

# Resolving subglacial hydrology network dynamics through seismic observations on an Alpine glacier.

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A 3-year PhD research defended by **Ugo NANNI** on December 3<sup>rd</sup> 2020

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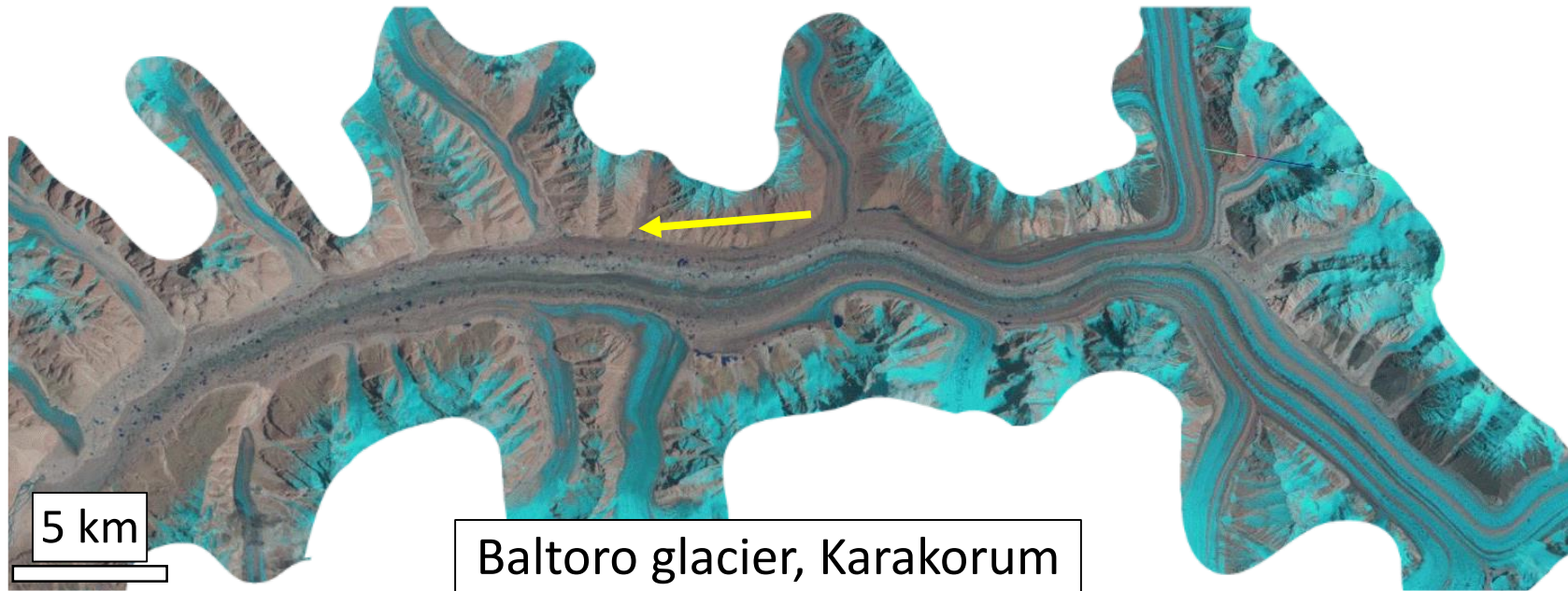
Anne Oberman (SED, ETH Zürich)

Mauro Werder (VAW, ETH Zürich)

# My first step in glaciology

25 years of glaciers movement in one second

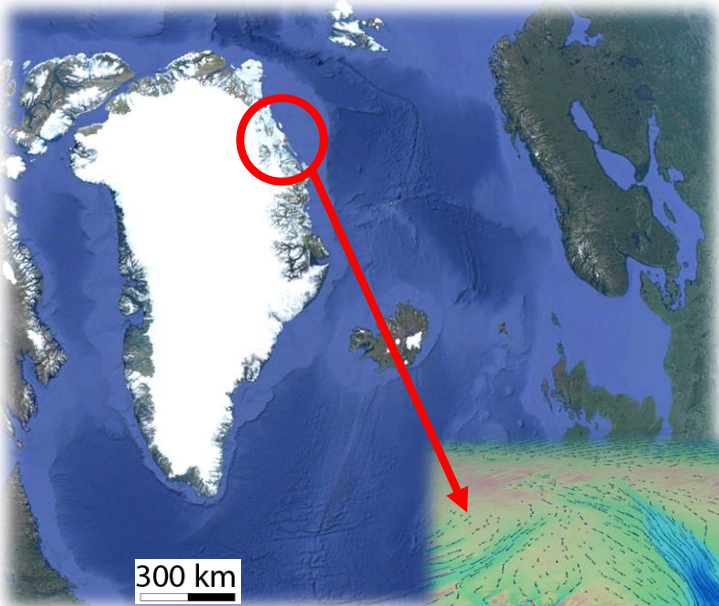
1990



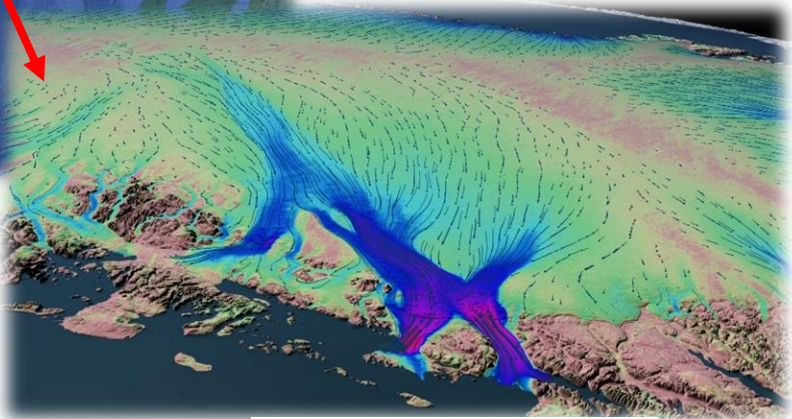
Up to 200 m/year

(Paul, 2015; Quincey et al., 2008)

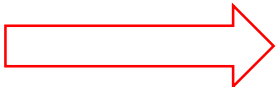
# Glaciers and ice sheets drive sea-level-rise



- In Greenland glaciers flow up to several kilometers per year!
- Ice goes to the ocean where it increases sea-level rise



© NASA  
Speed (km.yr<sup>-1</sup>)  
0.001 0.1 1 >3

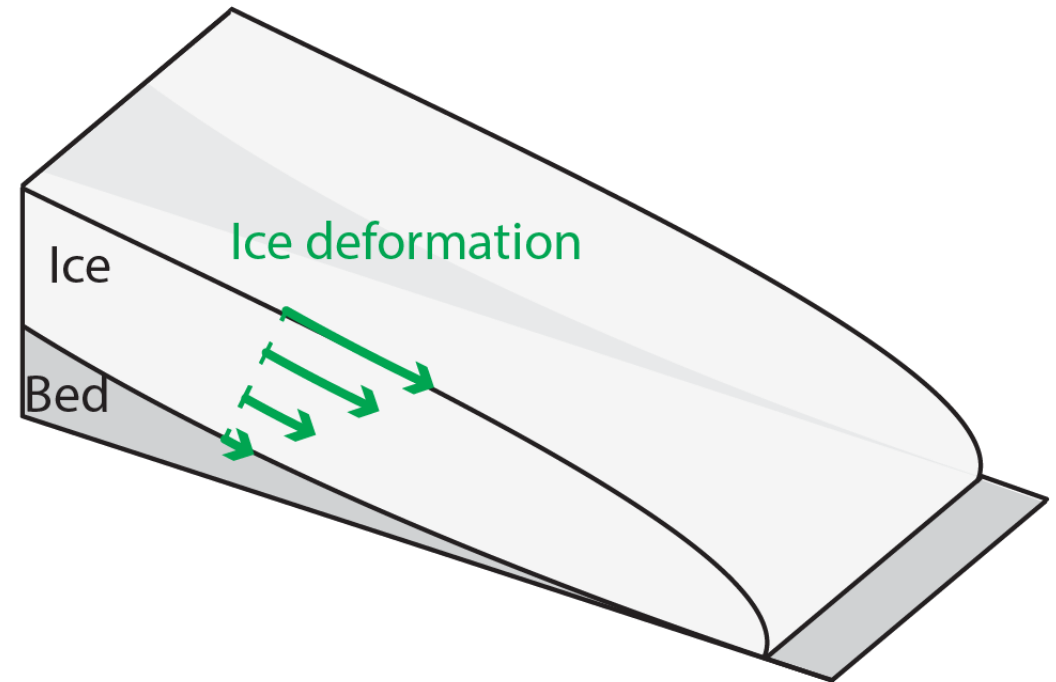


A flood in France (2016)

# On the dynamics of glaciers

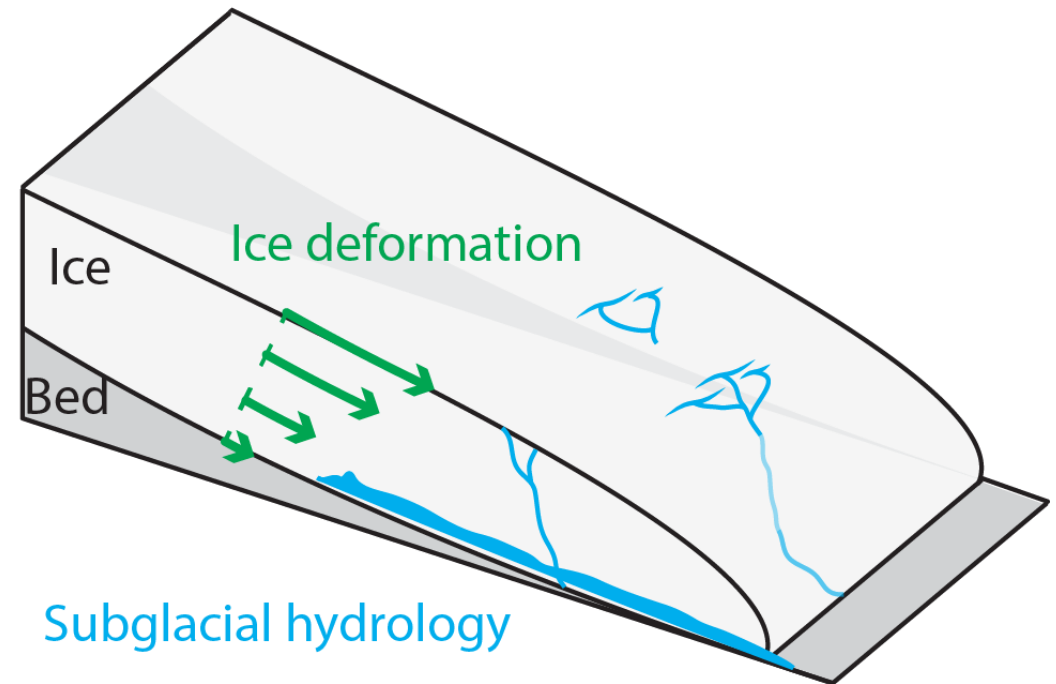
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- Glaciers form by snow accumulation
- Ice slowly deforms and flows downhill



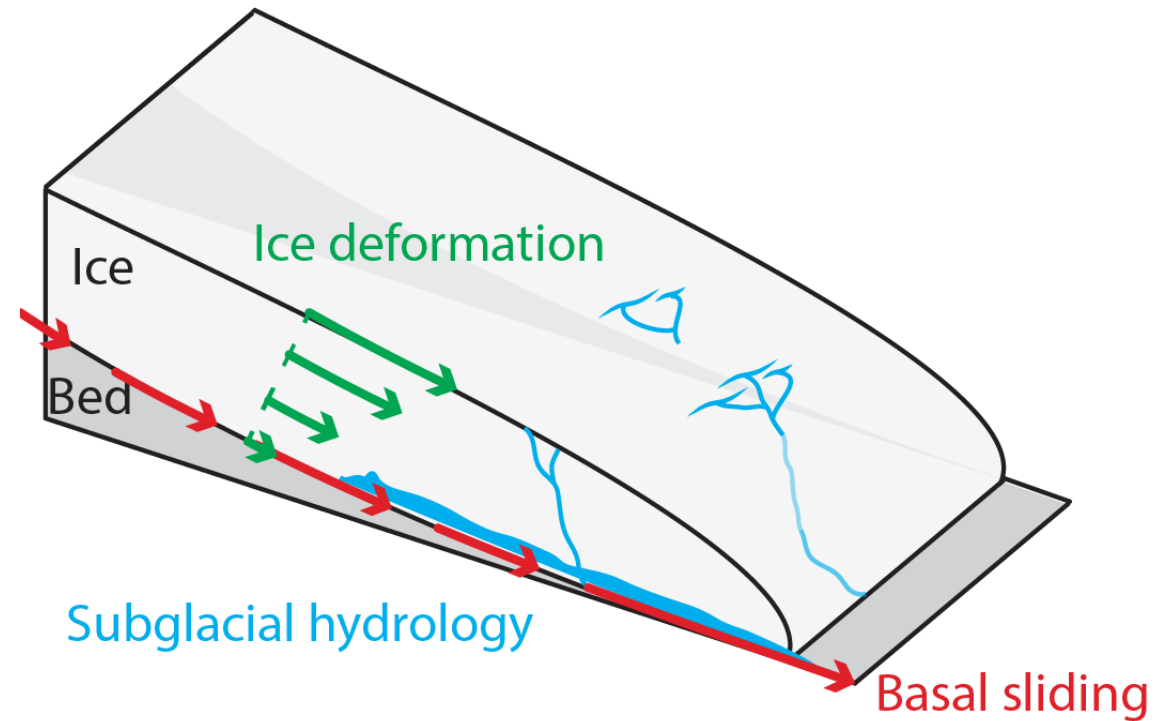
# On the dynamics of glaciers

- Glaciers form by snow accumulation
- Ice slowly deforms and flows downhill
- At low altitudes surface melt occurs and meltwater penetrates glaciers



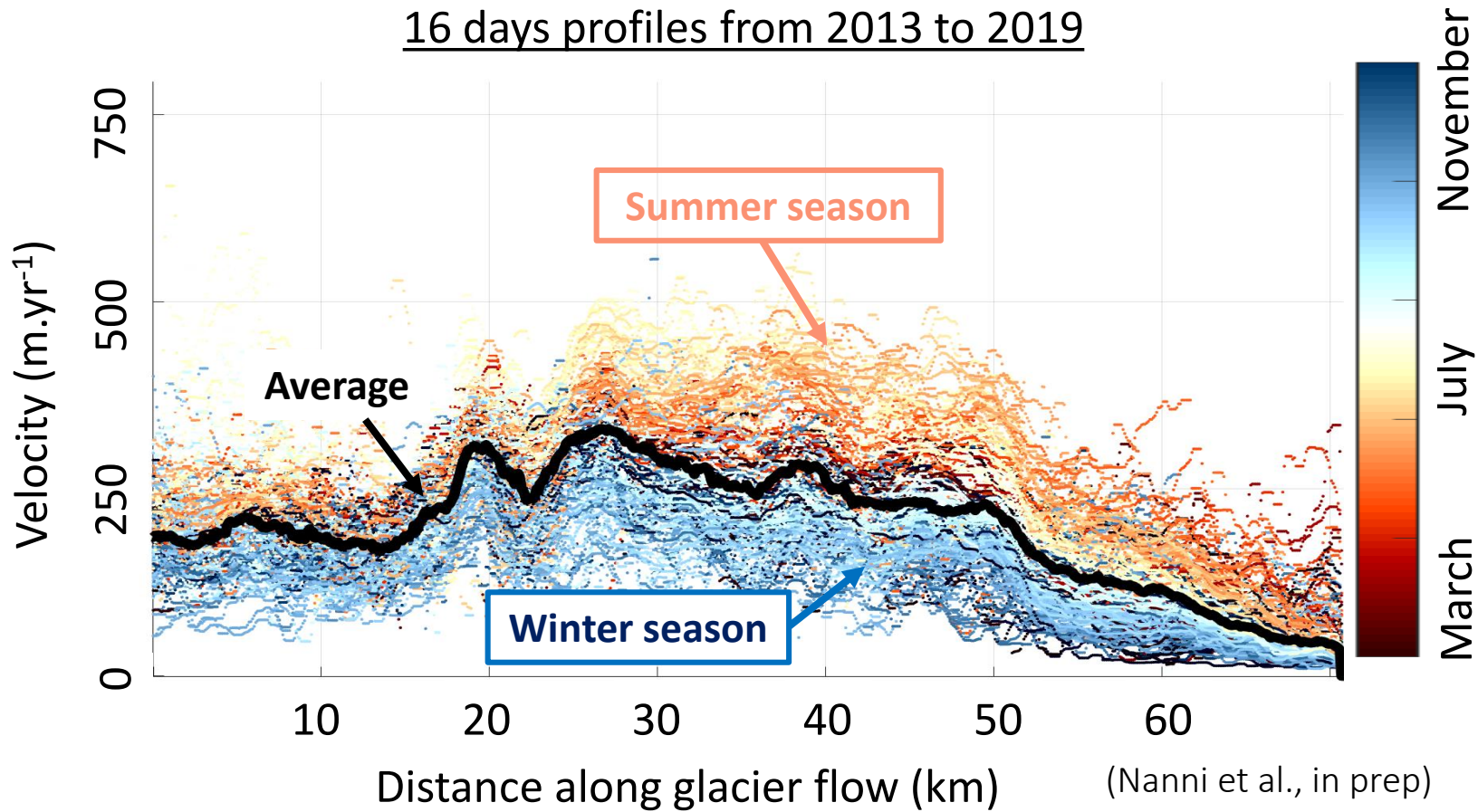
# On the dynamics of glaciers

- Glaciers form by snow accumulation
- Ice slowly deforms and flows downhill
- In low altitudes surface melt occurs and meltwater penetrates glaciers
- Subglacial waterflow modulates **sliding** by lubrication



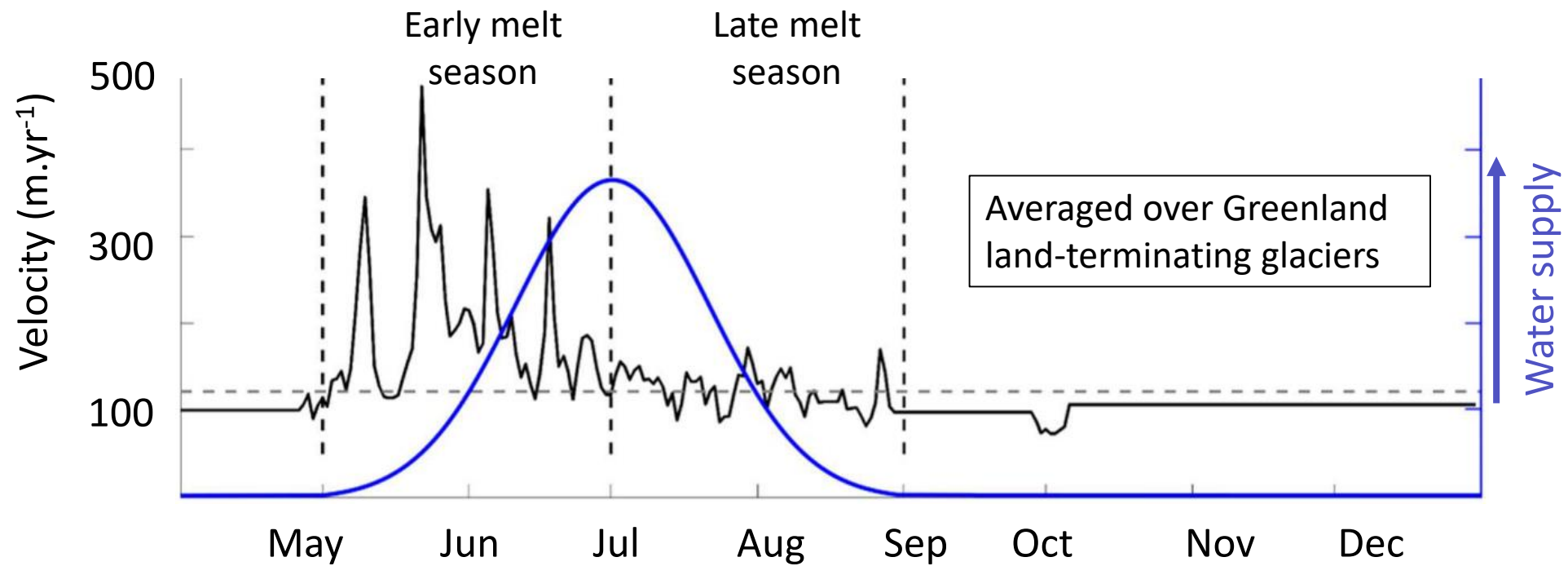
Up to 50 to 90%  
of ice flow

# My second step in glaciology



Fedchenko glacier,  
Pamir

# A complex response to water supply

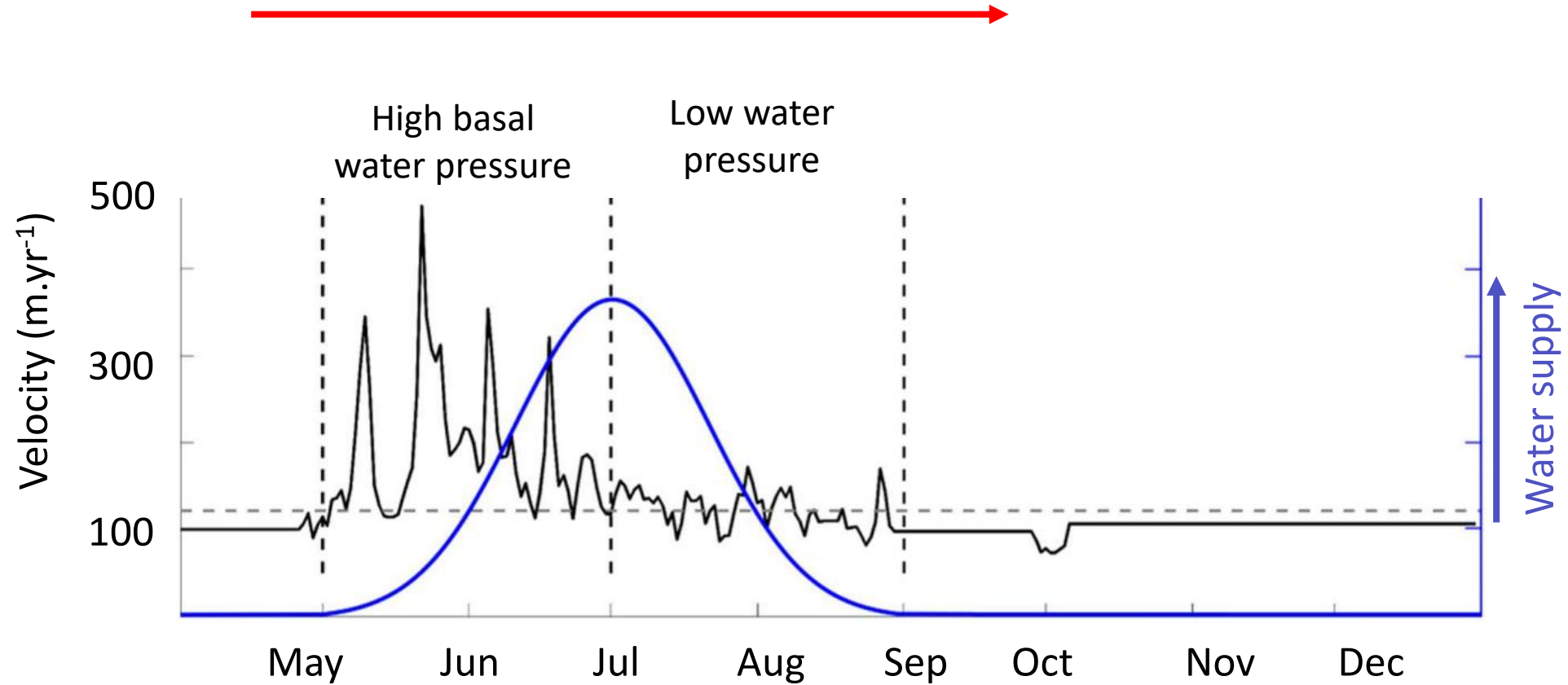


(Davison et al., 2019)



# No direct relationship water/sliding

## Evolution of the subglacial drainage system



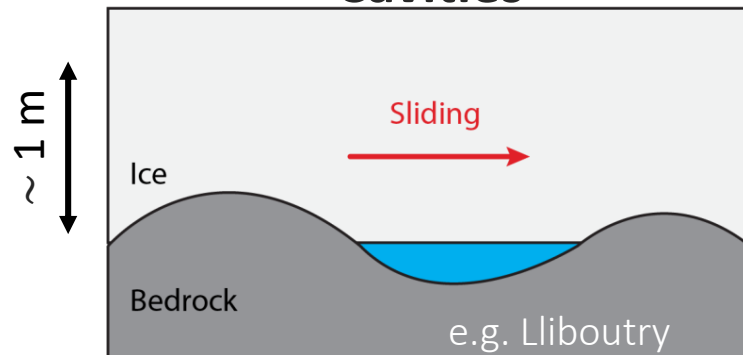
(Davison et al., 2019)

# A complex drainage system

## Evolution of the subglacial drainage system



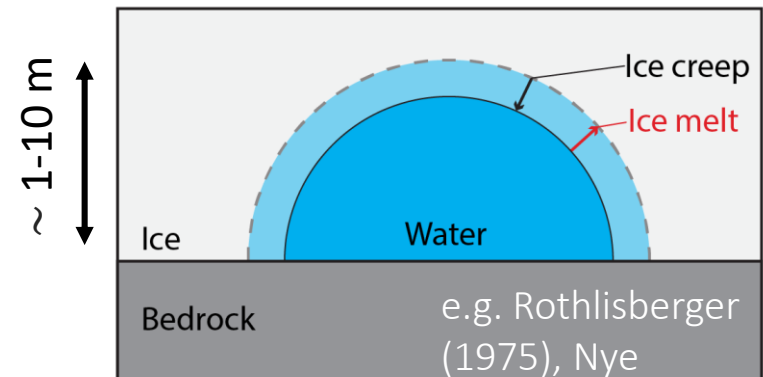
Inefficient and distributed:  
**Cavities**



High basal water pressure

More glacier flow

Efficient and localized:  
**Channels**



Low basal water pressure

Less glacier flow

# Limited measurements

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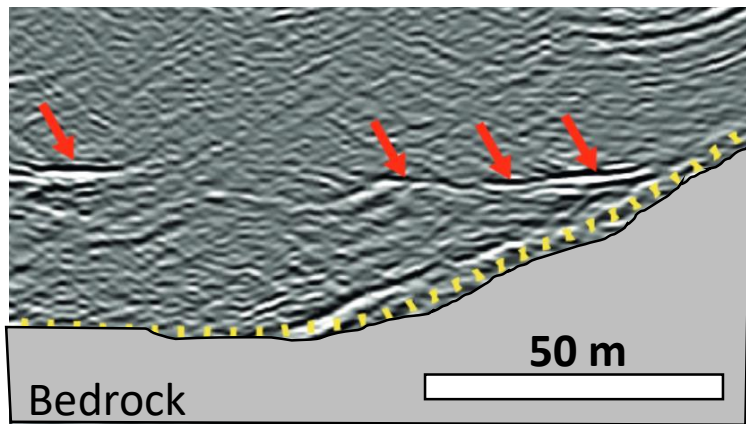
How to measure a system rapidly evolving in time and strongly heterogeneous in space?

# Limited measurements

How to measure a system rapidly evolving in time and strongly heterogeneous in space?

## Ground penetrating radar

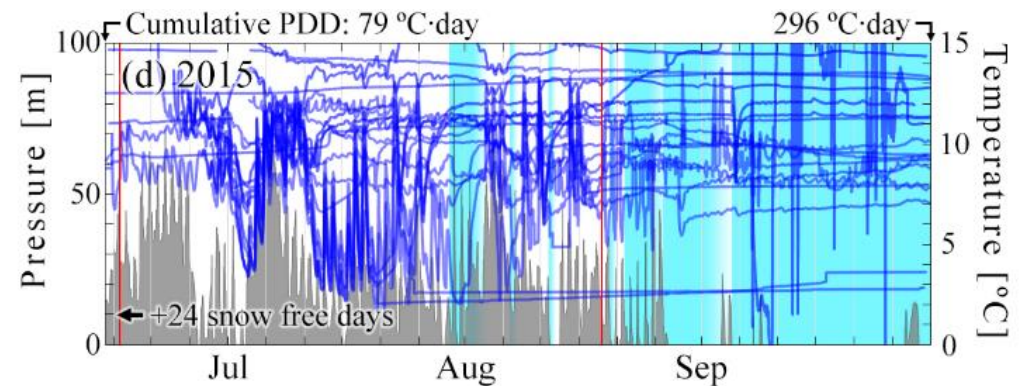
Limited access to physical properties



August 2019, Rhonegletscher  
(Church et al., 2020)

## Basal water pressure measurements

Punctual and highly heterogeneous



Results of 700+ boreholes pressure sensors  
(Rada and Schoof, 2018)

# Key questions remain

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- Where are cavities and channels?
- How do they develop?
- What are their hydraulic properties?

# Great uncertainties on the fate of glaciers

## Surface Melt–Induced Acceleration of Greenland Ice-Sheet Flow 2002

H. Jay Zwally,<sup>1\*</sup> Waleed Abdalati,<sup>2</sup> Tom Herring,<sup>3</sup> Kristine Larson,<sup>4</sup> Jack Saba,<sup>5</sup> Konrad Steffen<sup>6</sup>

ARTICLE

2019

<https://doi.org/10.1038/s41467-019-12039-2>

OPEN

## Rapid accelerations of Antarctic Peninsula outlet glaciers driven by surface melt

Peter A. Tuckett<sup>1</sup>, Jeremy C. Ely<sup>1\*</sup>, Andrew J. Sole<sup>1</sup>, Stephen J. Livingstone<sup>1</sup>, Benjamin J. Davison<sup>2</sup>, J. Melchior van Wessem<sup>3</sup> & Joshua Howard<sup>1</sup>

## Decadal slowdown of a land-terminating sector of the Greenland Ice Sheet despite warming 2015

Andrew J. Tedstone<sup>1</sup>, Peter W. Nienow<sup>1</sup>, Noel Gourmelen<sup>1</sup>, Amaury Dehecq<sup>1,2</sup>, Daniel Goldberg<sup>1</sup> & Edward Hanna<sup>3</sup>

Dominant **inefficient** drainage system?

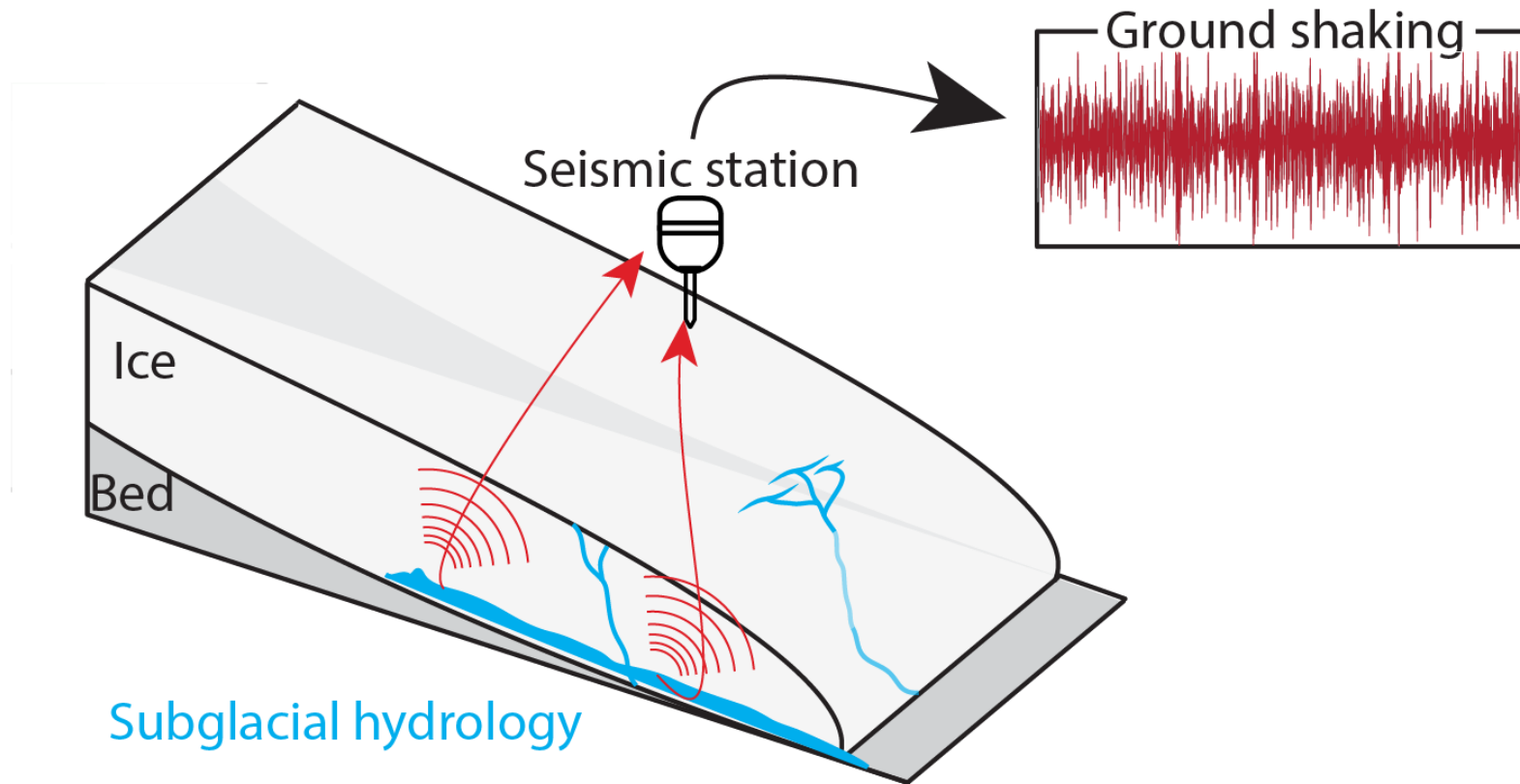
Dominant **efficient** drainage system?

# Time to find a **new way** to observe subglacial hydrology

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# Can seismology help?



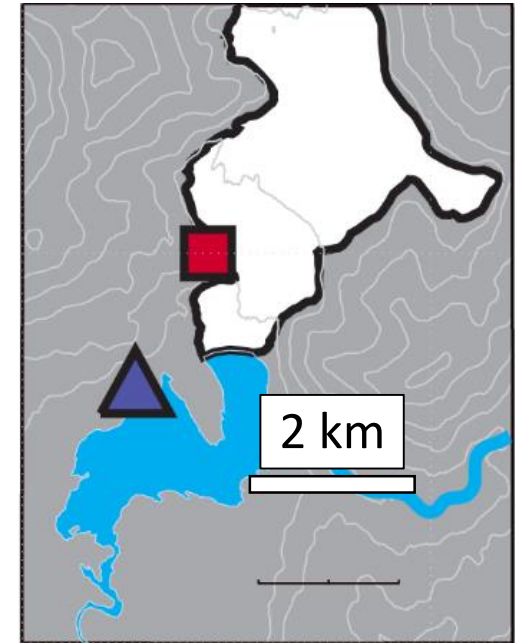
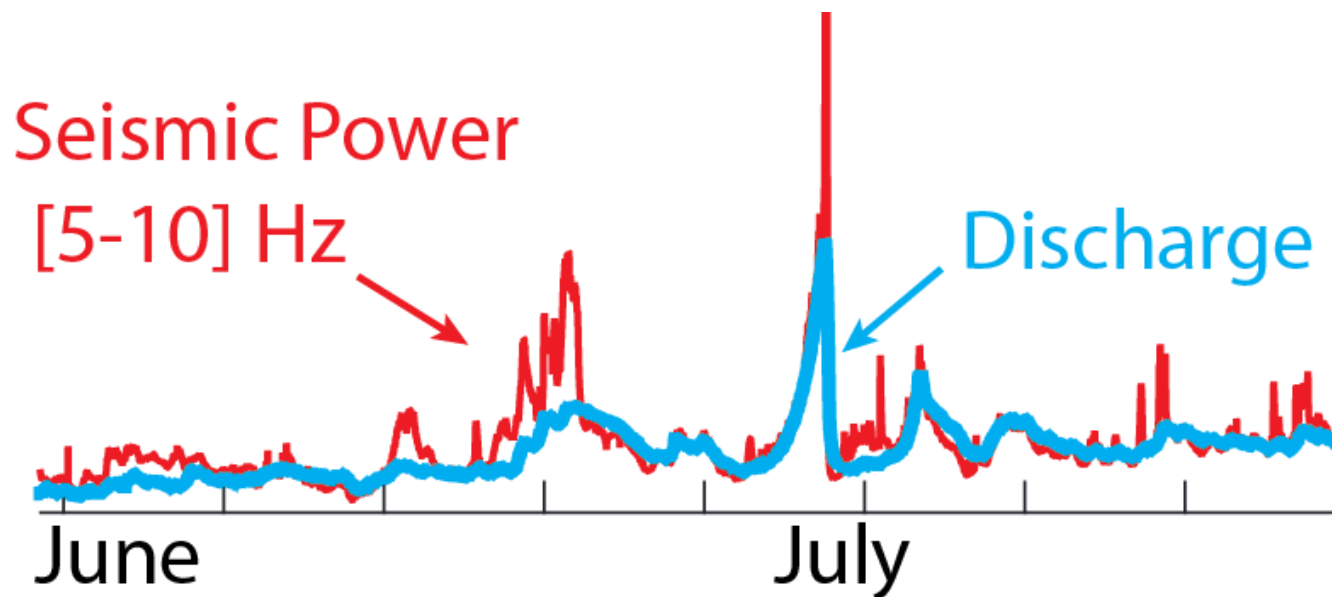


# A new-born tool to study subglacial hydrology

## Subglacial discharge at tidewater glaciers revealed by seismic tremor

2015

Timothy C. Bartholomaus<sup>1</sup>, Jason M. Amundson<sup>2</sup>, Jacob I. Walter<sup>1</sup>, Shad O'Neel<sup>3</sup>, Michael E. West<sup>4</sup> and Christopher F. Larsen<sup>4</sup>



Mendenhall glacier, Alaska

# A promising physical framework

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Gimbert et al., (2014, 2016):

- Seismic power scales with **hydraulic RADIUS** and **hydraulic PRESSURE gradient**



**Study and invert subglacial hydraulic properties**

# Limitations at the beginning of my PhD

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When/where can we apply it

- To other glaciers?
- To complete melt-season?  
(*at lower discharge?*)

What can we observe?

- Only sensitive to channels?
- Spatial information?

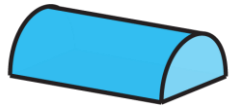
# My questions

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#1

Can we **MEASURE** subglacial-water-flow-induced seismicity over complete melt-seasons?



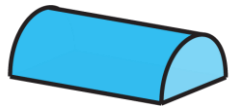
#2

What is the **TEMPORAL** dynamics of subglacial hydraulic properties over complete melt-seasons?



#3

Can we **LOCATE** distributed sources of seismic noise?



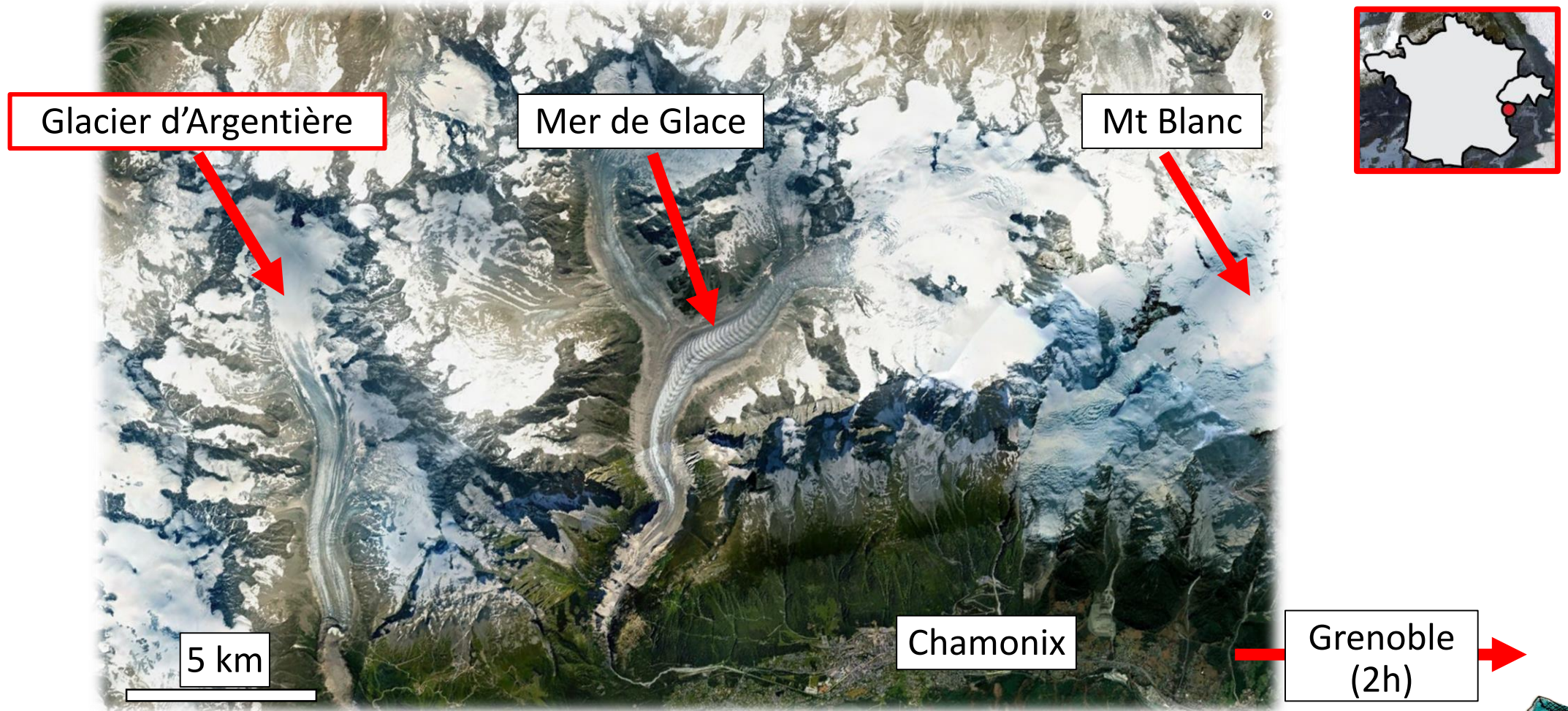
#4

What is the **SPATIAL** dynamics of cavities and channels?

**Part I**

**Part II**

# Glacier d'Argentière: a field-scale laboratory



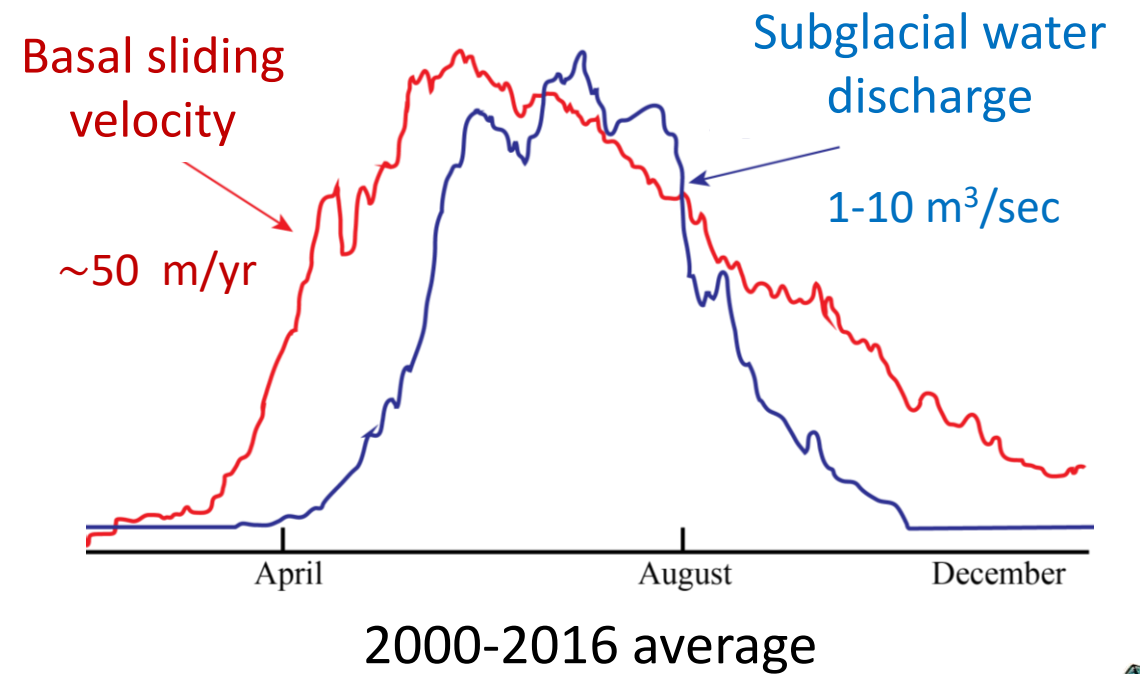
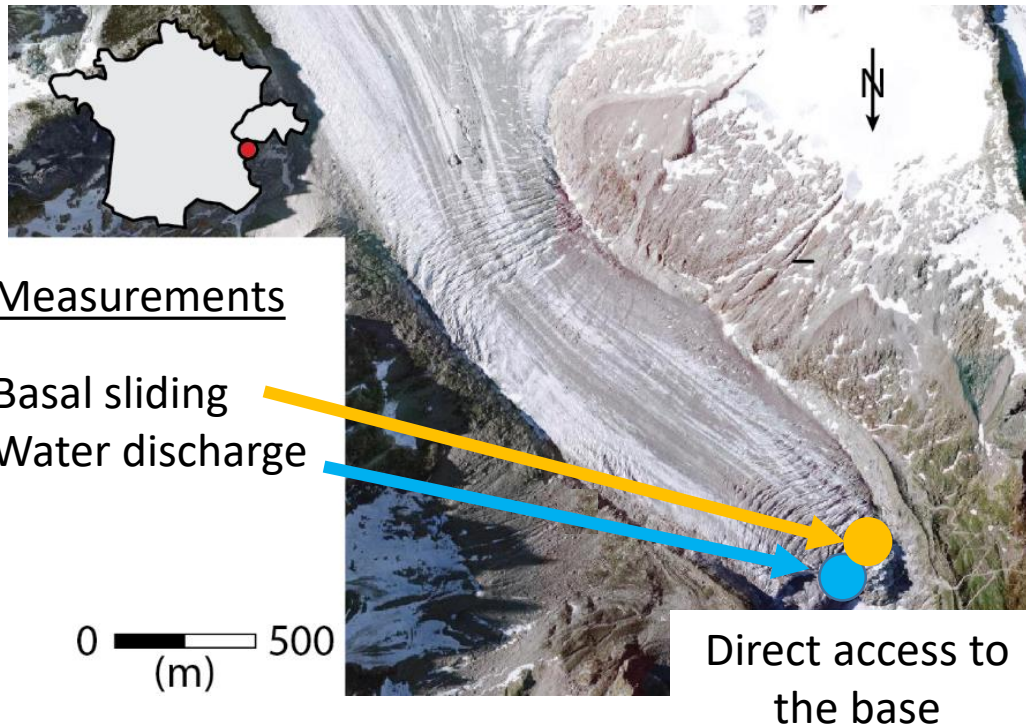
# Unique measurements

14/08/2019 10:00

- 30+ years of measurements of **water discharge** and **sliding**
- High sensitivity to subglacial water flow

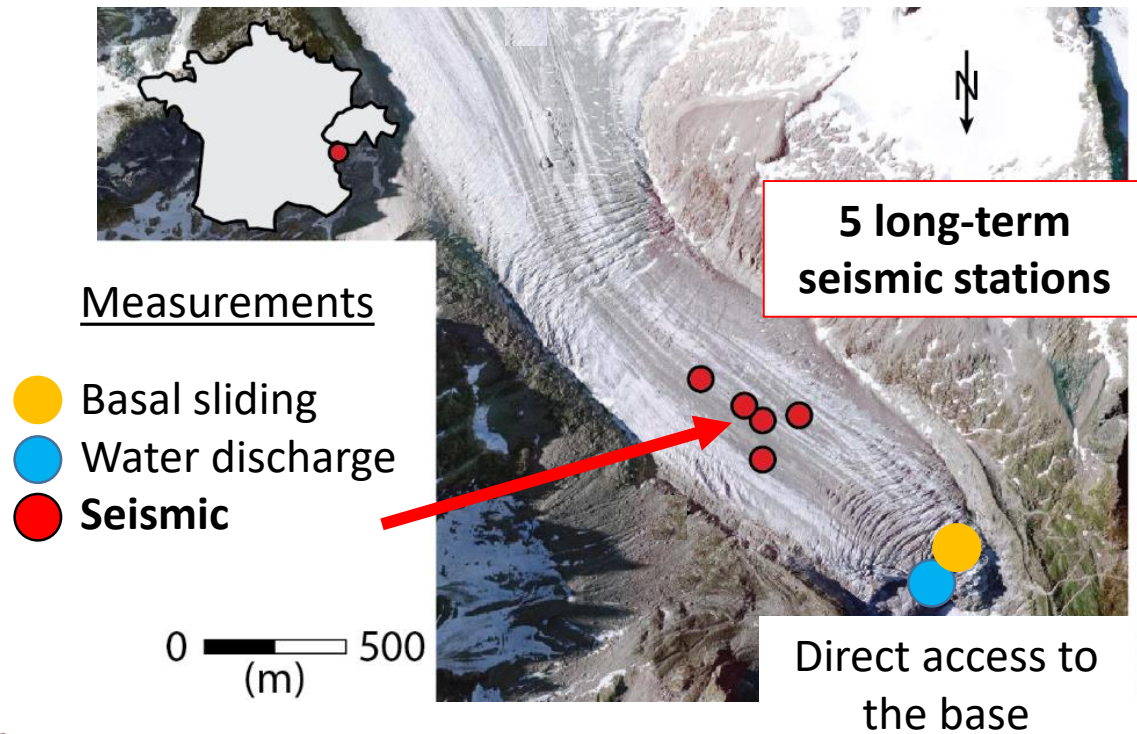


©L. Moreau



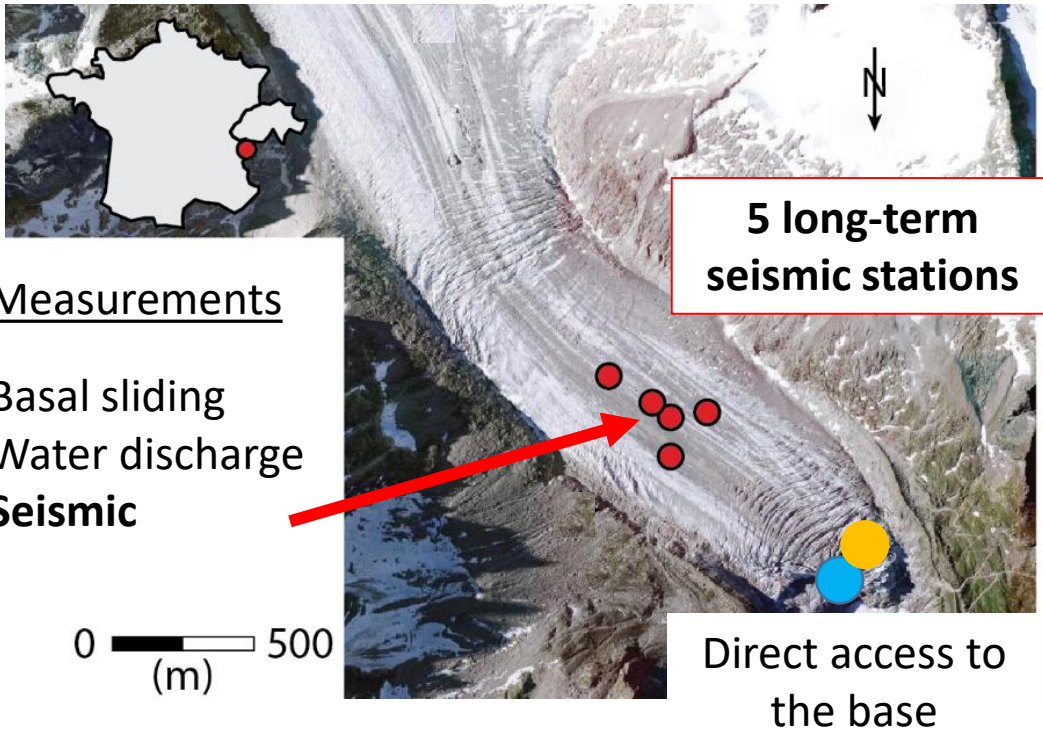
# Seismic measurements: temporal

- Up to 7 seismic stations maintained from spring **2016** to winter **2020**
  - Collaboration with Fabian Walter and Dominik Graeff from ETH Zurich



In collaboration with the SAUSSURE project: a multidisciplinary investigation of the subglacial processes on glacier d'Argentière.

# Seismic measurements: temporal



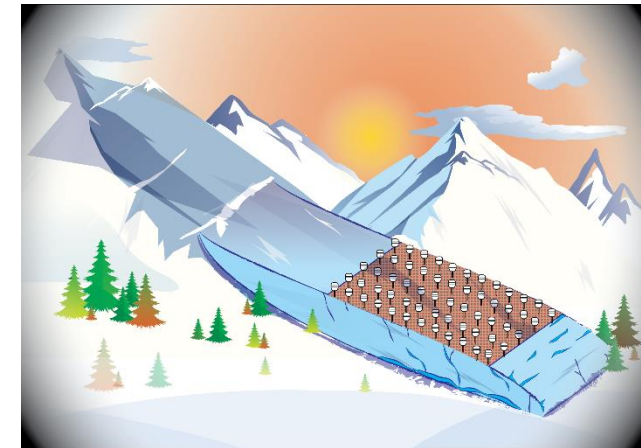
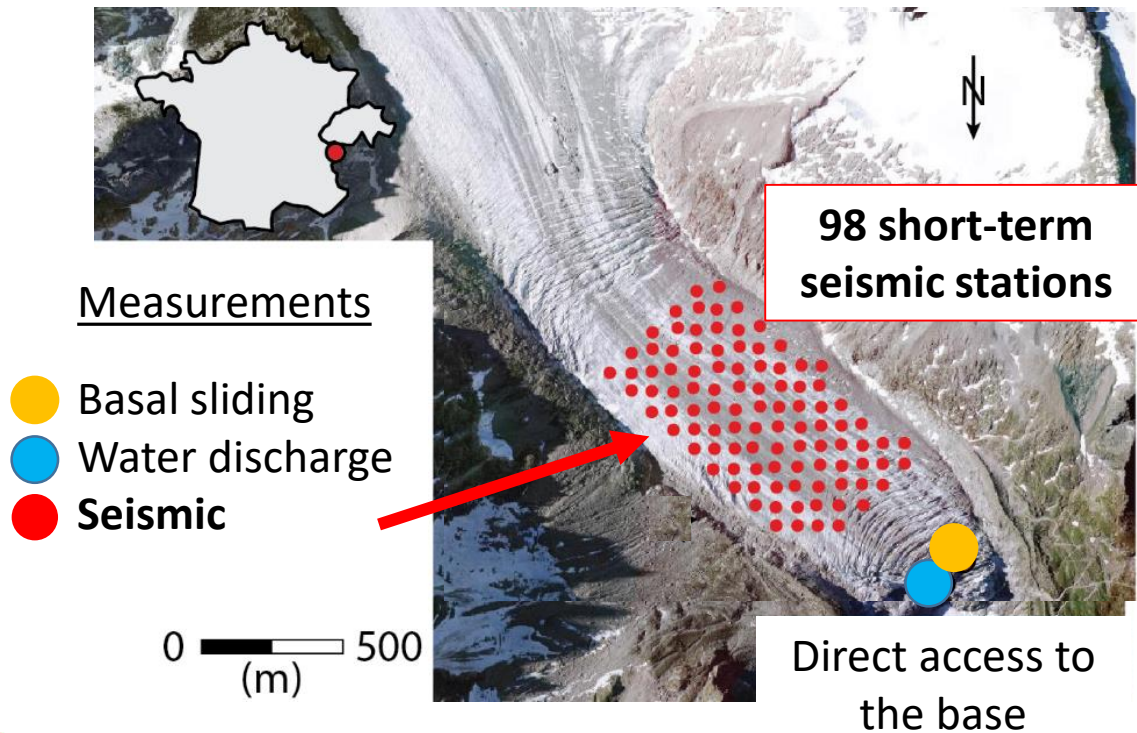
~ 70 days of maintenance + casing and cabling preparation





# Seismic measurements: spatial

- 98 seismic stations maintained for one-month in spring 2018
- A cross-disciplinary and cross-institutes collaboration



In collaboration with the RESOLVE project: a development of a multi-instrument platform for interdisciplinary research.

So what did I observe?

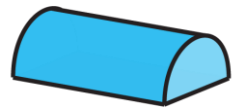


# Part I: Temporal investigation of subglacial water flow

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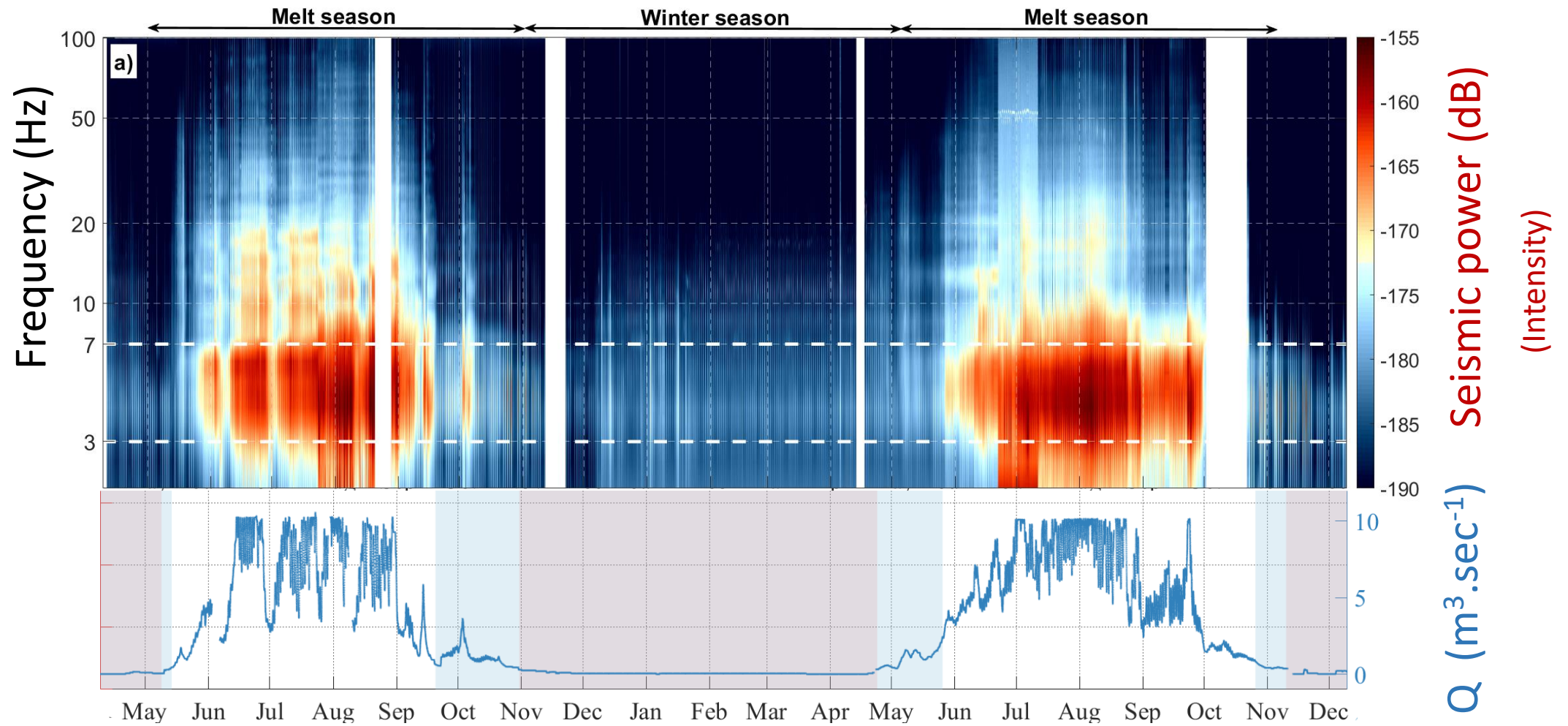
**#1** Can we **MEASURE** subglacial-water-flow-induced seismicity over complete melt seasons?



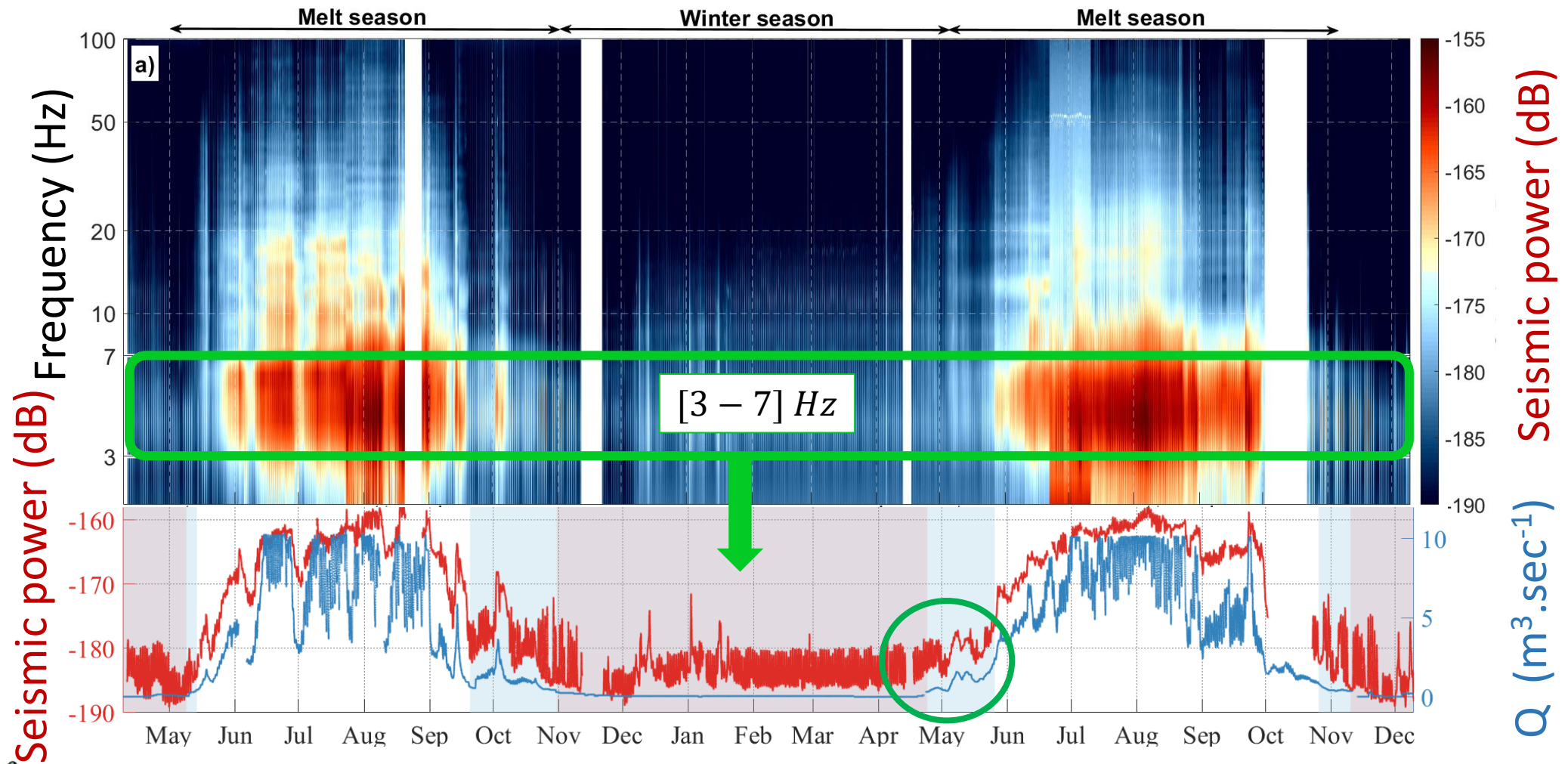
**#2** What is the **TEMPORAL** dynamics of subglacial hydraulic properties over complete melt seasons?



# Seismic measurements



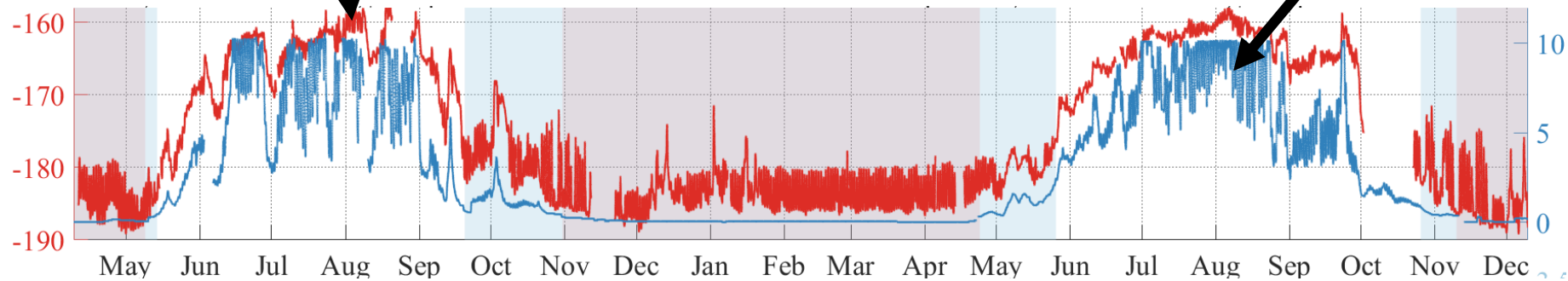
# Seismic measurements



# Notations

$P_w$  = seismic power

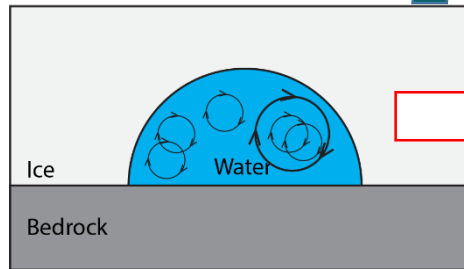
$Q$  = water discharge



# Theoretical end-members

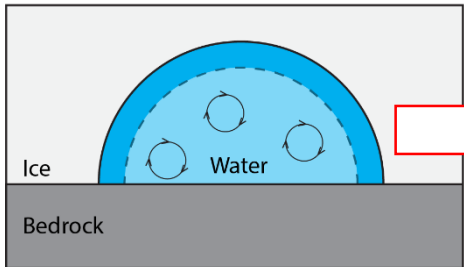
(Gimbert et al., 2016)

2 predicted responses



Only **Pressure gradient  $S$**  varies

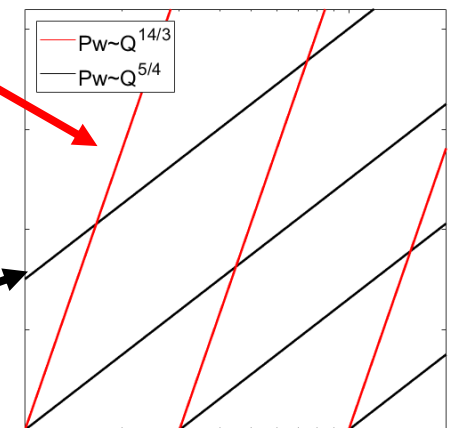
$$\rightarrow P_w \propto Q^{14/3}$$



Only **Hydraulic radius  $R$**  varies

$$\rightarrow P_w \propto Q^{5/4}$$

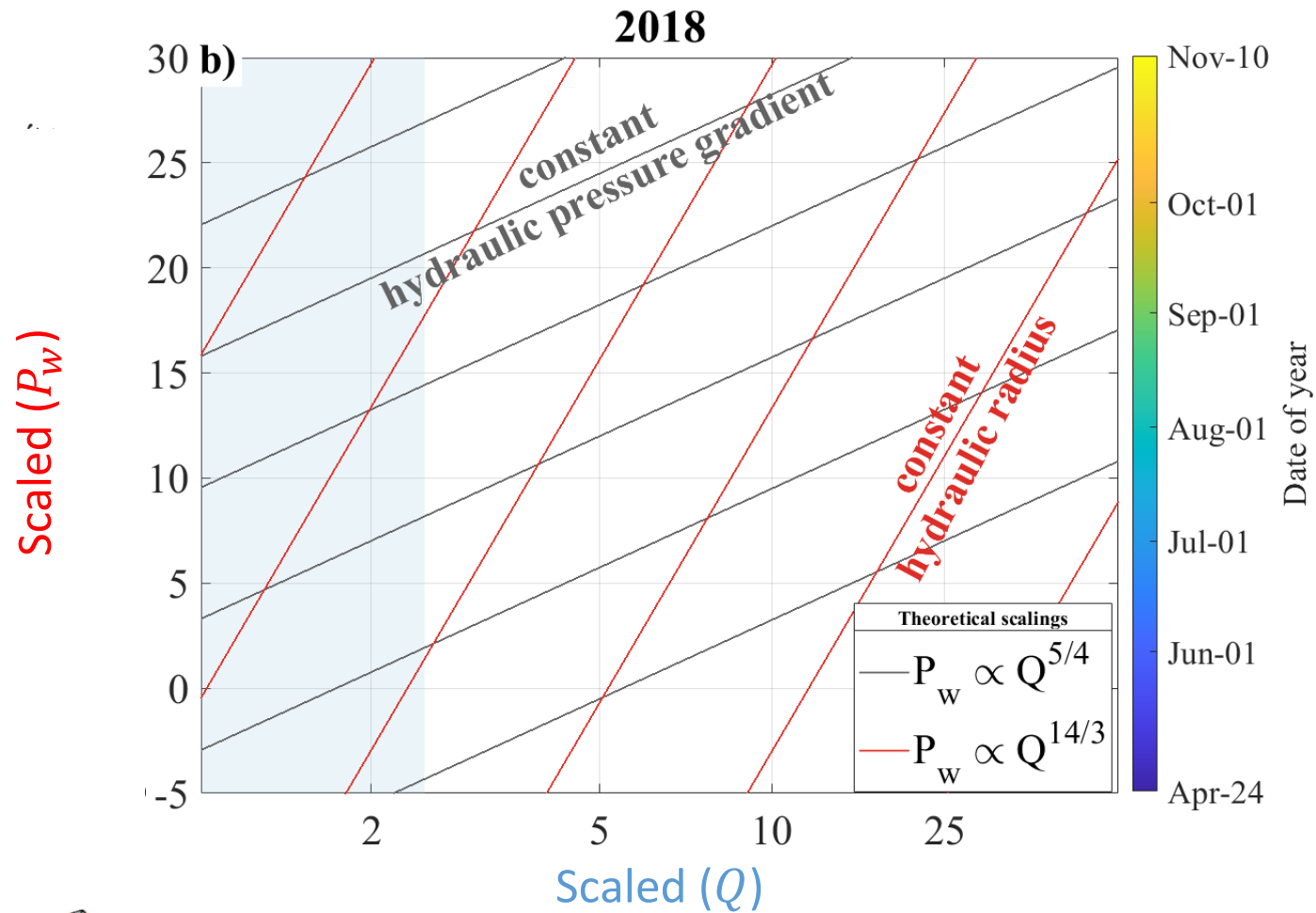
Log-Log representation



scaled ( $Q$ )

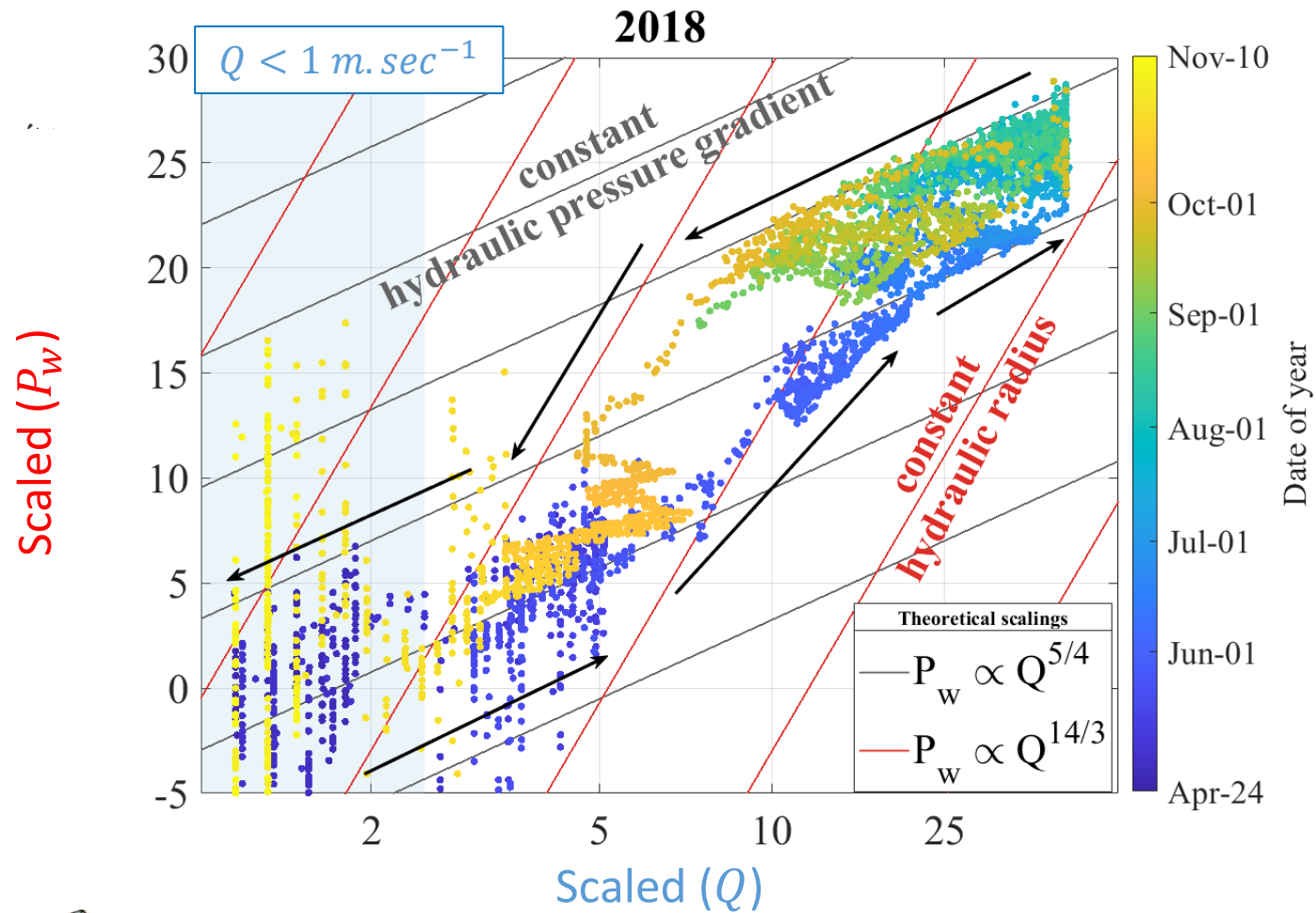
scaled ( $P_w$ )

# Trends at seasonal scales



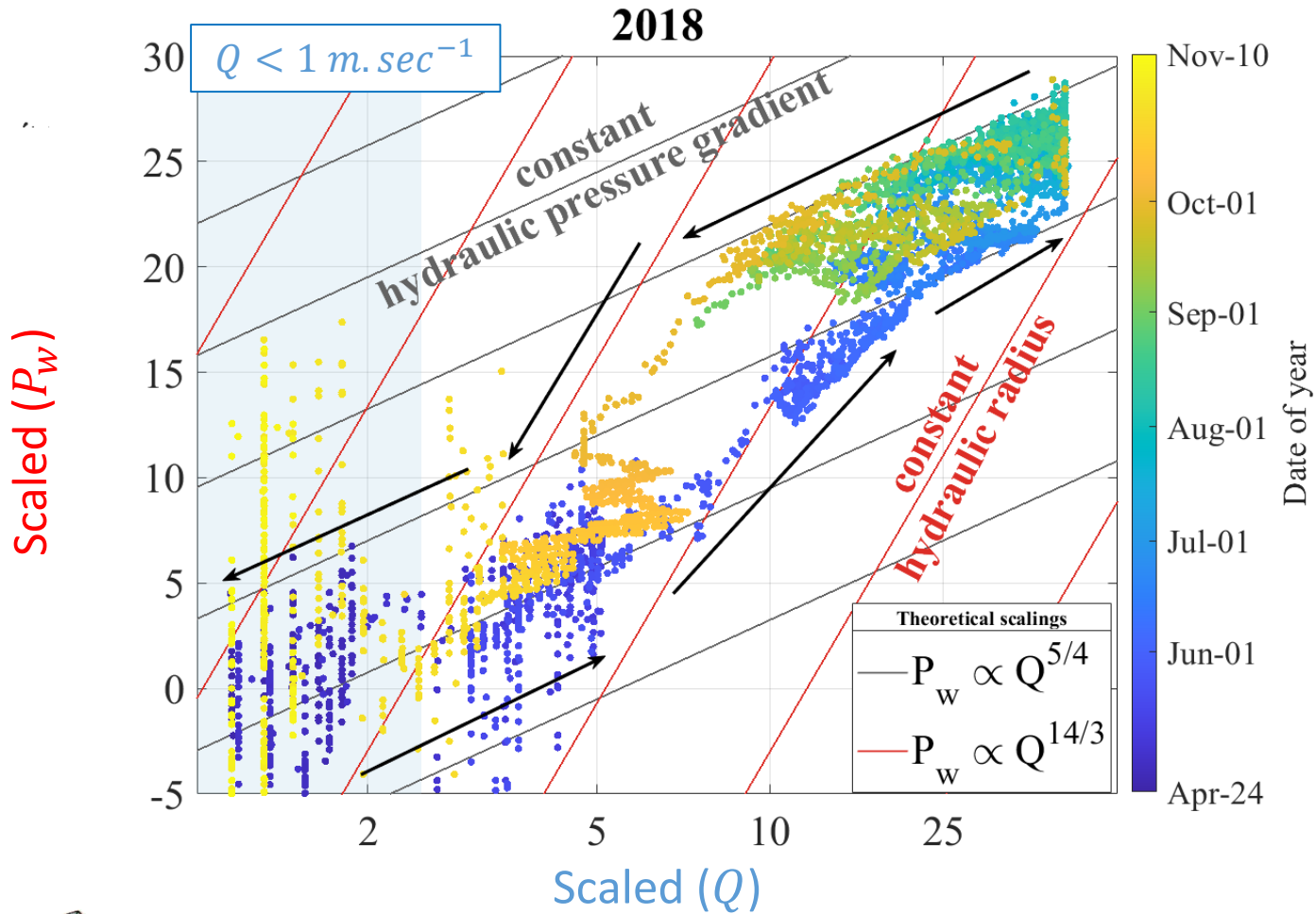


# Trends at seasonal scales



- Consistency between observations and predictions

# #1 | USED SEISMOLOGY TO STUDY COMPLETE MELT SEASON



- Consistency between observations and predictions

Now invert hydraulic properties  $S$  and  $R$

$$Q \sim R^{2/3} S^{1/2}$$

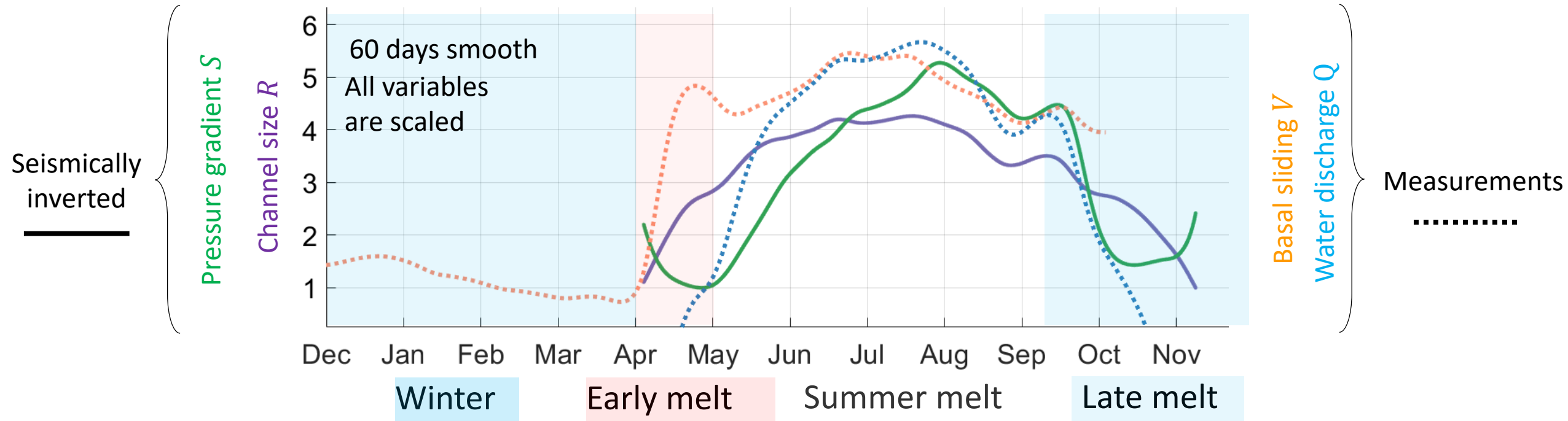
$$P_w \sim R^{7/3} S^{7/3}$$

(Gimbert et al., 2016)

(Nanni et al., 2020)

# Inversion of hydraulic properties

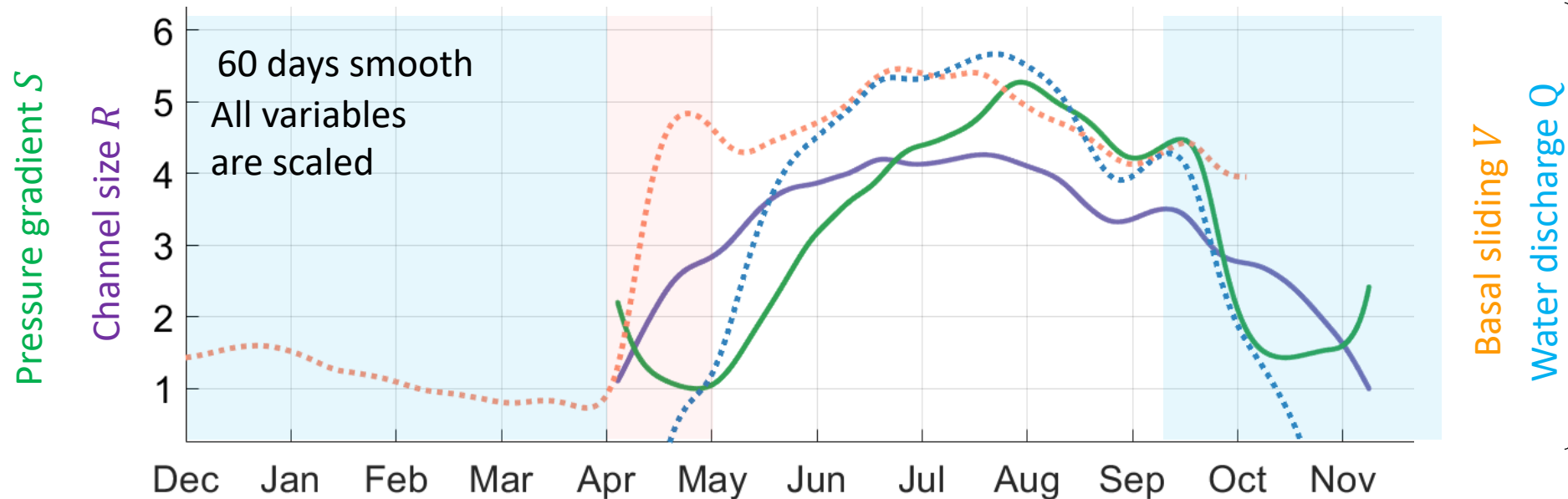
Melt season of 2018



(Nanni et al., 2020)

# Inversion of hydraulic properties

Melt season of 2018



Winter

$V \rightarrow$

Early melt

$V \nearrow$   
 $R \nearrow$   
 $S \searrow$

Summer melt

$V \rightarrow$   
 $R \rightarrow$   
 $S \nearrow$

Late melt

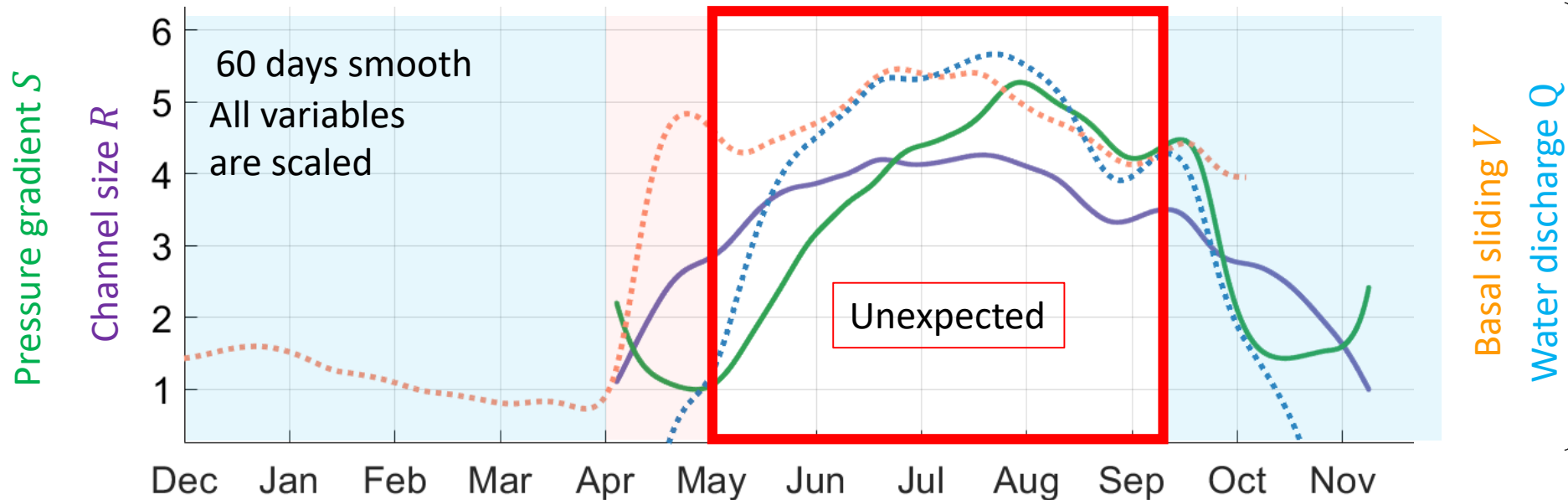
$V \searrow$   
 $R \searrow$   
 $S \searrow$

Well-marked seasonality

(Nanni et al., 2020)

# #2 | SUCCESSFULLY INVERTED HYDRAULIC PROPERTIES

Melt season of 2018



Winter

Early melt

Summer melt

Late melt

$V$  →

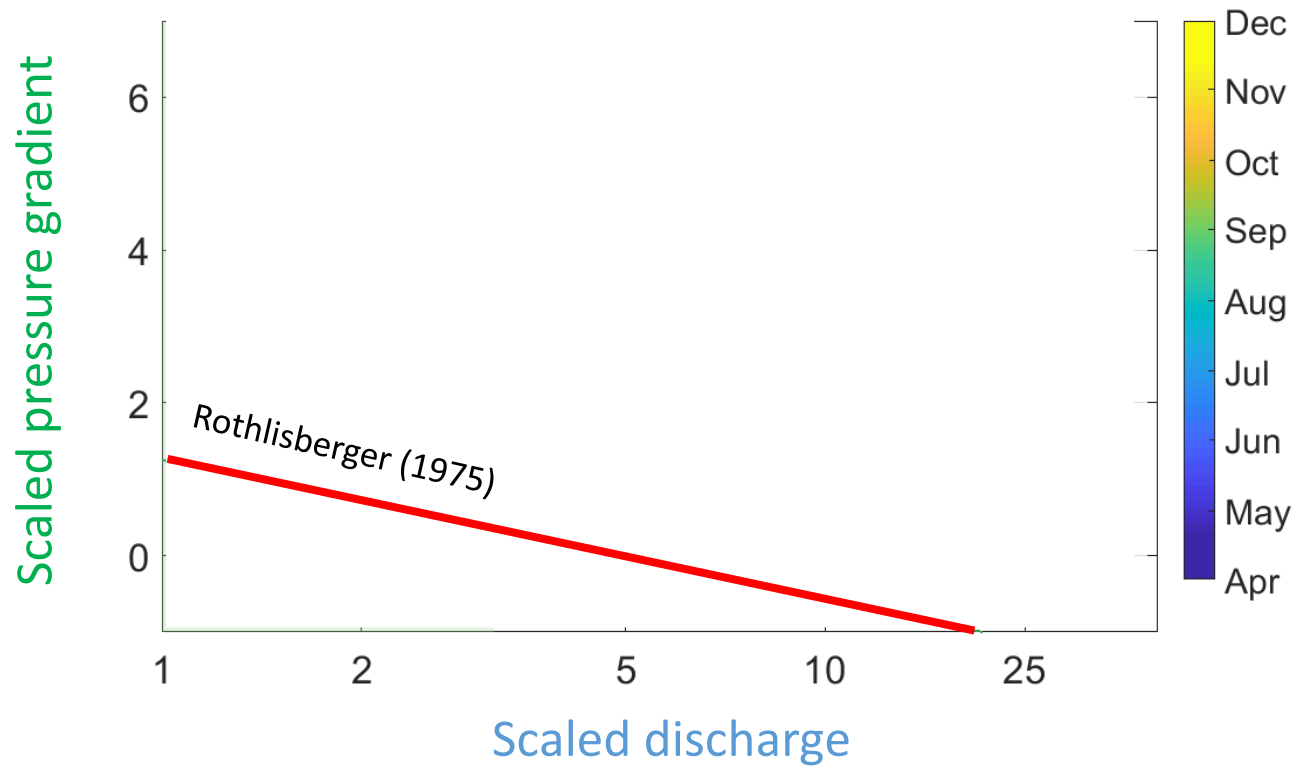
$V$  ↗  
 $R$  ↗  
 $S$  ↘

$S$  ↗

$V$  ↘  
 $R$  ↘  
 $S$  ↘

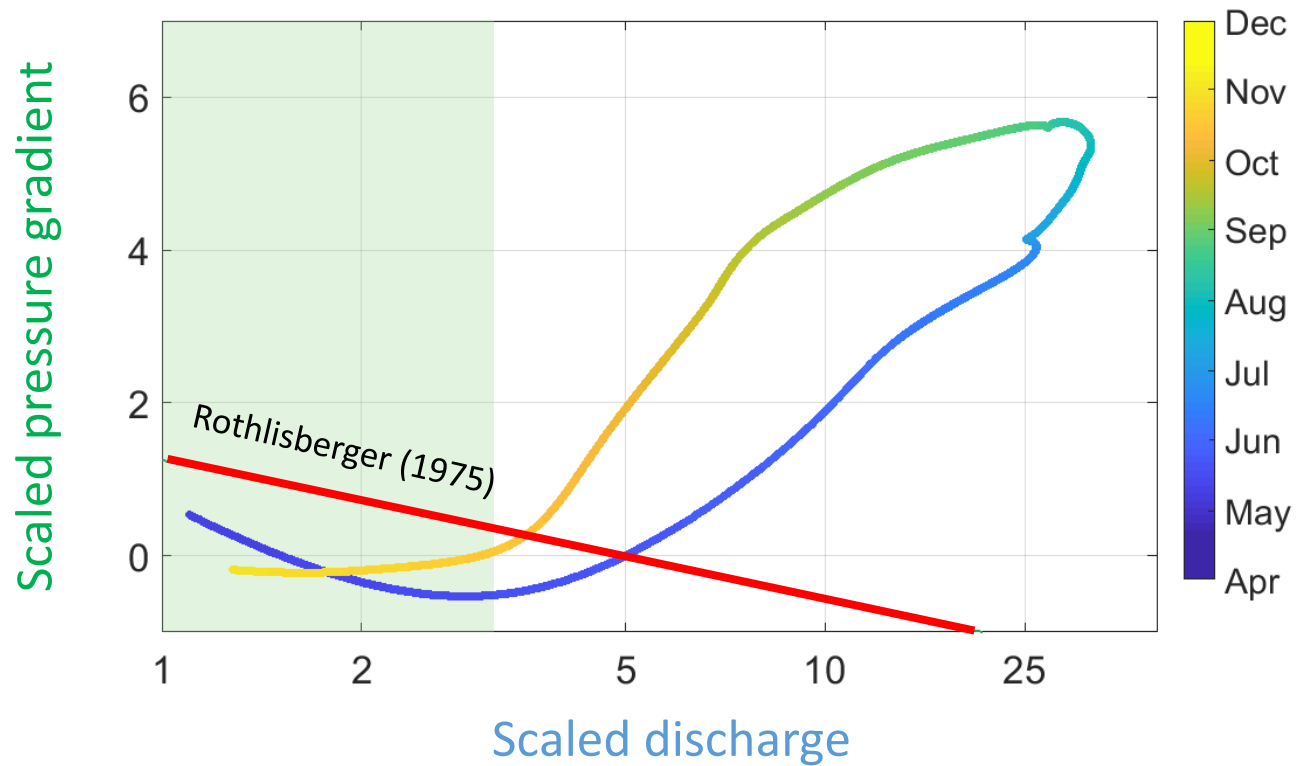
Well-marked seasonality

# Channel dynamics: theory



- Steady-state and equilibrium prediction for channel dynamics by Rothlisberger (1975)

# Channel dynamics: theory VS observation



- Steady-state and equilibrium prediction for channel dynamics by Rothlisberger (1975)
- Out of equilibrium and **pressurized** at high discharge

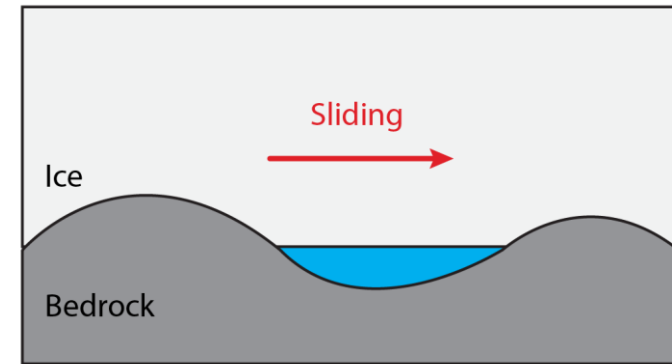
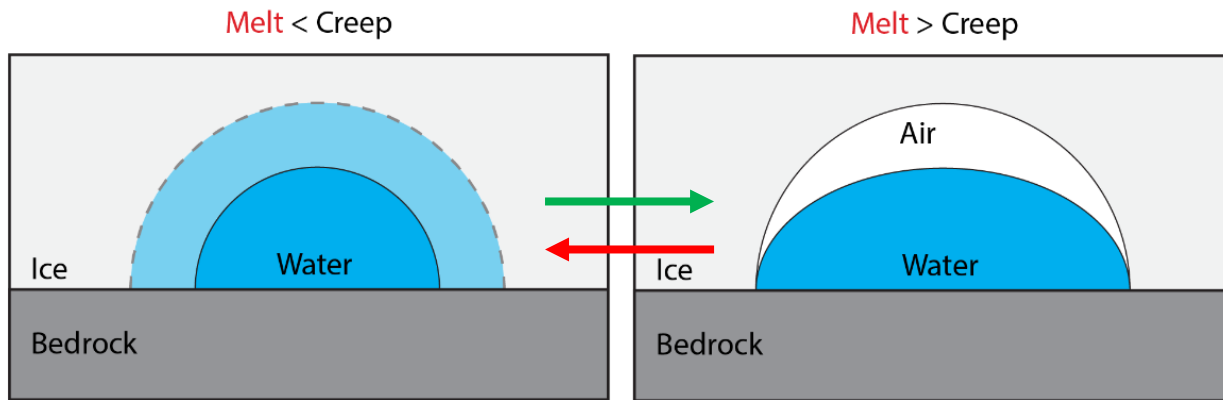
(Nanni et al., 2020)

# Potential cause(s) for high pressure in summer

Short term water input =  
Transient state

or/and

Cavities dominate the  
seismic power ?



Kinetics of water supply > channel's response time

Cavities might be pressurized

*Previously thought to be noise-free*

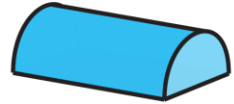


# Part II: Spatial investigation of subglacial water flow

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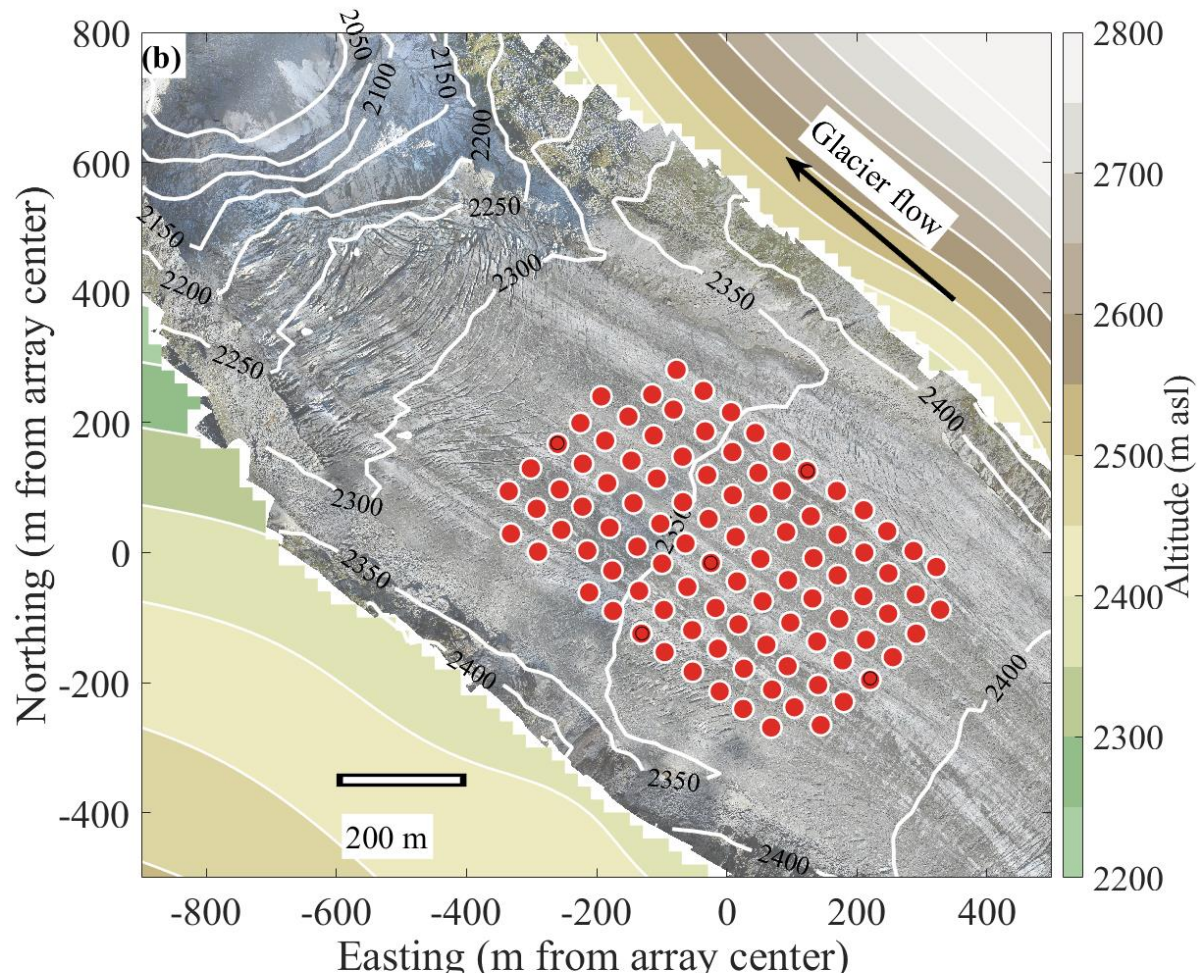
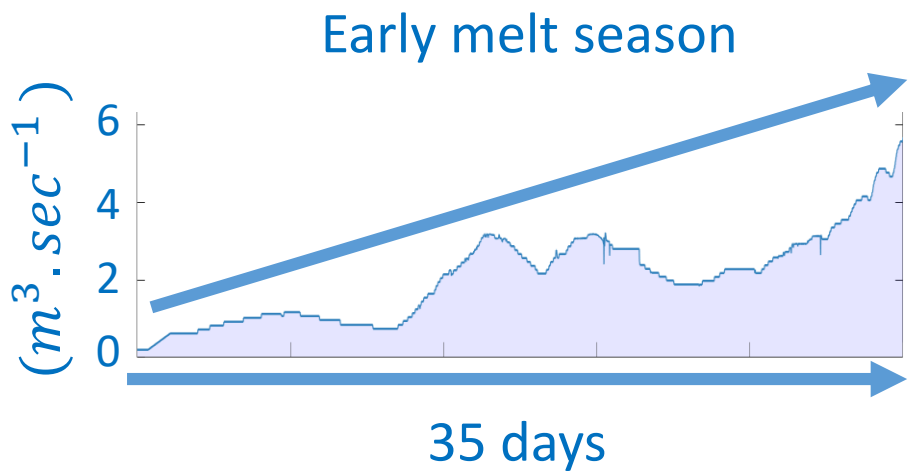
**#3** Can we **LOCATE** distributed sources of seismic noise?



**#4** What is the **SPATIAL** dynamics of cavities and channels?



# Measurements: 98 seismic sensors

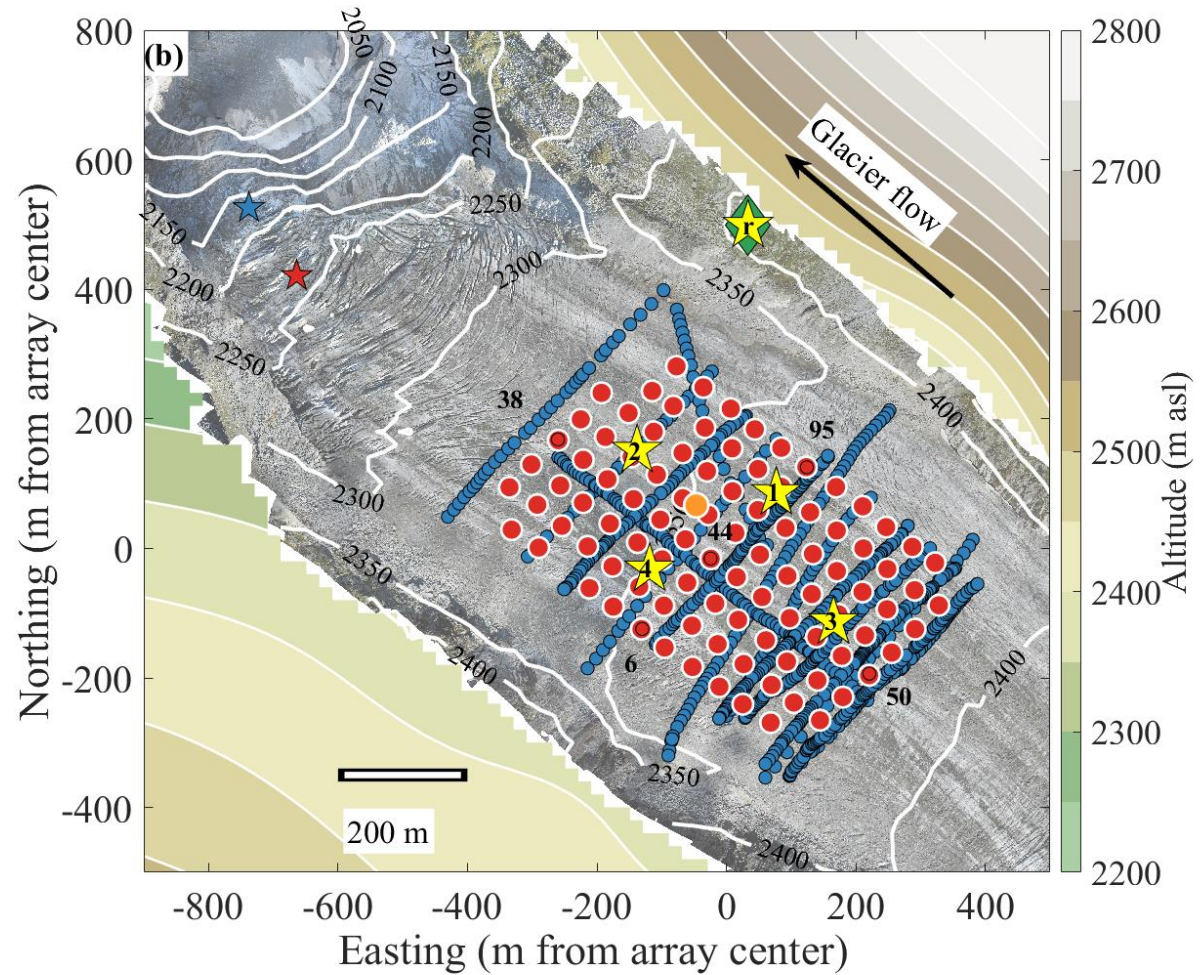


(Gimbert, Nanni, Roux et al., 2020)

# The RESOLVE-Argentière project



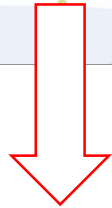
- | Seismic measurements       |                              |
|----------------------------|------------------------------|
| ●                          | Nodes sensors                |
| ●                          | Surface borehole seismometer |
| Complementary measurements |                              |
| ★                          | GNSS antennas                |
| ●                          | GPR tracks                   |
| ★                          | Subglacial wheel             |
| ◆                          | Weather station              |
| ★                          | Water discharge gauge        |



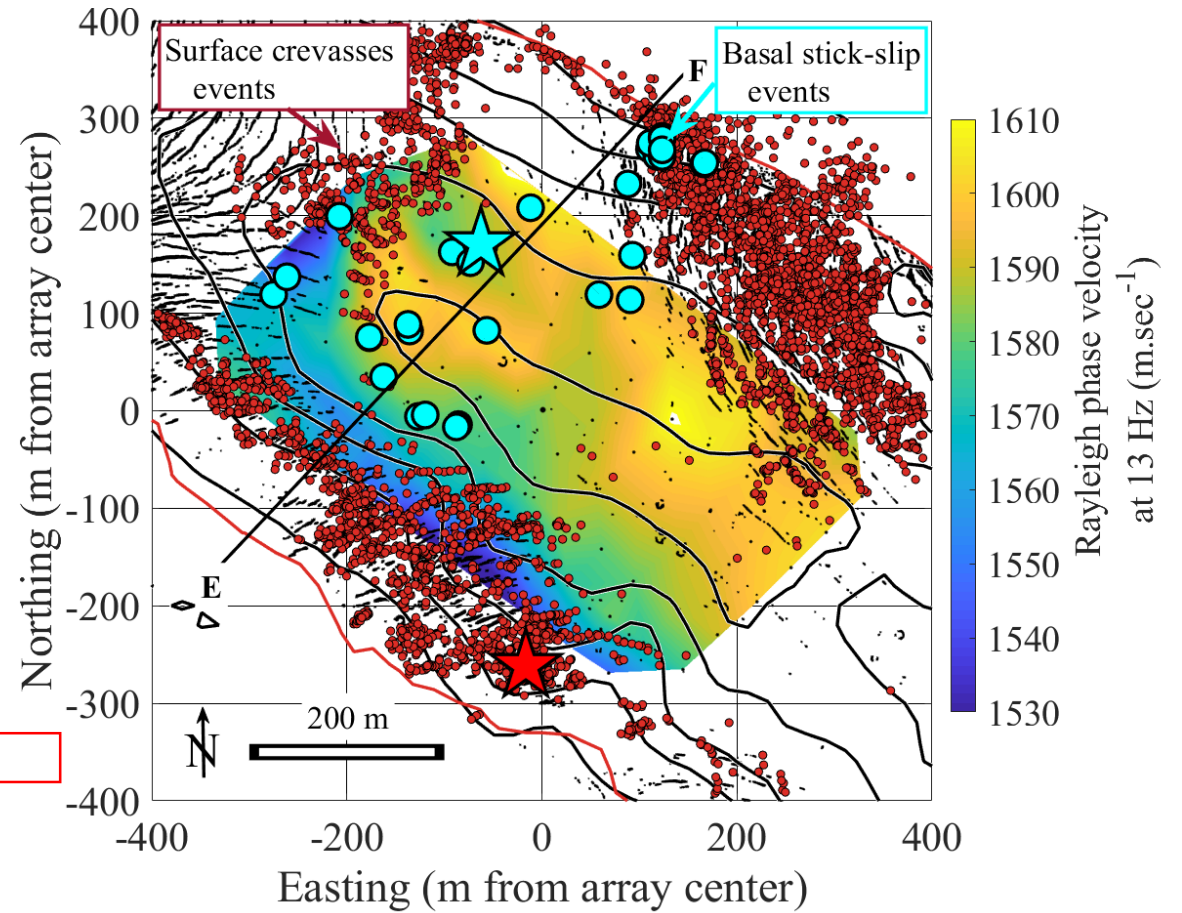
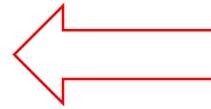
Add  
RESOLVE  
paper

(Gimbert, Nanni, Roux et al., 2020)

# The RESOLVE-Argentière project

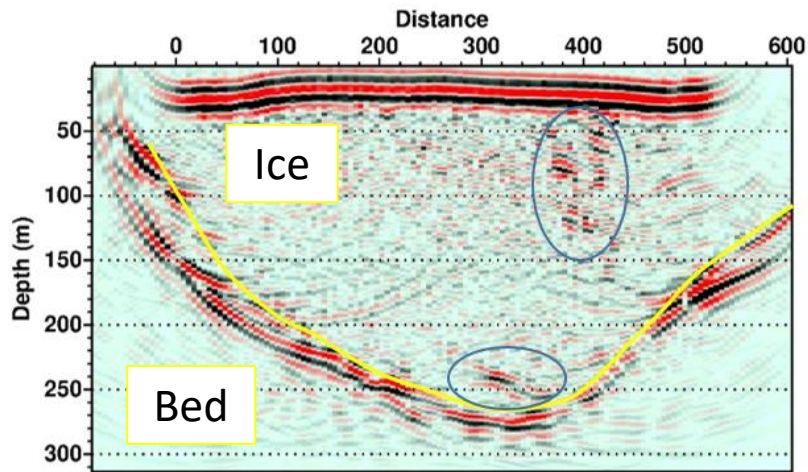


A wide range of **seismic analysis** presented in our community paper.

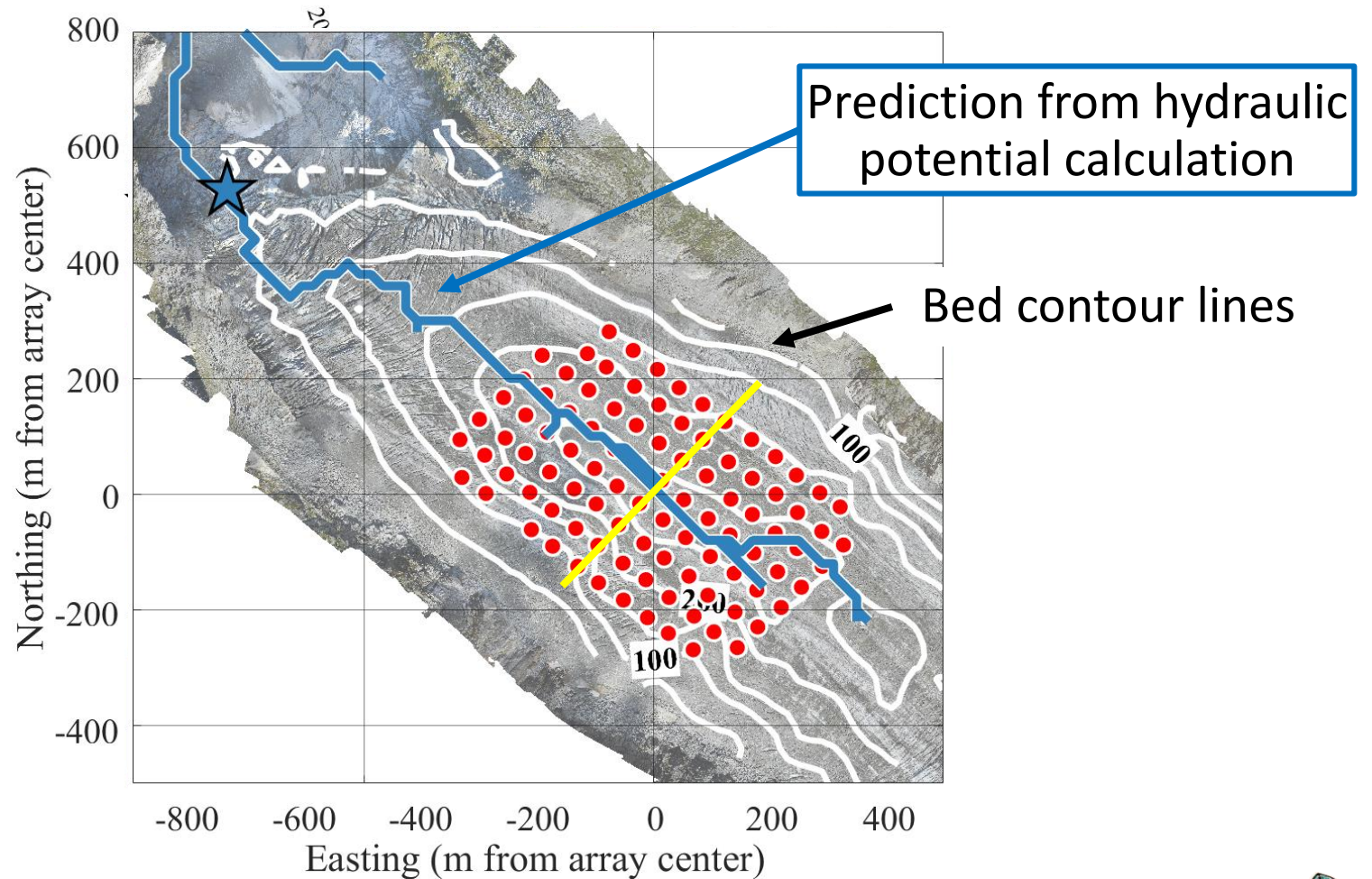


(Gimbert, Nanni, Roux et al., 2020)

# Glacier geometry and waterways



GPR imaging results



(Gimbert, Nanni, Roux et al., 2020)

# How to locate **distributed** noise sources ?

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Very few studies ...

*Venkatesh et al., 2003; Stehly et al., 2006; Burtin et al., 2010; Corciulo et al., 2013;  
Chmiel et al., 2019*

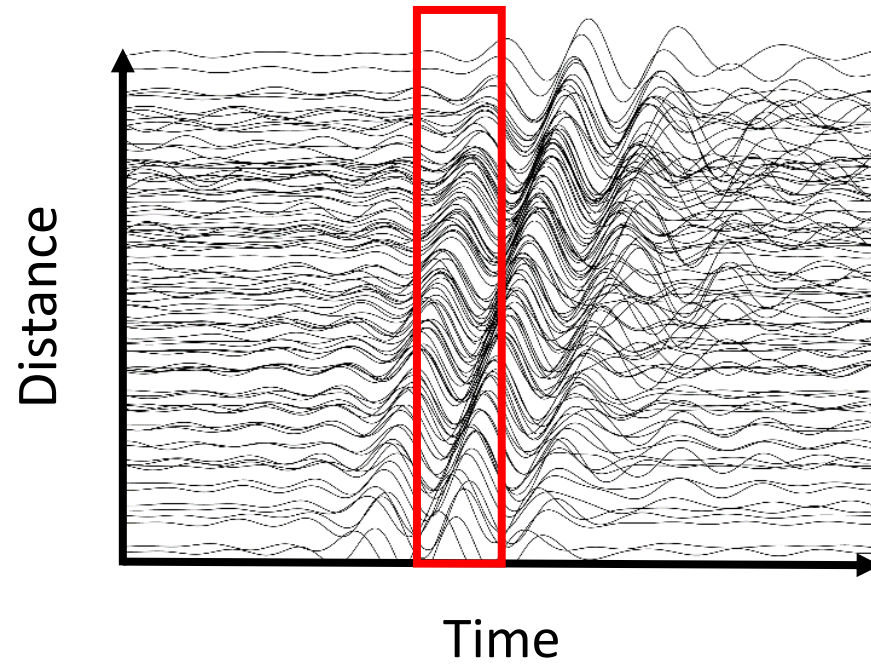
# How to locate **punctual** sources ?

$$u(t) = Ae^{i\omega t}$$

Amplitude      Phase



Phase differences ~ time delays



# Phase coherence for a punctual source

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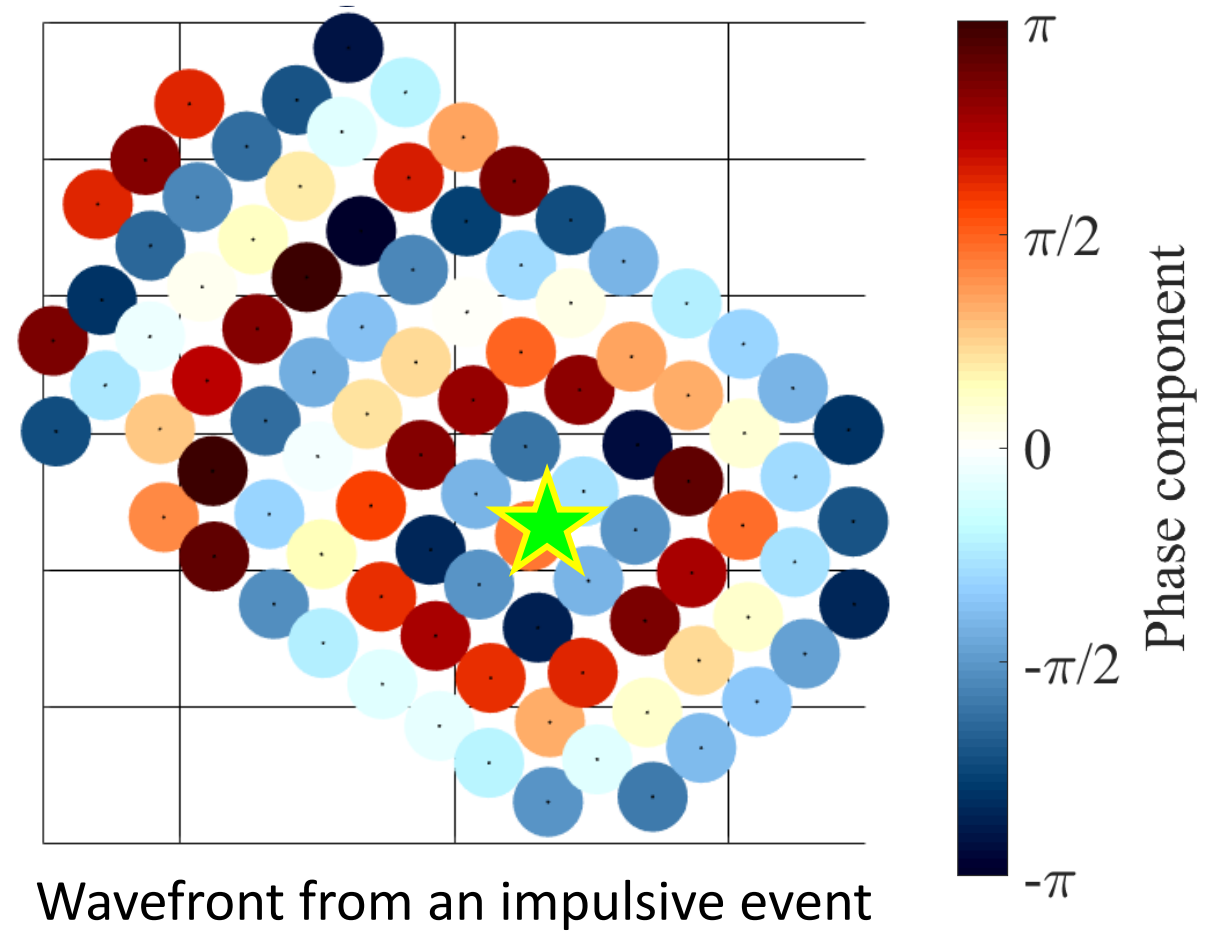
Wavefront when throwing  
a stone in a lake



# Phase coherence for a punctual source



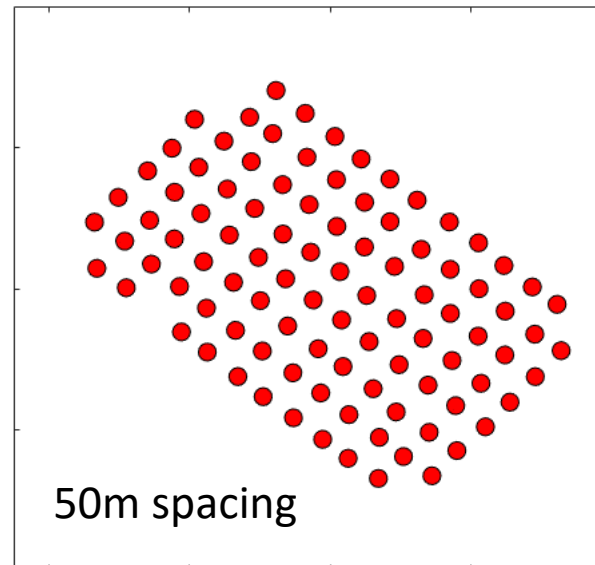
Wavefront when throwing a stone in a lake



# MFP: the Match-field-processing method

- Assume a unique source over 1 second-signal
- Minimize misfit  $|\text{Phase}_{\text{model}} - \text{Phase}_{\text{observed}}|$  (*gradient-based minimization*)

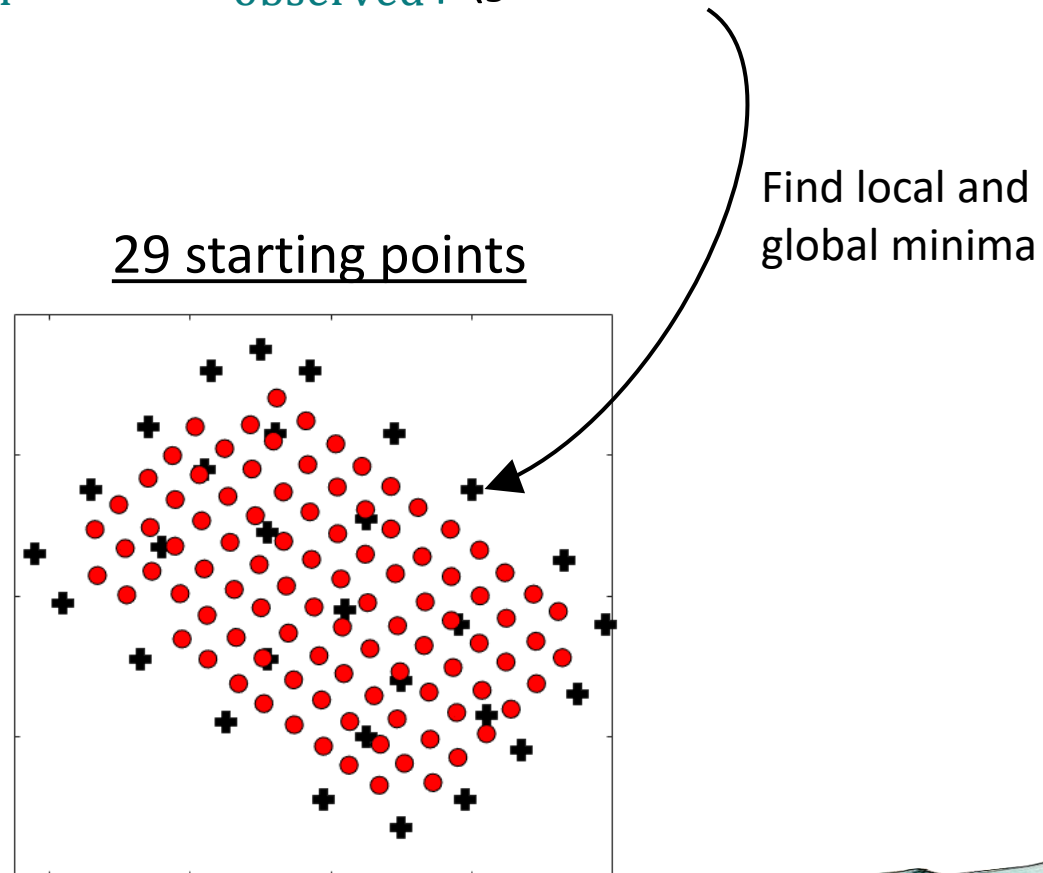
Seismic array



(e.g. Kuperman et al., 1997; Corciulo et al., 2013; Chmiel et al., 2019)

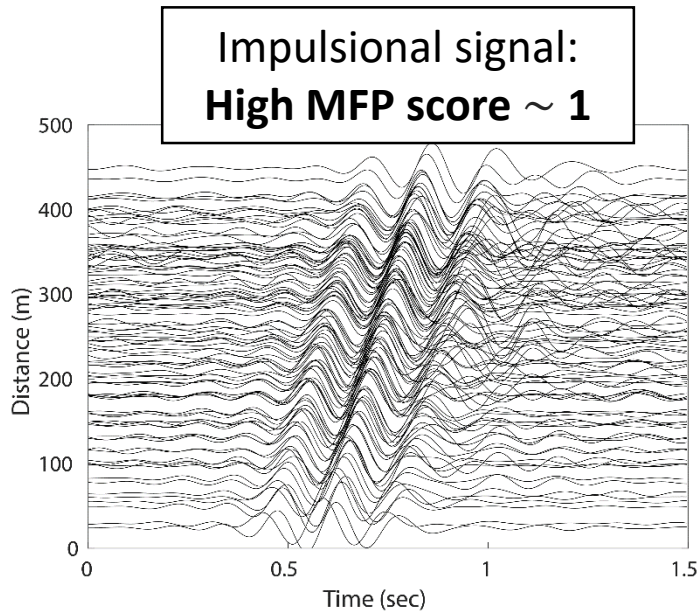
# MFP: the Match-field-processing method

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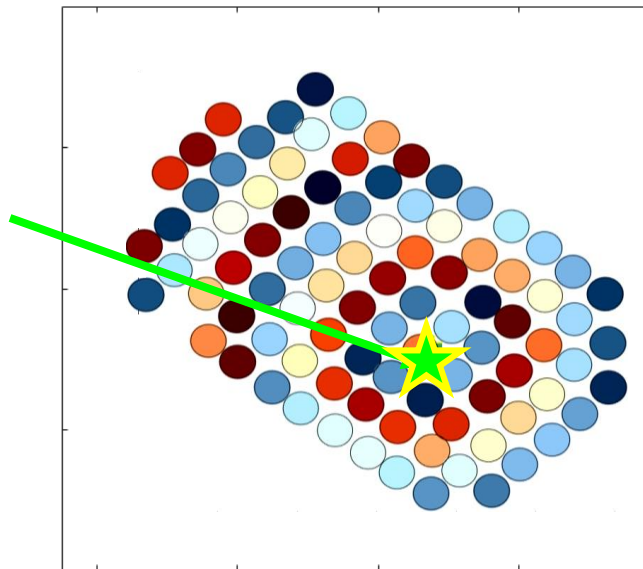


# Punctual source: easy

- Assume a unique source over 1 second-signal
- Minimize misfit  $|\text{Phase}_{\text{model}} - \text{Phase}_{\text{observed}}|$  (*gradient-based minimization*)
- MFP score  $\propto$  phase coherency over the array



Unique location

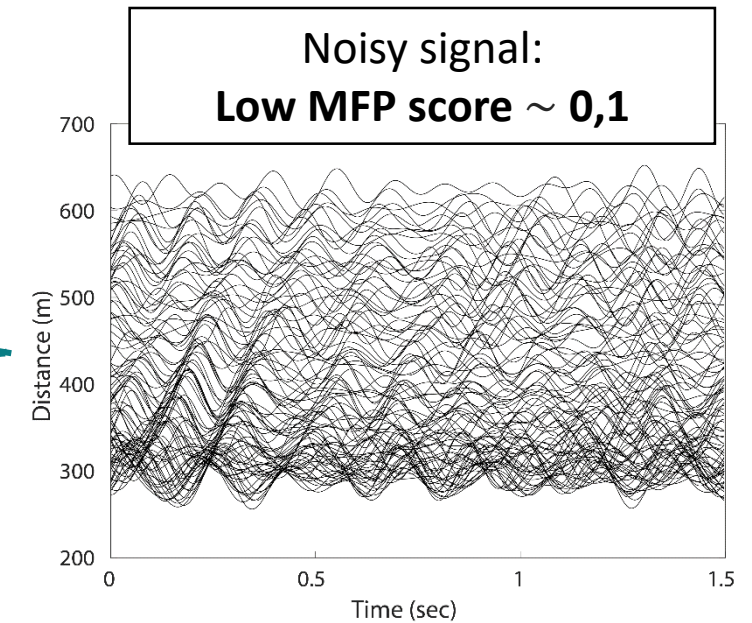
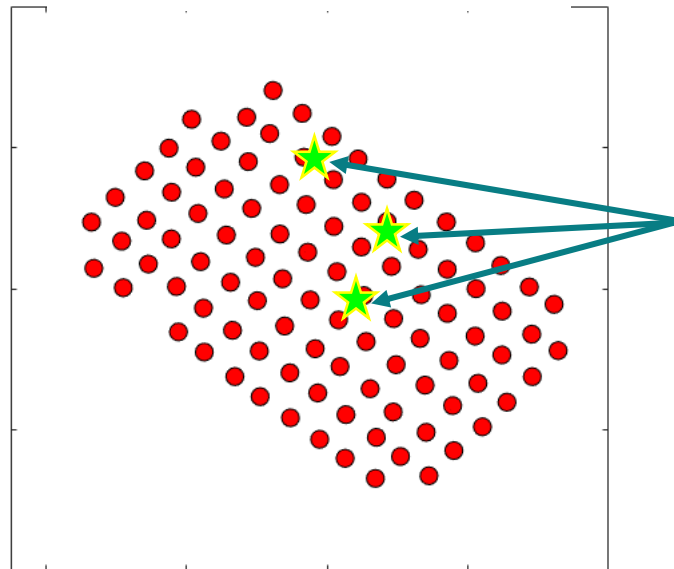


# Distributed sources: tricky

- Assume a unique source over 1 second-signal
- Minimize misfit  $|\text{Phase}_{\text{model}} - \text{Phase}_{\text{observed}}|$  (*gradient-based minimization*)
- MFP score  $\propto$  phase coherency over the array

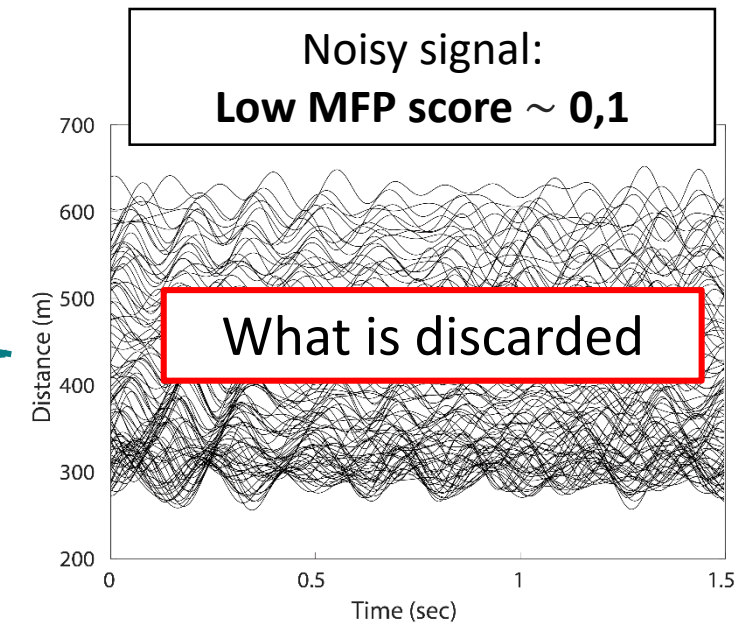
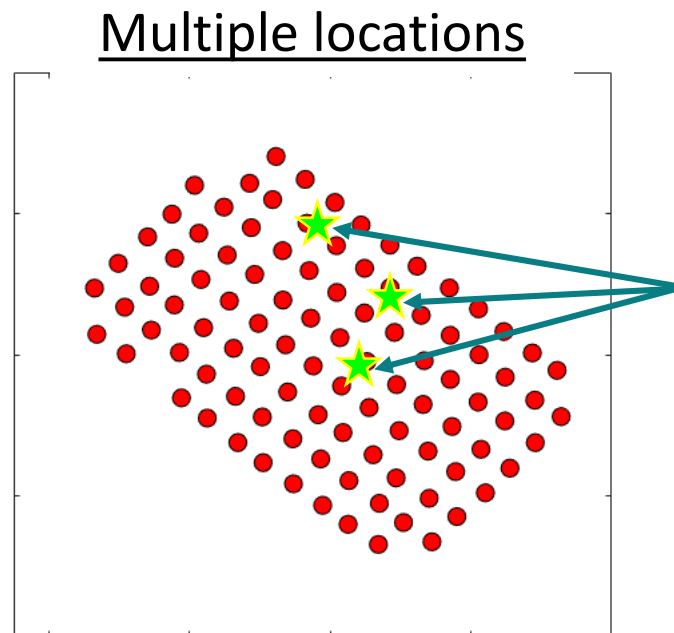
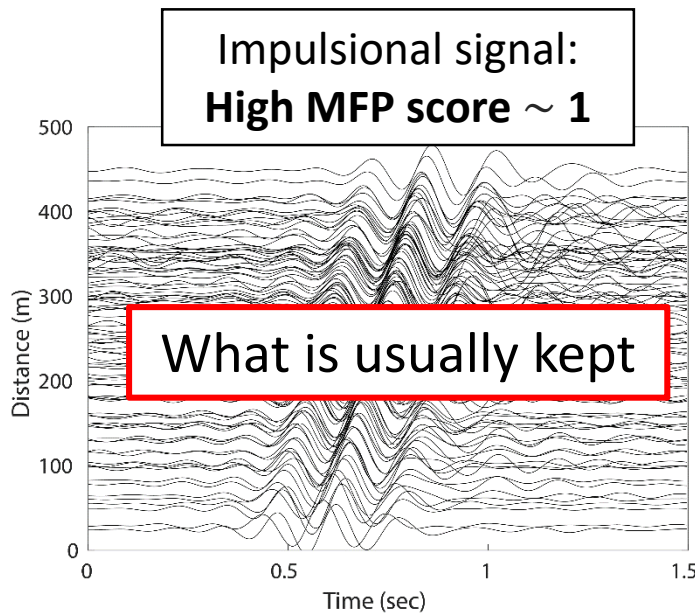


Multiple locations



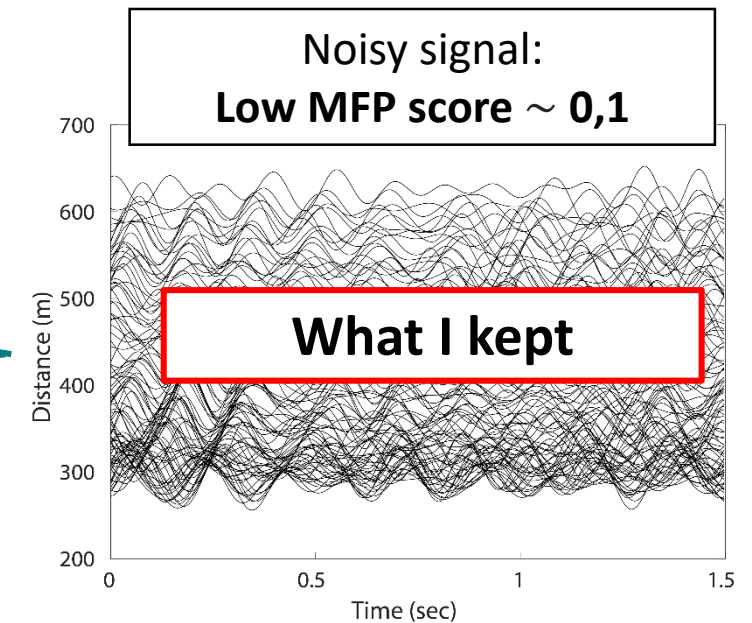
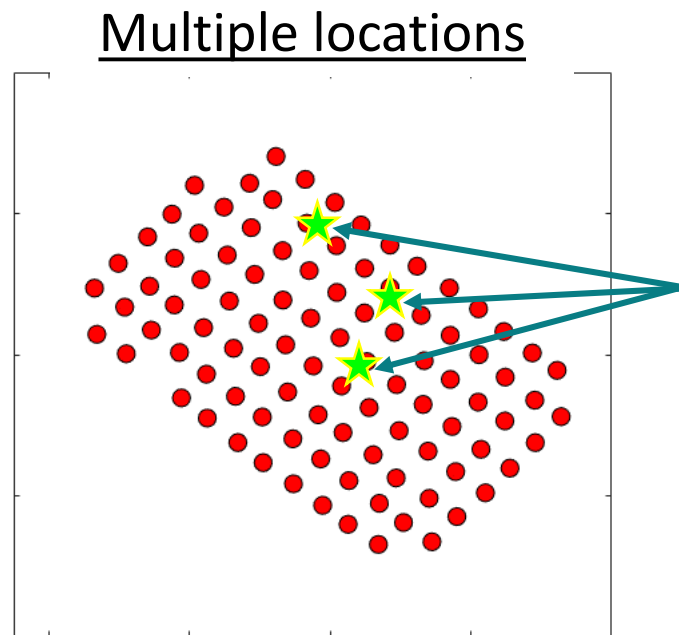
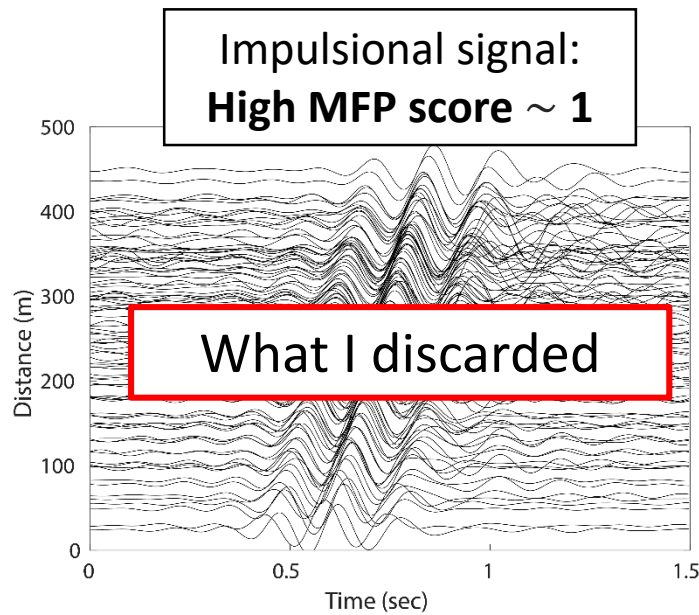
# Distributed sources: tricky

- Assume a unique source over 1 second-signal
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- MFP score  $\propto$  phase coherency over the array



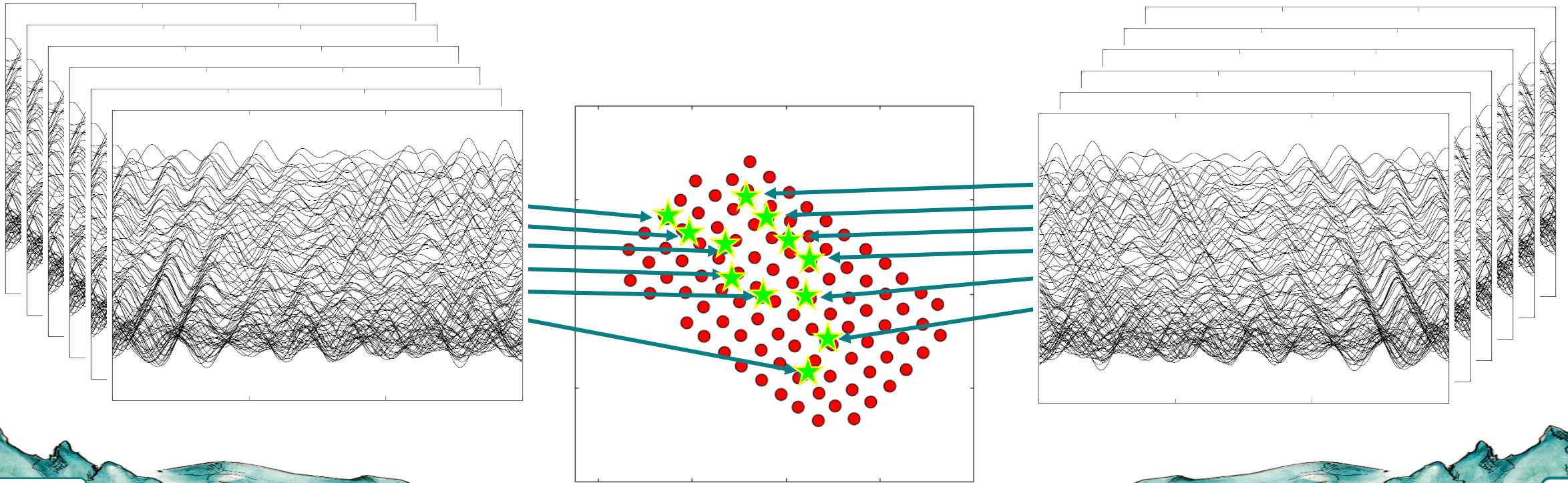
# A CONCEPTUAL ADVANCE!

- Assume a unique source over 1 second-signal
- Minimize misfit  $|\text{Phase}_{\text{model}} - \text{Phase}_{\text{observed}}|$  (gradient-based minimization)
- MFP score  $\propto$  phase coherency over the array



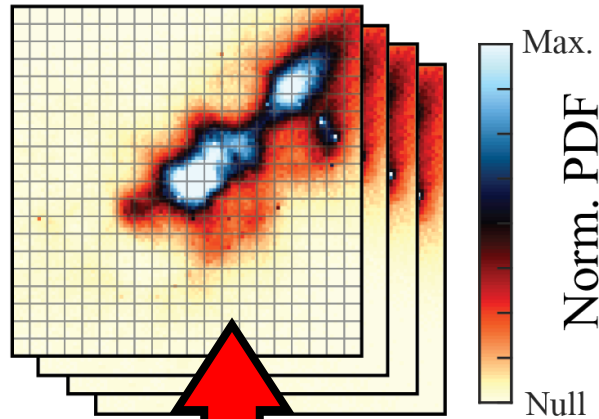
## A CONCEPTUAL ADVANCE!

- Subglacial water flow: **low MFP** score (several sources are active simultaneously)
- I stack each 1 second-location over long time periods ( $\sim$  days)

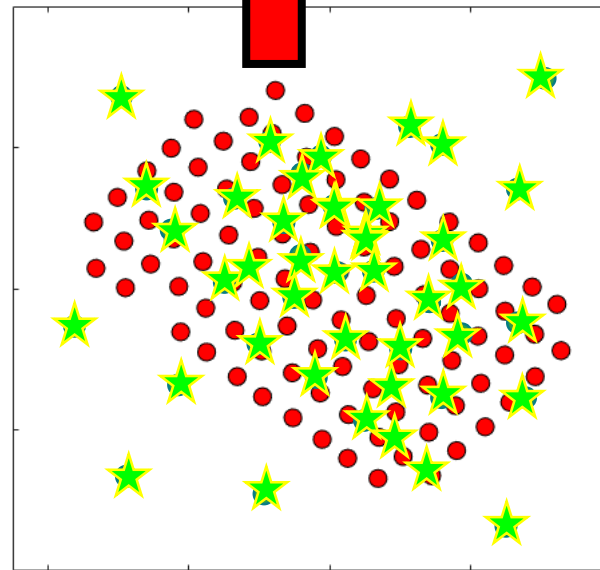




# Making density probability maps



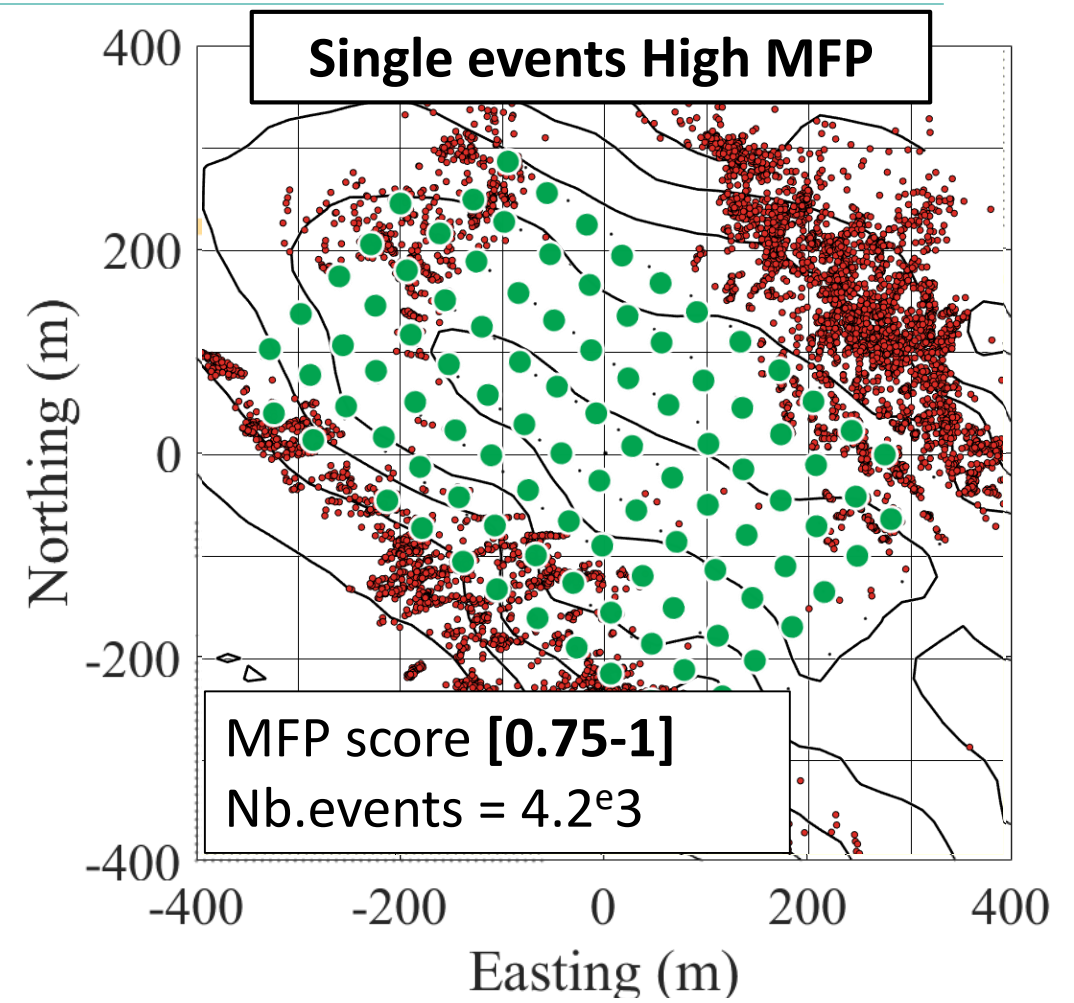
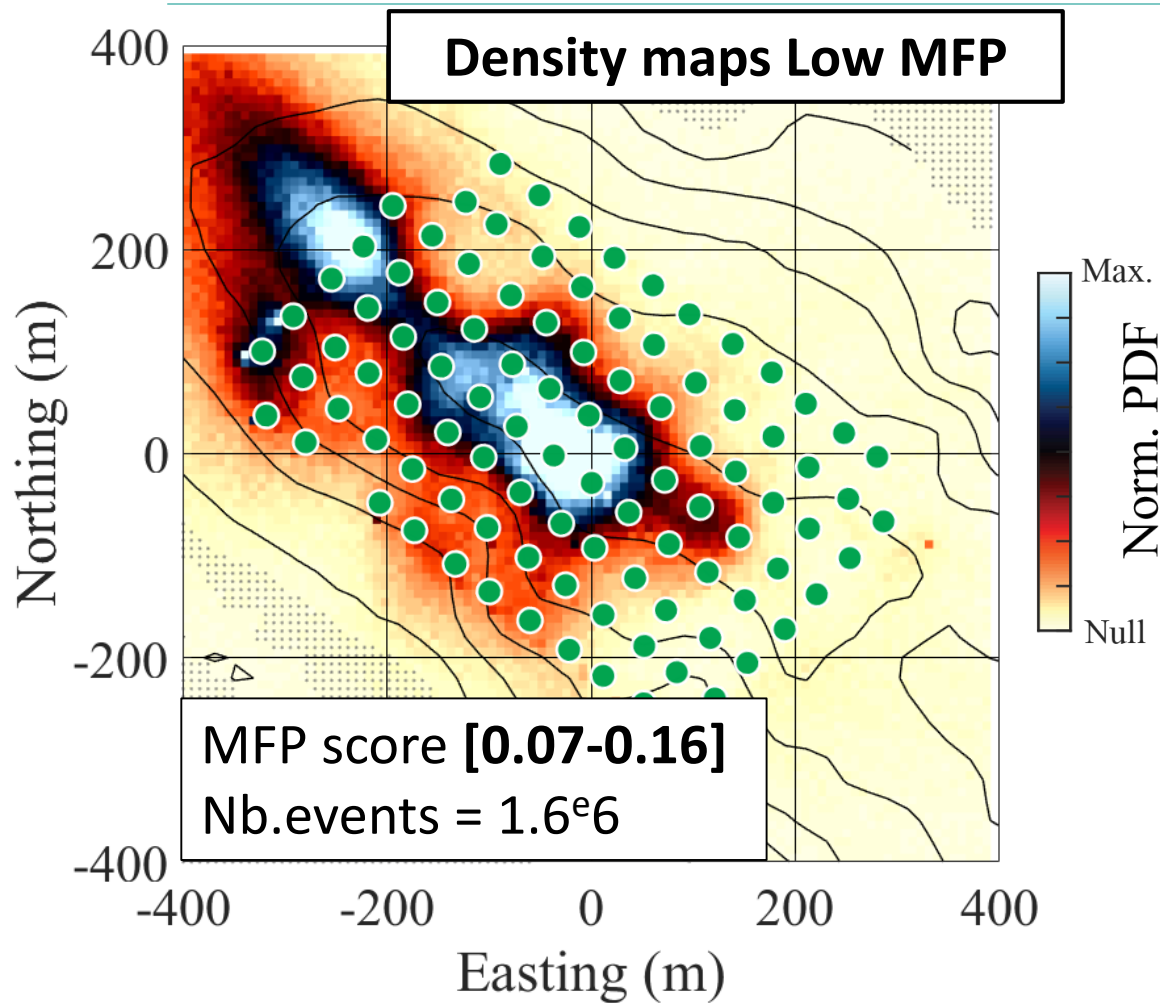
Up to 50+ millions potential locations per day



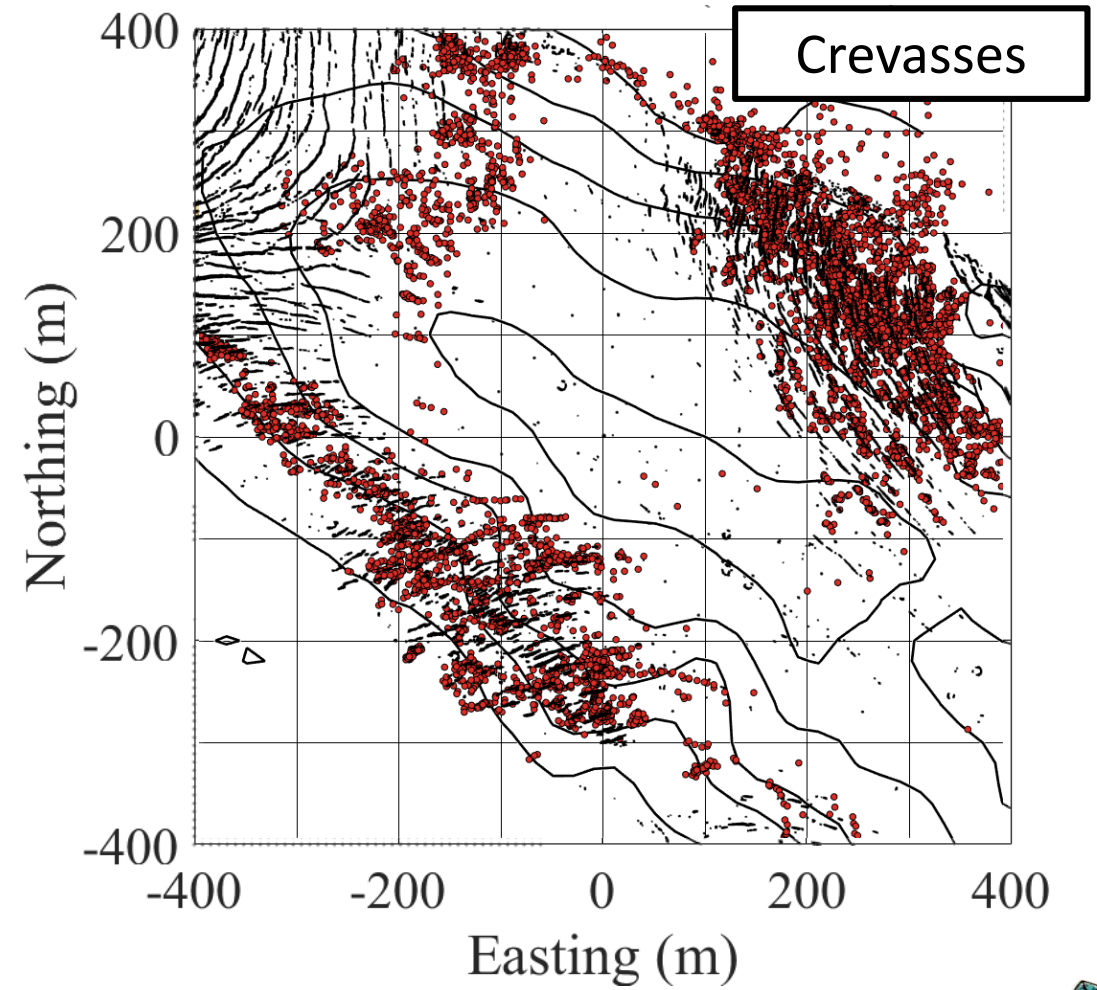
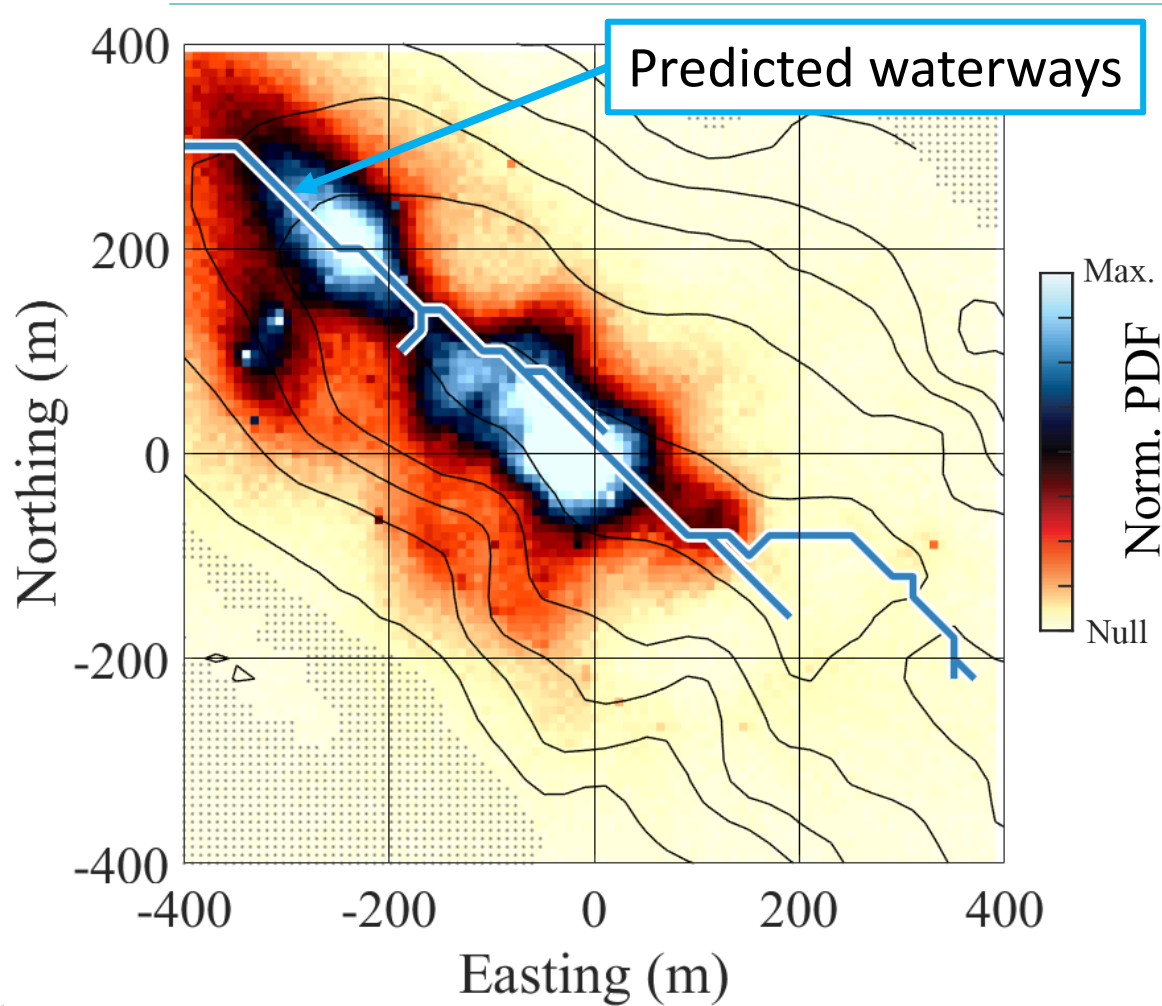
I selected realistic values:

- Phase velocity  
[1500-3600 m.sec<sup>-1</sup>]
- Source positions  
± 400m from array center in (x,y,z)

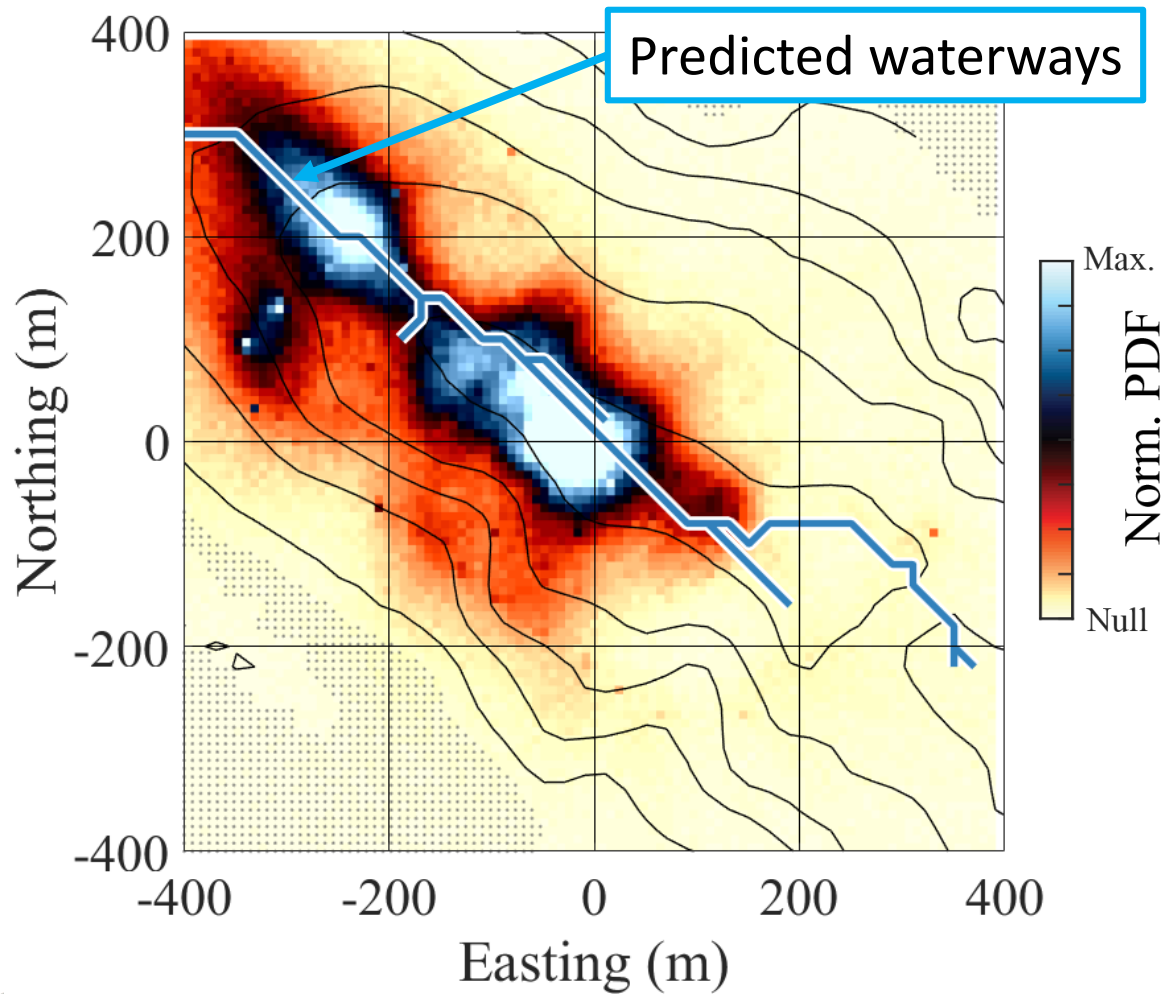
# Patterns of noise and punctual sources



# Patterns of noise and punctual sources

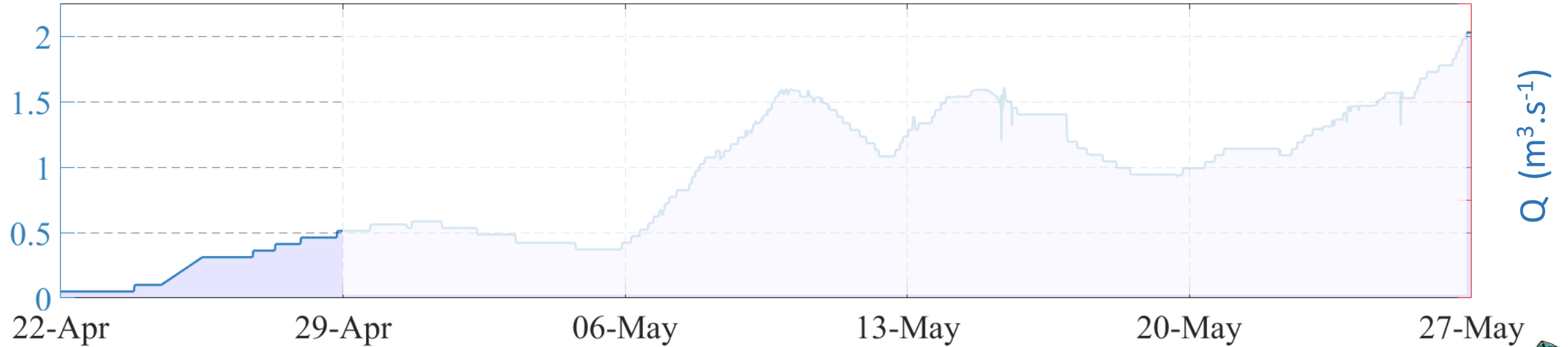
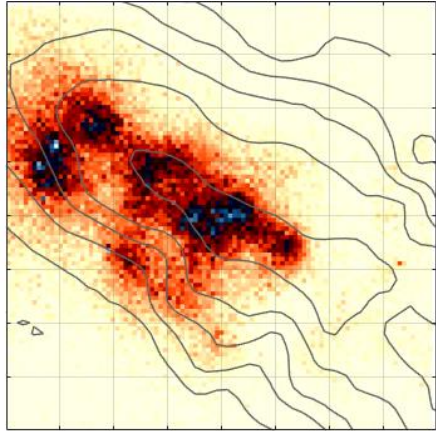


# #3 I AM CAPABLE OF LOCATING SUBGLACIAL WATER FLOW

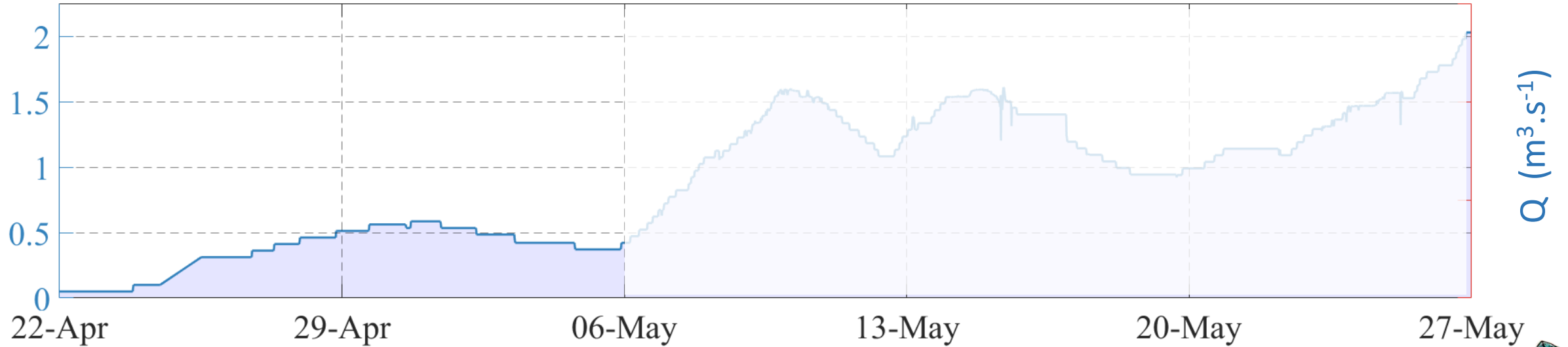
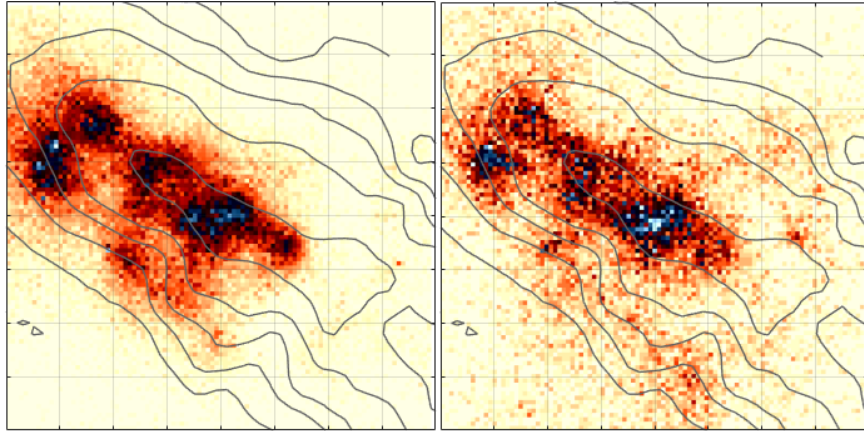


- Along-flow geometry
- ~ 50m width of source location
  - Due to seismic wavelength? (300m at 5Hz)
  - Spread sources?

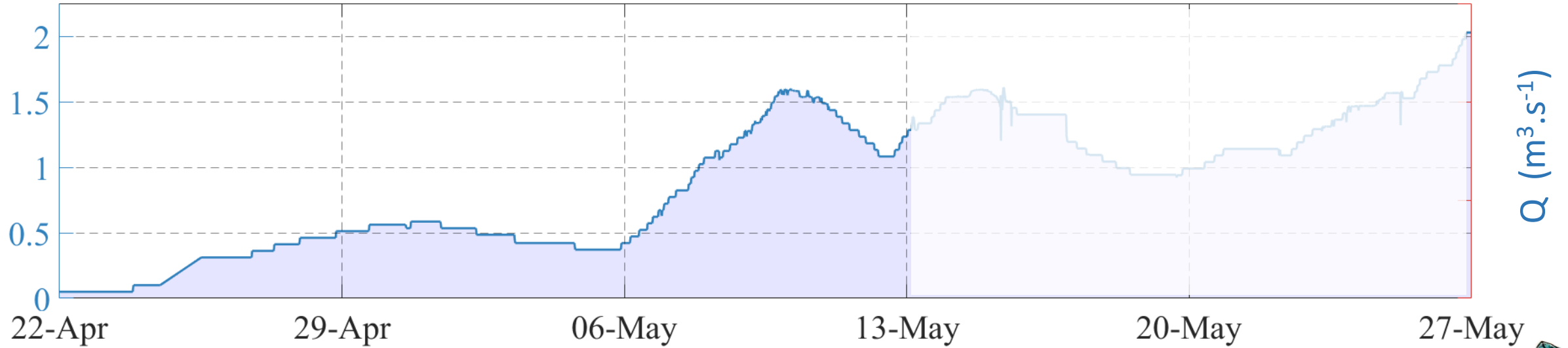
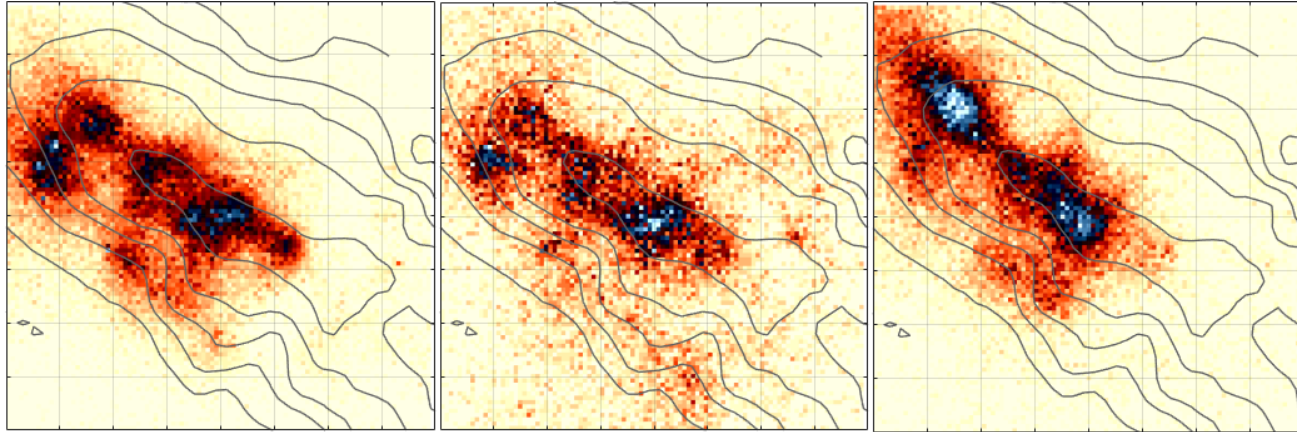
# Spatio-temporal dynamics



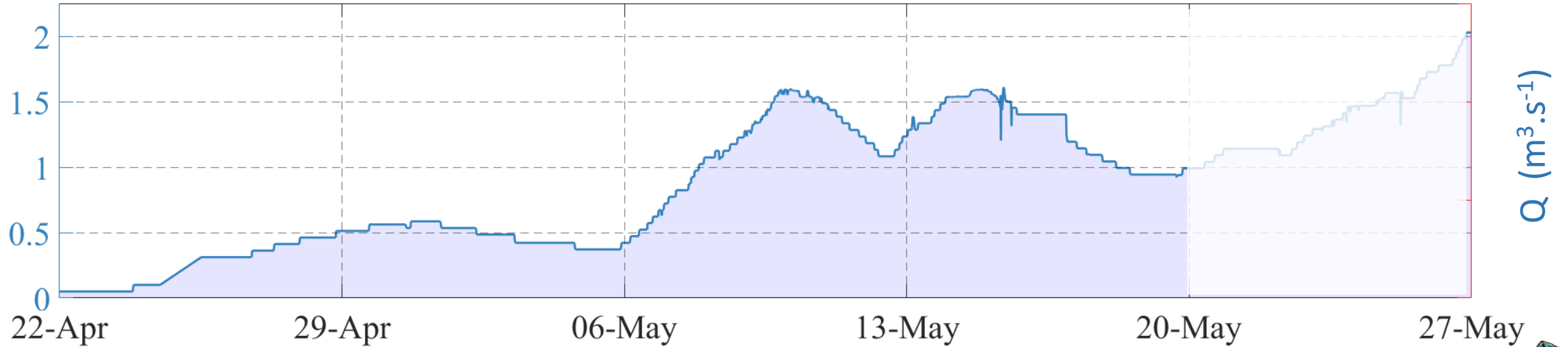
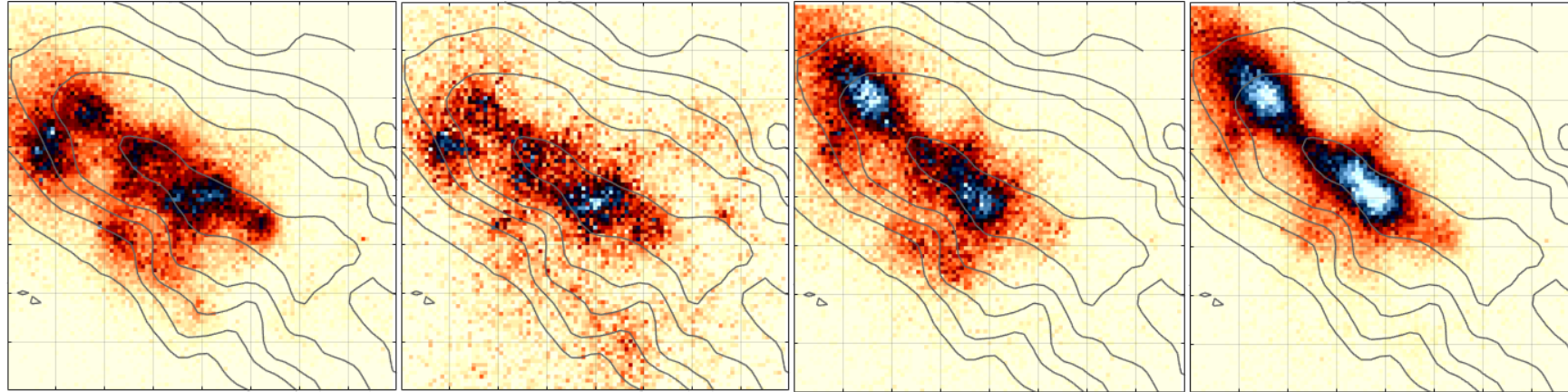
# From distributed ...



# From distributed ...

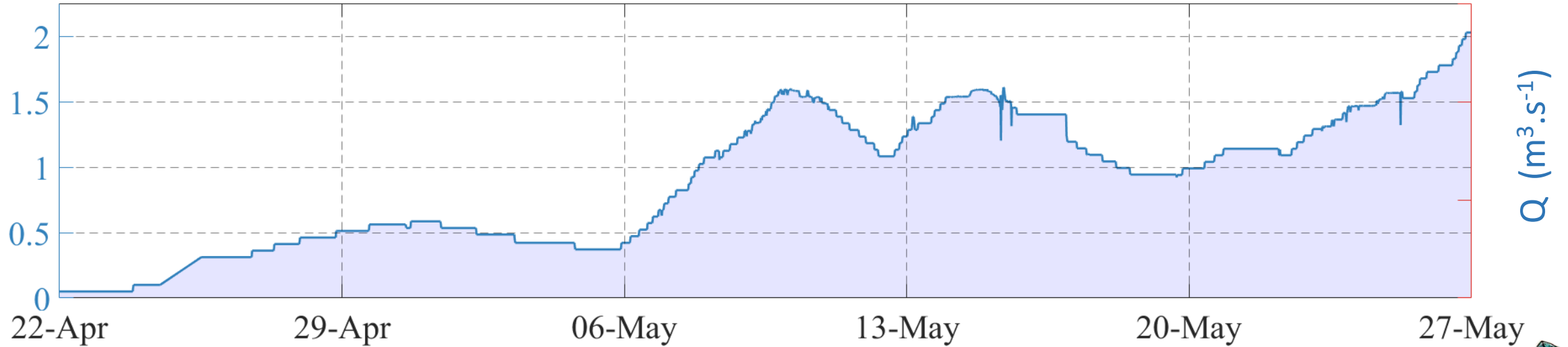
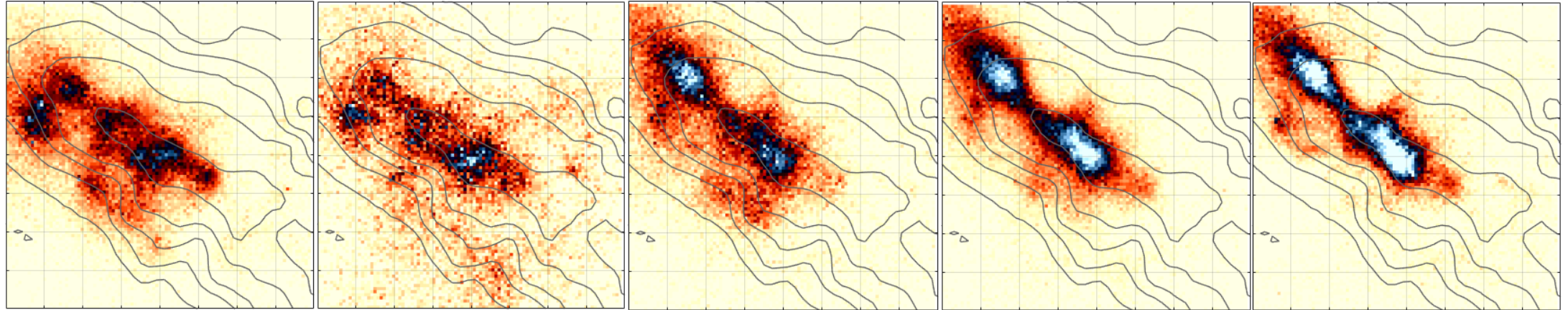


# From distributed ... to localized

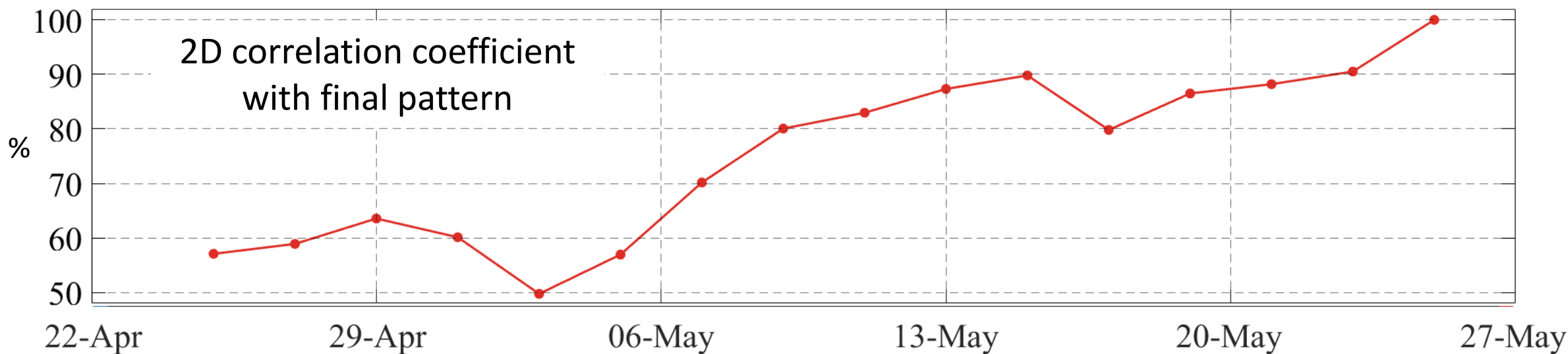
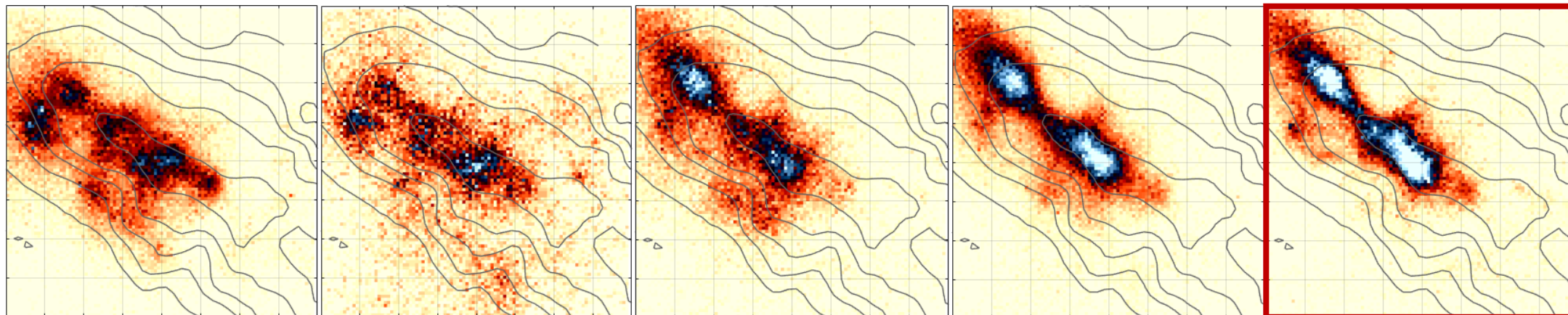




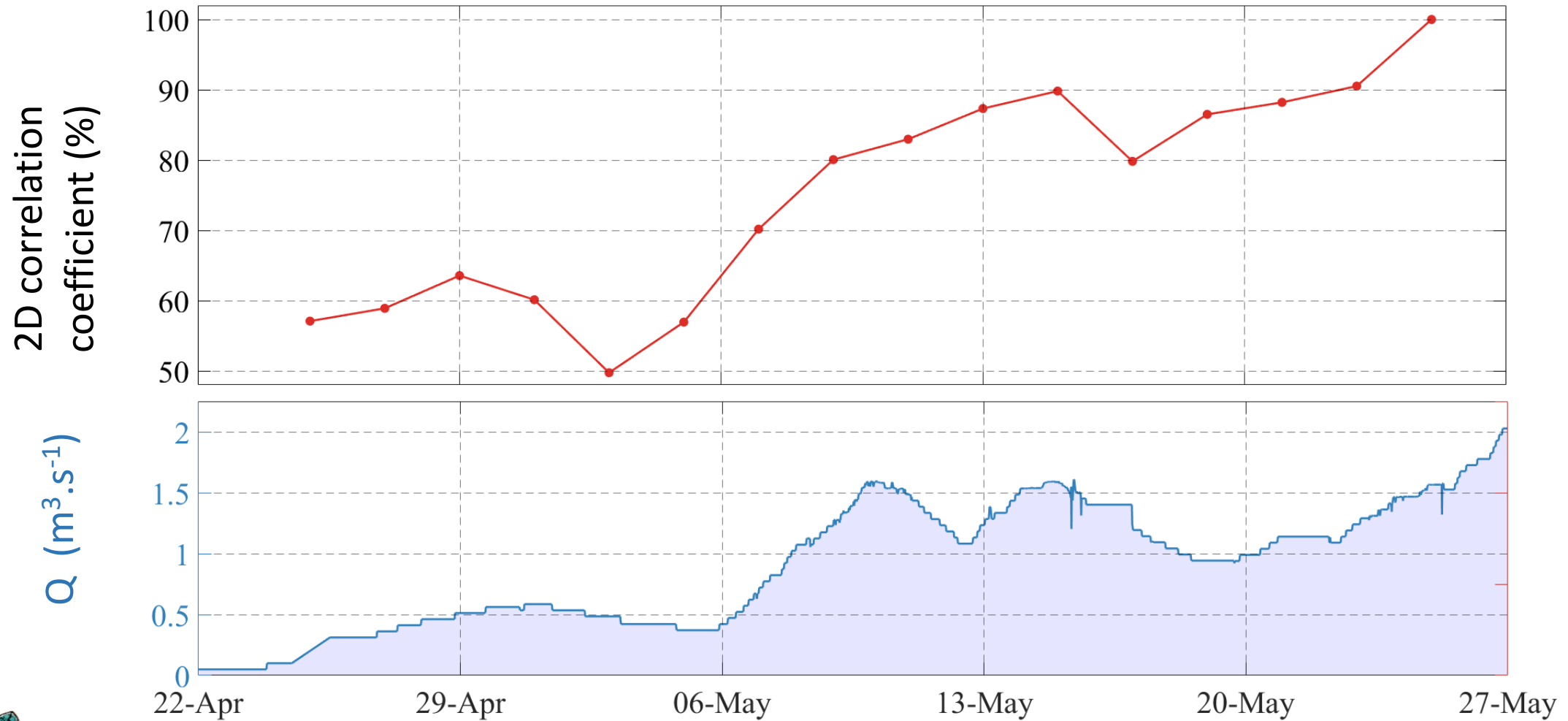
# From distributed ... to localized



# #4 | AM CAPABLE OF CAPTURING SUBGLACIAL HYDROLOGY DYNAMICS

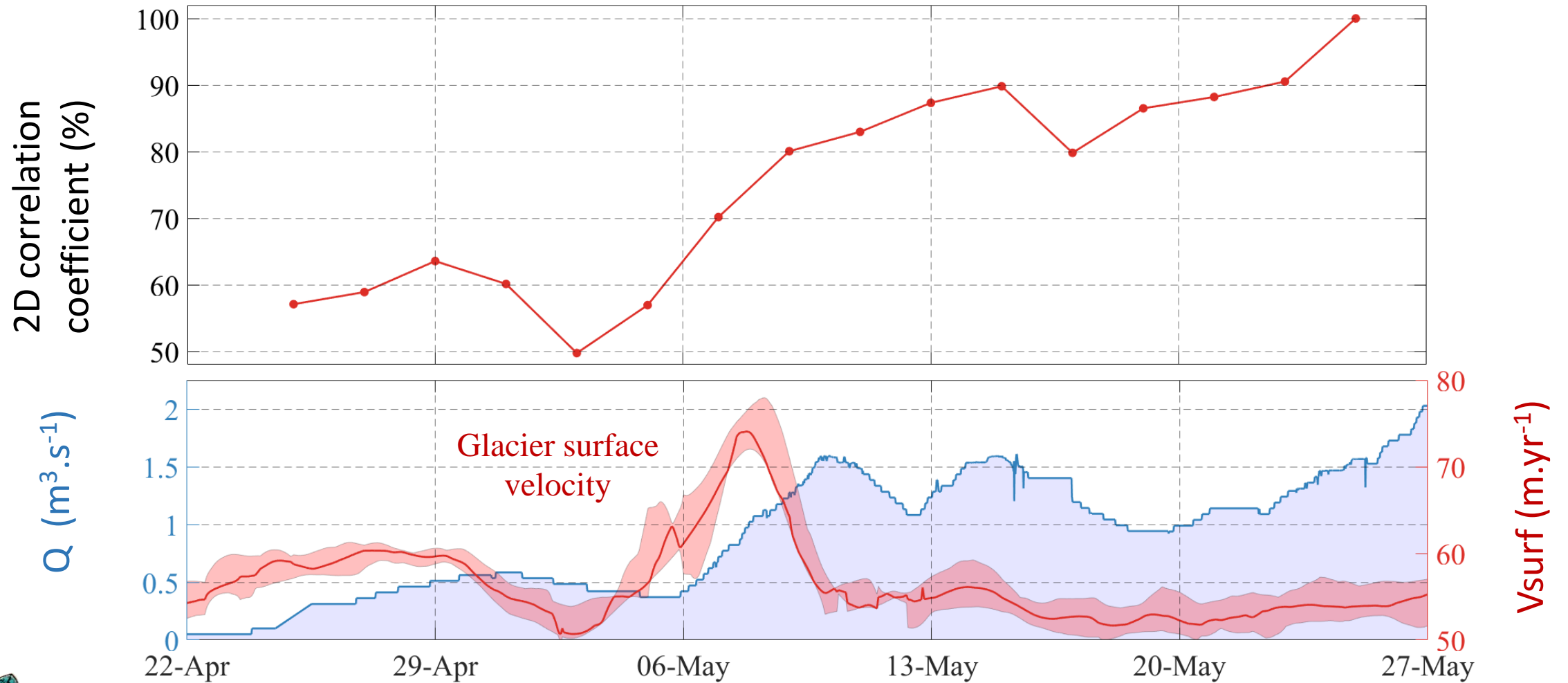


# Spatial dynamics and hydraulic properties



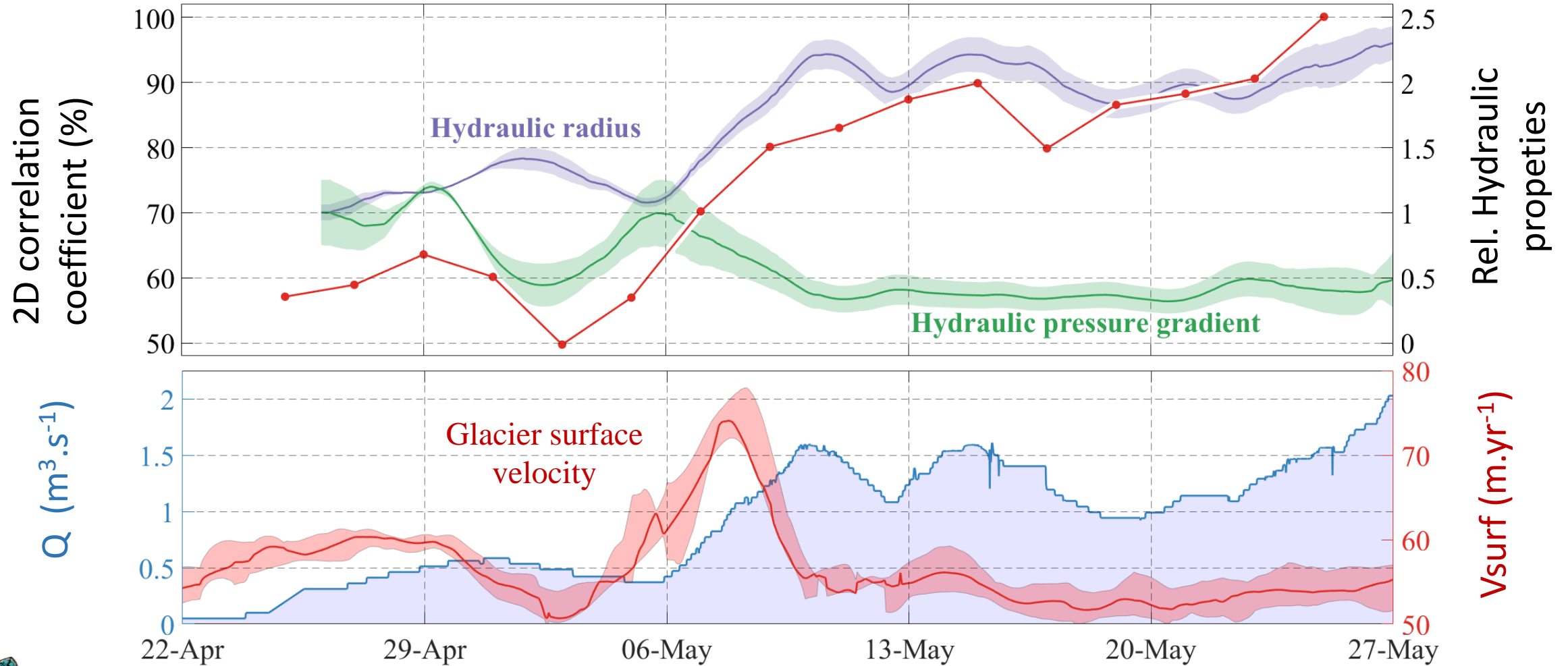
(Nanni et al., subm.)

# Spatial dynamics and hydraulic properties



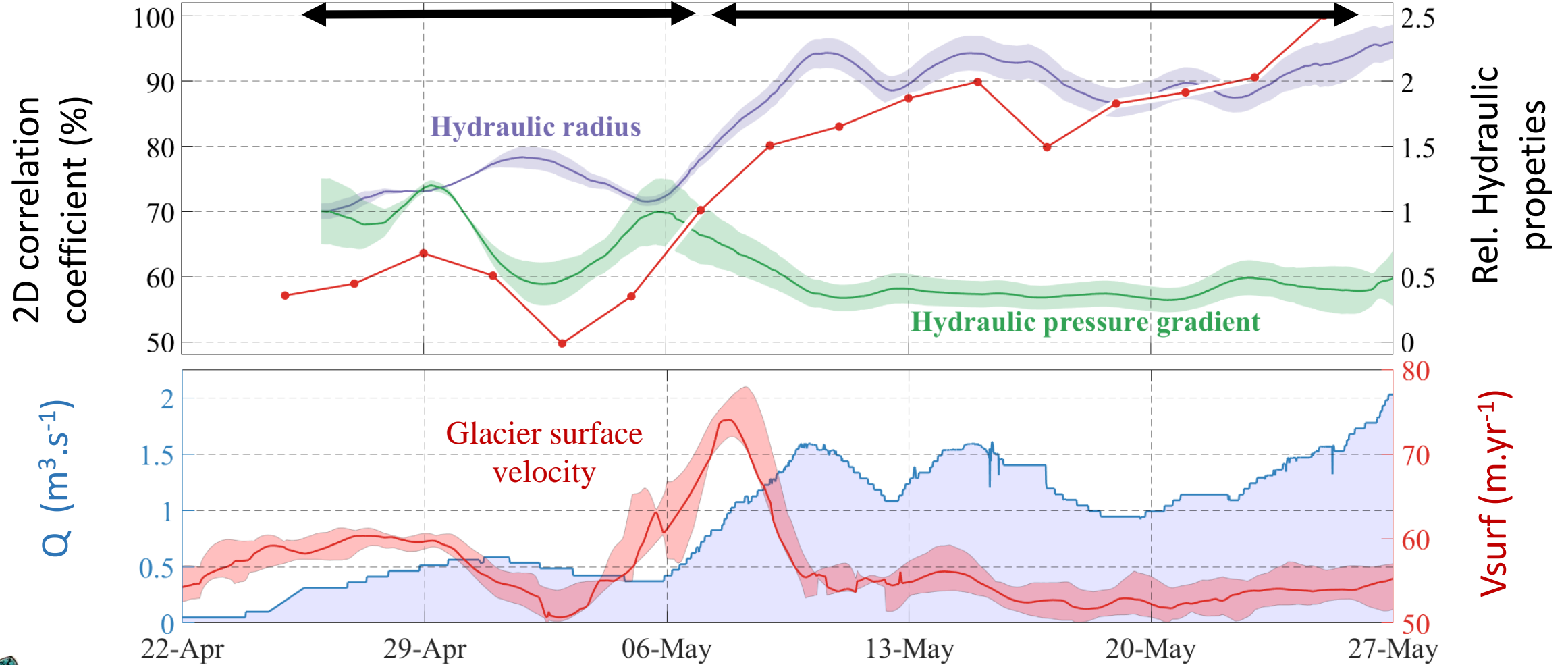
(Nanni et al., subm.)

# Spatial dynamics and hydraulic properties



(Nanni et al., subm.)

# From inefficient to efficient?



(Nanni et al., subm.)

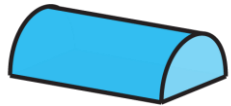
# My questions on the methodology

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**#1**

Can we **MEASURE** subglacial-water-flow-induced seismicity over complete melt-seasons?



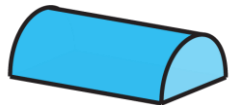
**#2**

What is the **TEMPORAL** dynamics of subglacial hydraulic properties over complete melt-seasons?



**#3**

Can we **LOCATE** distributed sources of seismic noise?



**#4**

What is the **SPATIAL** dynamics of cavities and channels?

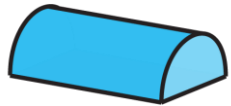
# My questions on the methodology

---



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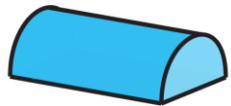
#2

What is the **TEMPORAL** dynamics of subglacial hydraulic properties over complete melt-seasons?



#3

Can we **LOCATE** distributed sources of seismic noise?



#4

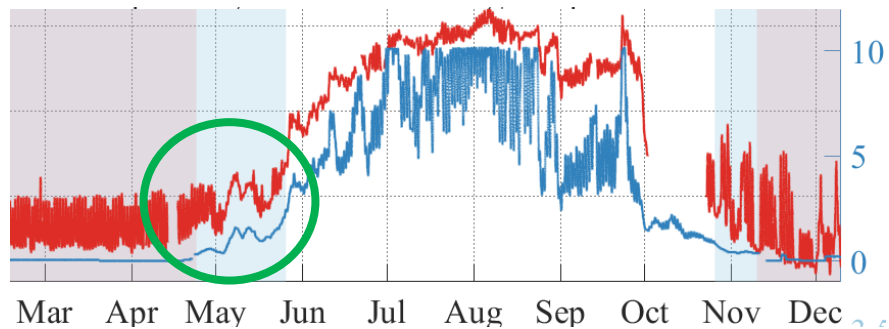
What is the **SPATIAL** dynamics of cavities and channels?



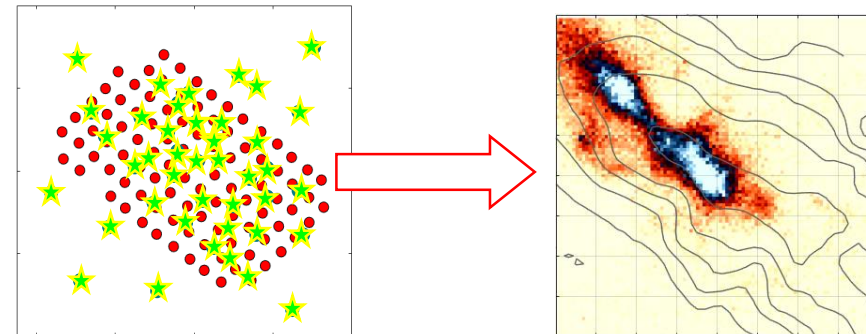
# My conclusions on methodological aspects

I USED SEISMOLOGY TO STUDY **COMPLETE MELT-SEASON**

I WAS CAPABLE OF **SPATIALLY LOCATING SUBGLACIAL WATER FLOW**



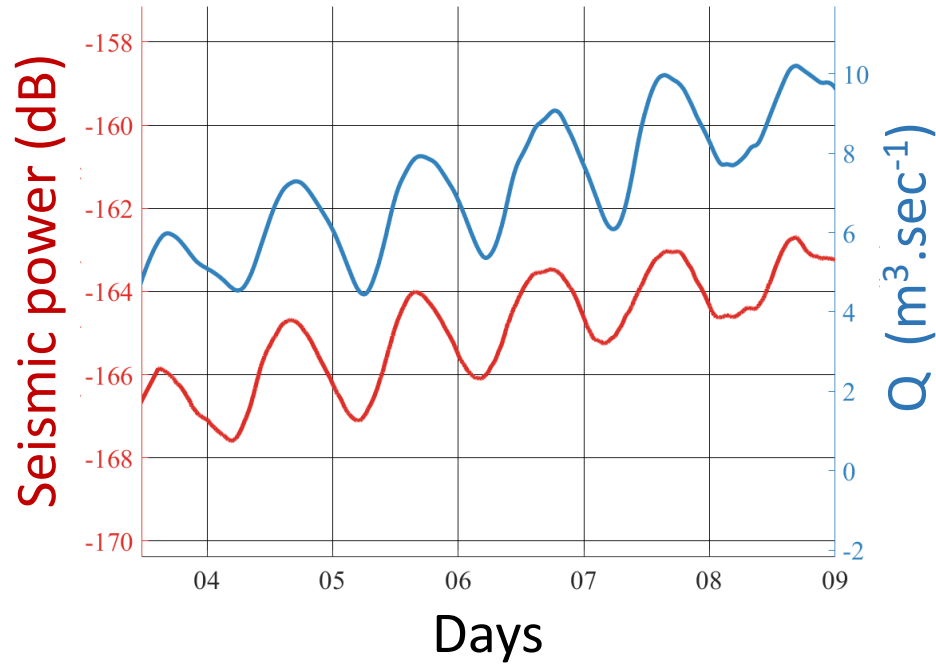
Published in The Cryosphere



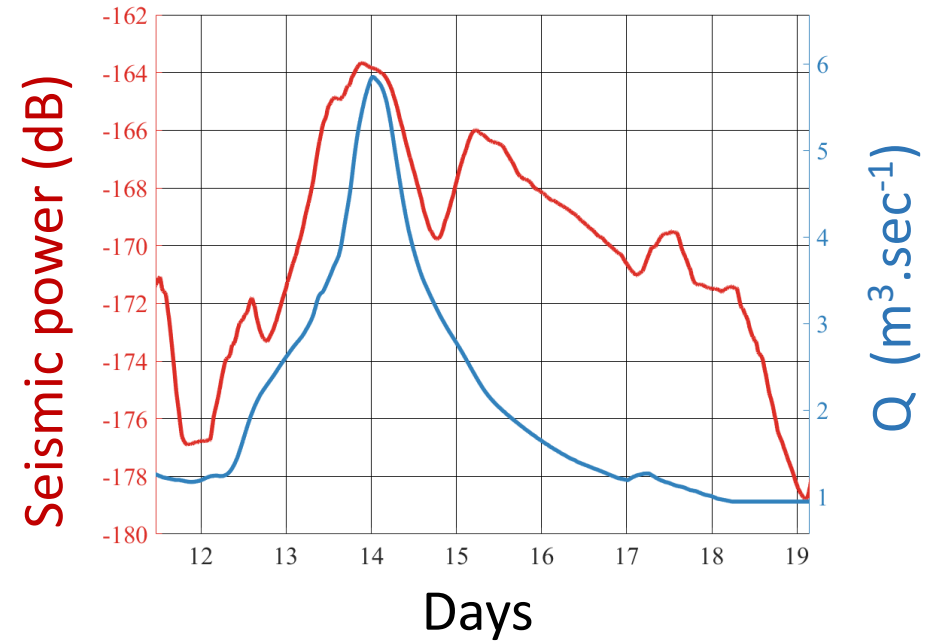
Submitted to PNAS + published in SRL

# Perspectives: different timescales

Daily variations



Storm event



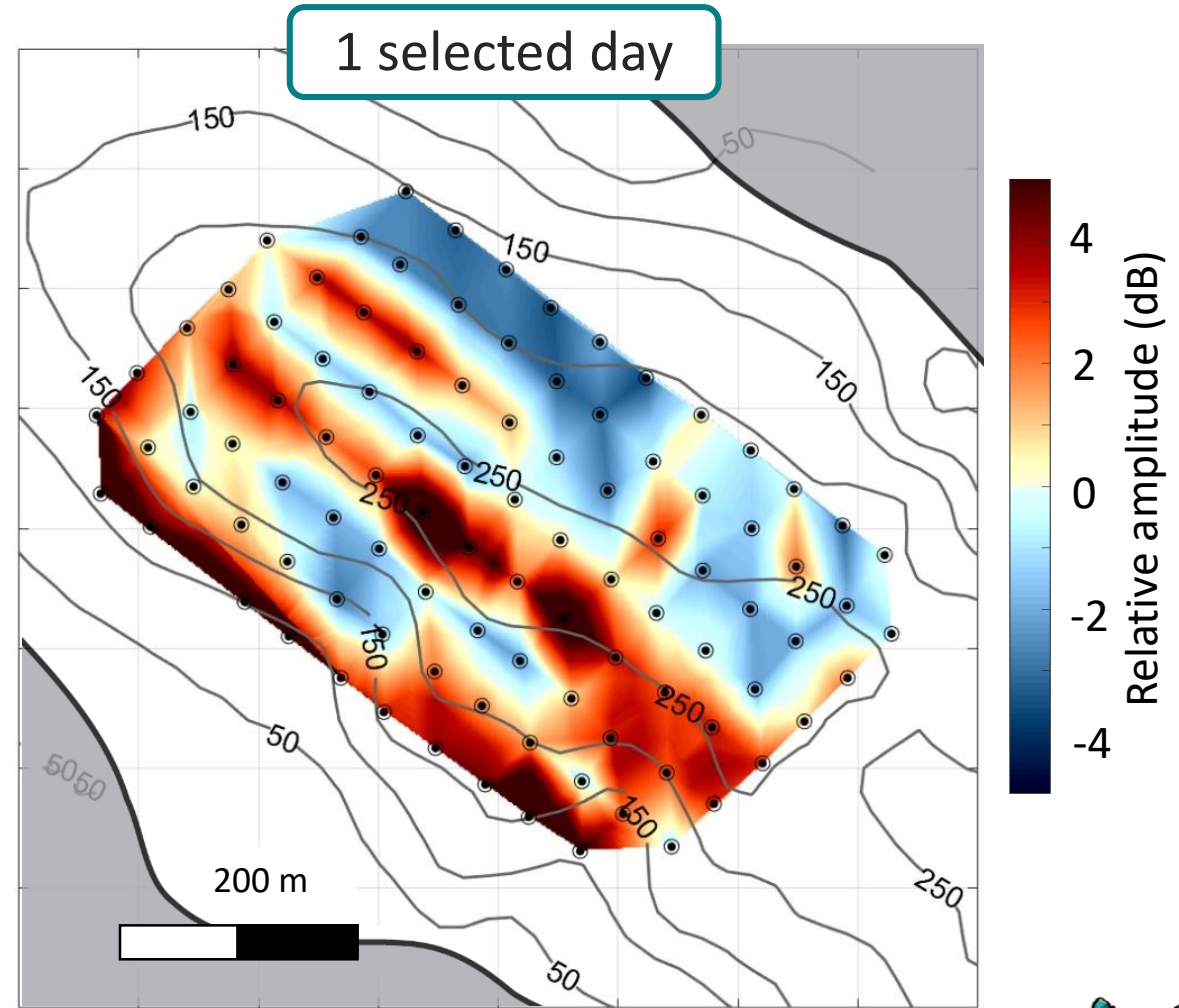
Investigate kinetic effect and transient states

# Perspectives: spatial variations of amplitudes

$$u(t) = Ae^{i\omega t}$$

Amplitude      Phase

- Might allow to spatialized hydraulic properties
- Complex effect of attenuation/amplification



(Nanni et al., in prep.)

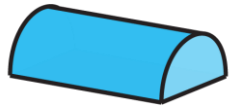
# My questions on the studied processes

---



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Can we MEASURE subglacial-water-flow-induced seismicity over complete melt-seasons?



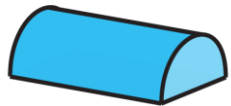
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What is the **TEMPORAL** dynamics of subglacial hydraulic properties over complete melt-seasons?



#3

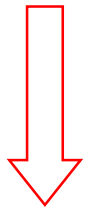
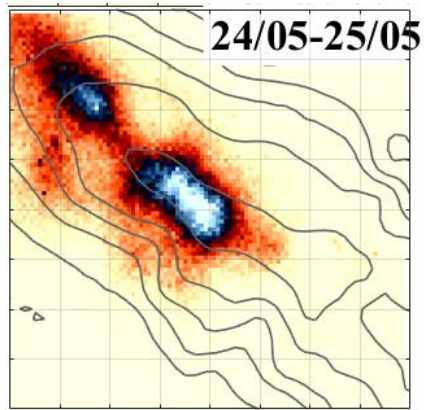
Can we LOCATE distributed sources of seismic noise?



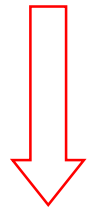
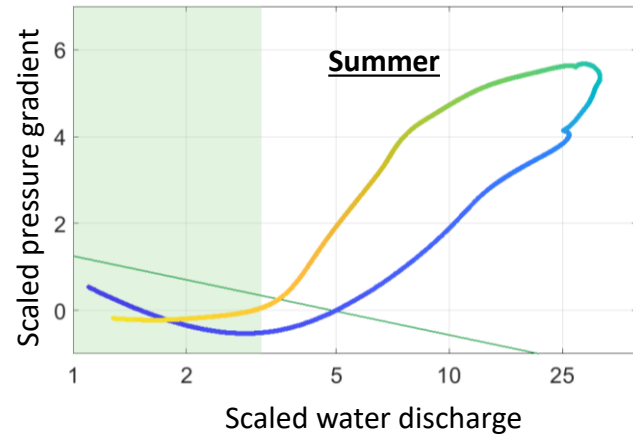
#4

What is the **SPATIAL** dynamics of cavities and channels?

# My conclusions on the studied processes

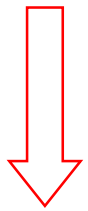
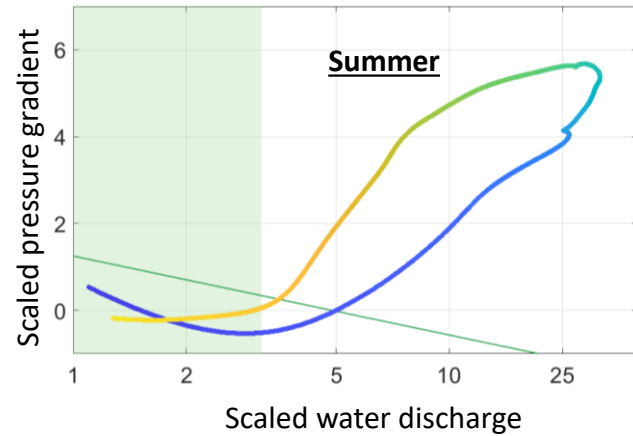
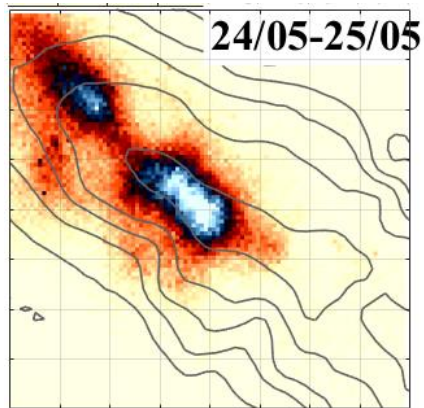


Localized water flow

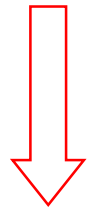


High pressure gradient in summer!

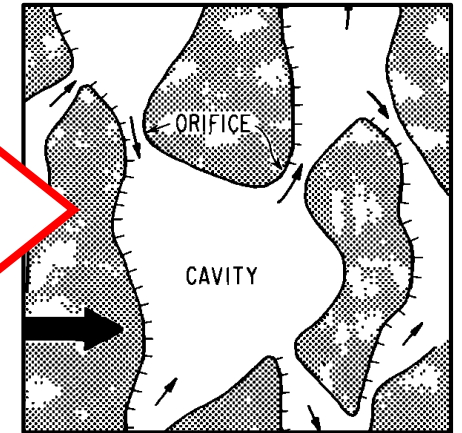
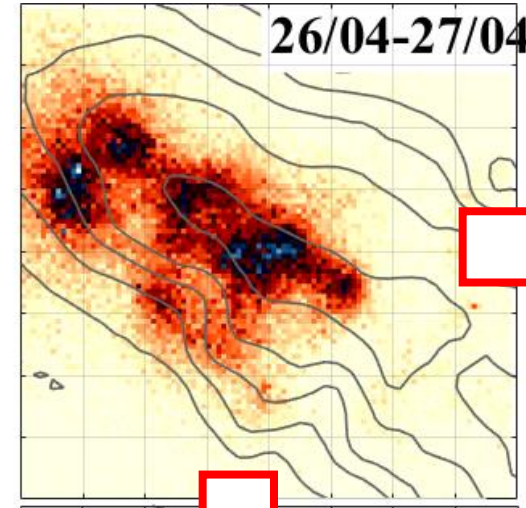
# My conclusions on the studied processes



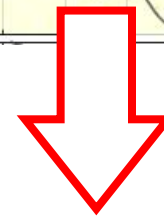
Localized water flow



High pressure gradient in summer!



Linked cavity  
(Kamb, 1987)

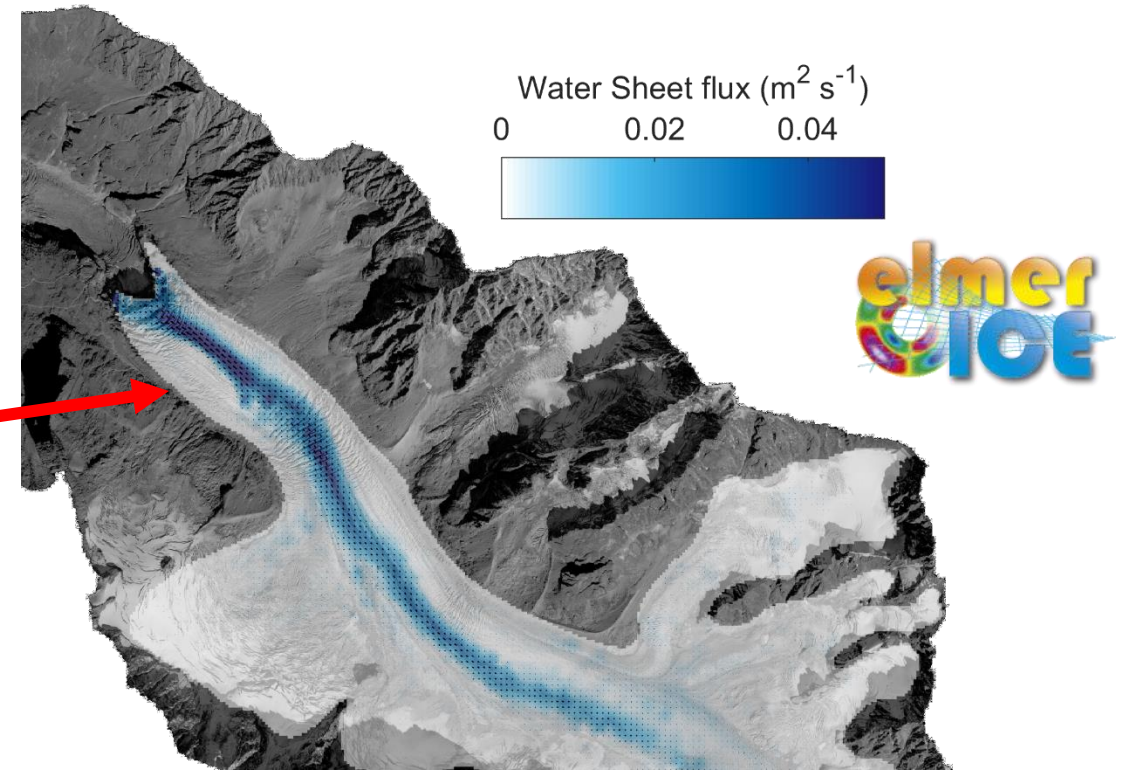
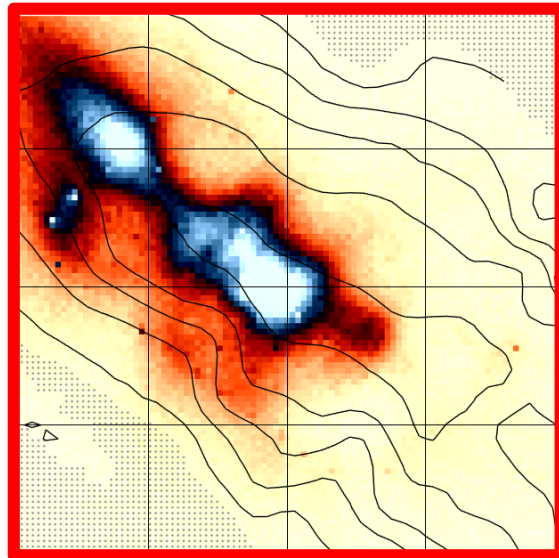


I can observe distributed water flow in the cavities with seismology

# Implication for subglacial hydrology dynamics

- Do we observe cavities only?
- Do cavities dominate the drainage system?

**Modelling** subglacial hydrology with Elmer/Ice-GlaDS coupling by A. Gilbert



# Perspectives: we need to study other settings

---



My PhD



# Current (or soon) dense seismic experiments

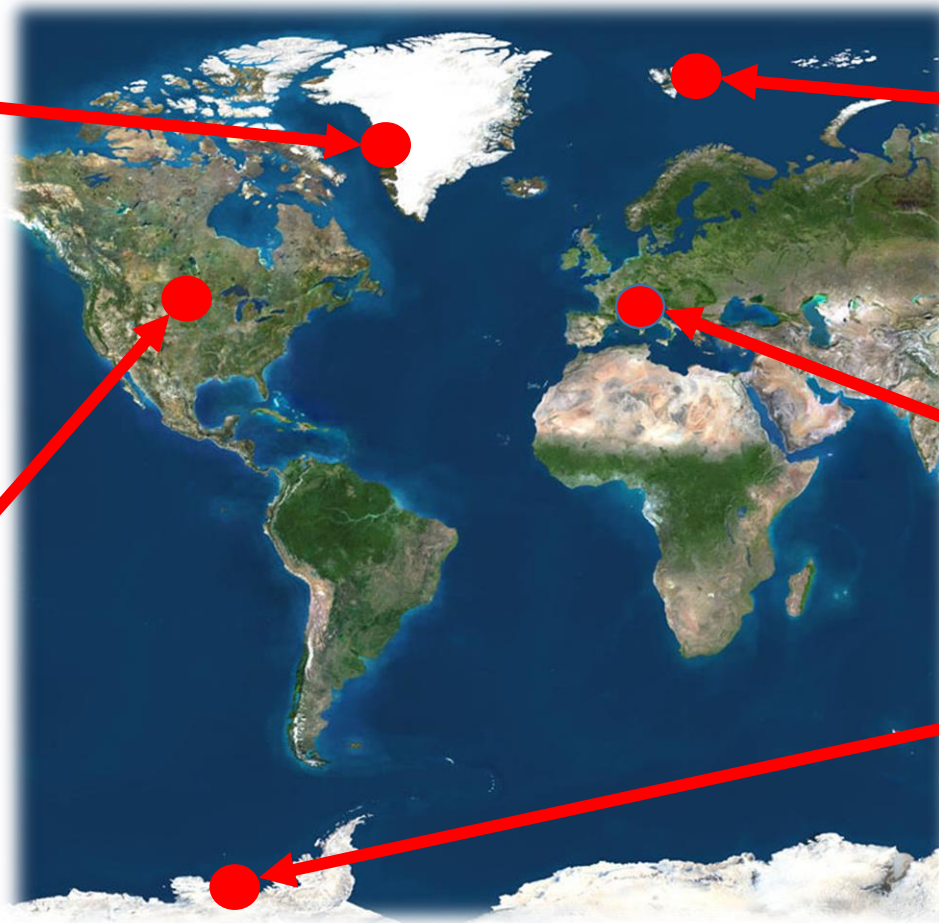
## Subglacial lakes in Greenland

(S. Livingstone, A. Booth and others - UK)

*My post-doc?*

## Subglacial hydrology and stick-slips in Canada

(N. Stevens, L. Zoet and others - USA)



## Soft-bedded glaciers and surges in Spitzberg

(T. Schuler, A. Kholer, and others - Norway)

*My post-doc?*

## My PhD

## Grounding line dynamics and subglacial hydrology in Antarctica – 1,000 sensors

(The International Thwaites Glacier collaboration)

# Perspectives: continue sharing beyond academia



An artistic collaboration with EdZ



Presenting my works during the « Week of science »

Making comics with 12 other PhD students



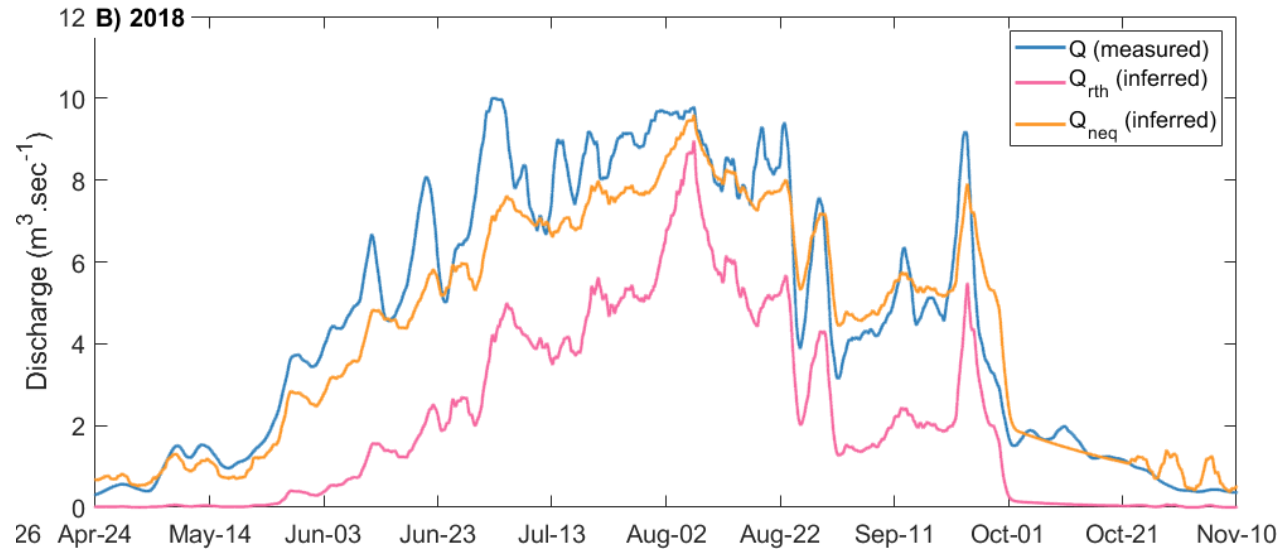
A collaboration during the Grenoble Scientific Game Jam



THANK YOU ALL

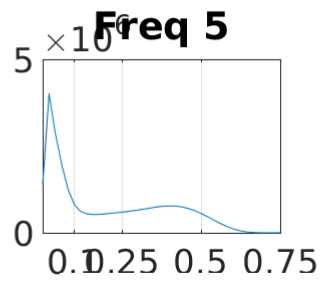
AND COLLEAGUES, LAB MEMBERS, FAMILY ...

# Implication for monitoring Q

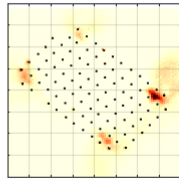


- Using the relation between Q and Pw for channels out-of-equilibrium allow to estimate Q from Pw with less than 10% error compared to more than 65% if channels are assumed to be at equilibrium.

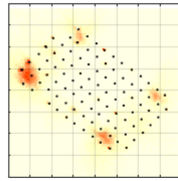




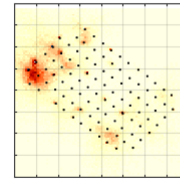
a) Beam [0.0054-0.01]



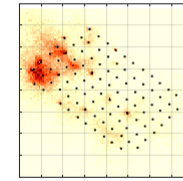
b) Beam [0.016-0.021]



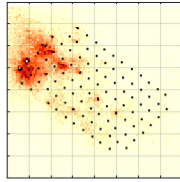
c) Beam [0.026-0.031]



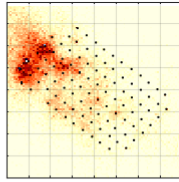
d) Beam [0.037-0.042]



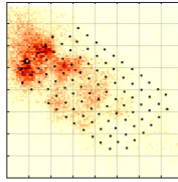
e) Beam [0.047-0.052]



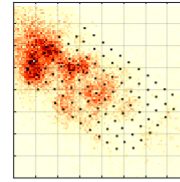
f) Beam [0.058-0.062]



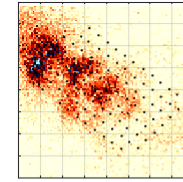
g) Beam [0.068-0.073]



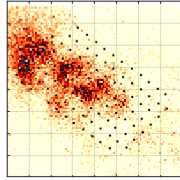
h) Beam [0.078-0.083]



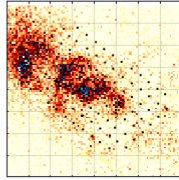
i) Beam [0.089-0.094]



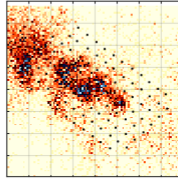
j) Beam [0.099-0.1]



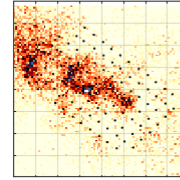
k) Beam [0.11-0.11]



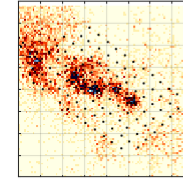
l) Beam [0.12-0.12]



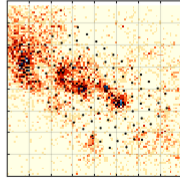
m) Beam [0.13-0.14]



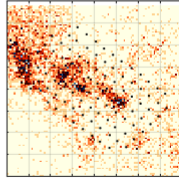
n) Beam [0.14-0.15]



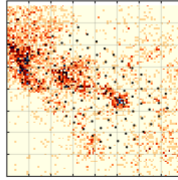
o) Beam [0.15-0.16]



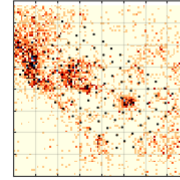
p) Beam [0.16-0.17]



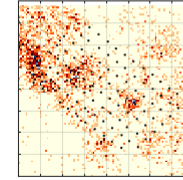
q) Beam [0.17-0.18]



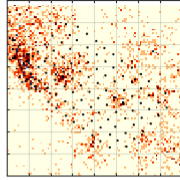
r) Beam [0.18-0.19]



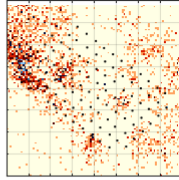
s) Beam [0.19-0.2]



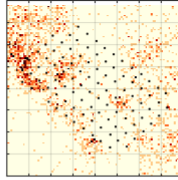
t) Beam [0.2-0.21]



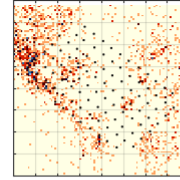
u) Beam [0.21-0.22]



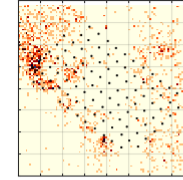
v) Beam [0.22-0.23]

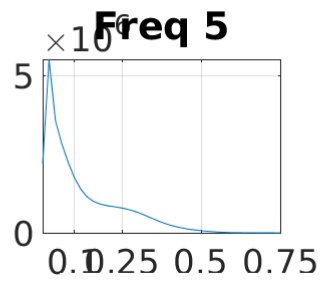


w) Beam [0.23-0.24]

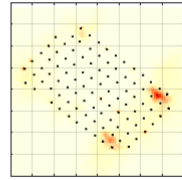


x) Beam [0.24-0.25]

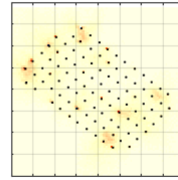




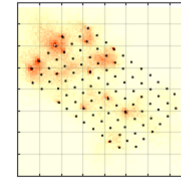
a) Beam [0.0054-0.01]



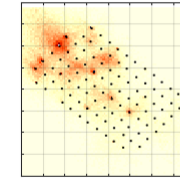
b) Beam [0.016-0.021]



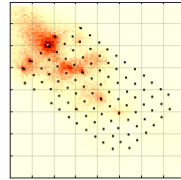
c) Beam [0.026-0.031]



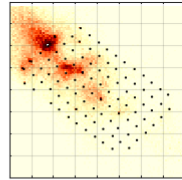
d) Beam [0.037-0.042]



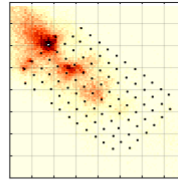
e) Beam [0.047-0.052]



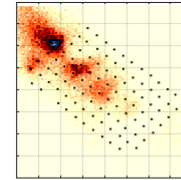
f) Beam [0.058-0.062]



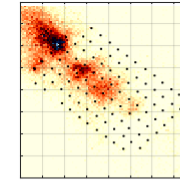
g) Beam [0.068-0.073]



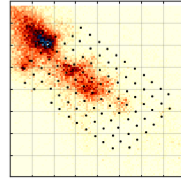
h) Beam [0.078-0.083]



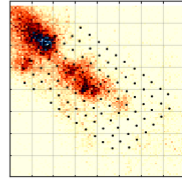
i) Beam [0.089-0.094]



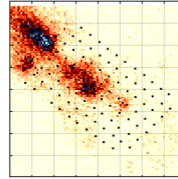
j) Beam [0.099-0.1]



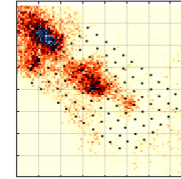
k) Beam [0.11-0.11]



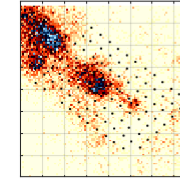
l) Beam [0.12-0.12]



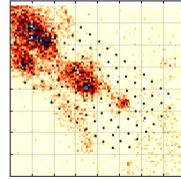
m) Beam [0.13-0.14]



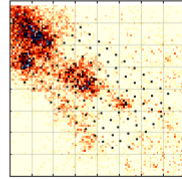
n) Beam [0.14-0.15]



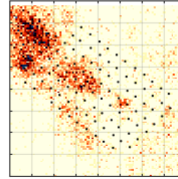
o) Beam [0.15-0.16]



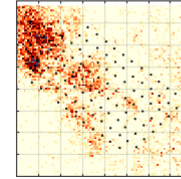
p) Beam [0.16-0.17]



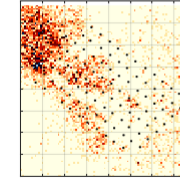
q) Beam [0.17-0.18]



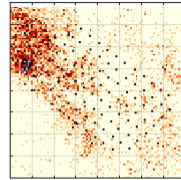
r) Beam [0.18-0.19]



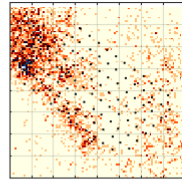
s) Beam [0.19-0.2]



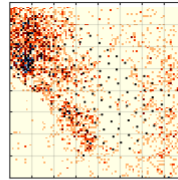
t) Beam [0.2-0.21]



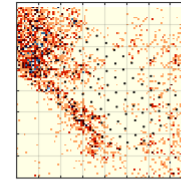
u) Beam [0.21-0.22]



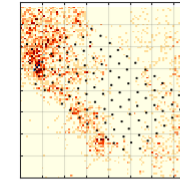
v) Beam [0.22-0.23]

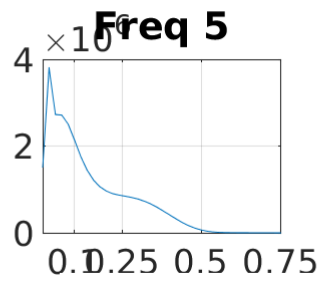


w) Beam [0.23-0.24]

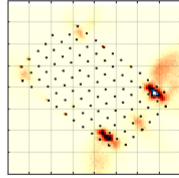


x) Beam [0.24-0.25]

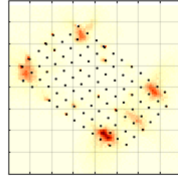




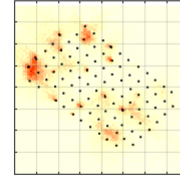
a) Beam [0.0054-0.01]



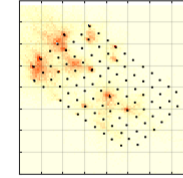
b) Beam [0.016-0.021]



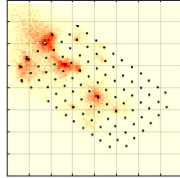
c) Beam [0.026-0.031]



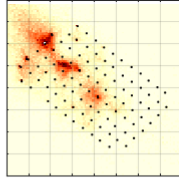
d) Beam [0.037-0.042]



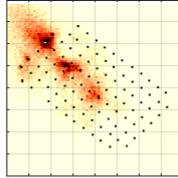
e) Beam [0.047-0.052]



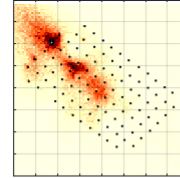
f) Beam [0.058-0.062]



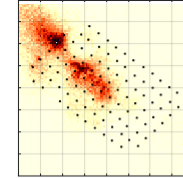
g) Beam [0.068-0.073]



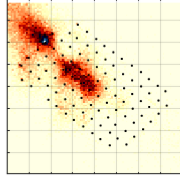
h) Beam [0.078-0.083]



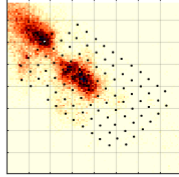
i) Beam [0.089-0.094]



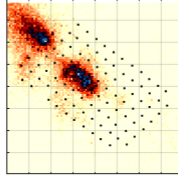
j) Beam [0.099-0.1]



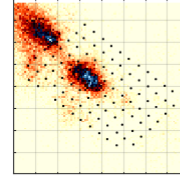
k) Beam [0.11-0.11]



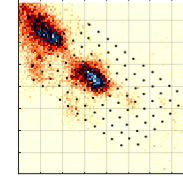
l) Beam [0.12-0.12]



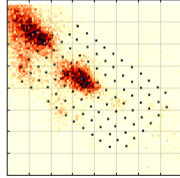
m) Beam [0.13-0.14]



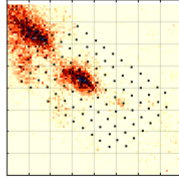
n) Beam [0.14-0.15]



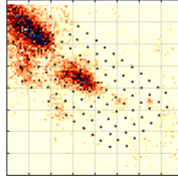
o) Beam [0.15-0.16]



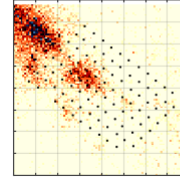
p) Beam [0.16-0.17]



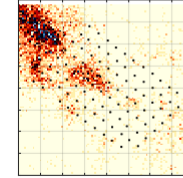
q) Beam [0.17-0.18]



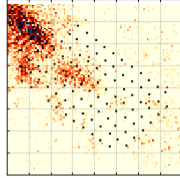
r) Beam [0.18-0.19]



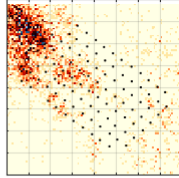
s) Beam [0.19-0.2]



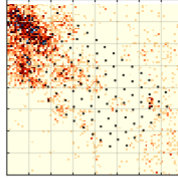
t) Beam [0.2-0.21]



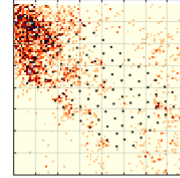
u) Beam [0.21-0.22]



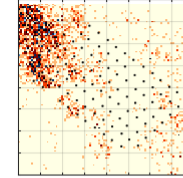
v) Beam [0.22-0.23]



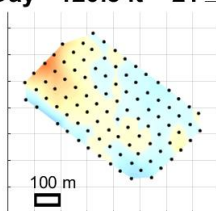
w) Beam [0.23-0.24]



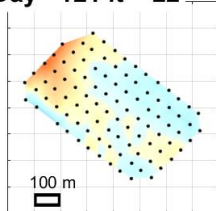
x) Beam [0.24-0.25]



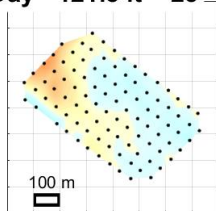
a) Day =120.5 it = 21



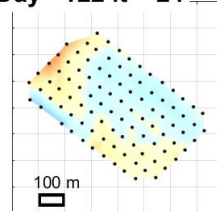
b) Day =121 it = 22



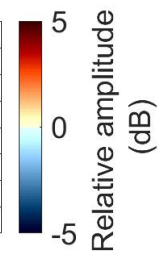
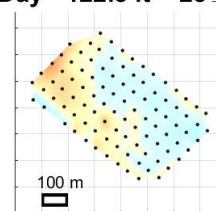
c) Day =121.5 it = 23



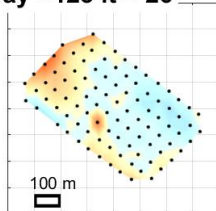
d) Day =122 it = 24



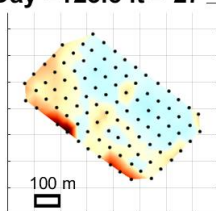
e) Day =122.5 it = 25



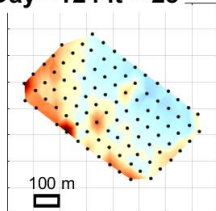
f) Day =123 it = 26



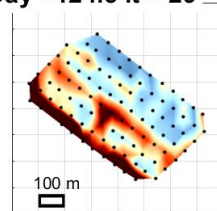
g) Day =123.5 it = 27



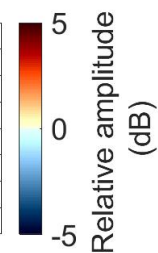
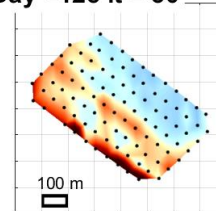
h) Day =124 it = 28



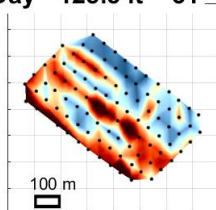
i) Day =124.5 it = 29



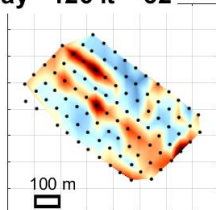
j) Day =125 it = 30



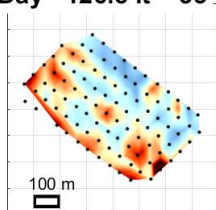
k) Day =125.5 it = 31



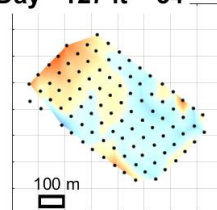
l) Day =126 it = 32



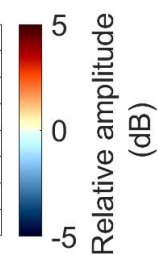
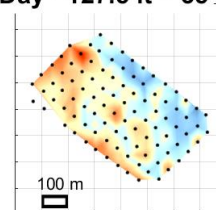
m) Day =126.5 it = 33



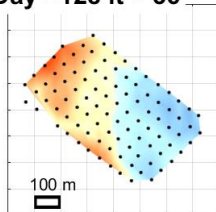
n) Day =127 it = 34



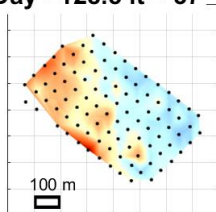
o) Day =127.5 it = 35



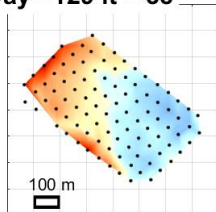
p) Day =128 it = 36



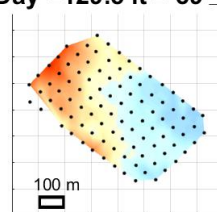
q) Day =128.5 it = 37



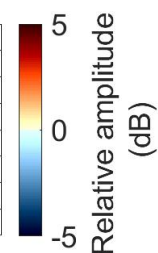
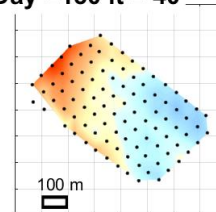
r) Day =129 it = 38



s) Day =129.5 it = 39

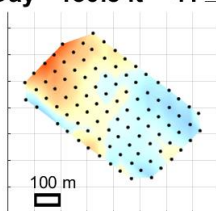


t) Day =130 it = 40

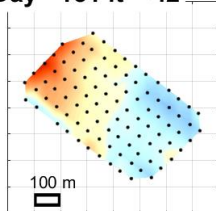




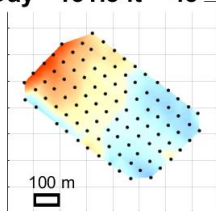
a) Day = 130.5 it = 41



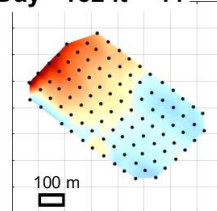
b) Day = 131 it = 42



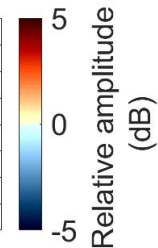
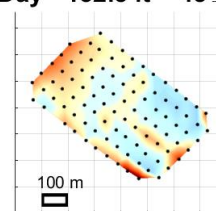
c) Day = 131.5 it = 43



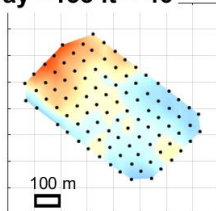
d) Day = 132 it = 44



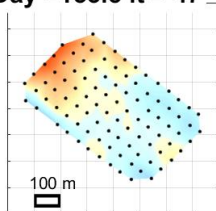
e) Day = 132.5 it = 45



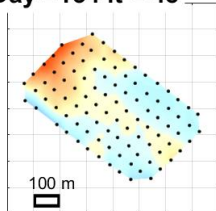
f) Day = 133 it = 46



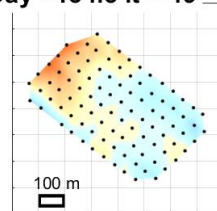
g) Day = 133.5 it = 47



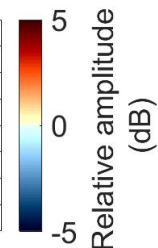
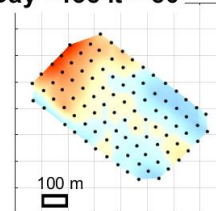
h) Day = 134 it = 48



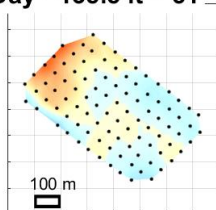
i) Day = 134.5 it = 49



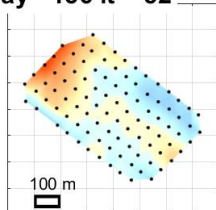
j) Day = 135 it = 50



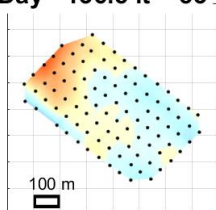
k) Day = 135.5 it = 51



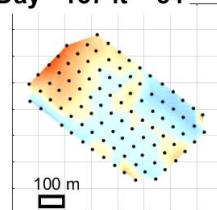
l) Day = 136 it = 52



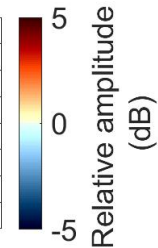
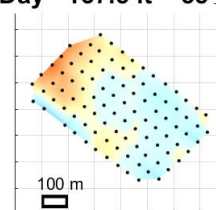
m) Day = 136.5 it = 53



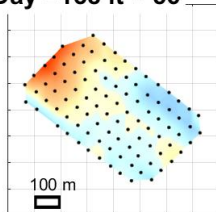
n) Day = 137 it = 54



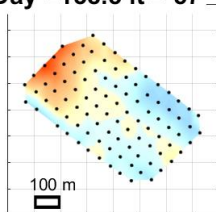
o) Day = 137.5 it = 55



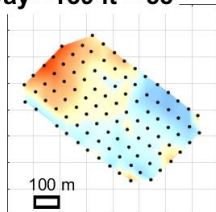
p) Day = 138 it = 56



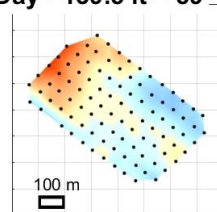
q) Day = 138.5 it = 57



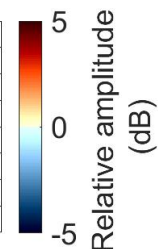
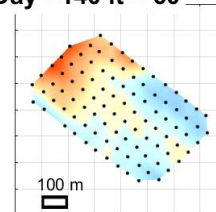
r) Day = 139 it = 58



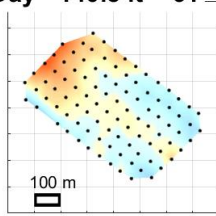
s) Day = 139.5 it = 59



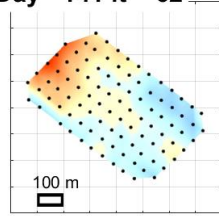
t) Day = 140 it = 60



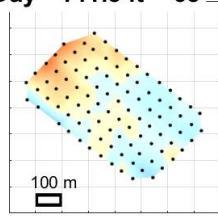
a) Day = 140.5 it = 61



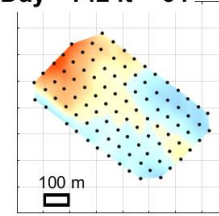
b) Day = 141 it = 62



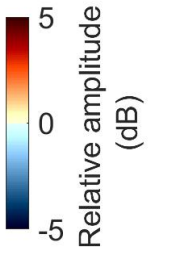
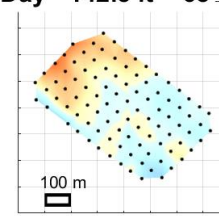
c) Day = 141.5 it = 63



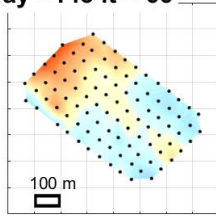
d) Day = 142 it = 64



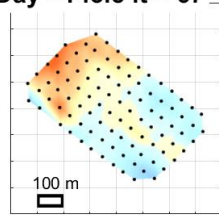
e) Day = 142.5 it = 65



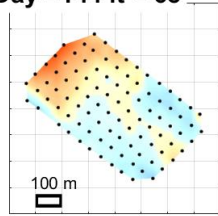
f) Day = 143 it = 66



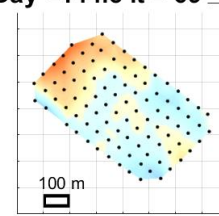
g) Day = 143.5 it = 67



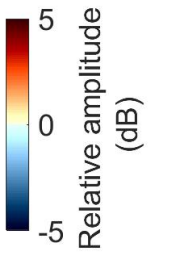
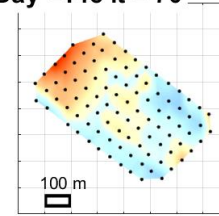
h) Day = 144 it = 68



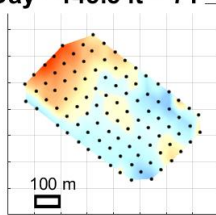
i) Day = 144.5 it = 69



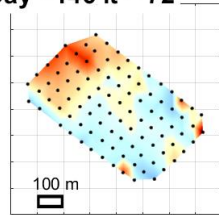
j) Day = 145 it = 70



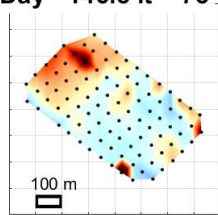
k) Day = 145.5 it = 71



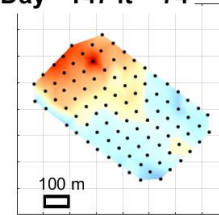
l) Day = 146 it = 72



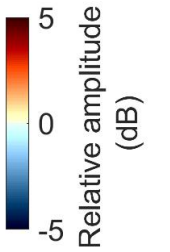
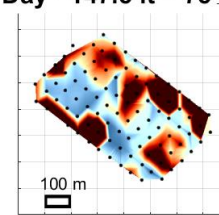
m) Day = 146.5 it = 73



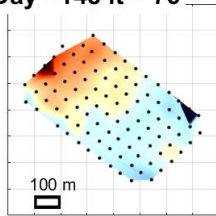
n) Day = 147 it = 74



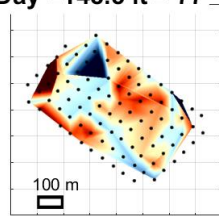
o) Day = 147.5 it = 75



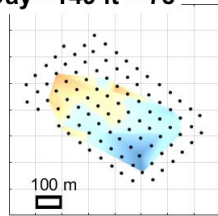
p) Day = 148 it = 76



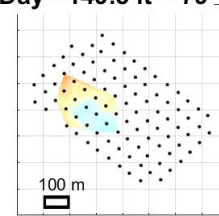
q) Day = 148.5 it = 77



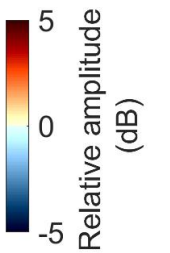
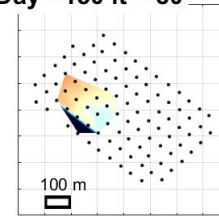
r) Day = 149 it = 78



s) Day = 149.5 it = 79



t) Day = 150 it = 80



# Deriving seismic power – discharge scalings

From (Gimbert et al., 2016)

- Noise power from turbulent flow scales as  $P_w \propto \zeta W u_*^{14/3}$ 
  - with  $\zeta = \left(\frac{H}{k_s}\right)$ ,  $k_s$  the wall roughness and  $H$  the flow depth
  - and  $u_*$  the shear velocity and  $W$  the river width

For subglacial channels we assume:

- Uniform pressure fluctuations along the walls
  - so  $W = \Gamma$  the wetted perimeter
- $H \ll k_s$  so we can neglect variations in  $\zeta$
- Subglacial channel flow is steady and uniform at large scale
  - so  $u_* = \sqrt{gRS}$
  - with  $R = \frac{A}{\Gamma}$  the Hydraulic radius and  $S = -\frac{1}{\rho g} \frac{\partial p}{\partial x} + \tan \theta$  the pressure gradient

# Deriving seismic power – discharge scalings

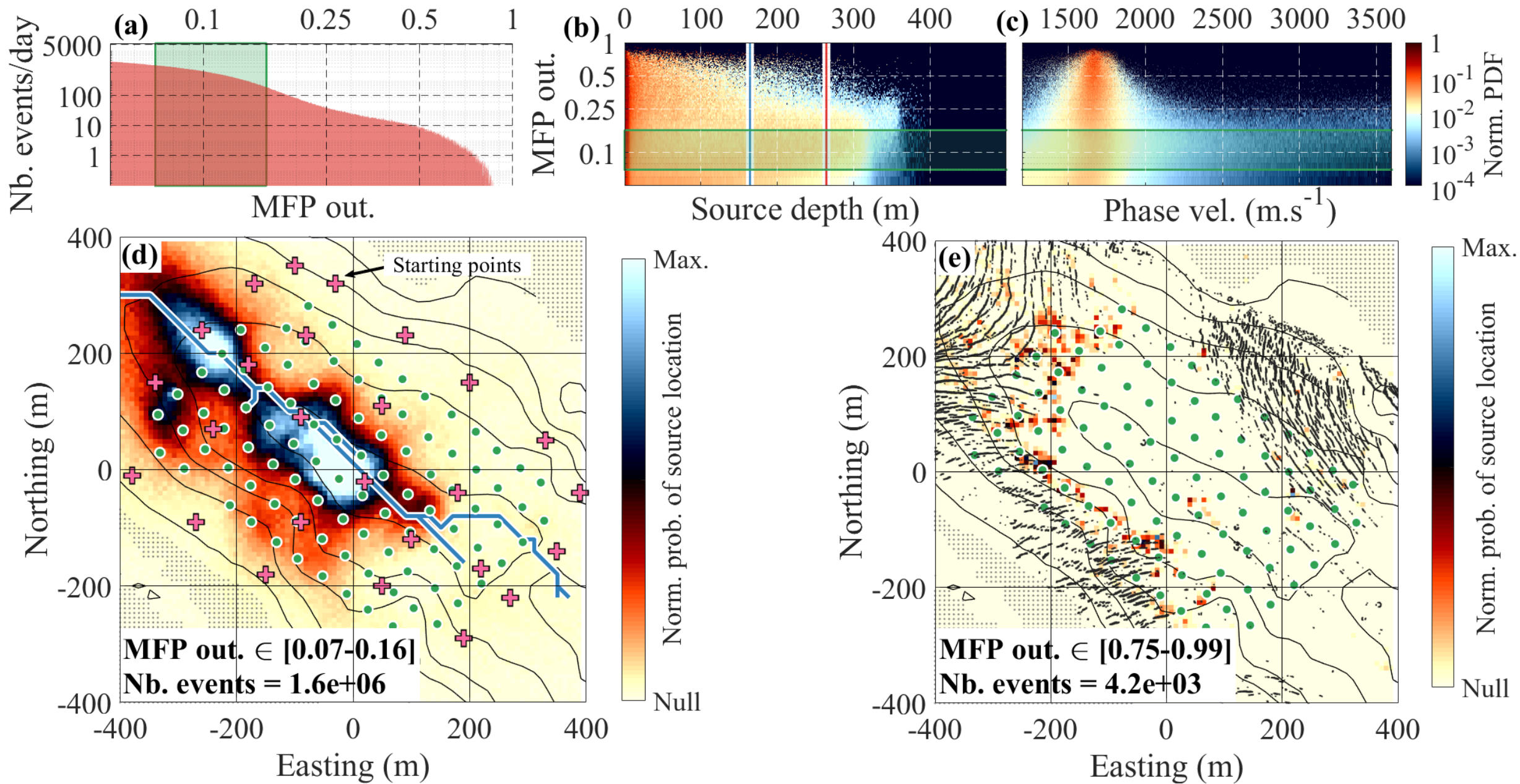
From (Gimbert et al., 2016)

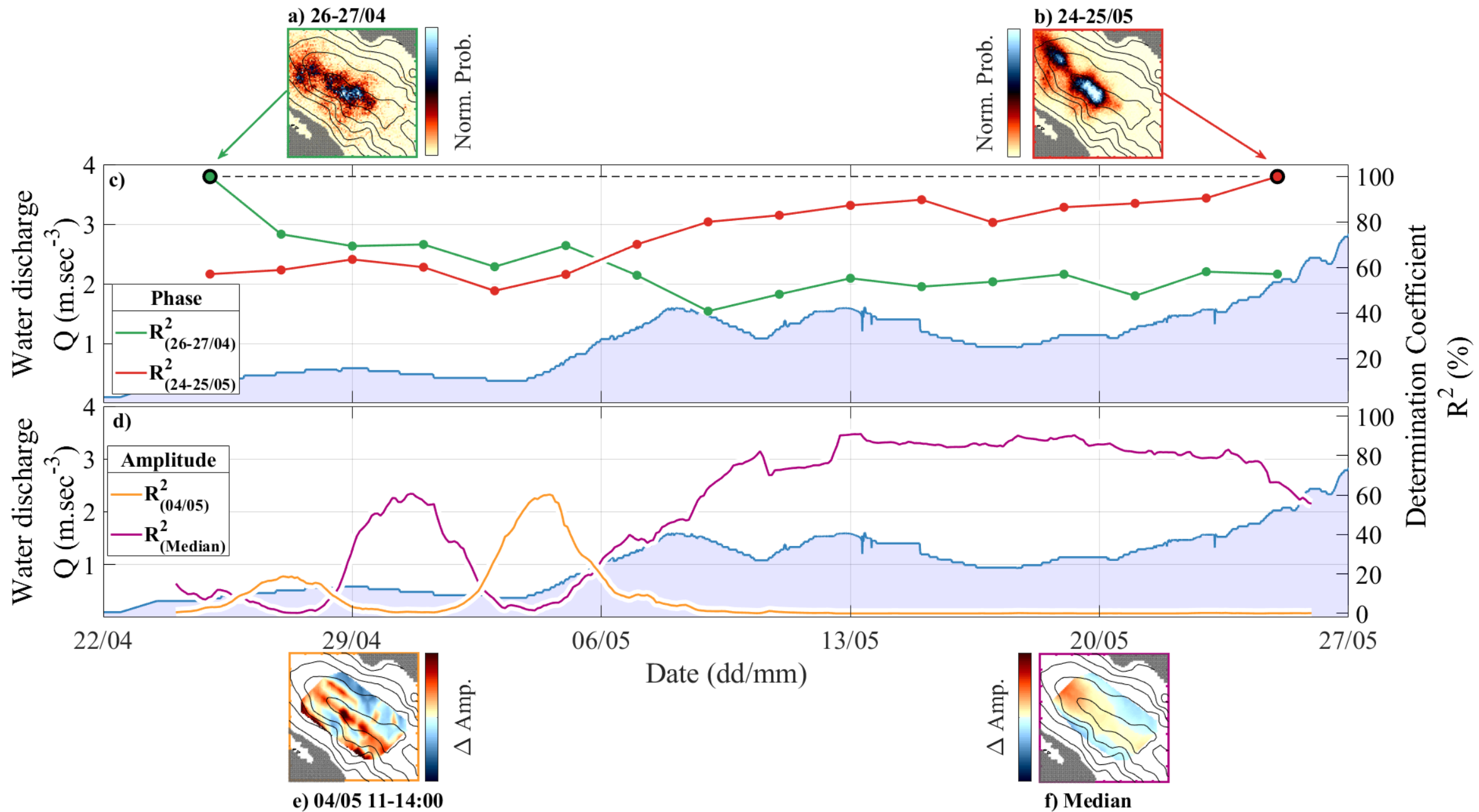
- We then define the flow discharge as  $Q = AU$ 
  - with  $U = \frac{R^{2/3}S^{1/2}}{n}$  the Manning's formulation
- Noise power becomes:  $P_w \propto \Gamma R^{7/3} S^{7/3}$  and  $Q \propto AR^{2/3} S^{1/2}$
- Defining  $\beta$  the shape function with  $\Gamma = \beta R$  and  $A = \beta R^2$  we can define:

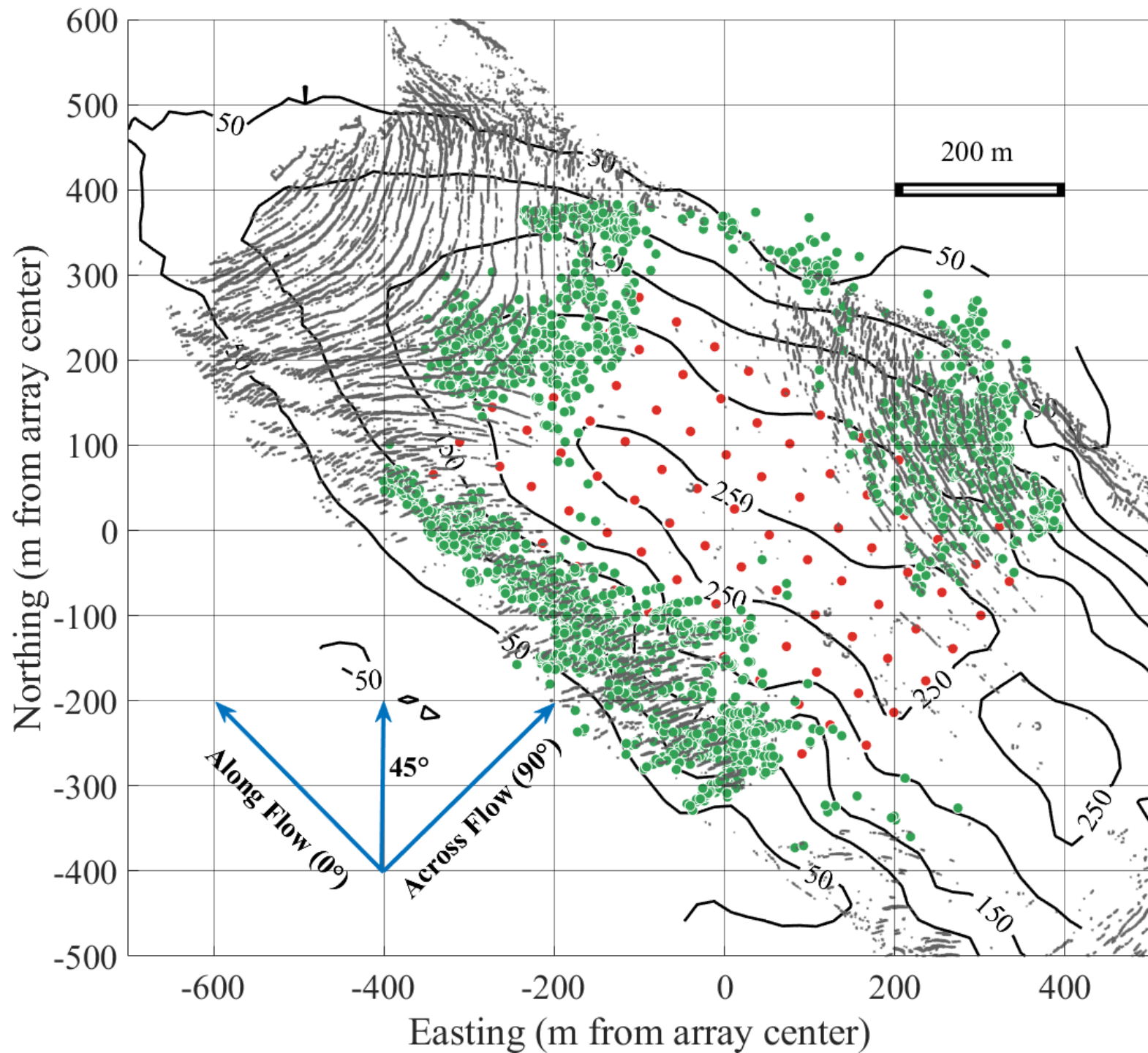
$$\begin{aligned} P_w &\propto \beta^{-11/3} R^{-82/9} Q^{14/3} \\ P_w &\propto \beta^{-1/4} S^{41/24} Q^{5/4} \end{aligned}$$

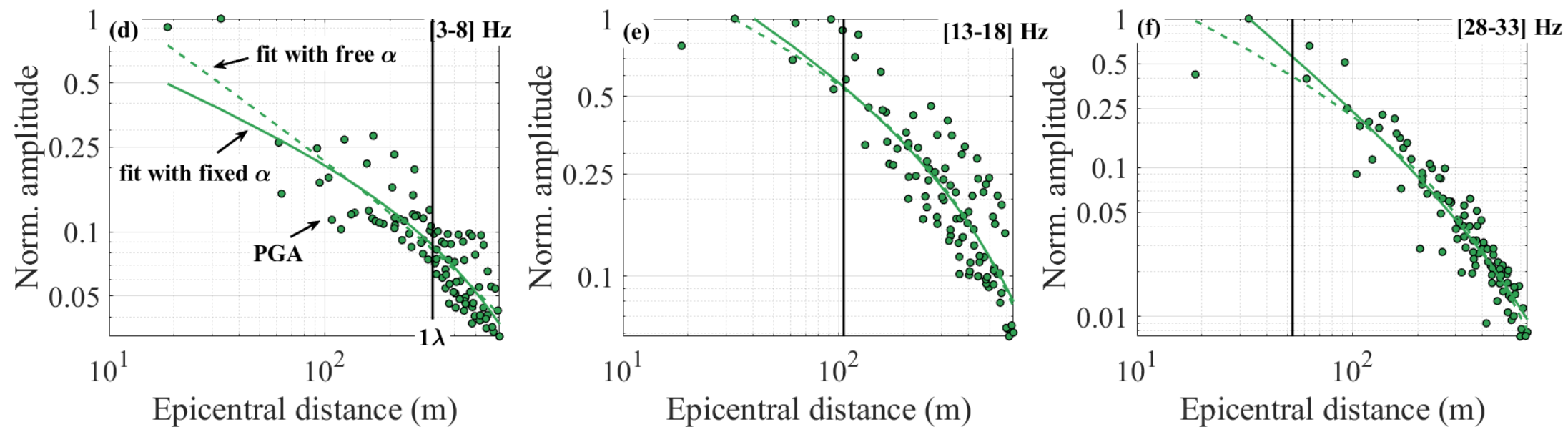
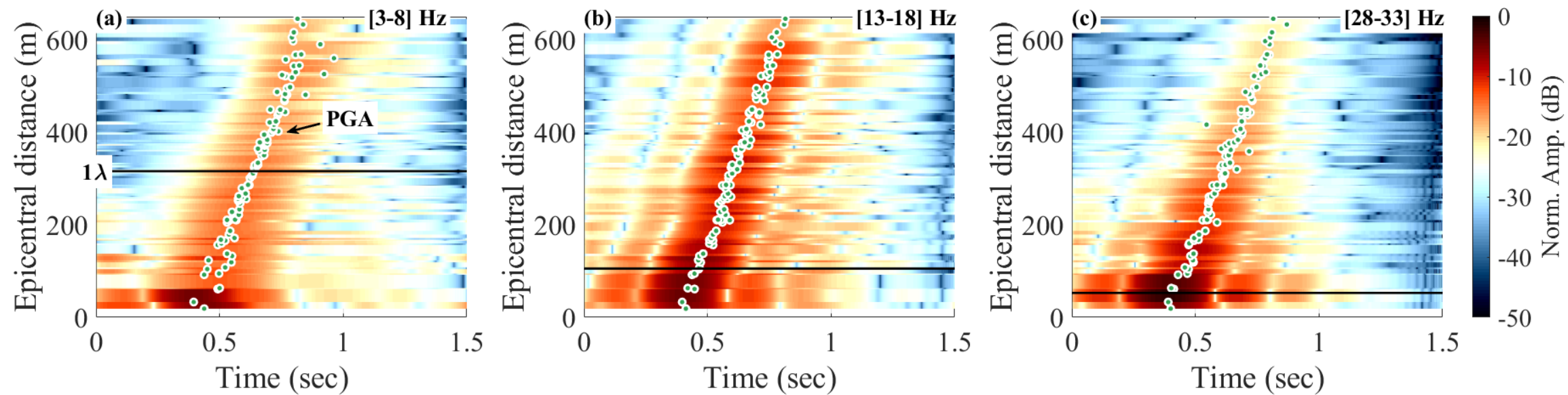


$$\begin{aligned} P_w &\propto Q^{14/3} \\ P_w &\propto Q^{5/4} \end{aligned}$$

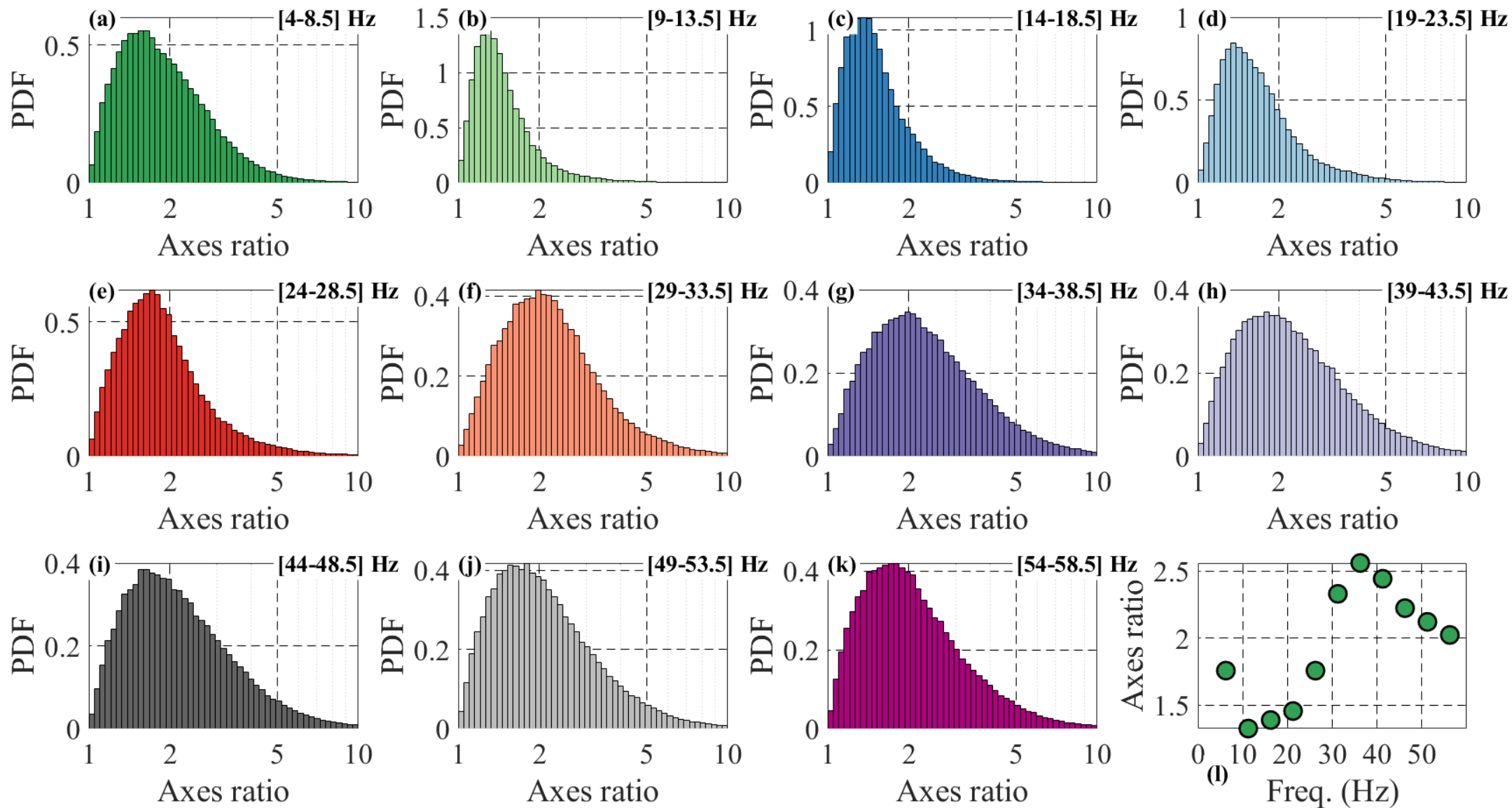


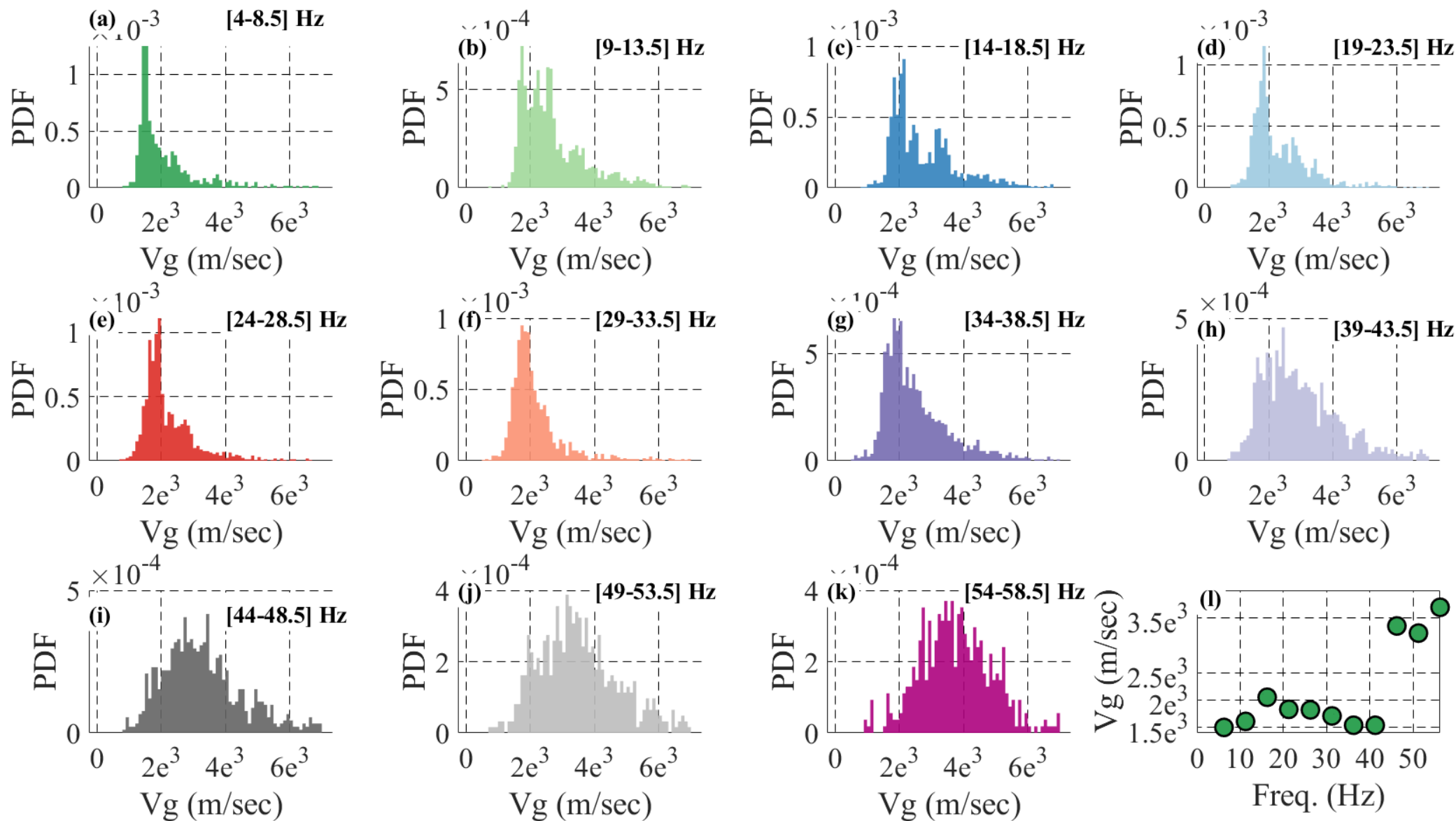


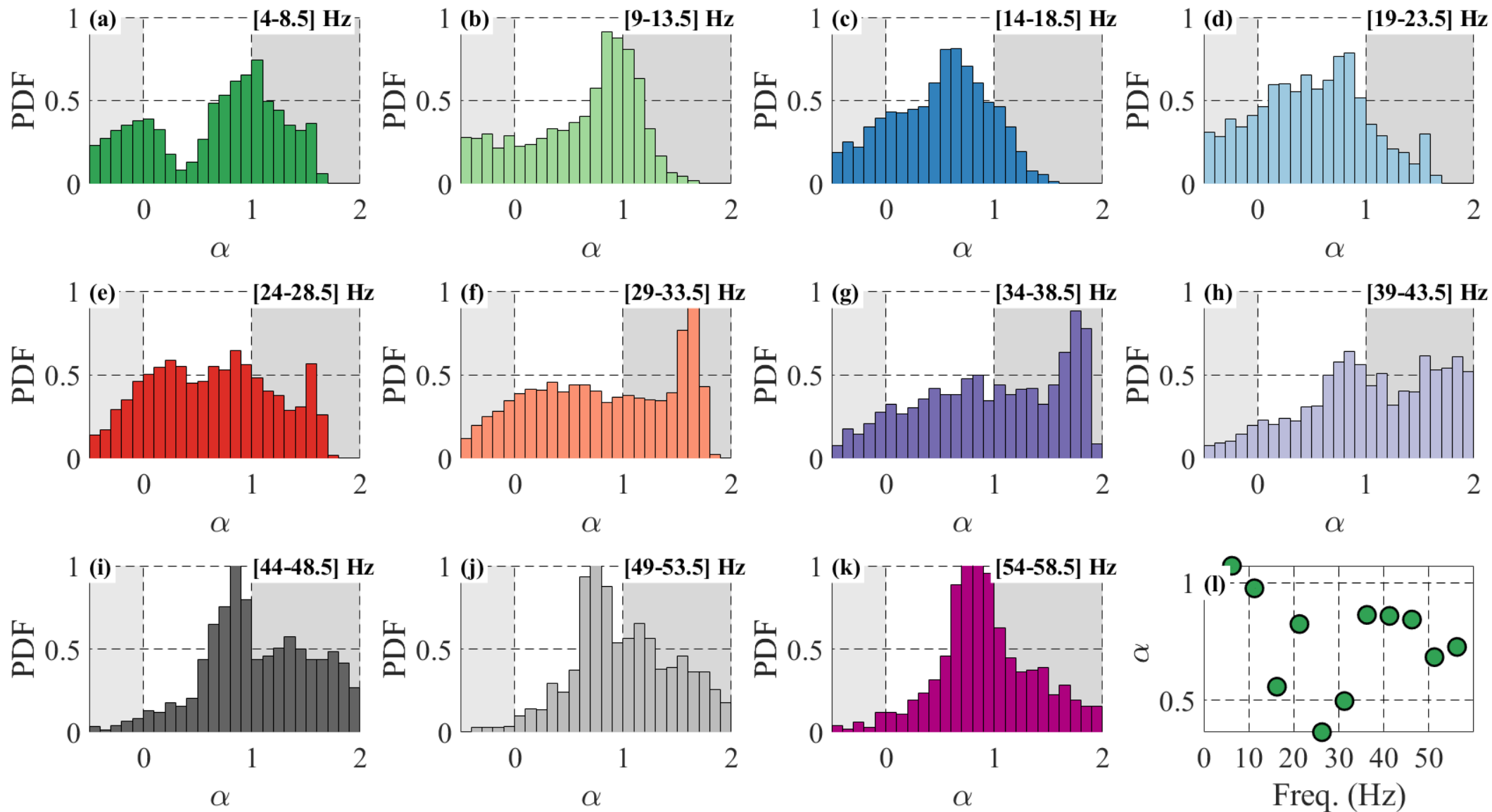


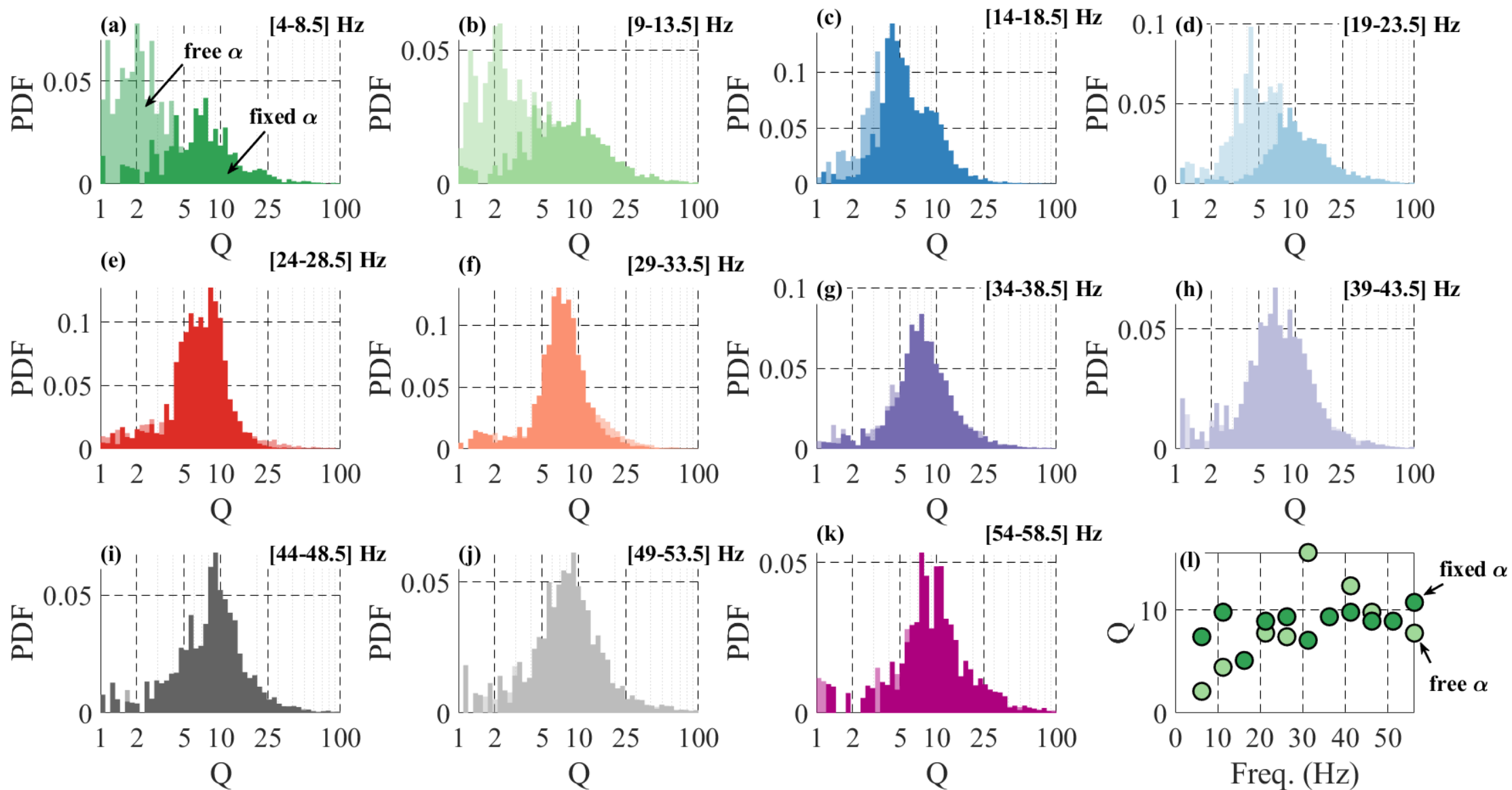


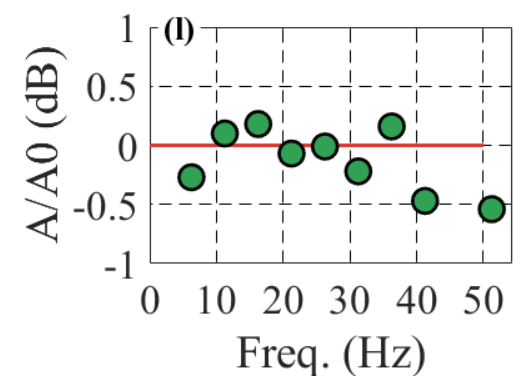
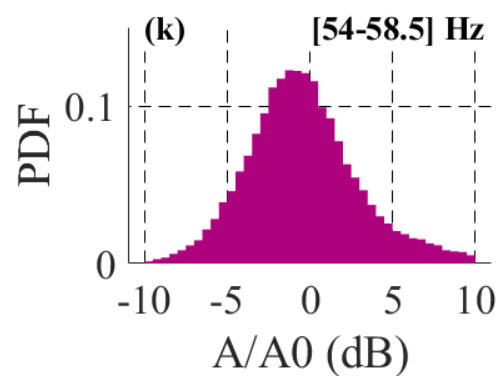
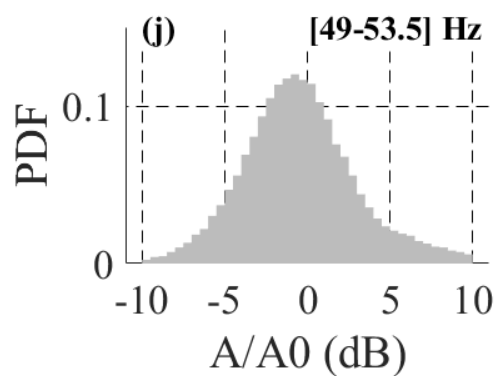
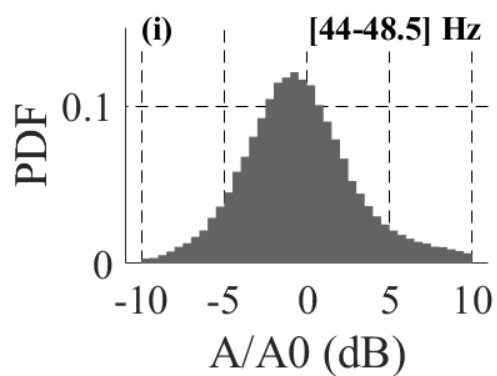
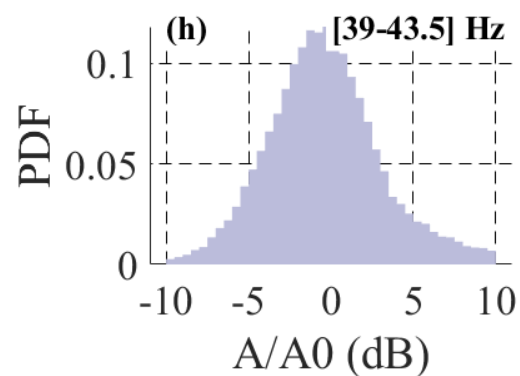
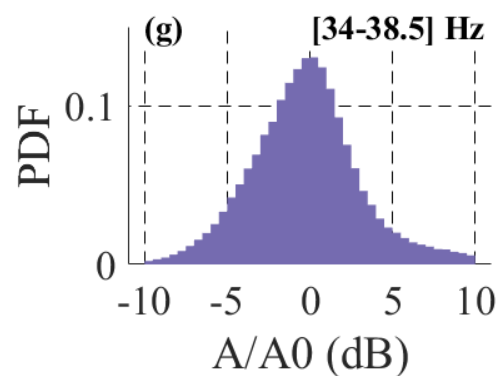
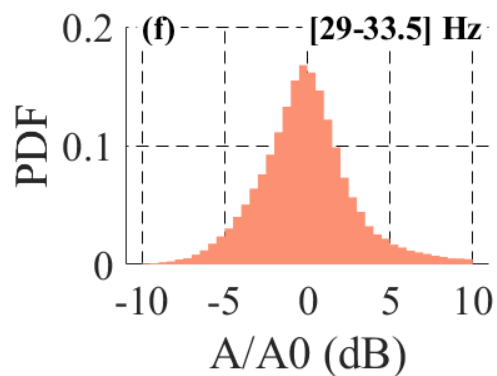
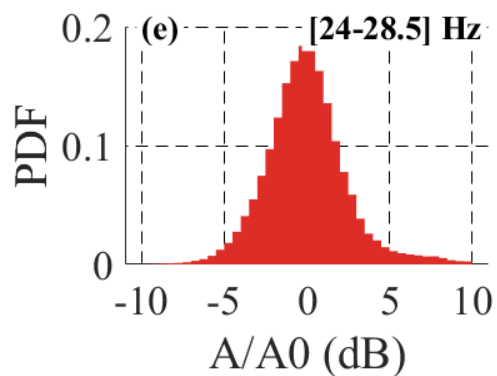
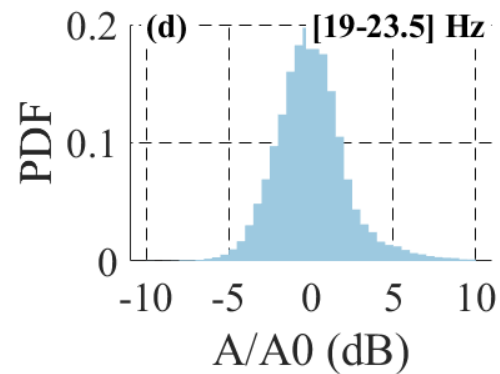
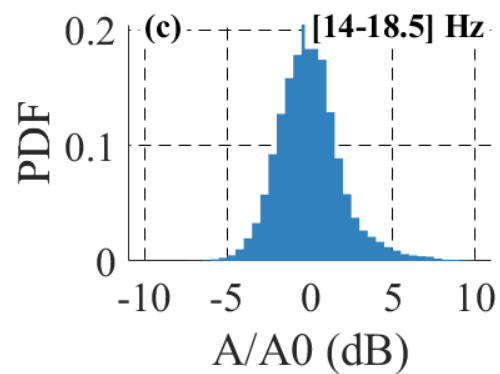
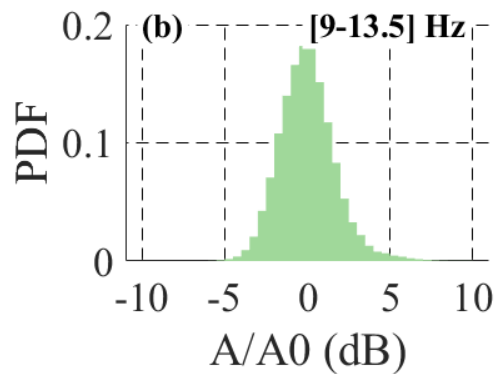
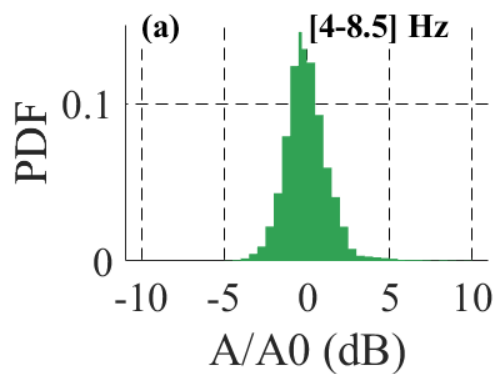


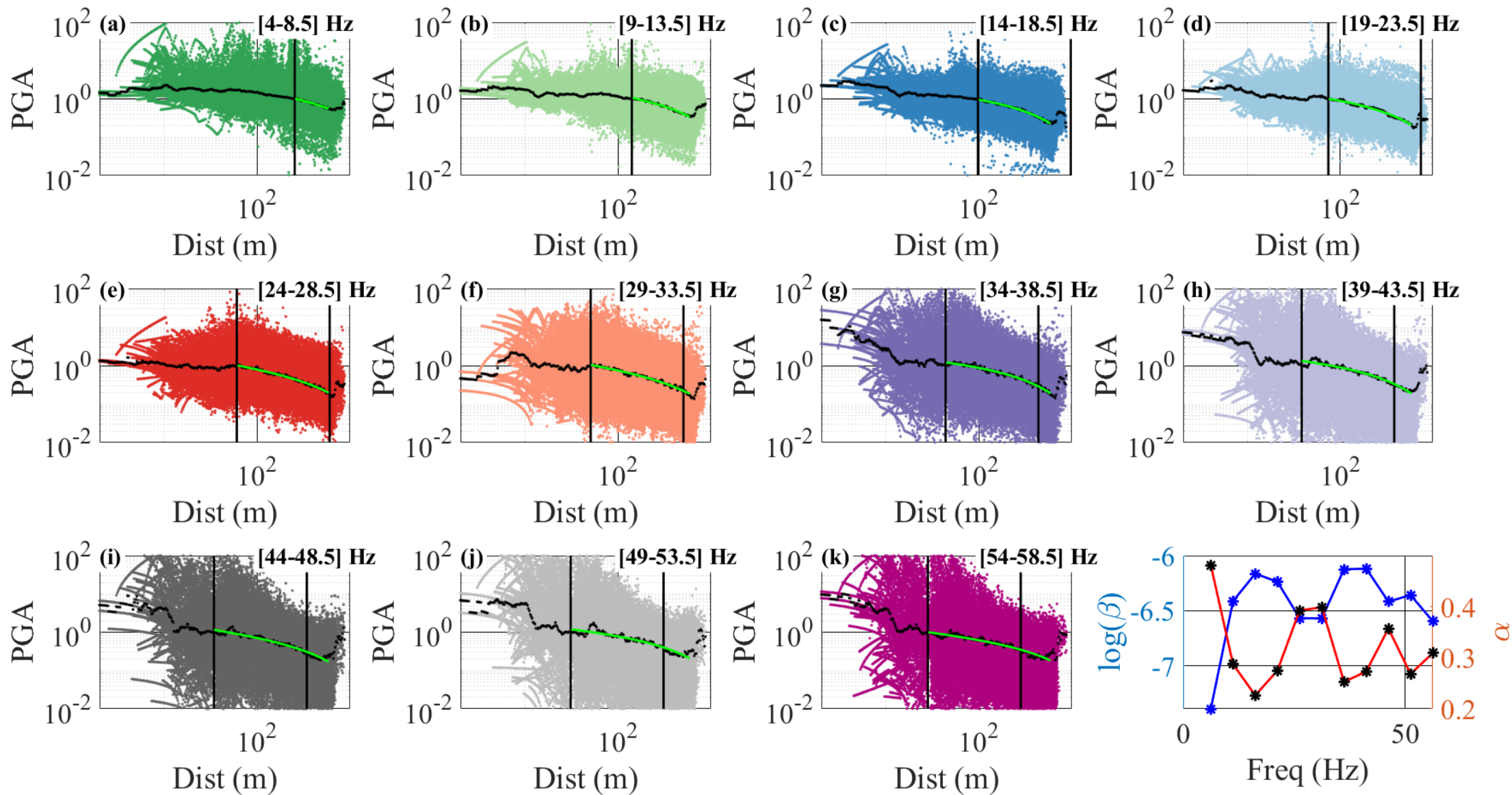




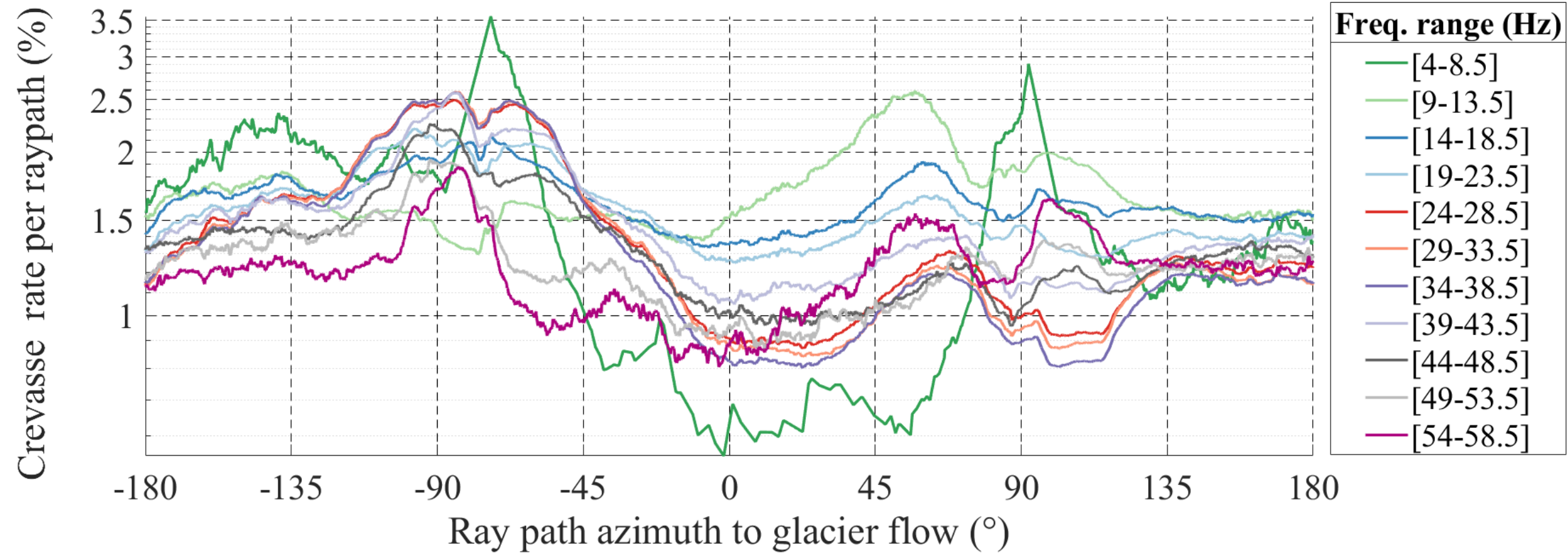




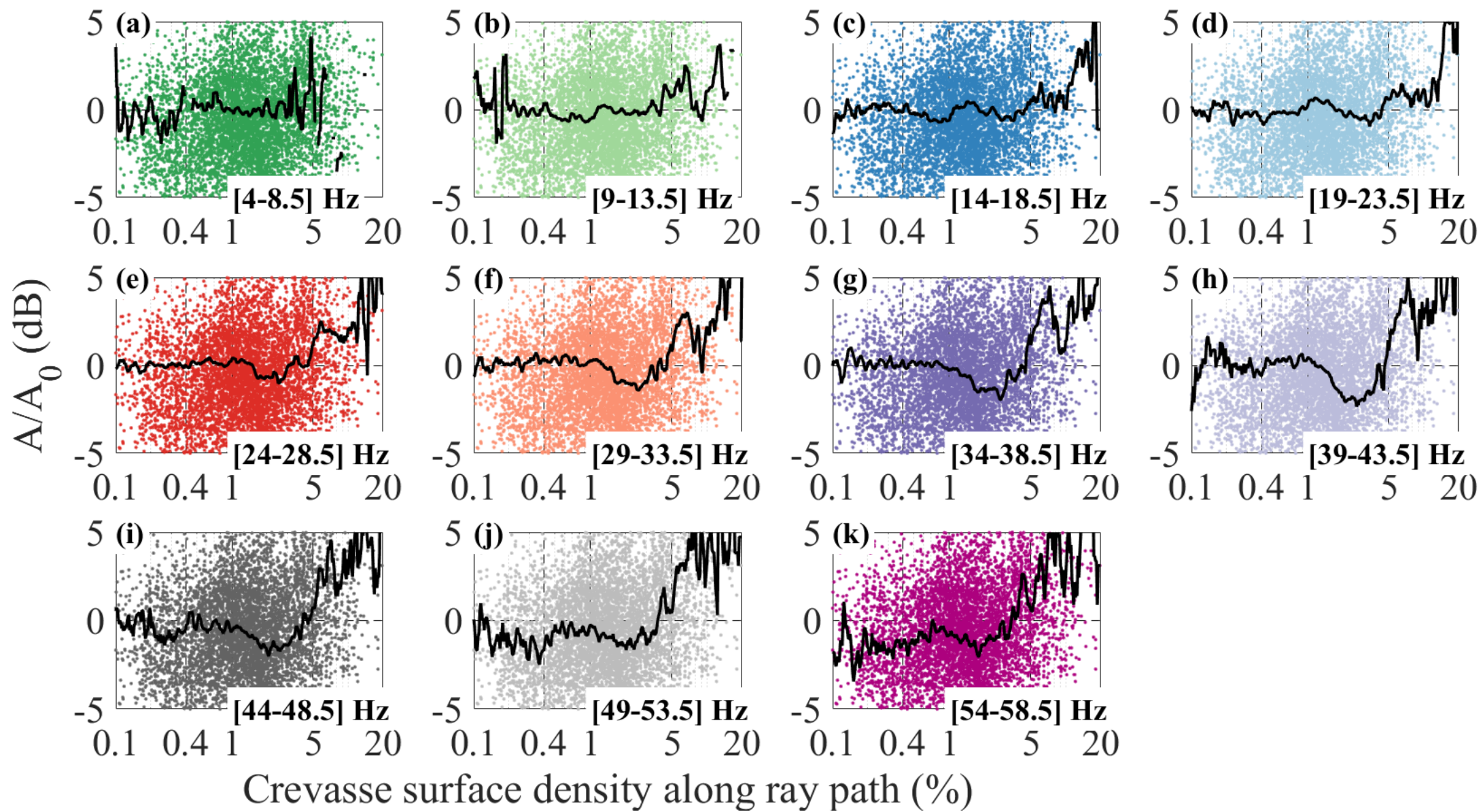


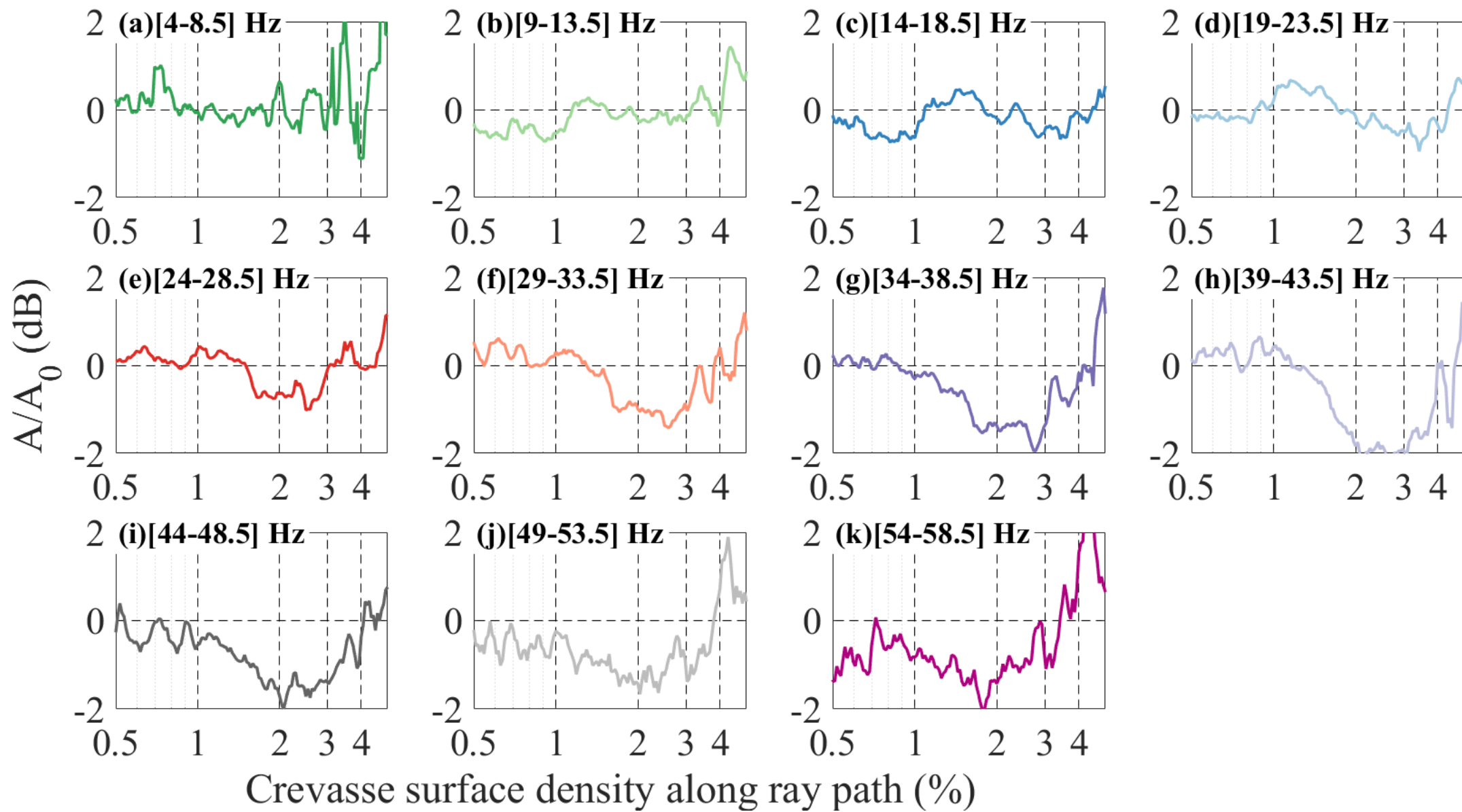




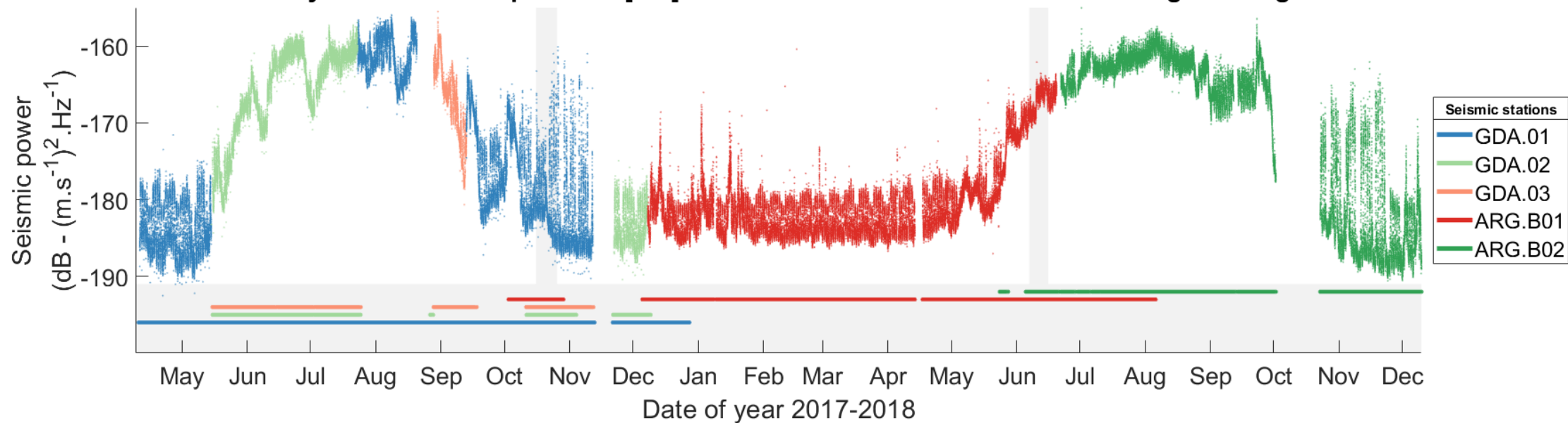






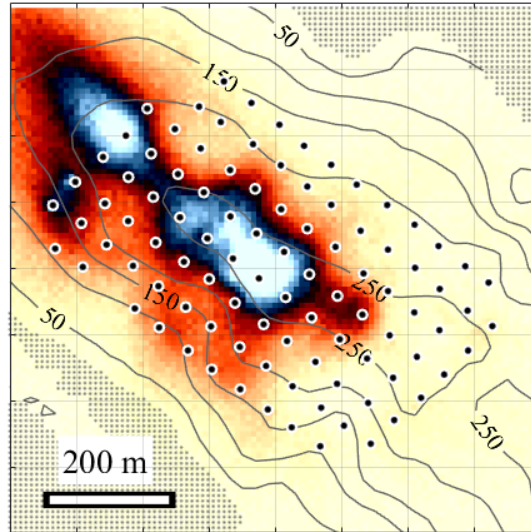


Assembly of the seismic power at [3-5] Hz from the five seismic stations at Argentière glacier

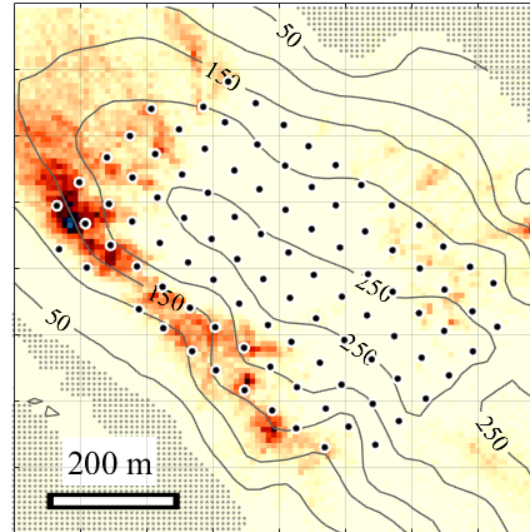


Max.  
Norm. prob. of source location  
Null

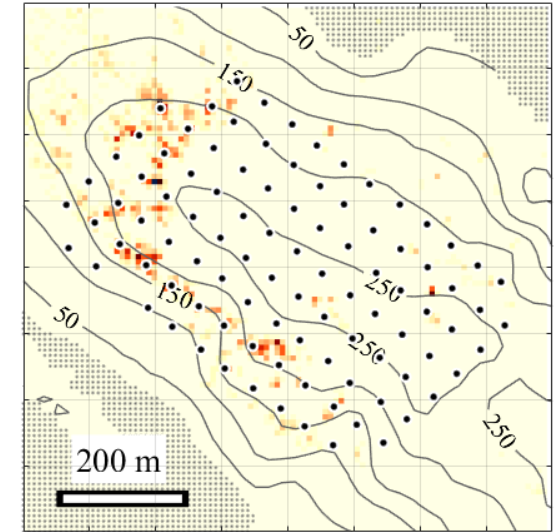
a) Beam [0.07-0.16]  
 $5 \pm 2$  Hz



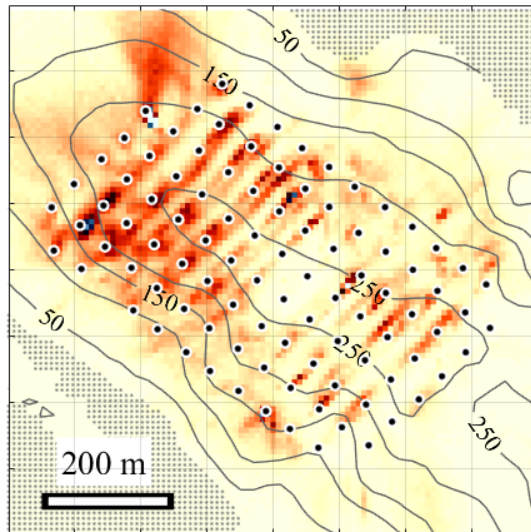
b) Beam [0.4-0.6]  
 $5 \pm 2$  Hz



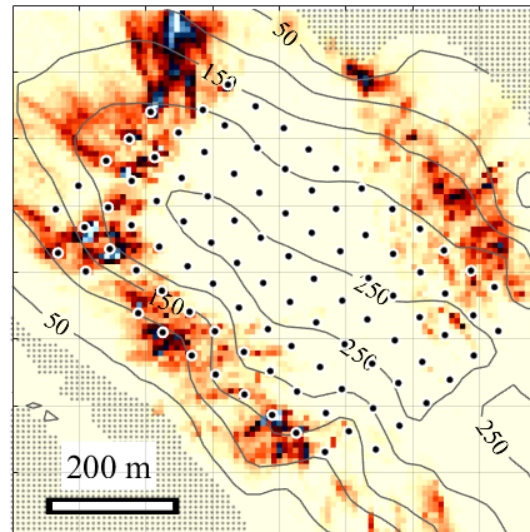
c) Beam [0.75-0.99]  
 $5 \pm 2$  Hz



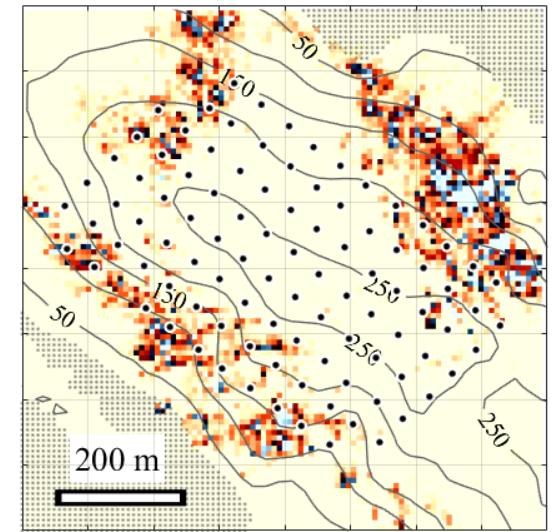
d) Beam [0.07-0.16]  
 $15 \pm 4$  Hz

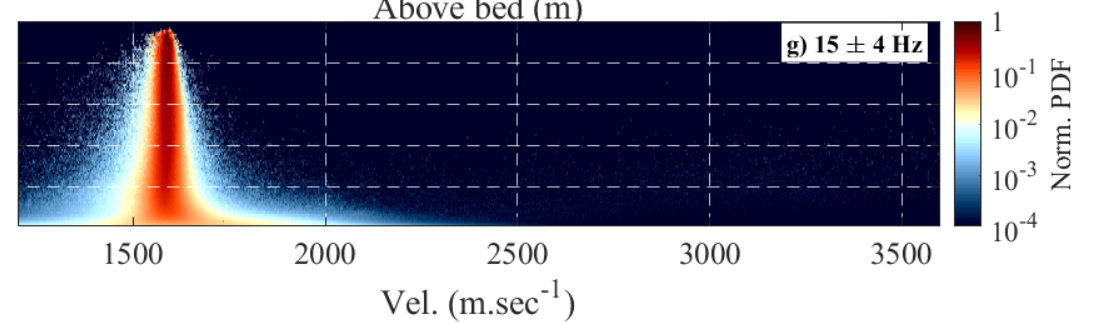
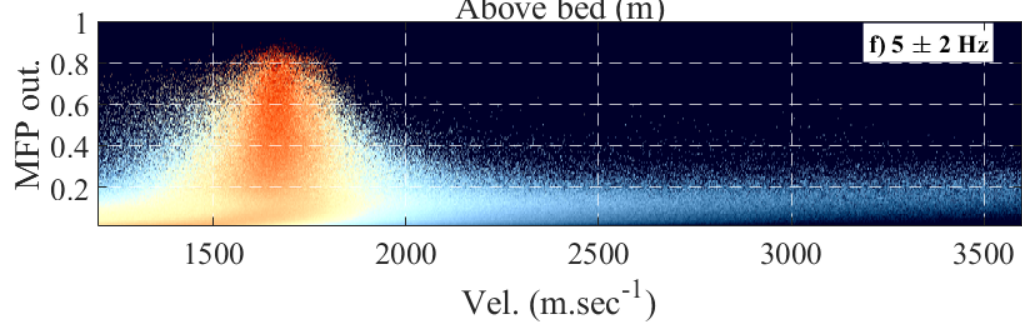
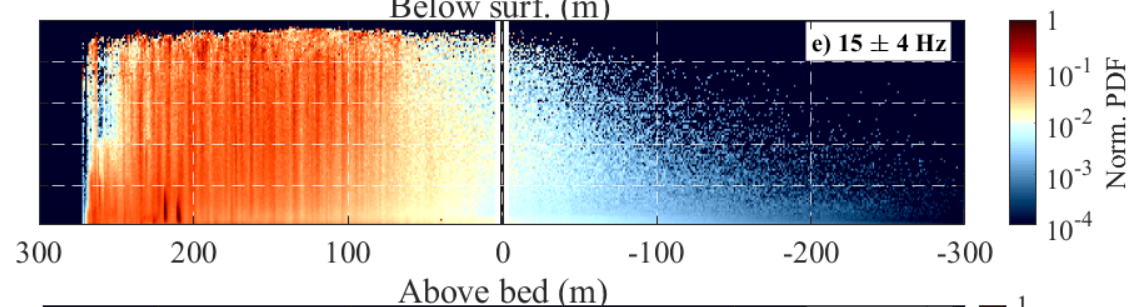
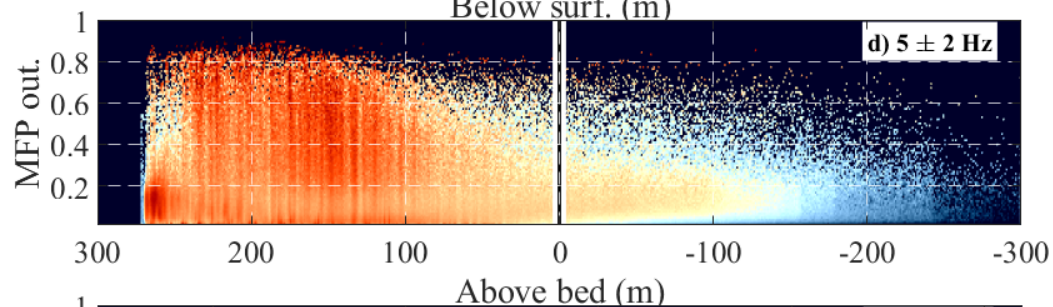
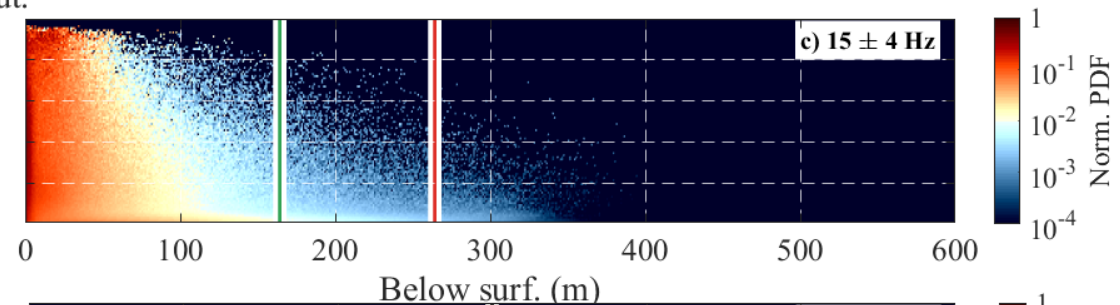
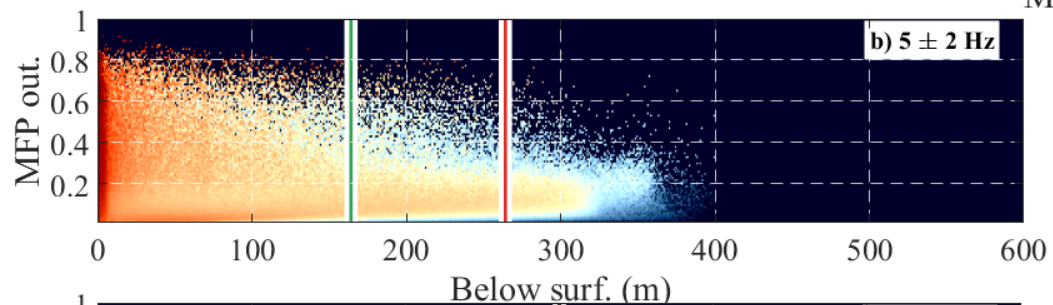
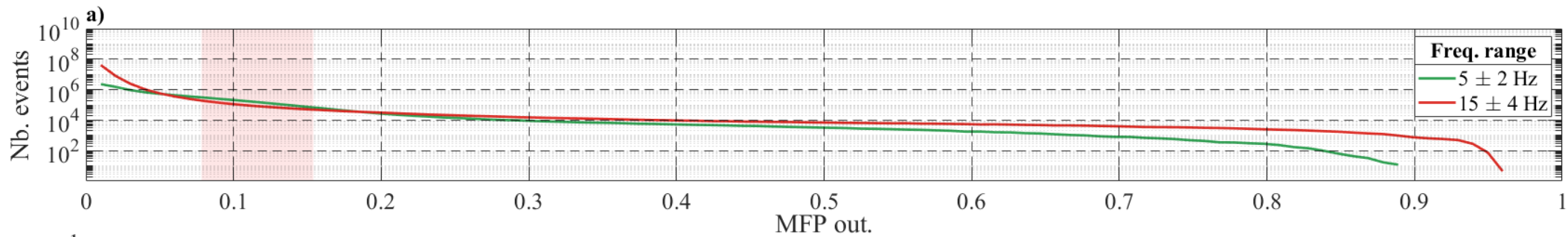


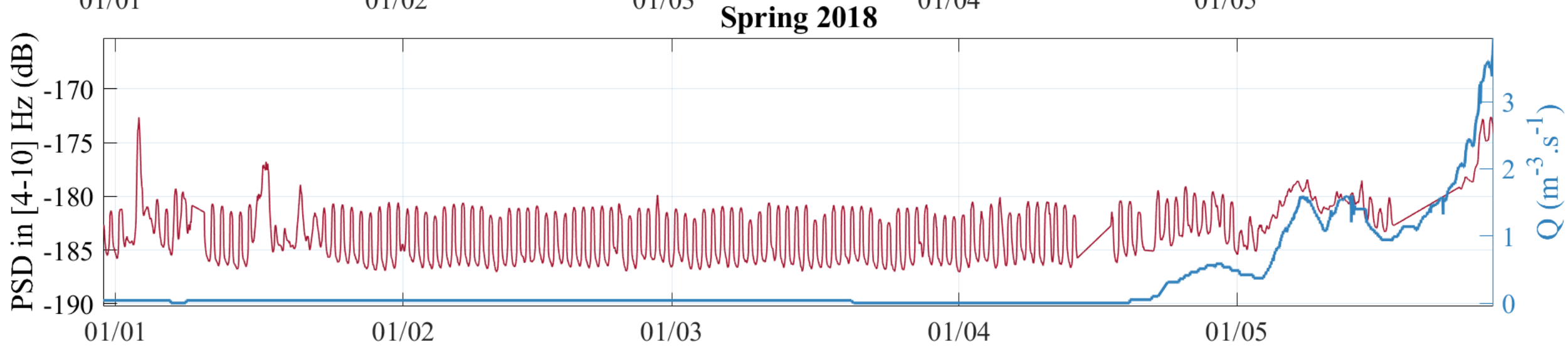
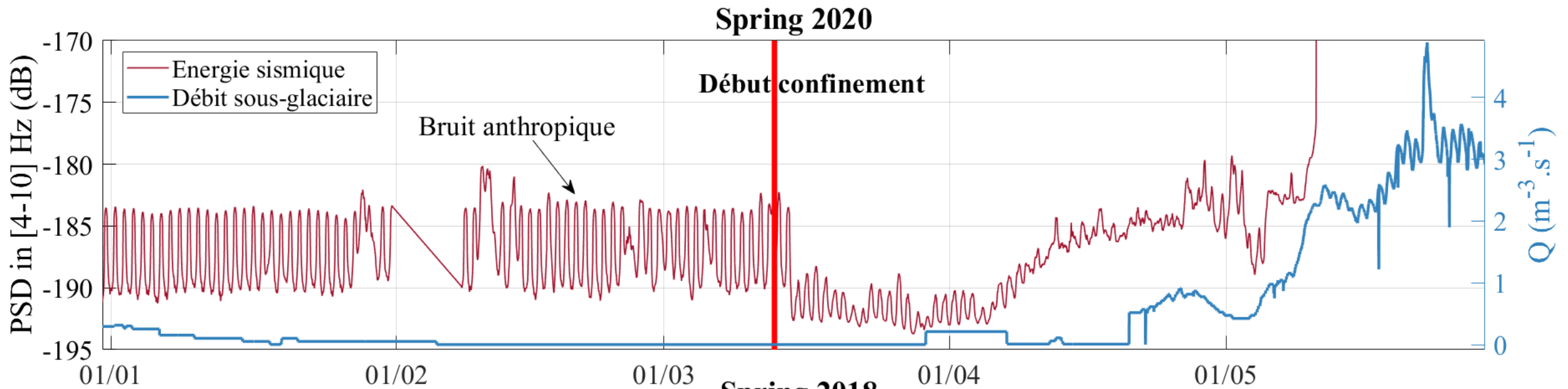
e) Beam [0.4-0.6]  
 $15 \pm 4$  Hz



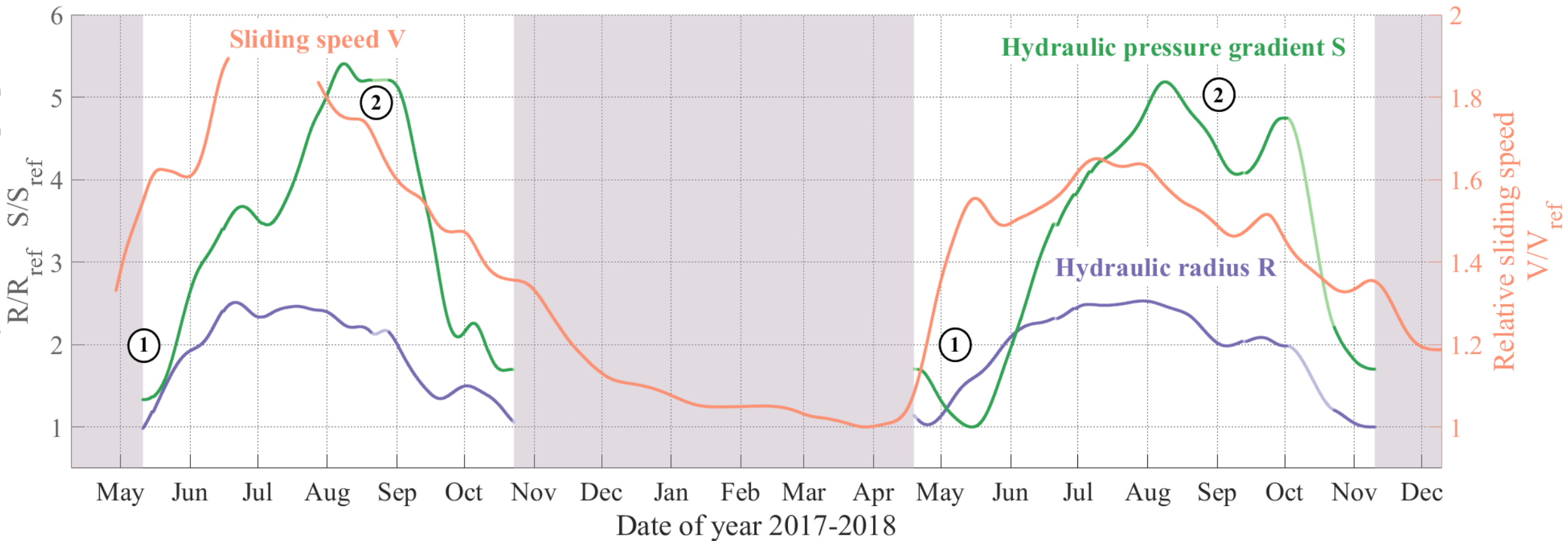
f) Beam [0.75-0.99]  
 $15 \pm 4$  Hz



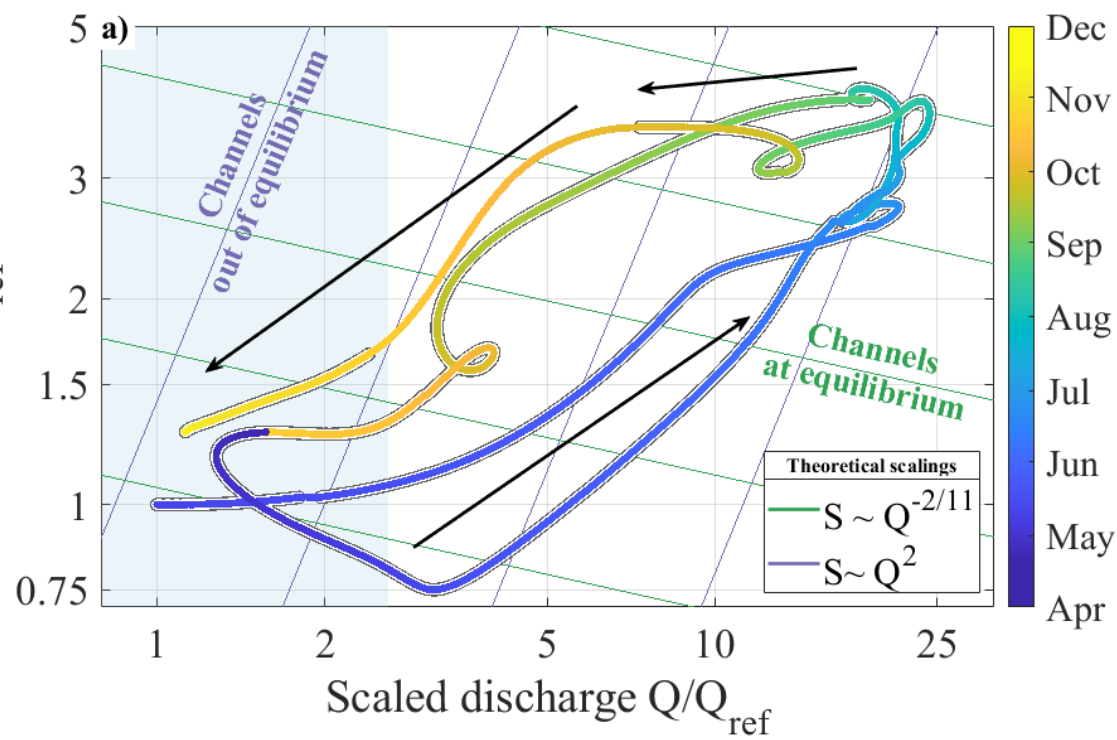




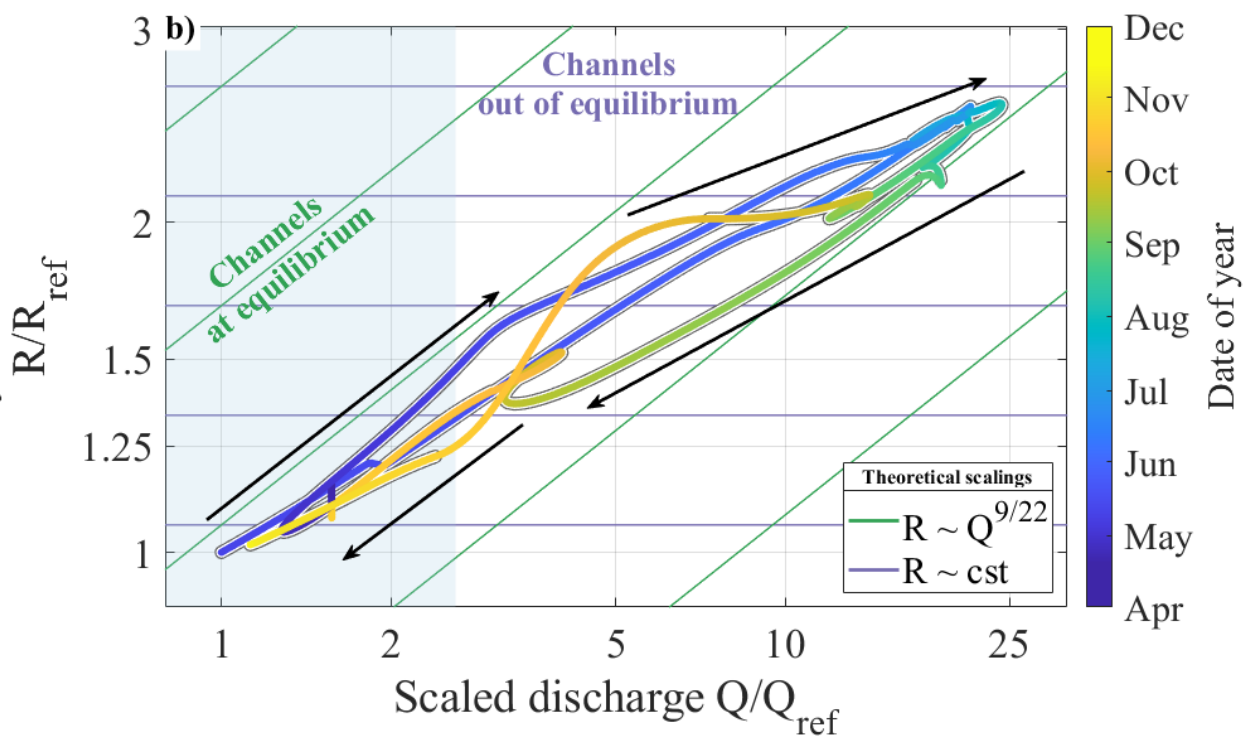
Channels hydraulic relative properties



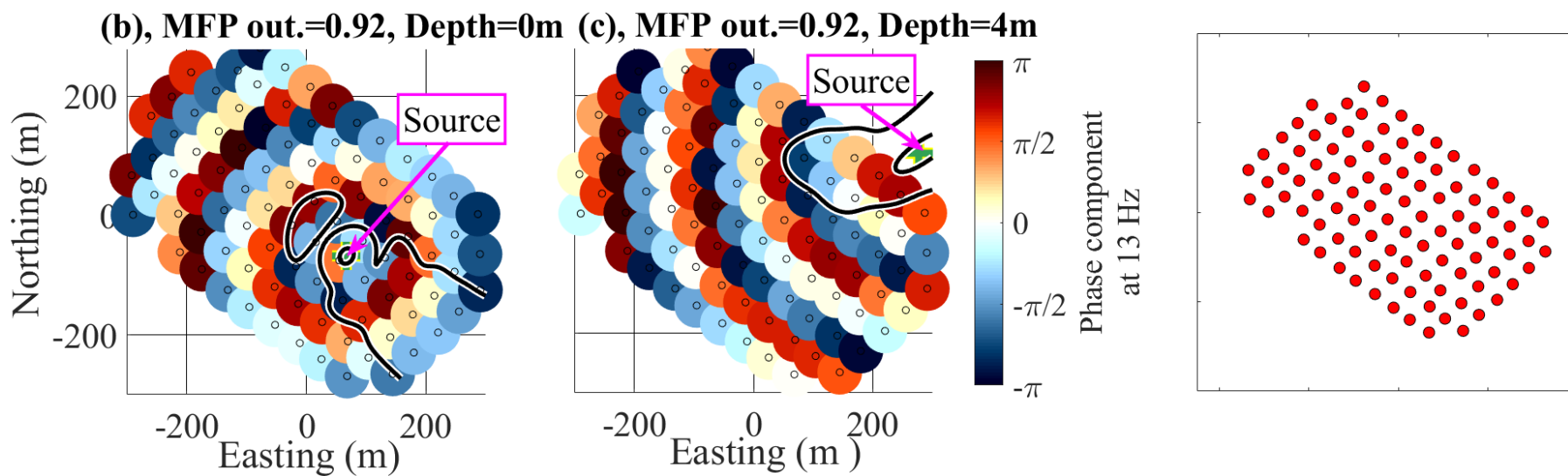
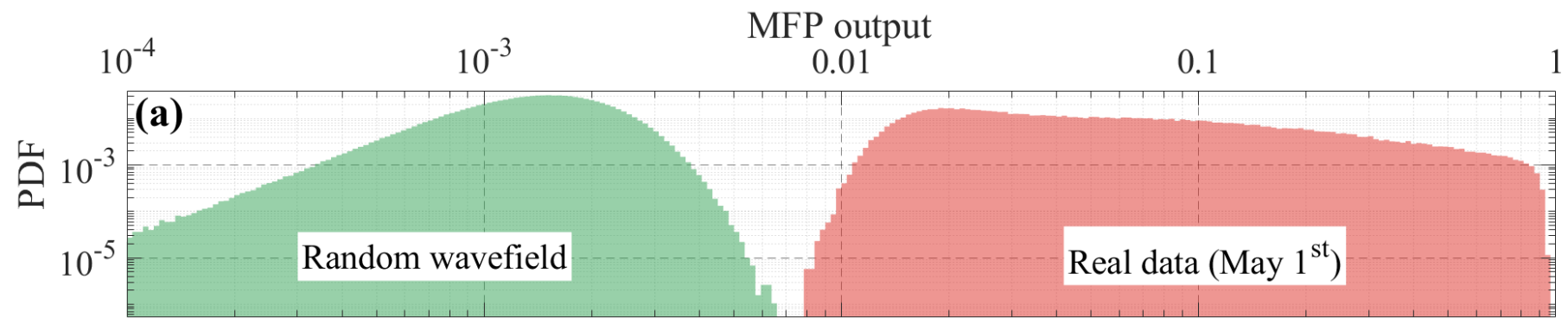
Rel. Hydraulic Pressure Gradient

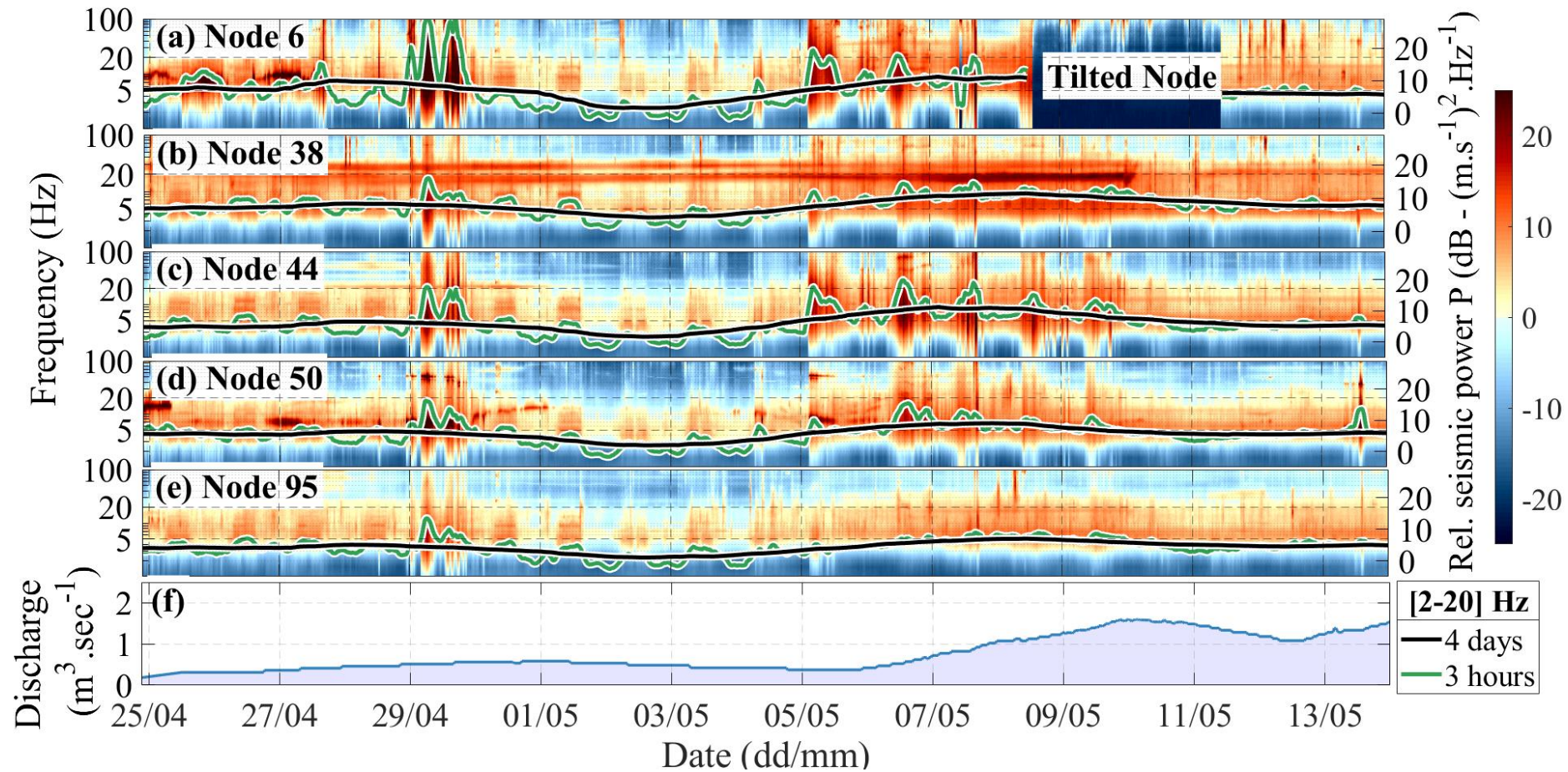


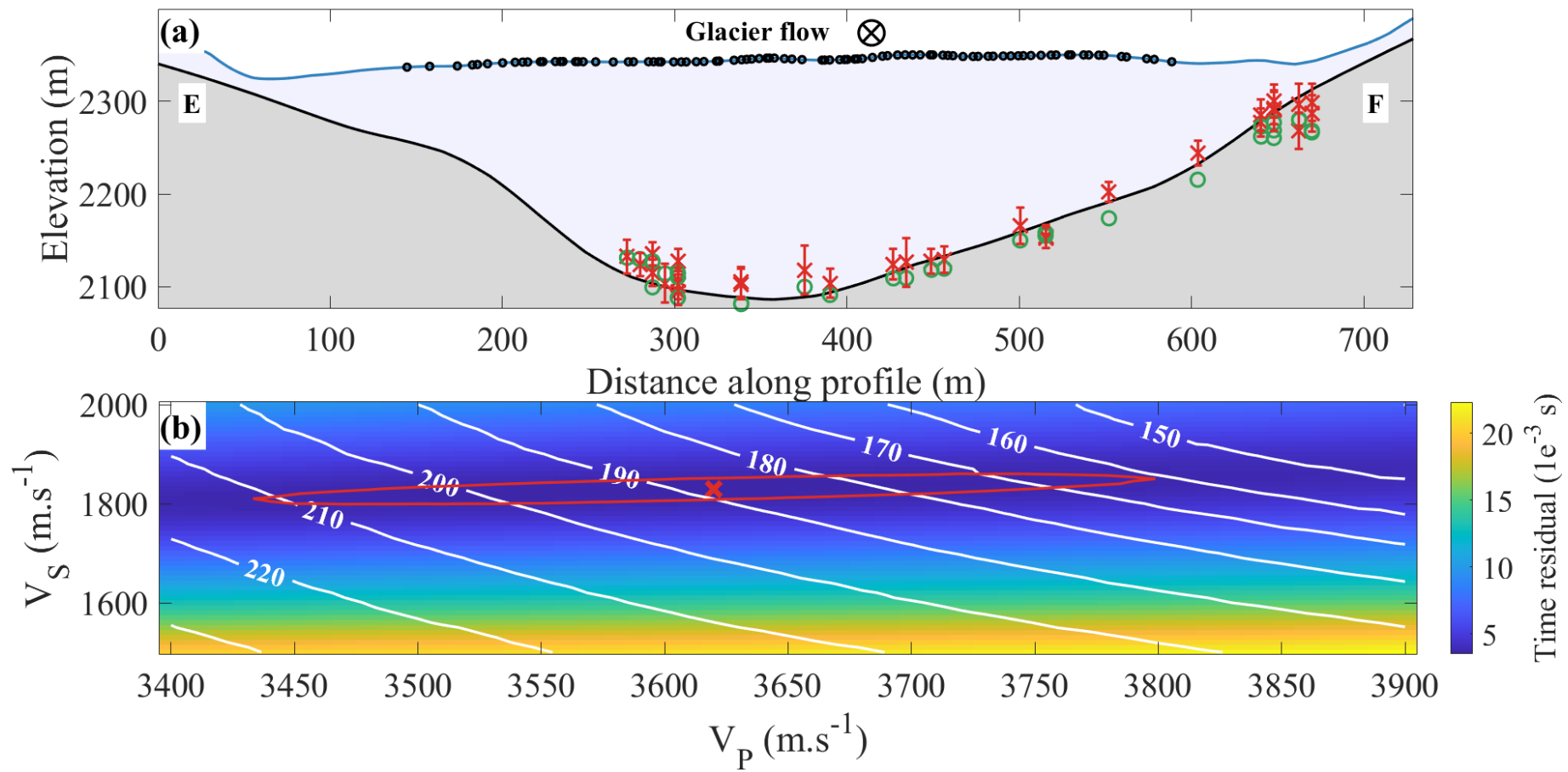
Rel. Hydraulic Radius

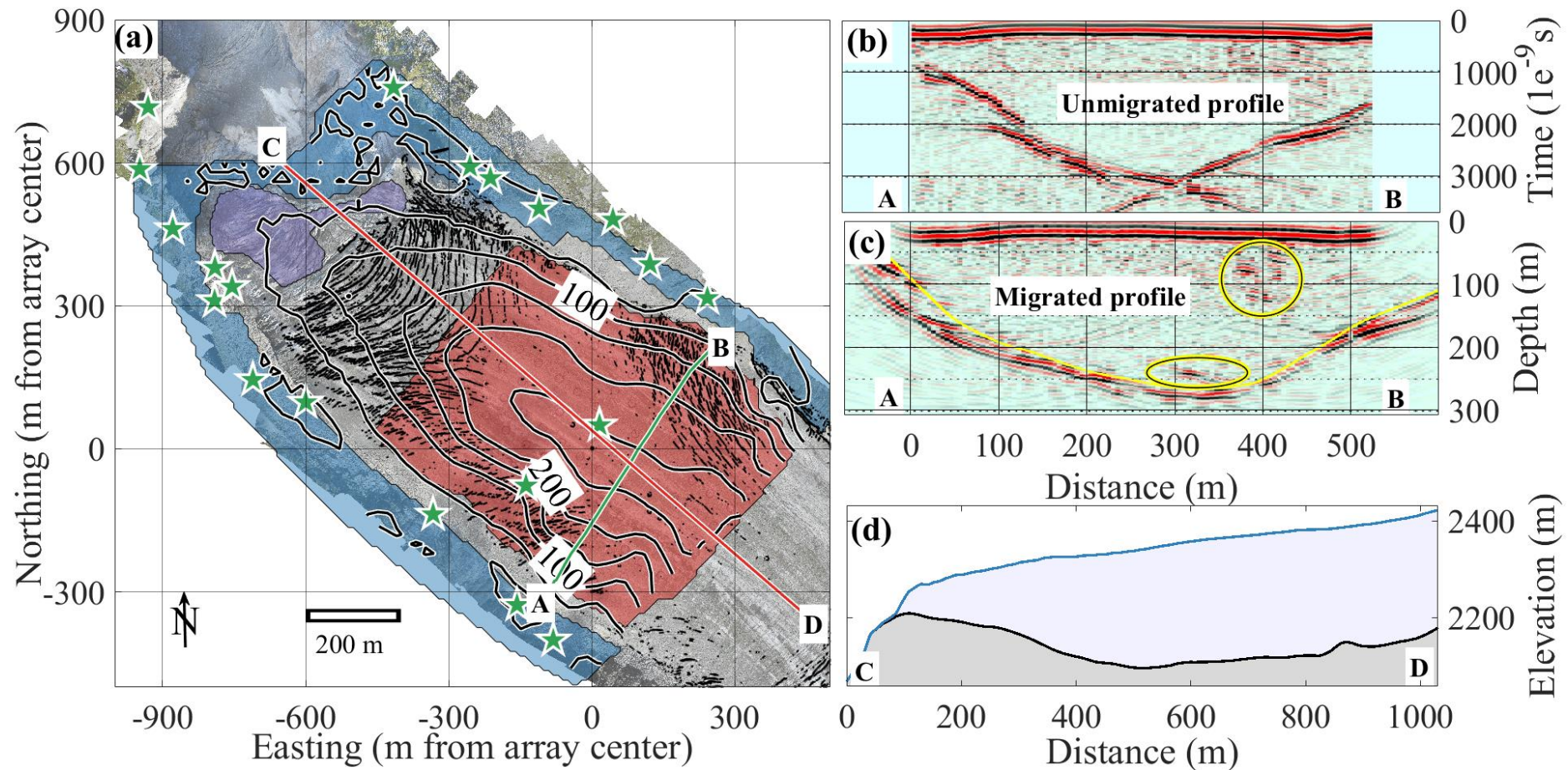


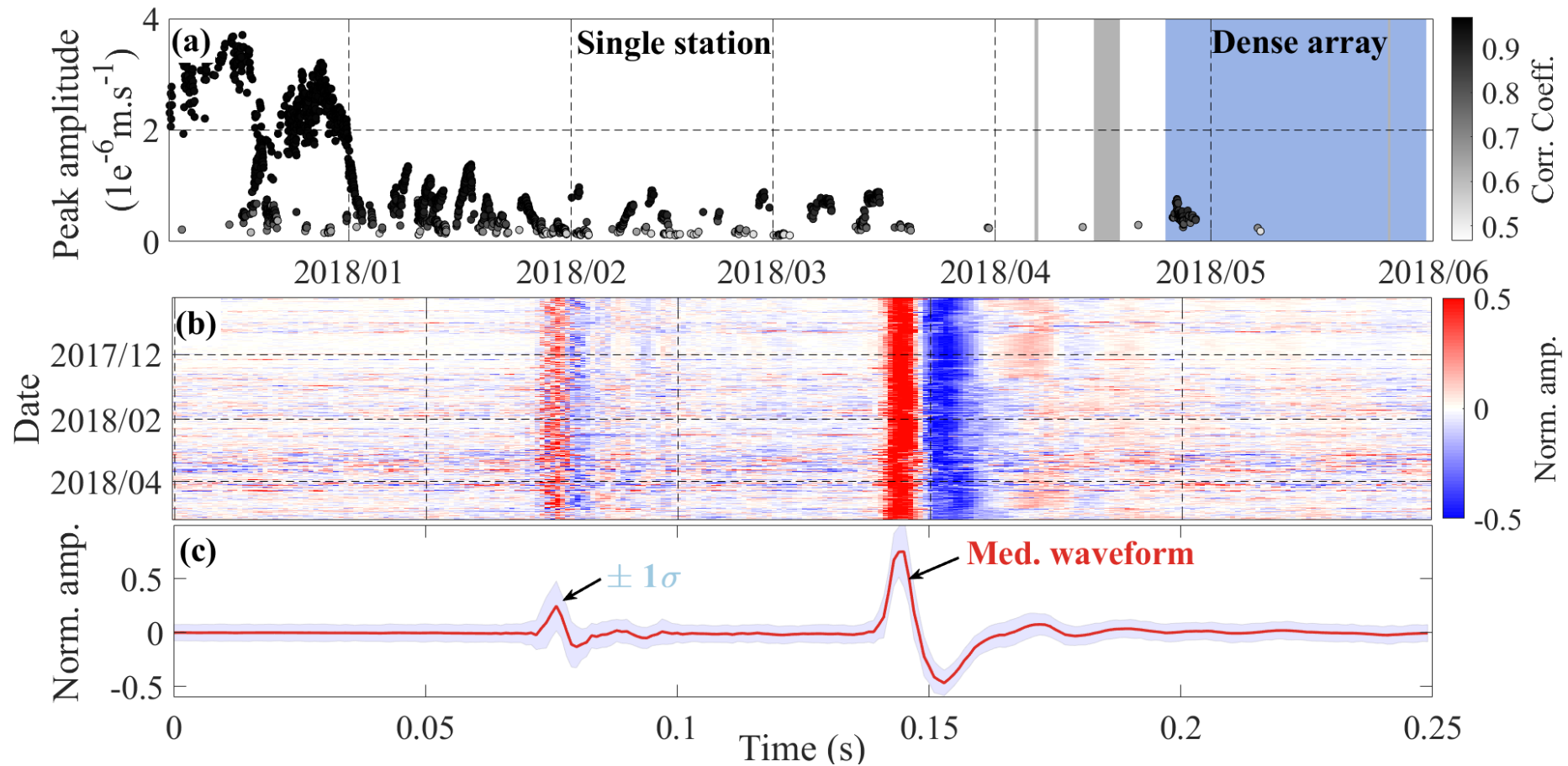


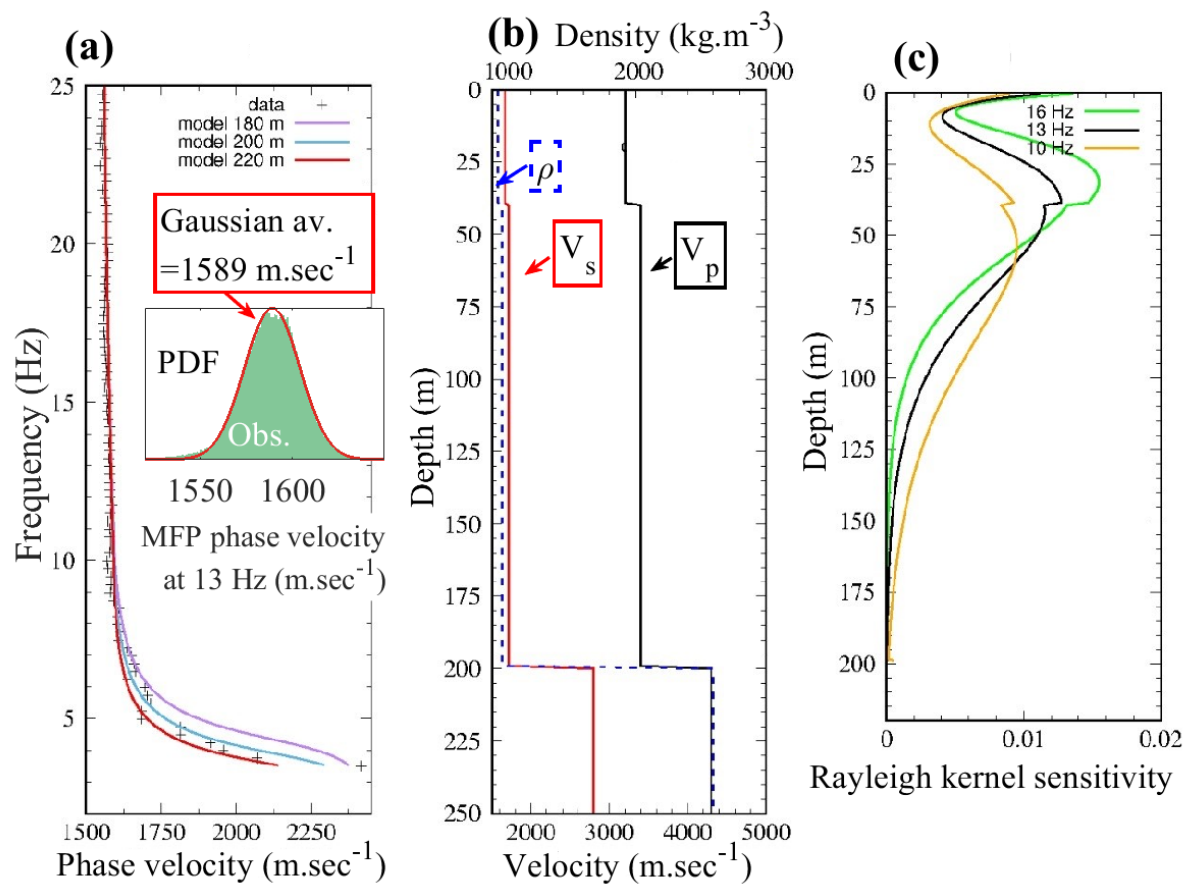




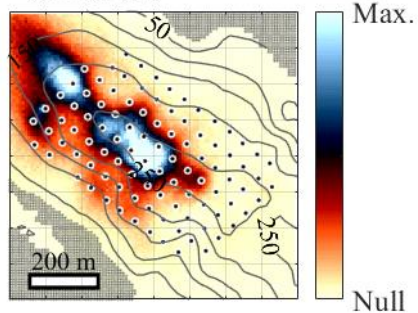




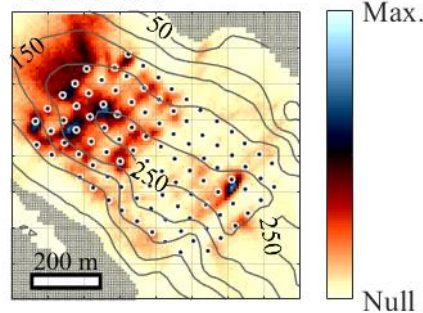




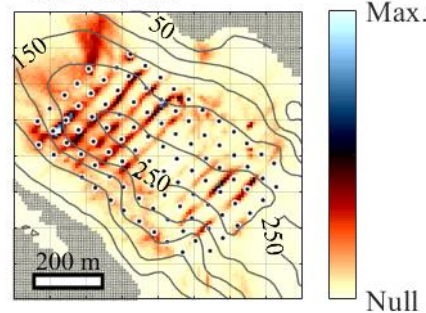
**a) Beam [0.07-0.16]**  
 **$5 \pm 2$  Hz**



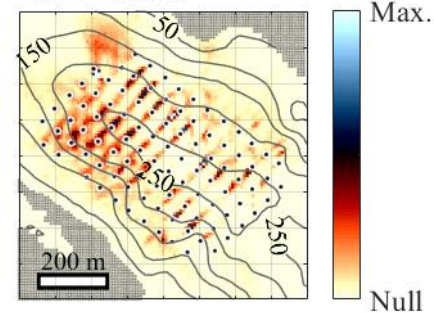
**b) Beam [0.07-0.16]**  
 **$9 \pm 2$  Hz**



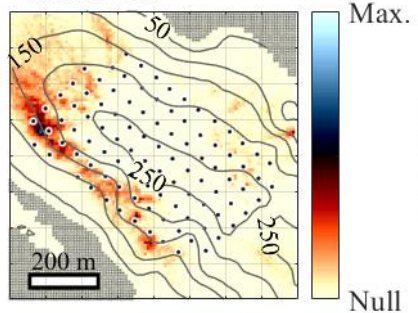
**c) Beam [0.07-0.16]**  
 **$13 \pm 2$  Hz**



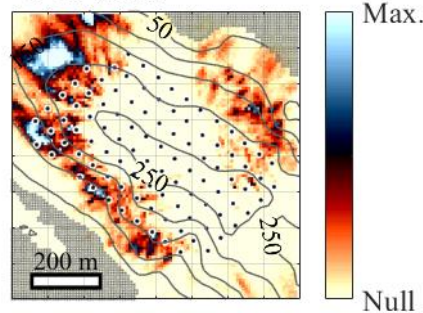
**d) Beam [0.07-0.16]**  
 **$17 \pm 2$  Hz**



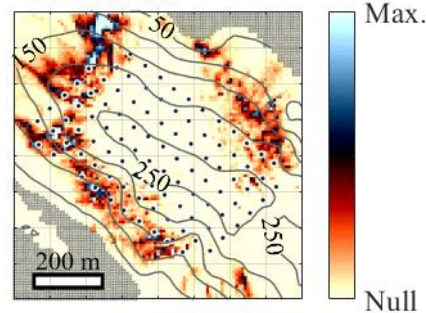
**e) Beam [0.4-0.6]**  
 **$5 \pm 2$  Hz**



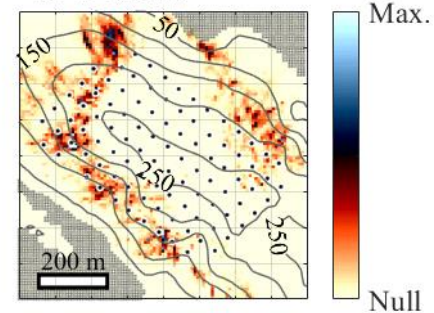
**f) Beam [0.4-0.6]**  
 **$9 \pm 2$  Hz**



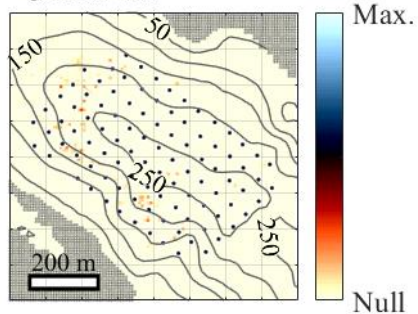
**g) Beam [0.4-0.6]**  
 **$13 \pm 2$  Hz**



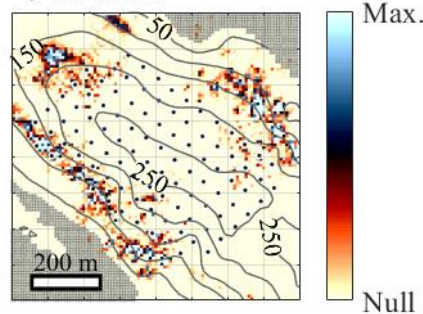
**h) Beam [0.4-0.6]**  
 **$17 \pm 2$  Hz**



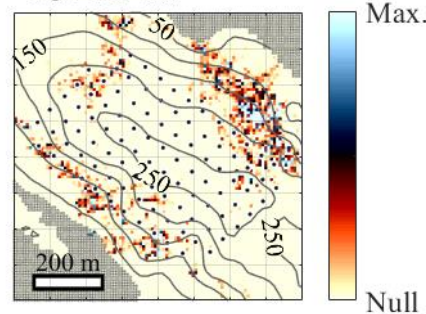
**i) Beam [0.8-0.99]**  
 **$5 \pm 2$  Hz**



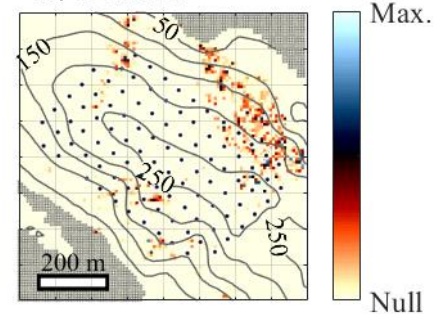
**j) Beam [0.8-0.99]**  
 **$9 \pm 2$  Hz**

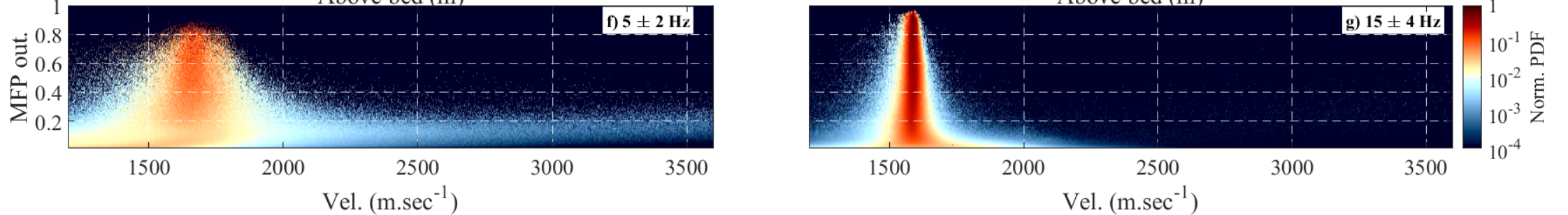
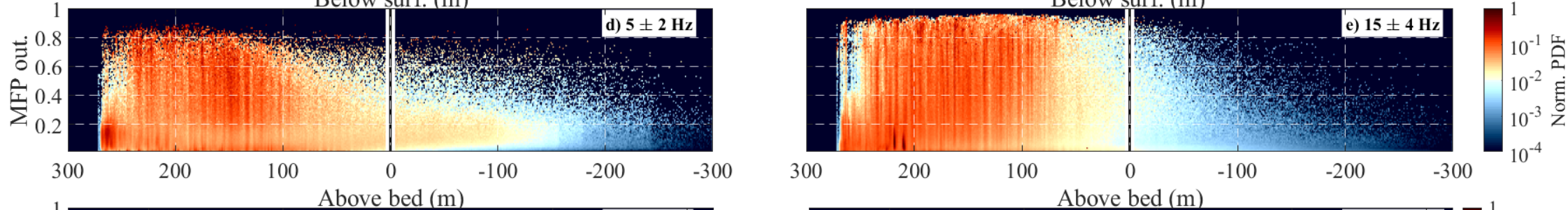
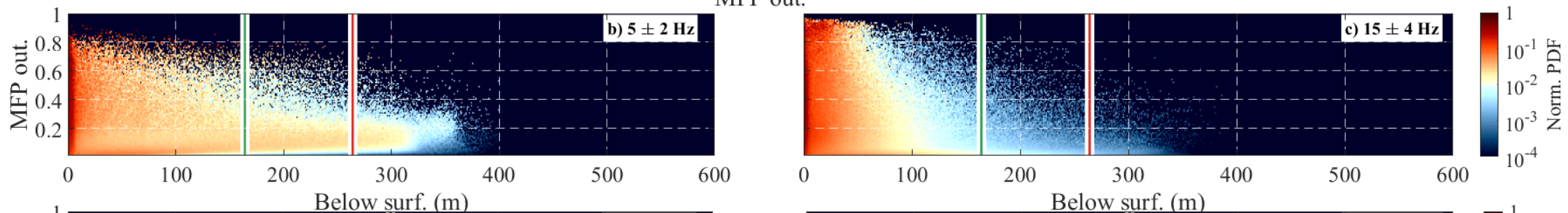
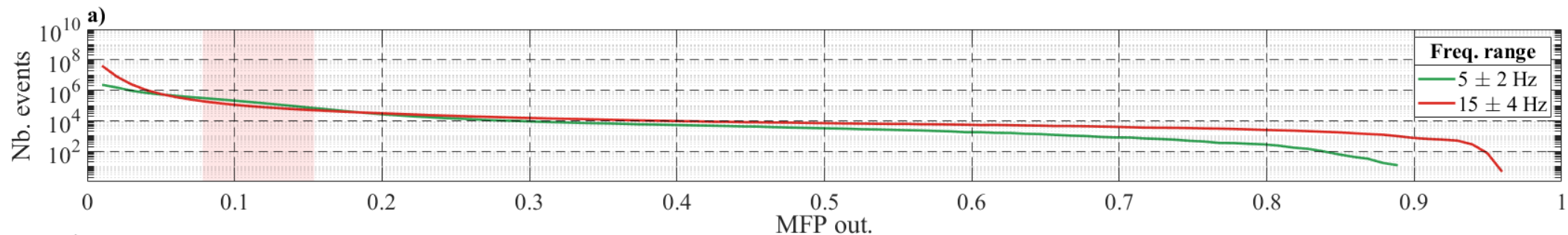


**k) Beam [0.8-0.99]**  
 **$13 \pm 2$  Hz**



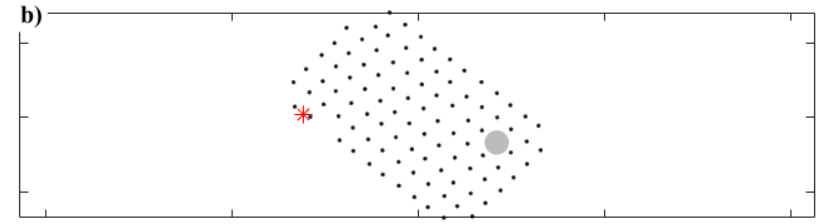
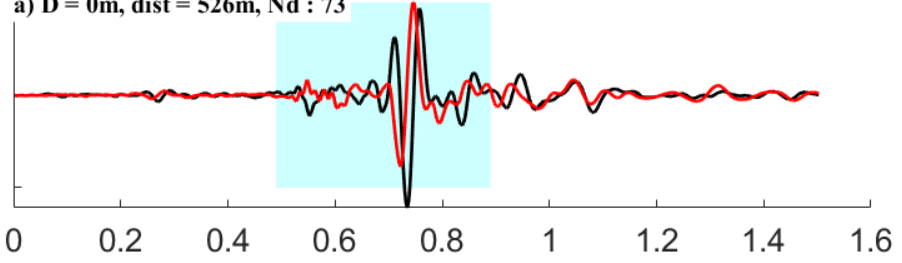
**l) Beam [0.8-0.99]**  
 **$17 \pm 2$  Hz**



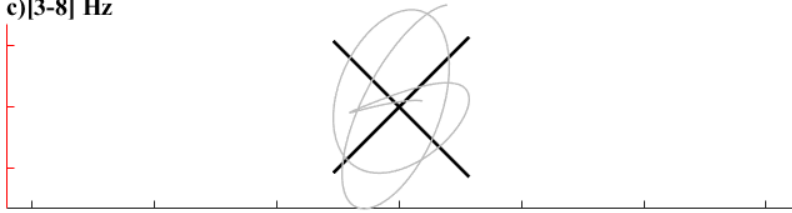




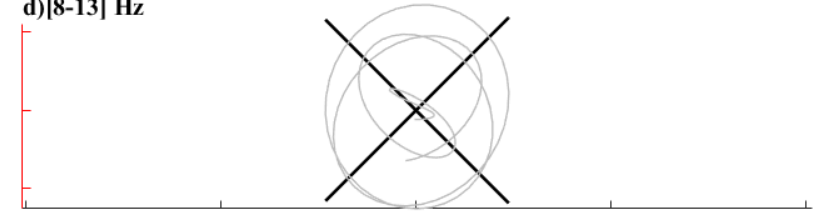
a)  $D = 0\text{m}$ ,  $\text{dist} = 526\text{m}$ ,  $N_d : 73$



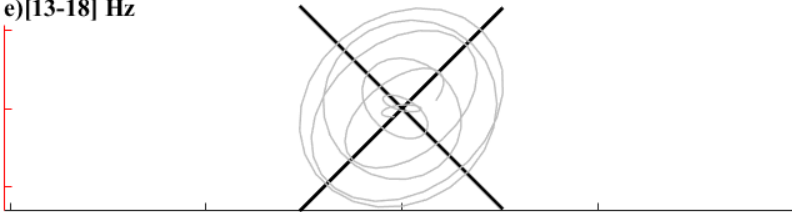
c) [3-8] Hz



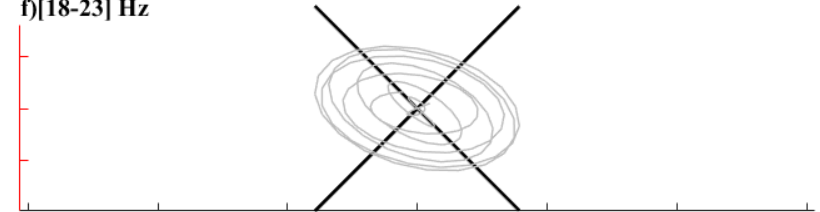
d) [8-13] Hz



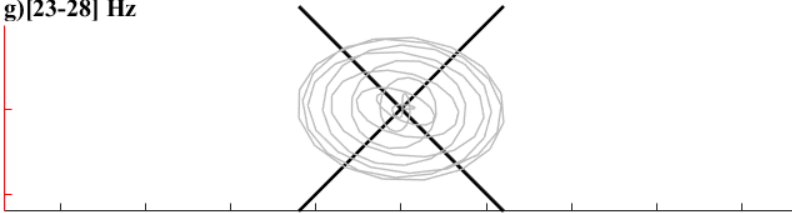
e) [13-18] Hz



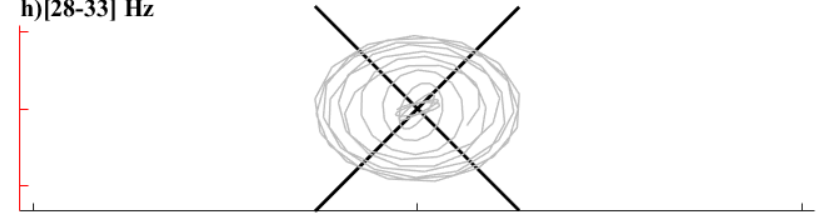
f) [18-23] Hz

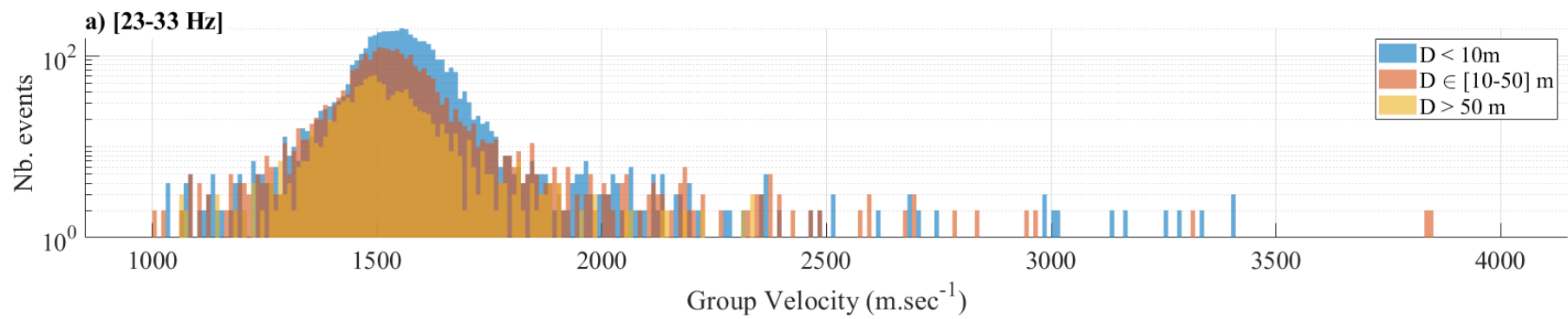
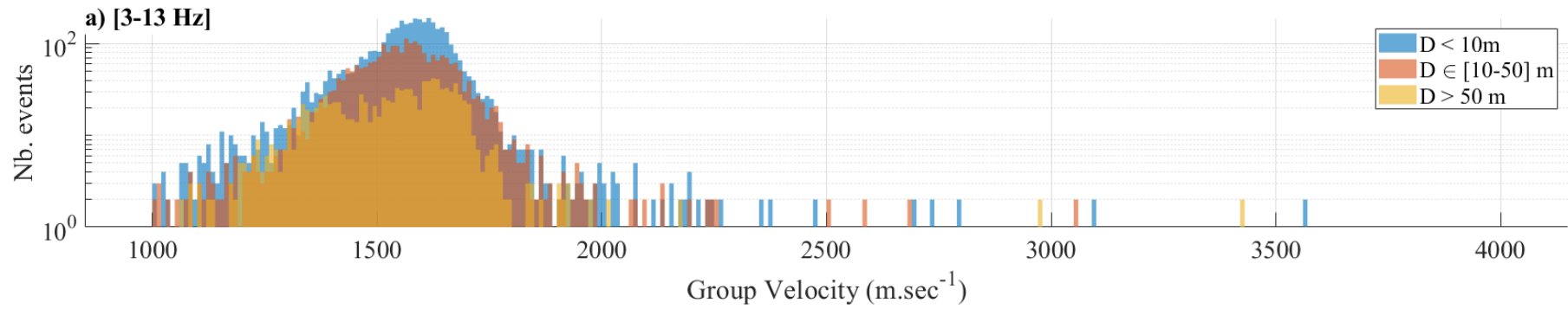


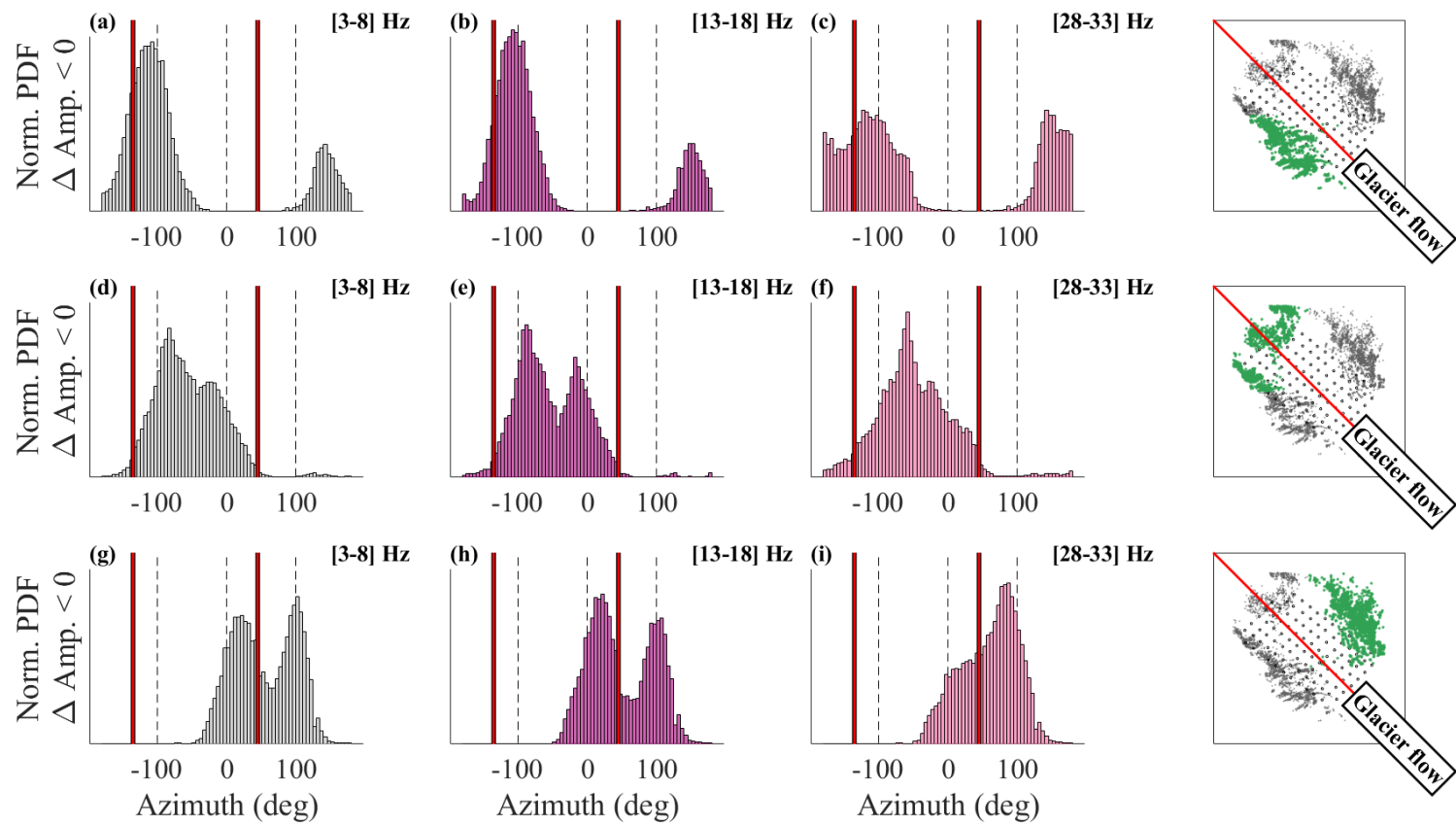
g) [23-28] Hz

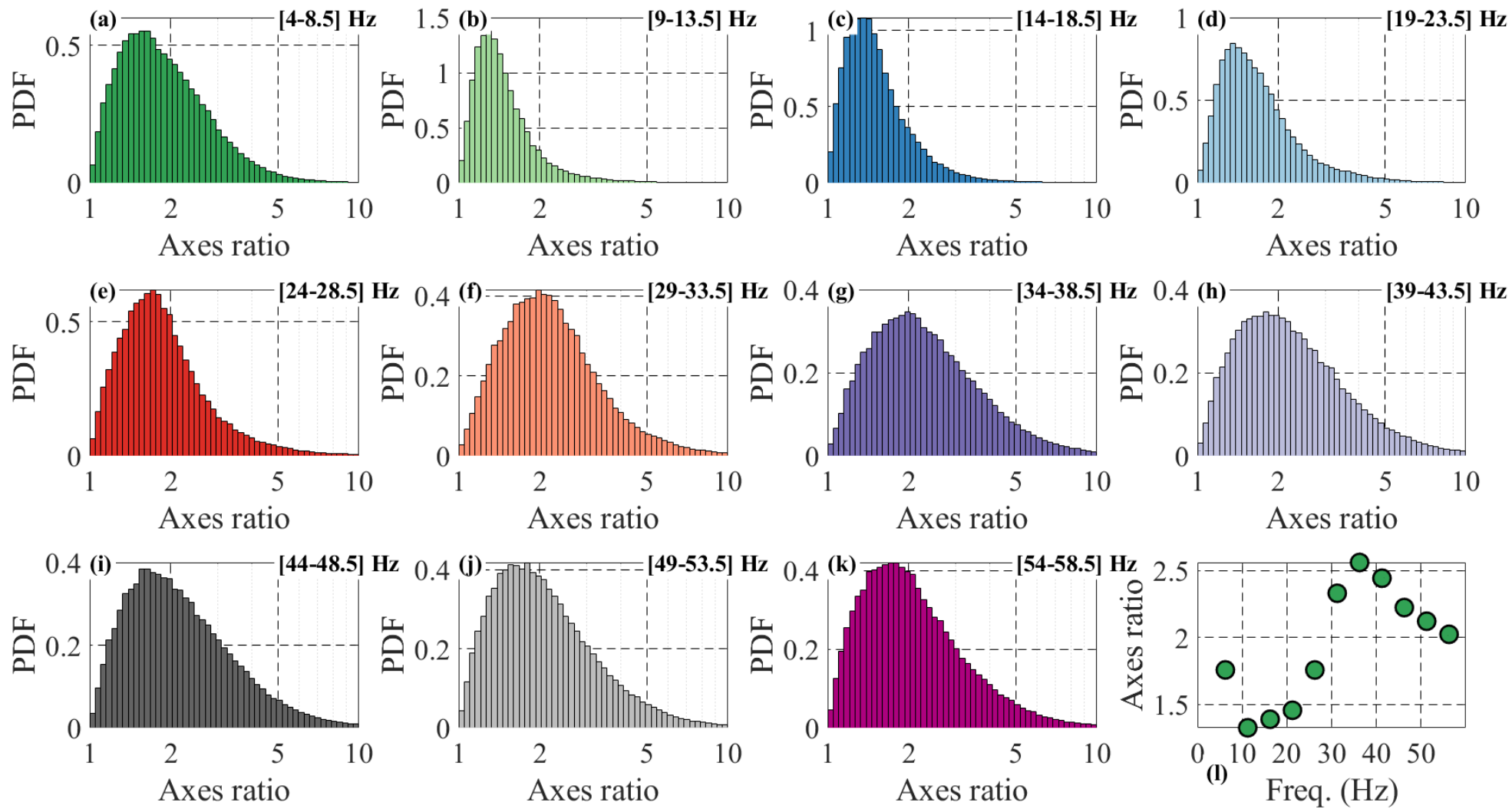


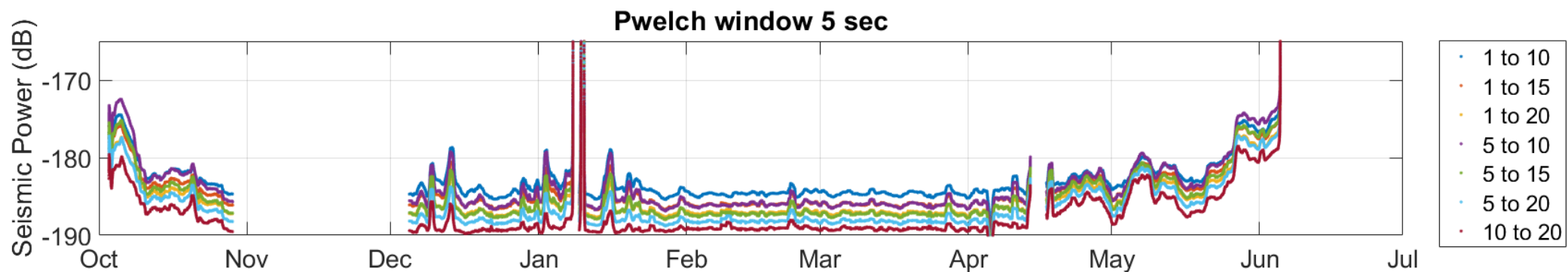
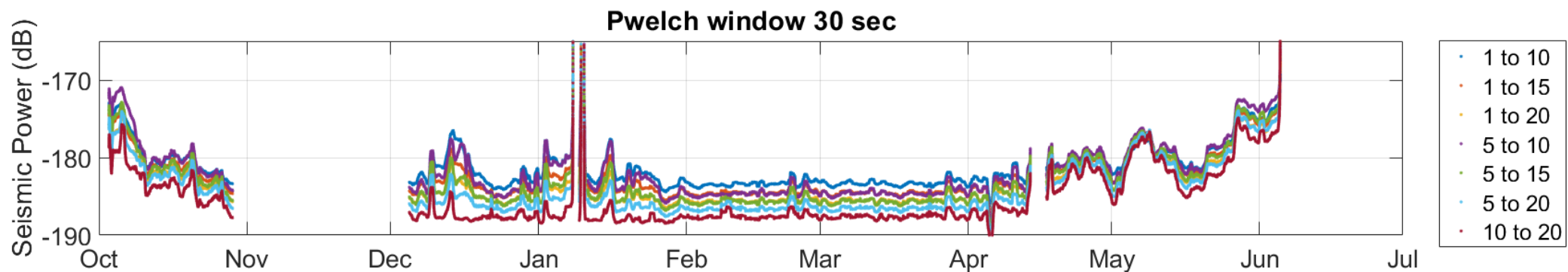
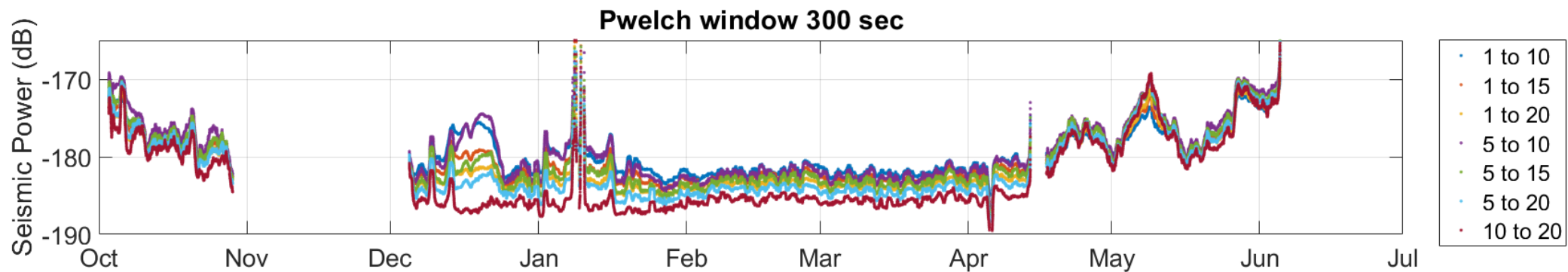
h) [28-33] Hz

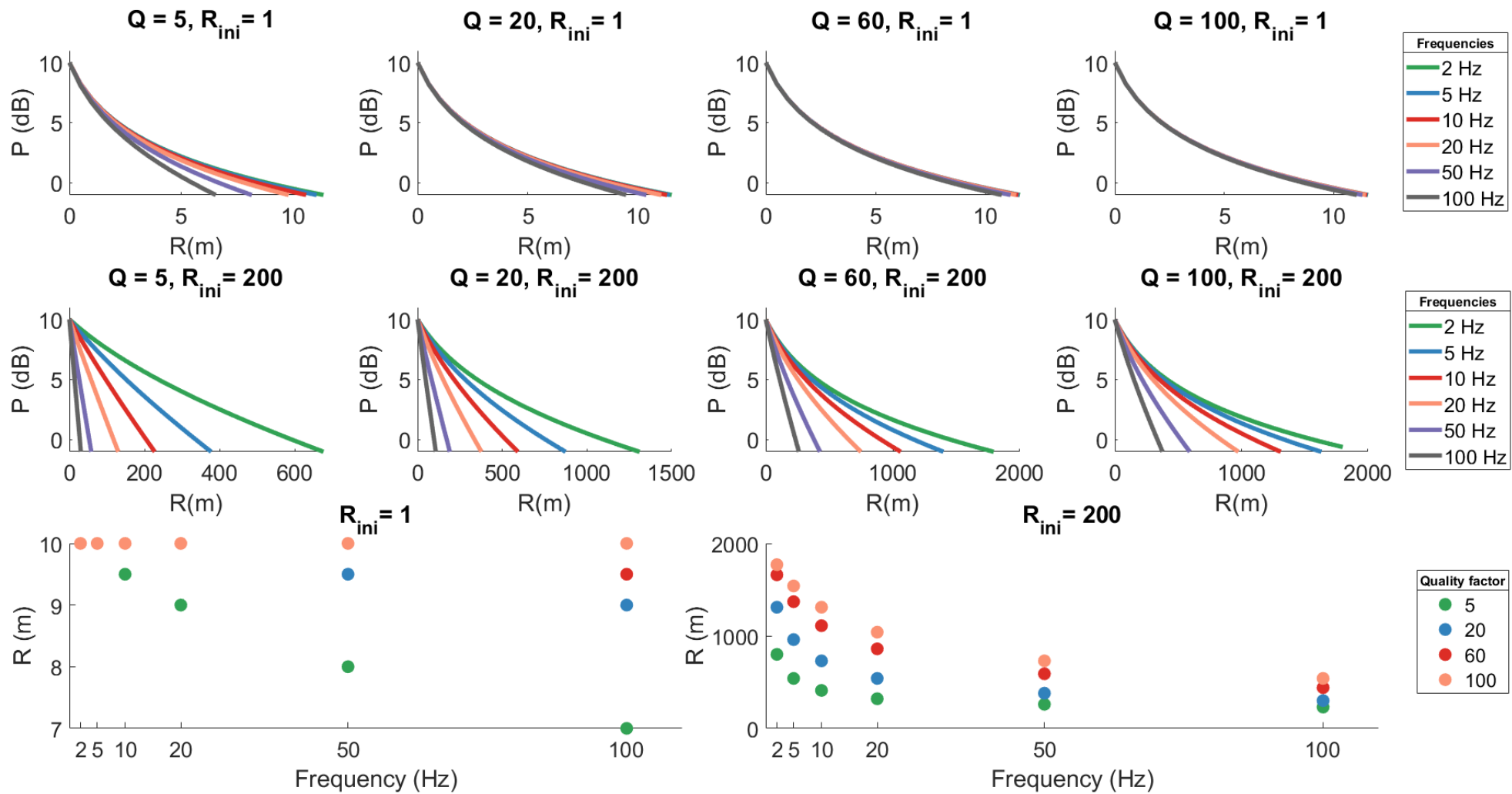




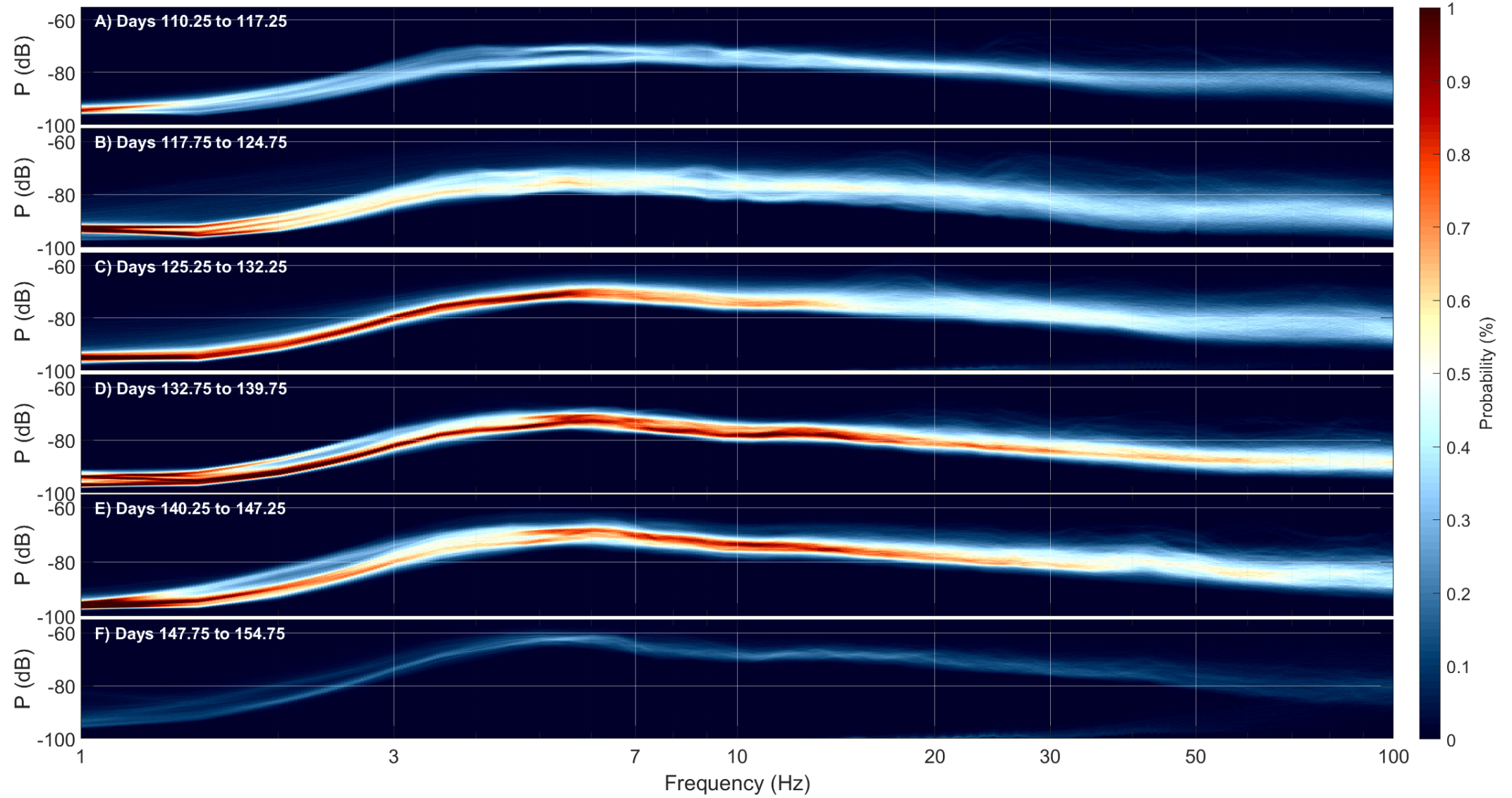




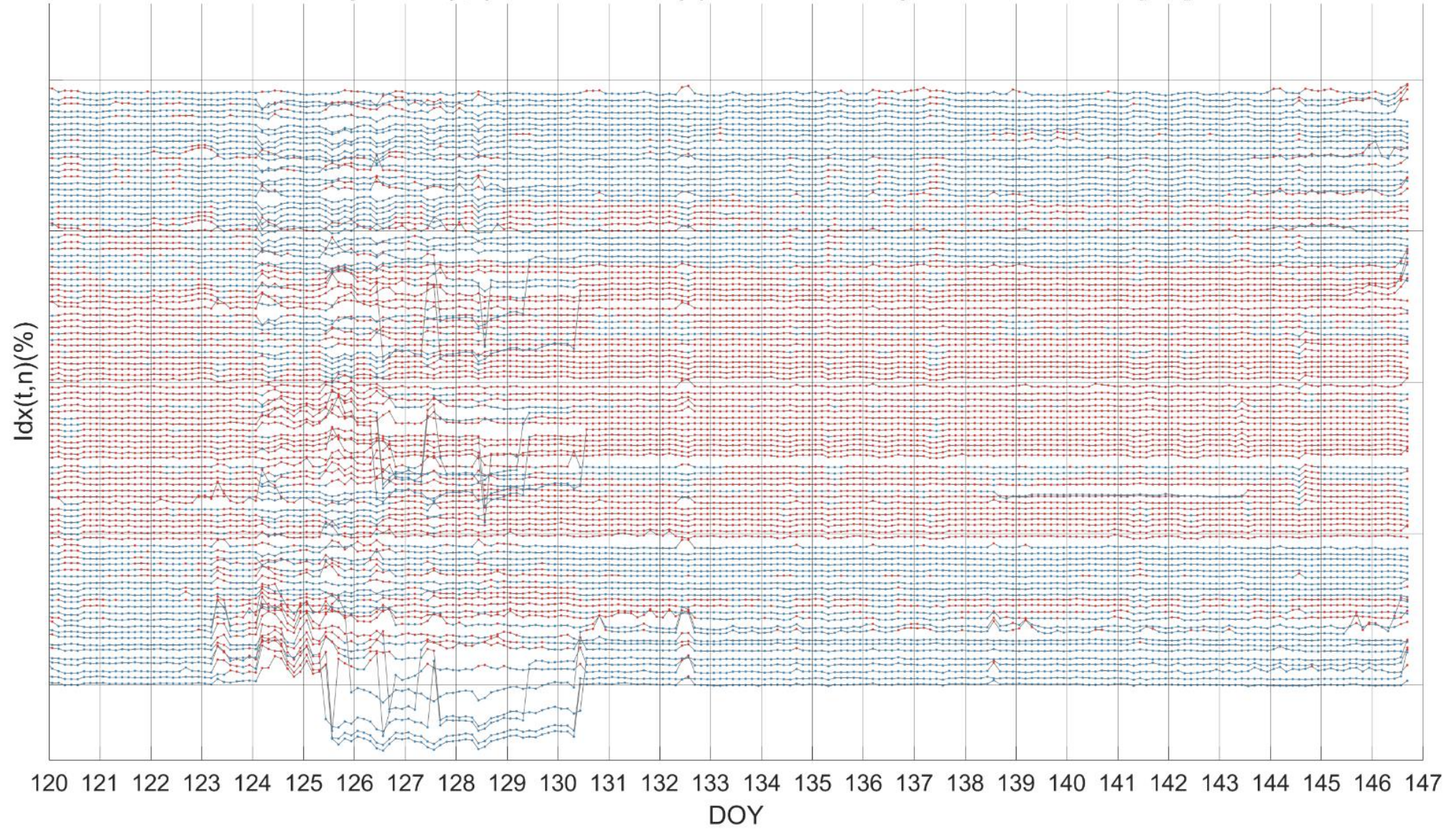




Energy distribution over the 97 NODES for different time periods



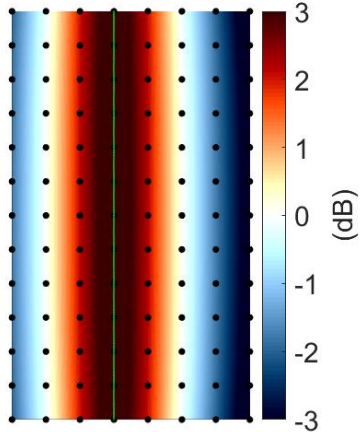
Variability index (t,n) for each node (n) calculated every t =3 hours for f in [3-7] Hz



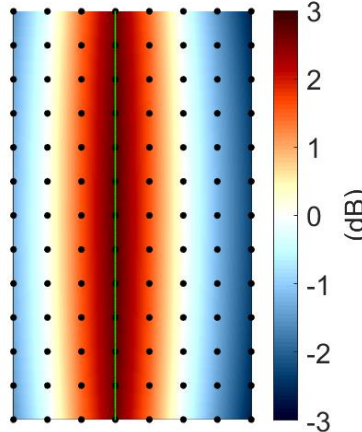


### Synthetic model for surface waves (f=5 Hz)

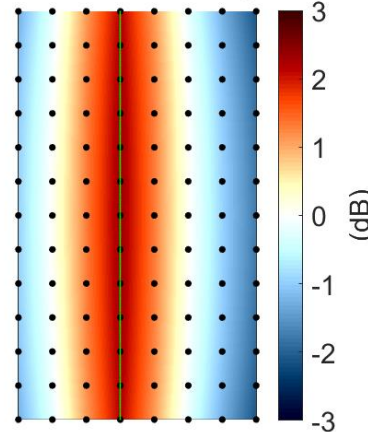
Q = 4 H = 0.1 Bg = 0%



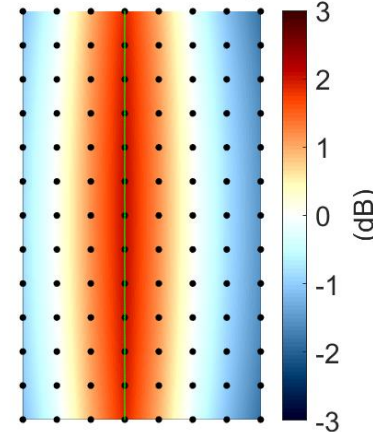
Q = 8 H = 0.1 Bg = 0%



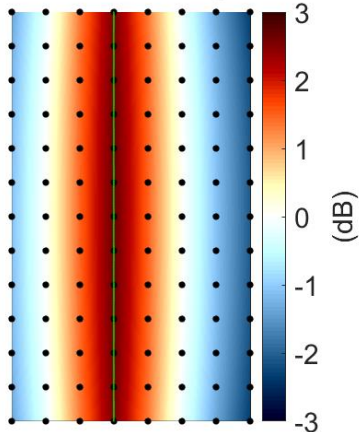
Q = 16 H = 0.1 Bg = 0%



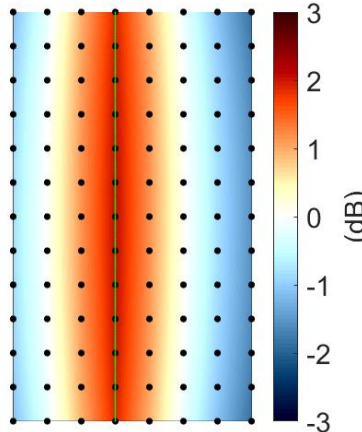
Q = 32 H = 0.1 Bg = 0%



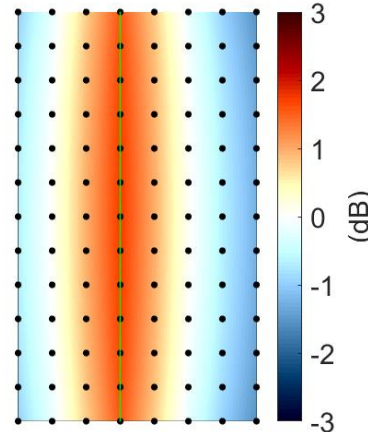
Q = 4 H = 0.1 Bg = 10%



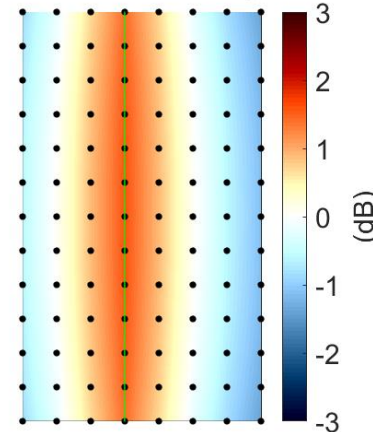
Q = 8 H = 0.1 Bg = 10%

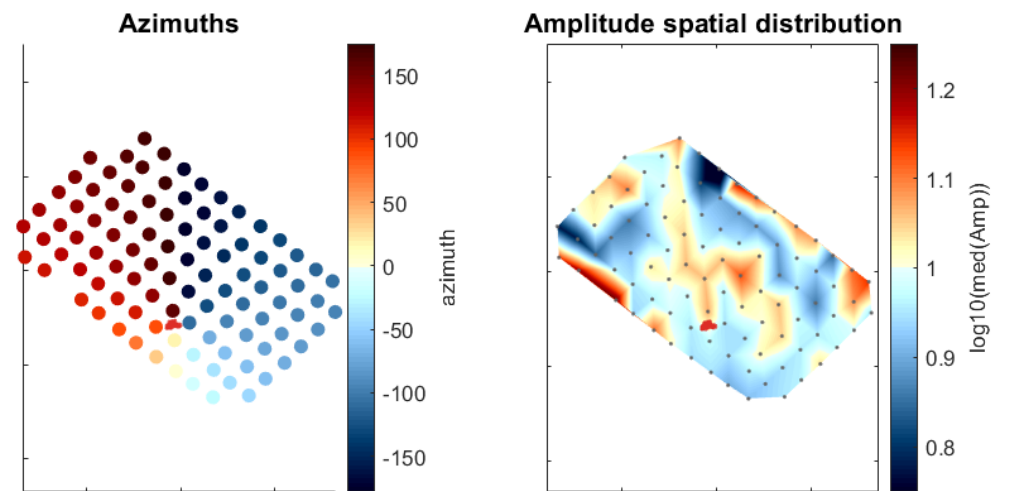
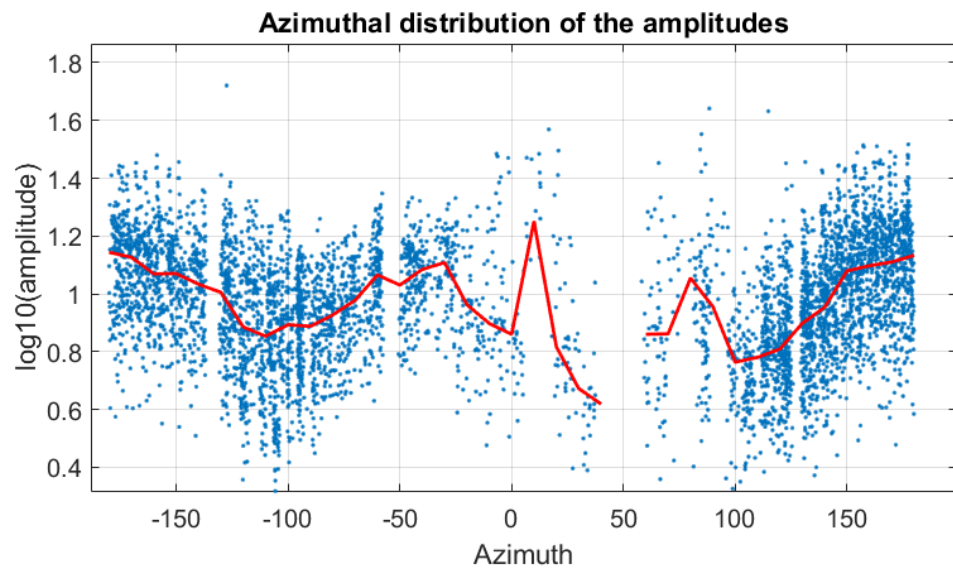
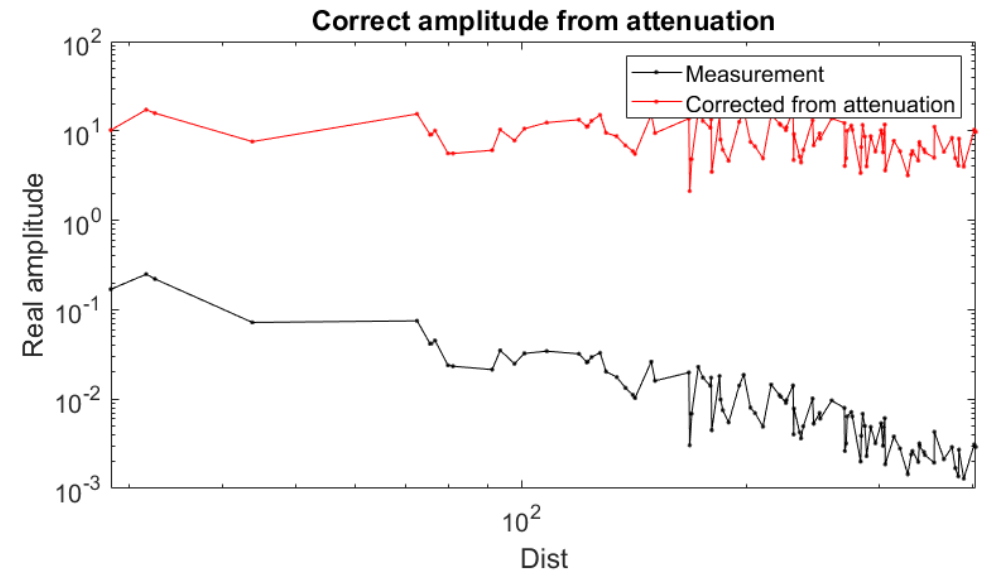
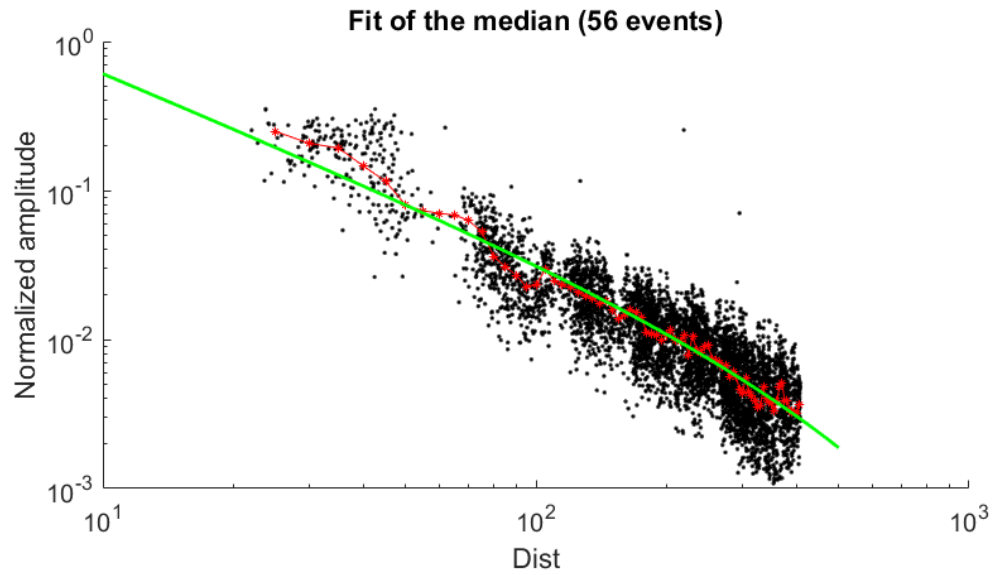


Q = 16 H = 0.1 Bg = 10%

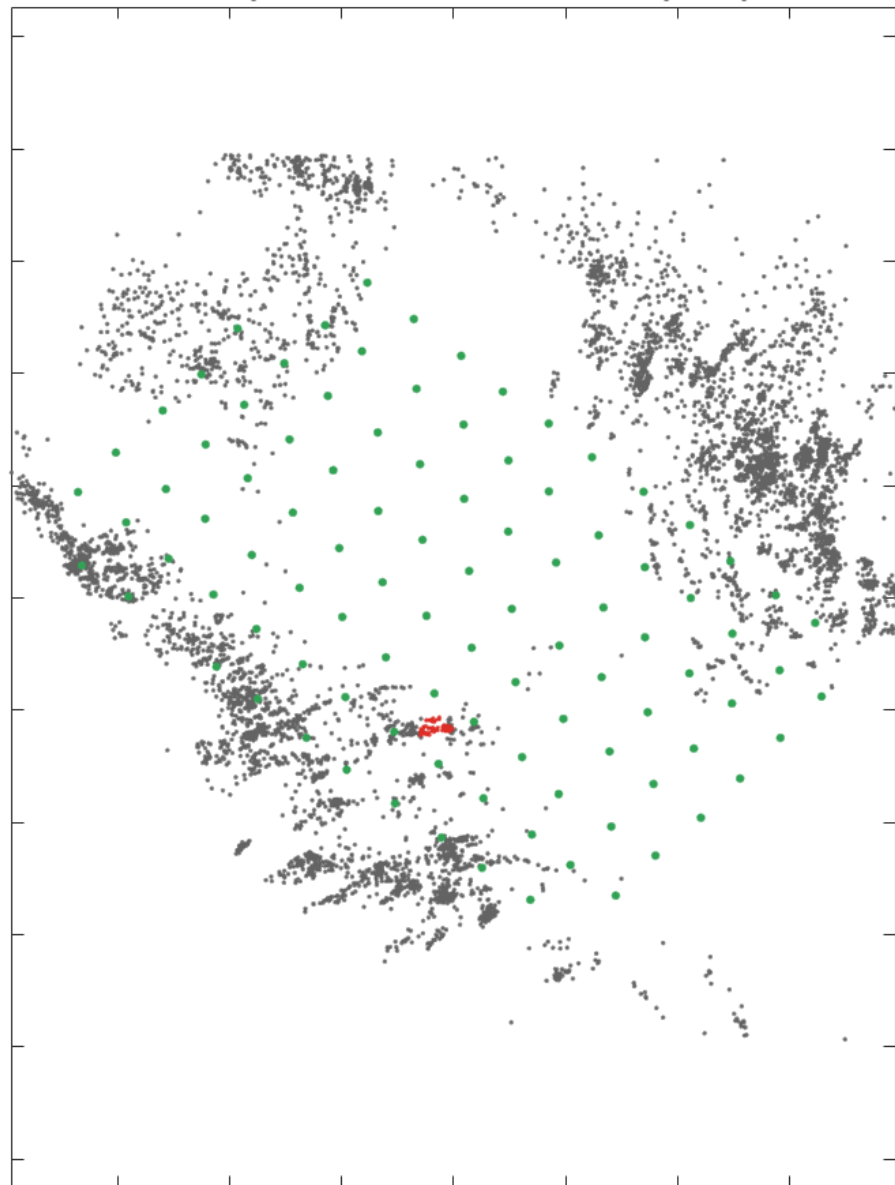


Q = 32 H = 0.1 Bg = 10%

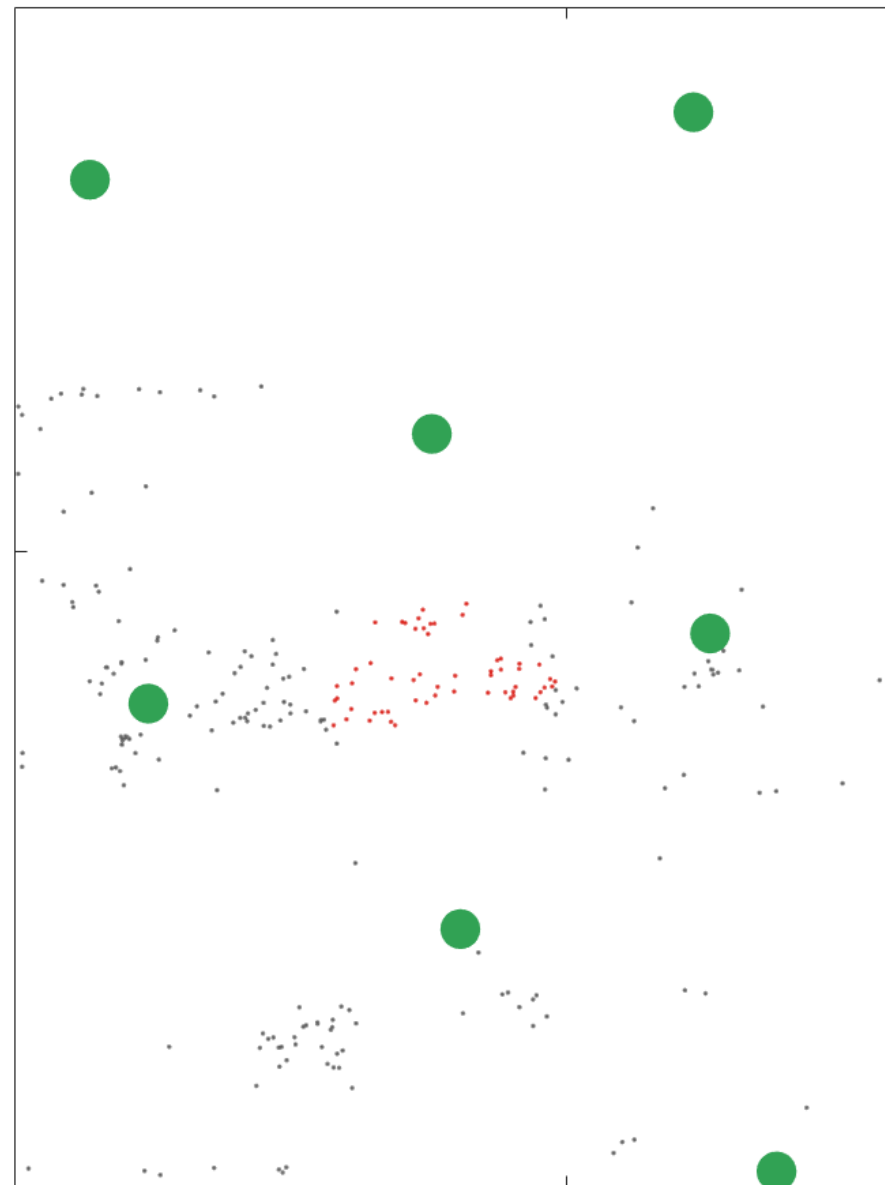




Events with  $p > 0.8$  location over the complete period



Zoom on the studied crevasse



Day 140

