

# Novel Signatures of Dark Matter in Laser-Interferometric Gravitational-Wave Detectors

Yevgeny Stadnik

Kavli Fellow

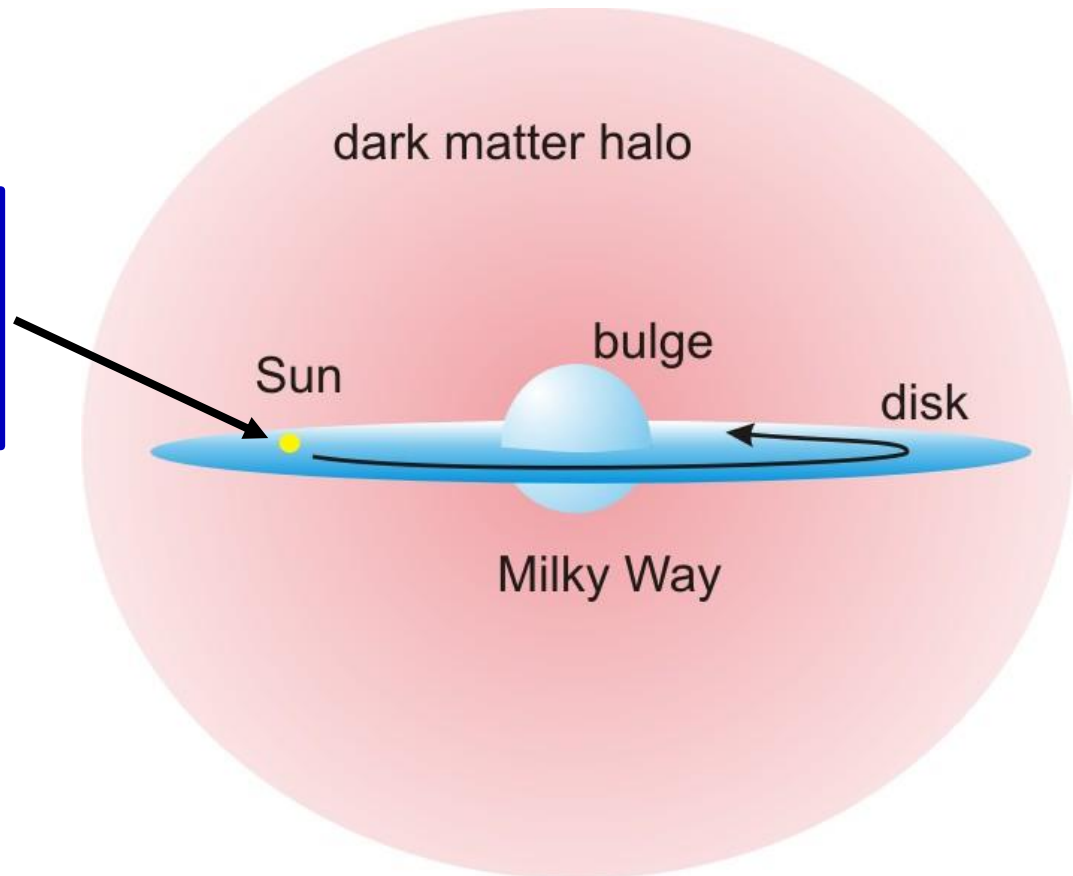
Kavli IPMU, University of Tokyo, Japan



# Motivation

Strong astrophysical evidence for existence of **dark matter** (~5 times more dark matter than ordinary matter).

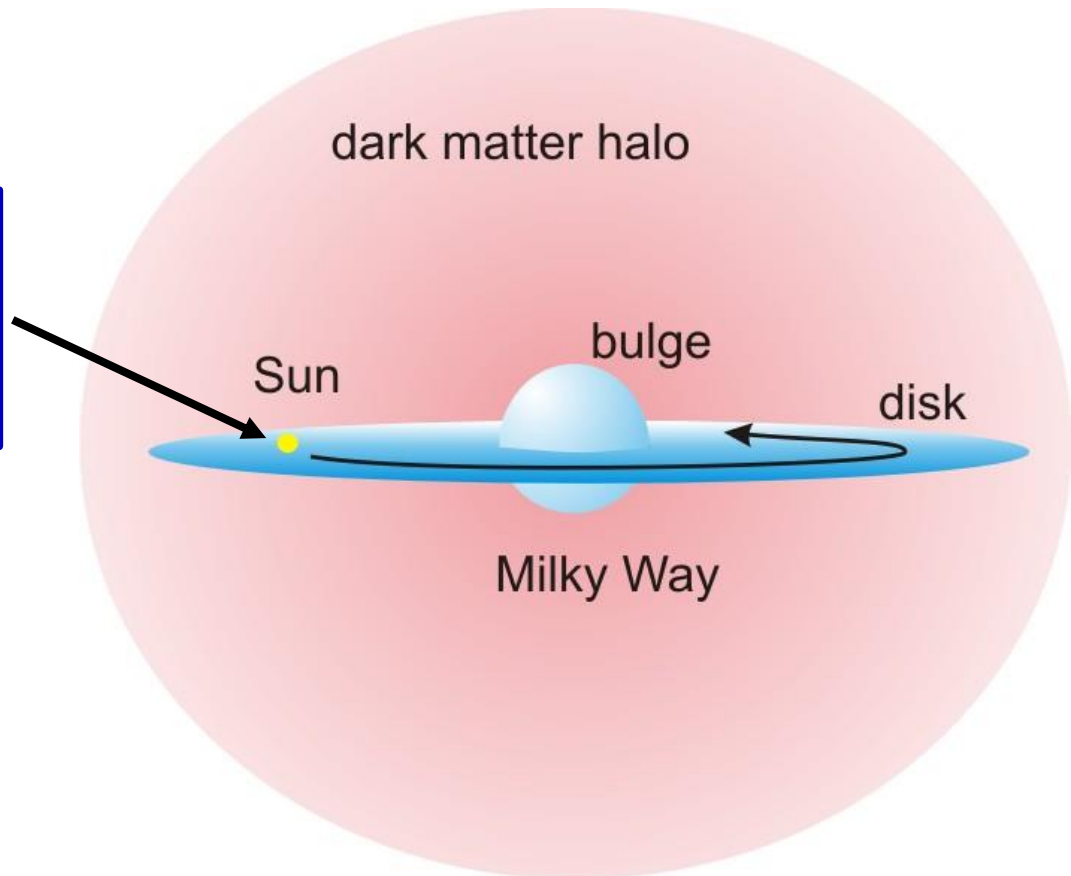
$$\rho_{\text{DM}} \approx 0.4 \text{ GeV/cm}^3$$
$$v_{\text{DM}} \sim 300 \text{ km/s}$$



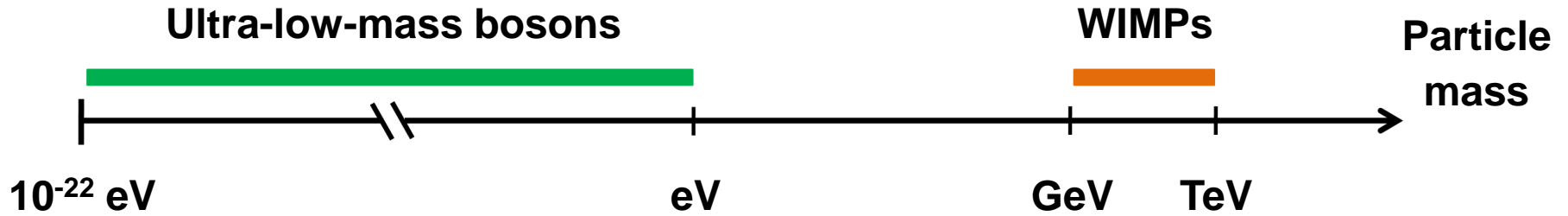
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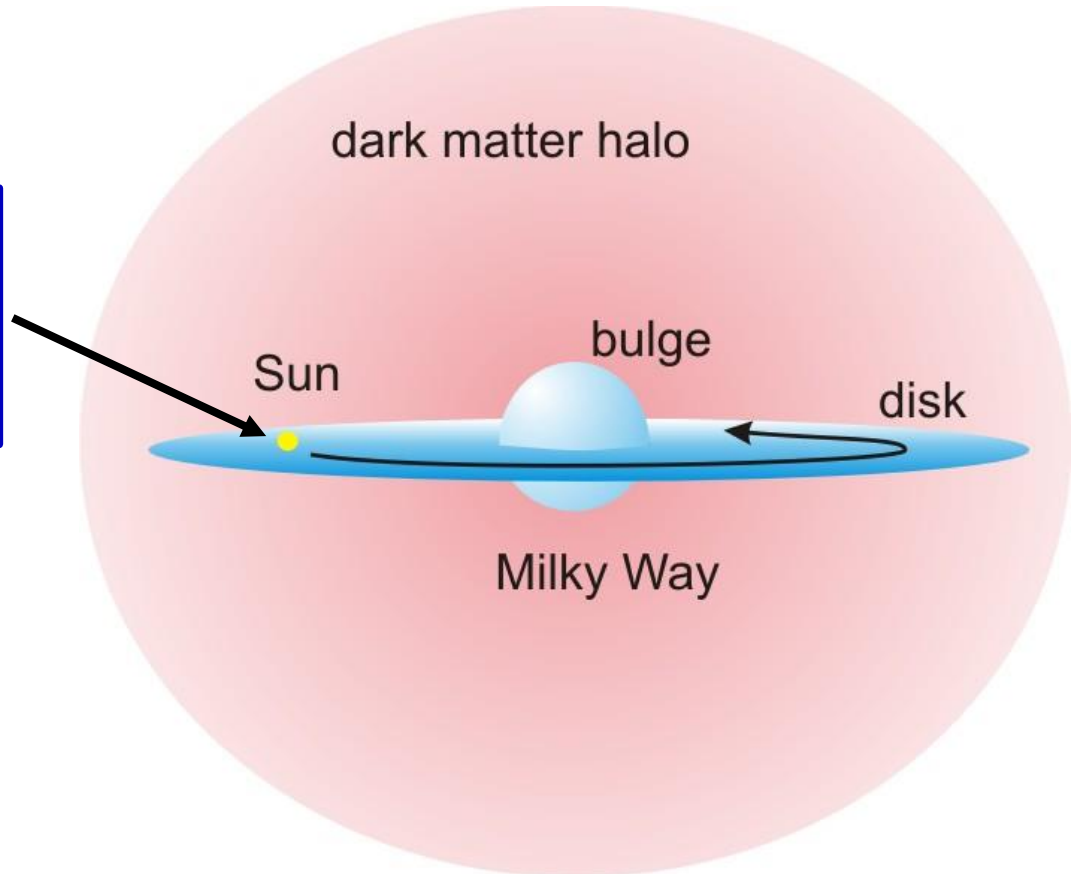
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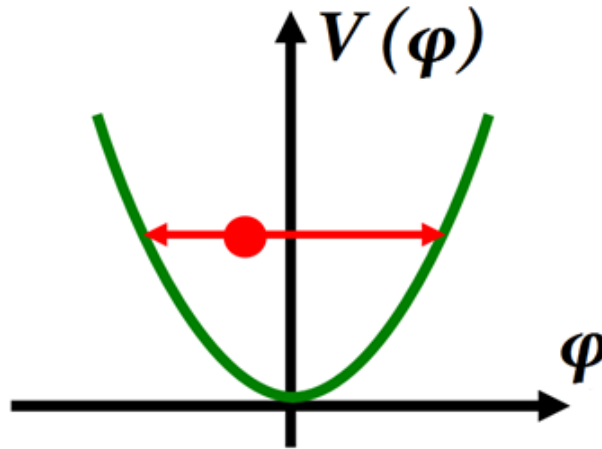


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# Low-mass Spin-0 Dark Matter

- Low-mass spin-0 particles form a coherently oscillating classical field  $\varphi(t) = \varphi_0 \cos(m_\varphi c^2 t/\hbar)$ , with energy density  $\langle \rho_\varphi \rangle \approx m_\varphi^2 \varphi_0^2/2$  ( $\rho_{\text{DM,local}} \approx 0.4 \text{ GeV/cm}^3$ )



$$V(\phi) = \frac{m_\phi^2 \phi^2}{2}$$

$$\ddot{\phi} + m_\phi^2 \phi \approx 0$$

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$\lambda_{\text{dB},\varphi} / 2\pi \leq L_{\text{dwarf galaxy}} \sim 1 \text{ kpc}$

Classical field

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Classical field

- *Wave-like* signatures [cf. *particle-like* signatures of WIMP DM]

# Dark Matter-Induced Cosmological Evolution of the Fundamental Constants

[Stadnik, Flambaum, *PRL* **114**, 161301 (2015); *PRL* **115**, 201301 (2015)],

[Hees, Minazzoli, Savalle, Stadnik, Wolf, *PRD* **98**, 064051 (2018)]

$$\mathcal{L}_\gamma = \frac{\phi}{\Lambda_\gamma} \frac{F_{\mu\nu} F^{\mu\nu}}{4} \Rightarrow \frac{\delta\alpha}{\alpha} \approx \frac{\phi_0 \cos(m_\phi t)}{\Lambda_\gamma}$$

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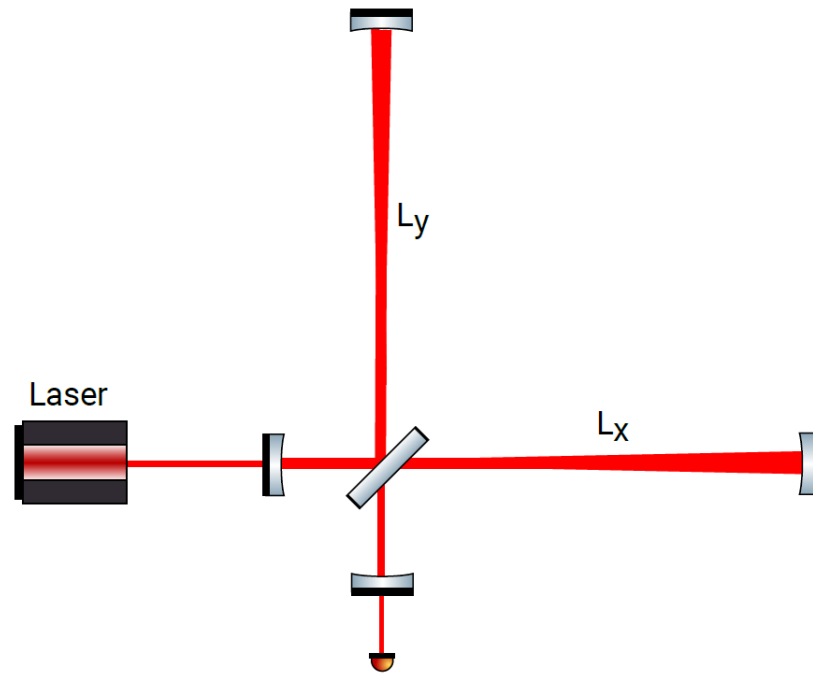
**Solid material**



$$L \sim Na_B = N/(m_e \alpha)$$

# Laser Interferometry Searches for Oscillating Variations in Fundamental Constants due to Dark Matter

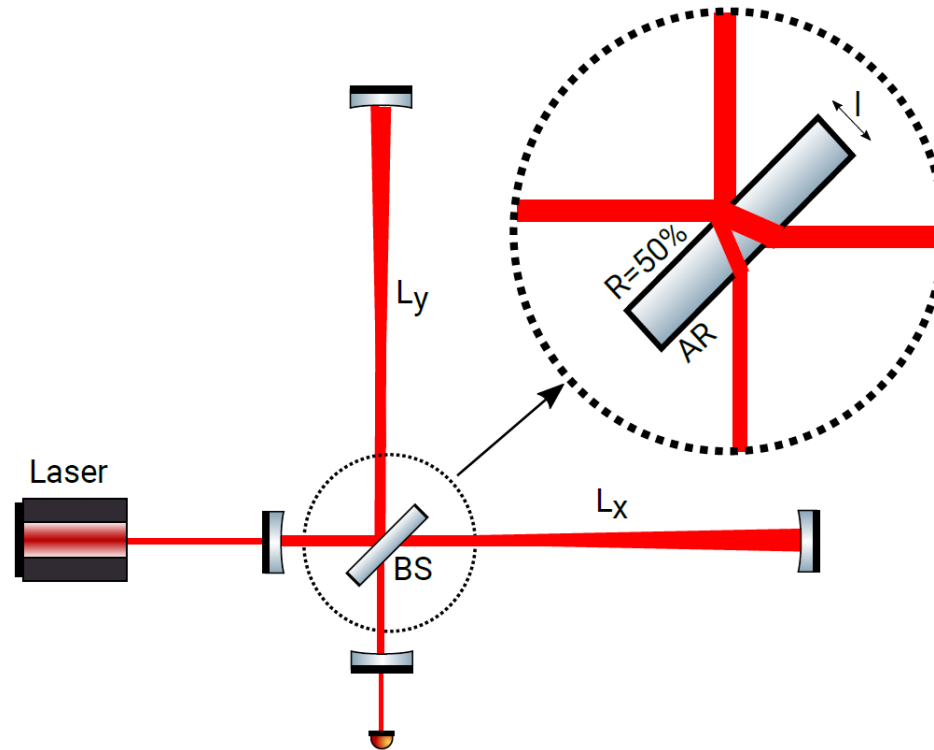
[Grote, Stadnik, arXiv:1906.06193]



**Michelson interferometer (GEO 600)**

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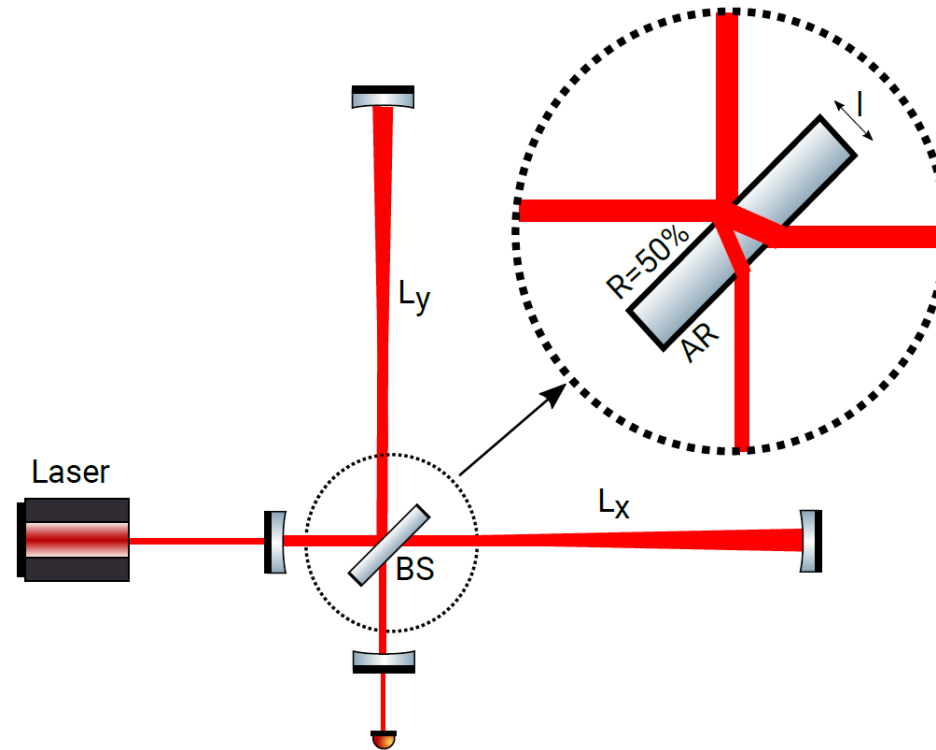
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- Geometric asymmetry from beam-splitter:  $\delta(L_x - L_y) \sim \delta(nl)$

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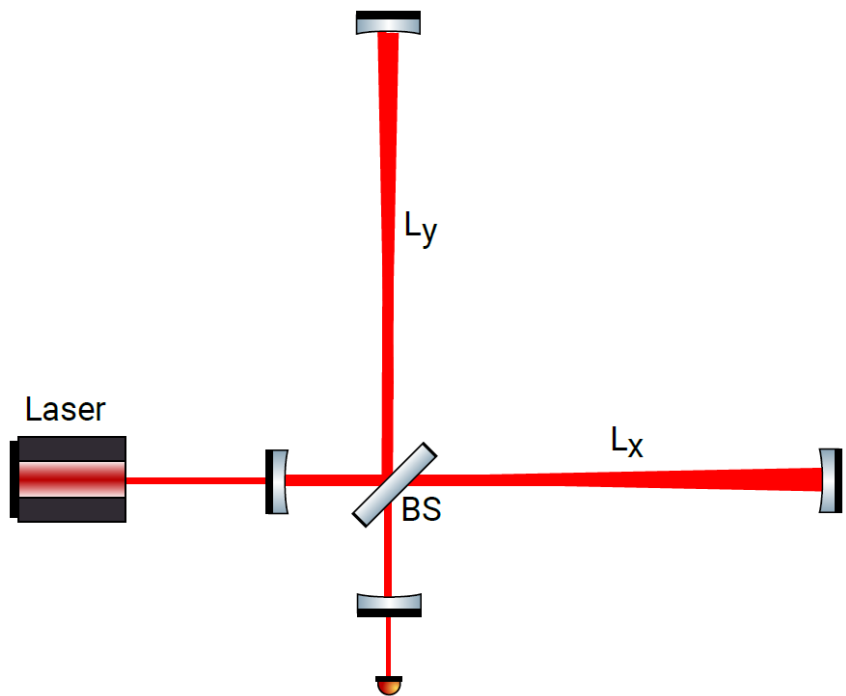
- Geometric asymmetry from beam-splitter:  $\delta(L_x - L_y) \sim \delta(nl)$
- Both broadband and resonant narrowband searches possible:  $f_{\text{DM}} \approx f_{\text{vibr,BS}} \sim v_{\text{sound}}/l$ ,  $Q \sim 10^6$  enhancement



# Michelson vs Fabry-Perot-Michelson Interferometers

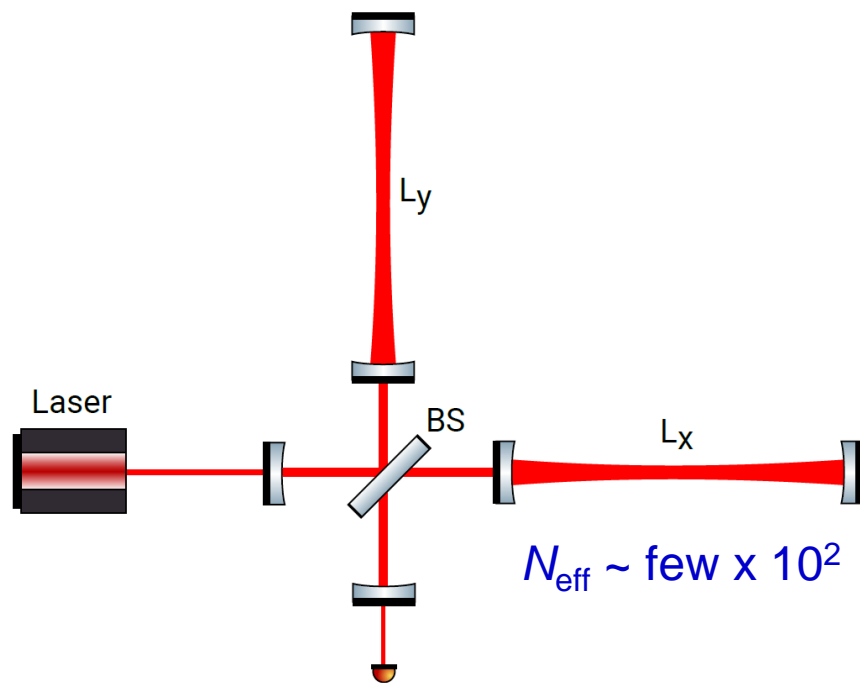
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**Michelson interferometer  
(GEO 600, Fermilab holometer)**



$$\delta(L_x - L_y)_{BS} \sim \delta(nl)$$

**Fabry-Perot-Michelson interferometer  
(LIGO, VIRGO, KAGRA)**

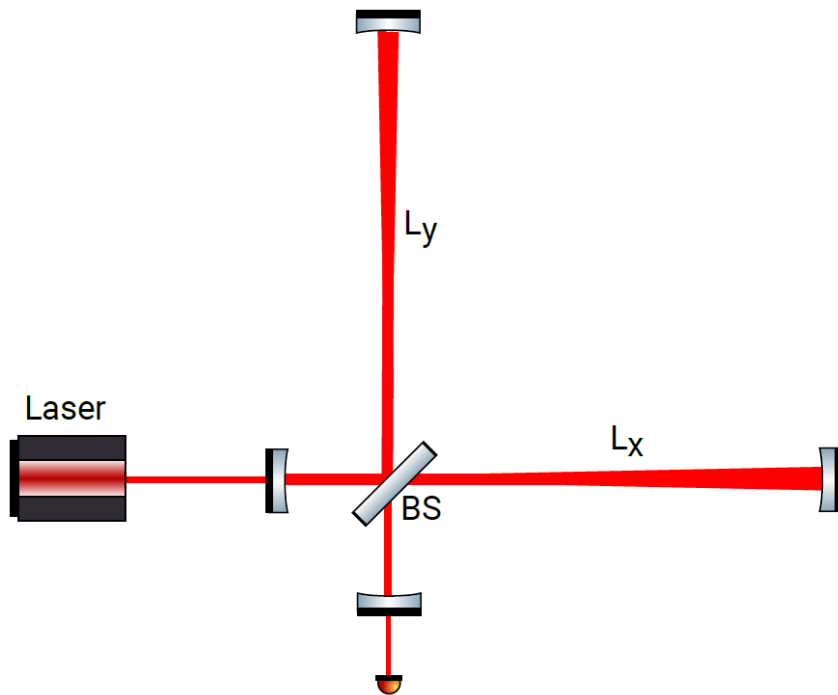


$$\delta(L_x - L_y)_{BS} \sim \delta(nl)/N_{\text{eff}}$$

# Michelson vs Fabry-Perot-Michelson Interferometers

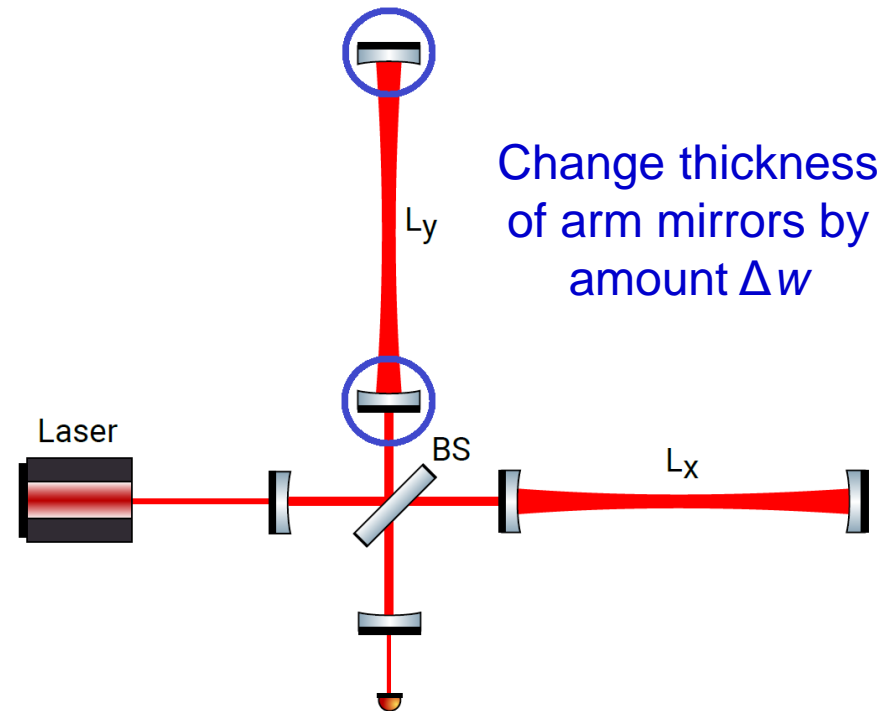
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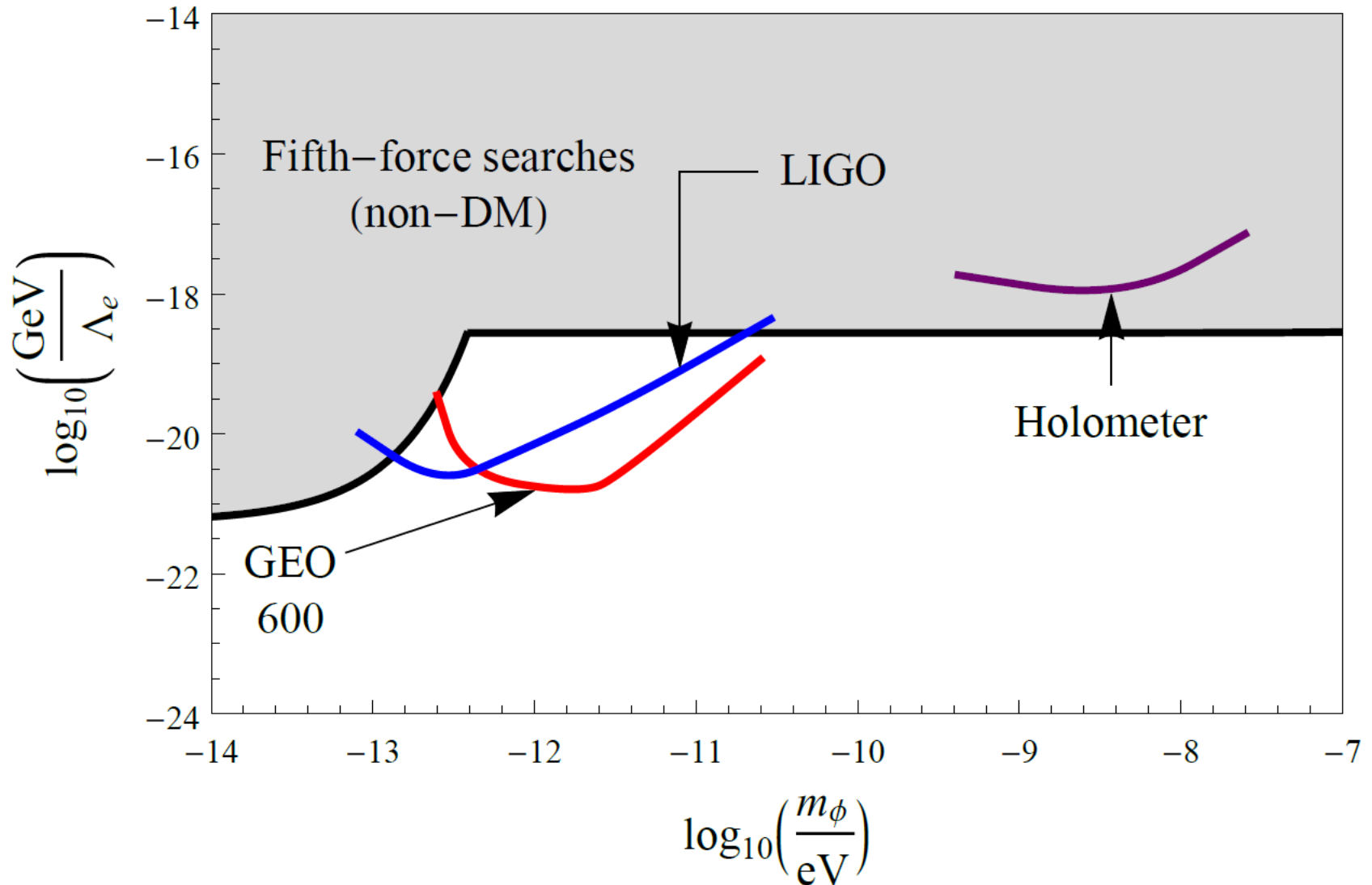
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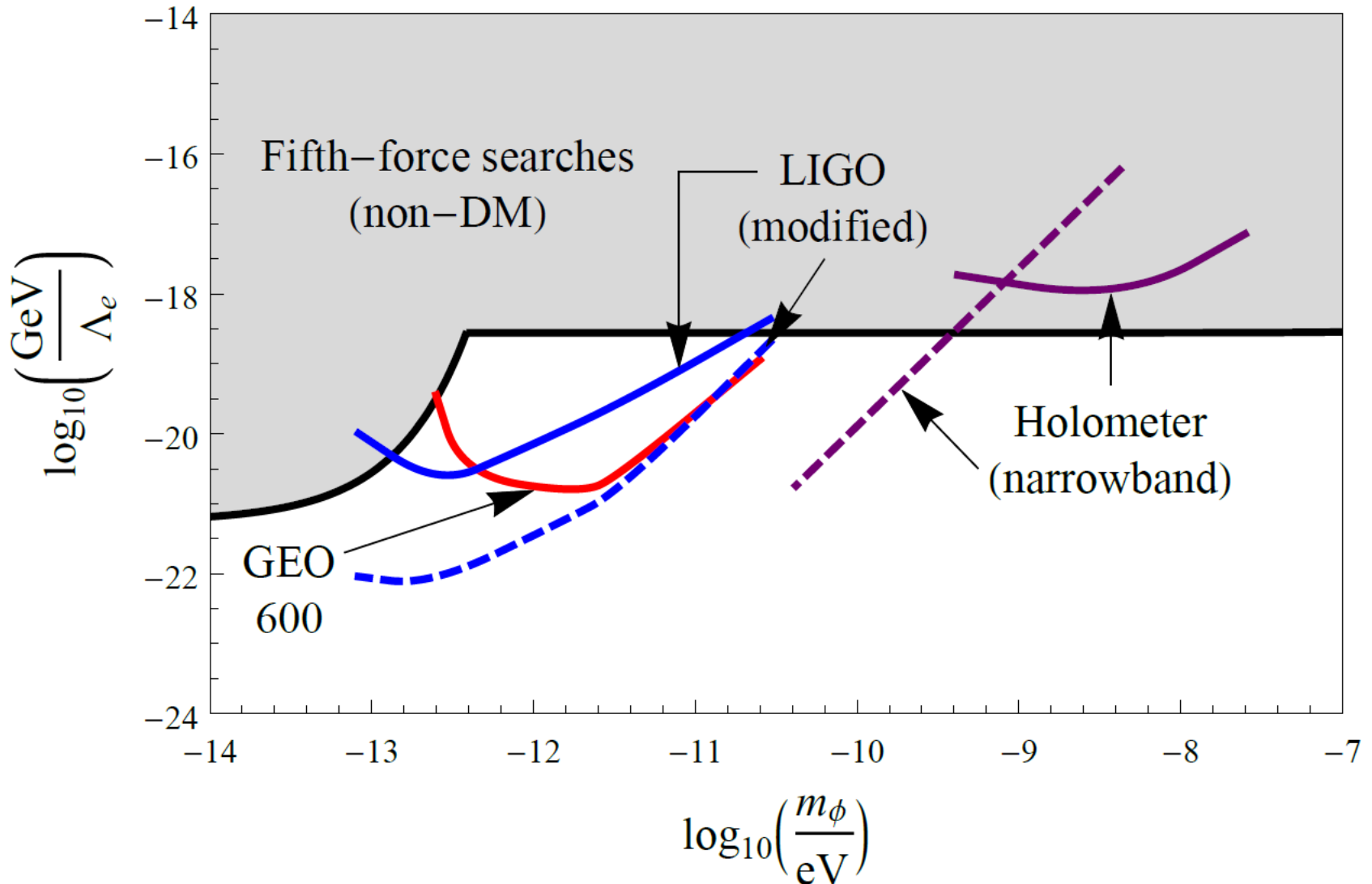


$$\delta(L_x - L_y) \approx \delta(\Delta w)$$

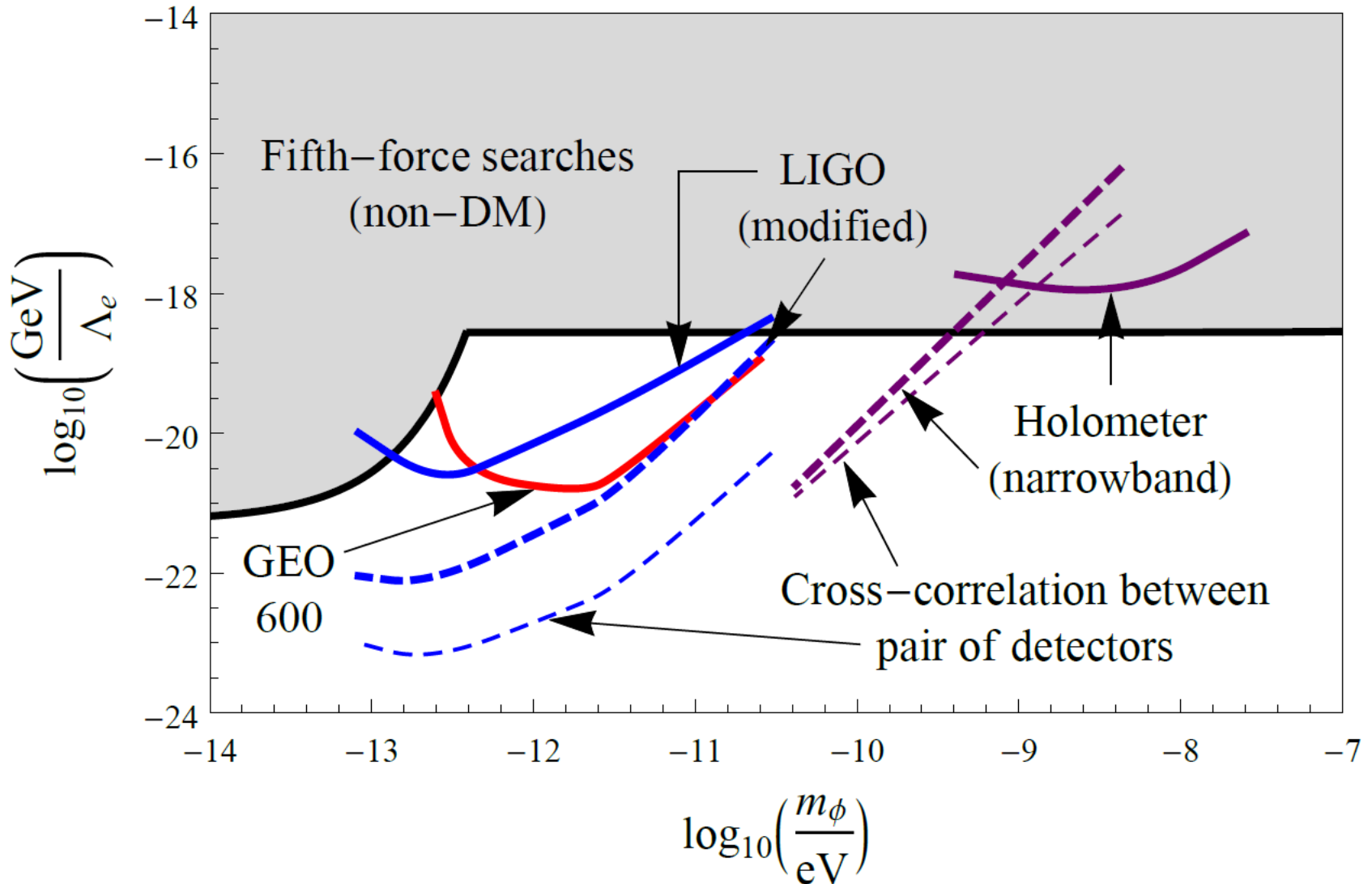
# Linear Interaction of Scalar Dark Matter with the Electron



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# Summary

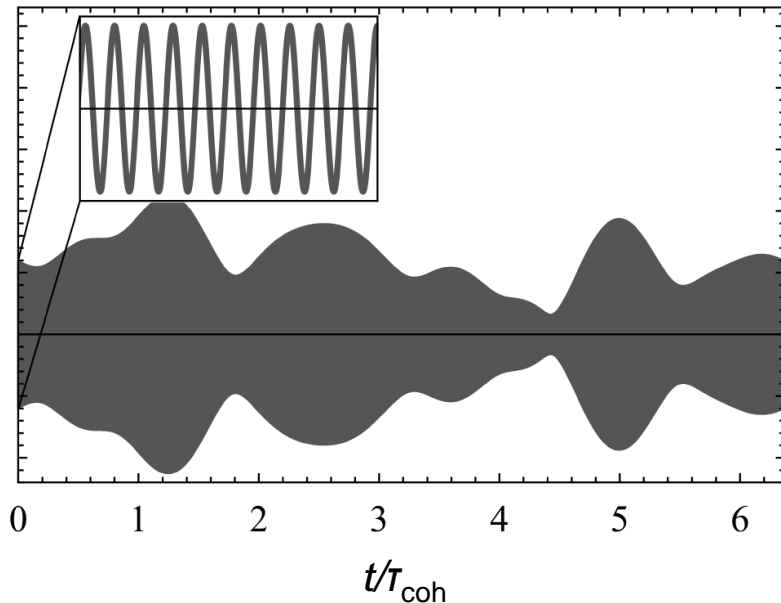
- Existing laser-interferometric gravitational-wave detectors are sensitive probes of scalar dark-matter fields oscillating at audio-band frequencies
- Changing arm mirror thicknesses by  $\sim 10\%$  can greatly boost the sensitivity of Fabry-Perot-Michelson interferometers (LIGO, VIRGO, KAGRA) to dark matter
- (Small-scale) Interferometry experiments can be adapted to perform resonant narrowband searches
- Existing interferometers also sensitive to the passage of macroscopic dark-matter objects through detectors

# Back-Up Slides

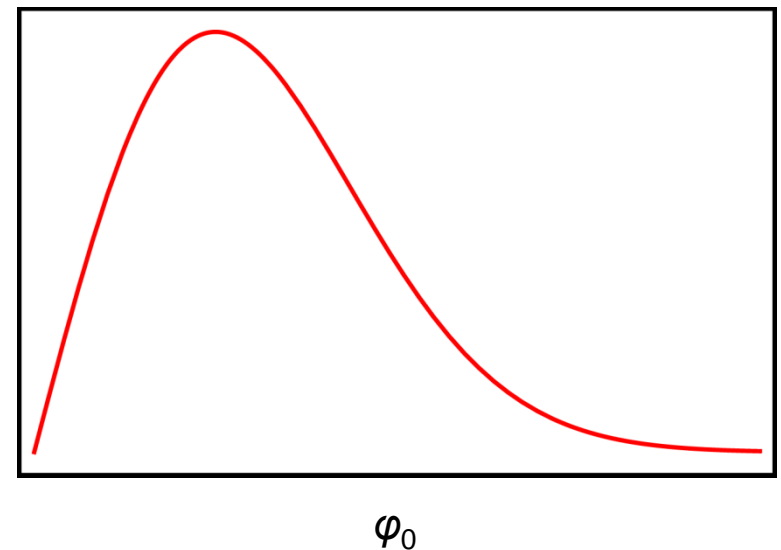
# Temporal Coherence

- *Low-mass spin-0 particles form a coherently oscillating classical field*  $\varphi(t) = \varphi_0 \cos(m_\varphi c^2 t/\hbar)$ , with energy density  $\langle \rho_\varphi \rangle \approx m_\varphi^2 \varphi_0^2/2$  ( $\rho_{\text{DM,local}} \approx 0.4 \text{ GeV/cm}^3$ )
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Evolution of  $\varphi_0$  with time



Probability distribution function of  $\varphi_0$





# Dark Matter-Induced Cosmological Evolution of the Fundamental Constants

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$$\mathcal{L}_f = -\frac{\phi}{\Lambda_f} m_f \bar{f} f \Rightarrow \frac{\delta m_f}{m_f} \approx \frac{\phi_0 \cos(m_\phi t)}{\Lambda_f}$$

$$\phi = \phi_0 \cos(m_\phi t - \underline{\mathbf{p}_\phi \cdot \mathbf{x}}) \Rightarrow \underline{\mathbf{F}} \propto \underline{\mathbf{p}_\phi \sin(m_\phi t)}$$

$$\left. \begin{aligned} \mathcal{L}'_\gamma &= \frac{\phi^2}{(\Lambda'_\gamma)^2} \frac{F_{\mu\nu} F^{\mu\nu}}{4} \\ \mathcal{L}'_f &= -\frac{\phi^2}{(\Lambda'_f)^2} m_f \bar{f} f \end{aligned} \right\} \Rightarrow \frac{\delta\alpha}{\alpha} \propto \frac{\delta m_f}{m_f} \propto \delta\rho_\phi$$

$$\mathbf{F} \propto \nabla \rho_\phi$$

# Dark Matter-Induced Cosmological Evolution of the Fundamental Constants

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Consider quadratic couplings of an oscillating classical scalar field,  $\varphi(t) = \varphi_0 \cos(m_\varphi t)$ , with SM fields.

$$\mathcal{L}_f = -\frac{\phi^2}{(\Lambda'_f)^2} m_f \bar{f} f \quad \text{c.f.} \quad \mathcal{L}_f^{\text{SM}} = -m_f \bar{f} f \quad \Rightarrow \quad m_f \rightarrow m_f \left[ 1 + \frac{\phi^2}{(\Lambda'_f)^2} \right]$$

$$\Rightarrow \frac{\delta m_f}{m_f} = \frac{\phi_0^2}{(\Lambda'_f)^2} \cos^2(m_\phi t) = \frac{\phi_0^2}{2(\Lambda'_f)^2} + \frac{\phi_0^2}{2(\Lambda'_f)^2} \cos(2m_\phi t)$$

$$\rho_\phi = \frac{m_\phi^2 \phi_0^2}{2} \quad \Rightarrow \quad \phi_0^2 \propto \rho_\phi$$

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**'Slow' drifts** [Astrophysics  
(high  $\rho_{\text{DM}}$ ): BBN, CMB]  
**+ Gradients** [Fifth forces]

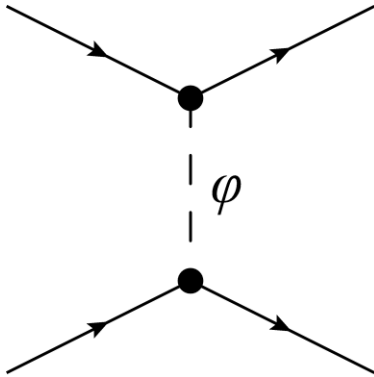
**Oscillating variations**  
[Laboratory (high precision)]

# Fifth Forces: Linear vs Quadratic Couplings

[Hees, Minazzoli, Savalle, Stadnik, Wolf, *PRD* **98**, 064051 (2018)]

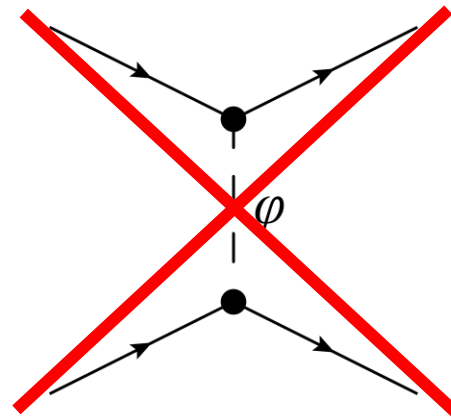
Consider the effect of a massive body (e.g., Earth) on the scalar DM field

Linear couplings ( $\phi\bar{X}X$ )



$$\phi = \phi_0 \cos(m_\phi t) - A \frac{e^{-m_\phi r}}{r}$$

Quadratic couplings ( $\phi^2\bar{X}X$ )



$$\phi = \phi_0 \cos(m_\phi t) \left( 1 - \frac{B}{r} \right)$$



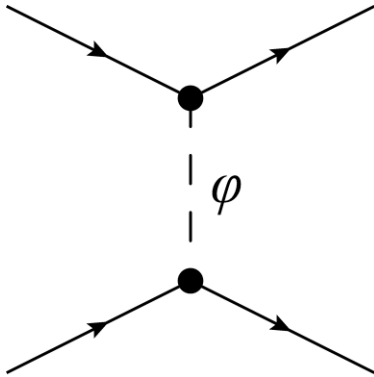
**Gradients + screening/amplification**

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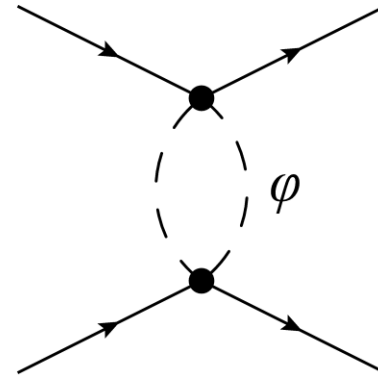
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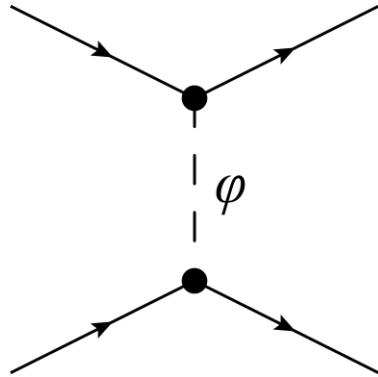
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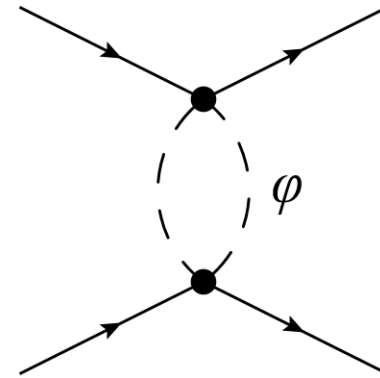


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**Motional gradients:**  $\phi_0 \cos(m_\phi t - \mathbf{p}_\phi \cdot \mathbf{x})$

**“Fifth-force” experiments: torsion pendula, atom interferometry**

Quadratic couplings ( $\phi^2\bar{X}X$ )

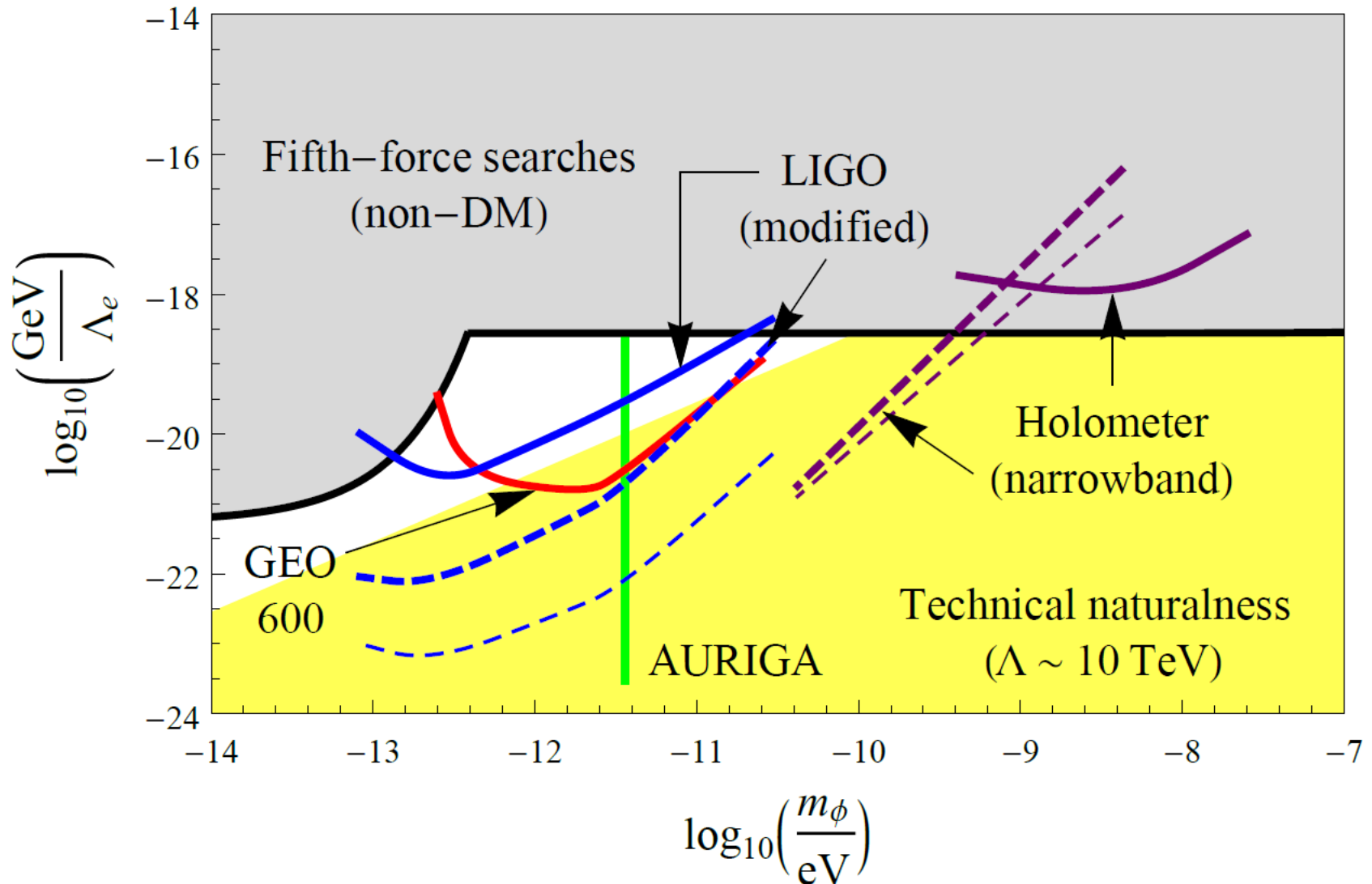


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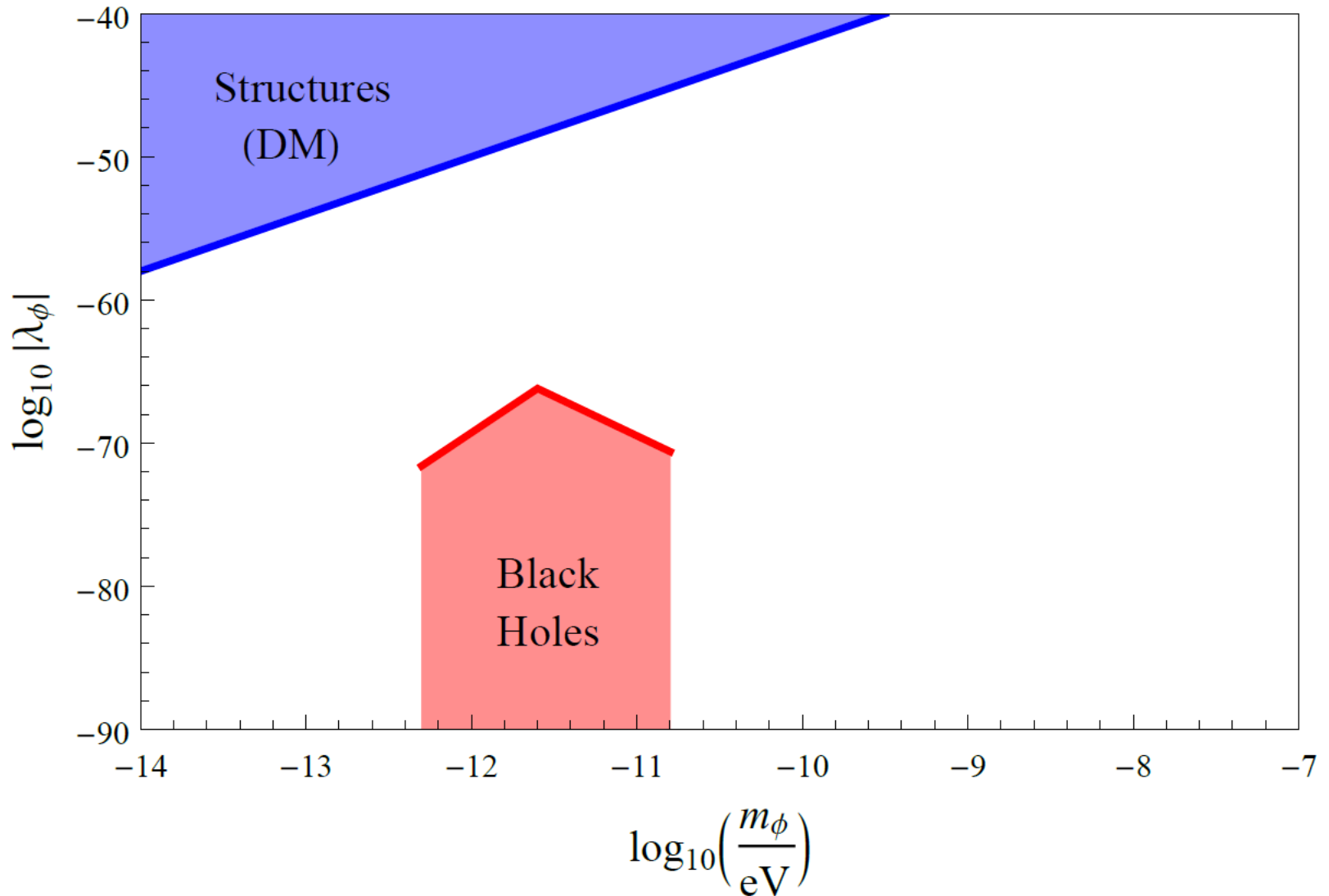


**Gradients + screening/amplification**

# Constraints on Linear Interaction of Scalar Dark Matter with the Electron



# Quartic Self-Interaction of Scalar





# Constraints on Linear Interaction of Scalar Dark Matter with the Higgs Boson

**Rb/Cs constraints:**

[Stadnik, Flambaum, *PRA* **94**, 022111 (2016)]

**2 – 3 orders of magnitude improvement!**

