

```
def derivatives_in_spherical_coordinates():
    Print_Function()
    X = (r,th,phi) = symbols('r theta phi')
    curv = [[r*cos(phi)*sin(th),r*sin(phi)*sin(th),r*cos(th)],[1,r,r*sin(th)]]
    (er,eth,ephi,grad) = MV.setup('e_r e_theta e_phi',metric='[1,1,1]',coords=X,curv=curv)
    f = MV('f','scalar',fct=True)
    A = MV('A','vector',fct=True)
    B = MV('B','grade2',fct=True)
    print 'f =',f
    print 'A =',A
    print 'B =',B
    print 'grad*f =',grad*f
    print 'grad|A =',grad|A
    print '-I*(grad^A) =',-MV.I*(grad^A)
    print 'grad^B =',grad^B
    return
```

Code Output:

$$f = f$$
$$A = A^r e_r + A^\theta e_\theta + A^\phi e_\phi$$
$$B = B^{r\theta} e_r \wedge e_\theta + B^{r\phi} e_r \wedge e_\phi + B^{\phi\phi} e_\theta \wedge e_\phi$$
$$\nabla f = \partial_r f e_r + \frac{1}{r^2} \partial_\theta f e_\theta + \frac{\partial_\phi f}{r^2 \sin^2(\theta)} e_\phi$$
$$\nabla \cdot A = \frac{A^\theta}{\tan(\theta)} + \partial_\phi A^\phi + \partial_r A^r + \partial_\theta A^\theta + \frac{2A^r}{r}$$
$$-I(\nabla \wedge A) = r^2 \left(A^\phi \sin(2\theta) - \frac{1}{2} \cos(2\theta) \partial_\theta A^\phi + \frac{1}{2} \partial_\theta A^\phi - \partial_\phi A^\theta \right) e_r + \left(-r^2 \sin^2(\theta) \partial_r A^\phi - 2r A^\phi \sin^2(\theta) + \partial_\phi A^r \right) e_\theta + \left(r^2 \partial_r A^\theta + 2r A^\theta - \partial_\theta A^r \right) e_\phi$$
$$\nabla \wedge B = \frac{1}{r^2} \left(r^2 \partial_r B^{\phi\phi} + 4r B^{\phi\phi} - \frac{2B^{r\phi}}{\tan(\theta)} - \partial_\theta B^{r\phi} + \frac{\partial_\phi B^{r\theta}}{\sin^2(\theta)} \right) e_r \wedge e_\theta \wedge e_\phi$$