

```
def Maxwells_Equations_in_Geometric_Calculus():
    Print_Function()
    X = symbols('t x y z')
    (g0,g1,g2,g3,grad) = MV.setup('gamma*t|x|y|z',metric='[1,-1,-1,-1]',coords=X)
    I = MV.I
    B = MV('B','vector',fct=True)
    E = MV('E','vector',fct=True)
    B.set_coef(1,0,0)
    E.set_coef(1,0,0)
    B *= g0
    E *= g0
    J = MV('J','vector',fct=True)
    F = E+I*B
    print r'\text{Pseudo Scalar \;\;} I =',I
    print '\\text{Magnetic Field Bi-Vector \;\;\;\;} B = \\bm{B\\gamma_{t}} =',B
    print '\\text{Electric Field Bi-Vector \;\;\;\;} E = \\bm{E\\gamma_{t}} =',E
    print '\\text{Electromagnetic Field Bi-Vector \;\;\;\;} F = E+IB =',F
    print '%\\text{Four Current Density \;\;\;\;} J =',J
    gradF = grad*F
    print '#Geometric Derivative of Electomagnetic Field Bi-Vector'
    gradF.Fmt(3,'grad*F')
    print '#Maxwell Equations'
    print 'grad*F = J'
    print '#Div $E$ and Curl $H$ Equations'
    (gradF.grade(1)-J).Fmt(3,'%\\grade{\\nabla F}_{1} -J = 0')
    print '#Curl $E$ and Div $B$ equations'
    (gradF.grade(3)).Fmt(3,'%\\grade{\\nabla F}_{3} = 0')
    return
```

Code Output:

Pseudo Scalar $I = \gamma_t \wedge \gamma_x \wedge \gamma_y \wedge \gamma_z$

Magnetic Field Bi-Vector $B = \boldsymbol{B}\boldsymbol{\gamma_t} = -B^x\gamma_t \wedge \gamma_x - B^y\gamma_t \wedge \gamma_y - B^z\gamma_t \wedge \gamma_z$

Electric Field Bi-Vector $E = \boldsymbol{E}\boldsymbol{\gamma_t} = -E^x\gamma_t \wedge \gamma_x - E^y\gamma_t \wedge \gamma_y - E^z\gamma_t \wedge \gamma_z$

Electromagnetic Field Bi-Vector $F = E + IB = -E^x\gamma_t \wedge \gamma_x - E^y\gamma_t \wedge \gamma_y - E^z\gamma_t \wedge \gamma_z - B^z\gamma_x \wedge \gamma_y + B^y\gamma_x \wedge \gamma_z - B^x\gamma_y \wedge \gamma_z$

Four Current Density $J = J^t\gamma_t + J^x\gamma_x + J^y\gamma_y + J^z\gamma_z$

Geometric Derivative of Electomagnetic Field Bi-Vector Maxwell Equations

$$\boldsymbol{\nabla} F = J$$

Div E and Curl H Equations Curl E and Div B equations

```
def Dirac_Equation_in_Geometric_Calculus():
    Print_Function()
    vars = symbols('t x y z')
    (g0,g1,g2,g3,grad) = MV.setup('gamma*t|x|y|z',metric='[1,-1,-1,-1]',coords=vars)
    I = MV.I
    (m,e) = symbols('m e')
    psi = MV('psi','spinor',fct=True)
    A = MV('A','vector',fct=True)
    sig_z = g3*g0
    print '\\text{4-Vector Potential \;\;\;\;} \\bm{A} =',A
    print '\\text{8-component real spinor \;\;\;\;} \\bm{\\psi} =',psi
    dirac_eq = (grad*psi)*I*sig_z-e*A*psi-m*psi*g0
    dirac_eq.simplify()
    dirac_eq.Fmt(3,r'%\\text{Dirac Equation \;\;\;} \\nabla \\bm{\\psi} I \\sigma_{z}-e\\bm{A}\\bm{\\psi}-m\\bm{\\psi}\\gamma_{t} = 0')
    return
```

Code Output:

4-Vector Potential $\mathbf{A} = A^t\gamma_t + A^x\gamma_x + A^y\gamma_y + A^z\gamma_z$

8-component real spinor $\boldsymbol{\psi} = \psi + \psi^{tx}\gamma_t \wedge \gamma_x + \psi^{ty}\gamma_t \wedge \gamma_y + \psi^{tz}\gamma_t \wedge \gamma_z + \psi^{xy}\gamma_x \wedge \gamma_y + \psi^{xz}\gamma_x \wedge \gamma_z + \psi^{yz}\gamma_y \wedge \gamma_z + \psi^{txyz}\gamma_t \wedge \gamma_x \wedge \gamma_y \wedge \gamma_z$

```
def Lorentz_Tranformation_in_Geometric_Algebra():
    Print_Function()
    (alpha,beta,gamma) = symbols('alpha beta gamma')
    (x,t,xp,tp) = symbols("x t x' t'")
    (g0,g1) = MV.setup('gamma*t|x',metric='[1,-1]')
    from sympy import sinh,cosh
    R = cosh(alpha/2)+sinh(alpha/2)*(g0^g1)
    X = t*g0+x*g1
    Xp = tp*g0+xp*g1
    print 'R = ',R
    print r"%t\bm{\gamma_{t}}+x\bm{\gamma_{x}} = t'\bm{\gamma_{t'}}+x'\bm{\gamma_{x'}} = R\lp t'\bm{\gamma_{t}}+x'\bm{\gamma_{x}}\rp R^{\dagger}"
    Xpp = R*Xp*R.rev()
    Xpp = Xpp.collect()
    Xpp = Xpp.subs({2*sinh(alpha/2)*cosh(alpha/2):sinh(alpha),sinh(alpha/2)**2+cosh(alpha/2)**2:cosh(alpha)})
    print r"%t\bm{\gamma_{t}}+x\bm{\gamma_{x}} =",Xpp
    Xpp = Xpp.subs({sinh(alpha):gamma*beta,cosh(alpha):gamma})
    print r"%f{\sinh}{\alpha} = \gamma\beta",
    print r"%f{\cosh}{\alpha} = \gamma",
    print r"%t\bm{\gamma_{t}}+x\bm{\gamma_{x}} =",Xpp.collect()
    return
```

Code Output:

$$R = \cosh\left(\frac{\alpha}{2}\right) + \sinh\left(\frac{\alpha}{2}\right)\gamma_t \wedge \gamma_x$$

$$t\gamma_t + x\gamma_x = t'\gamma_t' + x'\gamma_x' = R(t'\gamma_t + x'\gamma_x)R^\dagger$$

$$t\gamma_t + x\gamma_x = \left(2t'\sinh^2\left(\frac{\alpha}{2}\right) + t' - x'\sinh(\alpha)\right)\gamma_t + \left(-t'\sinh(\alpha) + 2x'\sinh^2\left(\frac{\alpha}{2}\right) + x'\right)\gamma_x$$

$$\sinh(\alpha) = \gamma\beta$$

$$\cosh(\alpha) = \gamma$$

$$t\gamma_t + x\gamma_x = \left(-\beta\gamma x' + 2t'\sinh^2\left(\frac{\alpha}{2}\right) + t'\right)\gamma_t + \left(-\beta\gamma t' + 2x'\sinh^2\left(\frac{\alpha}{2}\right) + x'\right)\gamma_x$$