

# CYCLOIDAL GAIT WITH DOUBLE SUPPORT PHASE FOR THE NAO HUMANOID ROBOT

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## Abstract

The commercial Nao humanoid robot has 11 DOF in legs. Even if these legs include 12 revolute joints, only 11 actuators are employed to control the walking of the robot. Under such conditions, the mobility of the pelvis and that of the oscillating foot are mutually constrained at each step. Besides, the original gait provided by the manufacturer company of the Nao employs only single support phases during the walking. Because of both issues, the reduced mobility in legs and the use of only single support phases, the stability of the walking is affected. To contribute to improving such stability, in this paper an approach is proposed that incorporates a double support phase and a gait based on cycloidal time functions for motions of the pelvis and those of the oscillating foot. To assess the stability of the walking an index is applied, which is based on the notion of zero-moment point (ZMP) of the static foot at each step. Results of experimental tests show that the proposed gait enhances the stability of the robot during the walking.

**Keywords:** Nao humanoid robot, gait, stability, cycloidal walking pattern, single support phase, double support phase.

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## 1. Introduction

Most of the humanoid robots studied in the scientific literature have kinematic chains with 6 degrees of freedom (DOF) per leg so that the poses (i. e. positions and orientations) of both the torso and the oscillating foot can be fully controlled in the 3D space during the walking [1–7]. However, the popular Nao humanoid robot has only 11 DOF in the legs [8]. Even if this robot has 12 revolute joints in the legs, it uses only 11 motors to control the joint motions. Indeed, the rotations of the sixth and seventh joints are controlled by using only one actuator. Under such conditions, the 3D motion of the torso and the oscillating foot cannot be independently specified. Thus, the mobility of these bodies is mutually constrained. On the other hand, the original gait provided by the manufacturer company of the Nao uses only a single support phase (SSP) during a step of the walking. Consequently, getting stable gaits in the robot becomes a complex issue.

In contrast with a walking based only on SSP that one centered on both, single and double support phases, improve the stability of walking. SSP implicates only one static foot whereas the double support phase (DSP) involves two static feet during a step. The double support period allows avoiding jumps of accelerations of bodies in such a way that the ZMP smoothly transfers from the former support to the new support [9]. On the other hand, in the specific case of the Nao an advantage could be taken of the DSP because, during the period employed for that phase, the conditions

for an elemental walking of the robot [10] could be accomplished. That is why in this paper a strategy based on the inclusion of a DSP is considered to try to improve the stability of the Nao's walking. Additionally, a gait based on cycloidal functions for translational and rotational displacements of the torso and the free foot will be implemented. As a result, a more stable and efficient walking of the robot is gotten.

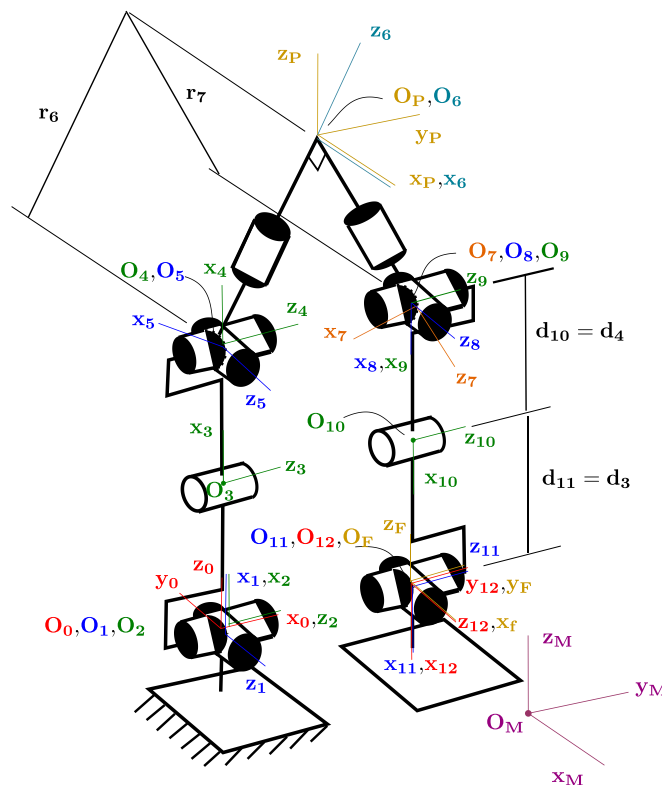
## 2. Material and Methods

### 2.1. The Nao humanoid robot

The Nao robot has 25 DOF distributed as follows: five in each arm, one in each hand, two for the head, and eleven for the legs. The first public version of this robot was presented in 2008 [8]. It is 0.57 m tall and about 4.5 kg of weight. **Fig. 1** shows the kinematic scheme of the robot's legs.

Each leg has six revolute joints however, the rotations in the two joints attached to the pelvis are produced by only one actuator. Indeed, these motions are constrained in such a way that reciprocal turnings must be always accomplished.

Some strategies for gait planning have been proposed in the literature for the Nao robot e.g. [11], however, the technique applied by Aldebaran to the humanoid is based on the inverse pendulum method [12] in such a way that rectilinear paths are followed by the robot. A gait obtained for the Nao by applying this technique will be termed *Aldebaran gait* in this paper. It must be observed that such a gait is not explicitly known in terms of motions of the pelvis and the oscillating foot but as a result of the inverse pendulum control technique that determines the control signals for the joint variables.



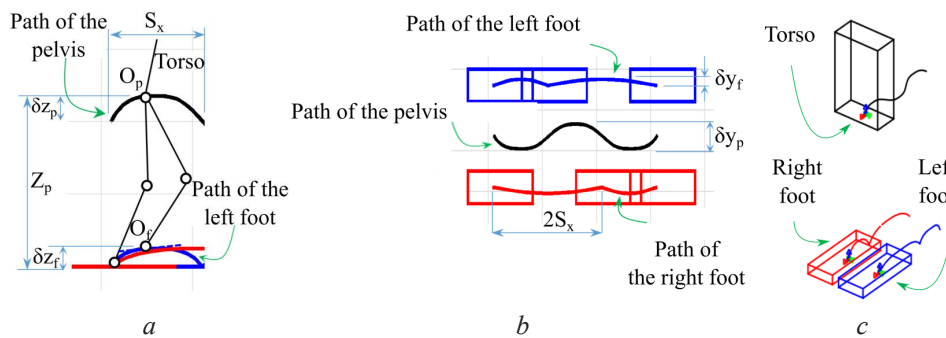
**Fig. 1.** Kinematic scheme of legs of the *Nao* robot (static right foot: *srf*)

The Aldebaran Robotics Company developed the Nao robot to achieve a low-cost platform supplemented by its communication library. The programming of the Nao is based on the application of Naoqi, a framework that can be employed in programming languages like C++, Python, or Java. The main software development tool is Choregraph [13] a blocks programming language. For physical simulation, the software of Nao employs Webots for Nao, a special version of We-

bots [14] compatible with Choregraph. The Nao robot includes systems to measure positions and current on each joint.

## 2. 2. Kinematics of the robot

The gait of a humanoid robot is specified by the desired translational and rotational motions of the pelvis and the oscillating foot during the walking. Clearly, a gait is associated with the robot's walking pattern that is defined by the reference control signals of its joint variables. The desired poses of each body should be described by six time-functions: three for position and three for orientation. In a previous work [15] an interesting family of cycloidal functions was proposed to specify a 3D gait of a humanoid robot. Such functions are applied in this work to the Nao to describe the Cartesian coordinates for position and the Bryant angles for orientation of the orthonormal frames  $\Sigma_p(O_p, x_p, y_p, z_p)$ , attached to the pelvis, and  $\Sigma_f(O_f, x_f, y_f, z_f)$ , attached to the oscillating foot. Both poses with respect to a frame  $\Sigma_M(O_M, x_M, y_M, z_M)$  attached to the ground. These frames are shown in **Fig. 1**. The Bryant angles  $\lambda, \mu, \nu$  are those of three successive rotations applied to the reference frame  $\Sigma_M$  about the axes  $x, y, z$ , respectively, in order to match the orientation of the frame to be described ( $\Sigma_p$  or  $\Sigma_f$ ). The physical meaning of the parameters that define the linear motion of the robot is shown in **Fig. 2**.



**Fig. 2.** Main parameters of linear motion of a cycloidal gait for a humanoid [13]:  
*a* – Side view, *b* – Top view, *c* – Isometric view

To model the kinematic chain of the Nao robot, this one is described by employing the modified version of the Denavit-Hartenberg method given in [16]. At each step of the robot, the successive links are numbered from 0 for the static foot to 12 for the oscillating foot. Orthonormal reference frames are attached to the links and are also numbered, as shown in **Fig. 1** for the static right foot (*srf*). Let's note that the numbering of links and frames is inverted for the static left foot (*slf*) and consequently a kinematic model is obtained for *srf* and another one for *slf*. Then, the geometric parameters that define the pose of the frame  $\Sigma_i(O_i, x_i, y_i, z_i)$  with respect to the frame  $\Sigma_{i-1}(O_{i-1}, x_{i-1}, y_{i-1}, z_{i-1})$  are identified ( $i=1, 2, \dots, 12$ ). The joint variable  $\theta_i$  is the angle from  $x_{i-1}$  to  $x_i$  about  $z_i$ . The supplementary frame  $\Sigma_p(O_p, x_p, y_p, z_p)$  attached to the pelvis is rotated by a constant angle  $\theta_p$  about the  $x_6$  axis of the  $\Sigma_6$  frame.

The kinematic models are presented in [17]. They are employed in simulations of the kinematics of the robot in this paper. The numerical values in millimetres for the distances shown in **Fig. 1** are:  $d_3=d_{11}=103$ ;  $d_4=d_{10}=100$  and  $r_6=r_7=71.2$ . Besides,  $\theta_p = 45^\circ$  for *srf* and  $\theta_p = -45^\circ$  for *slf*. The full list of the geometric parameters can be observed in [15]. Because of the constraint in joints attached to the pelvis, the relationship (1) holds during the walking between the joint variables  $\theta_6$  and  $\theta_7$ , associated with the 6<sup>th</sup> and the 7<sup>th</sup> joints respectively:

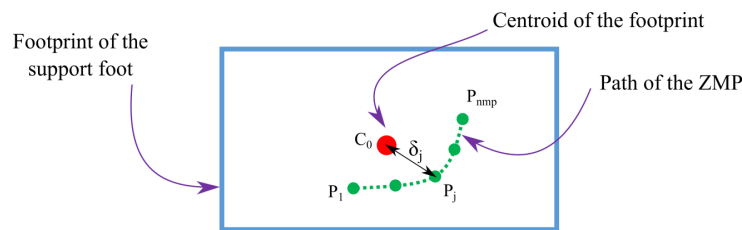
$$\theta_6 = \theta_7. \quad (1)$$

An essential issue to take into account in specifying the parameters of a cycloidal gait of the Nao robot is associated with the constraint (1). As previously indicated, the twelve operational coordinates that describe the poses of the pelvis and the oscillating foot cannot be arbitrarily specified

because the legs don't have enough DOF to control all of them. So, only a part of such coordinates and the corresponding parameters should be specified.

### 2. 3. Stability of the Nao during the walking

The behaviour of the *zero-moment point* (ZMP) [18] on the static feet is applied in this paper to measure the stability of the humanoid robot while walking. During a period of simple support, the closer the set of the zero-moment points to the centroid  $C_0$  of the footprint is, the better is the stability of the robot. To measure the distance of such a set, the coordinates corresponding to a sample of  $n_{mp}$  zero-moment points  $P_j$  are considered ( $j=1, \dots, n_{mp}$ ), which correspond to the  $k$ -th step ( $k=1, \dots, n_{ws}$ ) in SSP during a walking of  $n_{ws}$  steps. These coordinates are obtained in a physical simulation of the robot by using Webots for Nao. Then, the  $\delta_j$  distances are computed between each  $P_j$  point of the sample and the centroid  $C_0$  of the sole of the support foot. The zero moment points of the set and  $C_0$  are schematized in the sole of the humanoid in **Fig. 3**, and a distance  $\delta_j$  is also represented.



**Fig. 3.** Sample of zero moment points  $P_j$  for the  $k$ -th step of a walking

The mean value  $\bar{\delta}$  and the standard deviation  $\delta_\sigma$  of the set of distances  $\delta_j$  are computed and replaced in the following function:

$$\delta_k^* = \bar{\delta} + \delta_\sigma, \quad (2)$$

where

$$\bar{\delta} = \frac{1}{n_{mp}} \sum_{i=1}^{n_{mp}} \delta_i, \quad (3)$$

$$\delta_\sigma = \sqrt{\frac{1}{n_{mp}} \sum_{i=1}^{n_{mp}} (\bar{\delta} - \delta_i)^2}. \quad (4)$$

The function  $\delta_k^*$  defined by (2) characterizes a typical distance of the sample of zero moment points from the centroid of the footprint at the  $k$ -th step of the walking. Thus, such a function can be employed as a measure of the stability of the robot during the step. On the other hand, by taking into account that a walking should be completed by  $n_{ws}$  steps, and the values of  $\delta_k^*$  are known at each step, then the numerical value of a global measure  $\delta_w^*$  can also be computed to assess the stability of the robot associated with a foot in the whole walking by applying the following function:

$$\delta_w^* = \bar{\delta}^* + \delta_\sigma^*, \quad (5)$$

where  $\bar{\delta}^*$  is the mean value and  $\delta_\sigma^*$  is the standard deviation of the set of  $\delta_k^*$  ( $k=1, \dots, n_{ws}$ ) corresponding to the steps of the foot in the whole walking.

### 3. Results: analysis of gaits

To carry out the approach proposed in this paper, three gaits employed for a specific walking are analysed. The first one is the original Aldebaran gait. The others are cycloidal gaits specified

with different sets of numerical values of parameters for motions of the pelvis and the oscillating foot. In the considered walking the *Nao* must go through 1000 mm on a rectilinear path with a speed of 54.945 mm/sec. This speed was established by taking into account the sampling rate available in Choregraphe to acquire data from a walking.

The gait of Case 1, called *Simulated Aldebaran Gait*, is focussed on the identification of parameters of cycloidal functions that approximate the motions of the pelvis and the oscillating foot of the original Aldebaran gait, which apply only SSP. In the gait of Case 2, named *DS Cycloidal Gait* (DS means double support), the found parameters of Case 1 are modified in such a way that both SSP and DSP are employed preserving the stability of the walking. Finally, in the gait of Case 3, called *EDS Cycloidal Gait* (EDS means enhanced double support), the parameters of Case 2 are still modified in such a way that the stability of the robot during the walking be improved compared with the precedent cases.

### 3. 1. Simulated Aldebaran Gait

In the robot programming of motion for Case 1, control signals for the 12 joints variables are generated by using Choregraphe based on the inverse pendulum method and taking into account the constraint (1). Then, during a simulation of the walking in Choregraphe, such control signals are acquired by employing a sampling rate of about 14 Hz. This sample of control signals is then supplied to the software developed in Matlab for motion simulation of the robot. From the results, the parameters of cycloidal functions are identified to simulate the Aldebaran gait in Matlab as a reference gait. The cycloidal functions are defined for three stages of the walking: *starting*, *cruising* and *stopping*. To start the walking, a half-cycloidal starting function is applied to the pelvis during the first step until reaching the cruising speed. Then such a body has to preserve a constant speed during the cruising stage. Finally, in the course of the last step, a half-cycloidal stopping function is specified to the pelvis until getting the resting at the last pose.

The points of the kinematic chain whose linear motions must be specified are  $O_p$  for the pelvis, and  $O_f$  for the oscillating foot (**Fig. 1**). The periods obtained for the three stages are 2 sec for starting and stopping and 14.2 for cruising.

In the three cases study the specified Cartesian coordinates with respect to the frame  $\Sigma_M$  of  $O_p$  and  $O_f$  at the starting point are:  $x_{Op} = 0$ ,  $y_{Op} = -50$ ,  $z_{Op} = 234.7$ ,  $x_{Of} = 0$  (*rf* and *lf*),  $y_{Of} = 0$  (*lf*),  $y_{Of} = -100$  (*rf*),  $z_{Of} = 0$  (*rf* and *lf*),  $S_x = 30$ . All units are in millimetres (*lf* means left foot and *rf* means right foot). The orientations of the torso (attached to the pelvis) and that of the free foot in the starting posture of the robot are such that the frames  $\Sigma_p$  and  $\Sigma_f$  are parallel to the frame  $\Sigma_M$ .

### 3. 2. Cycloidal gaits

Taking into account the behaviour observed in Case 1, a process is considered to try to improve the stability of the *Nao*'s walking in cases 2 and 3. This process is illustrated in **Fig. 4**. It is based on the specification of cycloidal gaits in such a way that the desired rectilinear path of the walking is accomplished. Let's note in **Fig. 4** that some activities of the process are achieved by employing different software platforms (Matlab and Webots for *Nao*), and finally the experimental tests are carried out by using the *Nao* robot. Improvements in the stability of the *Nao*'s gait could be obtained by testing different sets of numerical values of parameters for the cycloidal gait and including a DSP at each step. For the studies reported here a period  $T_{ds} = 0.11$  sec was employed which corresponds to about 16 % of the period of one step. As a reference to take this value, some amounts reported in the literature were taken into account. Indeed, periods of 20 % and 15 % of one step have been reported for human walking [19] and a humanoid robot [20], respectively.

An essential issue to consider in defining parameters of a cycloidal gait is associated with the constraint (1). Indeed, such a constraint complicates the specification of the ideal poses of the pelvis and the oscillating foot.

The following coordinates are considered as those of the highest priority: those of positions of  $O_p$  and  $O_f$ , those of orientation of the pelvis, those of the yaw and roll of the oscillating foot. Consequently, the pitch of this foot is not controlled and a perturbation could occur when this foot arrives at the ground or takes off the ground. Certainly, such a perturbation already arise in the

original Aldebaran gait. It is the main source of instability. It must be observed that during the proposed double support phase the aforesaid perturbation could decrease because the ideal orientations of feet would be compatible with that of the pelvis during the period  $T_{ds}$ .

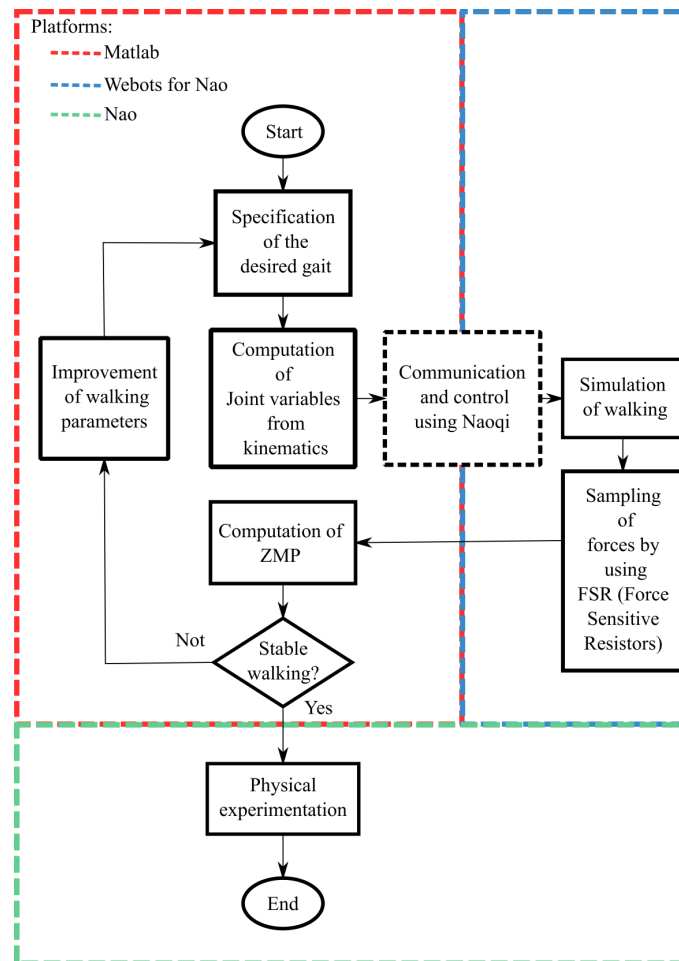


Fig. 4. Process applied to improve the stability of the Nao's walking

#### 4. Discussion of the results

The numerical values obtained of parameters for the Simulated Aldebaran Gait (Case 1) are given in **Table 1**. It was perceived that the Aldebaran Gait completes double or triple oscillations during a step in motions of the pelvis and the oscillating foot for certain stages. That is why two or three values are identified for the parameters  $\delta z_p$ ,  $\delta y_{lf}$  and  $\delta y_{rf}$  in **Table 1**. Such multiple oscillations during a step are not achieved in the cycloidal gait. On the other hand for the Aldebaran Gait it was observed that, before starting the walking, a preliminary motion was completed for the pelvis. Likewise, after stopping the motion of feet, an additional displacement of the pelvis is accomplished. Both issues occur in a situation of double support. Thus, in **Table 1** for the Case 1 two supplementary segments of motion are considered: BW (*before walking*) and AS (*after stopping*) with periods of 1.35 sec. and 1.14 sec, respectively. The corresponding data are displayed in additional rows of **Table 1**.

Simulations of Case 1 shown that not significant oscillations occur of the orientation coordinates of the Nao's torso. Such oscillations were of the order of  $\pm 0.001^\circ$ . So, it is considered that the motion of the torso is only translational. Furthermore, neither yaw nor roll rotations were observed in the oscillating foot. Only pitch rotations were appreciated on this body by an amount of about  $\pm 19^\circ$ . Besides, the results ratify that only single support phases arise in the Aldebaran gait.

On the other hand, after the implementation of several tests in the process of Fig. 4 the sets of numerical values of the parameters for cycloidal gaits of cases 2 and 3 were established. Table 1 gives these values. By applying them the motions of the torso and the oscillating foot can be simulated. The results of such a simulation for Case 3 are observed in Fig. 5.

Several simulations were carried out to assess the stability of the robot in the three cases. For cases 1 and 3 the obtained samples of the ZMP on the footprint of the Nao are presented in Fig. 6. The corresponding values of the stability index  $\delta_k^*$  are compared at each step in Fig. 7. The values of the stability index  $\delta_w^*$  of the whole walking are compared for cases 1 and 3 in Fig. 8. Global improvements are perceived in the stability of the feet with the EDS Cycloidal Gait compared with the Simulated Aldebaran Gait. The values of the index  $\delta_w^*$  go from 38.58 mm and 39.51 mm for  $lf$  and  $rf$ , respectively, in Case 1, to 31.89 and 30.83 mm for  $lf$  and  $rf$ , respectively, in Case 3. These reductions signify improvements by 17.34 % and 21.9 % in the stability of the Nao with the left foot and the right foot, respectively.

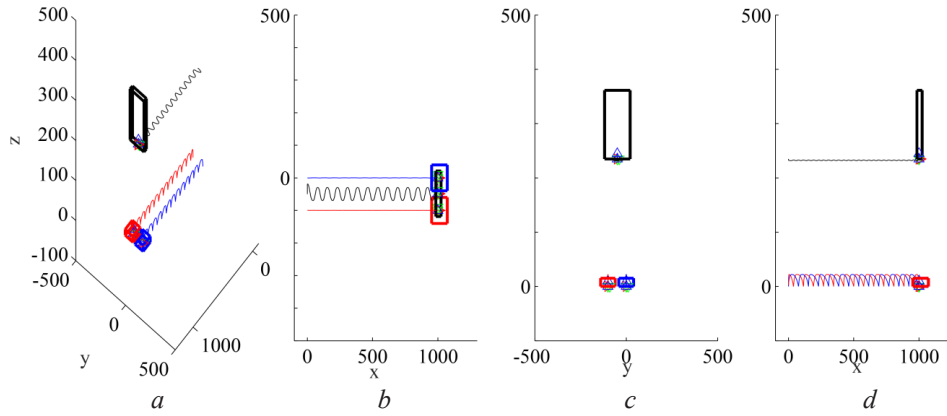
**Table 1**

Numerical values (mm) of parameters for cycloidal motions of cases study

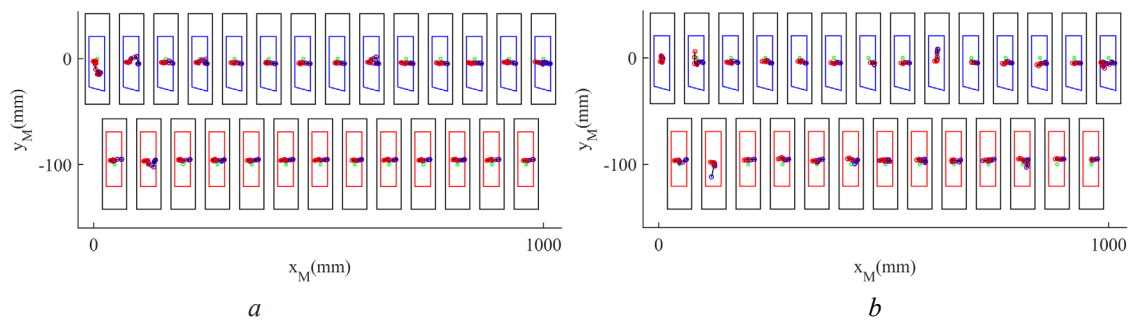
Case study	Smt*	$\delta x_p$	$\delta y_p$	$\delta z_p$	$\delta x_{lf}$	$\delta y_{lf}$	$\delta z_{lf}$	$\delta x_{rf}$	$\delta y_{rf}$	$\delta z_{rf}$
1. Simulated Aldebaran Gait	<i>BW</i>	-9.2	31	0.7 -3.5	0.0	0.0	0.0	0.0	0.0	0.0
	<i>St</i>	13	-51	1.7	0.0	0.0	0.0	38	0.2 -0.4 0.1	20
	<i>Cr</i>	37	41	1.2	77	0.2 -0.3 0.1	20	77	-0.1 0.2 -0.1	20
	<i>Sp</i>	30	51	-1.1 0.8 -0.3	0.0	0.0	0.0	38	-0.1 0.2 -0.1	20
	<i>AS</i>	7.0	-31	1.7	0.0	0.0	0.0	0.0	0.0	0.0
2. DS Cycloidal Gait	<i>BW</i>	0.0	31	0.7	0.0	0.0	0.0	0.0	0.0	0.0
	<i>St</i>	18	-51	-3.5	0.0	0.0	0.0	38	0.0	20
	<i>Cr</i>	37	41	1.2	77	0.0	20	77	0.0	20
	<i>Sp</i>	18	51	-1.1	0.0	0.0	0.0	38	0.0	20
	<i>AS</i>	0.0	-31	2.0	0.0	0.0	0.0	0.0	0.0	0.0
3. EDS Cycloidal Gait	<i>BW</i>	0.0	30	0.1	0.0	0.0	0.0	0.0	0.0	0.0
	<i>St</i>	20	-50	-3.1	0.0	0.0	0.0	38	0.0	22
	<i>Cr</i>	37	40	1.3	77	0.0	22	77	0.0	22
	<i>Sp</i>	15	50	-1.1	0.0	0.0	0.0	38	0.0	22
	<i>AS</i>	0.0	-30	2.8	0.0	0.0	0.0	0.0	0.0	0.0

Note: \* – abbreviations: Smt – segment, BW – before walking, AS – after stopping, St – starting (SSP), Cr – Cruising, Sp – Stopping (SSP)

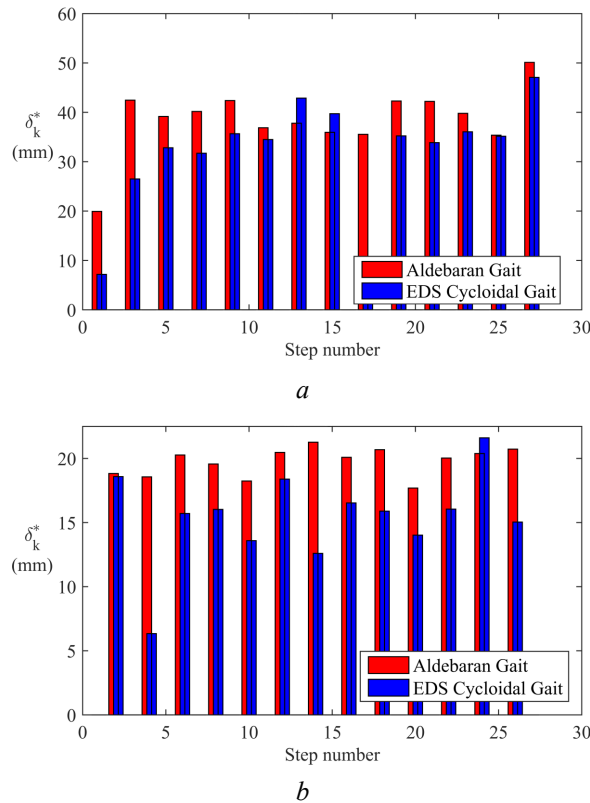
Finally, sequences of postures of the robot during the experimental walking are shown for cases 1 and 3, respectively, in Fig. 9 (Case 1) and Fig. 10 (Case 3). As observed in these figures, with respect to the path of reference the robot gets a better position at the end of the walking by employing the gait of Case 3 compared with the position gotten with the gait of Case 1.



**Fig. 5.** Views of motion-simulation in Matlab© of the torso and oscillating feet for the EDS Cycloidal Gait (Case 3): *a* – isometric; *b* – top; *c* – front; *d* – side

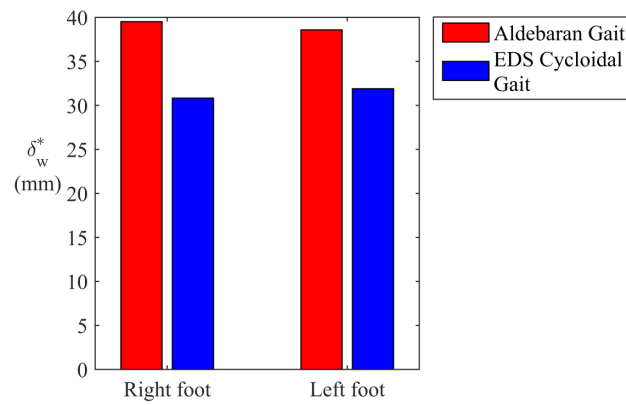


**Fig. 6.** Behaviour of ZMP on the footprints per step. Simulation in Matlab with data obtained from Webots for Nao: *a* – Aldebaran Gait; *b* – EDS Cycloidal Gait

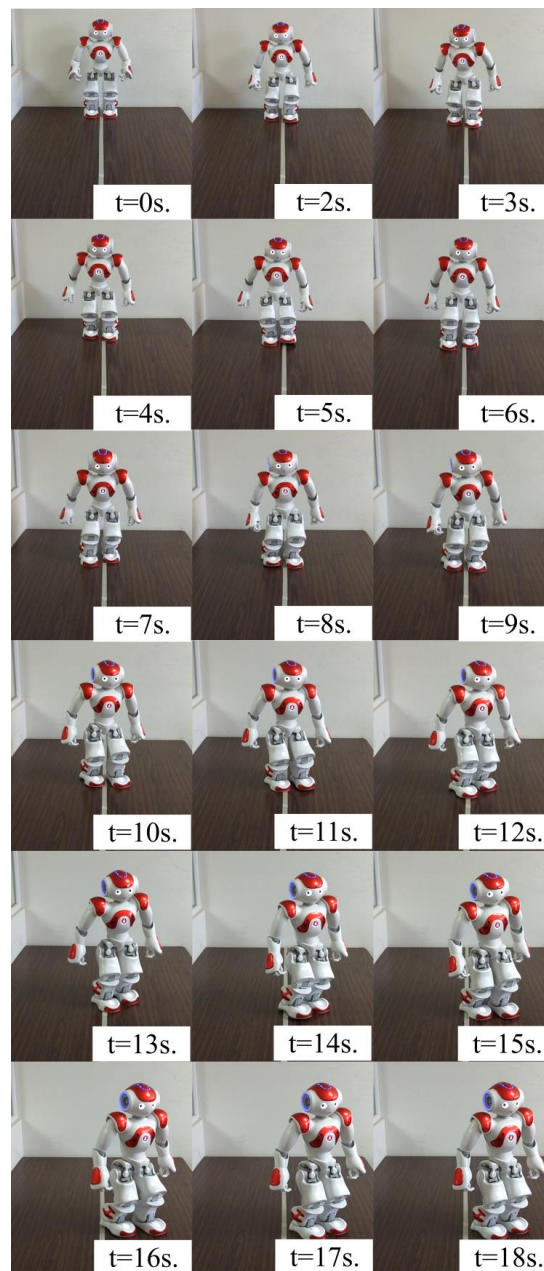


**Fig. 7.** Stability index  $\delta_k^*$  at each step: *a* – left foot; *b* – right foot

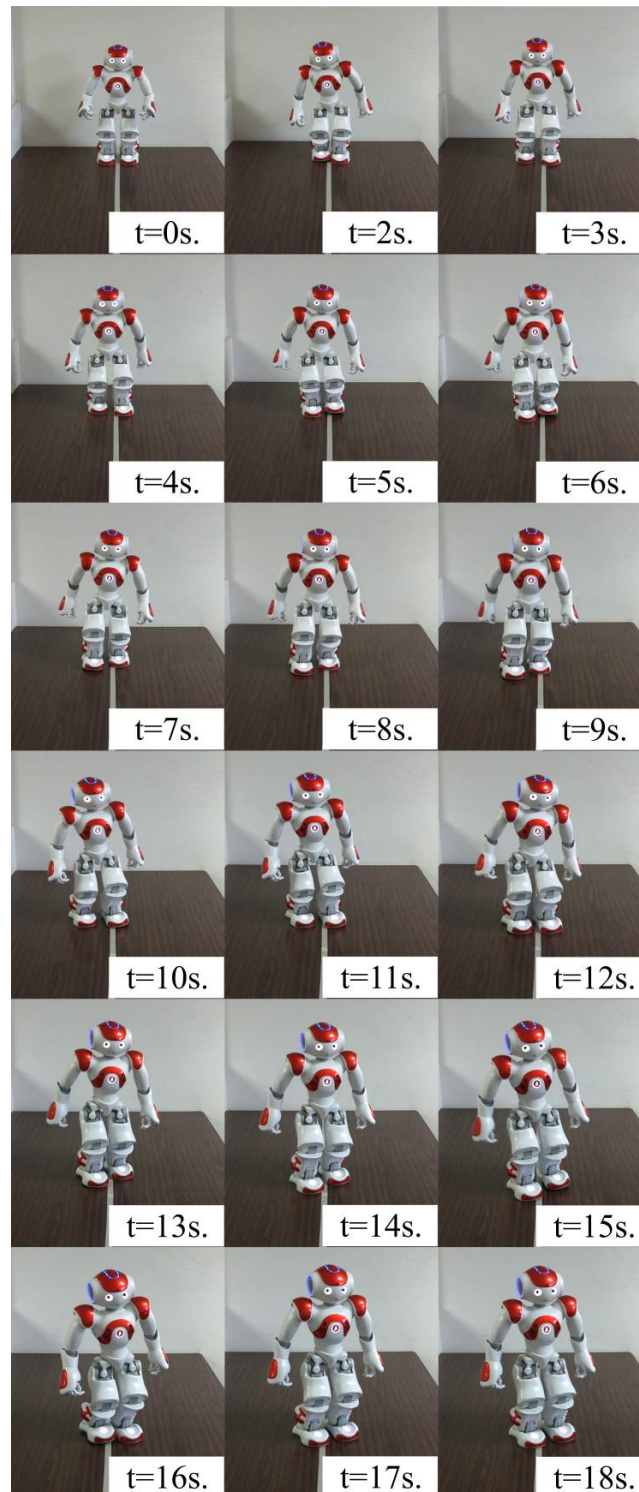




**Fig. 8.** Stability index  $\delta_w^*$  for the whole walking



**Fig. 9.** Case 1. Postures of the Nao during the *Aldebaran Gait*. Front view. Only SSP are applied



**Fig. 10.** Case 3. Postures of the Nao during the *EDS Cycloidal Gait*. SSP and DSP are employed

## 5. Conclusions

A strategy was proposed in this paper to improve the stability of the Nao humanoid robot during the walking. This robot has only 11 DOF in the legs. The proposed strategy is based on the integration of a double support phase and cycloidal motions to the gait of the robot. As a result, a significant improvement was gotten in the stability of the robot during the walking. The obtained simulations and the experimental results prove the enhancement.

To measure the stability of the robot, the indices  $\delta_k^*$  (for one step) and  $\delta_w^*$  (for the whole walking) were introduced in the paper. These ones represent typical deviations of the ZMP from the centroid of the footprint of the robot. Consequently, the smaller are the indices the better is the stability of the robot during the walking. Substantial improvements were obtained in the index  $\delta_w^*$  for the whole walking.

Thanks to the analysis accomplished in this work, it was appreciated that multiple transversal fluctuations occur in motions of both oscillating foot and the torso during the walking by employing the original Aldebaran Gait. Such fluctuations could be a source of instability and involve more energy consumption of the robot. That is why in future works studies of energy consumption related to the gait of the robot will be carried out. Furthermore, to improve the stability of the Nao's walking as much as possible by taking into account the approach introduced here, an optimization study will be also achieved in the future.

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