



#### **On-line Course**

### Laboratory Session: Developing Imputation Techniques in Python

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#### **Outline**

- Part 1: Machine Learning Tools
- Part 2: The Imputation with ETER Data
  - Trend Smoothing Code
  - Donor Code
- Part 3: Conclusions & Future Works

# Machine Learning (ML) Tools

Platform: Anaconda (https://docs.anaconda.com/anaconda/install/)

Programming Language: Python

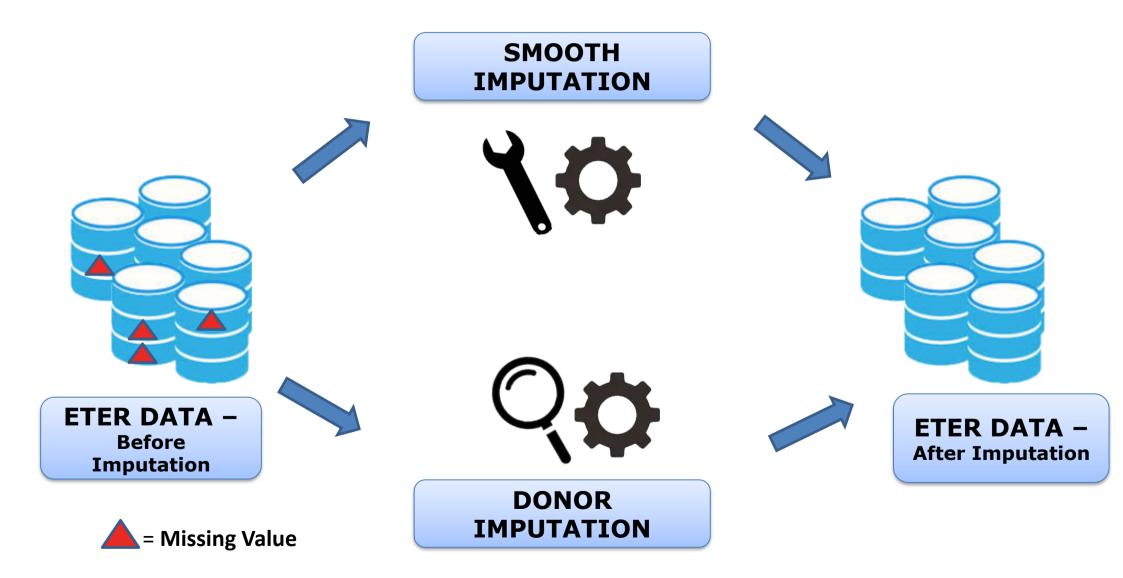


Library: Pandas (<u>https://pandas.pydata.org/</u>) Scikit-Learn (<u>https://scikit-learn.org/stable/</u>)

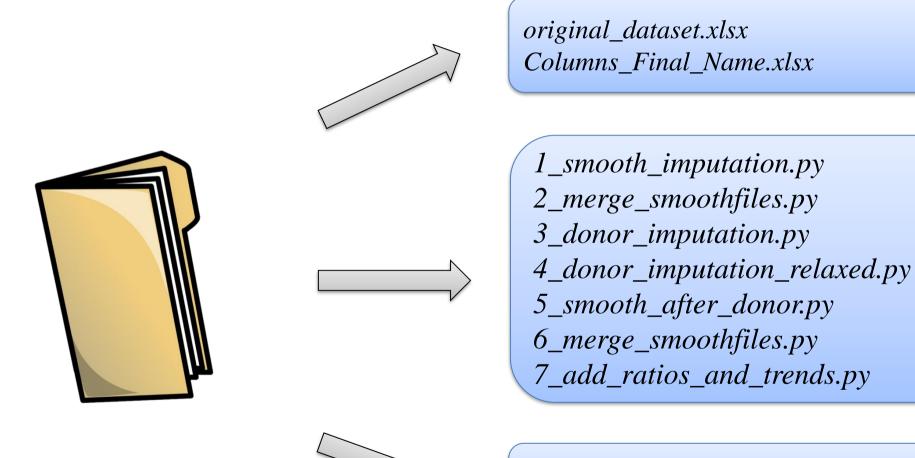
Recommended Lecture\*: Prof. Renato Bruni, "Optimization and Machine Learning for the Imputation of Missing Interconnected Data"

\*(strongly suggested before this lecture)

#### **Workflow Overview**

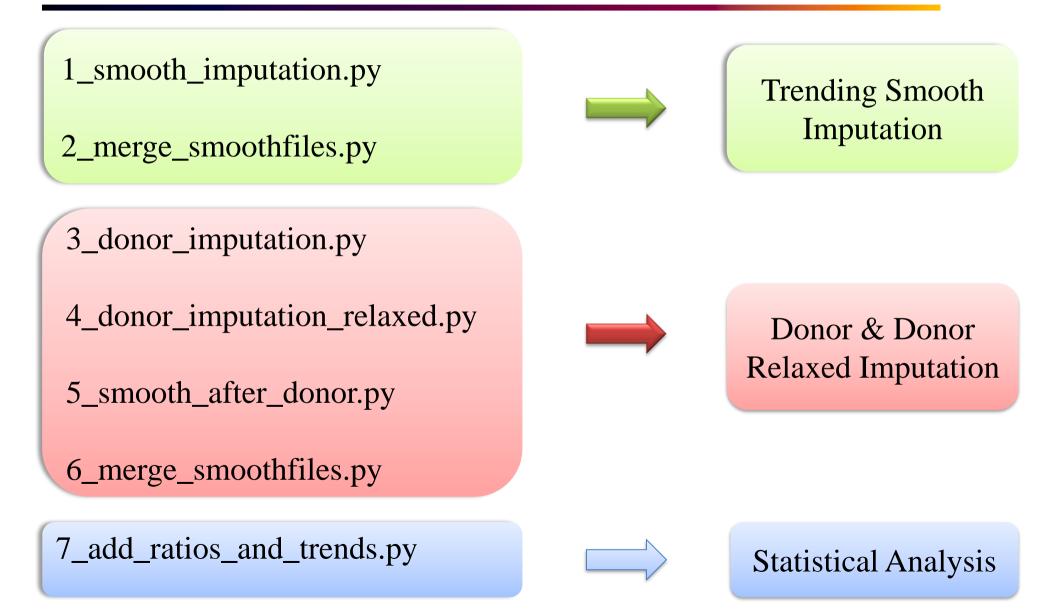


## **Directory Structure**



columns\_ordered.pkl columns\_ordered\_bibliometric.pkl

# **Python Code Pipeline**



#### **Imputation Procedure**

#### Objective:

In our work we want to reconstruct as much as possible missing values through the Machine Learning procedures. We consider 2 different types of missing value: **single** or **small sequence** and **almost complete** or **full sequence**. These different situations are tackled with 2 different methods : **Smooth Imputation** or **Donor Imputation**.

- Smooth Imputation: (Impute from the same Institution) Combination of the weighted average and the linear regression considering the time series.
- Donor Imputation: (Impute from the Donor Institution) For each Institution under imputation, find a similar complete Institution (Donor) at least for the variable we need, and use the values of the latter to impute the missing values of the former.

### **Smooth Imputation**

#### Main Steps:

- > 1. Data Preparation & Cleaning Part.
- > 2. ETER ID check about **Missing Sequence** (single, consecutive or full).
- S. Extraction of Training and Test Data, computing Linear Regression Model and Weighted Average.
- > 4. Combination between LR and WA :

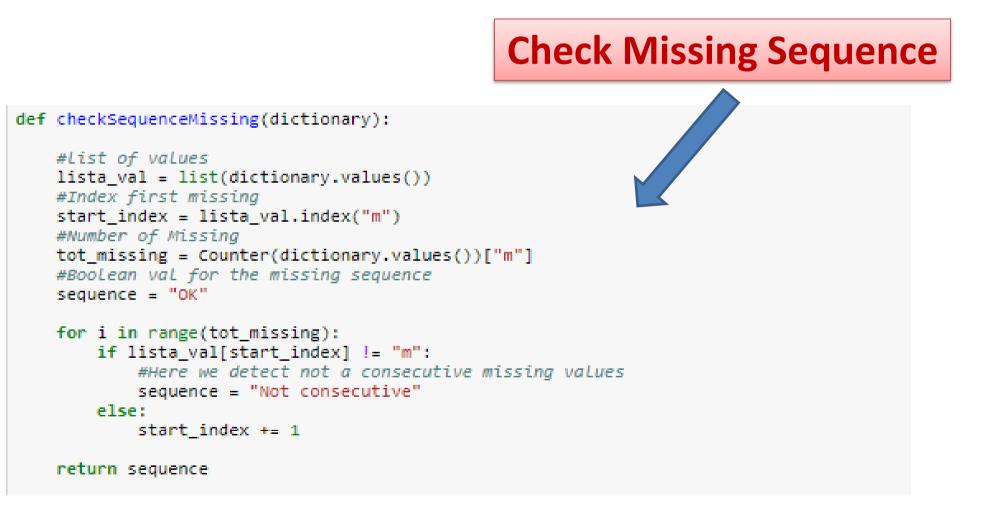
Coefficient 
$$a = \frac{2/m}{\min_{\substack{h \neq i}} \{v_h\}}$$

 $v_i = (a^2 / a^2 + 1) v_i^{WA} + (1 / a^2 + 1) v_i^{LR}$ 

 $\begin{array}{l} m = \textit{slope} \text{ of } LR \text{ model }, \\ \textit{min} \left\{ \mathcal{V}_h \right\} \text{ minimum available value} \end{array}$ 

- 5. If the result is Negative, really unfeasible, we use the Exponetiation Operation applied with an exponent in (0,1) to obtain a positive value in line with the Trend.
- > 6. Add Imputed values in the final Dataset.

# **Different types of Missing Values**



#### **Institution Data Extraction**

```
# SMOOTH Function
#Imputed value using linear regression (We exploit the implementation of Linear Regression model from Scikit-Learn)
from sklearn import linear model
#The year are selected according to the data available. The user can modify the list according to the available data.
def imputation missing LR WA(dataset, variable, vear=[2017, 2016, 2015, 2014, 2013, 2012, 2011]);
   not consecutive missing = 0
   tutti coef = []
   # Working considering the ETER ID
   for institute in tqdm(sorted(list(set(dataset["ETER ID"])))):
       print("Working with this Institute: " + str(institute))
                                                                                          Select ETER ID
       #print()
       #Extract a small dataset about the info of that ETER ID
       a = DataFrame(dataset[dataset["ETER ID"] == institute].copy())
       #Extract just info about the imputed variable and Reference year
       d = DataFrame(a[["Reference year",variable]].copy())
       #Dictionary Creation {Year:value: for instance 2016:31, 2015:20, 2014:m.....2011:11}
       valori = dict(d.values.tolist())
```

### **Model Preparation**

```
#Function transforms missing value "m", we need of at Least 2 real values to make our prediction
#Check about it and the presence of at Least 1 element in the dictionary.
if len(valori.keys()) >= 1 and len(valori.keys()) <=7 and Counter(list(valori.values()))["m"] >=1 and Counter(list(valori
   print("We work with: " + str(institute))
   #print(vaLori)
   #Check about the missing typology
   if any(i in valori.values() for i in replace) == False:
       print("This Institue "+ institute + " does not have missing different from m")
       seq = checkSequenceMissing(valori)
       #Here Institution with missing in different years not consecutive
       if sea == "Not consecutive":
           #Used in the weighted average
           fattore peso = 2
                                                                                      Type of Missing
           not consecutive missing += 1
           #print(institute)
           #print(vaLori)
       #Consecutive Missing
       else:
           #Used in the weighted average
           fattore peso = 10
       #Small dataset composed by English Institution Name, Year and Imputed Variable; sorted by the year.
       pp = a[["English Institution Name", "Reference year", variable]]
       pp = pp.sort_values(by=["Reference year"])
       #Linear Rearession Part
       Test = []
       Train = []
       #Indexes of the small dataframe
       indici = list(pp.index.values)
                                                               Train & Test Data
       valori_cambiati_indici = []
       for i in range(len(pp)):
           #2 is the column imputed
           if pp.iloc[i,2] == "m":
               Test.append(i)
               valori cambiati indici.append(indici[i])
           else:
               Train.append(i)
```

### **Linear Combination: LR - WA**

```
#Training --> Rows with data
#Test --> Rows with missing("m")
```

#In position 1 there is our X independent variable (Reference Year).

```
X_train = pp.iloc[Train,1]
X_test = pp.iloc[Test,1]
```

```
y_train = pp.iloc[Train,2]
y_test = pp.iloc[Test,2]
```

```
# Create Linear regression object
regr = linear_model.LinearRegression()
```

```
#Make the Reshape, cause X must be a Matrix
# Train the model using the training set
regr.fit(np.array(X_train).reshape(-1,1), y_train)
```

```
# Make predictions using the testing set
pred = regr.predict(np.array(X_test).reshape(-1,1))
```

#From an array to List our prediction
pred = [int(elem) for elem in list(pred) ]

#### **Linear Regression Model**

#### Weighted Average

#WEIGHTED AVERAGE PART according to the Temporal

```
if Test[0] > Train[-1]:
```

numeratore = 0
peso = 1
tot\_peso = 0

```
for elem in y_train:
```

peso \*= fattore\_peso
numeratore += peso\*elem
tot\_peso += peso

```
#WA Computation
media_pesata = numeratore/tot_peso
```

```
elif Test[0] < Train[-1]:</pre>
```

```
numeratore = 0
peso = len(y_train)*1000
tot_peso = 0
```

for elem in y\_train:

```
peso = peso/fattore_peso
numeratore += peso*elem
tot_peso += peso
```

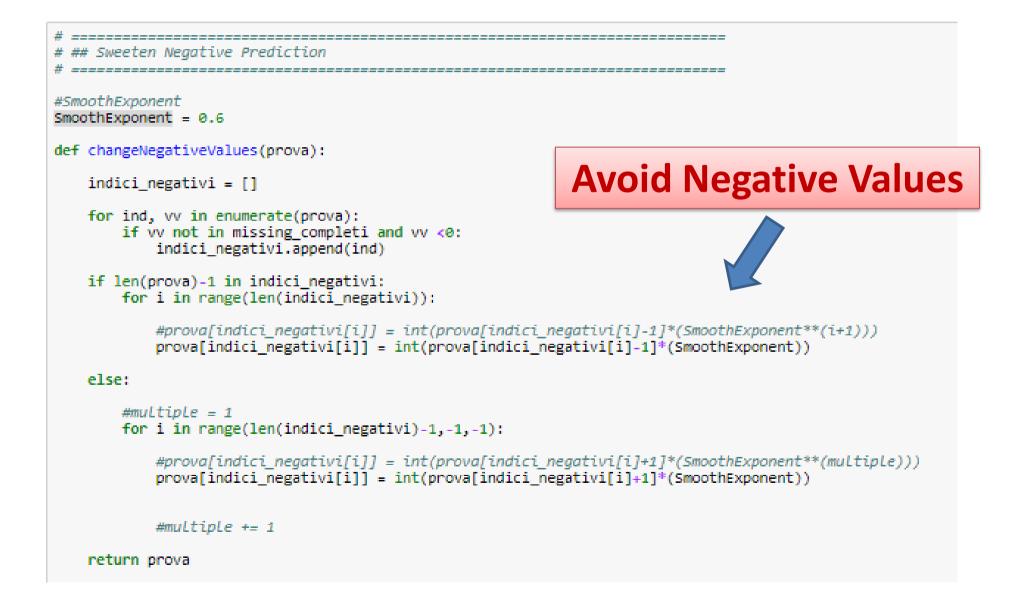
```
#WA Computation
media_pesata = int(numeratore/tot_peso)
```

```
print("Values from the analysis: LR & WA \n")
print("Starting with these values: \n")
print(valori)
print()
print("Coeff (Slope) for LR Model")
print(regr.coef_)
print("Linear Regression Prediction")
print(pred)
print("Weighted Average Prediction")
print(media_pesata)
print()
```

#### **Smooth Value Computation**

```
#We need to normalize the angular coefficient for the growth, going from 1 to 1000 is different
#respect to go from 1000 to 2000
normalizzatore = min(y train)
#Here we make a check for the infinite values, in case where the min is 0
if normalizzatore == 0:
    normalizzatore = 1
#Our Coefficient "a" (Coefficient "a" in Linear Combination between LR and
#Nome Variabile = coeff a
                                                                             «a» Coefficient
#ALL Variables except PhD
coeff a = 2* abs(regr.coef ) / normalizzatore
#PhD Students
#coeff = 4* abs(rear.coef ) / normaLizzatore
tutti_coef.append(coeff_a)
#coeff = abs(regr.coef )
print("Our 'coeff a' is: " + str(coeff a[0]))
#Linear Combination between Linear Regression(LR) and Weighted Average(WA)
\#\text{Smooth} = [a^2 / (a^2 + 1)](WA) + [1 / (a^2 + 1)](LR)
# if a --> 0 LR will have a coefficient equals to 1, otherwise WA increases its weight.
final val imputed = []
for i in range(len(pred)):
   vvv = pred[i]
    if vvv < 0:
        final val imputed.append(vvv)
    else:
        linear_comb = (coeff_a[0]**2/(coeff_a[0]**2 +1 ))*media_pesata + (1/(coeff_a[0]**2 +1 ))*pred[i]
        final_val_imputed.append(linear_comb)
print()
print("Value Imputed")
print(final val imputed)
print()
print()
for i in range(len(valori_cambiati_indici)):
    dataset[variable][valori cambiati indici[i]] = round(final val imputed[i],2)
```

### **Exponentiation Operation**



#### **Smooth Example - Students**

#### Eter ID: FR0026

Working with this ETER ID Institution: FR0026 This Institution does not have missing different from 'm'

Starting Values:

Year - Studets 2017 - 18728 2016 - 'm' 2015 - 'm' 2014 - 17203 2013 - 16808 2012 - 16618 2011 - 16143

```
Values from the analysis LR and WA
Coeff (Slope) for LR Model: 425.05
Linear Regression Prediction: [17780 , 18205]
Weighted Average Prediction: 16192
```

```
Our 'coeff_a': 0.053
Value Imputed: [2015:17776, 2016:18199]
```

#### **Smooth Example - Students**

#### Eter ID: SI0022

Working with this ETER ID Institution: SI0022 This Institution does not have missing different from 'm'

Starting Values:

Year - Studets 2016 - 19 2015 - 24 2014 - 26 2013 - 'm' 2012 - 'm' 2011 - 'm'

```
Values from the analysis LR and WA
Coeff (Slope) for LR Model: -3.5
Linear Regression Prediction: [37, 33, 30]
Weighted Average Prediction: 25
```

```
Our 'coeff_a': 0.368
Value Imputed: [2011:36, 2012:32, 2013:29]
```

# **Donor Imputation**

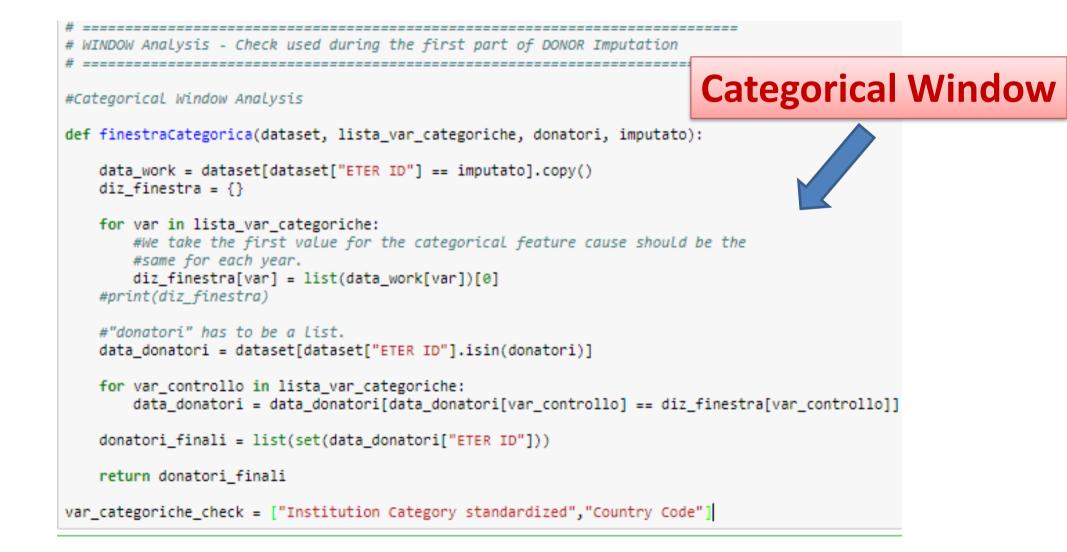
#### Main Steps:

- > 1. Data Preparation (add Country Similarity) & Cleaning Part.
- > 2. ETER ID check about **Missing Sequence** (*almost complete* or *full*).
- > 3. Creation of the container for all possible **Donor Institutions.**
- > 4. "Window" filter on categorical variables and Size, Trend and Ratios.
- 5. Computation of the Distance Function based on multiple features, with the extraction of the nearest Donor Institution.
- 6. Value imputation, if possible with the application of a normalization method.
- > 7. Add Imputed values in the final Dataset.

#### **Initial set of Donors**

```
# Selection of DONOR Institutions
# _____
#DONATORT with valid values in all variables considered.
values good donor = 5
replace = ["a", "x", "xc", "xr", "nc", "c", "s", "Null"]
                                                                       Donor Selection
#Create a dictionary with all the variables that we can donate
donatori_diz_poss = {"completi":[], "non_completi":[]}
for i in set(imputation test["ETER ID"]);
   #The Flag "buono" counts the number of variables a donor can donate.
   buono = 0
   for var in variabili imputazione:
       valori = list(imputation test[imputation test["ETER ID"] == i][var])
       if any(i in valori for i in replace) == False:
           #Add Check for the number of 0 missing values
           if Counter(valori)["m"] == 0 and (len(valori) == 6 or len(valori) == 7);
               buono += 1
   if buono == len(variabili imputazione):
       donatori diz poss["completi"].append(i)
    #Specify number of variables to consider an Institution as "good" Donor in the list "non_completi"
   if buono > values good donor:
       #At Least 5 variables completed
       donatori diz poss["non completi"].append(i)
#Check to maintain the number of times an Institution will be selected as Donor
#Choose the typology of Institution that can be Donor
#donatore scelto = { nn:0 for nn in donatori diz poss["completi"]}
donatore scelto = { nn:0 for nn in donatori diz poss["non completi"]}
#For the moment we work with Institutions complete in all the variables.
#donatori completi = donatori diz poss["completi"]
donatori_completi = donatori_diz_poss["non_completi"]
print("Total Number of Donor selected: " + str(len(donatori_completi)))
```

# Applying filters on the initial set of Donors



#### Filters on the set of Donors

#Main part Window Filter Analysis

```
diz final id size = {}
                                                            Initial Set of Selected Donors
diz final id trend = {}
print()
print("Identification of feasible Donors")
print()
for univ imputata in todm(diz eterid da imputare):
   #print("Working with " + str(univ imputata))
   #print(len(donatori))
   # 1 - Window for the Categorical filter
   donatori prima finestra = finestraCategorica(imputation test, var categoriche check, donatori, univ imputata )
   #print(Len(donatori prima finestra))
   #Check about the number of donor Institutions we find out
   if len(donatori prima finestra) == 0:
       #print("No Donor respects the CATEGORICAL Window")
       #print()
       #print()
                                                  Set of Selected Donors is reduced
       pass
   else:
       #print("Go On - SIZE Window")
       # 2 - Window for the size filter
       donatori_seconda_finestra, diz_size_id_val = finestraSize(imputation_test, variabili_correlazione, donatori_prima_finestr
                                              univ imputata )
       #print(Len(donatori seconda finestra))
       #print()
       diz_final_id_size[univ_imputata] = diz_size_id_val
       #print(diz size id val)
       #print()
       #Check about the number of donor Institutions we find out.
       if len(donatori seconda finestra) == 0:
           #print("No Donor respects the SIZE Window")
```

#### Filters on the set of Donors



diz\_accoppiamento\_imputato\_donatori[univ\_imputata] = donatori\_quarta\_finestra

### **Distance Function: using Country**

```
_____
 SIMILARITY NATIONS - Add Feature
# _____
#This part is useful for the computation on the distance to choose a possible Donor
#considering also the feature about Geographical region.
similarity country = {}
#All possible Country Code
country = set(list(starting dataset["Country Code"]))
country = ["NL", "BE", "LU", "CH", "LI", "DE", "AT", "IT", "ES", "GR", "PT", "HU", "CZ", "LT", "LV", "PL", "EE", "SK",
          "AL", "BG", "HR", "ME", "SI", "MK", "RS", "RO", "NO", "SE", "DK", "FI", "IS", "UK", "IE", "MT", "FR", "CY", "TR"]
for naz in country:
   if naz in ["NL", "BE", "LU", "CH", "LI"] :
       similarity country[naz] = 1
   elif naz in ["DE", "AT"]:
       similarity country[naz] = 2
   elif naz in ["IT", "ES", "GR", "PT"]:
       similarity_country[naz] = 3
   #EST del Nord
   elif naz in ["HU", "CZ", "LT", "LV", "PL", "EE", "SK"]:
       similarity_country[naz] = 4
                                                                      Country Similarity
   #EST del SUD
   elif naz in ["AL", "BG", "HR", "ME", "SI", "MK", "RS", "RO"]:
       similarity country[naz] = 5
   elif naz in ["NO", "SE", "DK", "FI","IS"]:
       similarity country[naz] = 6
   elif naz in ["UK", "IE", "MT"]:
       similarity country[naz] = 7
   elif naz in ["FR"]:
       similarity_country[naz] = 8
   elif naz in ["CY", "TR"]:
       similarity_country[naz] = 9
   else:
       #Check for the Nation without a specific region.
       print(naz)
```

#### Distance Funct. : using Size, Trend, ...

```
def creareVettore Knn(name_imputato, lista_donatori, diz_valori_imputato, diz_size, diz_trend):
   #Big vector for all the distances
   distanze = []
   missing = ["a", "x", "xc", "xr", "nc", "c", "s", "Null", "m"]
   for nome in lista donatori:
        Norint("Working with " + nome)
        indice donatore = imputation test[imputation test["ETER ID"] == nome].index[0]
        distanza singola univ = []
        for var in diz valori imputato:
                                                                         KNN Vector
            #print(var)
           #print()
           if var == "Size":
               distanza singola univ.append(calcoloMaxVariazione(diz size[nome]))
               #print("SIZE")
                #print(calcoloMaxVariazione(diz size[nome]))
            if var == "Trend":
               distanza singola univ.append(calcoloMaxVariazione(diz_trend[nome]))
               #print("TREND")
                #print(calcoloMaxVariazione(diz trend(nome)))
            if var == "Num Val Selected":
               #This function compute the number of variables the Donor can give to the
               #Institution imputed
               distanza singola univ.append(calcoloNumeroMissing(name imputato,nome))
```

#### **Distance Funct.: other variables**

```
if var == "Institution Category standardized" :
    valore donat = imputation test.loc[indice donatore]["Institution Category standardized"]
    #print(valore donat)
    #print(diz_valori imputato[var])
    if valore donat == diz valori imputato[var]:
        distanza singola univ.append(0)
    elif valore donat in missing:
                                                                 KNN Vector
        #distanza sinaola univ.append(np.NaN)
        distanza singola univ.append(3)
    else:
        distanza singola univ.append(3)
if var == "Institution Category - English" :
    valore_donat = imputation_test.loc[indice_donatore]["Institution Category - English"]
    #print(valore donat)
    #print(diz valori imputato[var])
    if valore donat == diz valori imputato[var]:
        distanza singola univ.append(0)
    elif valore donat in missing:
        distanza singola univ.append(3)
        #distanza singola univ.append(np.NaN)
    else:
        distanza singola univ.append(3)
if var == "Distance education institution":
    valore donat = imputation test.loc[indice donatore]["Distance education institution"]
    #print(valore donat)
    #print(diz valori imputato[var])
    if valore donat == diz valori imputato[var]:
        distanza singola univ.append(0)
    elif valore donat in missing:
        distanza singola univ.append(3)
        #distanza singola univ.append(np.NaN)
    else:
        distanza singola univ.append(3)
```

#### **Donor Example – All Variables**

Working with ETER ID DE0256

Possible DONOR Institutions: 508

Categorical Filter Available Categorical Variables: {'Institution Category standardized': 2, 'Country Code': 'DE'} DONOR Institutions selected: 89

Size Filter Available Size Variables: {} DONOR Institutions selected: 89

Trend Filter Available Trend Variables: {} DONOR Institutions selected: 89

Ratio Filter Available Ratio Variables: {} DONOR Institutions selected: 89

#### Imputed: DE0256 → Donor: DE0245

#### **Donors after Filtering**

[ DE0337 DE0341 DE0211 DE0189 DE0312 DE0315 DE0366 DE0338 DE0232 DE0316 DE0302 DE0334 DE0234 DE0309 DE0247 DE0271 DE0226 DE0307

DE0224 DE0369 DE0372 DE0265 DE0227 DE0248 DE0313 DE0205 DE0295]

Working with: DE0256 Possible DONOR Institutions: 89

Variables Available for Distance Computation:

{'Institution Category standardized': 2, 'Institution Category- English': 'university of applied sciences', 'Country Code': 'DE', 'Distance education institution': 0, 'Legal status': 1, 'Num\_Val\_Selected': 0}

Best DONOR available: DE0245 (Katholische Stiftungsfachhochschule München) , Distance: 2.0

#### **Donor Example – Rescaled Values**

#### Imp.: FI0024 $\rightarrow$ Donor: FI0021

Working with this ETER ID Institution: FI0024

(After Donor Imputation - No Available Institutions) Start Relaxed Donor Imputation

Best DONOR available: FI0021, Distance: 6.2

Start Normalization Available Variable:{Students\_afterSmooth, Graduates\_afterSmooth} Selected Variable Normalization: Students\_afterSmooth

FI0024 - Students{Year:Value}
{2016:824, 2015:840, 2014:861, 2013:788, 2012:774, 2011:659}

FI0021 - Students{Year:Value}
{2016:4020, 2015:4032, 2014:4002, 2013:4240, 2012:4338, 2011:4517}

FI0021 - Academic Staff FTE{Year:Value}
{2016:305.2959, 2015:297.3551, 2014:295.7779, 2013:304.2254, 2012:290, 2011:284.445}

Final Imputation for Academic Staff FTE - FI0024 {2016:63, 2015:62, 2014:64, 2013:57, 2012:52, 2011:41



Normalization

### Conclusions

- **Fast** imputation of several types of missing values.
- > Different imputation techniques for **short** or **full sequences**.
- Really flexible according to the request of the user.
- > Applicable to every ETER variable.
- Could be easily adapted to other educational data, or other interconnected data with different origin.
- Code avialble in Python, can take advantage of several libraries for instance **Pandas** to handle with *Excel files* and **Scikit-learn** with many <u>Machine Learning Tools</u>.

### **Further Developments**

- For many incomplete Institutions, we have scarcity of Donors: missing values are often too much and they are concentrated on some types of Institutions, so those types are very difficult to impute. Possible other sources for <u>data integration</u>?
- Smooth Imputation works initially with a univariate model, and later Ratios are used to connect the different variables. Maybe a native <u>multivariate extension</u> is possible ?
- If a Donor contains errors, its errors are propagated when it is used for imputation. We plan to study further filtering techniques for Donors.
- > Full **Parallelization** ?

# THANK YOU for your attention! Any Questions ?