

PROBLEM N°7

Static speaker

Team Ecole polytechnique

IPT problem n°7: Static Speaker

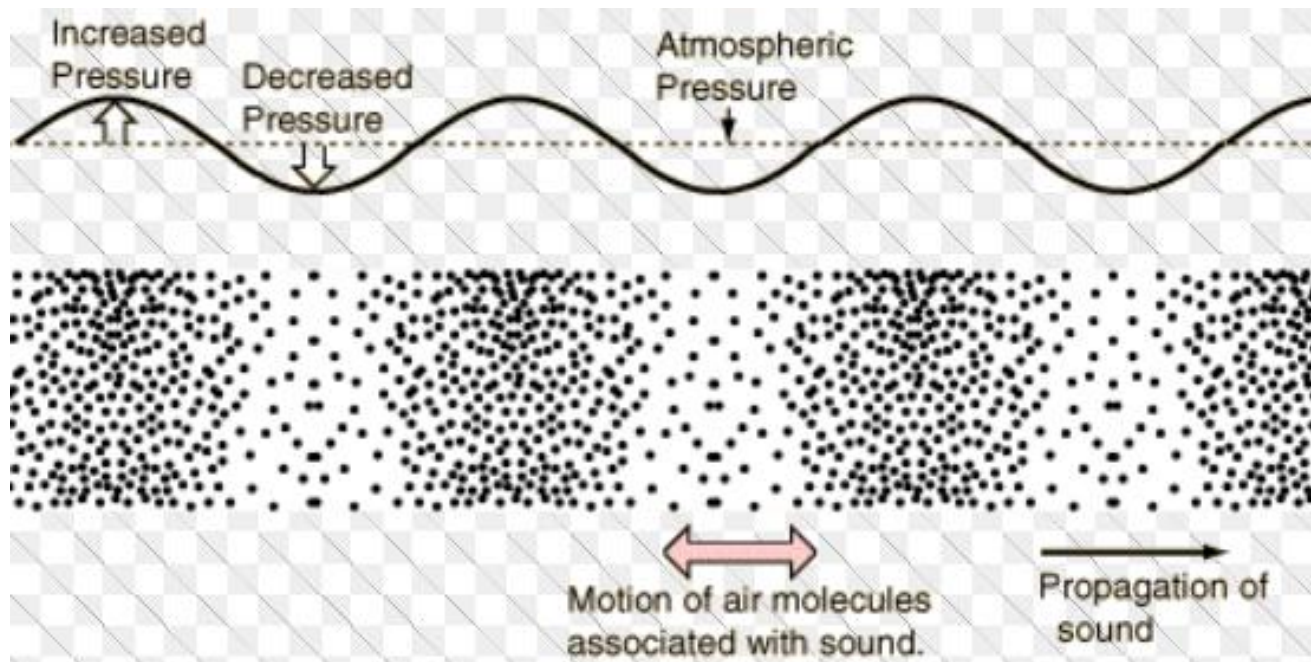
Build an audio speaker without any moving part. Discuss the maximum bandwidth, signal-to-noise ratio and power efficiency achieved with your design. Is it possible to modify your device to use it as a microphone ?

IPT problem n°7: Static Speaker

*Build an audio speaker **without any moving part**. Discuss the maximum bandwidth, signal-to-noise ratio and power efficiency achieved with your design. Is it possible to modify your device to use it as a microphone ?*

What is sound ?

- Trigger a pressure wave : $\frac{1}{c_0^2} \frac{\partial^2 p}{\partial t^2} - \Delta_x p = \text{source term}$ p the pressure, c_0 the velocity of sound in air



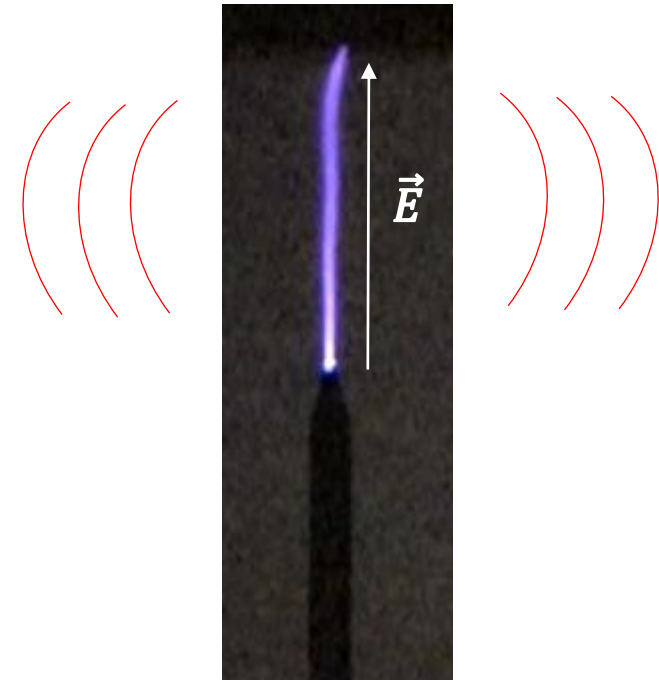
- Air particules must move.
- Objective: no mechanical part moving.

<http://hyperphysics.phy-astr.gsu.edu>

Sound out of heat?

- A way to produce a variation of **pressure** :
dilatation & contraction by quick variation of **temperature** !

- Arc = plasma = very quick heat transfert



- Electrical **modulation** of the discharge : Sound !

Sound emission in plasma

- A pressure wave : $\frac{1}{c_0^2} \frac{\partial^2 p}{\partial t^2} - \Delta_x p = \frac{\gamma-1}{c_0^2} \frac{\partial H}{\partial t} + \vec{\nabla} \cdot \vec{F}$ p the pressure, c_0 the velocity of sound in air, γ the Laplace coefficient of air

- 2 source terms

- Heat transfer (Joule effect)

$$H = C \cdot \vec{j} \cdot \vec{E}$$

$$\langle H \rangle = H_0 \left(1 + \frac{m_E + m_I}{2} + (m_E + m_I) \cos(\omega t) + m_E m_I \cos(2\omega t) \right)$$

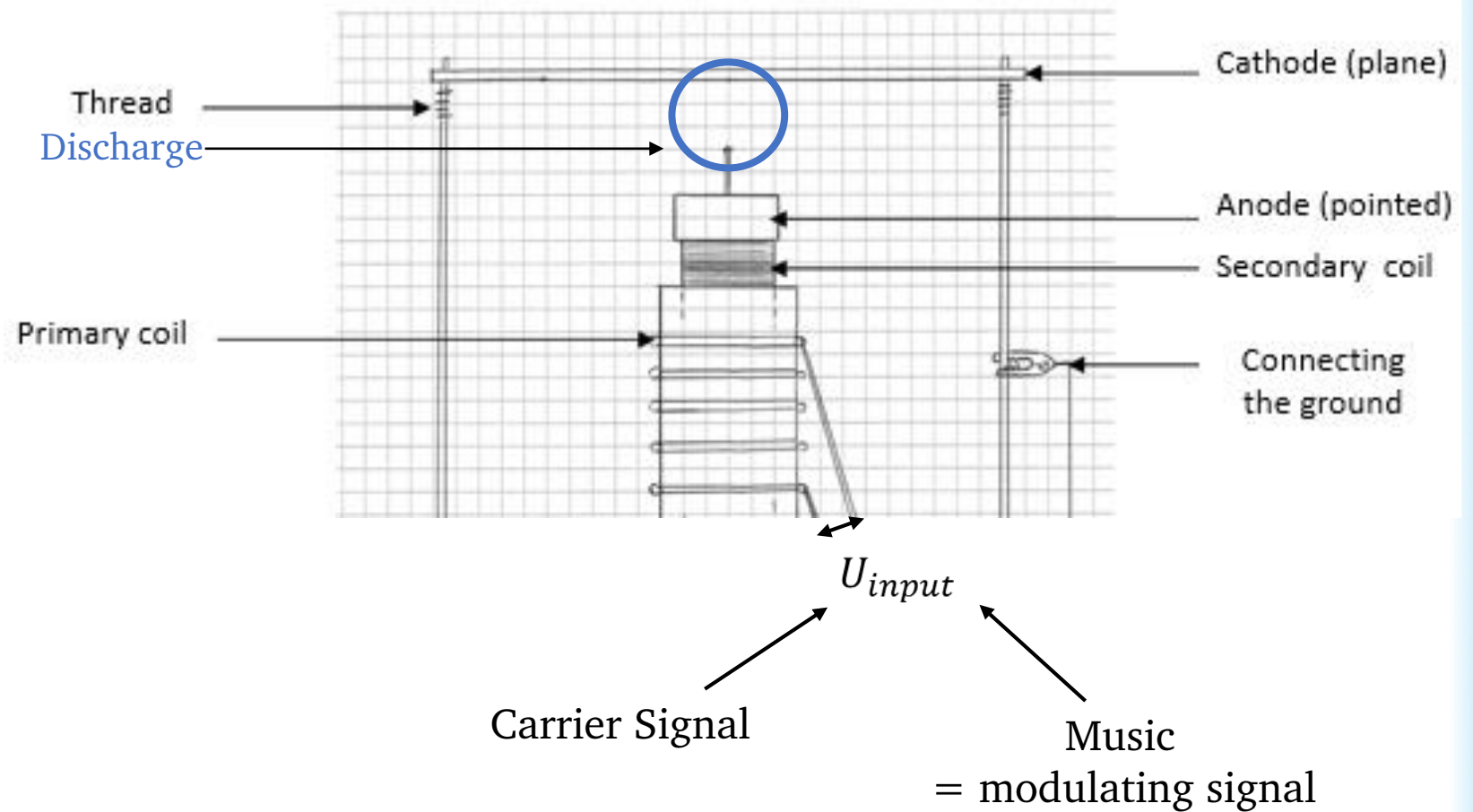
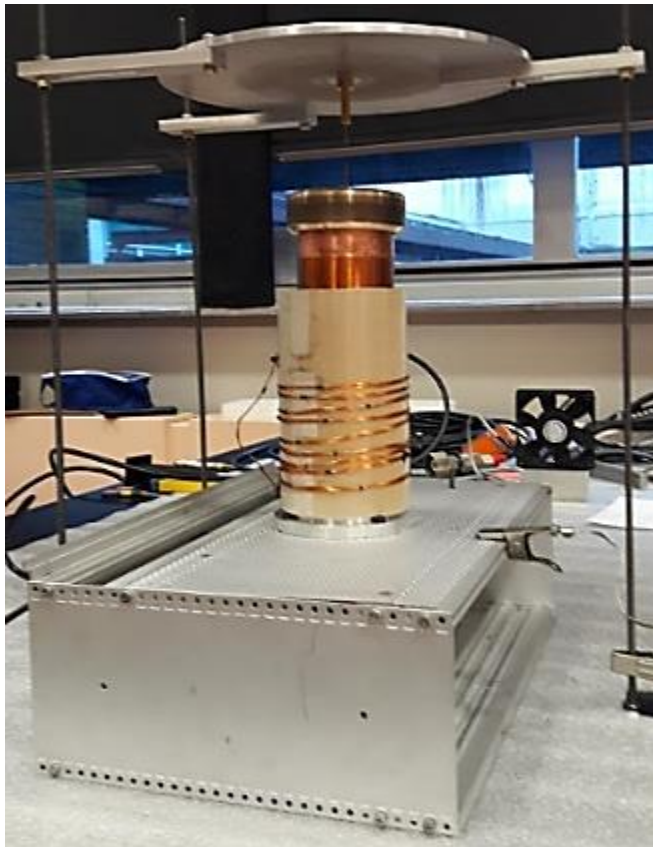
- Momentum transfer (Ions motion)

$$\vec{F} = q_i N_i E$$

$$\langle \vec{F} \rangle = \vec{F}_0 \left(1 + \frac{m_E^2}{2} + 2m_E \cos(\omega t) + m_E^2 \cos(2\omega t) \right)$$

Building a Plasma Speaker

Arcing in air \Rightarrow 30 kV/cm \Rightarrow a transformer



Plasma Speaker : it is possible !



IPT problem n°7: Static Speaker

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Discuss the maximum bandwidth, signal-to-noise ratio and power efficiency achieved with your design.

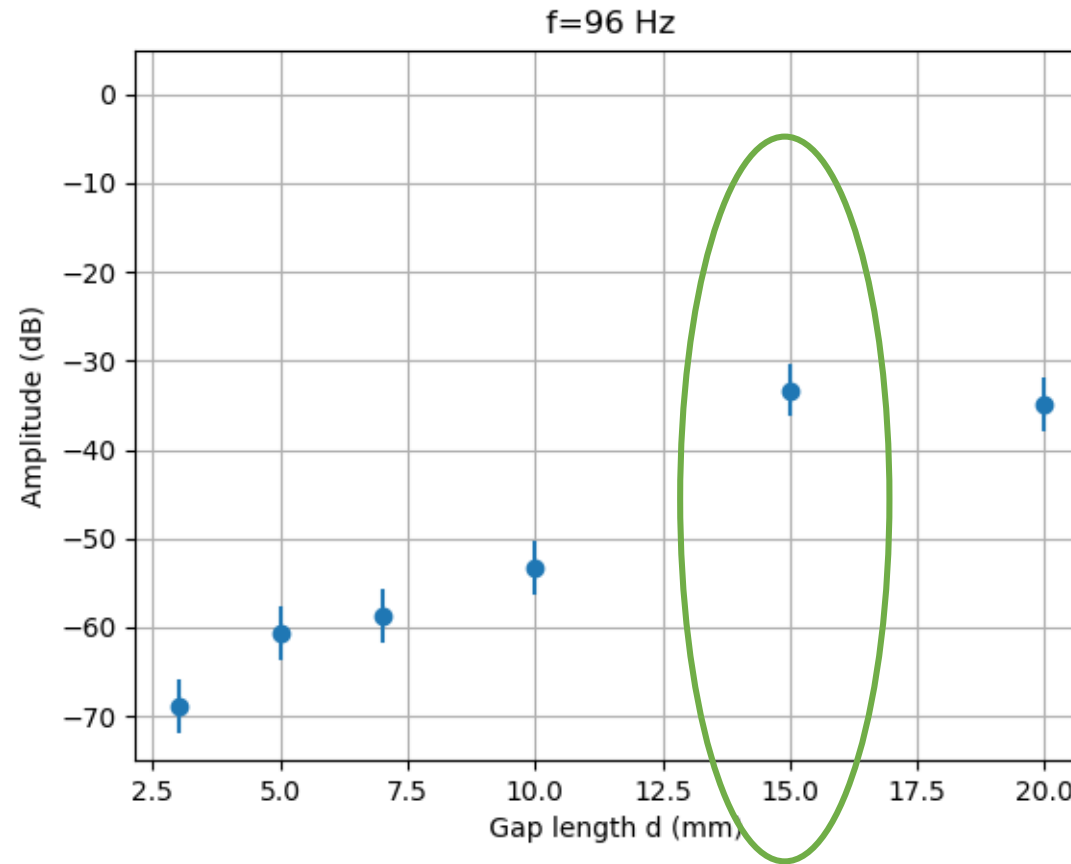
Is it possible to modify your device to use it as a microphone ?

Maximal bandwidth

Influence of gap length d



Influence of gap length d :



Best amplitude for $d = 15$ mm

Maximal bandwidth

Different kinds of discharges

Heat transfer H prominent



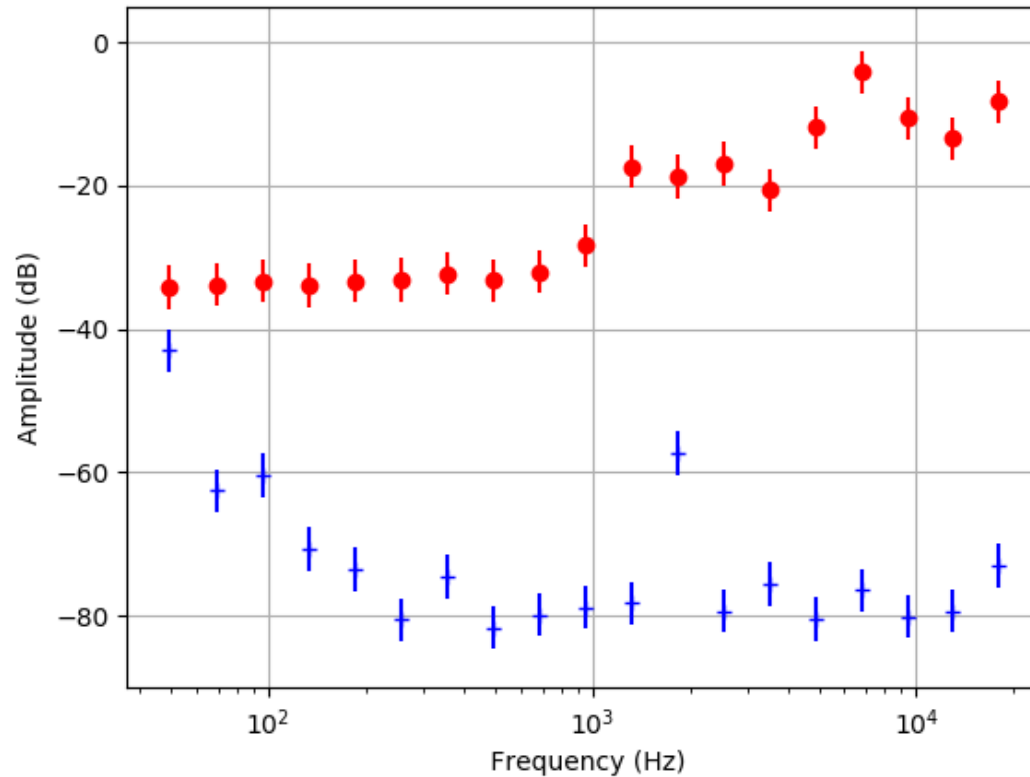
Corona



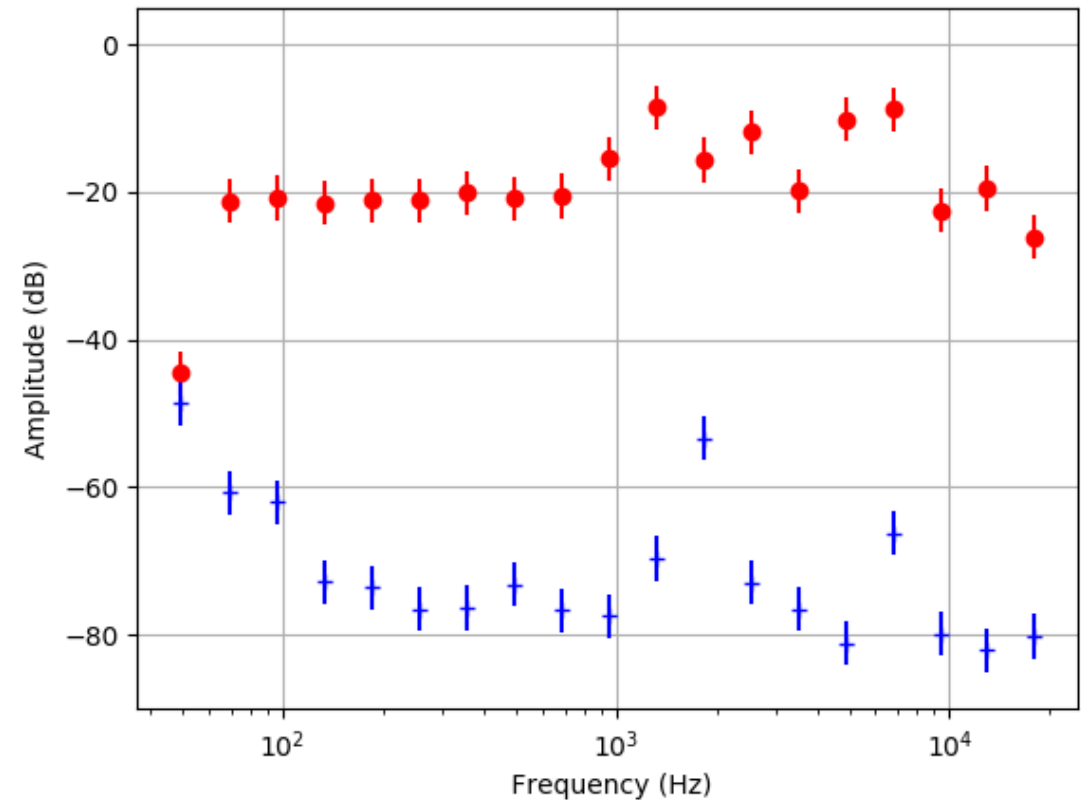
Momentum transfer prominent

Influence of discharge mode :

Arc



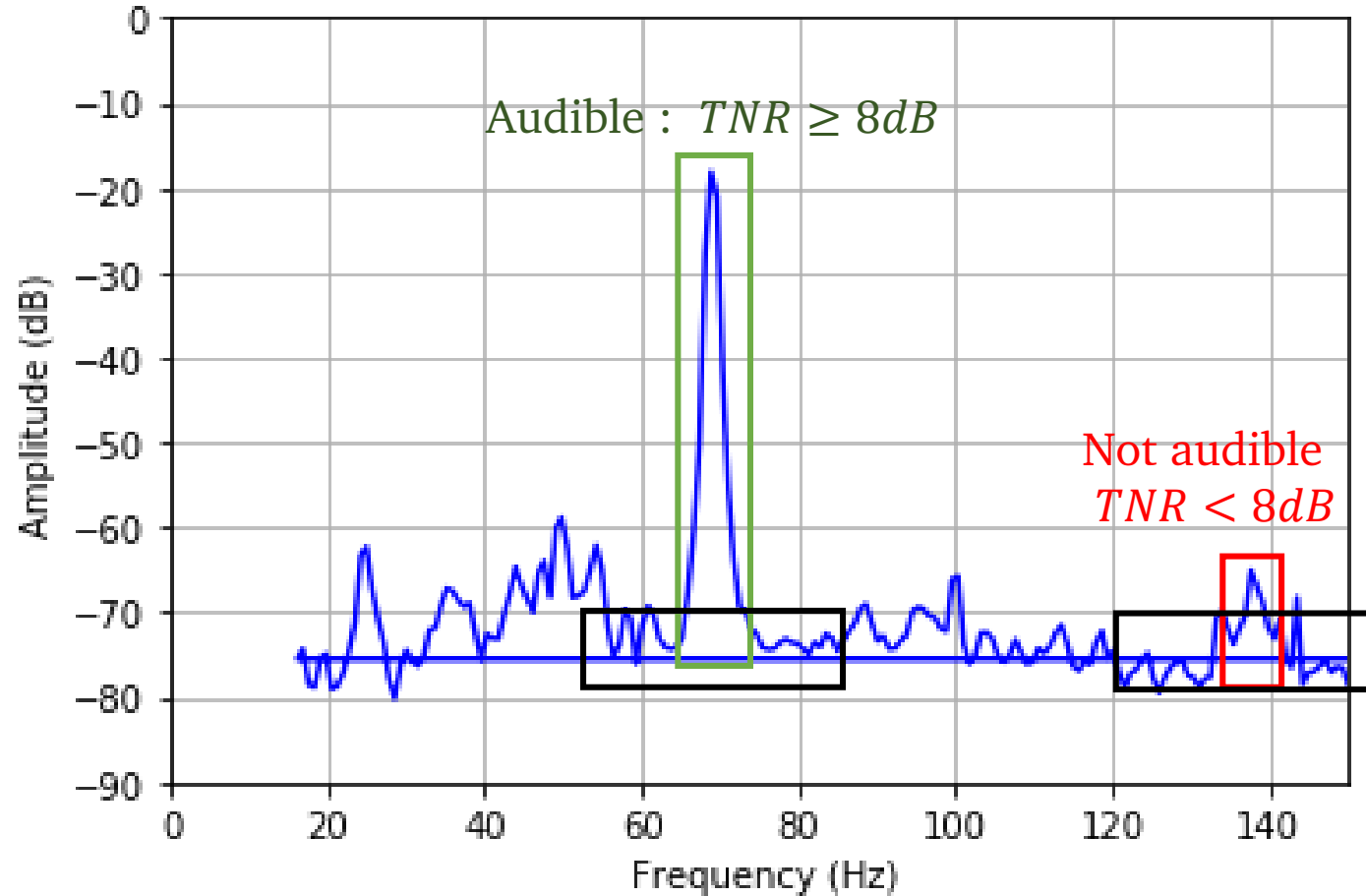
Corona



($d = 15$ mm, **red**: frequency response; **blue**: background)

Signal to Noise Ratio

TNR (Tone to Noise Ratio) according to *ECMA-74 International norm*

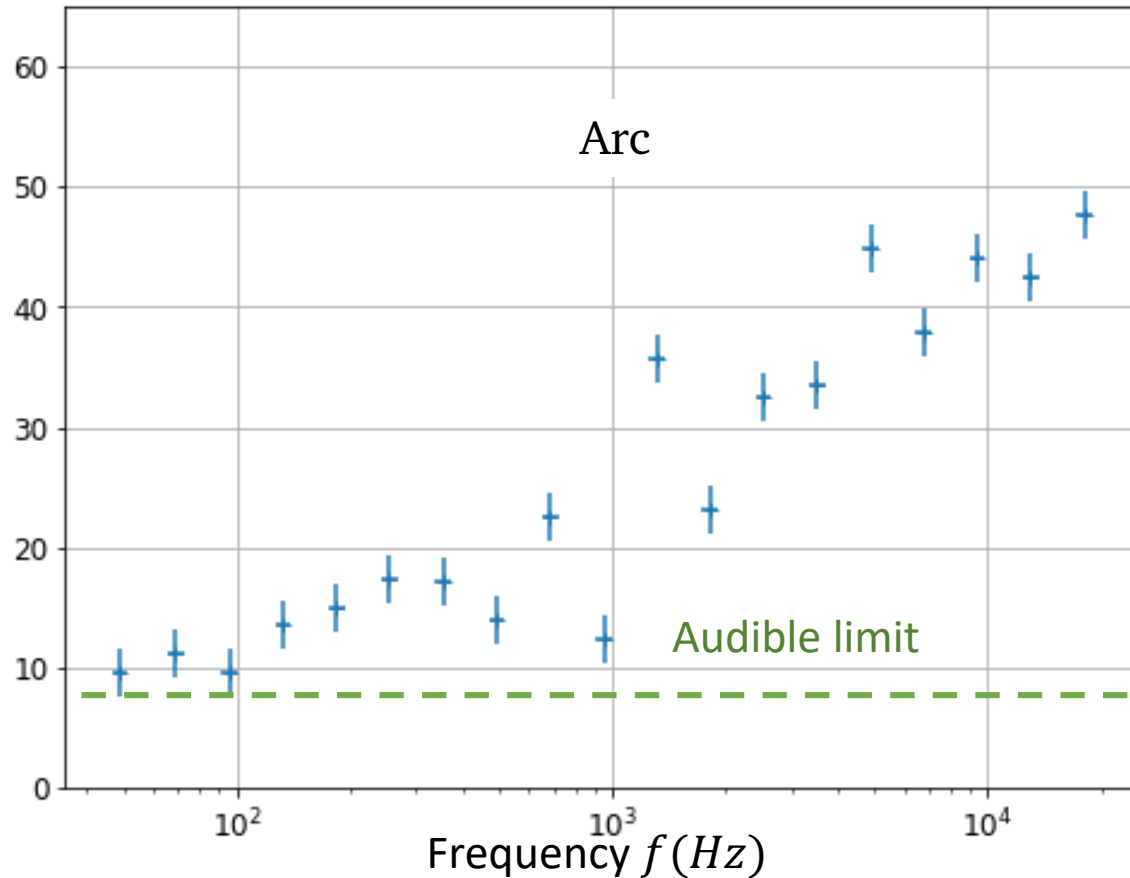


Signal to Noise Ratio

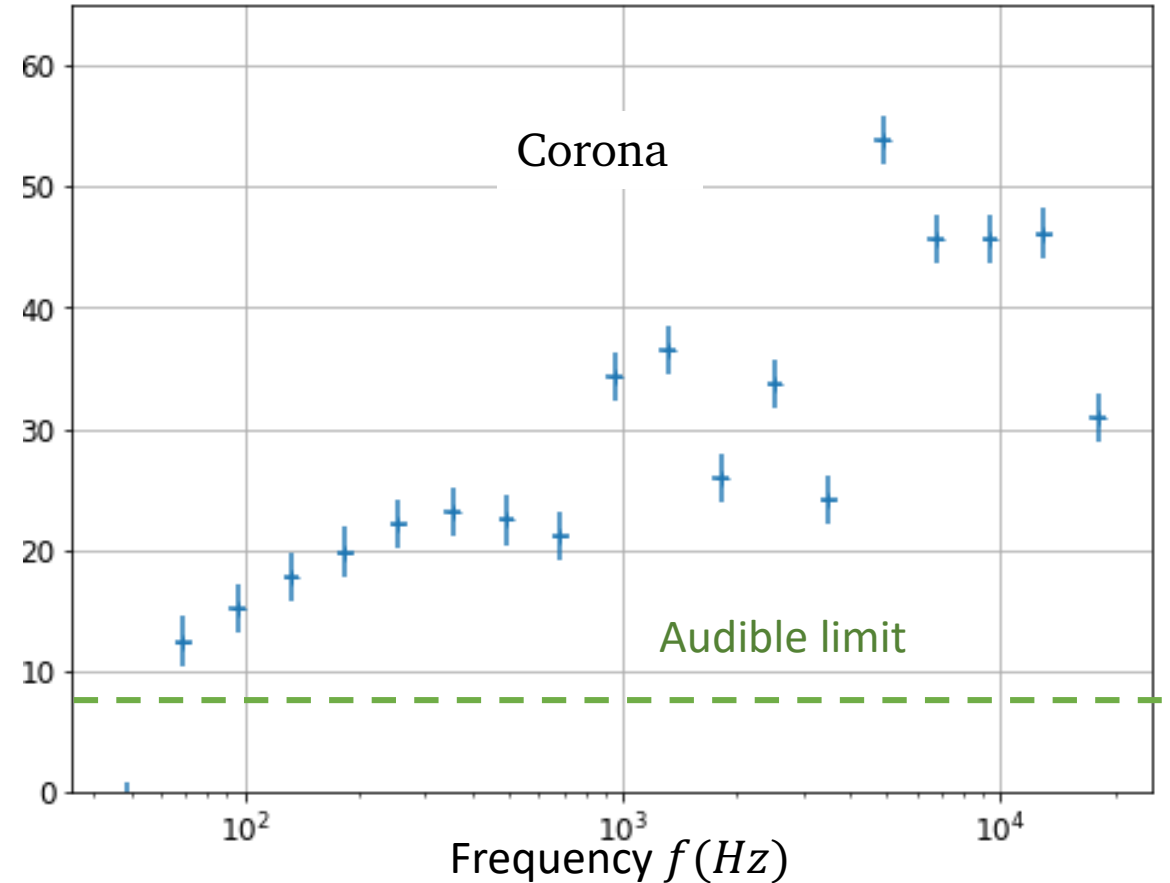
Tone to Noise Ratio

(same gap length $d=15$ mm)

TNR(dB)



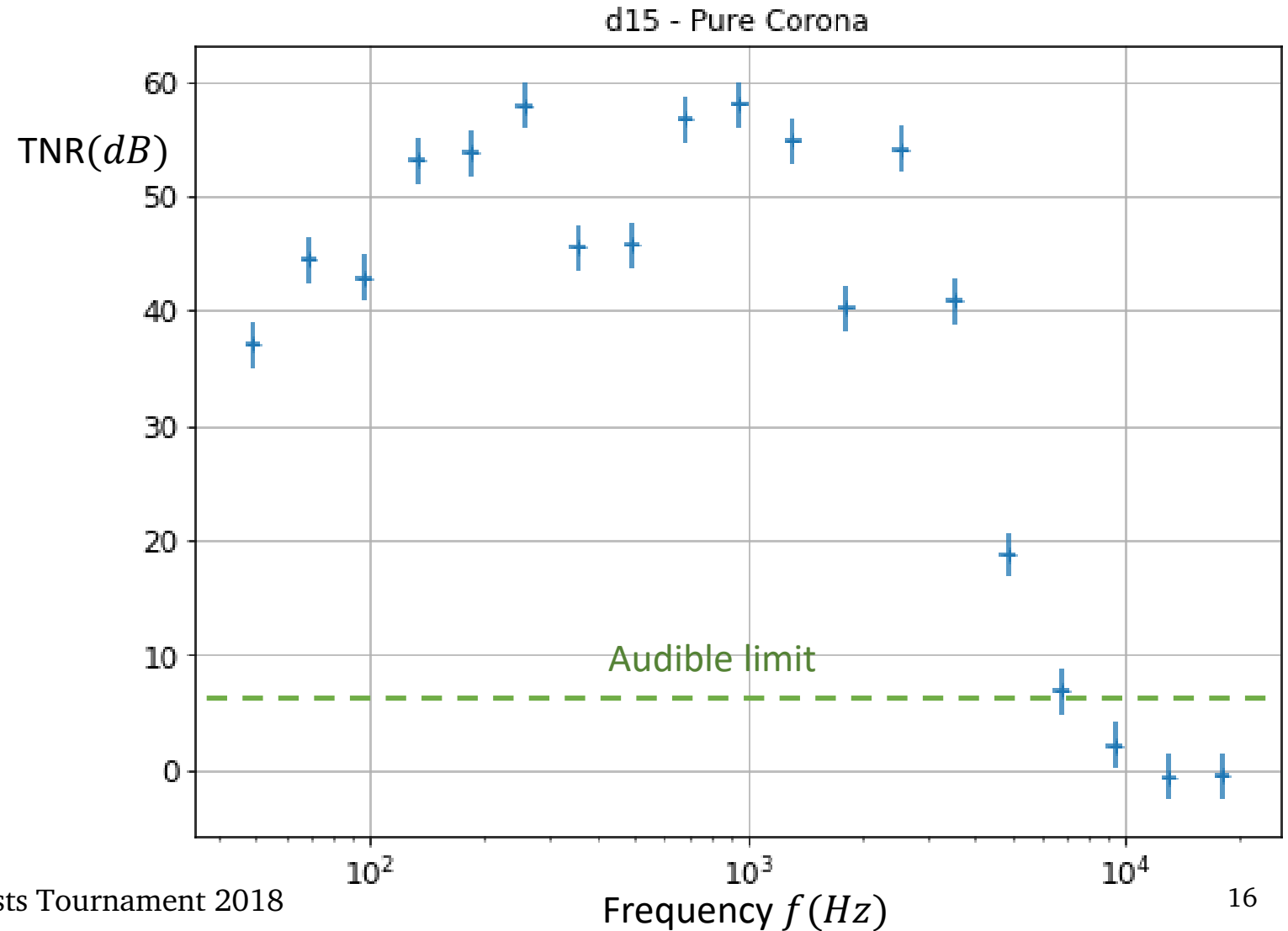
TNR(dB)



Signal to Noise Ratio

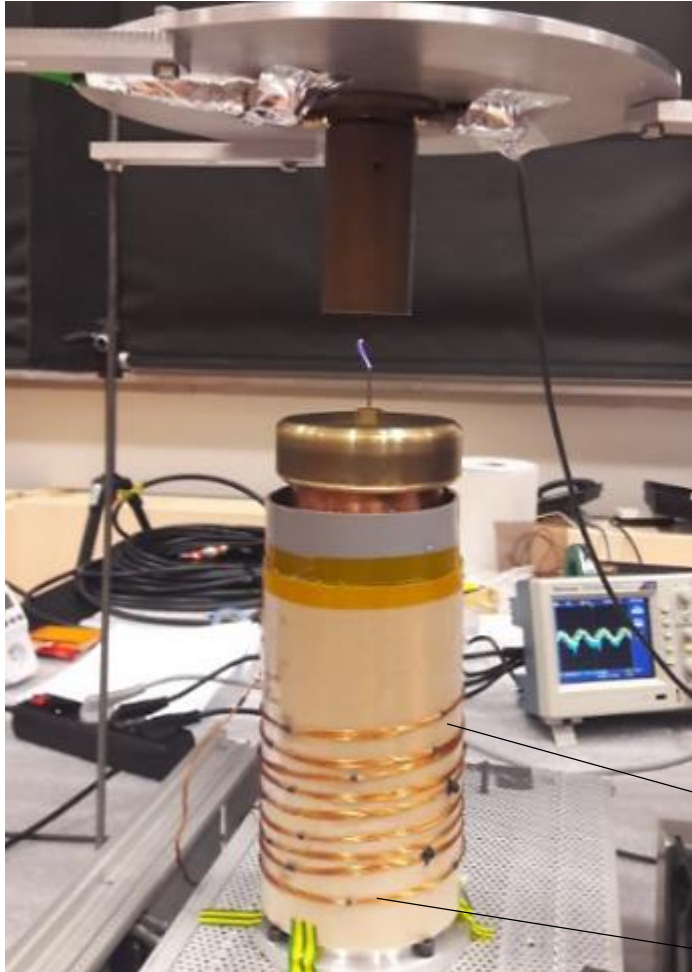
Tone to Noise Ratio

Tape
 ↓
 Dielectric
 ↓
 Purified Corona

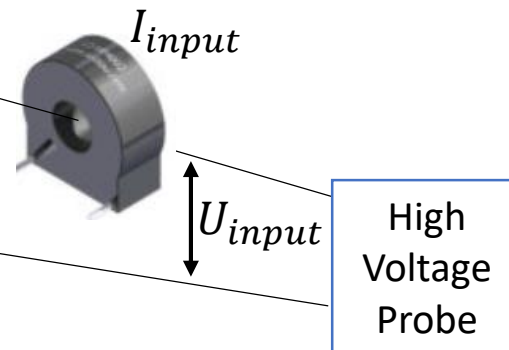


Power efficiency

Electrical Power

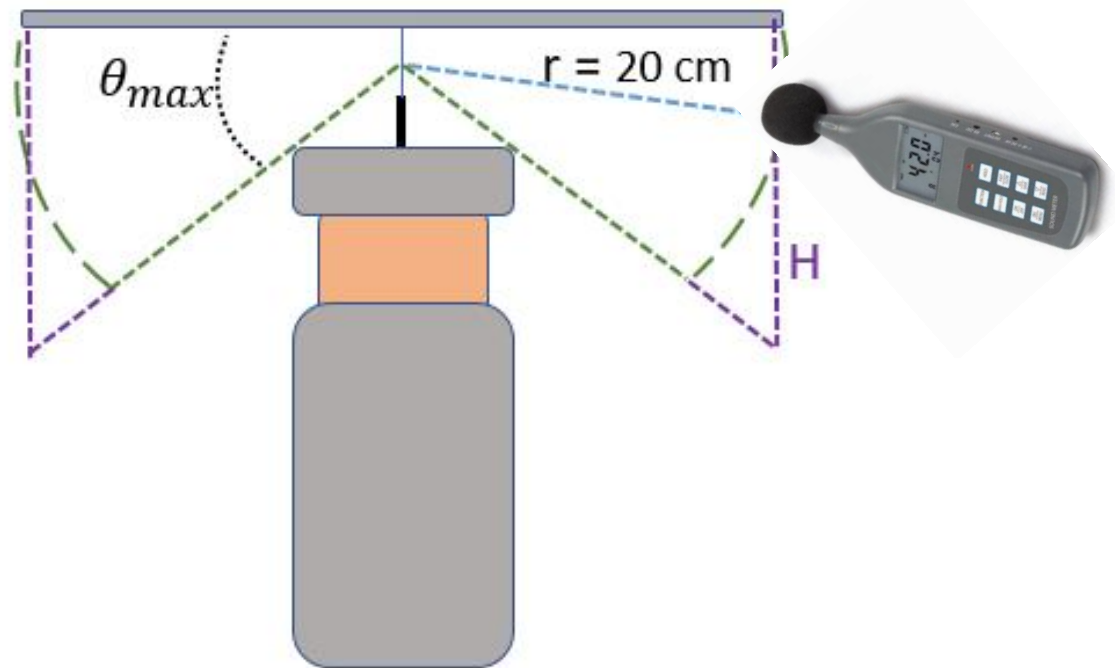
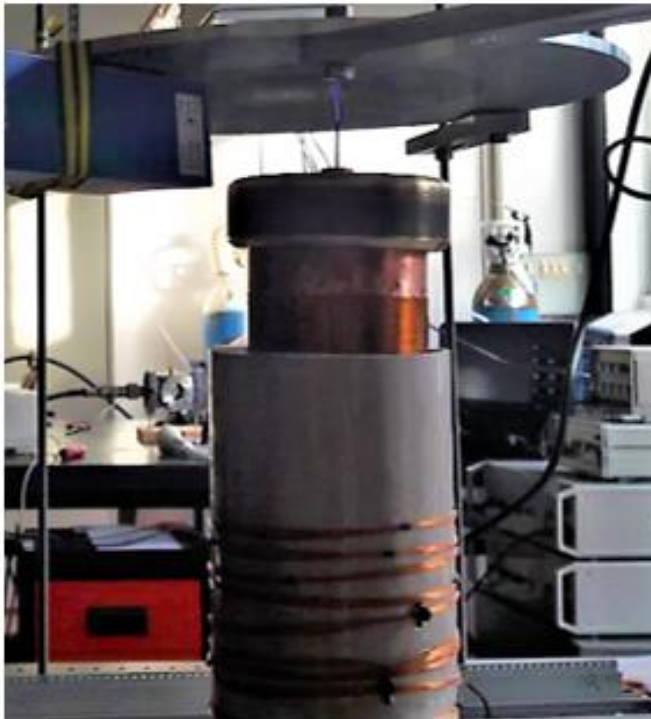


$$P_{elec} = \frac{1}{T} \sqrt{\int_0^T (I_{input}(t)U_{input}(t))^2 dt}$$



Power efficiency

Acoustic Power



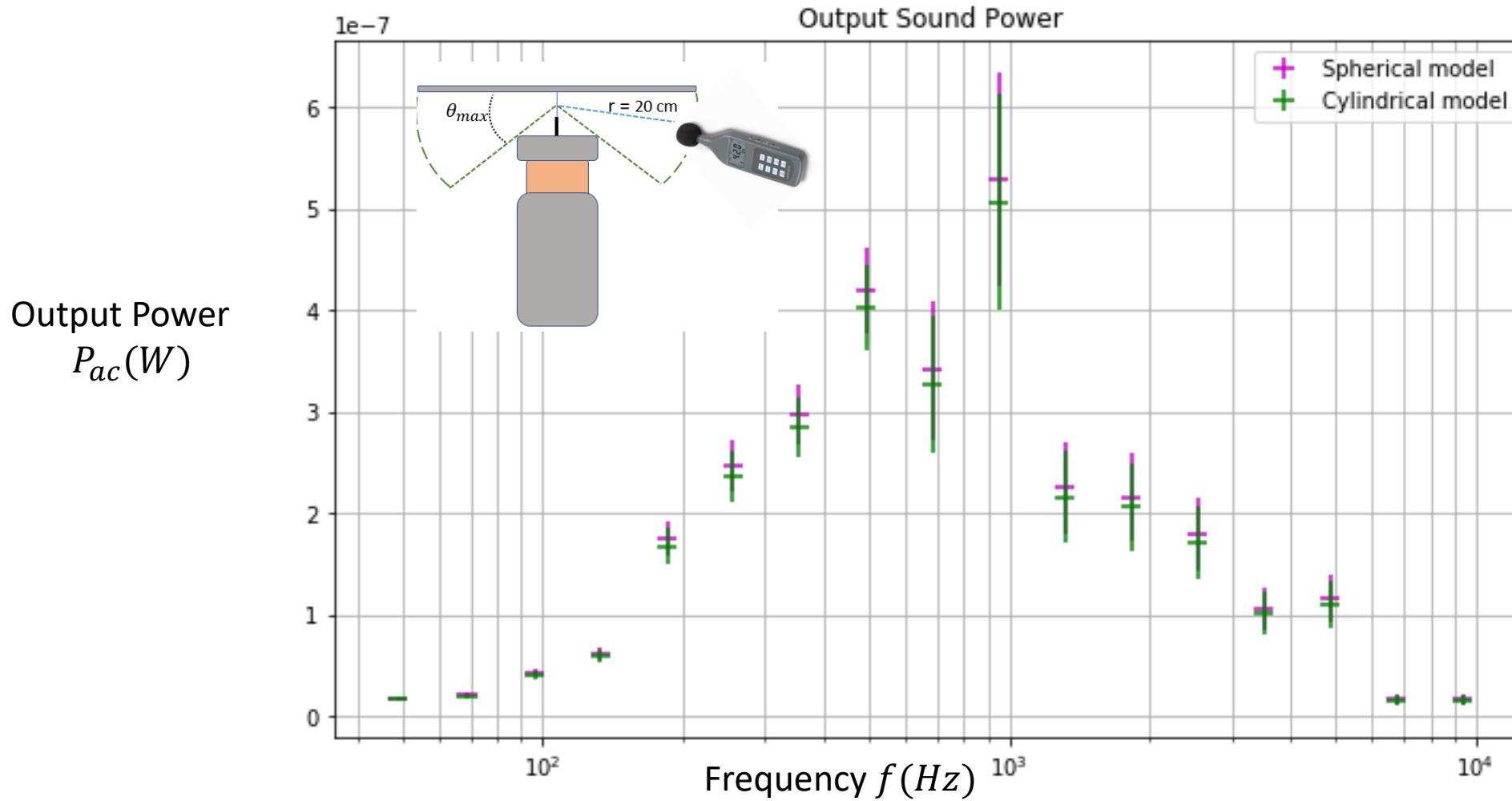
$$\text{Acoustic Power : } P_{ac} = S \times \frac{p^2}{\rho c}$$

$S = 2$ possible models : sphere or cylinder

$\rho, c, p =$ air density, speed of sound, air pressure

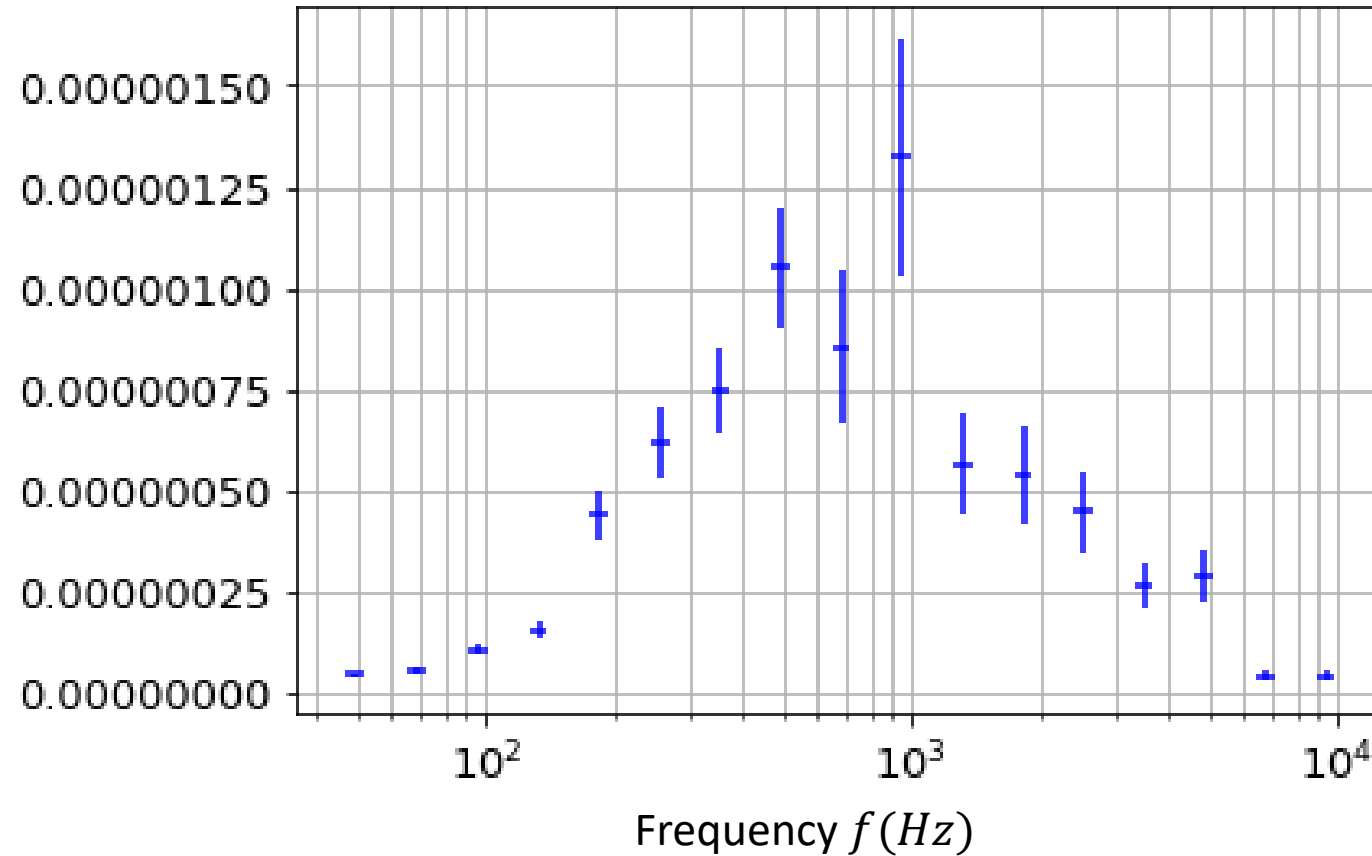
Power efficiency

Acoustic Power

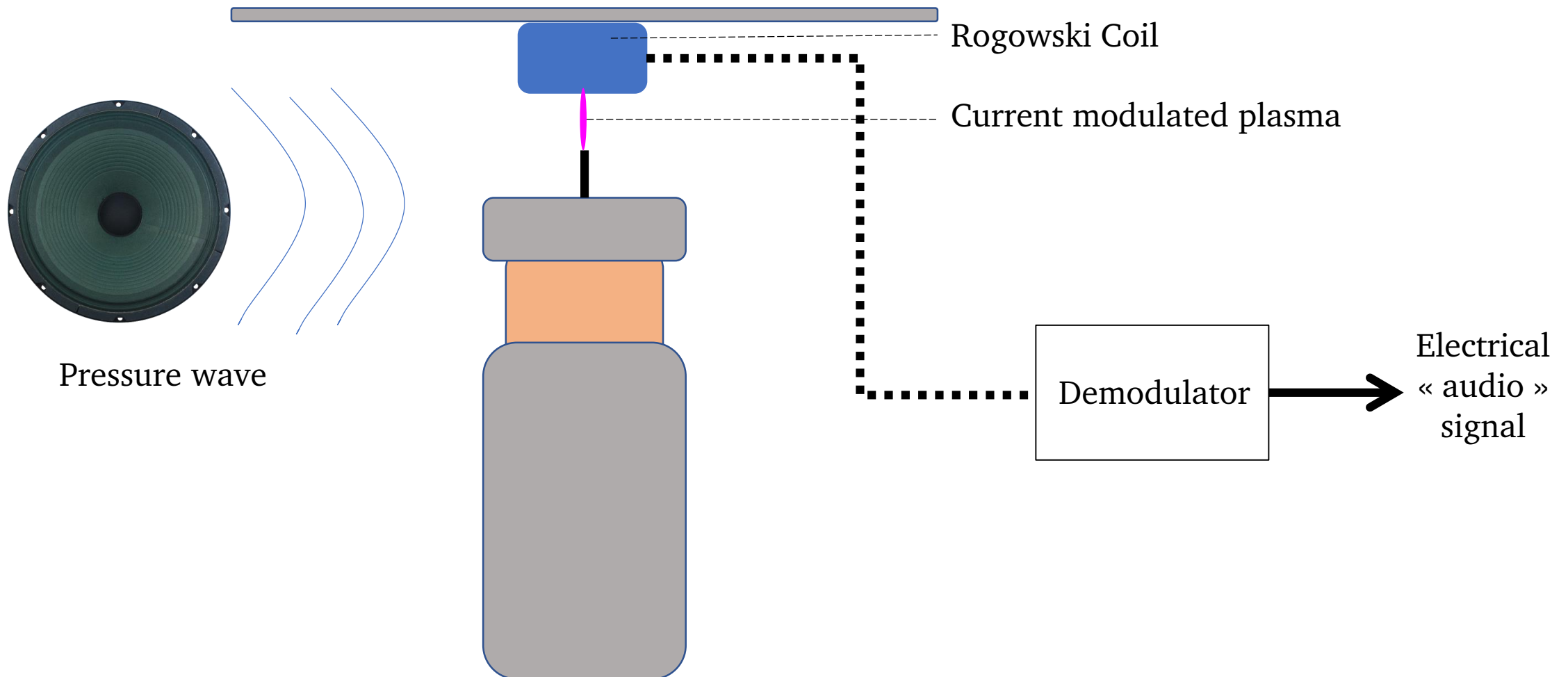


Power efficiency

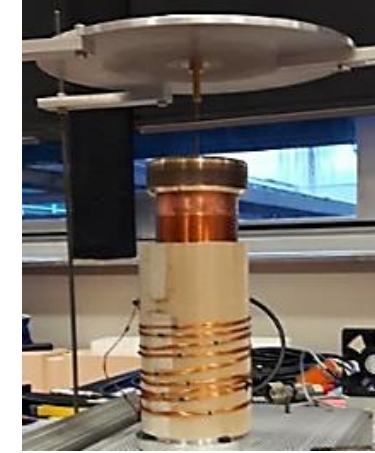
$$\text{Efficiency} = \frac{P_{ac}}{P_{elec}} (\%)$$



A « plasmicrophone »



Conclusion



Main objectives of the problem:

« *Build a static speaker* »:

Plasma speaker is OK.

« *Discuss the maximum bandwidth* » :

Whole spectrum accessible, best gap length is $\approx 15 \text{ mm}$
Corona better for $f < 1 \text{ kHz}$, arc better for high frequencies

« *Signal To Noise Ratio* » :

Best **Tone to Noise Ratio** (up to 60dB)
reached with a « pure » corona discharge

« *and Power efficiency* »:

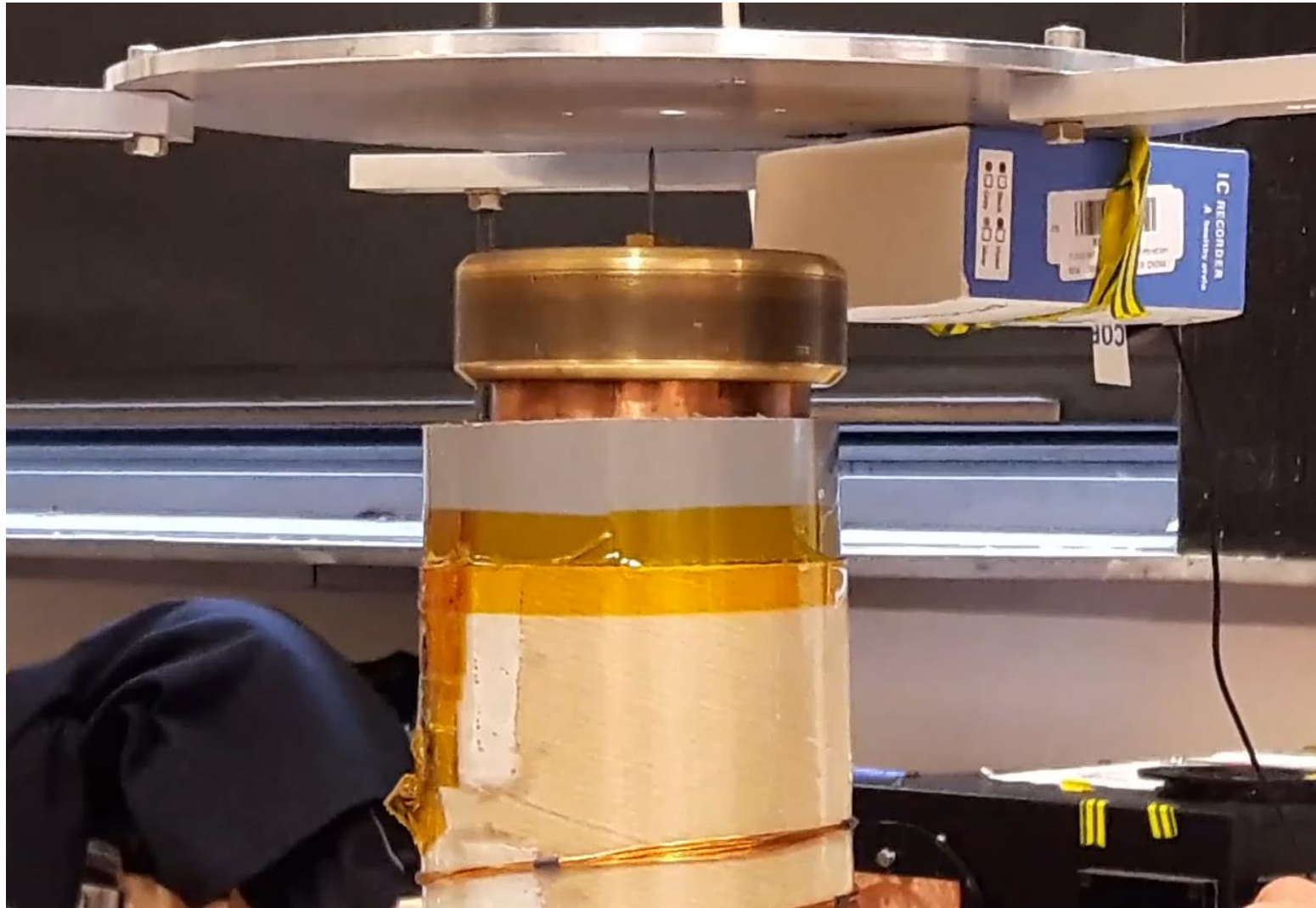
Weak efficiency ($2 \cdot 10^{-7} \%$) for **low**,
better ($15 \cdot 10^{-7} \%$) for **medium high frequencies**

« *use it as a microphone?* »

Theoretically possible.

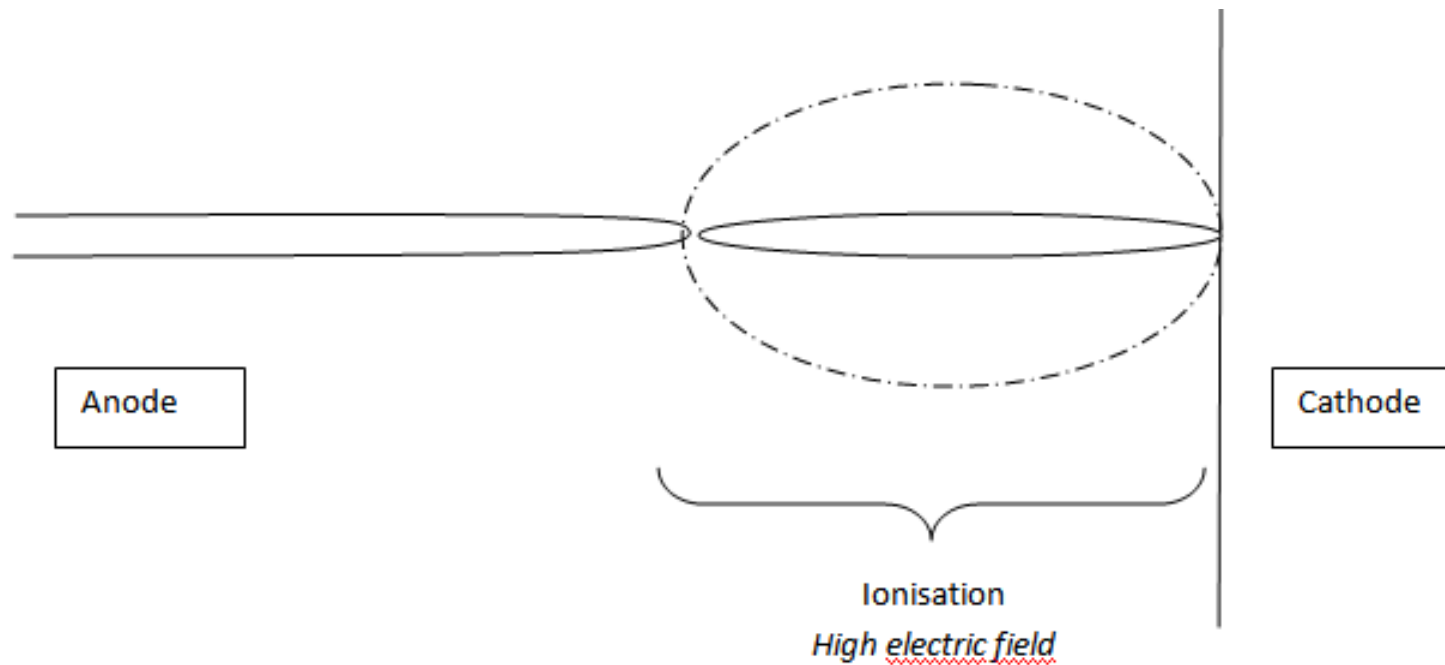
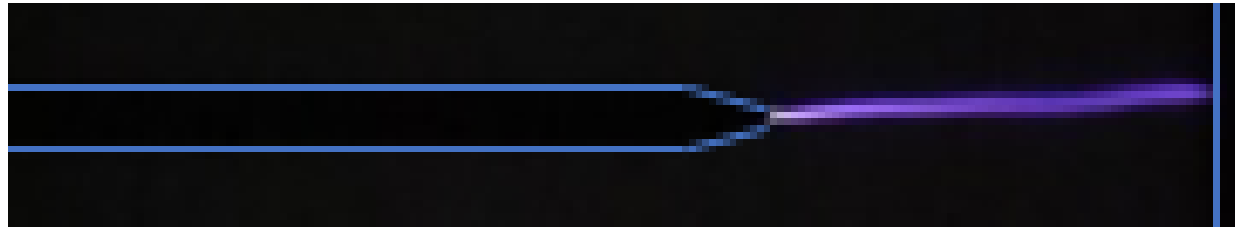
Thank you for listening !

The sound is really created by the plasma



Theory of plasma speakers

Different kinds of discharges

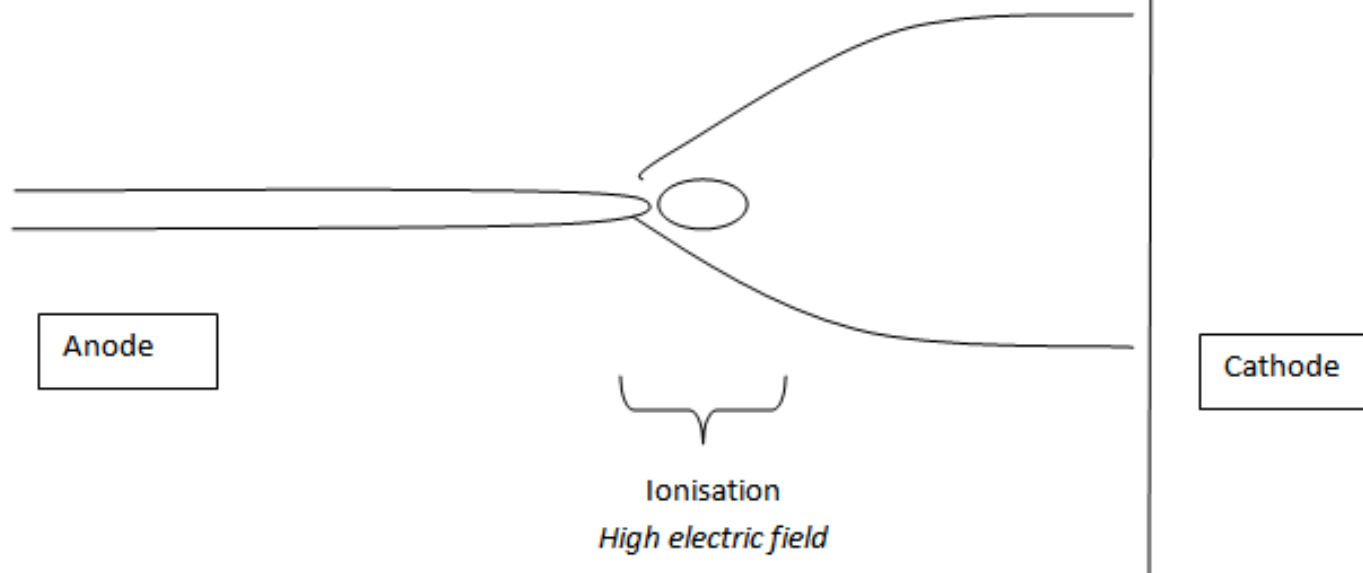


ARC DISCHARGE:

- high voltage, big ionisation
- Heat transfer H is prominent

Theory of plasma speakers

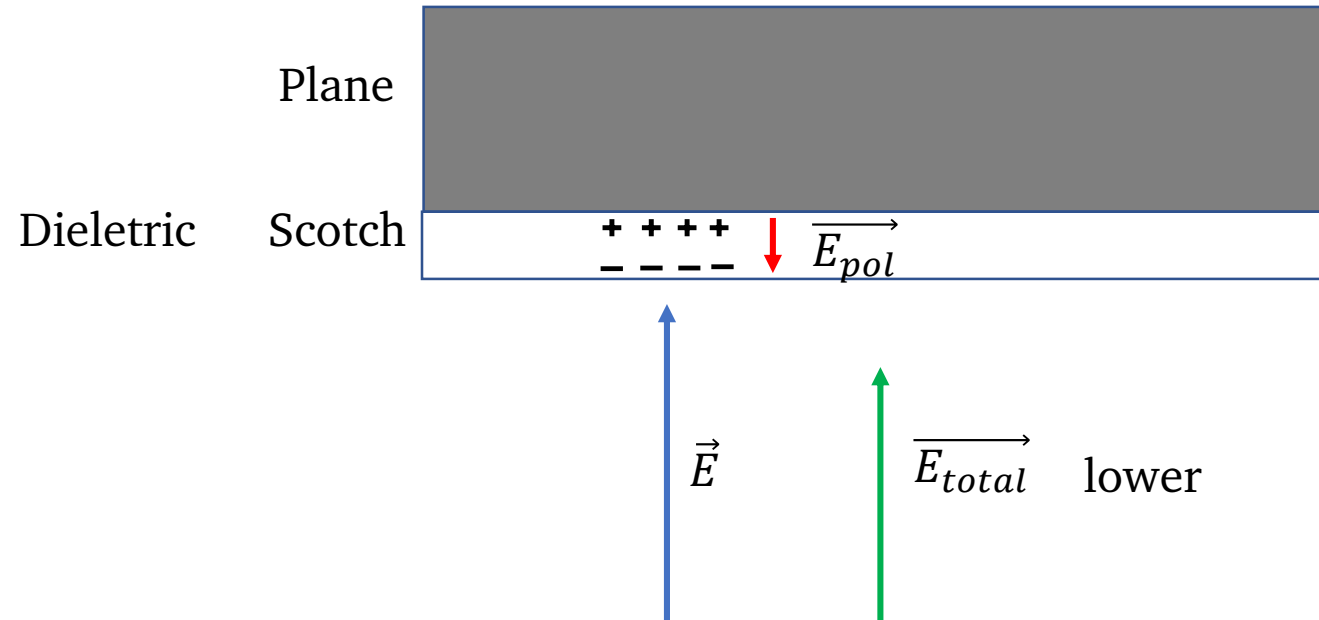
Different kinds of discharges



CORONA DISCHARGE:

- Complex geometry
- Lower current than in arc
- Momentum transfer is prominent

« Purifying » corona : Scotch tape !



About non-linearities

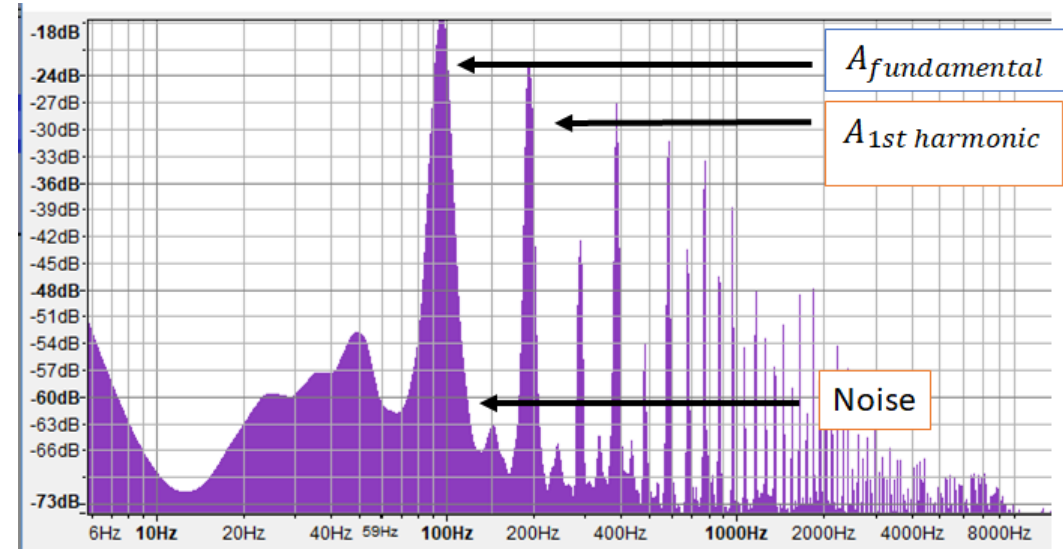
Two source terms :

$$\langle H \rangle = H_0 \left(1 + \frac{m_E + m_I}{2} + (m_E + m_I)\cos(\omega t) + m_E m_I \cos(2\omega t) \right)$$

$$\langle \vec{F} \rangle = \vec{F}_0 \left(1 + \frac{m_E}{2} + 2m_E \cos(\omega t) + m_E^2 \cos(2\omega t) \right)$$

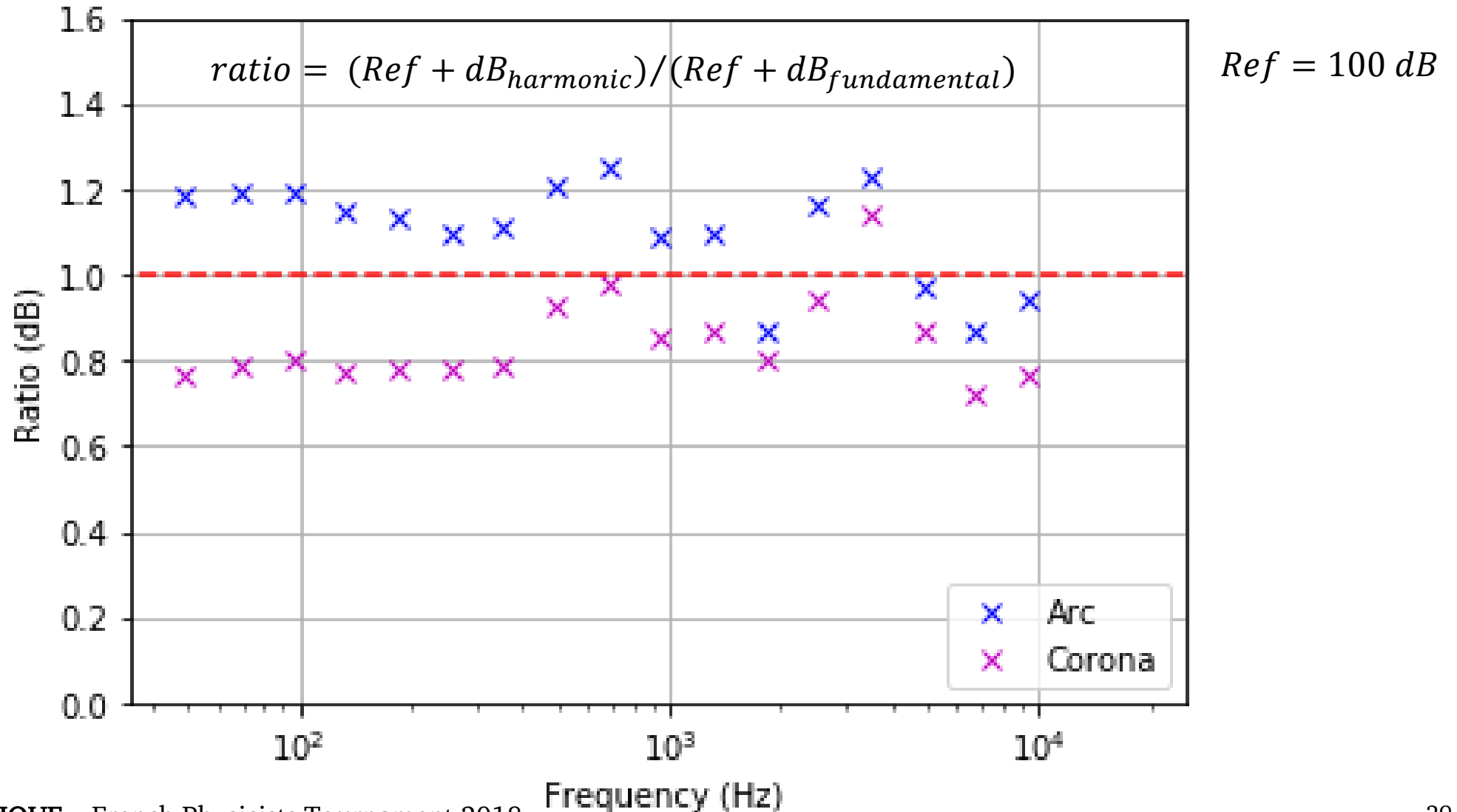
m_I, m_E : modulation rates of tension and current

Non-linearities occur with signal overmodulation



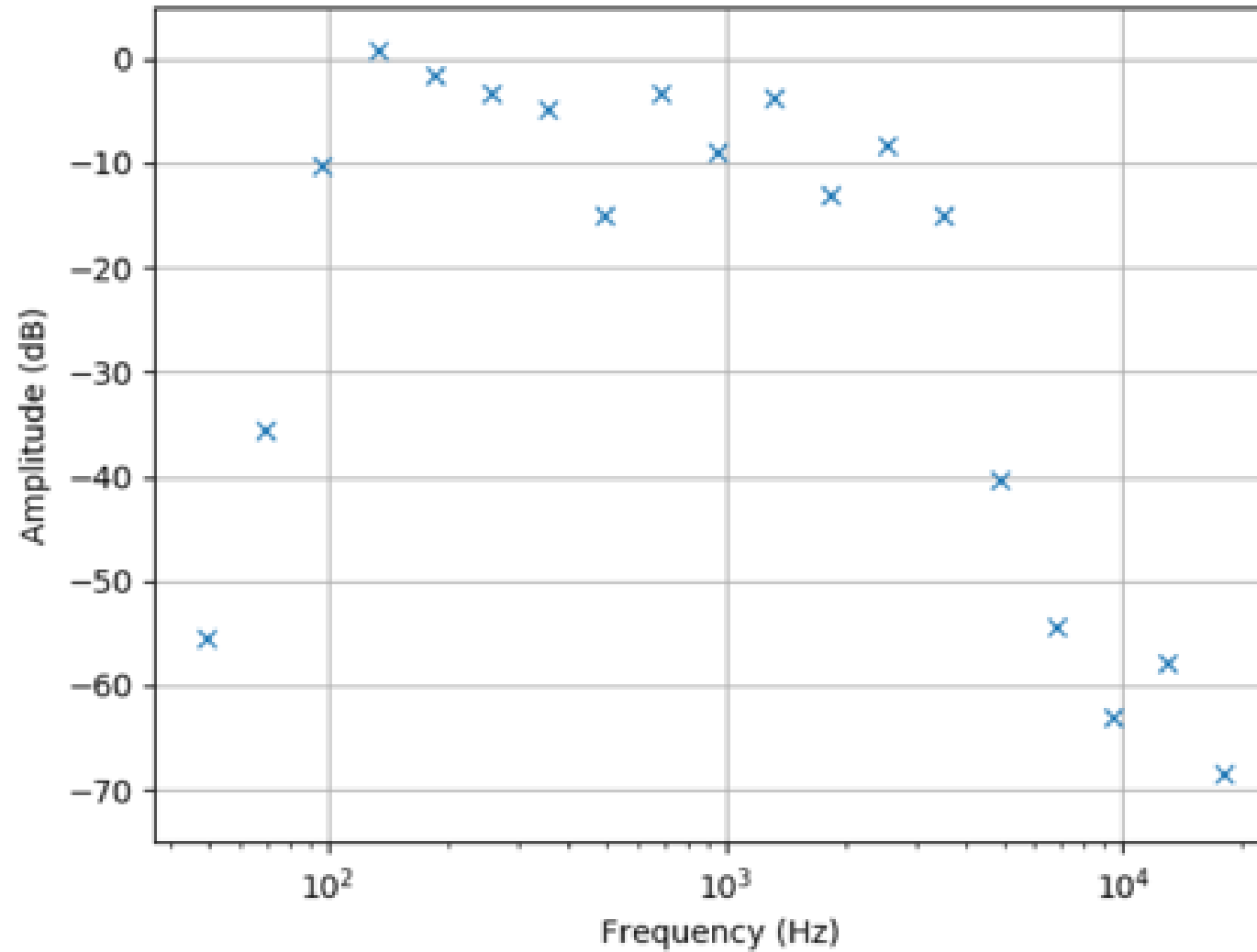
About non-linearities

importance of the 1st harmonic (2ω)



Sound Measurement

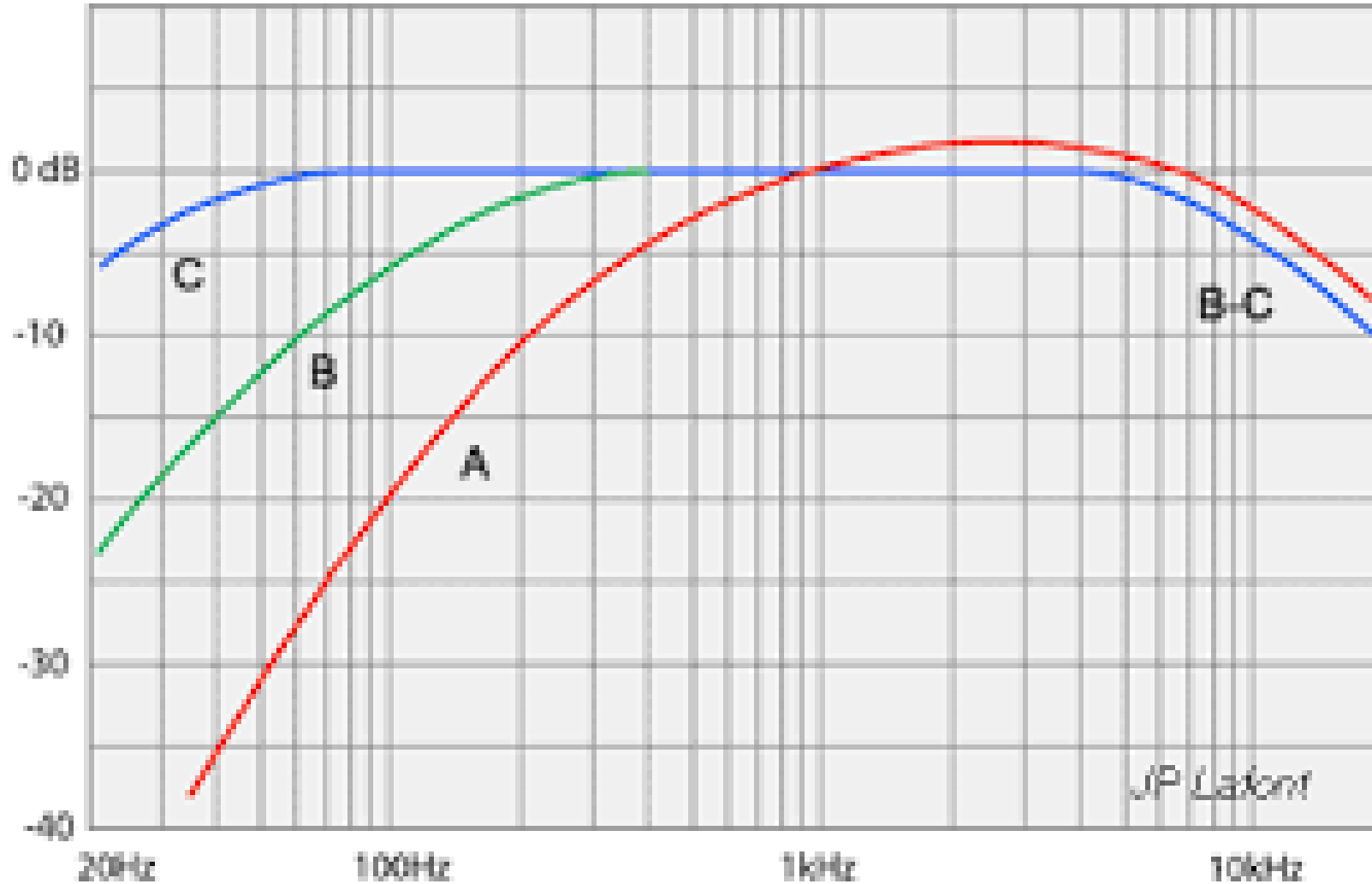
Influence of the microphone



Sound Measurement



Influence of the sonometer

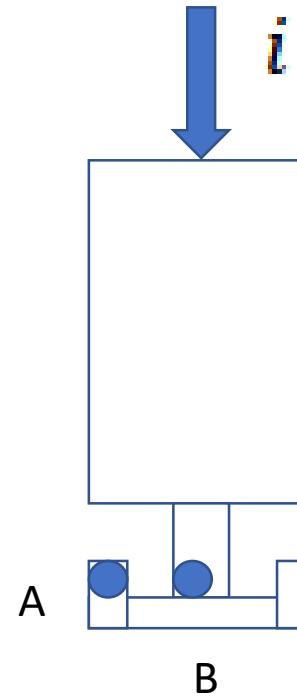


Chose the sonometer
weighting :
A, B, C
or **nothing**

Voltage and Current Measurements



Rogowski coil

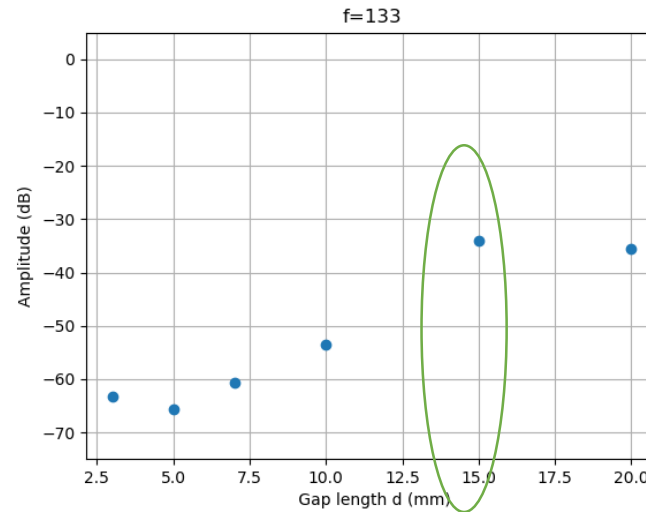
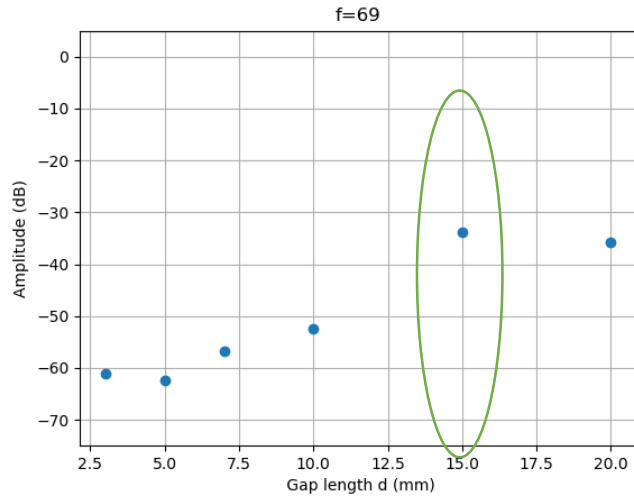


Inductive Shunt coil

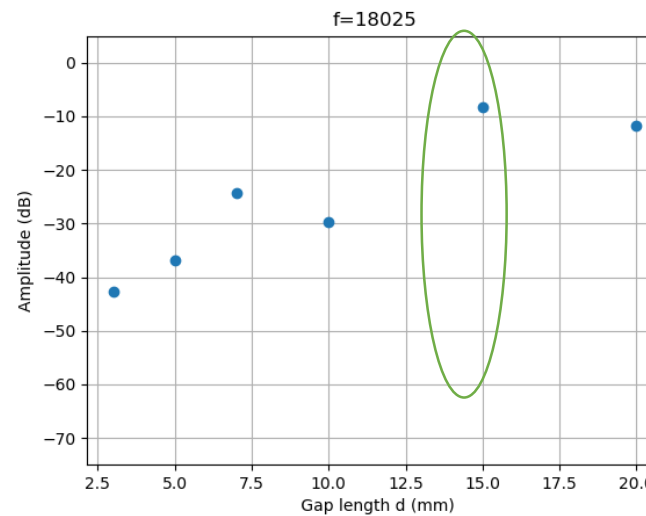
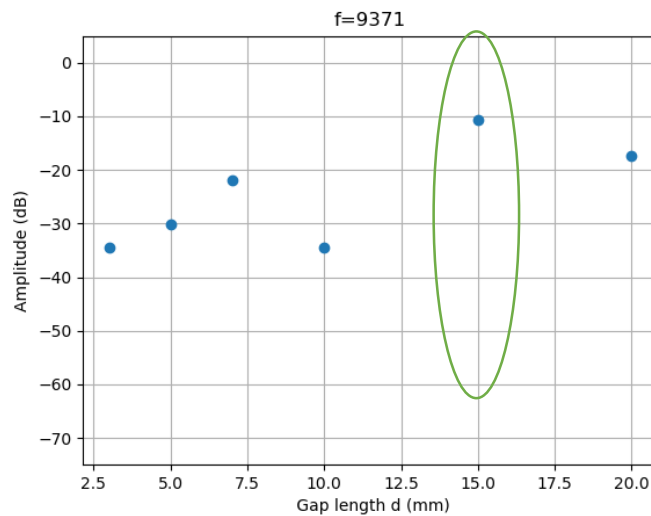
$$u_{AB} = L \frac{di}{dt}$$

$$L = 1.1 \text{ nH}$$

Influence of the distance inter electrode



Whole range of the audio spectrum:



$d = 15\text{mm}$ is an overall good distance

Stationary waves selected

2 obstacles at a distance L



L

$$2L = n \lambda, n \in \mathbb{N}$$

$$\lambda f = c_0$$

$$f_n = \frac{nc_0}{2L} \approx n \, 3.5 \, \text{kHz}$$