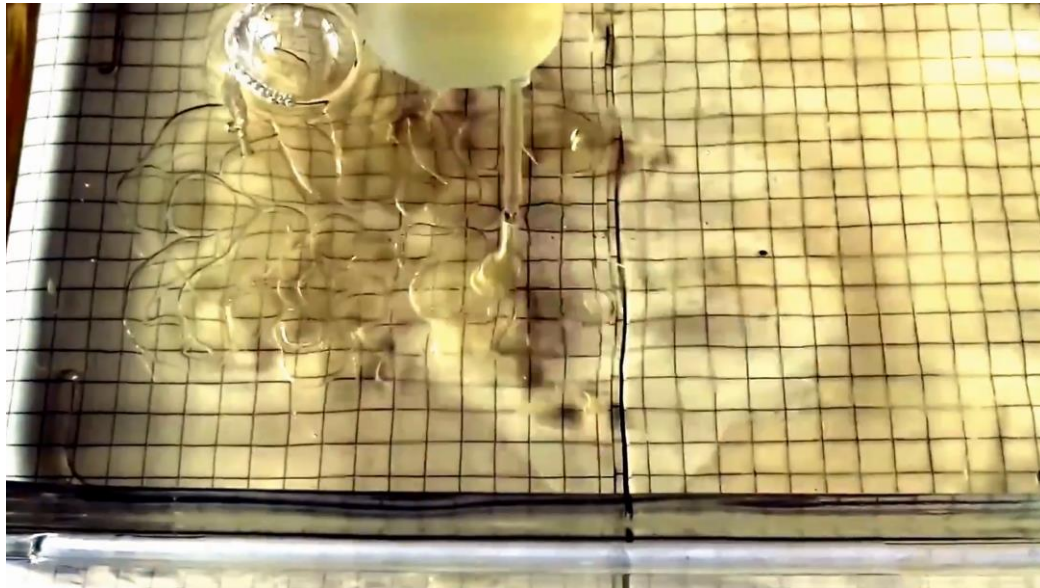


PROBLEM N°13

EGG WHITE PEARLS

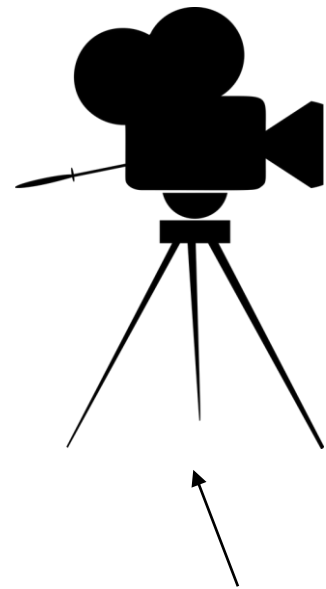
Team Ecole polytechnique

Egg white Pearls

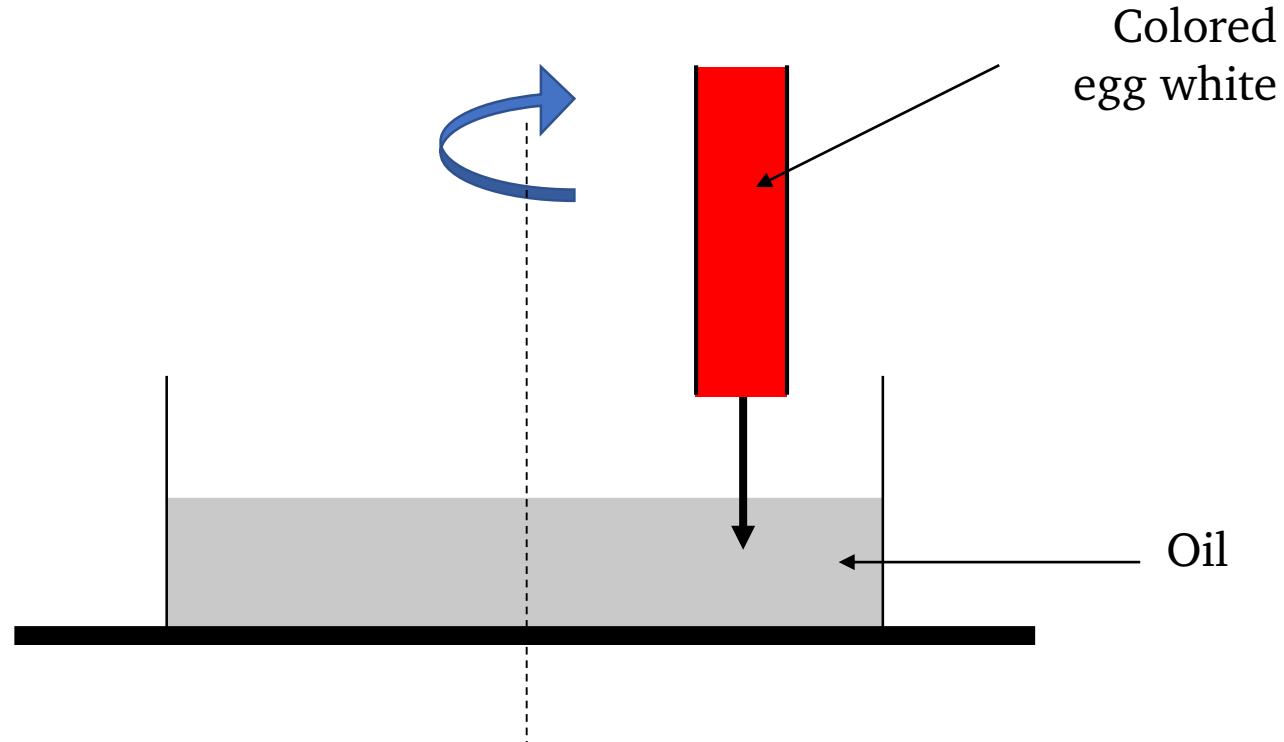


Egg whites are separated from the yolk and put into a syringe. From the syringe, the egg white is ejected into heated oil while the tip is in motion (video on IPT website). How does **the size** of the egg white pearls produced depend on the various parameters such as the **temperature of the oil, ejection and motion speed, nozzle diameter** or the non-Newtonian properties of egg whites?

Experimental setup



High-speed camera
1000fps



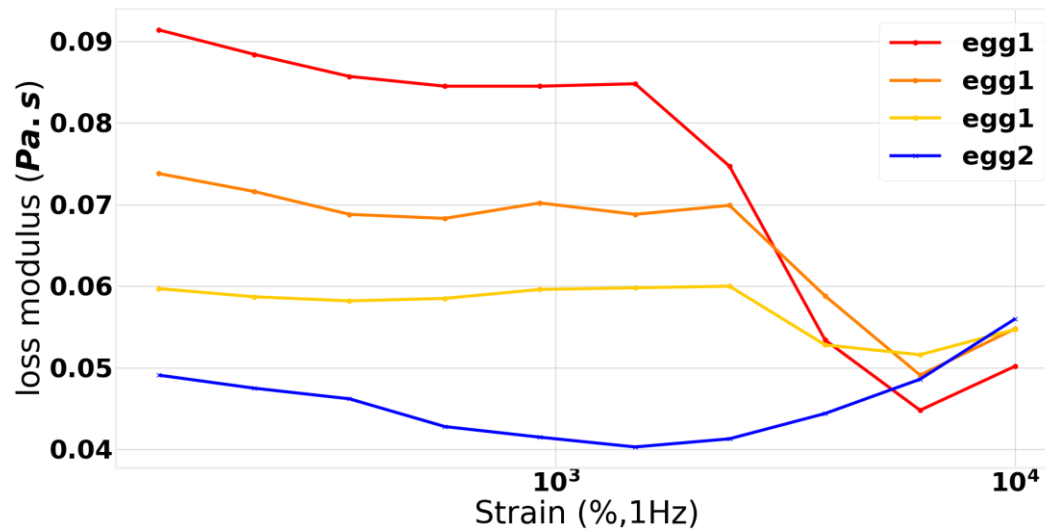
Variability between experiments



Egg white: approx. 90% water, 10% proteins (ovalbumin)

Viscoelastic, shear-thinning fluid

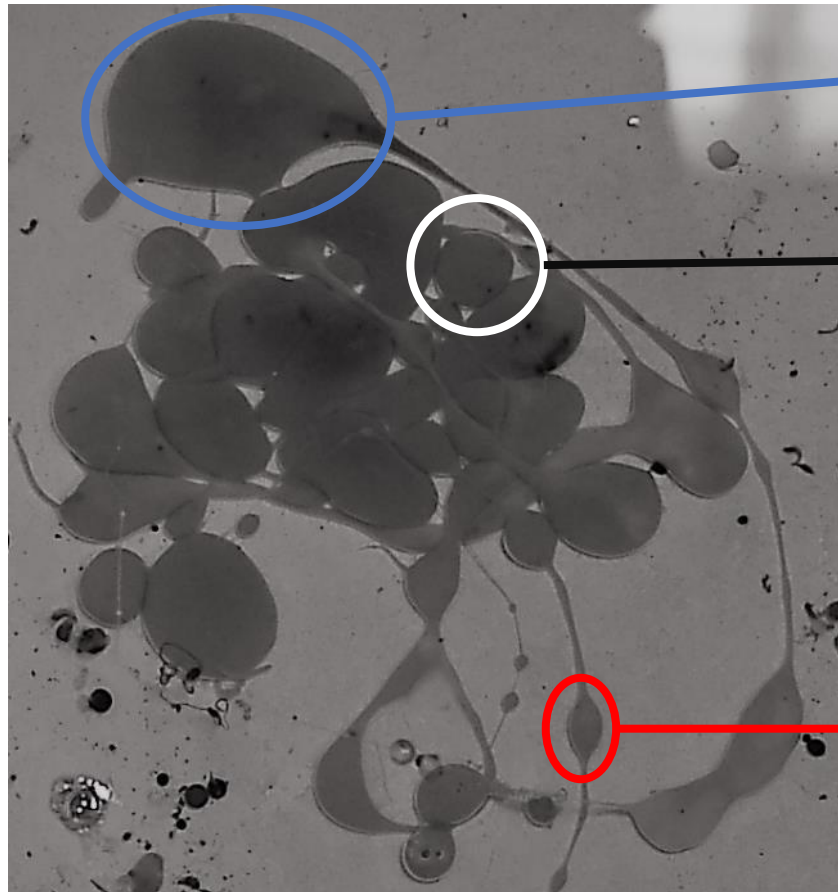
Inhomogeneous repartition of proteins



Variability :

- between successive experiments
- between different eggs

First observations



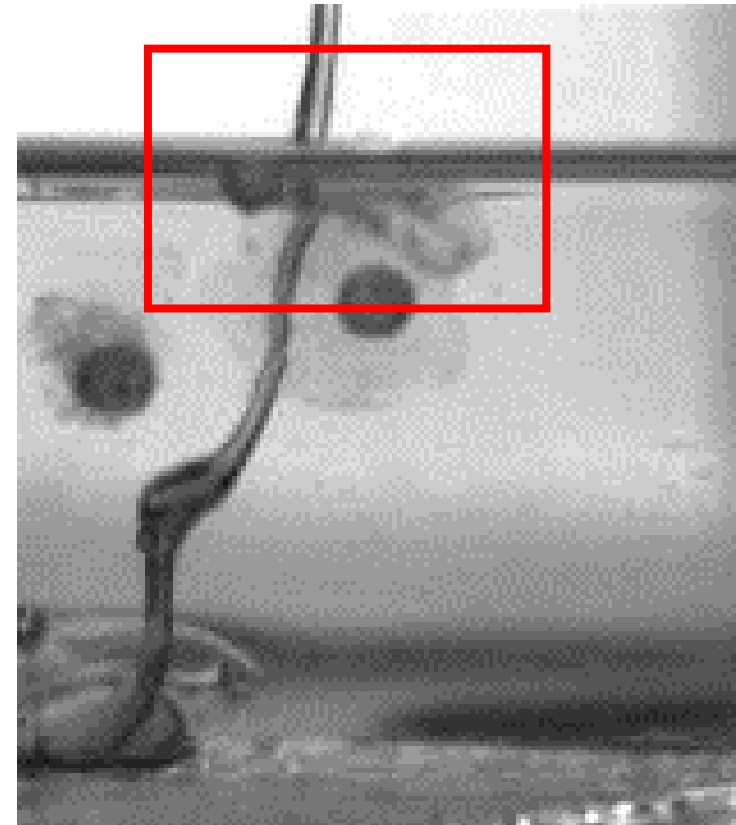
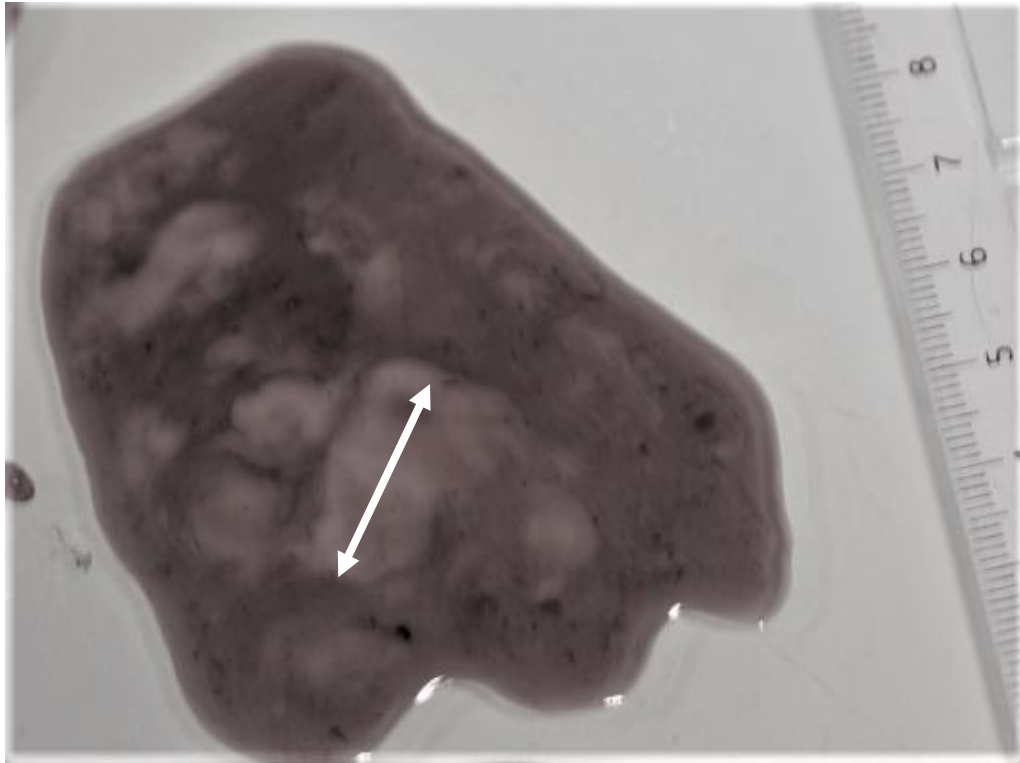
Big pearls: free shape, several cm

Medium pearls: rounded shape, 1-2cm

Small pearls: elongated, <1cm

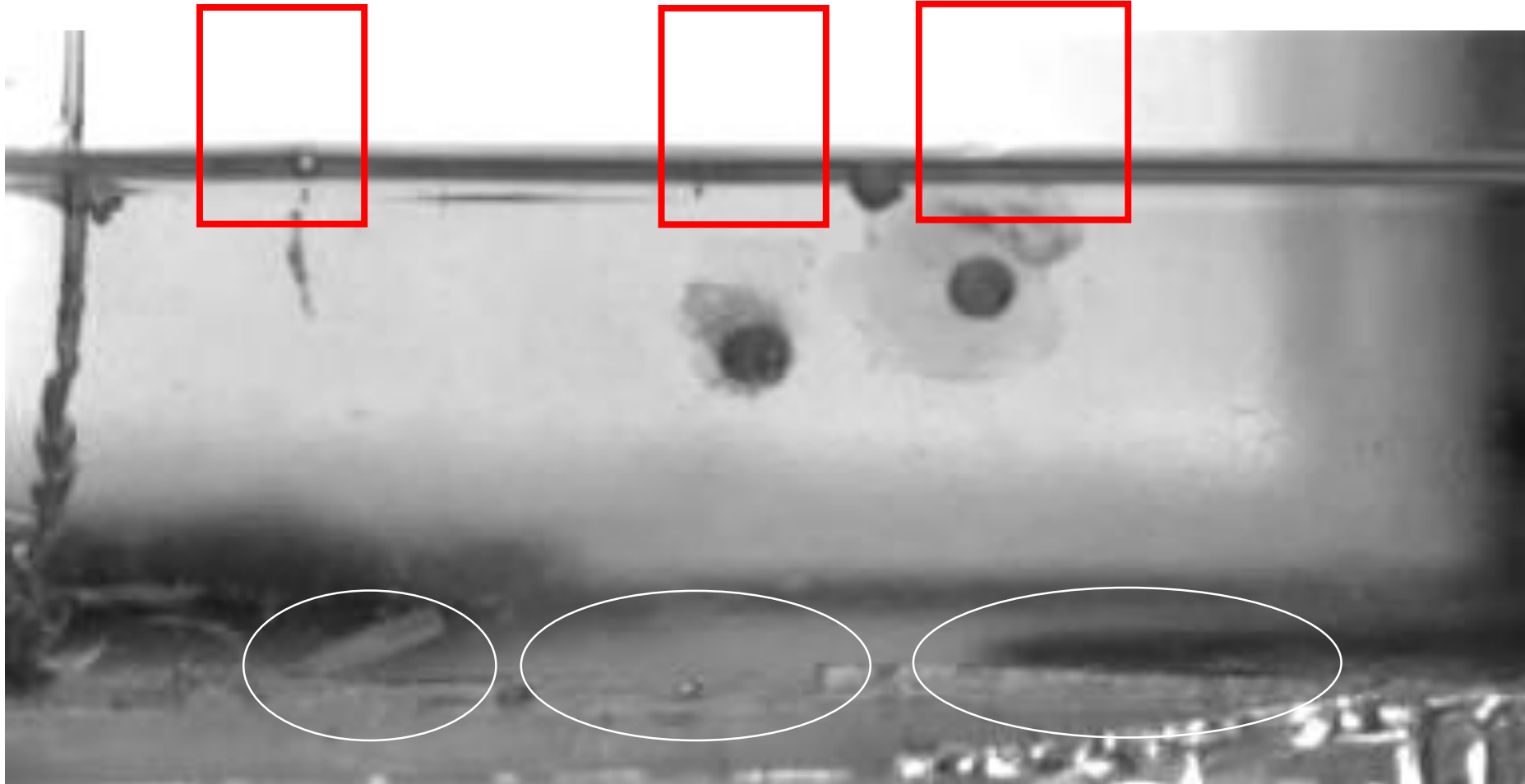
Formation of big pearls

Inhomogeneities

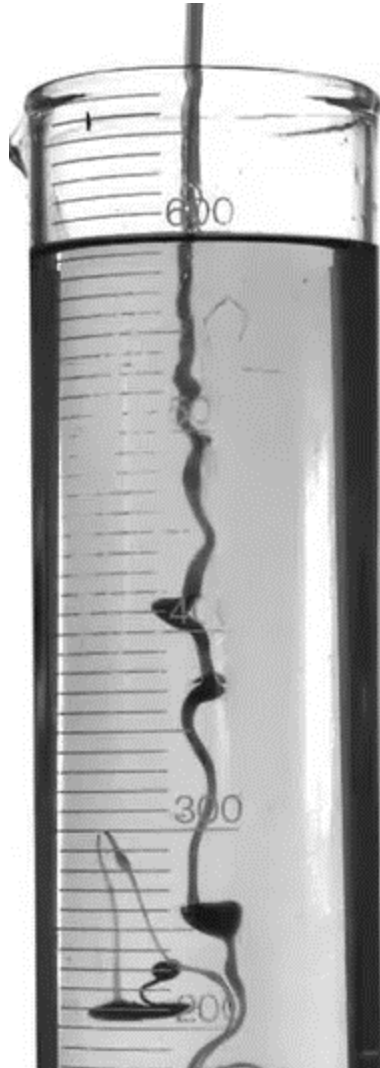


Formation of big pearls

Inhomogeneities



Formation of medium pearls



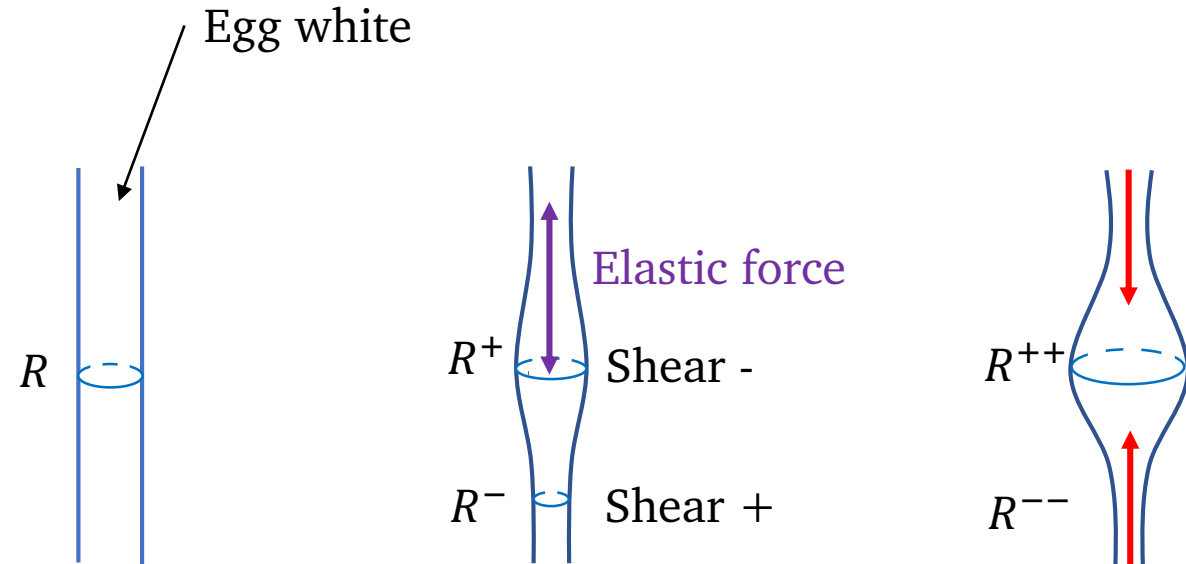
Instability similar to
Kelvin-Helmholtz



Formation of medium pearls



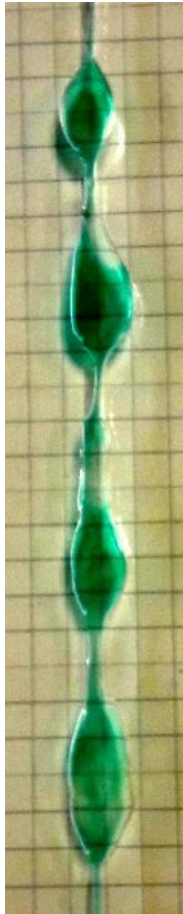
Maizena in oil



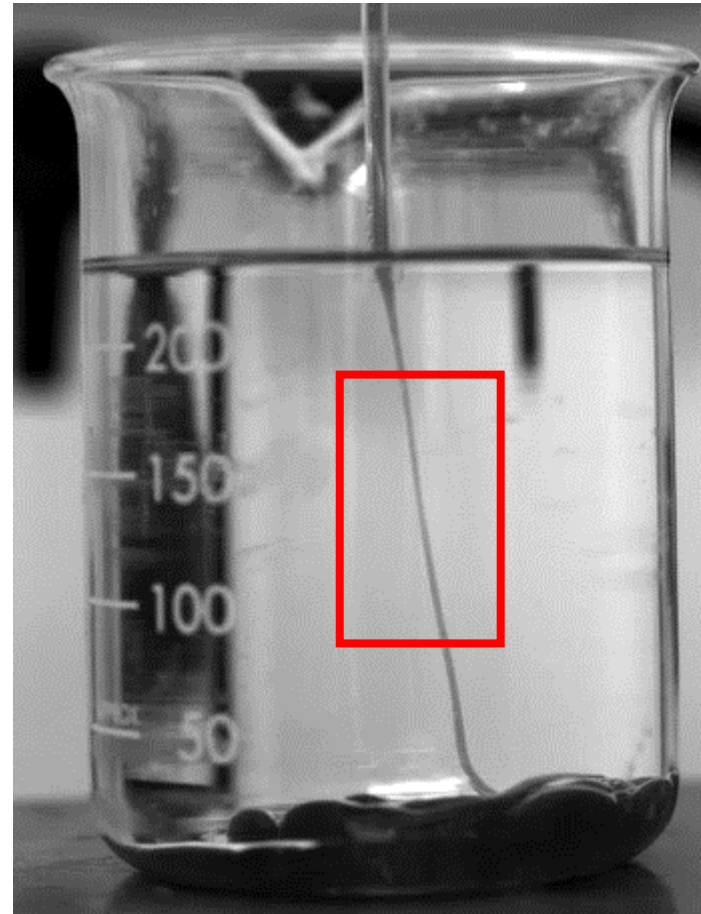
Transition medium to big pearls



Formation of small pearls

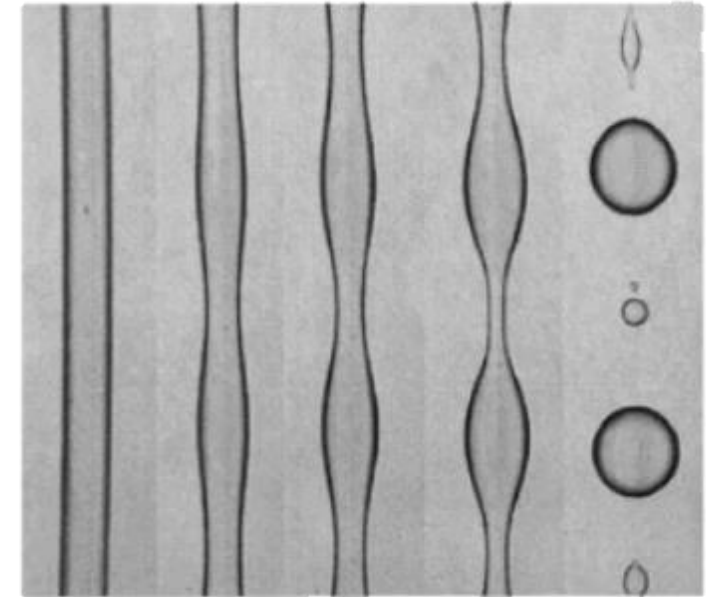


Small pearls



Formation

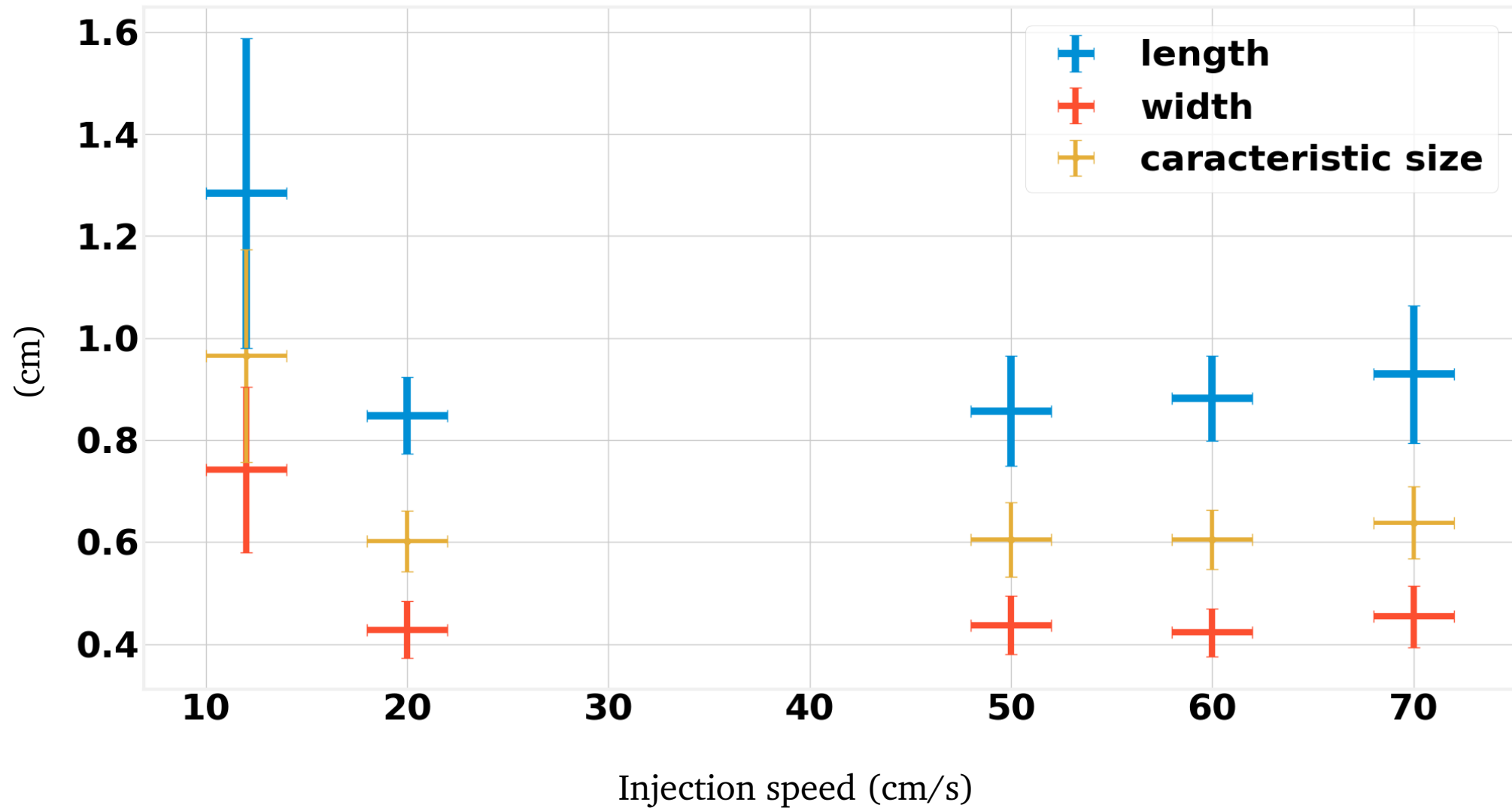
Rayleigh-Plateau instability



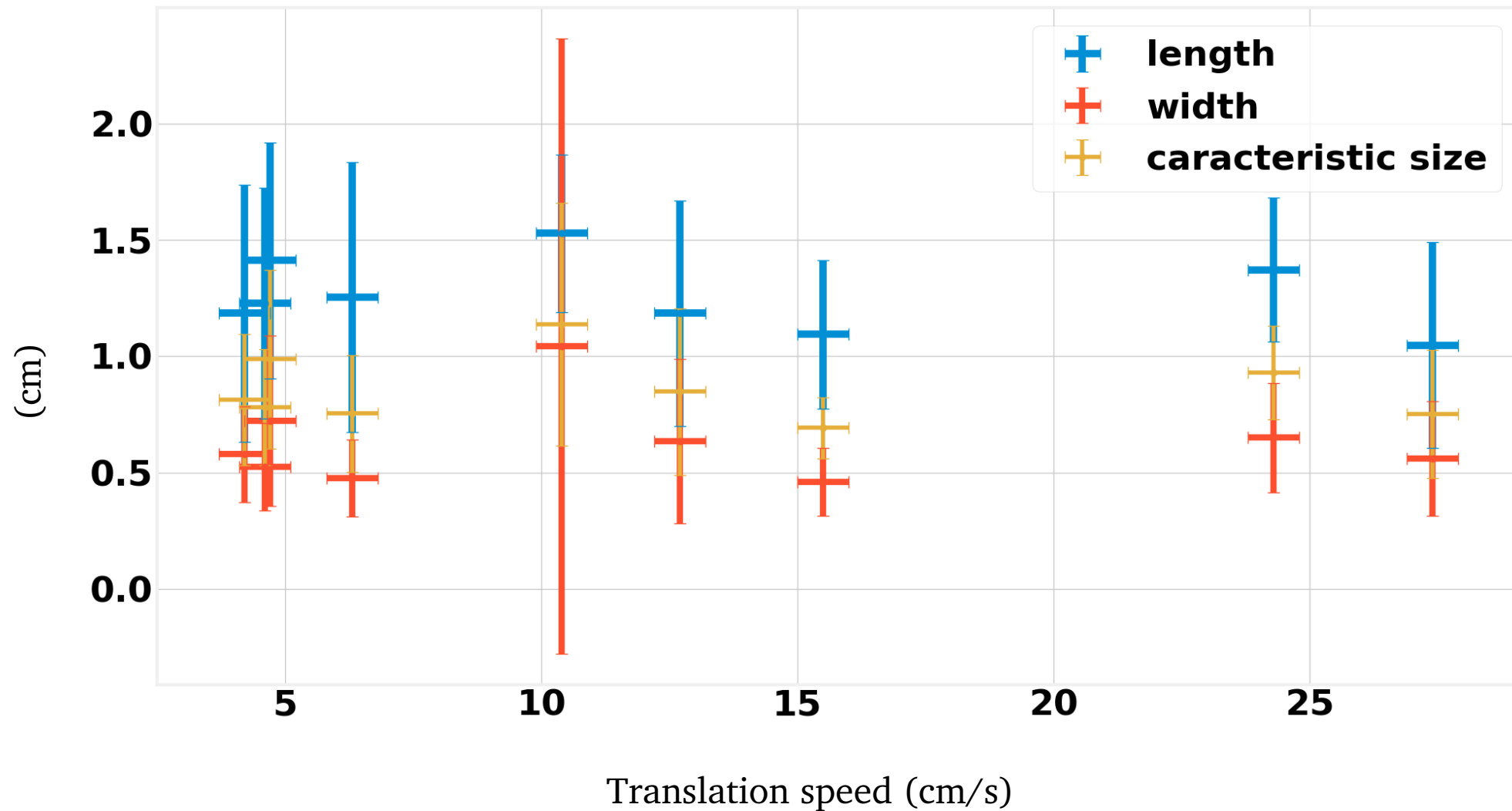
Elastic behavior \leftrightarrow surface tension

Z. Liu - Instability of a viscoelastic liquid jet with axisymmetric and asymmetric disturbances, ijmulflow 2008

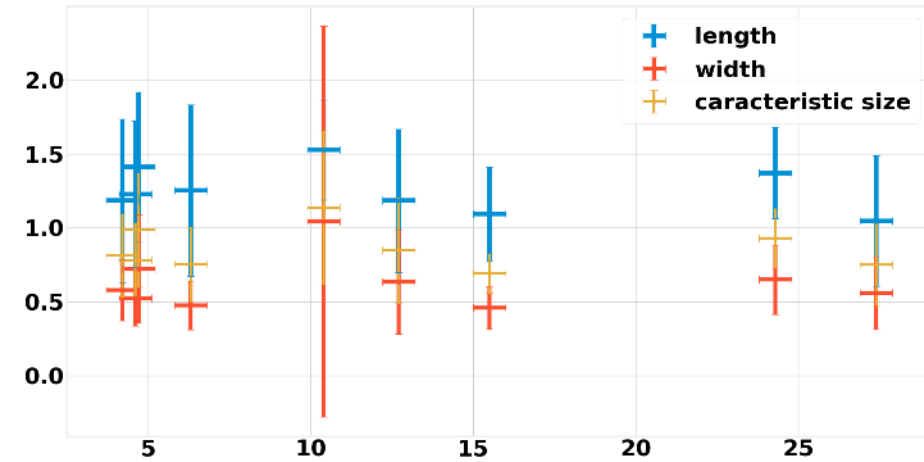
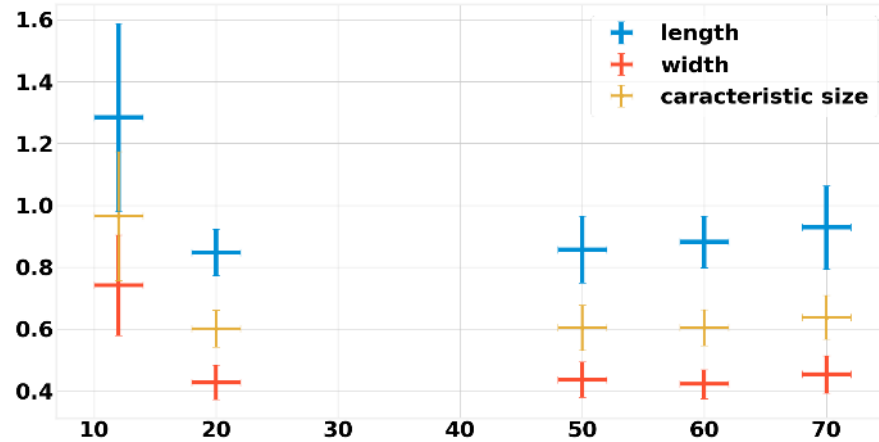
Translation and injection speed



Translation and injection speed



Speed does not influence pearl size

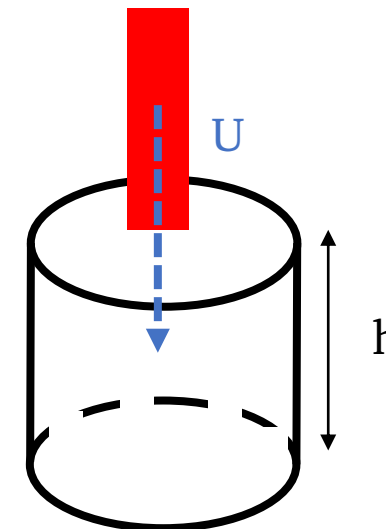


Kelvin-Helmholtz dispersion relation for speed: $\omega \propto kU$

Time spend falling: $t = h/U$

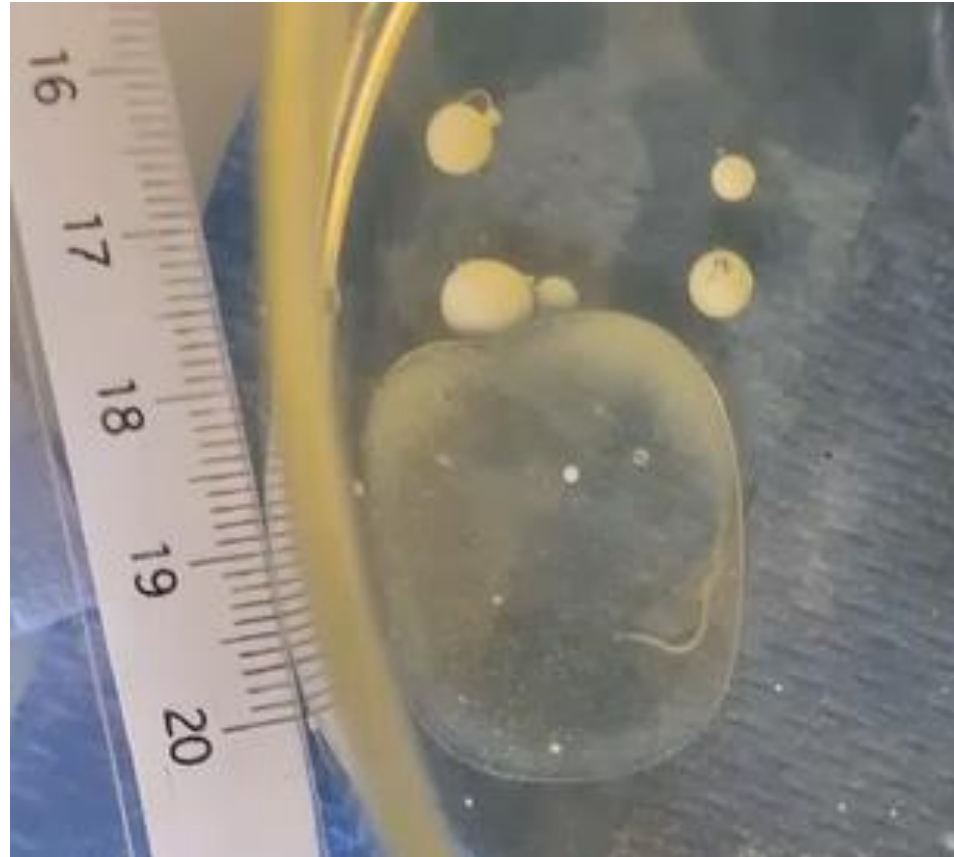
Growth of instability: $\omega t \propto kh$ no speed dependence !

True for injection speed \gg translation speed

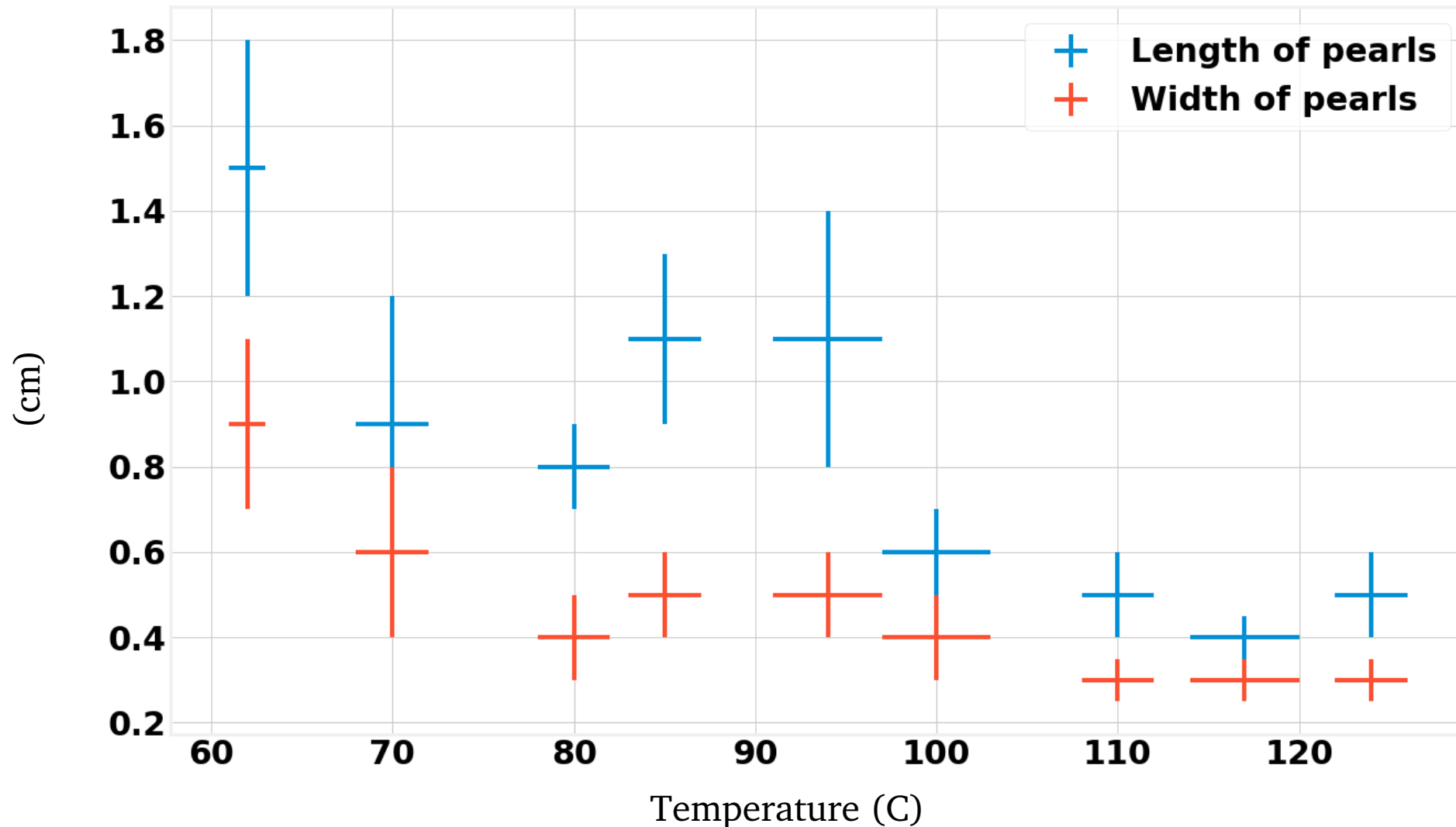


Influence of oil temperature

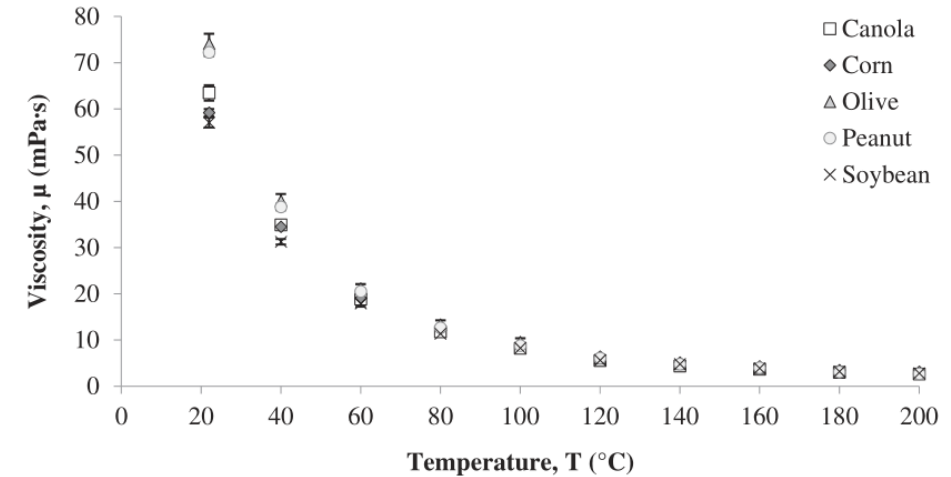
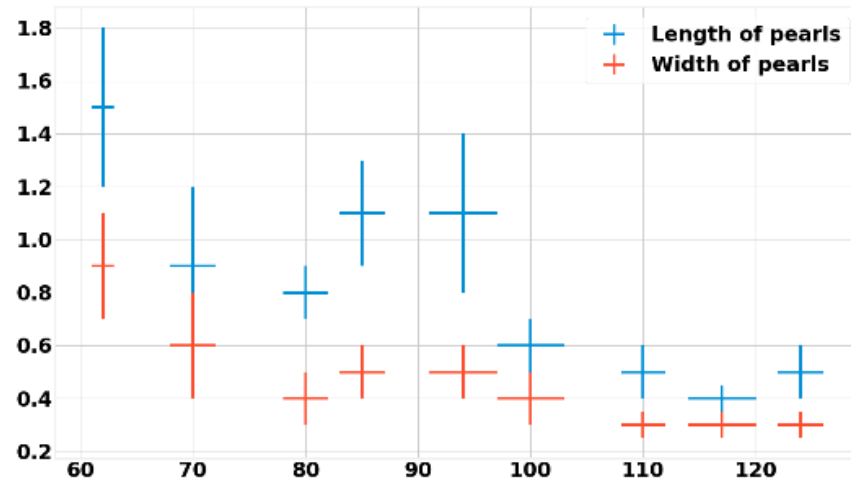
Dilatation is negligible



Influence of oil temperature



Influence of oil temperature



Temperature increases \Rightarrow viscosity decreases

Viscous K-Helmholtz dispersion relation: $\omega \approx k^2 \mu - f(k)$

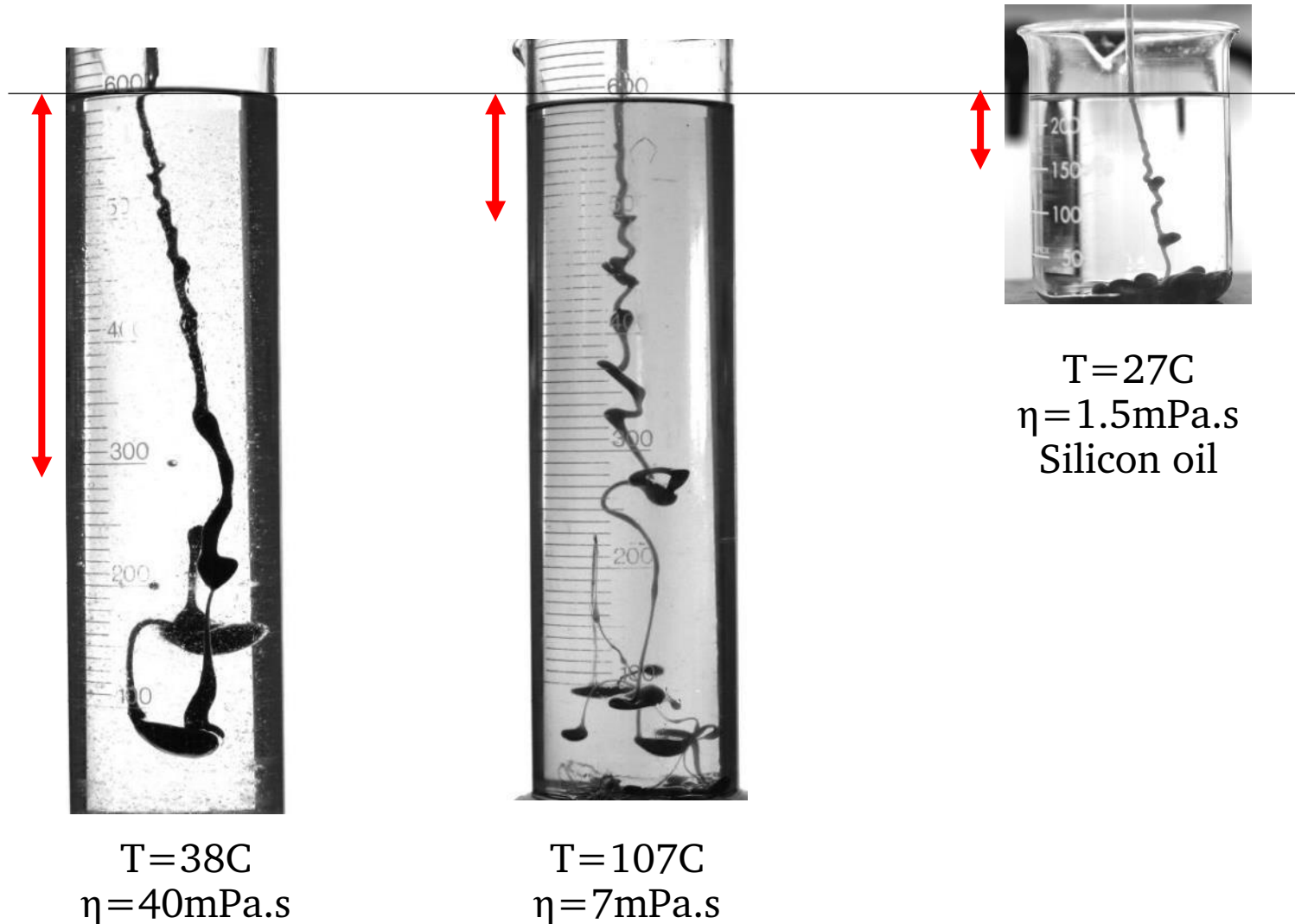
Fastest growing wavenumber: $k = \frac{-f'}{2\mu}$

Wavelength $2\pi/k$ decreases with temperature

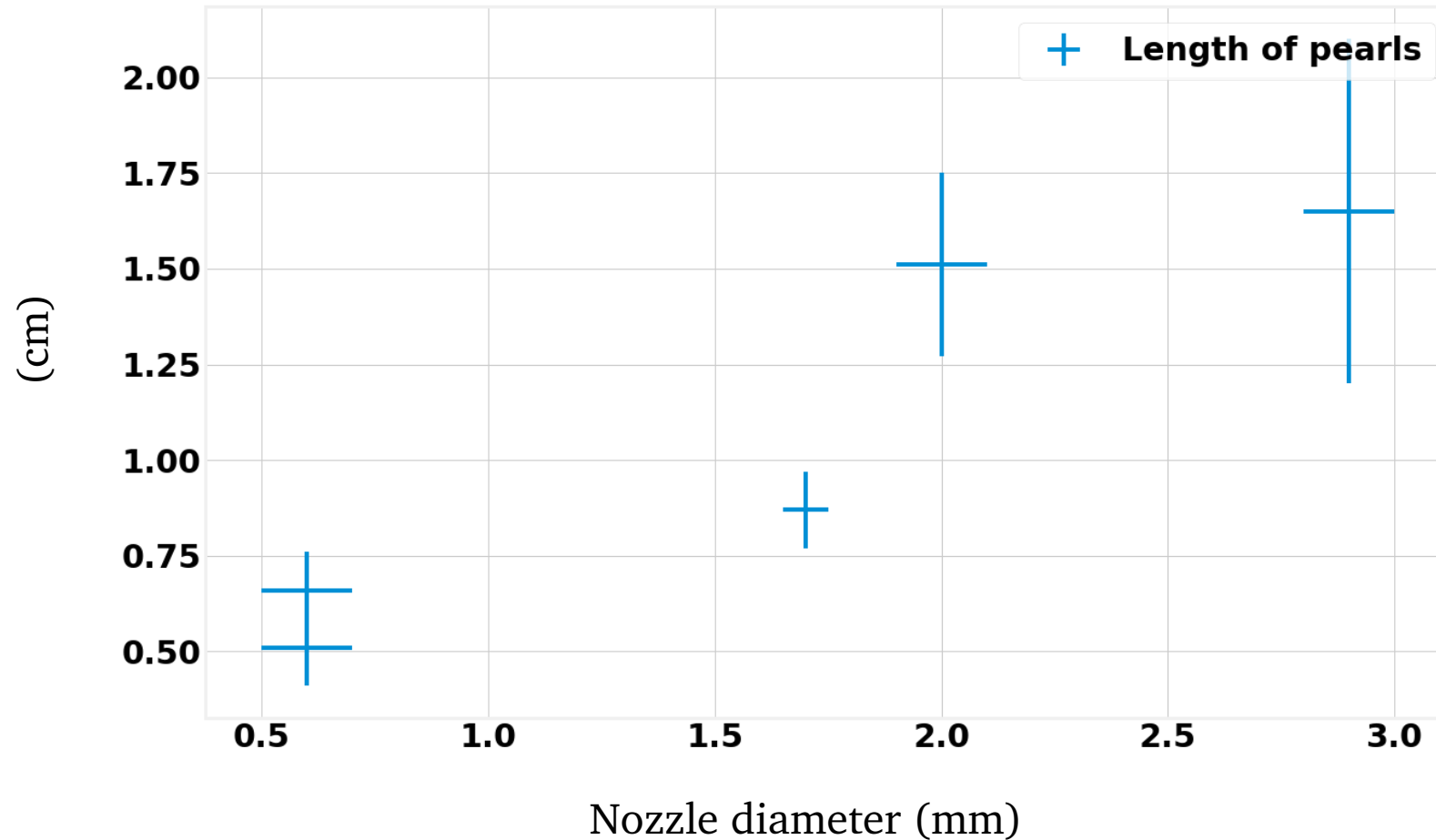
Sahasrabudhe - Density, viscosity, and surface tension of five vegetable oils at elevated temperatures: Measurement and modeling, IJFP 2017

Funada - Viscous potential flow analysis of Kelvin-Helmholtz instability in a channel, JFM 2001

Influence of oil temperature

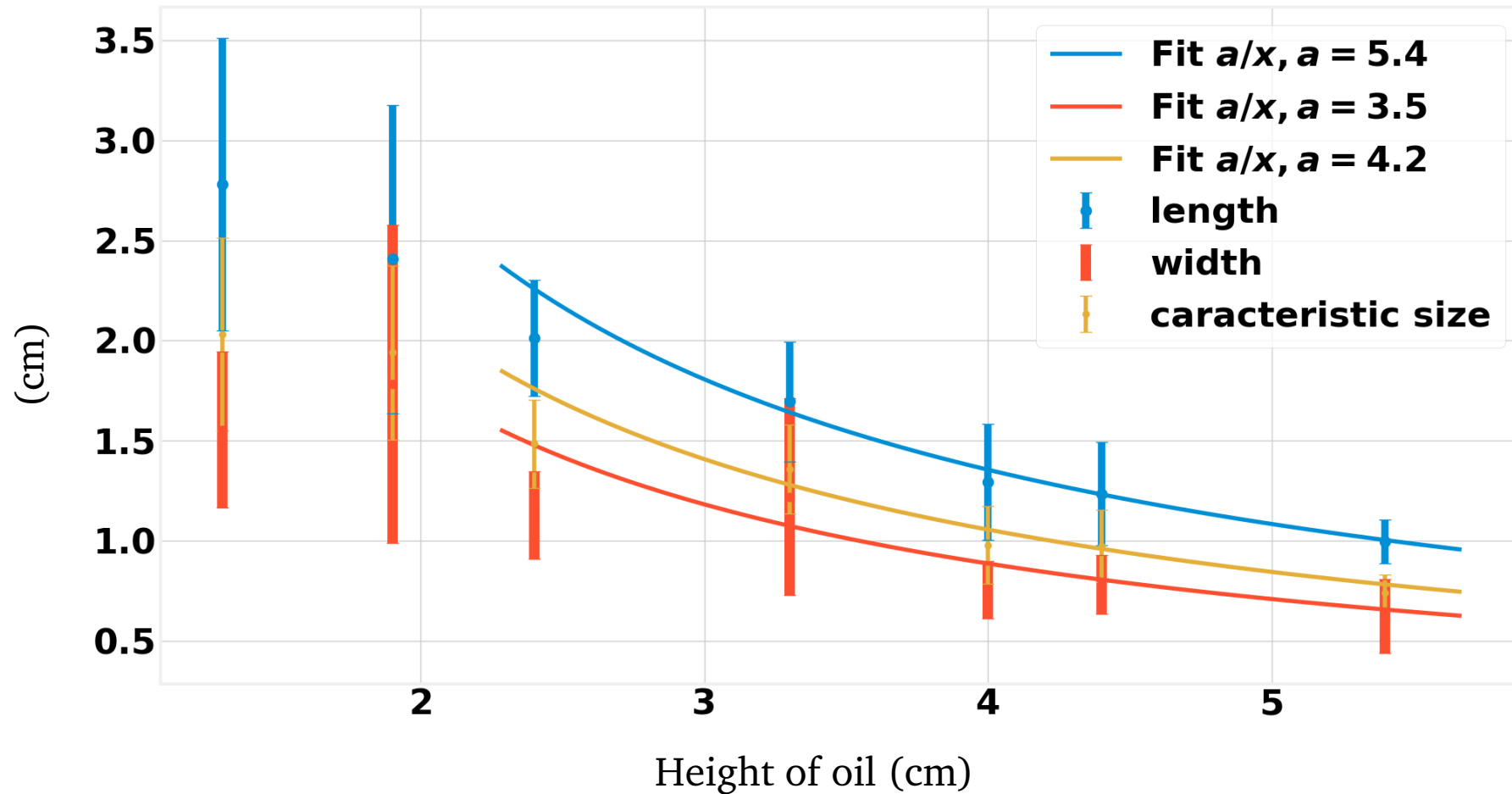


Influence of nozzle diameter

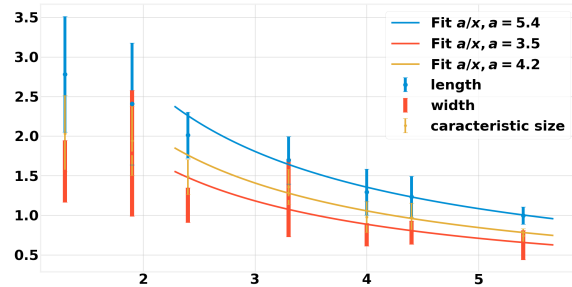


Diameter increase \Rightarrow Shear reduction
 \Rightarrow slower instability \Rightarrow less small pearls

Height of oil



Height of oil

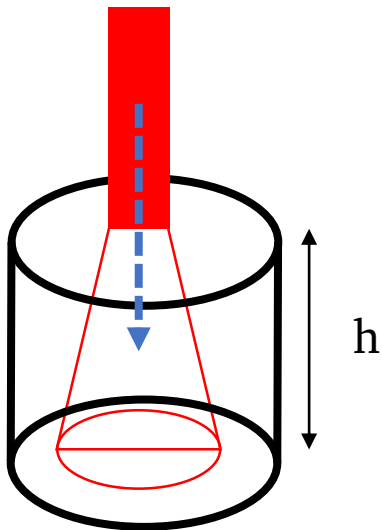


Low heights: instability creates droplets
decrease of big pearls

Higher heights (>3cm): instability has stabilized
more dispersion of pearls
less merging

Hypothesis:

- Fixed pearl size before merging
- Uniform diffusion of pearls in a cone
- Fixed height of pearls

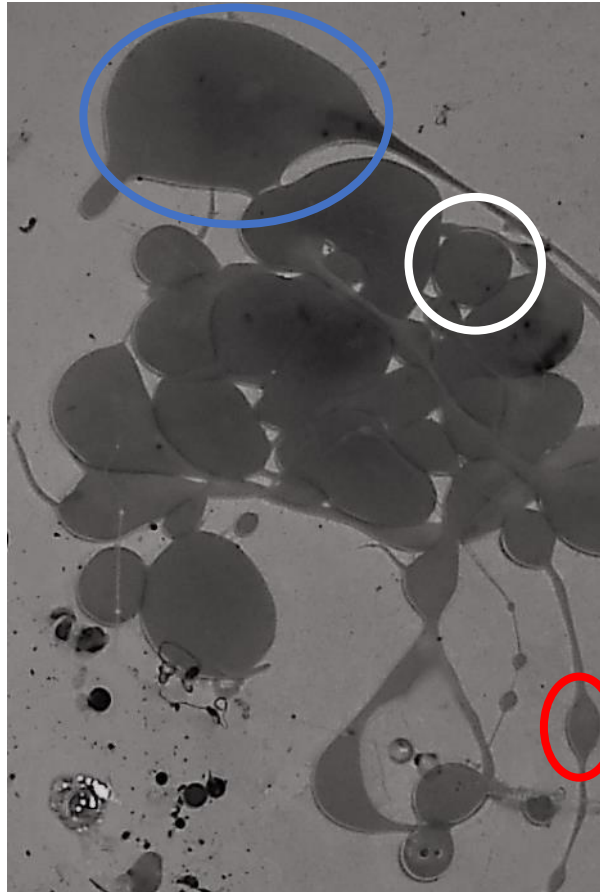


$$\frac{\text{number of pearls before merging}}{\text{number of pearls after merging}} \approx \frac{\sum \text{area of one pearl}}{\text{bottom area}}$$

$$L \propto \frac{1}{h}$$

Conclusion

Three kinds of pearls:



Big pearls ▶ accumulation and **inhomogeneities**

Medium pearls ▶ Kelvin-Helmholtz **instability** driven by **shear-thinning behavior**

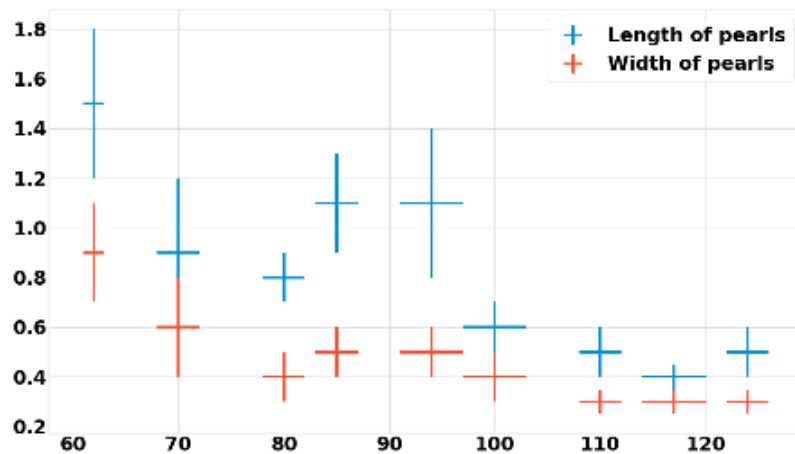
Small pearls ▶ Rayleigh-Plateau **instability** driven by **viscoelastic behavior**

Conclusion

How does the size of the egg white pearls produced depend on the various parameters such as the temperature of the oil, ejection and motion speed, nozzle diameter or the non-Newtonian properties of egg whites?

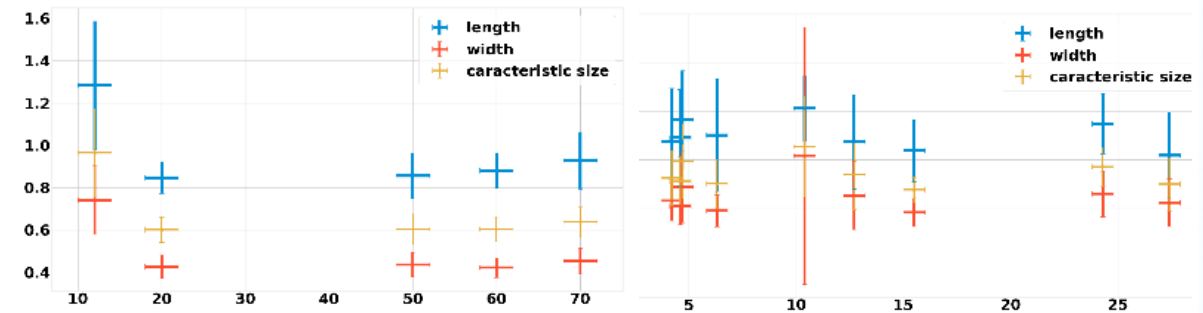
Influence on the size of pearls :

Decreases with temperature of the oil ▶ Viscosity decreases

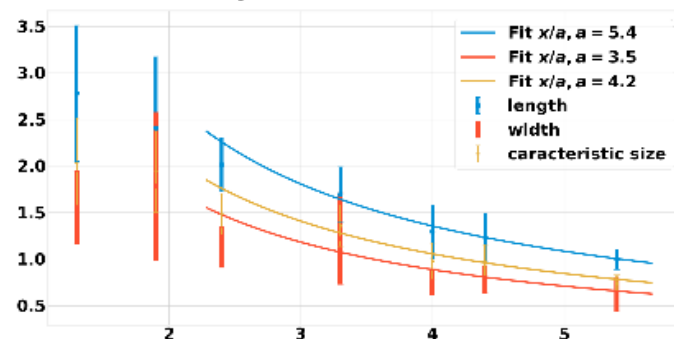


Constant with speed (translation/injection)

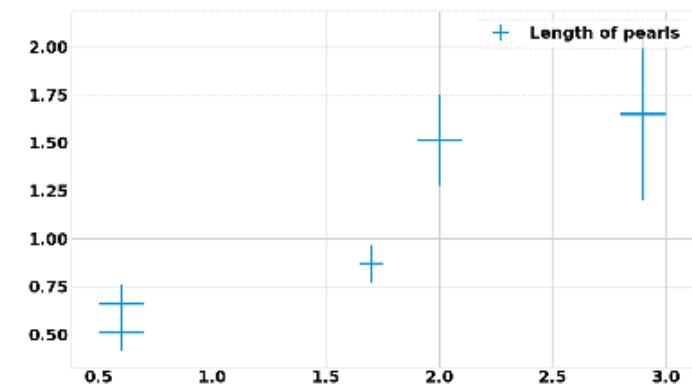
$$\omega t = kh$$



Decreases with oil height ▶ merging of pearls $L \propto \frac{1}{h}$



Decreases with diameter ▶ Slower instability



PROBLEM N°13

EGG WHITE PEARLS

ADDITIONAL SLIDES

Team Ecole polytechnique