

Robust non-linear control of a hybrid water pumping system based on induction motor

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ABSTRACT

This contribution presents a non-linear control of a hybrid pumping system supplied with a photovoltaic generator and a battery. This system is employed for delivering a continuous volume of water whatever the climatic conditions. In the DC side, a boost converter is controlled with the indirect double integral sliding mode controller (DISMC) for maximum power point tracking (MPPT). The DISMC is suitable for MPPT because it gives a fast response and reduces the amplitude of power oscillations. Then, a bidirectional buck-boost converter is adopted to ensure the energy management between the battery and the DC-bus, and this converter is controlled with integral sliding mode control (ISMC) theory. The non-linear predictive control (NPC) is chosen to drive an induction motor (IM), the NPC is known by its fast dynamic and high capacity to reject disturbances. The hybrid system is modelled in MATLAB/Simulink software. During simulations, the DISMC-MPPT is compared with other techniques such as sliding mode controller (SMC) MPPT and integral SMC MPPT, the DISMC provides the best tracking performances under different irradiances. Moreover, the designed controller for the bidirectional converter regulates the DC-link voltage with better performances than the classical PI controller. Lastly, the NPC regulates the speed of the IM with high robustness.

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1. INTRODUCTION

The sliding mode control (SMC) is suitable for fast maximum power point tracking (MPPT) because it is known by stability, fast-response and non-sensitivity to parameter variation [1]. The conventional hysteresis-modulation (HM) based SMC suffers from variable switching frequency and from the chattering phenomenon due to the high switching frequency operation. These drawbacks motivated the researchers to design an indirect SMC based on the pulse width modulation (PWM) technique. The conventional SMC with PWM exhibits an unwanted steady-state error and slow response [2], to improve the response of indirect SMC an integral term is added to the existing sliding surface to constitute the integral sliding mode controller (ISMC) [3, 4]. However, the construction of the indirect form of the ISMC derivates the state variables of the switching surface ($\dot{S}=0$), thus, the variable $\int x_i dt$ disappears from the equivalent control term u_{eq} , and the correction of steady-state error is deteriorated [5, 6]. Therefore, an integral term is added for the second time $\int(\int x_i dt)dt$ to nullify the steady-state error introduced by the indirect ISMC, this new technique is called

PWM based double integral SMC (DISMC) [2]. The DISMC shows a fast response and reduces the steady-state error [4]. The bidirectional (BDC) DC-DC converter is the key factor of energy management between PV source, battery, and different loads [7, 8]. However, the use of two PI controllers to control the bidirectional converter does not guarantee good performances when the system operates outside of the operating point [9, 10]. For that reason, the features of the ISMC theory are exploited to control the bidirectional converter in this paper.

The discovering of field-oriented control (FOC) in 1972 has revolutionized the control theory of the induction motor (IM) [11-13]. However, the FOC technique uses coordinate transformation which makes it complex to implement, in addition, it is sensitive to internal parameters variation of the machine [14, 15]. To minimize the complexity of FOC and improving its dynamic new control techniques have been founded, namely sliding mode control (SMC), and direct torque control (DTC) [16, 17]. The IM model is non-linear in nature, furthermore, the IM is applied to external disturbances (load torque) and to internal parameter variations. Therefore, the robust non-linear predictive control (NPC) is applied to control the IM in this work. The NPC uses high order calculations to optimize a cost function; the complexity of calculation could be reduced using the Taylor series expansion of the output's variables [18, 19].

This contribution proposes a high-performance control scheme for a hybrid water pumping system. Section 2 presents a brief description of the different stages of the pumping system. Section 3 presents the different control strategies for the pumping system. First, a cascaded controller based on DISMC is presented for MPPT. Afterward, two other controllers based on ISMC theory are designed to control the bidirectional flow of the energy. Finally, the control scheme for the IM based on NPC is explained. Simulation results and analysis are reported to section 4, followed by general conclusions.

2. CIRCUIT CONFIGURATION

A hybrid water pumping system is presented in Figure 1. The overall system comprises a PV array as a principal source of energy and a battery pack considered as a second power source. The system includes static DC-DC converters such as a unidirectional boost converter used for MPPT and a bidirectional buck-boost converter which ensures the bidirectional flow of the energy between the DC-bus and the battery. Finally, a two-level inverter controls an induction motor with a centrifugal pump.

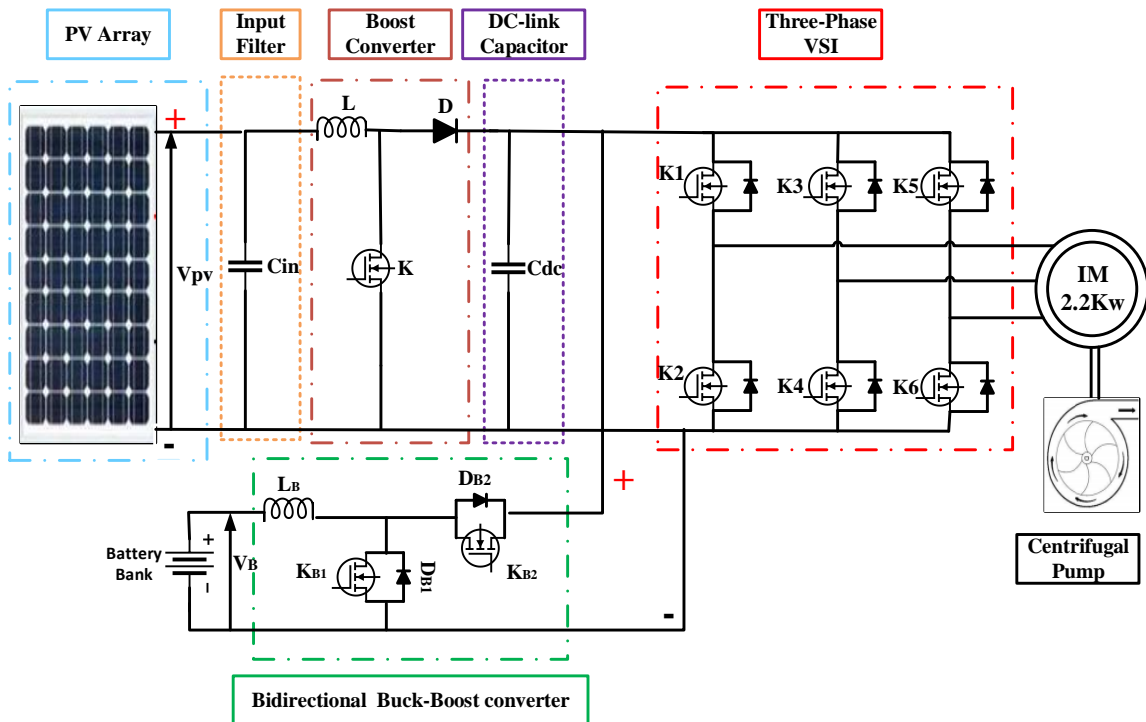


Figure 1. Block diagram of the hybrid system

3. CONTROL STRATEGIES

Diverse controllers are proposed to control the hybrid system, and are listed as follows:

- A DISMC based on PWM is designed to track the maximum power point (MPP) with high efficiency.
- The bidirectional buck-boost converter is controlled with the ISMC theory to regulate the DC-bus voltage.
- Control of the induction motor with the generalized predictive controller.

3.1. Maximum power point tracking control

Figure 2 shows the MPPT control scheme, in which a perturb and observe (P&O) algorithm generates the reference voltage V_{pv}^* . Then, a DISMC is used to force the state trajectory of the boost converter to follow the reference voltage given by the P&O algorithm.

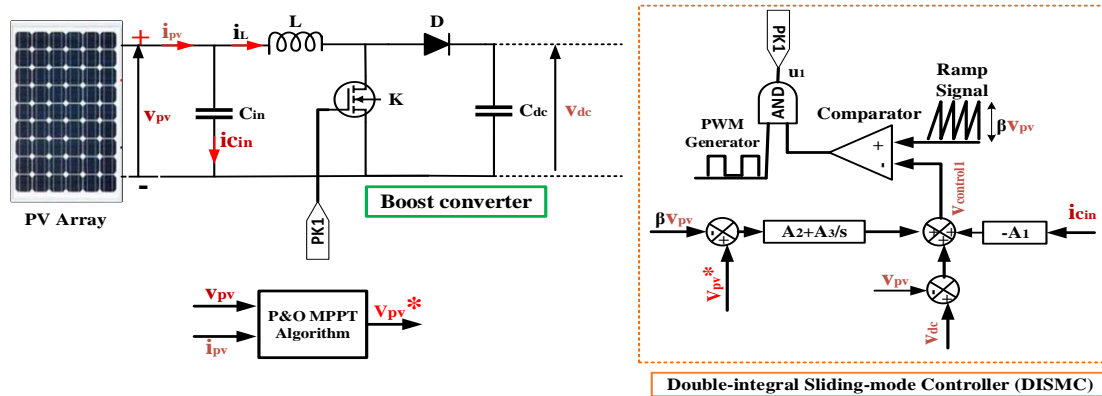


Figure 2. DISMC- MPPT algorithm control scheme

3.1.1. Design of a double integral sliding mode controller for MPPT

Considering that the boost converter operates in continuous conduction mode (CCM), The average state-space model of the boost converter is presented in term of the switching signal u_1 as,

$$\dot{x}_1 = f(x_1) + g(x_1)u_1 \tag{1}$$

$$\text{Where, } x_1 = [i_L \ v_{pv}]^T, \ f(x_1) = \begin{bmatrix} \frac{v_{pv} - v_{dc}}{L} & \frac{v_{pv}}{r_{pv} C_{in}} - \frac{i_L}{C_{in}} \end{bmatrix}^T \text{ and } g(x_1) = \begin{bmatrix} \frac{v_{dc}}{L} & 0 \end{bmatrix}^T$$

Where, r_{pv} is the dynamic resistance of the PV array. The general control law to control the voltage v_{pv} is:

$$u_1 = \begin{cases} 0 & \text{when } S_1 > 0 \\ 1 & \text{when } S_1 < 0 \end{cases} \tag{2}$$

Where S_1 is the switching surface, which is expressed as,

$$S_1 = a_1 e_1 + a_2 e_2 + a_3 e_3 + a_4 e_4 \tag{3}$$

The terms a_1 - a_4 denote the sliding surface parameters, and e_1 - e_4 are the error signals.

$$\begin{cases} e_1 = i_L^* - i_L & / & i_L^* = A(V_{pv}^* - \beta v_{pv}) \\ e_2 = V_{pv}^* - \beta v_{pv} \\ e_3 = \int (V_{pv}^* - \beta v_{pv}) dt \\ e_4 = \int \left[\int (V_{pv}^* - \beta v_{pv}) dt \right] dt \end{cases} \tag{4}$$

Where, A is the amplified gain of the voltage error. The application of the indirect SMC is achieved through the computation of the equivalent control u_{1eq} . This can be derived from the invariance condition, $\dot{S}_1=0$,

$$\dot{S}_1 = a_1 \dot{e}_1 + a_2 \dot{e}_2 + a_3 \dot{e}_3 + a_4 \dot{e}_4 = 0 \tag{5}$$

$$\text{Then, } u_{1eq} = 1 - A_1 \frac{i_{c_{in}}}{v_{dc}} - \frac{v_{pv}}{v_{dc}} + A_2 \frac{e_2}{v_{dc}} + A_3 \frac{e_3}{v_{dc}} \tag{6}$$

$$\text{With, } A_1 = \left(\frac{A\beta L}{C_{in}} + \frac{a_2\beta L}{a_1 C_{in}} \right), A_2 = \frac{a_3 L}{a_1} \text{ and } A_3 = \frac{a_4 L}{a_1}$$

$A_1, A_2,$ and A_3 parameters are empirically determined according to the existence and stability criterions [2, 4]. The control law of the indirect sliding mode control is derived using PWM technique, comparing control signal $v_{control1}$ with a ramp signal v_{ramp1} .

$$\begin{cases} v_{control1} = (v_{dc} - v_{pv}) - A_1 i_{c_{in}} + A_2 e_2 + A_3 e_3 \\ v_{ramp1} = \beta v_{pv} \end{cases} \tag{7}$$

3.2. The control strategy of the bidirectional converter

The BDC is considered as the intermediate link between the battery and the DC bus. If the DC-link voltage is greater than the reference voltage $v_{dc} > V_{dc}^*$, the BDC operates in buck mode to store the excess of energy in the battery. On the other hand, if $v_{dc} < V_{dc}^*$ the battery discharges to inject the required current into the DC-bus, in this case, the BDC works in boost mode [20, 21]. The direction of the current is reversed from one mode to another. To control the BDC in both modes of operation two strategies of control are proposed as presented in Figure 3.

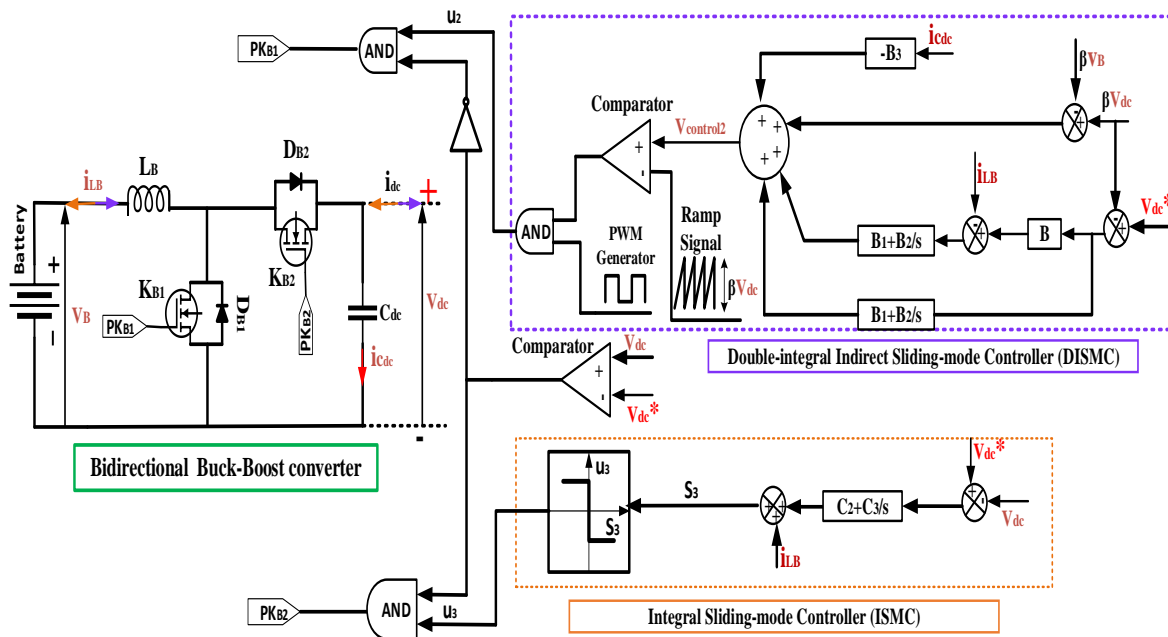


Figure 3. The proposed control scheme for the bidirectional converter

3.2.1. Design of a double integral sliding mode controller for the boost converter mode

Considering that the boost converter operates in CCM, and the chosen state variables are the inductor current i_{LB} and the DC-link voltage v_{dc} . The dynamic of the boost converter is described with the differential equations in (8), where u_2 refers to the state of the switch K_{B1} .

$$\dot{x}_2 = f(x_2) + g(x_2)u_2 \quad (8)$$

$$\text{Where, } x_2 = [i_{LB} \ v_{dc}]^T, \ f(x_2) = \begin{bmatrix} \frac{v_B - v_{dc}}{L} & \frac{i_{LB}}{C_{dc}} - \frac{v_{dc}}{r_{dc} C_{dc}} \end{bmatrix}^T \text{ and } g(x_2) = \begin{bmatrix} \frac{v_{dc}}{L} & \frac{-i_{LB}}{C_{dc}} \end{bmatrix}^T$$

r_{dc} is the dynamic resistance of the DC bus.

The sliding surface is formed with the state variables errors (9).

$$S_2 = b_1 e_1 + b_2 e_2 + b_3 e_3 + b_4 e_4 \quad (9)$$

where e_1 - e_4 are the current and voltage errors, and B is the gain which amplifies the voltage error.

$$\begin{cases} e_1 = i_{LB}^* - i_{LB} & / \ i_{LB}^* = B(V_{dc}^* - \beta v_{dc}) \\ e_2 = V_{dc}^* - \beta v_{dc} \\ e_3 = \int (e_1 + e_2) dt \\ e_4 = \int \left[\int (e_1 + e_2) dt \right] dt \end{cases} \quad (10)$$

Substituting the dynamic of the step-up converter in the derivative of the sliding surface ($\dot{S}_2=0$) gives,

$$\dot{S}_2 = b_1 \left(\frac{v_{dc} - v_B - u_2 v_{dc}}{L_B} - B\beta \frac{ic_{dc}}{C_{dc}} \right) - b_2 \beta \frac{ic_{dc}}{C_{dc}} + b_3 (e_1 + e_2) + b_4 \int (e_1 + e_2) dt \quad (11)$$

The equivalent control signal u_{2eq} of the boost converter is obtained by solving the following equation $\dot{S}_2=0$,

$$u_{eq2} = 1 - \frac{\beta L_B}{C_{dc} v_{dc}} (B + \frac{b_2}{b_1}) ic_{dc} - \frac{v_B}{v_{dc}} + \frac{b_3 L_B}{b_1 v_{dc}} (V_{dc}^* - \beta v_{dc}) + \frac{b_3 L_B}{b_1 v_{dc}} [B(V_{dc}^* - \beta v_{dc}) - i_{LB}] + \frac{b_4 L_B}{b_1 v_{dc}} \int (V_{dc}^* - \beta v_{dc}) dt + \frac{b_4 L_B}{b_1 v_{dc}} \int [B(V_{dc}^* - \beta v_{dc}) - i_{LB}] dt \quad (12)$$

The control law is derived using the PWM technique, comparing the voltage control signal $v_{control2}$ with a ramp signal v_{ramp2} .

$$\begin{cases} v_{control2} = B_1 (V_{dc}^* - \beta v_{dc}) + B_1 [B(V_{dc}^* - \beta v_{dc}) - i_{LB}] + B_2 \int (V_{dc}^* - \beta v_{dc}) dt + B_2 \int [B(V_{dc}^* - \beta v_{dc}) - i_{LB}] dt - B_3 ic_{dc} + G_s (v_{dc} - v_B) \\ v_{ramp2} = G_s v_{dc} \end{cases} \quad (13)$$

Here, the factor $G_s = \beta$ ($0 < G_s < 1$) is used to downscale voltage magnitude to a practical level. B_1 - B_3 are constant parameters determined according to reachability and stability conditions [5, 22]. The duty ratio is multiplied with a signal of the pulse generator to ensure that the duty ratio is always less than 1. Figure 3 illustrates the control scheme of the implemented DISMC-PWM.

$$B_1 = G_s \frac{b_3}{b_1} L_B, \ B_2 = G_s \frac{b_4}{b_1} L_B \text{ and } B_3 = G_s \frac{\beta L_B}{C_{dc}} (B + \frac{b_2}{b_1})$$

3.2.2. Design of Integral sliding mode controller for the buck converter mode

Considering that the buck converter operates in CCM, and the chosen state variables are the inductor current I_{LB} and the DC-link voltage V_{dc} . The dynamic of the buck converter is described with the differential equations (14), where u_3 refers to the state of the switch K_{B2} .

$$\dot{x}_3 = f(x_3) + g(x_3)u_3 \quad (14)$$

where, $x_3 = [i_{LB} \ v_{dc}]^T$, $f(x_3) = \begin{bmatrix} -v_B & i_{dc} \\ L_B & C_{dc} \end{bmatrix}^T$ and $g(x_3) = \begin{bmatrix} v_{dc} & -i_{LB} \\ L_B & C_{dc} \end{bmatrix}^T$

the switching surface S_3 is formed with the DC-link voltage error (e_1), the integration of this error (e_2) and the inductor current i_{LB} . The sliding surface S_3 is expressed in (15),

$$S_3 = c_1 e_1 + c_2 e_2 + i_{LB} \tag{15}$$

where, c_1 and c_2 are the sliding surface parameters determined according to reachability condition [9, 25], the errors are given by,

$$\begin{cases} e_1 = V_{dc}^* - v_{dc} \\ e_2 = \int (V_{dc}^* - v_{dc}) dt \end{cases} \tag{16}$$

the control discrete function of the buck converter is concluded from the transversality condition [25].

$$u_3 = \begin{cases} 1 & \text{when } S_3 < 0 \\ 0 & \text{when } S_3 > 0 \end{cases} \tag{17}$$

the derivative of the switching surface is given in equation (18),

$$\dot{S}_3 = -c_1 \left(\frac{i_{dc}}{C_{dc}} - \frac{u_3 i_{LB}}{C_{dc}} \right) + c_2 e_1 + \left(\frac{u_3 v_{dc}}{L_B} - \frac{v_B}{L_B} \right) \tag{18}$$

solving the equation ($\dot{S}_3=0$), the control signal would be:

$$u_{3eq} = \frac{\frac{c_1 i_{dc}}{C_{dc}} + \frac{v_B}{L_B} - c_2 (V_{dc}^* - v_{dc})}{\frac{c_1 i_{LB}}{C_{dc}} + \frac{v_{dc}}{L_B}} \tag{19}$$

3.3. Non-linear predictive control of induction motor

Figure 4 presents the non-linear predictive control of the induction motor. The mathematical model of the IM is presented in the two-dimensional stator reference frame (α - β) [26] is:

$$\dot{x} = f(x) + g(x)u(t) \tag{20}$$

where, $x = [i_{s\alpha} \ i_{s\beta} \ \phi_{r\alpha} \ \phi_{r\beta} \ \omega_m]^T$, $u(t) = [u_{s\alpha} \ u_{s\beta}]^T$,

$$f(x) = \begin{pmatrix} -\gamma i_{s\alpha} + \frac{K}{T_r} \phi_{r\alpha} + pK \omega_m \phi_{r\beta} \\ -\gamma i_{s\beta} + \frac{K}{T_r} \phi_{r\beta} - pK \omega_m \phi_{r\alpha} \\ \frac{L_m}{T_r} i_{s\alpha} - \frac{1}{T_r} \phi_{r\alpha} - p\omega_m \phi_{r\beta} \\ \frac{L_m}{T_r} i_{s\beta} - \frac{1}{T_r} \phi_{r\beta} + p\omega_m \phi_{r\alpha} \\ \frac{pL_m}{JL_r} (\phi_{r\alpha} i_{s\beta} - \phi_{r\beta} i_{s\alpha}) - \frac{f_r}{J} \omega_m - \frac{T_l}{J} \end{pmatrix} \text{ and } g = [g_{11} \ g_{12}] = \begin{pmatrix} \frac{1}{\sigma L_s} & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{\sigma L_s} & 0 & 0 & 0 \end{pmatrix}^T$$

where, $u_{sa}, u_{sb}, i_{sa}, i_{sb}$ are the stator voltages and the stator currents, respectively, and ϕ_{ra}, ϕ_{rb} are rotor fluxes. The constant parameters of the model are defined by,

$$\sigma = 1 - \left(\frac{L_m^2}{L_s L_r} \right); K = \frac{L_m}{\sigma L_s L_r}; \gamma = \frac{1}{\sigma L_s} (R_s + R_r \frac{L_m^2}{L_r^2})$$

where, L_s, L_r are stator and rotor inductances, and L_m is the mutual inductance, R_s, R_r are stator and rotor resistances, and $T_r = L_r/R_r$ is rotor time constant, p number of poles pair, T_l load torque, J inertia coefficient, f_r friction coefficient. The square of rotor flux and the speed are two chosen output to be regulated,

$$y = h(x) = (y_1 \ y_2)^T = (h_1(x) \ h_2(x))^T = (\omega_m \ \phi_r^2 = \phi_{ra}^2 + \phi_{rb}^2)^T \tag{21}$$

the controlled variables can be expressed with Lie derivatives as,

$$Y(t) = \begin{pmatrix} y(t) \\ \dot{y}(t) \\ \ddot{y}(t) \end{pmatrix} = \begin{pmatrix} h(x) \\ L_f h(x) \\ L_f^2 h(x) \end{pmatrix} + \begin{pmatrix} 0_{2 \times 1} \\ 0_{2 \times 1} \\ G_1(x)u(t) \end{pmatrix} \tag{22}$$

where, $G_1(x) = \begin{pmatrix} L_{g_{11}} L_f h_1(x) & L_{g_{12}} L_f h_1(x) \\ L_{g_{21}} L_f h_2(x) & L_{g_{22}} L_f h_2(x) \end{pmatrix}$, $L_f^i h(x) = [L_f^i h_1(x) \ L_f^i h_2(x)]^T$, $0 \leq i \leq 2$

where, $L_f h_j(x)$ operator is Lie derivative notation of the function h_j with the respect to $f(x)$.

The basic idea behind the predictive control consists of the construction of a control law $u(t)$ able to force the system trajectory to follow the desired trajectory in a future horizon $(t+\tau_r)$. The control law is obtained through the optimization of the cost function expressed as,

$$J = \frac{1}{2} \int_0^{\tau_r} (y(t+\tau) - y_r(t+\tau))^T (y(t+\tau) - y_r(t+\tau)) d\tau \tag{23}$$

using Taylor series expansion of the outputs and of the reference outputs the cost function can be rewritten as [15, 18]:

$$J = (Y(t) - Y_r(t))^T \bar{\Pi} (Y(t) - Y_r(t)) \tag{24}$$

where, $Y_r(t) = \begin{pmatrix} y_r(t) & \dot{y}_r(t) & \ddot{y}_r(t) \end{pmatrix}^T$, $y_r = (\omega_m^* \ \phi_r^{2*})^T$ and

$$\bar{\Pi} = \int_0^{\tau_r} \bar{T}(\tau)^T \bar{T}(\tau) d\tau = \begin{pmatrix} \tau_r I_{2 \times 2} & \frac{\tau_r^2}{2} I_{2 \times 2} & \frac{\tau_r^3}{6} I_{2 \times 2} \\ \frac{\tau_r^2}{2} I_{2 \times 2} & \frac{\tau_r^3}{3} I_{2 \times 2} & \frac{\tau_r^4}{8} I_{2 \times 2} \\ \frac{\tau_r^3}{6} I_{2 \times 2} & \frac{\tau_r^4}{8} I_{2 \times 2} & \frac{\tau_r^5}{20} I_{2 \times 2} \end{pmatrix} = \begin{pmatrix} \bar{\Pi}_1 & \bar{\Pi}_2 \\ \bar{\Pi}_2^T & \bar{\Pi}_3 \end{pmatrix}$$

the optimal control law is deduced by setting the following condition,

$$\frac{\partial J}{\partial u} = 0 \Leftrightarrow G_1(x)^T \begin{bmatrix} \bar{\Pi}_2^T & \bar{\Pi}_3 \end{bmatrix} M + G_1(x)^T \bar{\Pi}_3 G_1(x) u(t) = 0 \tag{25}$$

finally, the control law $u(t)$ is obtained by,

$$u(t) = -G_1(x)^{-1} \left[\overline{\Pi}_3^{-1} \overline{\Pi}_2^T I_{2 \times 2} \right] M \tag{26}$$

the conditions $\{ \phi_{r\alpha}^2 + \phi_{r\beta}^2 \neq 0 \}$ and $\{ \phi_{r\alpha}, \phi_{r\beta} \} \neq 0 \}$ should be fulfilled to inverse the matrix $G_1(x)$ [15].

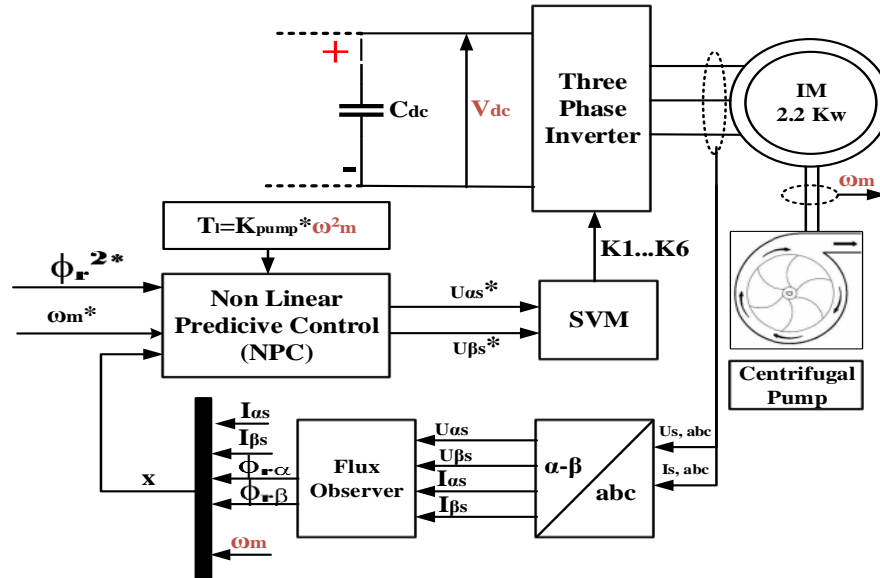


Figure 4. Non-linear predictive control of induction motor

4. SIMULATION RESULTS AND ANALYSIS

The hybrid pumping system has been tested in MATLAB / Simulink™ software. The principal data of the hybrid pumping system are listed in Table 2. Figure 5 (a) shows that linear and sudden irradiances are applied to the system, and the temperature is fixed at 25 ° C value due to its little effect on power variation. Figure 5 (b) describes the evolution of PV voltage, the controller based on DISCM-MPPT tracks fastly the reference voltage V_{pv}^* provided by P&O algorithm. In addition, a zoomed view on the PV voltage curve illustrates that the voltage fluctuations are small when the MPP is reached. In order to make a fair comparison possible, the designed DISMC-MPPT is compared with both the conventional SMC-MPPT and the ISMC-MPPT under the same operating conditions of the system. Figure 5 (c) and Table 1 clearly show the improvement of the extracted power. From simulation data, it can be observed that the conventional SMC-MPPT presents the highest power fluctuations, the slower tracking speed and the largest steady-state error. The ISMC-MPPT increases the tracking speed, but the amplitude of power oscillation is not reduced significantly. In contrast, the DISM-MPPT reduces the amplitude of power oscillation and improves the other performances in comparison with ISMC-MPPT.

Table 1. Comparison of the MPPT properties in terms of power oscillations and tracking speed during sudden change of irradiance

MPPT Technique	Irradiance (W/m ²)					
	600	400	200	300	500	700
Track. speed	Track. speed	Track. speed	Track. speed	Track. speed	Track. speed	Track. speed
Oscill. (ms)	Oscill. (ms)	Oscill. (ms)	Oscill. (ms)	Oscill. (ms)	Oscill. (ms)	Oscill. (ms)
Power (W)	Power (W)	Power (W)	Power (W)	Power (W)	Power (W)	Power (W)
SMC	400 0.8	2 0.3	- 0.09	- 0.2	2 0.9	2 0.8
ISMC	69 0.6	1.2 0.3	- 0.07	- 0.16	1.85 0.9	1.8 0.8
DISMC	69 0.5	1 0.2	- 0.05	- 0.1	1.5 0.3	1.5 0.6

On the other side, the sliding mode control scheme for the bidirectional converter is compared with the conventional PI control scheme. Figures 6 (a) presents the regulated DC-link voltage with both control strategies. For the PI-based controller, it can be seen that the DC-link voltage moves away from its reference

when the bidirectional converter switches from one mode (charging/discharging) to another. On the other hand, the DC-link voltage is accurately regulated with the sliding mode controllers, in this case, the system presents an insignificant drop of voltage and short setting time when the operating mode changes. Furthermore, the voltage ripples are reduced with the proposed controller. The state of charge (SOC) shown in Figure 6 (b) reflects the battery's charging/discharging modes. The SOC increases when the battery is charging and vice versa. Figure 6 (c) shows that the inductor L_B operates in CCM mode, the battery receives the current from the DC-bus during charging (i_{LB} negative) and delivers the current to DC-bus for the time of discharge (i_{LB} positive).

It can be observed from Figure 7 (a) that the non-linear predictive controller tracks the reference speed with a very fast dynamic. The electromagnetic torque curve presents reduced ripples because the curves of stator currents are quite close to the sinusoid form, which is depicted in Figure 7 (b) and Figure 7 (c). Figure 7 (d) shows that the decoupling between the flux and the torque is achieved accurately because the flux stays close to its reference. Since the NPC controller tracks the reference speed with high performance, the centrifugal pump parameters (flowrate, hydraulic power) are improved. Figure 7 (e) and Figure 7 (f) illustrate that these parameters follow exactly their references.

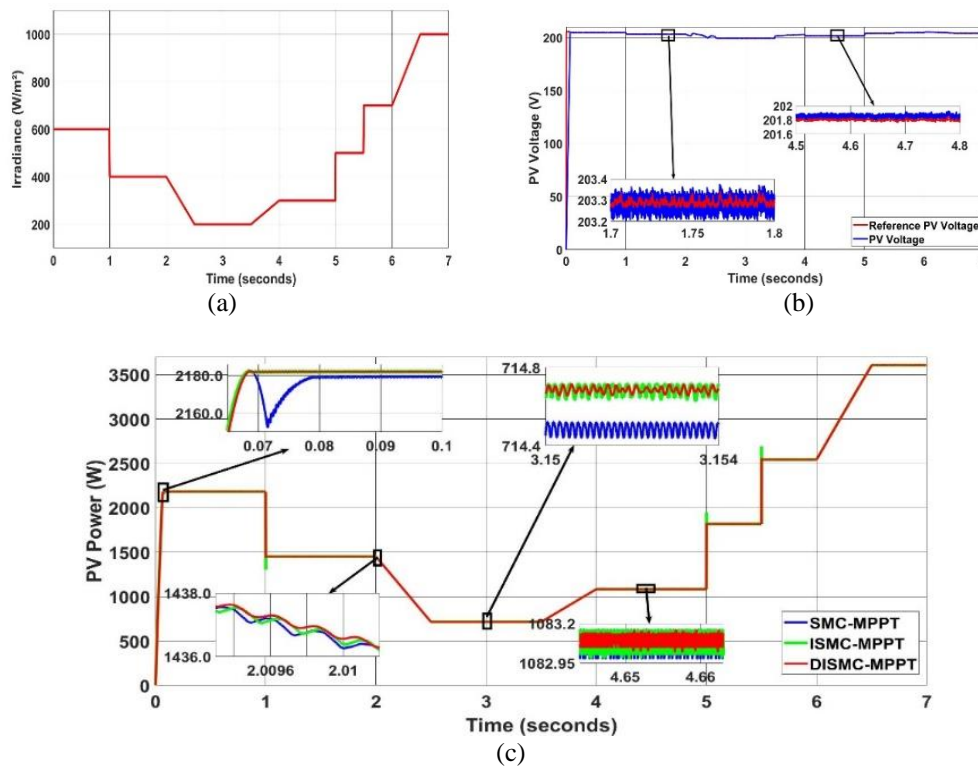


Figure 5. Simulation results of the PV array parameters under linear and sudden irradiances. (a) Irradiance, (b) PV voltage, (c) The extracted PV power for different methods

Table 2. Hybrid water pumping system parameters

Parameter		Value
PV array	Current at maximum power (I_{mp})	17.68A
	Voltage at maximum power (V_{mp})	204V
	Maximum power (P_m) at STC	3606.72W
Induction Motor Drive	Rated power (P_m)	2200W
	Rated speed (ω_r)	1430 rpm
	Rated frequency (f)	50Hz
	Nominal voltage (L-L)	230V
Centrifugal Pump	Rated flux (ϕ_r)	0.6Wb
	Rated pumping flow (Q_r)	10m ³ /h
	Rated pumping head (H_r)	50m
Battery Pack	Pump constant (K_{pump})	$6.55 \times 10^{-4} W/(r/s)^3$
	Nominal voltage (V_B)	192V

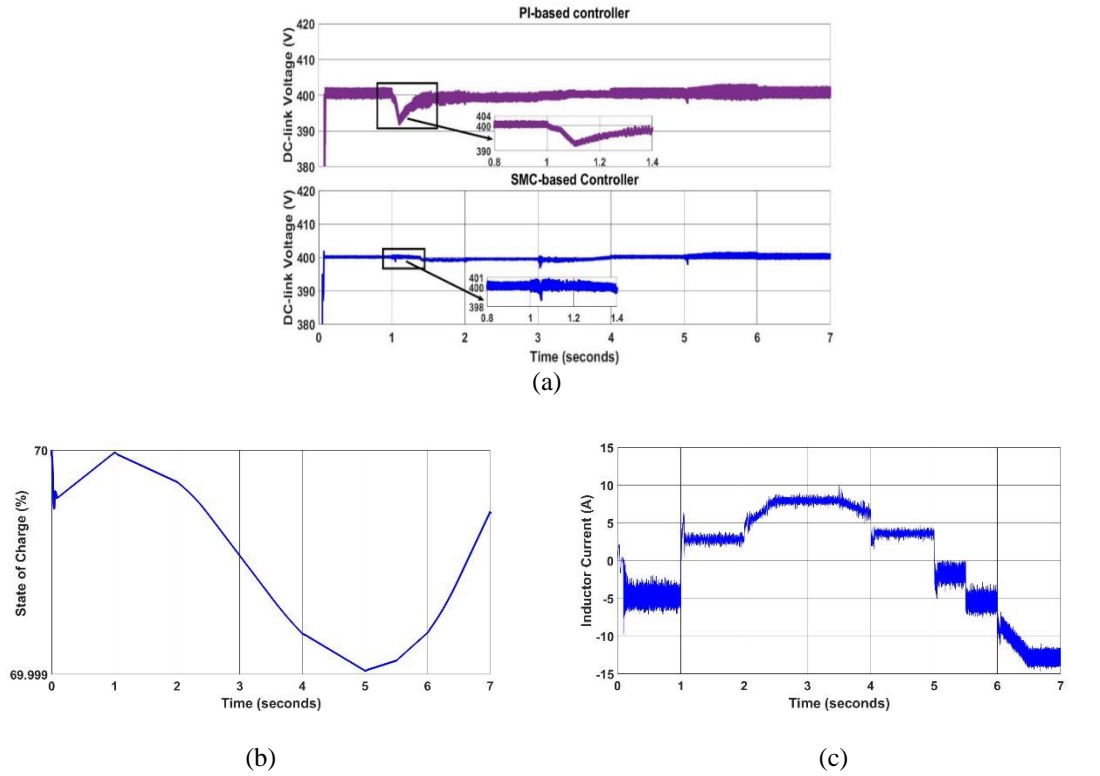
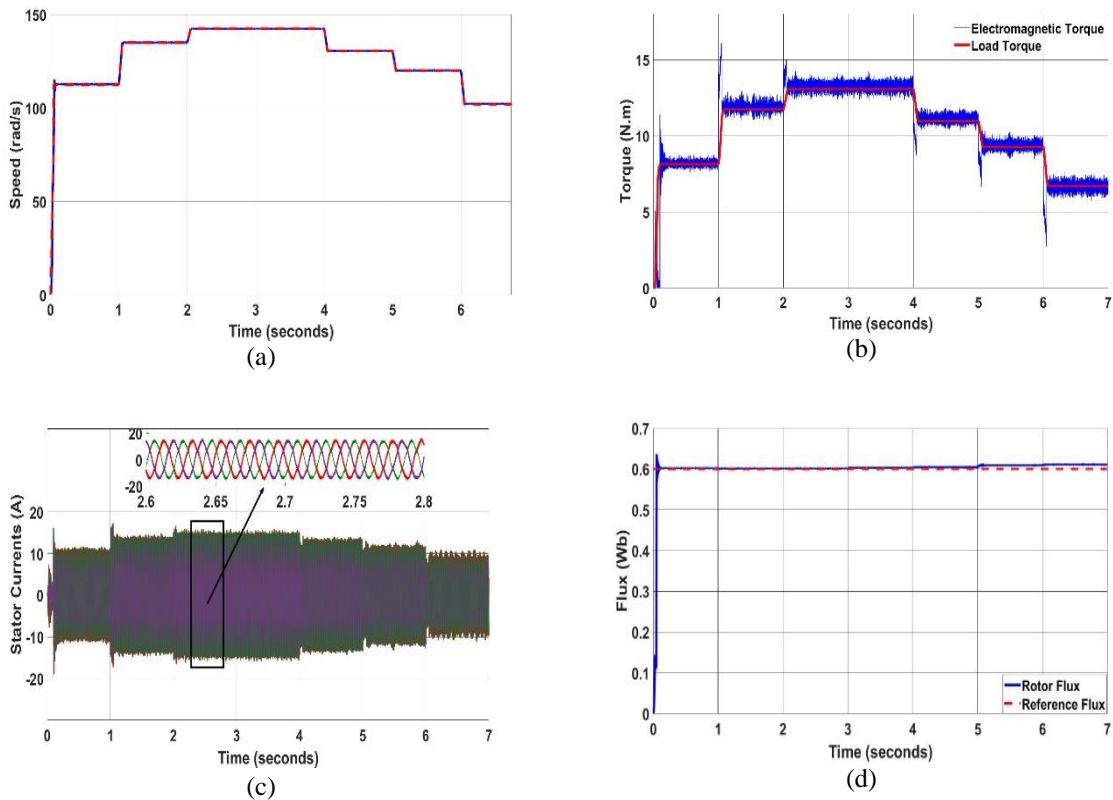


Figure 6. Simulation results of battery parameters under different load variations. (a) DC-link voltage for both PI and SMC methods, (b) state of charge, (c) the inductor current i_{LB}



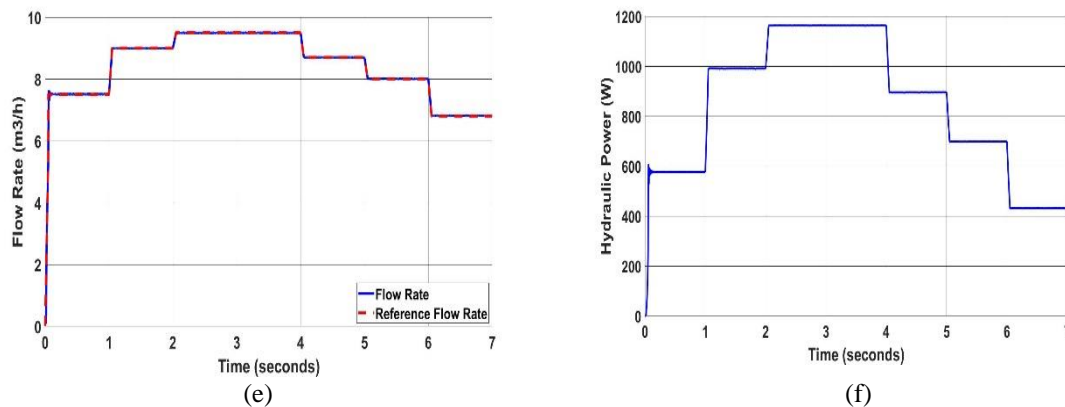


Figure 7. Simulation results of the motor-pump parameters
 (a) rotor speed, (b) electromagnetic torque, (c) stator currents, (d) rotor flux, (e) pump flowrate,
 (f) hydraulic power

5. CONCLUSION

A robust control scheme of a hybrid water pumping system based on an induction motor was presented in this paper. First, a cascaded controller based on P&O and the indirect double integral SMC is designed to track the MPP. Second, the integral sliding mode control theory has been used to control the bidirectional buck-boost converter. The third stage of the system consists of a three-phase inverter which controls the speed and torque of an induction motor with the non-linear predictive control technique. Analyzing simulation results, it is found that the DISMC-MPPT tracks the MPP with better performances than both SMC-MPPT and ISMC-MPPT methods. The bidirectional converter controlled with the conventional PI controller is not able to preserve the desired response. However, the control scheme based on ISMC theory showed high robustness and operated properly in different irradiances and speeds. Moreover, the NPC exhibited high tracking performances of the speed, fast torque response and fewer ripples in the torque. Since the IM is controlled with high performances, the pump parameters (hydraulic power, flowrate) are improved.

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