



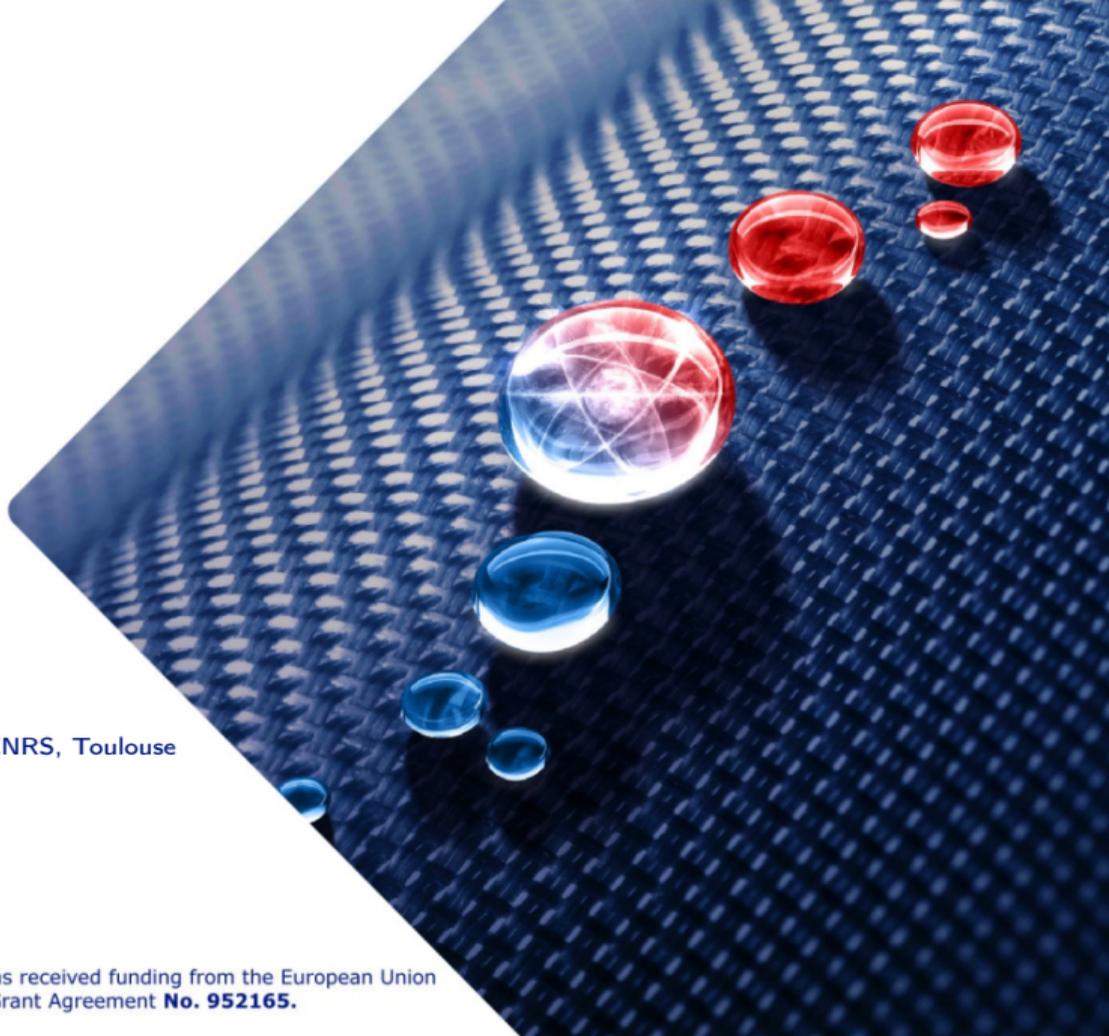
Targeting Real chemical accuracy at the EXascale

Library development within TREX

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21/04/2021

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(France)



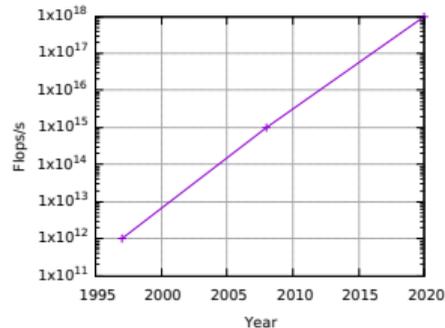
Targeting Real Chemical Accuracy at the Exascale project has received funding from the European Union Horizon 2020 research and innovation programme under Grant Agreement No. 952165.



Presentation of TREX

Worldwide technological competition

- 1997 : Teraflops/s¹
- 2008 : Petaflops/s
- 2020? : Exaflops/s



- Expected increase of computational power is *exponential*
- Moore's Law is ending
- Technological breakthrough needed (quantum computing?)

¹flops/s: floating point operations per second

Worldwide technological competition

- 1997 : Terascale : Distributed parallelism
- 2008 : Petascale : Multi-core chips or accelerators
- 2020? : Exascale : Hybrid architectures are inevitable

Peak flops/s improved by $1000\times$. What about

- Memory capacity per core?
- Memory bandwidth? latency?
- I/O bandwidth? latency?
- Network bandwidth? latency?

Transition to exascale will be painful

- Network becomes slow vs computation
- Memory per core decreases
- Heterogeneous machines (accelerators)
- Need to find even more fine-grained parallelism

Very few applications will scale

- Exascale machines will run high throughput computing (HTC) workloads

HORIZON
2020

Targeting Real chemical accuracy at the EXascale

Fact Sheet

[News & Multimedia](#)

Project description

Complex quantum molecular simulations of unprecedented speed and accuracy

Computers and the rapid mathematical calculations they are able to perform, which would take human beings years to accomplish, have provided the fuel to power innovation. High-performance computing (HPC) and high-throughput computing (HTC) have enabled us to simulate large-scale complex processes and analyse tremendous amounts of data, benefitting applications ranging from climate research and drug discovery to material design. Emerging exascale computers will make the best even better, 50 times faster than today's most powerful supercomputers. The EU-funded TREX project is developing a platform that combines the upcoming exascale HPC and HTC architectures for stochastic quantum chemical simulations of unprecedented accuracy. The software and services will be designed for ease of use to ensure widespread utilisation, spurring a new age of discovery in molecular simulations.

[Hide the project objective](#)

Project Information

TREX

Grant agreement ID: 952165

Status

Ongoing project

Start date

1 October 2020

End date

30 September 2023

Funded under

H2020-EU.1.4.1.3.

Overall budget

€ 4 998 847,50

EU contribution

€ 4 998 847,50

Coordinated by

UNIVERSITEIT TWENTE

Netherlands



QMC

- Extremely precise model
- Expensive in CPU
- Fully parallel
- Perfectly well adapted to HPC (in 2011, 0.96 PFlops/s)

Journal of COMPUTATIONAL CHEMISTRY

WWW.CHEMSONLINE

FULL PAPER

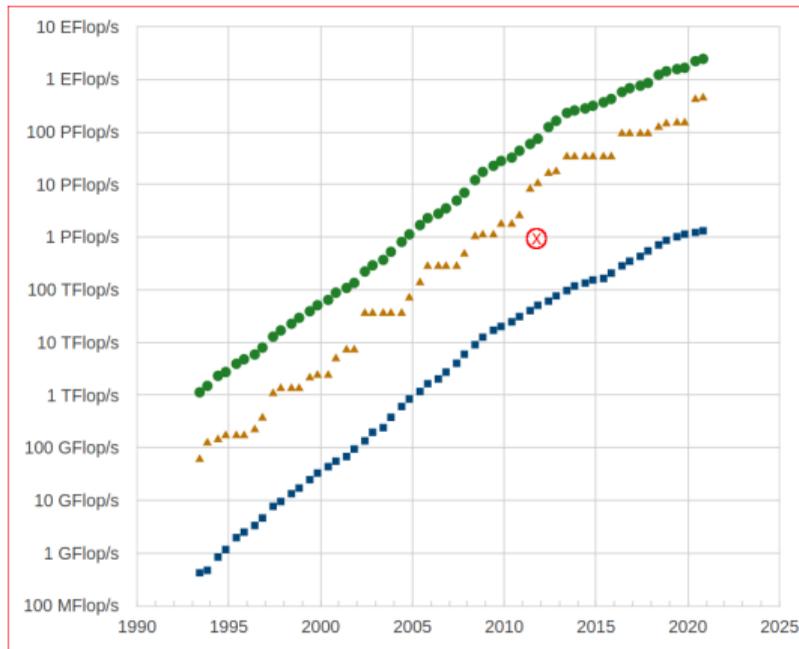
Quantum Monte Carlo for Large Chemical Systems: Implementing Efficient Strategies for Petascale Platforms and Beyond

Anthony Scemama,^{a[a]} Michel Caffarel,^[a] Emmanuel Oseret,^[b] and William Jalby^[b]

Various strategies to implement efficiently quantum Monte Carlo (QMC) simulations for large chemical systems are presented. These include: (i) the introduction of an efficient algorithm to calculate the computationally expensive Slater matrices. This novel scheme is based on the use of the highly localized character of atomic Gaussian basis functions (not the molecular orbitals as usually done), (ii) the possibility of keeping the memory footprint minimal, (iii) the important enhancement of single-core performance when efficient optimization tools are used, and (iv) the definition of a universal, dynamic, fault-tolerant, and load-balanced framework adapted to all kinds of computational platforms (massively parallel machines, clusters, or distributed grids).

These strategies have been implemented in the QMC-Chem code developed at Toulouse and illustrated with numerical applications on small peptides of increasing sizes (158, 434, 1056, and 1731 electrons). Using 10–80 k computing cores of the Curie machine (GENCI-TGCC-CEA, France), QMC-Chem has been shown to be capable of running at the petascale level, thus demonstrating that for this machine a large part of the peak performance can be achieved. Implementation of large-scale QMC simulations for future exascale platforms with a comparable level of efficiency is expected to be feasible. © 2013 Wiley Periodicals, Inc.

DOI: 10.1002/jcc.23216



Stochastic solution of the electronic Schrödinger equation (nuclei are fixed):

$$\begin{aligned}
 E &= \frac{\langle \Phi | \hat{H} | \Phi \rangle}{\langle \Phi | \Phi \rangle} = \frac{\langle \Phi | \hat{H} | \Psi \rangle}{\langle \Phi | \Psi \rangle} = \frac{\int \Phi(r_1, \dots, r_N) \hat{H} \Psi(r_1, \dots, r_N) dr_1 \dots dr_N}{\int \Phi(r_1, \dots, r_N) \Psi(r_1, \dots, r_N) dr_1 \dots dr_N} \\
 &= \frac{\int [\Phi(r_1, \dots, r_N) \Psi(r_1, \dots, r_N)] \frac{\hat{H} \Psi(r_1, \dots, r_N)}{\Psi(r_1, \dots, r_N)} dr_1 \dots dr_N}{\int [\Phi(r_1, \dots, r_N) \Psi(r_1, \dots, r_N)] dr_1 \dots dr_N} \\
 &\sim \frac{1}{M} \sum_M \frac{\hat{H} \Psi(r_1, \dots, r_N)}{\Psi(r_1, \dots, r_N)}, \text{ sampled with } (\Psi \times \Phi)
 \end{aligned}$$

\hat{H} : Hamiltonian
 E : Energy

r_1, \dots, r_N : Electron coordinates
 Φ : Quasi-exact (fixed-node) wave function
 Ψ : Trial wave function

In practice

- Walker: vector $(r_1, \dots, r_N) \in \mathbb{R}^{3N}$ of electron coordinates
- Diffusion + drift with a birth/death process to sample the 3N-dimensional density $(\Psi \times \Phi)$
- At each step, $E_{\text{loc}}(r_1, \dots, r_N) = \frac{\hat{H}\Psi(r_1, \dots, r_N)}{\Psi(r_1, \dots, r_N)}$ is computed
- The total energy is the the average of all the computed E_{loc}

HPC

- Very low memory requirements (no integrals)
- Distribute walkers on different cores or compute nodes
- No blocking communication: near-ideal scaling
- Difficulty: parallelize within a QMC trajectory

Communication: Toward an improved control of the fixed-node error in quantum Monte Carlo: The case of the water molecule

Michel Caffarel,¹ Thomas Applencourt,¹ Emmanuel Giner,² and Anthony Scemama¹

¹Laboratoire de Chimie et Physique Quantique, CNRS-Université de Toulouse, Toulouse, France

²Dipartimento di Scienze Chimiche e Farmaceutiche, Università degli Studi di Ferrara, Ferrara, Italy

(Received 22 March 2016; accepted 6 April 2016; published online 20 April 2016)

All-electron Fixed-node Diffusion Monte Carlo calculations for the nonrelativistic ground-state energy of the water molecule at equilibrium geometry are presented. The determinantal part of the trial wavefunction is obtained from a selected Configuration Interaction calculation [Configuration Interaction using a Perturbative Selection done Iteratively (CIPSI) method] including up to about 1.4×10^6 of determinants. Calculations are made using the cc-pCVnZ family of basis sets, with $n = 2$ to 5. In contrast with most quantum Monte Carlo works no re-optimization of the determinantal part in presence of a Jastrow is performed. For the largest cc-pCV5Z basis set the lowest upper bound for the ground-state energy reported so far of $-76.43744(18)$ is obtained. The fixed-node energy is found to decrease regularly as a function of the cardinal number n and the Complete Basis Set limit associated with *exact nodes* is easily extracted. The resulting energy of $-76.43894(12)$ — in perfect agreement with the best experimentally derived value — is the most accurate theoretical estimate reported so far. We emphasize that employing selected configuration interaction nodes of increasing quality in a given family of basis sets may represent a simple, deterministic, reproducible, and systematic way of controlling the fixed-node error in diffusion Monte Carlo. *Published by AIP Publishing*. [<http://dx.doi.org/10.1063/1.4947093>]

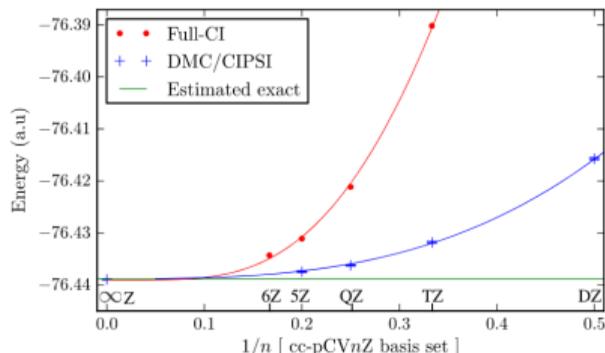


FIG. 1. CBS extrapolation of FCI and DMC/CIPSI energies. Error bars on DMC data are plotted but almost imperceptible.

- As $(\Psi \times \Phi)$ is a probability density, $(\Psi \times \Phi) \geq 0$ so Φ has the same sign as Ψ : fixed-node (FN) approximation.
- FN: only approximation of QMC. If the nodes of Ψ coincide with the exact nodes, we obtain the exact energy
- Using increasingly large sCI determinant expansions (CIPSI), the fixed-node error can be controlled



Partners



Codes

- CHAMP
- QMC=Chem
- TurboRVB
- NECI
- Quantum Package
- GammCor
- QML

- TREX CoE: Targeting REal chemical accuracy at the eXascale
- Started in Oct. 2020
- Objective: Make codes ready for exascale systems
- Two regimes:
 - Single exascale run
 - Thousands of petascale simulations in high-throughput (HTC)
- How: Instead of re-writing codes, provide libraries
 - One library for high-performance (QMCKI)
 - One library for exchanging information between codes (input of QMC is Ψ)

QMC kernel library (QMCKl)

- Progress in quantum chemistry may require codes with new ideas/algorithms
- New ideas/algorithms are implemented by physicists/chemists
- Different scientists have different programming language knowledge/preference
- Exascale machines will be horribly complex to program

Question

Is it reasonable to ask physicists/chemists to write codes for exascale machines?

(from <https://github.com/jeffhammond/dpcpp-tutorial>)

Vector addition

```
do i=1,n
  Z(i) = Z(i) + A * X(i) + Y(i)
end do
```

```
std::vector<float> h_X(length,xval);
std::vector<float> h_Y(length,yval);
std::vector<float> h_Z(length,zval);

try {

  sycl::queue q(sycl::default_selector{});

  const float A(aval);

  sycl::buffer<float,1> d_X { h_X.data(), sycl::range<1>(h_X.size()) };
  sycl::buffer<float,1> d_Y { h_Y.data(), sycl::range<1>(h_Y.size()) };
  sycl::buffer<float,1> d_Z { h_Z.data(), sycl::range<1>(h_Z.size()) };

  q.submit([&](sycl::handler& h) {

    auto X = d_X.template get_access<sycl::access::mode::read>(h);
    auto Y = d_Y.template get_access<sycl::access::mode::read>(h);
    auto Z = d_Z.template get_access<sycl::access::mode::read_write>(h);

    h.parallel_for<class nstream>( sycl::range<1>{length}, [=] (sycl::id<1> it) {
      const int i = it[0];
      Z[i] += A * X[i] + Y[i];
    });
  });
  q.wait();
}
catch (sycl::exception & e) {
  std::cout << e.what() << std::endl;
  return 1;
}
```



```
std::vector<float> h_X(length,xval);
std::vector<float> h_Y(length,yval);
std::vector<float> h_Z(length,zval);

try {

    sycl::queue q(sycl::default_selector{});

    const float A(aval);

    sycl::buffer<float,1> d_X { h_X.data(), sycl::range<1>(h_X.size()) };
    sycl::buffer<float,1> d_Y { h_Y.data(), sycl::range<1>(h_Y.size()) };
    sycl::buffer<float,1> d_Z { h_Z.data(), sycl::range<1>(h_Z.size()) };

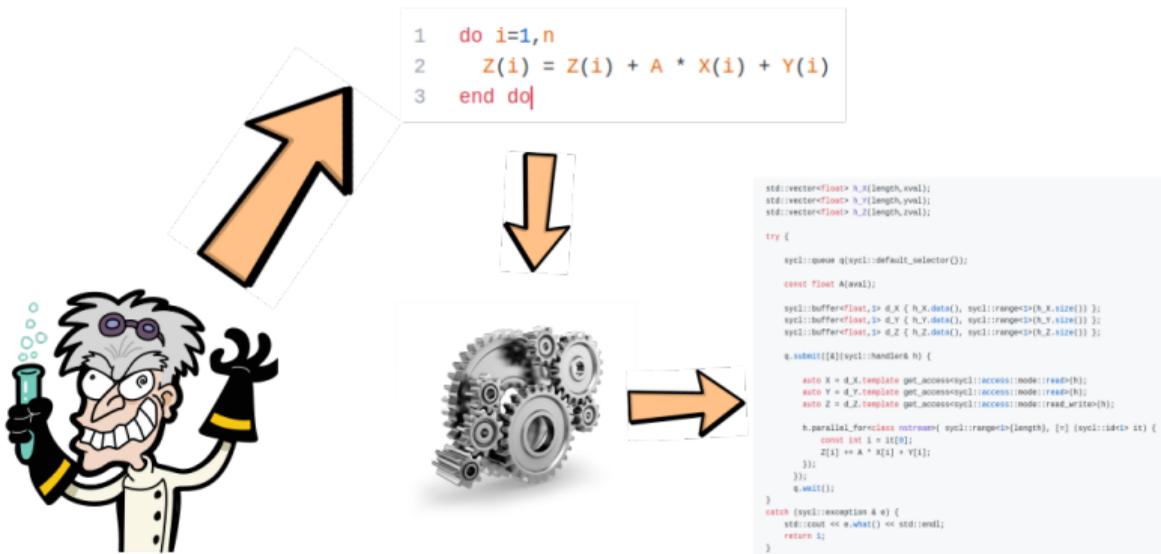
    q.submit([&](sycl::handler& h) {

        auto X = d_X.template get_access<sycl::access::mode::read>(h);
        auto Y = d_Y.template get_access<sycl::access::mode::read>(h);
        auto Z = d_Z.template get_access<sycl::access::mode::read_write>(h);

        h.parallel_for<class nstream>( sycl::range<1>(length), [=] (sycl::id<1> it) {
            const int i = it[0];
            Z[i] += A * X[i] + Y[i];
        });
    });
    q.wait();
}
catch (sycl::exception & e) {
    std::cout << e.what() << std::endl;
    return 1;
}
```

https://commons.wikimedia.org/wiki/File:Mad_scientist_transparent_background.svg

A compiler² that can read an average researcher's code and transform it into highly efficient code on an exascale machine.



²Wikipedia: A compiler is a computer program that translates computer code written in one programming language (the source language) into another language (the target language)

Artificial Intelligence is not ready yet . . .



https://commons.wikimedia.org/wiki/File:Mad_scientist_transparent_background.svg

```

1  do i=1,n
2    Z(i) = Z(i) + A * X(i) + Y(i)
3  end do
    
```



```

std::vector<float> h_x(length_xval);
std::vector<float> h_y(length_yval);
std::vector<float> h_z(length_zval);

try {
    sync::queue q(sync::default_selector());

    const float A{0.001};

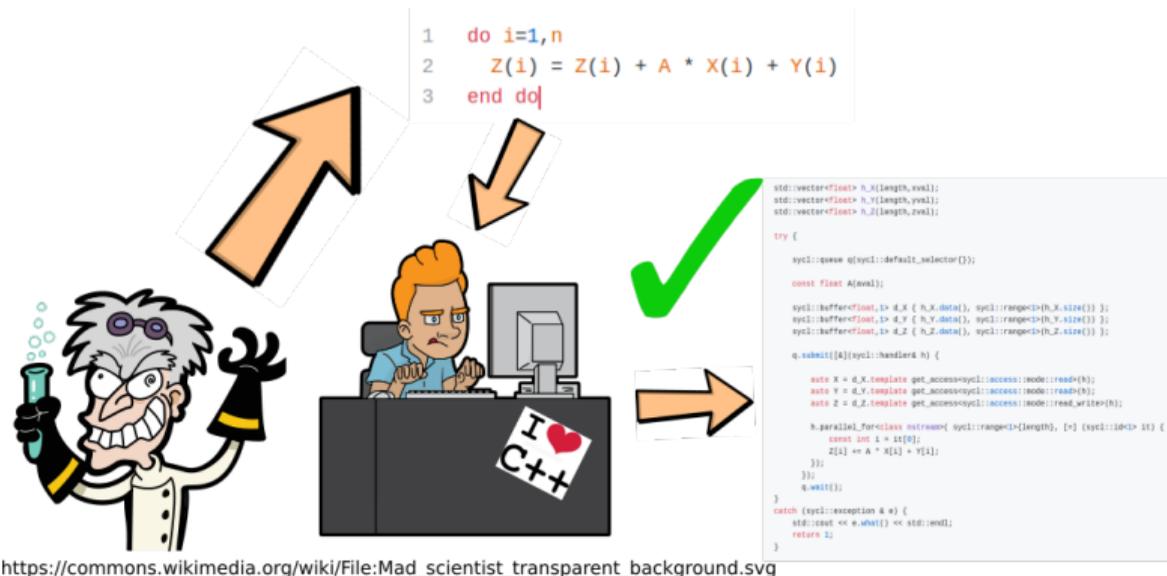
    sync::buffer<float, 1> d_x { h_x.data(), sync::range{0, h_x.size()}};
    sync::buffer<float, 1> d_y { h_y.data(), sync::range{0, h_y.size()}};
    sync::buffer<float, 1> d_z { h_z.data(), sync::range{0, h_z.size()}};

    q.submit([A]{sync::handler h {

        auto X = d_x.template get_access<sync::access::mode::read>(h);
        auto Y = d_y.template get_access<sync::access::mode::read>(h);
        auto Z = d_z.template get_access<sync::access::mode::read_write>(h);

        h.parallel_for<class ostream( sync::range{0, length}, [=] (sync::id<1> it) {
            const int i = it[h];
            Z[i] += A * X[i] + Y[i];
        });
    });
    q.wait();
}
catch (sync::exception & e) {
    std::cout << e.what() << std::endl;
    return 1;
}
    
```

... so let's use *Natural Intelligence* and add a human layer between the machine and the researchers : a **bio-compiler**



- Identify the common computational kernels of QMC
- Implement these kernels in a **human-readable library** (QMC experts)
- *Bio-compile* the human-readable library in a **HPC-library** (HPC experts)
- Scientists can link either library with their codes

For scientists

- We don't impose a programming language
- The code can stay easy to understand by the physicists/chemists
Performance-related aspects are delegated to the library
- Codes will not die with a change in architecture
- Scientific code development does not break the performance
- Scientists don't lose control on their codes

Separation of concerns

- Scientists will never have to manipulate low-level HPC code
- HPC experts will not be required to be experts in theoretical physics
- Better re-use of the optimization effort among the community

- The API is C-compatible: QMCKl appears like a C library \implies can be used in all other languages
- System functions in C (memory allocation, thread safety, *etc*)
- Computational kernels in Fortran for readability
- A lot of documentation (remember: the HPC compiler is a human!)

Literate programming is a programming paradigm introduced by Donald Knuth in which a computer program is given an explanation of its logic in a natural language, such as English, interspersed with snippets of macros and traditional source code, from which compilable source code can be generated. (Wikipedia)

Literate programming with *org-mode*:

- Here, comments are more important than code
- Can add graphics, \LaTeX formulas, tables, etc
- Documentation always synchronized with the code
- Some routines can be generated by embedded scripts
- Web site auto-generated when code is pushed
- Most of the the first EU report was auto-generated from the documentation

Instead of writing comments documenting code, we write code illustrating documentation.

File Edit Options Buffers Tools Table Org Text Help

Save Undo

#+TITLE: Atomic Orbitals

#+SETUPFILE: ../docs/theme.setup
 #+INCLUDE: ../tools/lib.org

The atomic basis set is defined as a list of shells. Each shell s is centered on a nucleus A , possesses a given angular momentum l and a radial function R_s . The radial function is a linear combination of \emph{primitive} functions that can be of type Slater ($p = 1$) or Gaussian ($p = 2$):

$$R_s(\mathbf{r}) = N_s |\mathbf{r} - \mathbf{R}_A|^{n_s} \sum_{k=1}^{N_{prim}} a_{ks} \exp(-\gamma_{ks} |\mathbf{r} - \mathbf{R}_A|^p).$$

In the case of Gaussian functions, n_s is always zero. The normalization factor N_s ensures that all the functions of the shell are normalized to unity. As this normalization requires the ability to compute overlap integrals, it should be written in the file to ensure that the file is self-contained and does not require the client program to have the ability to compute such integrals.

Atomic orbitals (AOs) are defined as

$$\chi_i(\mathbf{r}) = P_{\eta(i)}(\mathbf{r}) R_{\theta(i)}(\mathbf{r})$$

where $\theta(i)$ returns the shell on which the AO is expanded, and $\eta(i)$ denotes which angular function is chosen.

In this section we describe the kernels used to compute the values, gradients and Laplacian of the atomic basis functions.

- Headers
- Context...
- Polynomial part...
- Radial part
 - Gaussian basis functions

`-qmckl_ao_gaussian_vgl-` computes the values, gradients and Laplacians at a given point of `-n-` Gaussian functions centered at the same point:

```

- context-      input  | Global state
-X(3)-         input  | Array containing the coordinates of the points
-R(3)-         input  | Array containing the x,y,z coordinates of the center
-n-           input  | Number of computed Gaussians
-A(n)-         input  | Exponents of the Gaussians
-VGL(ldv,5)-   output | Value, gradients and Laplacian of the Gaussians
-ldv-          input  | Leading dimension of array -VGL-

```

Requirements :

- `-context-` is not 0
- `-n-` > 0
- `-ldv-` >= 5
- `-A(i)-` > 0 for all `-i-`
- `-X-` is allocated with at least `3 × 8` bytes
- `-R-` is allocated with at least `3 × 8` bytes
- `-A-` is allocated with at least `n × 8` bytes
- `-VGL-` is allocated with at least `n × 5 × 8` bytes

```

#+begin_src c :tangle (eval h func)
qmckl_exit_code
qmckl_ao_gaussian_vgl(const qmckl_context context,
                    const double *X,
                    const double *R,
                    const int64_t *n,
                    const int64_t *A,
                    const double *VGL,
                    const int64_t ldv);
#+end_src

#+begin_src f90 :tangle (eval f)
integer function qmckl_ao_gaussian_vgl_f(context, X, R, n, A, VGL, ldv) result(info)
use qmckl
implicit none
integer*8 , intent(in) :: context
real*8 , intent(in) :: X(3), R(3)
integer*8 , intent(in) :: n
real*8 , intent(in) :: A(n)
real*8 , intent(out) :: VGL(ldv,5)
integer*8 , intent(in) :: ldv

integer*8 :: i,j
real*8 :: Y(3), r2, t, u, v

```

U:0: qmckl_ao.org 85% (1493,0) <N> Git:context (Org ARew ? Undo-Tree Fill) Mail [1]

```

qmckl_ao_f.f90          qmckl_numprec_fh_func.f90
qmckl_ao_fh_func.f90   qmckl_numprec_func.h
qmckl_ao_func.h        qmckl_numprec.org
qmckl_ao.org           qmckl_numprec_private_type.h
qmckl_ao_private_func.h qmckl_numprec_type.h
qmckl_ao_private_type.h qmckl.org
qmckl_context.c        README.org
qmckl_context_fh_func.f90 table_of_contents
qmckl_context_fh_type.f90 test_qmckl
qmckl_context_func.h    test_qmckl_ao.c
qmckl_context.org       test_qmckl_ao_f.f90
qmckl_context_private_type.h test_qmckl.c
qmckl_context_type.h    test_qmckl_context.c
qmckl_distance_f.f90    test_qmckl_distance.c
qmckl_distance_fh_func.f90 test_qmckl_distance_f.f90
qmckl_distance_func.h  test_qmckl_error.c
qmckl_distance.org     test_qmckl_memory.c
qmckl_error.c          test_qmckl_numprec.c
qmckl_error_fh_func.f90 test_qmckl.org
(base) scenama@lpqdh82:~/Trex/qmckl/src$

```

```

char* qmckl_get_ao_basis_shell_ang_mom (const qmckl_context context) {
    if (qmckl_context_check(context) == QMCKL_NULL_CONTEXT) {
        return NULL;
    }

    qmckl_context_struct* const ctx = (qmckl_context_struct* const) context;
    assert (ctx != NULL);

    int32_t mask = 1 << 4;

    if ( (ctx->ao_basis.uninitialized & mask) != 0) {
        return NULL;
    }

    assert (ctx->ao_basis.shell_ang_mom != NULL);
    return ctx->ao_basis.shell_ang_mom;
}
~/Trex/qmckl/src/qmckl_ao.c [unix] [C] [ 15% ] (104/674,16)

```

```

#define QMCKL_INVALID_CONTEXT ((qmckl_exit_code) 183)
#define QMCKL_ALLOCATION_FAILED ((qmckl_exit_code) 184)
#define QMCKL_DEALLOCATION_FAILED ((qmckl_exit_code) 185)
#define QMCKL_INVALID_EXIT_CODE ((qmckl_exit_code) 186)
/* Context handling */

/* The context variable is a handle for the state of the library, */
/* and is stored in a data structure which can't be seen outside of */
/* the library. To simplify compatibility with other languages, the */
/* pointer to the internal data structure is converted into a 64-bit */
/* signed integer, defined in the ~qmckl_context~ type. */
/* A value of ~QMCKL_NULL_CONTEXT~ for the context is equivalent to a */
/* ~NULL~ pointer. */

/* #+NAME: qmckl_context */

typedef int64_t qmckl_context;
#define QMCKL_NULL_CONTEXT (qmckl_context) 0
/* Decoding errors */

/* To decode the error messages, ~qmckl_string_of_error~ converts an */
/* error code into a string. */

/* #+NAME: MAX_STRING_LENGTH */
/* : 128 */

const char* qmckl_string_of_error(const qmckl_exit_code error);
void qmckl_string_of_error_f(const qmckl_exit_code error,
                            char result[128]);

/* Updating errors in the context */

/* The error is updated in the context using ~qmckl_set_error~. */
/* When the error is set in the context, it is mandatory to specify */
/* from which function the error is triggered, and a message */
/* explaining the error. The exit code can't be ~QMCKL_SUCCESS~. */

/* # Header */
~/Trex/qmckl/include/qmckl.h [unix] [CPP] [ 31% ] (85/269,1)

```

Atomic Orbitals

The atomic basis set is defined as a list of shells. Each shell s is centered on a nucleus A , possesses a given angular momentum l and a radial function R_{sl} . The radial function is a linear combination of **primitive** functions that can be of type Slater ($p = 1$) or Gaussian ($p = 2$):

$$R_{sl}(\mathbf{r}) = \mathcal{N}_s |\mathbf{r} - \mathbf{R}_A|^n \sum_{k=1}^{N_{\text{basis}}} a_{ks} \exp(-\gamma_{ks} |\mathbf{r} - \mathbf{R}_A|^p).$$

In the case of Gaussian functions, n_s is always zero. The normalization factor \mathcal{N}_s ensures that all the functions of the shell are normalized to unity. As this normalization requires the ability to compute overlap integrals, it should be written in the file to ensure that the file is self-contained and does not require the client program to have the ability to compute such integrals.

Atomic orbitals (AOs) are defined as

$$\chi_i(\mathbf{r}) = P_{\eta(i)}(\mathbf{r}) R_{\theta(i)}(\mathbf{r})$$

where $\theta(i)$ returns the shell on which the AO is expanded, and $\eta(i)$ denotes which angular function is chosen.

In this section we describe the kernels used to compute the values, gradients and Laplacian of the atomic basis functions.

1 Polynomial part

1.1 Powers of $x - X_i$

The `qmckl_ao_power` function computes all the powers of the n input data up to the given maximum value given in input for each of the n points:

Atomic Orbitals

$$\nabla_z v_i = -2a_i (X_z - R_z) v_i$$

$$\Delta v_i = a_i (4|X - R|^2 a_i - 6) v_i$$

context	input	Global state
X(3)	input	Array containing the coordinates of the points
R(3)	input	Array containing the x,y,z coordinates of the center
n	input	Number of computed Gaussians
A(n)	input	Exponents of the Gaussians
VGL(ldv,5)	output	Value, gradients and Laplacian of the Gaussians
ldv	input	Leading dimension of array VGL

Requirements :

- context is not 0
- n > 0
- ldv >= 5
- A(i) > 0 for all i
- X is allocated with at least 3 × 8 bytes
- R is allocated with at least 3 × 8 bytes
- A is allocated with at least n × 8 bytes
- VGL is allocated with at least n × 5 × 8 bytes

```
qmckl_exit_code
qmckl_ao_gaussian_vgl(const qmckl_context context,
                    const double *X,
                    const double *R,
                    const int64_t *n,
                    const int64_t *A,
                    const double *VGL,
                    const int64_t ldv);
```

At each QMC step, we need to evaluate $E_{\text{loc}}(r_1, \dots, r_N) = \frac{\hat{H}\Psi(r_1, \dots, r_N)}{\Psi(r_1, \dots, r_N)}$:

- $\Psi(r_1, \dots, r_N)$
- $\Delta_i \Psi(r_1, \dots, r_i, \dots, r_N)$: kinetic energy
- $\vec{\nabla}_i \Psi(r_1, \dots, r_i, \dots, r_N)$: drift in the stochastic process

Main kernels

- AOs: $\chi(r)$, $\vec{\nabla}\chi(r)$, $\Delta\chi(r)$
- MOs: $\phi(r)$, $\vec{\nabla}\phi(r)$, $\Delta\phi(r)$
- Slater determinants (value, gradient, Laplacian)
- Pseudo-potential
- Jastrow correlation factor (eN, ee, eeN)

- 1 Kernel extraction: QMC experts agree on the mathematical expression of the problem
- 2 A mini-application is written to find the best data layout with HPC experts from real-size examples
- 3 The kernel is written in the documentation library
- 4 HPC experts provide an HPC version of the kernel with the same API
- 5 The library is linked in the QMC codes of the CoE

$$J_{\text{een}}(r, R) = \sum_{\alpha=1}^{N_{\text{nucl}}} \sum_{i=1}^{N_{\text{elec}}} \sum_{j=1}^{i-1} \sum_{p=2}^{N_{\text{nord}}} \sum_{k=0}^{p-1} \sum_{l=0}^{p-k-2\delta_{k,0}} c_{lkp\alpha} (r_{ij})^k \left[(R_{i\alpha})^l + (R_{j\alpha})^l \right] (R_{i\alpha} R_{j\alpha})^{(p-k-l)/2}$$

can be rewritten as

$$J_{\text{een}}(r, R) = \sum_{p=2}^{N_{\text{nord}}} \sum_{k=0}^{p-1} \sum_{l=0}^{p-k-2\delta_{k,0}} \sum_{\alpha=1}^{N_{\text{nucl}}} c_{lkp\alpha} \sum_{i=1}^{N_{\text{elec}}} \bar{R}_{i,\alpha,(p-k-l)/2} \bar{P}_{i,\alpha,k,(p-k+l)/2} \quad (\downarrow \text{complexity})$$

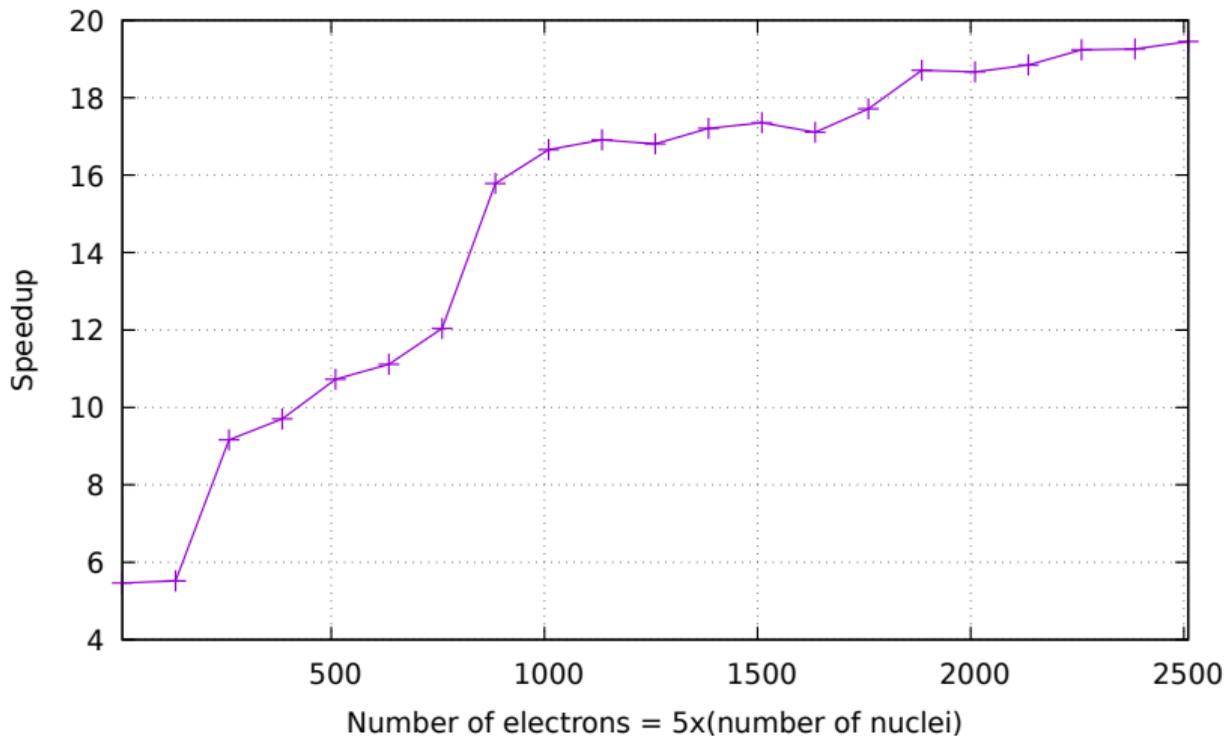
with

$$\bar{P}_{i,\alpha,k,l} = \sum_{j=1}^{N_{\text{elec}}} \bar{r}_{i,j,k} \bar{R}_{j,\alpha,l}. \quad (\text{GEMM})$$

$$\begin{aligned}
 \nabla_{im} J_{\text{een}}(r, R) = & \sum_{p=2}^{N_{\text{nord}}} \sum_{k=0}^{p-1} \sum_{l=0}^{p-k-2\delta_{k,0}} \sum_{\alpha=1}^{N_{\text{nucl}}} c_{lkp\alpha} \sum_{i=1}^{N_{\text{elec}}} \bar{G}_{i,m,\alpha,(p-k-l)/2} \bar{P}_{i,\alpha,k,(p-k+l)/2} + \\
 & \bar{G}_{i,m,\alpha,(p-k+l)/2} \bar{P}_{i,\alpha,k,(p-k-l)/2} + \bar{R}_{i,\alpha,(p-k-l)/2} \bar{Q}_{i,m,\alpha,k,(p-k+l)/2} + \\
 & \bar{R}_{i,\alpha,(p-k+l)/2} \bar{Q}_{i,m,\alpha,k,(p-k-l)/2} + \delta_{m,4} (\\
 & \bar{G}_{i,1,\alpha,(p-k+l)/2} \bar{Q}_{i,1,\alpha,k,(p-k-l)/2} + \bar{G}_{i,2,\alpha,(p-k+l)/2} \bar{Q}_{i,2,\alpha,k,(p-k-l)/2} + \\
 & \bar{G}_{i,3,\alpha,(p-k+l)/2} \bar{Q}_{i,3,\alpha,k,(p-k-l)/2} + \bar{G}_{i,1,\alpha,(p-k-l)/2} \bar{Q}_{i,1,\alpha,k,(p-k+l)/2} + \\
 & \bar{G}_{i,2,\alpha,(p-k-l)/2} \bar{Q}_{i,2,\alpha,k,(p-k+l)/2} + \bar{G}_{i,3,\alpha,(p-k-l)/2} \bar{Q}_{i,3,\alpha,k,(p-k+l)/2})
 \end{aligned}$$

with

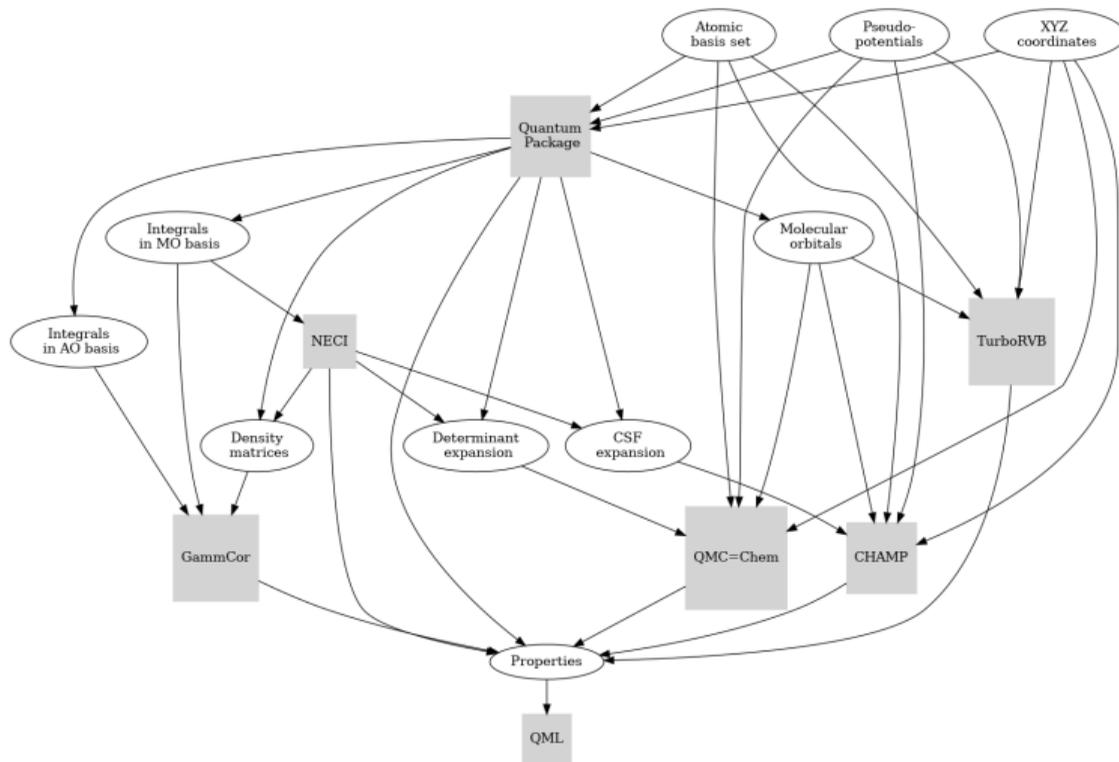
$$\bar{G}_{i,m,\alpha,l} = \frac{\partial (R_{i\alpha})^l}{\partial r_i}, \quad \bar{g}_{i,m,j,k} = \frac{\partial (r_{ij})^k}{\partial r_i}, \quad \text{and } \bar{Q}_{i,m,\alpha,k,l} = \sum_{j=1}^{N_{\text{elec}}} \bar{g}_{i,m,j,k} \bar{R}_{j,\alpha,l}$$

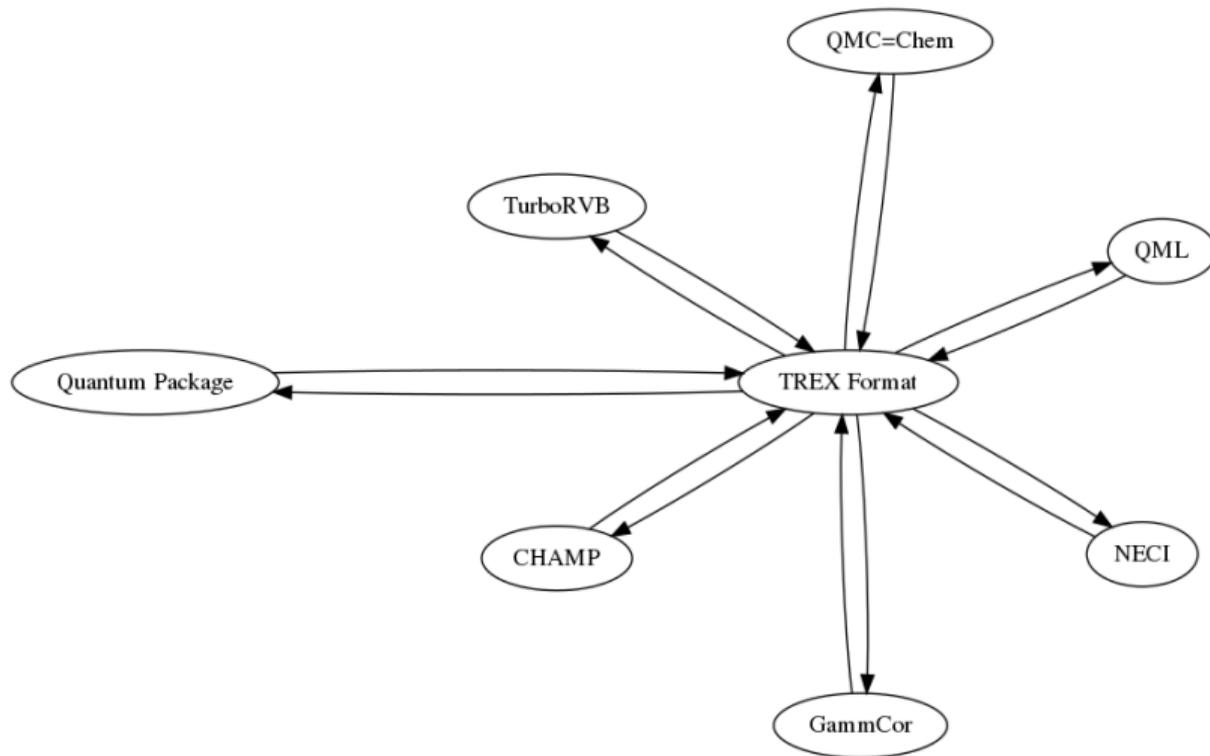


~ 80% of the AVX-512 peak is reached on a Skylake CPU.



TREXIO: The TREX I/O library



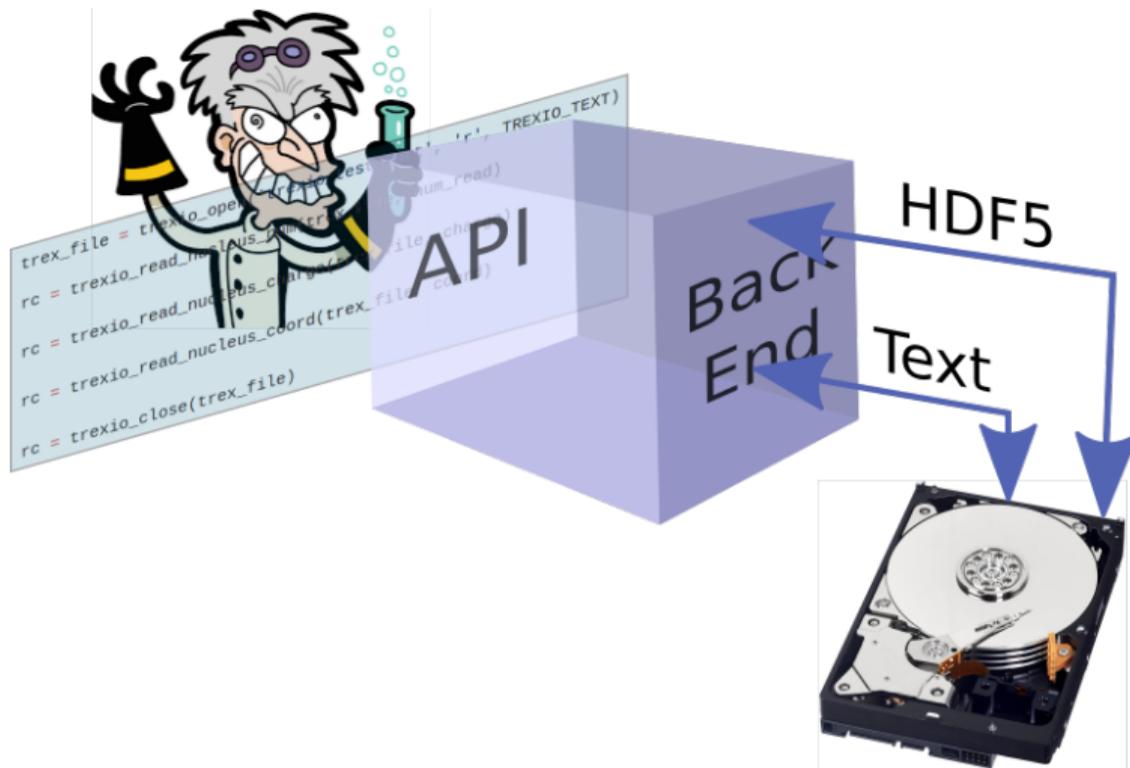


Front-end

- Definition of an API for to read/write wave functions
- C-compatible API: Easy bindings in other languages

Back-end

- HDF5: Efficient I/O
- Text: debugging, fallback when HDF5 can't be installed



Groups

Electron	AO	Basis	ECP	OneRDM
Nucleus	MO	Determinants	Jastrow	TwoRDM

Data

- Inside each group, multiple values.
- Strong conventions (atomic units, ordering of cartesian orbitals, *etc*)
- File is self-contained: no external knowledge is necessary to compute $\Psi(r_1, \dots, r_n)$ (normalization factors, basis set parameters, *etc*)

- Computable function names:
trexio_<read|write|has>_<group>_<data>[_32|_64]
- return code for error handling
- Auto-generated from a JSON config file defining groups, data and types

```
"electron": {
  "up_num"      : [ "int", [ ] ]
  , "dn_num"    : [ "int", [ ] ]
},

"nucleus": {
  "num"        : [ "int" , [           ] ]
  , "charge"   : [ "float", [ "nucleus.num" ] ]
  , "coord"    : [ "float", [ "nucleus.num", "3" ] ]
  , "label"    : [ "char" , [ "nucleus.num", "32" ] ]
  , "point_group" : [ "char" , [ "32" ] ]
},
```

```

subroutine read_xyz(trex_file, xyz_filename)
  use trexio
  implicit none
  integer*8, intent(in)      :: trex_file
  character*(128), intent(in) :: xyz_filename
  integer*8                  :: nucl_num      ! Number of nuclei
  character*(256)            :: title        ! Title of the file
  character*(32), allocatable :: nucl_label(:) ! Atom labels
  real*8, allocatable        :: nucl_charge(:) ! Nuclear charges
  real*8, allocatable        :: nucl_coord(:, :) ! Nuclear coordinates
  integer*8                  :: i
  integer                    :: j
  integer                    :: info
  double precision, parameter :: a0 = 0.52917721067d0

  open(unit=10, file=xyz_filename)

  read(10, *) nucl_num

  allocate(nucl_label(nucl_num), &
           nucl_charge(nucl_num), &
           nucl_coord(3, nucl_num) )

  read(10, '(A)') title

  do i=1, nucl_num
    read(10, *) nucl_label(i), nucl_coord(1:3, i)

    info = trexio_element_number_of_symbol(trim(nucl_label(i)), j)
    call check_success(info, 'Unable to convert symbol to number')

    nucl_charge(i) = dble(j)
  end do

  close(10)

  ! Convert into atomic units
  nucl_coord = nucl_coord / a0

  info = trexio_write_nucleus_num(trex_file, nucl_num)
  call check_success(info, 'Unable to write number of nuclei')

  info = trexio_write_nucleus_coord(trex_file, nucl_coord)
  call check_success(info, 'Unable to write nuclear coordinates')

  info = trexio_write_nucleus_charge(trex_file, nucl_charge)
  call check_success(info, 'Unable to write nuclear charges')

  info = trexio_write_nucleus_label(trex_file, nucl_label)
  call check_success(info, 'Unable to write nuclear labels')

  beta_num = int(sum(nucl_charge(:)))/2
  alpha_num = int(sum(nucl_charge(:))) - beta_num

  info = trexio_write_electron_up_num(trex_file, alpha_num)
  call check_success(info, 'Unable to write up electrons')

  info = trexio_write_electron_dn_num(trex_file, beta_num)
  call check_success(info, 'Unable to write dn electrons')

end subroutine read_xyz

```

- TREX web site : <https://trex-coe.eu>
- QMCKl documentation : <https://trex-coe.github.io/qmckl>
- QMCKl repository : <https://github.com/trex-coe/qmckl>
- TREXIO repository : <https://github.com/trex-coe/trexio>