



New Family of Neutrosophic Soft Sets

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Abstract: The goal of this paper is to study and discuss the neutrosophic soft set theory by introducing, new family of neutrosophic soft sets and because the concept of topological spaces is one of the most powerful concepts in system analysis, we introduced the concept of neutrosophic soft topological spaces depending on this the new family. Furthermore, we introduced new definitions, properties, concerning the neutrosophic soft closure, the neutrosophic soft interior, the neutrosophic soft exterior and the neutrosophic soft boundary in details.

Keywords : neutrosophic soft set theory, of neutrosophic soft topological spaces , new operations for neutrosophic soft sets. families of neutrosophic soft sets.

1. Introduction

D Molodtsov[1] introduced the notion of soft set in 1999 . In the same year F Smarandache firstly introduced the neutrosophic set theory [2]. Which is the generalization of the class set conventional fuzzy set [3] and intuitionistic set fuzzy [4]. The soft set theory and the neutrosophic set theory have been applied to many different fields, (see for example [5-64]) .

In 2012 Maji[65] combined the concept of soft set and neutrosophic set together by introducing the current mathematical framework called neutrosophic soft set and later this concept has been modified by S.Bromi[66] . Faruk[67] redefined neutrosophic soft set, and their operations, also presented an application of neutrosophic soft set, in decision making . In 2017 Bera[68] introduced neutrosophic soft topological spaces using different subsets of the parameters set for each soft set . In 2019 and In 2020 Taha[69] and Evanzalin[70] introduced the neutrosophic soft topological spaces differently from the study[58] . More works on the concept, of neutrosophic soft set can be found in [71, 72, 73, 74, 75, 76, 77, 78, 79, 80,81,82] .

In this research , we studied and discussed the neutrosophic soft set theory by introducing, new family of neutrosophic soft sets, new operations for neutrosophic soft sets and we also we introduce the theory of neutrosophic soft topological spaces depending on this the new family.

The research is organized as follows: In section2, we first recall the necessary definitions needed in this work we then recall two families of neutrosophic soft sets with explaining the properties of each family. In section3, the neutrosophic soft set theory is studied and discussed by introducing, new family of neutrosophic soft sets [namely third family], new operations for neutrosophic soft sets, comparison between the new family and other families, new definitions and examples. In section4, the theory of neutrosophic soft topological spaces is investigated depending on the new family and also, new definitions, characterization, the neutrosophic soft closure, the neutrosophic

soft interior, the neutrosophic soft exterior and the neutrosophic soft boundary are introduced in details .

2. Preliminaries

In this section, we will recall the necessary definitions needed in this work, we then recall two families of neutrosophic soft sets with explaining the properties of each family .

2.1. Definition [83]

If K is the initial universe then the neutrosophic set A is defined as follows:

$$A = \{ \langle k, T_A(k), I_A(k), V_A(k) \rangle, k \in K \}$$

where, the functions $T, I, V : K \rightarrow] - 0, +1 [$ and

$$- 0 \leq T_A(k) + I_A(k) + V_A(k) \leq +3$$

For any two neutrosophic sets:

$$A = \{ \langle k, T_A(k), I_A(k), V_A(k) \rangle, k \in K \} .$$

$$B = \{ \langle k, T_B(k), I_B(k), V_B(k) \rangle, k \in K \} .$$

- ❖ $A \subseteq B \leftrightarrow T_A(k) \leq T_B(k), I_A(k) \leq I_B(k), V_A(k) \geq V_B(k)$, for all, $k \in K$.
- ❖ $A \cup B = \{ \langle k, T_A(k) \vee T_B(k), I_A(k) \vee I_B(k), V_A(k) \wedge V_B(k) \rangle, k \in K \}$.
- ❖ $A \cap B = \{ \langle k, T_A(k) \wedge T_B(k), I_A(k) \wedge I_B(k), V_A(k) \vee V_B(k) \rangle, k \in K \}$.
- ❖ $A = B \leftrightarrow A \subseteq B$ and $B \subseteq A$.
- ❖ The complement of A denoted by A^c is defined as:
 $(A)^c = \{ \langle k, 1 - T_A(k), 1 - I_A(k), 1 - V_A(k) \rangle, k \in K \}$.

2.2. Definition [1]

Let K be an initial universe set and E be a set of parameters. Consider a set $A \neq \emptyset, A \subseteq E$. A pair (F, A) is called a soft set (over K) if and only if F is a mapping from A into the set of all the subsets of K .

First family [65]

Let K be an initial universe set and E_K be a set of parameters . Consider a set $D \neq \emptyset, D \subseteq E_K$. A pair (F, D) is called a neutrosophic soft set (over K) if and only if F is a mapping from A into the set of all the neutrosophic sets over K .

Note that , we will denote simply by F_D of the pair (F, D) and the set of all the neutrosophic sets over K with respect to this family will be denoted by $N_1(K)$.

Let $F_{1D}, F_{2D} \in N_1(K)$. Then :

- 1) The union between them $(F_D \sqcup G_B)$ is defined by $H = F_D \sqcup G_B$ as follows :

$$T_{H(p)}(k) = \begin{cases} T_{F(p)}(k) & \text{if } p \in D \setminus B \\ T_{G(p)}(k) & \text{if } p \in B \setminus D \\ \max \{ T_{F(p)}(k), T_{G(p)}(k) \} & \text{if } p \in D \cap B \end{cases}$$

$$I_{H(p)}(k) = \begin{cases} I_{F(p)}(k) & \text{if } p \in D \setminus B \\ I_{G(p)}(k) & \text{if } p \in B \setminus D \\ \frac{(I_{F(p)}(k)+I_{G(p)}(k))}{2} & \text{if } p \in D \cap B \end{cases}$$

$$V_{H(p)}(k) = \begin{cases} V_{F(p)}(k) & \text{if } p \in D \setminus B \\ V_{G(p)}(k) & \text{if } p \in B \setminus D \\ \min\{V_{F(p)}(k), V_{G(p)}(k)\} & \text{if } p \in D \cap B \end{cases}$$

2) The interstation between them($F_D \cap G_B$) is defined by $H = F_D \cap G_B$ as follows :

$$T_{H(p)}(k) = \min \{T_{F(p)}(k), T_{G(p)}(k)\}$$

$$I_{H(p)}(k) = \frac{(I_{F(p)}(k)+I_{G(p)}(k))}{2}$$

$$V_{H(p)}(k) = \max \{V_{F(p)}(k), V_{G(p)}(k)\}.$$

3) $F_D \subseteq G_B$ if and only if

1) $D \subseteq B$

2) $T_{F(p)}(k) \leq T_{G(p)}(k), I_{F(p)}(k) \leq I_{G(p)}(k), V_{F(p)}(k) \geq V_{G(p)}(k)$, for all $p \in D, k \in K$.

4) The complement of F_D is defined as:

$$(F_D)^c = \{(p, \langle k, T_{F(p)}(k), I_{F(p)}(k), V_{F(p)}(k) \rangle, p \in D)\}.$$

2.3. Definition [70]

A neutrosophic soft set F_D over the universe K is called a null neutrosophic soft set and denoted by \emptyset_N if $T_{F(p)}(k) = 0, I_{F(p)}(k) = 0, V_{F(p)}(k) = 1$, for all $p \in D, k \in K$.

2.4. Definition [70]

A neutrosophic soft set F_D over the universe K is called an absolute neutrosophic soft set and denoted by K_N if $T_{F(p)}(k) = 1, I_{F(p)}(k) = 1, V_{F(p)}(k) = 0$, for all $p \in D, k \in K$.

Second family [66]

Let K be an initial universe set and E be a set of parameters, $P(Y)$ be the set of all the subsets of K and V be a neutrosophic set over E . Then a neutrosophic parameterized soft sets.

$$\Omega_V = \{ \langle p, T_V(p), I_V(p), W_V(p), f_V(p) \rangle, p \in E \}$$

where, the functions $T_V, I_V, W_V : E \rightarrow [0,1]$ and $f_V : E \rightarrow P(K)$

and $f_V(p) = \emptyset$ if $T_V(p) = 0, I_V(p) = 1$ and $W_V(p) = 1$.

Here, the functions T_V, I_V, W_V are called membership function, indeterminacy function and non-membership function of parameterized soft set (for short, Np_soft set), respectively.

Let $\Omega_V, \bar{\Omega}_L \in Np_soft$ set.

Now: If $f_V(p) = K, T_V(p)=0, I_V(p)=0$ and $W_V(p)=1, \forall p \in E$, then Ω_V is called a V_empty Np_soft set (for short Ω_{\emptyset_V}). If $V = \emptyset$, then the V_empty Np_soft set is called an empty Np_soft set (for short Ω_{\emptyset}). If $f_V(p) = K, T_V(p)=1, I_V(p)=0$ and $W_V(p)=0, \forall p \in E$, then, Ω_V is called a $V_universal$ Np_soft set (for short $\Omega_{\bar{V}}$), if $V = E$, then the $V_universal$ Np_soft set is called an $V_universal$ Np_soft set (for short $\Omega_{\bar{E}}$).

$$\Omega_V \subseteq \bar{\Omega}_L \Leftrightarrow T_V(p) \leq T_L(p), I_V(p) \geq I_L(p), W_V(p) \geq W_L(p), f_V(p) \subseteq f_L(p), p \in E.$$

$$\Omega_V \sqcup \bar{\Omega}_L = \{ \langle p, \max\{T_V(p), T_L(p)\}, \min\{I_V(p), I_L(p)\}, \min\{W_V(p), W_L(p)\}, f_V(p) \cup f_L(p) \rangle, p \in E \}.$$

$$\Omega_V \cap \cup_L = \{ \langle p, \min \{T_V(p), T_L(p)\}, \max \{I_V(p), I_L(p)\}, \max \{W_V(p), W_L(p)\}, f_V(p) \cap f_L(p) \rangle, p \in E \} .$$

The complement of Ω_V is defined as :

$$\Omega_V^c = \{ \langle p, W_V(p), I_V(p), L_V(p), f_{Vc}(p) \rangle, p \in E \}, \text{ where, } f_{Vc}(p) = K - f_V(p) .$$

3. Third family (New family)

In this section, we will study and discuss the neutrosophic soft set theory giving new definitions, example, new family of neutrosophic soft sets, new operations for neutrosophic soft sets and comparison between the new family and first family .

3.1. Definition

A neutrosophic soft set F_D on the universe K is denoted by the set of ordered pairs

$$F_D = \{ (p, f_D(p)), p \in E_K, \} .$$

It can be written as: $F_D = \{ (p, \{ \langle q^{(T_{f_D(p)}(q)), I_{f_D(p)}(q)), V_{f_D(p)}(q) \rangle \}, p \in E_K \} .$

Where,

f_D is a mapping such that

$$f_D : \begin{cases} D \rightarrow P(K) \\ D^c \rightarrow \langle q^{(0,0,1)} \rangle, q \in K . \end{cases}$$

E_K is the set of all possible paramerers under consideration with respect to $K, D \subseteq E_K .$

$P(K)$ is the set of all the neutrosophic sets over $K .$

Form now on , the set of all the neutrosophic sets over K with respect to this family (Third family) will be denoted by $N_3(K) .$

3.2. Example

Let $K = \{q_1, q_2, q_3, q_4\}$ and $D \subseteq E_K = \{p_1, p_2, p_3, p_4\}$, such that $D = \{p_1, p_2\} .$

Suppose that :

$$f_{1D}(p_1) = \{ \langle q_1^{(0,6',0,3',0,7)}, q_2^{(0,5',0,4',0,5)}, q_3^{(0,7',0,4',0,3)}, q_4^{(0,8',0,4',0,3)} \rangle \} .$$

$$f_{1D}(p_2) = \{ \langle q_1^{(0,7',0,3',0,5)}, q_2^{(0,6',0,7',0,3)}, q_3^{(0,7',0,3',0,5)}, q_4^{(0,6',0,3',0,6)} \rangle \} .$$

$$f_{2D}(p_1) = \{ \langle q_1^{(0,6',0,4',0,5)}, q_2^{(0,6',0,5',0,4)}, q_3^{(0,7',0,4',0,5)}, q_4^{(0,7',0,5',0,6)} \rangle \} .$$

$$f_{2D}(p_2) = \{ \langle q_1^{(0,7',0,6',0,6)}, q_2^{(0,8',0,4',0,5)}, q_3^{(0,7',0,4',0,6)}, q_4^{(0,6',0,3',0,5)} \rangle \} .$$

Then, we can view the neutrosophic soft sets F_{1D}, F_{2D} as :

$$F_{1D} = \left\{ \begin{aligned} & (p_1, \{ \langle q_1^{(0,6',0,3',0,7)}, q_2^{(0,5',0,4',0,5)}, q_3^{(0,7',0,4',0,3)}, q_4^{(0,8',0,4',0,3)} \rangle \}) \\ & (p_2, \{ \langle q_1^{(0,7',0,3',0,5)}, q_2^{(0,6',0,7',0,3)}, q_3^{(0,7',0,3',0,5)}, q_4^{(0,6',0,3',0,6)} \rangle \}) \end{aligned} \right\}$$

$$F_{2D} = \left\{ \begin{aligned} & (p_1, \{ \langle q_1^{(0,6',0,4',0,5)}, q_2^{(0,6',0,5',0,4)}, q_3^{(0,7',0,4',0,5)}, q_4^{(0,7',0,5',0,6)} \rangle \}) \\ & (p_2, \{ \langle q_1^{(0,7',0,6',0,6)}, q_2^{(0,8',0,4',0,5)}, q_3^{(0,7',0,4',0,6)}, q_4^{(0,6',0,3',0,5)} \rangle \}) \end{aligned} \right\}$$

Note that, if $f_D(p) = \langle q^{(0'0'1)} \rangle$, for all $p \in E, q \in K$, the element $(p, f_D(p))$ is not appeared in neutrosophic soft set F_D .

3.3. Definition

The neutrosophic soft complement F_D^c of F_D is defined by the mapping $f_{D^c}(p) = f_D^c(p)$, where $f_D^c(p)$ is the complement of the set $f_D(p)$.

That is :

$$F_D^c = \{(p, \{ \langle q^{(1-T_{f_D(p)(q)})' (1-I_{f_D(p)(q)})' (1-V_{f_D(p)(q)}) \rangle \}), p \in E_K\}.$$

3.4. Definition

Let $F_D \in N_3(K)$, if $f_D(p) = \langle q^{(0'0'1)} \rangle, \forall p \in E_K, q \in K$, then F_D is called the null neutrosophic soft set and denoted by $\tilde{\emptyset}_D$.

3.5. Definition

Let $F_D \in N_3(K)$ if $f_D(p) = \langle q^{(1'1'0)} \rangle, \forall p \in D, q \in K$, then F_D is called the absolute neutrosophic soft set and denoted by \tilde{K}_D .

3.6. Definition

Let $F_{1D} \in N_3(K)$, then F_{1D} is called a neutrosophic soft subset of F_{2D} and denoted by $F_{1D} \sqsubseteq F_{2D}$ if $f_{1D}(p) \sqsubseteq f_{2D}(p), \forall p \in E_K$.

3.7. Definition

Let $F_{1D}, F_{2D} \in N_3(K)$, then, the neutrosophic soft intersection $(F_{1D} \sqcap F_{2D})$ and the neutrosophic soft union $(F_{1D} \sqcup F_{2D})$ are defined by the mappings .

$$f_{1D}(p) \sqcap f_{2D}(p)$$

$$f_{1D}(p) \sqcup f_{2D}(p)$$

3.8. Example

Let us consider neutrosophic soft sets F_{1D}, F_{2D} in example .
Then ,

$$1) F_{1D} \sqcup F_{2D} = \left\{ \left(p_1, \{ \langle q_1^{(0,6'0,4'0,5)}, q_2^{(0,6'0,5'0,4)}, q_3^{(0,7'0,4'0,3)}, q_4^{(0,8'0,5'0,3)} \rangle \} \right), \left(p_2, \{ \langle q_1^{(0,7'0,6'0,5)}, q_2^{(0,8'0,7'0,3)}, q_3^{(0,7'0,4'0,5)}, q_4^{(0,6'0,3'0,5)} \rangle \} \right) \right\}$$

$$2) F_{1D} \sqcap F_{2D} = \left\{ \left(p_1, \{ \langle q_1^{(0,6'0,3'0,7)}, q_2^{(0,5'0,4'0,5)}, q_3^{(0,7'0,4'0,5)}, q_4^{(0,7'0,4'0,6)} \rangle \} \right), \left(p_2, \{ \langle q_1^{(0,7'0,3'0,5)}, q_2^{(0,6'0,5'0,4)}, q_3^{(0,7'0,3'0,6)}, q_4^{(0,6'0,3'0,6)} \rangle \} \right) \right\}$$

$$3) \quad (F_{2D})^c = \left\{ \begin{array}{l} (p_1, \{< q_1^{(0,4' 0,6' 0,5)}, q_2^{(0,4' 0,5' 0,6)}, q_3^{(0,3' 0,6' 0,5)}, q_4^{(0,3' 0,5' 0,4)} >\}) \\ (p_2, \{< q_1^{(0,3' 0,4' 0,4)}, q_2^{(0,2' 0,6' 0,5)}, q_3^{(0,3' 0,6' 0,4)}, q_4^{(0,4' 0,7' 0,5)} >\}) \\ (p_3, \{< q_1^{(1' 1' 0)}, q_2^{(1' 1' 0)}, q_3^{(1' 1' 0)}, q_4^{(1' 1' 0)} >\}) \\ (p_4, \{< q_1^{(1' 1' 0)}, q_2^{(1' 1' 0)}, q_3^{(1' 1' 0)}, q_4^{(1' 1' 0)} >\}) \end{array} \right\}$$

3.9. Proposition

Let $F_{1D} \in N_3(K)$, then :

- $F_{1D} \sqcup F_{1D} = F_{1D}$.
- $F_{1D} \cap F_{1D} = F_{1D}$.
- $F_{1D} \sqcup \tilde{\emptyset}_D = F_{1D}$.
- $F_{1D} \sqsubseteq F_{1D}$.
- $\tilde{\emptyset}_D \sqsubseteq F_{1D}$.
- $F_{1D} \sqsubseteq \tilde{K}_D$.
- $F_{1D} \cap \tilde{\emptyset}_D = \tilde{\emptyset}_D$.
- $F_{1D} \sqcup \tilde{K}_D = \tilde{K}_D$.
- $F_{1D} \cap \tilde{K}_D = F_{1D}$.

Proof : The proof of the remark is direct from the definition

3.10. Proposition

Let $F_{1D} \in N_3(K)$, then :

- $(\tilde{\emptyset}_D)^c = \tilde{K}_D$
- $(\tilde{K}_D)^c = \tilde{\emptyset}_D$
- $((F_{1D})^c)^c = F_{1D}$

Proof : Straightforward .

3.11. Proposition

Let F_{1D}, F_{2D} and $F_{3D} \in N_3(K)$, then :

- $F_{1D} \sqcup F_{2D} = F_{2D} \sqcup F_{1D}$.
- $F_{1D} \cap F_{2D} = F_{2D} \cap F_{1D}$.
- $(F_{1D} \sqcup F_{2D})^c = (F_{1D})^c \cap (F_{2D})^c$.
- $(F_{1D} \cap F_{2D})^c = (F_{1D})^c \sqcup (F_{2D})^c$.
- $(F_{1D} \cap F_{2D}) \sqcup F_{3D} = (F_{1D} \sqcup F_{3D}) \cap (F_{2D} \sqcup F_{3D})$.
- $(F_{1D} \sqcup F_{2D}) \cap F_{3D} = (F_{1D} \cap F_{3D}) \sqcup (F_{2D} \cap F_{3D})$.

Proof : Straightforward .

Comparison

Next ,we will compare (new family) with the first family .

1- Dentition of neutrosophic soft sets

First family	Third family(new family)
$F_D = \{(p, f_D(p)), p \in D, D \subseteq E_k\}$ Where, $F : D \rightarrow P(K)$	$F_D = \{(p, f_D(p)), p \in E_K, D \subseteq E_k\}$ Where, $F : \begin{cases} D \rightarrow P(K) \\ D^c \rightarrow \langle q^{(0,0,1)} \rangle, q \in K \end{cases}$

2- Intersection of neutrosophic soft sets	
First family	Third family(new family)
$F_{1A} \cap F_{2B} = F_{3(A \cap B)}$ $F_3: (A \cap B) \rightarrow P(K)$ $F_3(p) = F_1(p) \text{ or } F_2(p)$	$F_{1D} \cap F_{2D} = F_{3D}$ $F_3 : \begin{cases} D \rightarrow P(K) \\ D^c \rightarrow \langle q^{(0,0,1)} \rangle, q \in K \end{cases}$ $F_3(p) = F_1(p) \cap F_2(p)$

3- Union of neutrosophic soft sets	
First family	Third family(new family)
$F_{1A} \cup F_{2B} = F_{3(A \cup B)}$ $F_3: (A \cup B) \rightarrow P(K)$ $F_3(p) = \begin{cases} F_{1A} & \text{if } p \in A \setminus B \\ F_{2B} & \text{if } p \in B \setminus A \\ F_1(p) \cup F_2(p), & \text{if } p \in A \cap B \end{cases}$	$F_{1D} \cup F_{2D} = F_{3D}$ $F_3 : \begin{cases} D \rightarrow P(K) \\ D^c \rightarrow \langle k^{(0,0,1)} \rangle, k \in K \end{cases}$ $F_3(p) = F_1(p) \cup F_2(p)$

4- Complement of neutrosophic soft sets	
First family	Third family(new family)

$(F_D)^c = F^c_{\neg D}$ Where $F^c: D \rightarrow P(K)$ " Where, $\neg k$ is not k and $\neg D = \{ \neg k : k \in D \}$	$(F_D)^c = F^c_D$ Where, $F^c : \left\{ \begin{array}{l} D \rightarrow P(K) \\ D^c \rightarrow \langle q^{(0,0,1)} \rangle, q \in K \end{array} \right.$.
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4. Neutrosophic Soft Topology

In this section, we will investigate the theory of neutrosophic soft topological spaces depending on the new family $(N_3(K))$ and we present new definitions, characterization and properties concerning the neutrosophic soft closure, the neutrosophic soft interior, the neutrosophic soft exterior, the neutrosophic soft boundary .

4.1. Definition

Let K be the initial universe E_K be set of parameters , $D \subseteq E_K$ and $\mu \subseteq N_3(K)$, we say that μ is a neutrosophic soft topology on K , if it satisfies the following conditions :

- 1) $\tilde{\emptyset}_D, \tilde{K}_D \in \mu$.
- 2) $F_{1D} \cap F_{2D} \in \mu, \forall F_{1D}, F_{2D} \in \mu$.
- 3) $\cup \{F_{iD}, i \in I\} \in \mu, \forall F_{iD} \in \mu$.

The pair (K, μ) (or simply K) is a neutrosophic soft topological spaces or $((N_3 - Top)$ for short) .

- ❖ The elements of μ are called a neutrosophic open the family sets .
- ❖ A neutrosophic soft F_{1D} is called a neutrosophic soft closed set,if its complement is a neutrosophic soft open set .

4.2. Proposition

Let (K, μ) be $(N_3 - Top)$, then the family of neutrosophic soft closed sets $(C(\tilde{K}_D)$ for short) has the following properties :

- 1) $\tilde{\emptyset}_D, \tilde{K}_D \in C(\tilde{K}_D)$.
- 2) $F_{1D} \cup F_{2D} \in \mu, \forall F_{1D}, F_{2D} \in C(\tilde{K}_D)$.
- 3) $\cap \{F_{iD}, i \in I\} \in C(\tilde{K}_D), \forall F_{iD} \in C(\tilde{K}_D)$.

Proof : Straightforward.

4.3. Example

Let $K = \{q_1, q_2\}$, $D \subseteq E_K$, such that $D = \{p_1\}$ and $F_{1D}, F_{2D} \in N_3(K)$, such that :

$$F_{1D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,5,0,1,0,4)}, q_2^{(0,4,0,3,0,8)} \rangle \right\} \right) \right\}.$$

$$F_{2D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,5',0,1',0,3)}, q_2^{(0,5',0,3',0,6)} \rangle \right\} \right) \right\}.$$

Then, $\mu = \{ \tilde{\varnothing}_D, \tilde{K}_D, F_{1D}, F_{2D} \}$ is a neutrosophic soft topology on K and (K, μ) is a neutrosophic soft topological space.

4.4. Proposition

Let (K, μ_1) and (K, μ_2) be two neutrosophic soft topological spaces on K , then $(K, \mu_1 \cap \mu_2)$ is a neutrosophic soft topological spaces on K .

Poof:

Let (K, μ_1) and (K, μ_2) be two neutrosophic soft topological spaces on K . It can be seen clearly that $\tilde{\varnothing}_D, \tilde{K}_D \in \mu_1 \cap \mu_2$. If $F_{1D}, F_{2D} \in \mu_1 \cap \mu_2$, then $F_{1D} \in \mu_1$ and $F_{1D}, F_{2D} \in \mu_2$. It is given that $F_{1D} \cap F_{2D} \in \mu_1, F_{1D} \cap F_{2D} \in \mu_2$. Thus $F_{1D} \cap F_{2D} \in \mu_1 \cap \mu_2$. Let $\{F_{iD}, i \in I\} \in \mu_1 \cap \mu_2$, then $F_{iD} \in \mu_1, \forall i \in I$ and $F_{iD} \in \mu_2, \forall i \in I$. Then $F_{iD} \in \mu_1 \cap \mu_2, \forall i \in I$. So, we have $\sqcup \{F_{iD}, i \in I\} \in \mu_1 \cap \mu_2$

4.5. Remark

Let (K, μ_1) and (K, μ_2) be two neutrosophic soft topological spaces on K , then $(K, \mu_1 \cup \mu_2)$ may not be correct. It can be seen from the following example.

4.6. Example

Let $K = \{q_1, q_2\}, D \subseteq E_K$, such that $D = \{p_1\}$ and $F_{1D}, F_{2D} \in N_3(K)$,

such that :

$$F_{1D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,2',0,4',0,6)}, q_2^{(0,1',0,3',0,5)} \rangle \right\} \right) \right\}.$$

$$F_{2D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,4',0,6',0,8)}, q_2^{(0,3',0,5',0,7)} \rangle \right\} \right) \right\}.$$

Then, $\mu_1 = \{ \tilde{\varnothing}_D, \tilde{K}_D, F_{1D} \}$ and $\mu_2 = \{ \tilde{\varnothing}_D, \tilde{K}_D, F_{2D} \}$ are two neutrosophic soft topology on K . But $\mu_1 \cup \mu_2 = \{ \tilde{\varnothing}_D, \tilde{K}_D, F_{1D}, F_{2D} \}$ is not neutrosophic soft topology on K .

4.7. Definition

Let $F_D \in N_3(K)$. The interior of F_D is union of all neutrosophic soft open sets contained in F_D , denoted by $\text{int}(F_D)$. That is

$$\text{int}(F_D) = \sqcup \{ F_{1D} : F_{1D} \text{ is neutrosophic soft open set, } F_{1D} \sqsubseteq (F_D) \}.$$

4.8. Definition

Let $F_D \in N_3(K)$. The interior of F_D is intersection of all neutrosophic soft closed sets containing in F_D , denoted by $\text{cl}(F_D)$. That is

$$\text{cl}(F_D) = \sqcap \{ F_{1D} : F_{1D} \text{ is neutrosophic soft closed set, } F_{1D} \supseteq (F_D) \}.$$

4.9. Proposition

Let (K, μ) be $(N_3 - \text{Top})$, $F_D \in N_3(K)$. Then :

- 1) F_D is a neutrosophic soft open (closed) set if and only if $F_D = \text{int}(F_D)$ ($F_D = \text{cl}(F_D)$).
- 2) $\text{cl}((F_D)^c) = (\text{int}(F_D))^c$.
- 3) $\text{int}((F_D)^c) = (\text{cl}(F_D))^c$.

4.10. Proposition

Let $F_{1D}, F_{2D} \in N_3(K)$, Then :

1. $\text{int}(F_{1D}) \subseteq F_{1D}$.
2. $\text{int}(\text{int}(F_{1D})) = \text{int}(F_{1D})$.
3. $\text{int}(F_{1D}) \subseteq \text{int}(F_{2D})$, whenever $F_{1D} \subseteq F_{2D}$.
4. $\text{int}(F_{1D} \cap F_{2D}) = \text{int}(F_{1D}) \cap \text{int}(F_{2D})$.
5. $\text{int}(F_{1D} \cup F_{2D}) \supseteq \text{int}(F_{1D}) \cup \text{int}(F_{2D})$.
6. $F_{1D} \subseteq \text{cl}(F_{1D})$.
7. $\text{cl}(\text{cl}(F_{1D})) = \text{cl}(F_{1D})$.
8. $\text{cl}(F_{1D}) \subseteq \text{cl}(F_{2D})$, whenever $F_{1D} \subseteq F_{2D}$.
9. $\text{cl}(F_{1D} \cap F_{2D}) \subseteq \text{cl}(F_{1D}) \cap \text{cl}(F_{2D})$.
10. $\text{cl}(F_{1D} \cup F_{2D}) = \text{cl}(F_{1D}) \cup \text{cl}(F_{2D})$.

4.11. Remark

The converse of (property (1,3,6,9)) in above theorem is not true in general. It can be seen from the following examples.

4.12. Example

Let $K = \{q_1, q_2\}$, $D \subseteq E_K$, such that $D = \{p_1\}$ and $F_{1D}, F_{2D} \in N_3(K)$,
such that :

$$F_{1D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,5',0,5',0,5)}, q_2^{(0,4',0,4',0,4)} \rangle \right\} \right) \right\}$$

$$F_{2D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,6',0,6',0,6)}, q_2^{(0,3',0,3',0,3)} \rangle \right\} \right) \right\}$$

$$F_{3D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,5',0,5',0,6)}, q_2^{(0,3',0,3',0,4)} \rangle \right\} \right) \right\}$$

$$F_{4D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,6',0,6',0,5)}, q_2^{(0,4',0,4',0,3)} \rangle \right\} \right) \right\}$$

Then , $\mu = \{ \tilde{\emptyset}_D, \tilde{K}_D, F_{1D}, F_{2D}, F_{3D}, F_{4D} \}$ is a neutrosophic soft topology on K .

Note that :

- 1) $\text{int}(F_{1D} \cup F_{2D}) \not\subseteq \text{int}(F_{1D}) \cup \text{int}(F_{2D})$.
- 2) $F_{1D} \not\subseteq \text{int}(F_{1D})$

4.13. Example

Let $K = \{q_1, q_2\}$, $D \subseteq E_K$, such that $D = \{p_1\}$ and $F_{1D}, F_{2D} \in N_3(K)$,
such that :

$$F_{1D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,1',0,1',0,9)}, q_2^{(0,2',0,2',0,8)} \rangle \right\} \right) \right\}$$

$$F_{2D} = \left\{ \left(p_1, \left\{ \langle q_1^{(0,9',0,9',0,1)}, q_2^{(0,8',0,8',0,2)} \rangle \right\} \right) \right\}$$

Then , $\mu = \{ \tilde{\emptyset}_D, \tilde{K}_D, F_{1D}, F_{2D} \}$ is a neutrosophic soft topology on K .

Note that :

- 1) $\text{cl}(F_{1D}) \cup \text{cl}(F_{2D}) \not\subseteq \text{cl}(F_{1D} \cup F_{2D})$.

$$2) \quad \text{cl}(F_{1D}) \not\subseteq F_{1D} .$$

4.14. Definition

Let $F_D \in N_3(K)$. The neutrosophic soft exterior of F_D is denoted by $\text{ext}(F_D)$ and is defined as:
 $\text{ext}(F_D) = \text{int}((F_D)^c)$.

4.15. Definition

Let $F_D \in N_3(K)$. The neutrosophic soft boundary of F_D is denoted by $\text{br}(F_D)$ and is defined as:
 $\text{br}(F_D) = \text{cl}((F_D)^c) \cap (\text{cl}(F_D))$. It must be notion that $\text{br}(F_D) = \text{br}((F_D)^c)$.

4.16. Proposition

Let (K, μ) be $(N_3 - \text{Top})$, $F_D \in N_3(K)$. Then :

- 1) $\text{br}((F_D)^c) = \text{ext}(F_D) \sqcup \text{int}(F_D)$.
- 2) $\text{cl}(F_D) = \text{br}(F_D) \sqcup \text{int}(F_D)$.
- 3) $\text{br}(F_D) \cap \text{int}(F_D) = \tilde{\emptyset}_D$.
- 4) $\text{br}(\text{int}(F_D)) \subseteq \text{br}(F_D)$.

Proof : Straightforward .

4.17. Proposition

Let (K, μ) be $(N_3 - \text{Top})$, $F_D \in N_3(K)$. Then :

- 1) F_D is a neutrosophic soft open set $\leftrightarrow \text{br}(F_D) \cap (F_D) = \tilde{\emptyset}_D$.
- 2) F_D is a neutrosophic soft closed set $\leftrightarrow \text{br}(F_D) \subseteq (F_D)$.

Proof : Straightforward .

Conclusion

-The neutrosophic soft set theory is studied and discussed by introducing, new family of neutrosophic soft sets, new operations for neutrosophic soft set .

-The neutrosophic soft set theory is studied and discussed by introducing, new family of neutrosophic soft sets [namely third family], new operations for neutrosophic soft sets, comparison between the new family and other families, new definitions and examples.

- New definitions, characterization, the neutrosophic soft closure, the neutrosophic soft interior, the neutrosophic soft exterior and the neutrosophic soft boundary are introduced in details .

-We expect this research will promote the future study on theory of neutrosophic soft sets, the theory of neutrosophic soft topological spaces and many other general frameworks .

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Received: June 10, 2020. Accepted: Nov 23, 2020