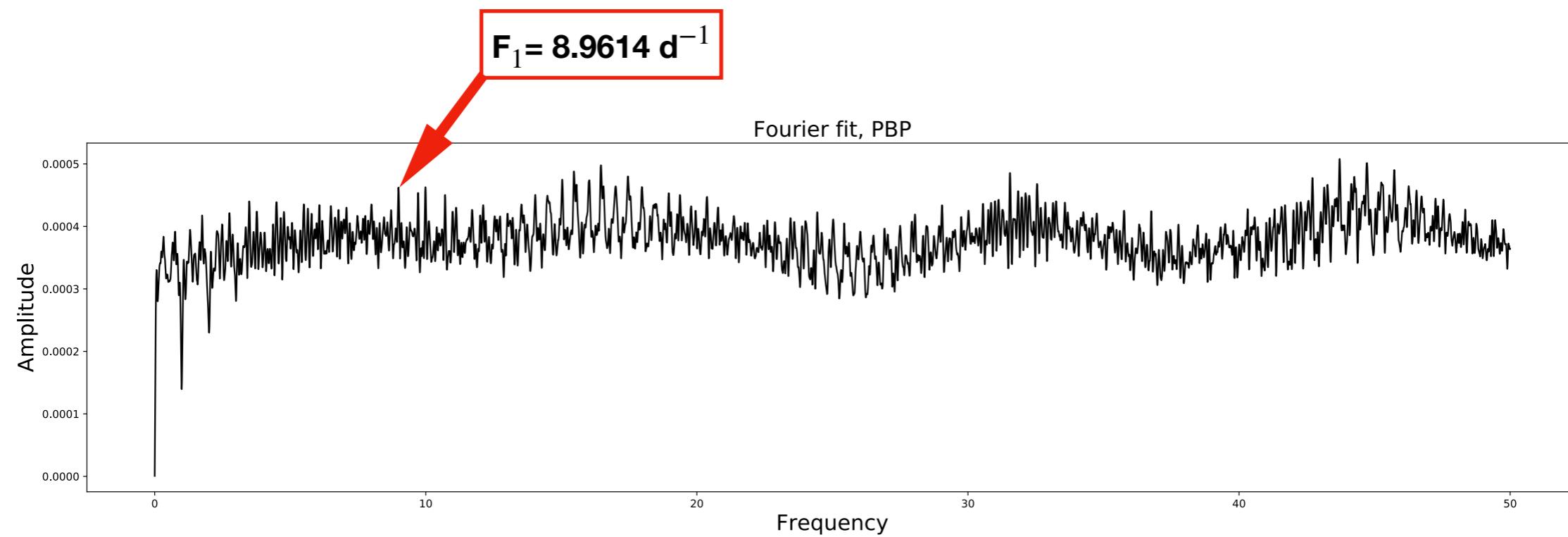
# Thank you!



# FAMIAS Analysis - FPF

- Computes the intensity of each wavelength bin across the line profile;
- No upper limit for mode ID;
- Fit done with synthetic line profiles;
- Computes the “goodness of fit” through a  $\chi^2$  statistical test;
- Relies on the pixel-by-pixel method.

# FAMIAS Analysis - FPF



**Fig. 8&9:** Pixel-by-pixel Fourier fit, order 32

# FAMIAS Analysis - MM

- Better suited for slower rotating stars;
- Uses a discriminant, computing the mode ID using information from the 1st (radial velocity) and 2nd (line width) line moments;
- The MM fitting in FAMIAS is done using existing theoretical models;
- Uses a  $\chi^2$  fit to determine the significance of the mode ID.

# FAMIAS Analysis - MM

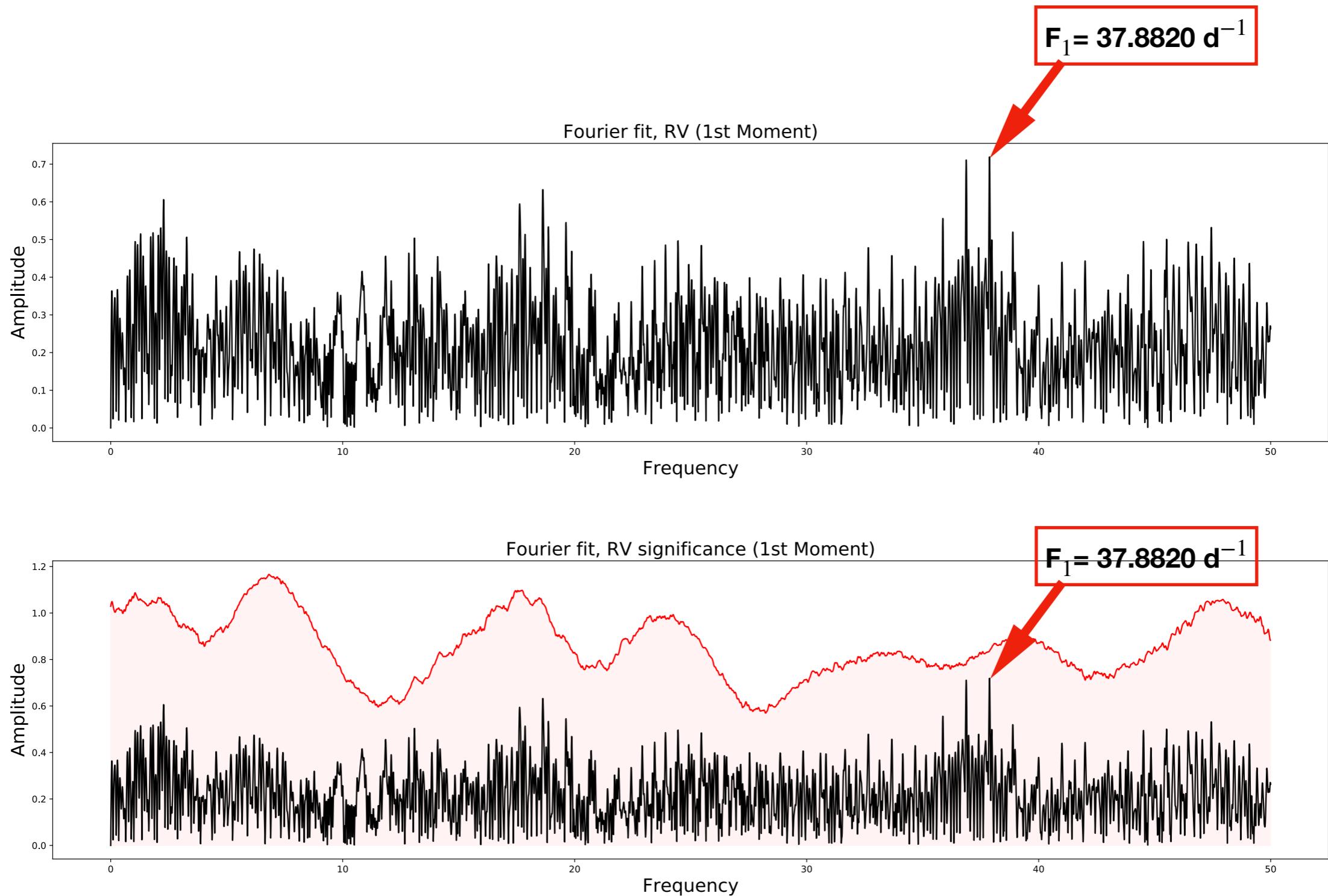
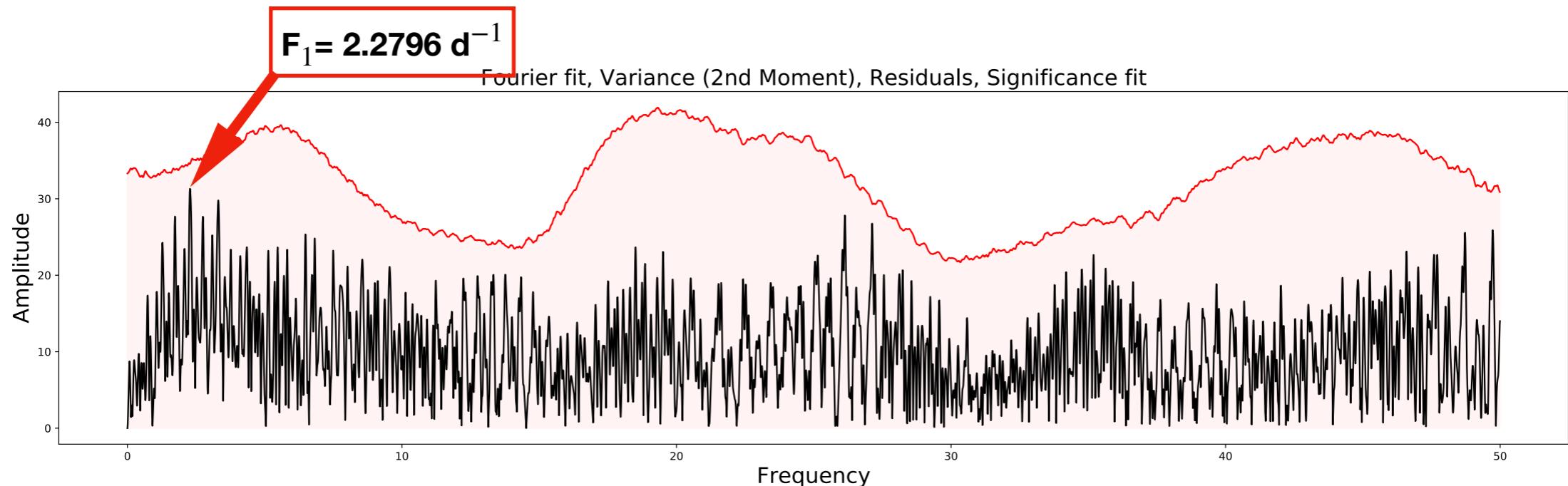
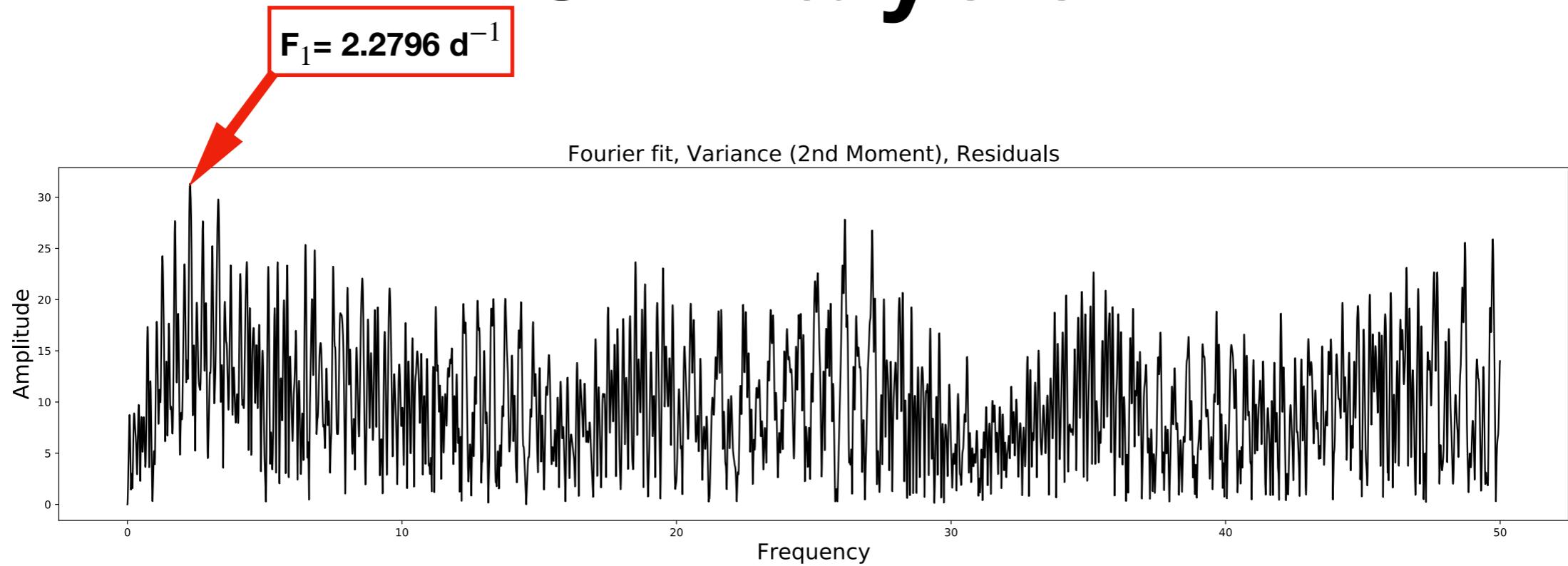


Fig. 10&11: Line moments Fourier fit, order 32

# FAMIAS Analysis - MM



**Fig. 14&15:** Line moments residual data set, Fourier fit, order 32

# FAMIAS Analysis

Order	Line Element	FPF (PBP) Analysis	Significant frequencies	Insignificant frequencies	MM (LPV) Analysis	Significant* frequencies	Insignificant frequencies
30	Ca I	yes	none	yes	yes	$16.5026d^{-1}$ $38.9769d^{-1}$	yes
31	Fe I	yes	none	yes	yes	none	yes
32	Fe I	yes	none	$8.9614d^{-1}$	yes	$14.5257d^{-1}$	yes
39	Fe I	yes	none	yes	none	none	yes

\* - the frequency is, first of all, significant when it comes to its SNR(> 3.5) and discovered in the 1st or 2nd line moment.