

1 **EMPIRICAL DAMAGE AND LIQUEFACTION FRAGILITY** 2 **CURVES FROM 2012 EMILIA EARTHQUAKE DATA**

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13 The study focuses on the effects of liquefaction on structures taken from data on about 1,000 private
14 residential masonry buildings located in several municipalities struck by the 2012 Emilia earthquake.
15 Survey data were collected by teams of experts coordinated by the Italian Department of Civil
16 Protection in the immediate post-earthquake emergency phase. They included information on
17 building characteristics and the level and extent of the damage to structural and non-structural
18 components. Furthermore, according to data related to the reconstruction process, information on the
19 liquefaction-induced type and extent of the damage was also collected. Through a comparative
20 analysis of the empirical damage, it was found that liquefaction strongly affected the buildings,
21 confirming its relevance in the damage scenario under specific subsoil conditions. Based on this
22 evidence, the paper proposes a correlation between structural damage and liquefaction when it comes
23 to deriving proper preliminary empirical fragility curves. A suitable parameter to define liquefaction
24 effects at ground level is introduced and correlated to damage grades defined according to the
25 European Macroseismic Scale: EMS-98.

26 27 **INTRODUCTION**

28 Liquefaction may become a major source of seismic risk for structures and infrastructures when loose
29 and saturated sandy soil layers are shallow enough to affect the behavior of buildings via either loss
30 of bearing capacity, potential for lateral spreading, liquefaction induced settlements. Severe structural
31 damage induced by liquefaction has occurred over time during the earthquakes in Anchorage (USA,
32 1964), Niigata (Japan, 1964), Kobe (Japan, 1995), Kocaeli (Turkey, 1999), Christchurch (New

33 Zealand, 2010 - 2011), Emilia-Romagna (Italy, 2012) and, more recently, Hualien (Taiwan, 2018)
34 and Palu (Indonesia, 2018). The effects of liquefaction on the buildings in these areas were
35 catastrophic, with rotations of entire structural complexes leading to a loss of functionality and
36 operative state (Tokimatsu et al. 1996; Yoshida et al. 2001; Cubrinovski 2013; Fioravante et al. 2013;
37 Chiaradonna et al. 2018b). Consequently, a great effort was made to understand building movements
38 on shallow foundations using centrifuge testing and numerical modeling (Balakrishnan and Kutter
39 1999; Kutter et al. 2004; Karamitros et al. 2013; Bray and Dashti 2014, Bouckovalas et al. 2015;
40 Hayden et al. 2015; Allmond et al., 2015; Adamidis and Madabhushi 2018; Hughes and Madabhushi
41 2019). In detail, Dashti and Bray 2013 individualized possible liquefaction-induced displacement
42 mechanisms in three different typologies: (a) volumetric strains caused by water flow in response to
43 transient gradients; (b) partial bearing failure due to soil softening; and (c) soil-structure-interaction-
44 induced building ratcheting during earthquake loading. Nevertheless, most of the research was
45 devoted to soil-structure-interaction studies on individual buildings, and these are strictly dependent
46 on the specific case under study, e.g., the type of structure and foundation system (Luque and Bray
47 2017). Very little research has been conducted on fragility curves related to soil liquefaction. Zhang
48 et al. (2008), however, derived fragility functions for different classes of typical bridges in California
49 when subjected to seismic shaking or liquefaction-induced lateral spreading. Lopez-Caballero and
50 Khalil (2018) assessed numerically the effect on a levee of the liquefaction-induced settlement of the
51 soil foundation in terms of analytical fragility curves constructed on the basis of a nonlinear dynamic
52 analysis. Furthermore, using a database of buildings affected by liquefaction during the 2010
53 Mexicali, 2010 New Zealand and 2011 Japan earthquakes, and with reference to building damage,
54 Cazares et al. (2012) proposed vulnerability functions that are obtained as a result of a combination
55 of the functions defined as empirical and those obtained through damage statistics.

56 Several approaches have been developed in the literature for correlating types of damage with seismic
57 intensity parameters through a fragility curve. There are methods based on simplified mechanism-
58 based procedures (Cosenza et al. 2005; Borzi et al. 2008), capacity spectrum methods (Iervolino et
59 al. 2007; Del Gaudio et al. 2015), and displacement-based methods (Calvi 1999; Crowley et al. 2004;
60 Borzi et al. 2008). There is, however, also a group of methods based on empirical observations of the
61 expected damage suffered during seismic events (Rota et al. 2008, Del Gaudio et al. 2017).

62 In the current study, the structural and non-structural damage caused to masonry buildings is analyzed
63 and empirical fragility curves are produced using observational damage data collected after the 2012
64 Emilia earthquake (section 2). Starting from an analysis of the structural damage described in AeDES
65 forms (Baggio et al. 2007), it has been possible to carry out both a qualitative and quantitative analysis
66 of the observed damage (section 3). In this way, the damage has been subsequently correlated with a

67 new parameter characterizing the liquefaction phenomenon. Different methodologies for estimating
68 fragility functions from data on damage grades and the parameters of potential liquefaction are
69 illustrated, discussed and applied to the database, leading to the derivation of EMS-98-based fragility
70 curves (section 4).

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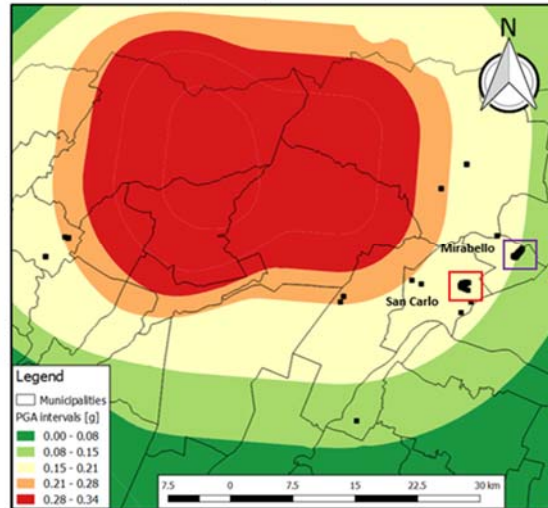
73 **RECONSTRUCTION PROCESS AND DATA COLLECTION ON DAMAGED BUILDINGS**

74 This section presents the reconstruction procedure and data collected after the 2012 Emilia-Romagna
75 earthquake. At the beginning, reconstruction process ordinances involved residential buildings:
76 Ordinance n. 29, 2012 for temporarily or partially unusable buildings; Ordinance n. 51, 2012 for
77 unusable buildings that have suffered severe damage; and Ordinance n. 86, 2012 for severely
78 damaged buildings requiring a seismic strengthening intervention or demolition and reconstruction.
79 For the first time in Italy, it was also possible to obtain grants for improving the foundation soil. An
80 increased economic contribution for reconstruction up to 15% of the total grant was provided in the
81 areas affected by liquefaction. Note that a specific documentation, aiming at certify liquefaction
82 effects, was required to obtain such extra funding. Moreover, microzonation studies were carried out
83 in the areas struck by the seismic events in order to identify and delimit areas with homogeneous
84 seismic behavior, distinguishing the areas susceptible to the amplification of seismic motion and those
85 susceptible to liquefaction.

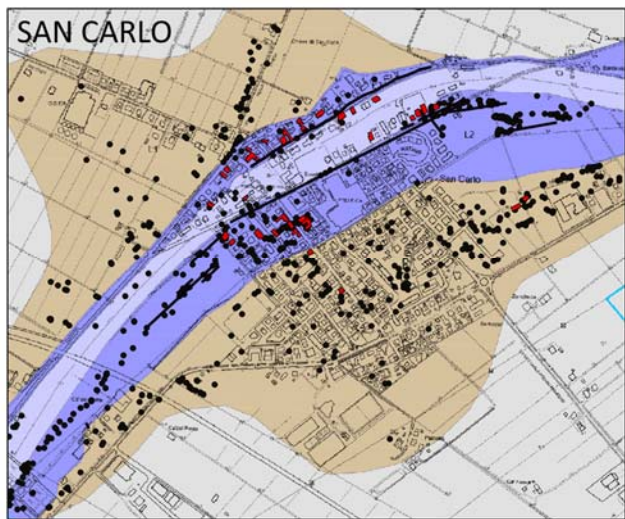
86 Several municipalities were affected by liquefaction, including: Cavezzo; Bondeno; Cento; Pieve di
87 Cento; the hamlet of San Carlo in Sant'Agostino; and Mirabello (Gruppo di lavoro RER, 2012). The
88 data related to liquefaction sites were collected and subsequently georeferenced in the GIS
89 environment (Morga et al. 2018; Spacagna et al. 2018). Figure 1a shows the spatial distribution of
90 cases affected by liquefaction (black squares), with a ShakeMap superimposition related to the event
91 of May 20, 2012.

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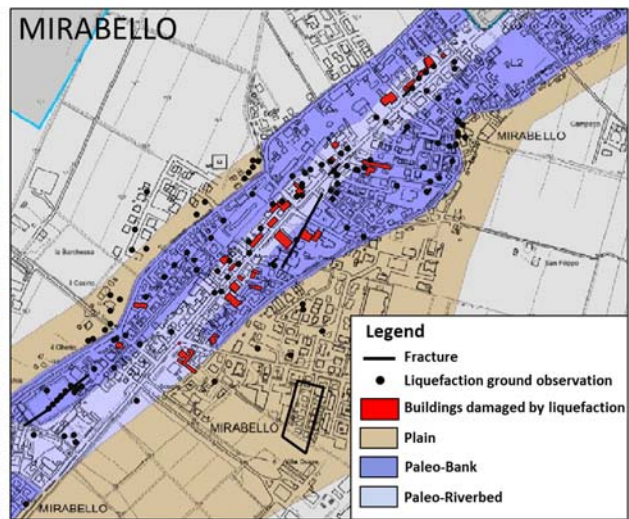
INGV ShakeMap: 20 May 2012 02:03:50 UTC M 5.9



(a)



(b)



(c)

93 **Figure 1:** ShakeMap (<http://shakemap.rm.ingv.it/shake/index.html>) representing the spatial
94 distribution of peak ground acceleration (PGA) and the buildings affected by liquefaction (a); San
95 Carlo (b) and Mirabello (c) dataset with geological maps and liquefaction evidences.

96 The peak ground acceleration (PGA) in the area under investigation ranged between 0.0 to 0.34 g.
97 The overlap with the spatial distribution of the liquefaction cases allowed us to see that most buildings
98 fall within an acceleration range of 0.15 to 0.21 g. The distribution of the sites affected by liquefaction
99 is concentrated in the areas related to the municipalities of San Carlo and Mirabello (Modoni et al.
100 2019). Since most of the buildings affected by liquefaction are located in these two municipalities,
101 the present study will only refer to them. Figures 1b and 1c show a comparison between the
102 distributions of liquefaction evidences and the geological maps of the two considered municipalities.
103 It can be observed that most of the liquefaction manifestations occurred along paleo-river beds and

104 paleo-channel systems originating from the depositional activity of the Reno river (Facciorusso et al.
 105 2012).

106 In order to investigate the effects of liquefaction on the behavior of structures, data related to masonry
 107 residential buildings located in San Carlo and Mirabello were collected. In detail, two sets of samples
 108 were identified and divided into two classes: a) a sample of structures not damaged by liquefaction
 109 (these structures may rest on soils that did not liquefy or that liquefy at depth without any consequence
 110 for the foundations; in the following these cases will be referred to as structures not damaged by
 111 liquefaction – NDL); and b) a sample of structures damaged by liquefaction (DL). Table 1 shows the
 112 frequencies of the samples.

113

114 **Table 1:** Number of masonry buildings from ISTAT 2011 and for NDL – DL samples.

		MUNICIPALITY		Total
		MIRABELLO	SAN CARLO	
No. of masonry buildings	Census			
	(ISTAT2011)	675	439	1114
	NDL buildings	277	373	650
	DL buildings	55	46	101

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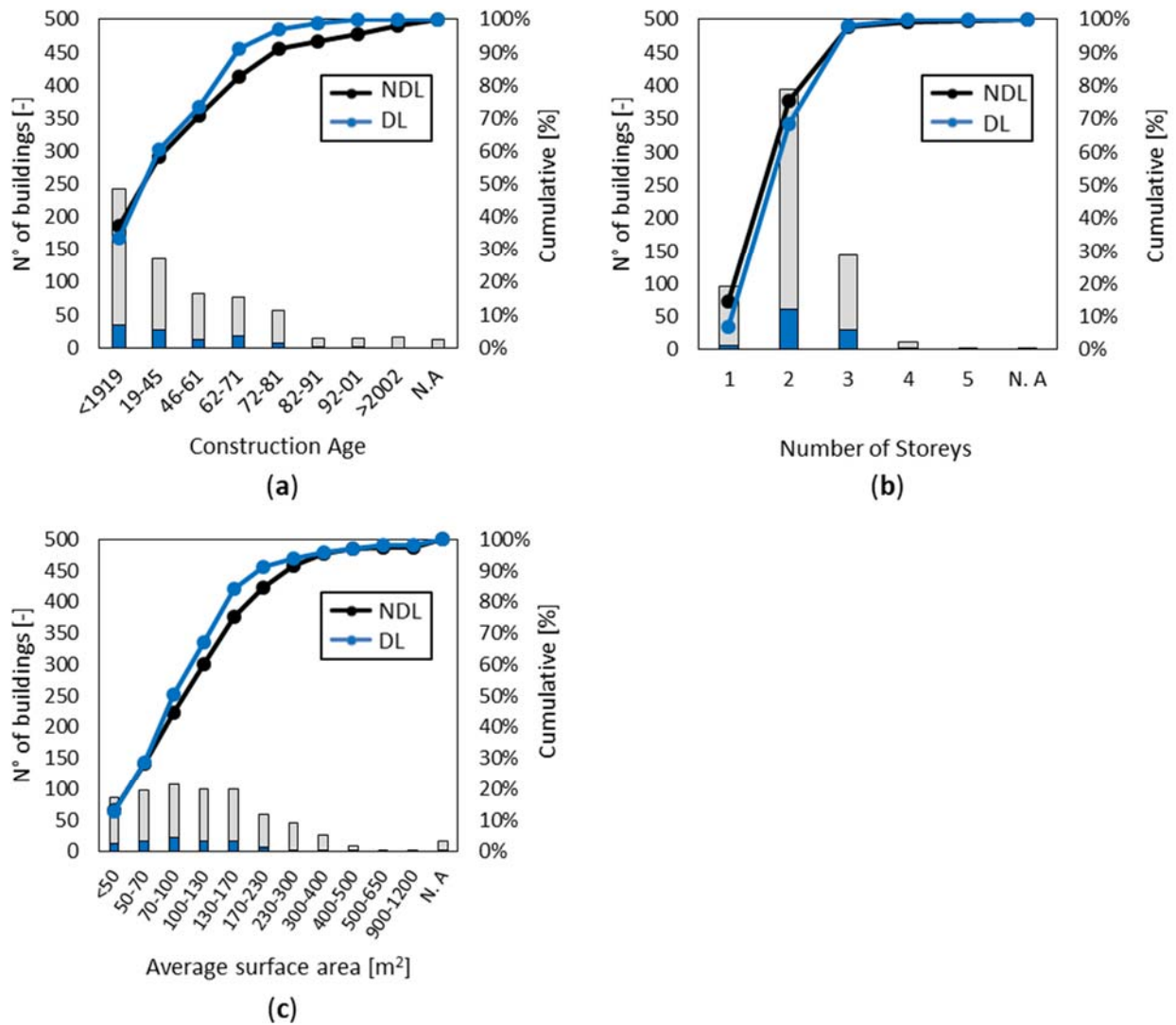
116 The number of buildings was also compared with the masonry residential buildings contained in the
 117 census data (ISTAT 2011). It was assumed that buildings without a usability request (1114-650-101
 118 = 363) did not suffer any structural damage. This hypothesis is reliable since requests for the
 119 evaluation of building usability were made by owners via the AeDES forms after the earthquake.
 120 Accordingly, the lack of data obtained from in situ inspections mainly means that no damage was
 121 suffered by these buildings.

122 The data contained in the AeDES forms were used to make an initial comparison between the NDL
 123 and DL buildings, in terms of construction age, number of floors, average story surface area, and
 124 masonry quality. These macro-parameters may greatly affect building behavior in case of seismic
 125 events and were thus analyzed to verify if they play a crucial role in defining the different empirical
 126 damage detected in the NDL and DL buildings. Indeed, the construction age allows defining the
 127 building type of design (i.e., for gravity loads only or with reference to obsolete or current seismic
 128 design rules), number of floors and surface area strongly affect the structural fundamental period of
 129 vibration and thus its behavior under seismic actions, and masonry quality determine the capacity of
 130 structural components to sustain horizontal actions provided by seismic events.

131 Figure 2 reports the frequency and cumulative percentage of the two classes of structure, i.e., NDL
132 and DL (751 buildings) as a function of the construction age, number of stories and average story
133 surface area. The construction age was classified according to eight periods (before 1919, between
134 1919 and 1945, 1946-1961, 1962-1971, 1972-1981, 1982-1991, 1991-2001, and after 2001), as
135 commonly adopted in the census data (and the AeDES forms). The trend of the cumulative percentage
136 was similar. Figure 2a shows that 82.6% of the NDL building dataset (corresponding to 455 buildings)
137 and 73.3% of the DL building dataset (corresponding to 92 buildings) were built before 1971. The
138 graph in Figure 2b shows that about 98% of the buildings in the datasets (corresponding to 635
139 buildings for the NDL class and 99 buildings for the DL class) had between one and three stories.
140 Finally, Figure 2c highlights that about 40% of the buildings (corresponding to 365 buildings for the
141 NDL and 63 buildings for the DL classes) had an average story surface area between 70-100 and 170-
142 230 m².

143 Consequently, it was possible to assume that the two classes are comparable in terms of the macro-
144 parameters affecting the structural vulnerability to seismic action. Moreover, the data related to the
145 quality of the masonry revealed a percentage of buildings of good quality and with regular texture
146 masonry (77% and 61% for the NDL and DL classes, respectively).

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148

149 **Figure 2:** Distribution and cumulative percentage of the no damaged by liquefaction ND and
 150 damaged by liquefaction DL buildings as a function of the construction age (a), number of stories
 151 (b) and average story surface area (c).

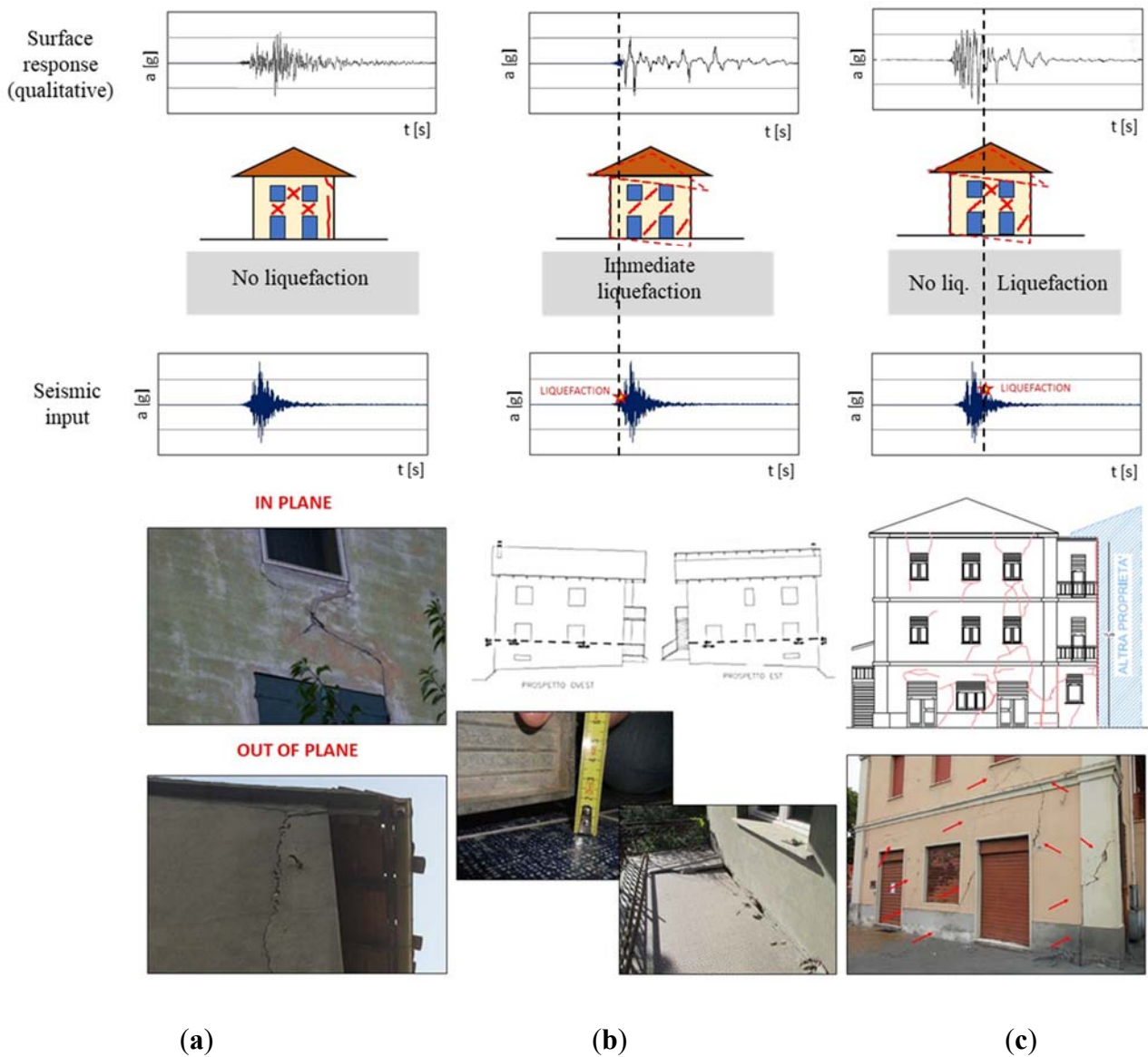
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154 **ANALYSIS OF LIQUEFACTION-INDUCED DAMAGE**

155 In the post-Emilia earthquake reconstruction process, documentation was required to: illustrate the
 156 damage sustained; describe the interventions needed to achieve building usability; and quantify the
 157 financial support sought from the government. The documentation related to the DL buildings shows
 158 that the typical damage caused by foundation settlement largely occurred in buildings that were also
 159 damaged by inertial effects (i.e., seismic effects on the superstructure). In particular, according to the
 160 observed damage, it can be assumed that in this case liquefaction was activated at different stages of

161 the seismic event at different sites, even if relatively close. The different behavior mostly depends on
 162 local conditions in terms of liquefiable soil layer density and thickness.



163

164

165 **Figure 3:** Empirical damage observed in the case of: no soil liquefaction (a); early liquefaction
 166 activation (b); combined inertial and liquefaction effects (c).

167 Figure 3 schematically represents three possible conditions related to the absence of liquefaction
 168 (Figure 3a), or the attainment of liquefaction at different stages (figures 3b, c). The figure also reports
 169 the type of structural damage commonly detected in Mirabello and San Carlo in such three cases. In
 170 the case of no liquefaction (Figure 3a), failures due to the out-of-plane mechanisms of walls or in-
 171 plane diagonal cracks (inclined at about $\pm 45^\circ$) are commonly detected in the structures. In the case of
 172 seismic events that suddenly activate liquefaction or in the case of liquefaction activated for
 173 accelerations much lower than the PGA (Figure 3b), the effects are mainly related to liquefaction.
 174 The common failures in such a case are rigid building rotations, with a relevant loss of functionality

175 of the structure, as well as one-way diagonal cracks due to foundation settlements. Damage caused
176 by inertial forces is mostly absent, because liquefaction works as a natural isolation system for the
177 superstructure. Finally, Figure 3c shows the combined effects of soil liquefaction and inertial forces
178 on the buildings, which are due to significant inertial forces on the superstructure and liquefaction-
179 induced damage. With the current state of knowledge, it is very difficult to predict when liquefaction
180 is activated, because it is very dependent on the characteristics of the soil.

181

182 **Comparative analysis of empirical damage: NDL vs. DL buildings**

183 A comparative analysis of the previously described damage to the NDL and DL buildings is carried
184 out herein using data from AeDES forms. In particular, the data refer to the severity and extent of the
185 damage detected in: vertical structural components (VS), (e.g., masonry vertical bearing walls); floors
186 (F); stairs (S); roofs (R); and infill-partitions (IP). The AeDES forms identify four damage levels for
187 each structural or non-structural component: no damage, D0; slight damage, D1; medium-severe
188 damage, D2-D3; and very heavy damage or collapse, D4-D5. The observed damage level definition
189 is based on the European Macroseismic Scale EMS98, integrated with the definitions used in the
190 GNDT survey form, GNDT 1993, Baggio et al. 2007, (Grünthal 1998).

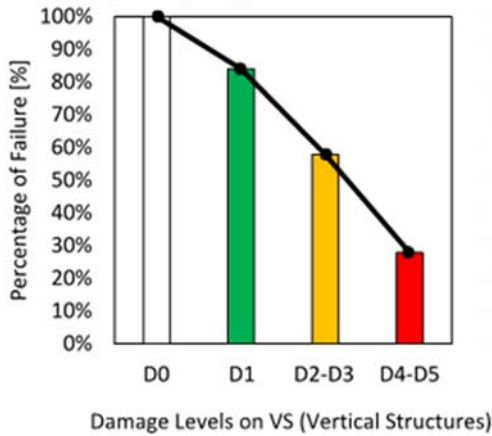
191 The damage extent is reported as follows: damage extent less than $1/3$; between $1/3$ and $2/3$; and
192 greater than $2/3$ of the storey components. Figure 4 shows a comparison between the DL and NDL
193 buildings in terms of cumulative damage probability matrices (C-DPMs) that represent the percentage
194 of buildings that reaches or exceeds the j -th level of damage in VSs.

195 The figure clearly shows that the DL-class buildings suffered damage to the VSs that was more severe
196 than that observed in the NDL sample. The data related to other structural or non-structural
197 components are summarized in Table 2 and confirm that the severity and extent of the damage
198 detected in the DL buildings was greater than that in the NDL buildings, especially with reference to
199 stairs.

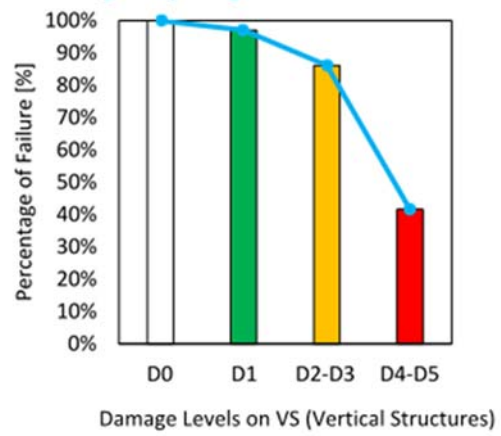
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201

No Damaged by Liquefaction – NDL class



Damaged by Liquefaction – DL class



(a)

(b)

202

Figure 4: Vertical structure (VS) - C-DPMs: NDL class (a); DL class (b).

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204

Table 2: Cumulative percentage of failure expressed as a function of the damage levels in the other structural components for both the NDL and DL samples.

205

	D1		D2-D3		D4-D5	
	NDL	DL	NDL	DL	NDL	DL
VS	84.0%	97.0%	57.8%	86.1%	27.8%	41.6%
F	62.5%	84.2%	35.7%	47.5%	22.8%	26.7%
S	36.6%	66.3%	27.2%	44.6%	21.7%	29.7%
R	52.0%	72.3%	35.7%	48.5%	24.3%	34.7%
IP	70.2%	92.1%	35.5%	51.5%	20.9%	26.7%

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Effects of structural vulnerability on empirical damage

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In order to analyze the effects of structural vulnerability on the empirical damage detected in the NDL and DL buildings, different subsets of buildings for each class are defined in this section according to data related to vertical and horizontal structure types. In particular, Section 3 of the AeDES forms (Baggio et al. 2007) identifies five vertical structure types: a) unknown; b) masonry with an irregular layout or bad quality without ties; c) masonry with an irregular layout or bad quality with ties; d) masonry with a regular layout or good quality without ties; and e) masonry with a regular layout or good quality with ties. Furthermore, six horizontal structure types are reported: a) unknown; b) vaults with no ties; c) vaults with ties; d) beams with flexible slabs; e) beams with semi-rigid slabs; and f) beams with rigid slabs. Neglecting unknown structural types, the combination of vertical and

217 horizontal structures leads to 20 masonry subsets of buildings, representing different vulnerability
 218 categories. Table 3 summarizes the number of buildings in each subset related to the NDL and DL
 219 classes, respectively. Note that the total number of buildings is slightly lower than that reported in
 220 Table 1 because, in a few cases, the “unknown” structural type was selected in the AeDES form. A
 221 mean empirical global damage factor, μ_D , has been computed for each subset as the mean value of the
 222 global damage related to each building, $\mu_{D,i}$, defined as:

$$\mu_{D,i} = \sum_j D_j \gamma_j \quad (1)$$

223 where D_j is the damage level and extent related to the j^{th} component (j=VS, F, S, R and IP), and γ_j
 224 is a coefficient, ranging between 0 and 1, accounting for the weight of the damage on the j^{th}
 225 component. D_j is computed as:

$$D_j = \frac{\sum_{D=D0}^{D5} D \cdot e_{k,D}}{5} \quad (2)$$

226 where D is the damage level (D0=0, D1=1, D2-D3=2.5, D4-D5=4.5) and $e_{k,D}$ is a coefficient
 227 accounting for the damage extent of the damage level D ; $e_{k,D}$ can assume three values depending on
 228 the percentage of the building affected by damage, k : $k < 1/3$, $e_{k,D} = 0.17$; k between $1/3$ and $2/3$,
 229 $e_{k,D} = 0.5$; and $k > 2/3$, $e_{k,D} = 0.83$) (Dolce et al. 2001).

230

231 **Table 3:** Number of buildings in 20 subsets of NDL and DL buildings according to the horizontal
 232 and vertical structure type.

Vertical structure (masonry walls) Horizontal structure (floor and beams)	Masonry structural units				Total
	Irregular layout or bad quality		Regular layout or good quality		
	w/o tie rods or tie beams	with tie rods or tie beams	w/o tie rods or tie beams	with tie rods or tie beams	
Vaults without tie rods	1 (-)	- (-)	2 (-)	2 (-)	5 (-)
Vaults with tie rods	- (-)	- (-)	3 (-)	5 (1)	8 (1)
Beams with flexible slabs	53 (16)	9 (1)	187 (19)	28 (4)	277 (40)
Beams with semi-rigid slabs	24 (8)	1 (-)	107 (18)	32 (7)	164 (33)
Beams with rigid slabs	2 (2)	2 (-)	40 (5)	96 (8)	140 (15)
Total	80 (26)	12 (1)	339 (42)	163 (20)	594 (89)

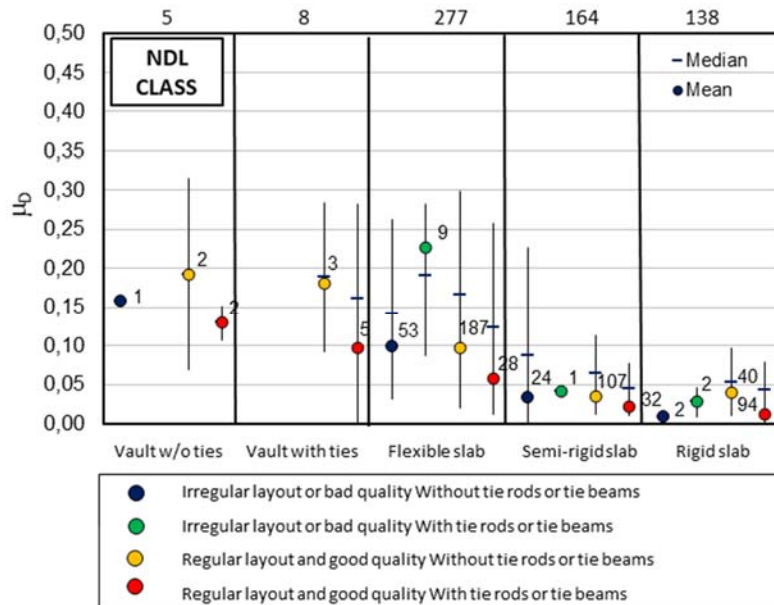
233 * Black for No Damaged by Liquefaction - NDL subsets; blue for Damaged by Liquefaction- DL
234 subsets.

235

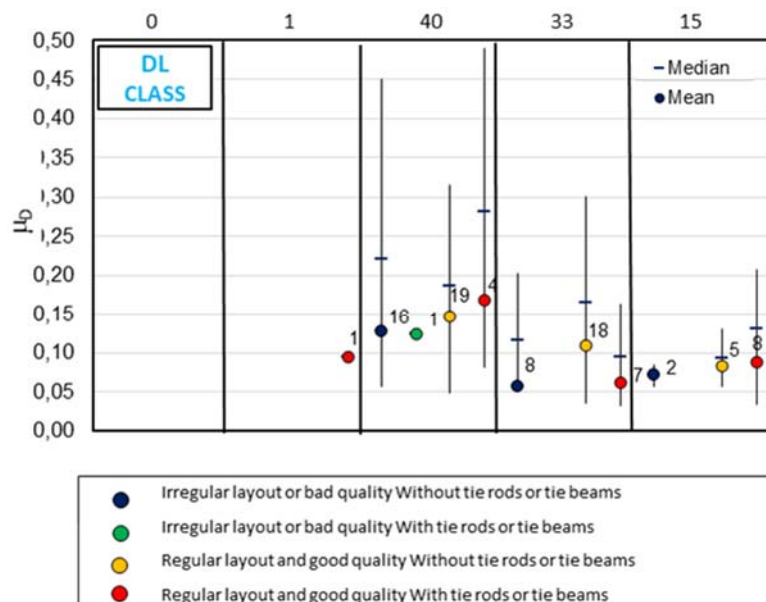
236 Figure 5 reports an overall comparison between the mean damage, μ_D , suffered by the different
237 subsets of data for the NDL (Figure 5a) and DL (Figure 5b) buildings, respectively. The number of
238 buildings required to compute the mean global damage of each subset is also reported in Figure 5 as
239 well as the median value of damage for each subset and the dispersion (i.e. 16th and 84 percentile).

240 Figure 5a shows a very similar value of μ_D (i.e., in the range 0.10 -0.20) for masonry buildings with
241 vaults with or without tie rods or with flexible slabs. However, it should be noted that the data for
242 buildings with vaults are very limited, and this may affect the results. As expected, the mean empirical
243 global damage decreases in the case of buildings with a horizontal structure characterized by semi-
244 rigid or rigid slabs, with values lower than 0.10 for each building subset. This result is consistent with
245 the favourable role of such structural components in the global behavior against seismic action.
246 Indeed, they allow the transfer of seismic actions on VSs leading to a desirable so-called “box-type”
247 building behavior. Furthermore, there is clear evidence of the benefits provided by a regular layout
248 and good quality masonry compared to an irregular layout and bad quality stonework. Accordingly,
249 a clear trend can be observed between the parameters influencing structural vulnerability to lateral
250 actions and the mean empirical global damage. In contrast, Figure 5b clearly shows that the trend
251 between the mean empirical global damage and the vertical/horizontal structural types is less evident
252 than in the NDL building class. This is probably because the liquefaction may induce localized effects
253 or the global rotation of the buildings that are less affected by those structural characteristics.
254 Furthermore, the mean empirical global damage peak value is greater in the DL class buildings than

255 in the NDL subsets: $\mu_D = 0.27$ versus $\mu_D = 0.20$. However, it should be noted that the number of
 256 buildings in each data subset for the DL class is significantly lower than in the NDL subsets and this
 257 may influence the results.



(a) No Damaged by Liquefaction – NDL class



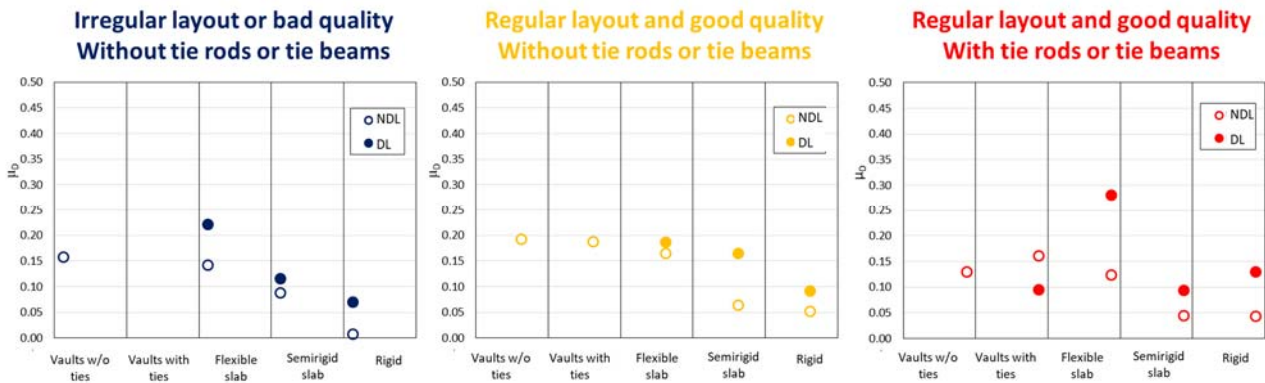
(b) Damaged by Liquefaction – DL class

258 **Figure 5:** Mean empirical damage as a function of the vulnerability categories of buildings.

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260 In order to better investigate the influence of masonry texture and quality on the global mean
 261 empirical damage, Figure 6 reports a direct comparison of their trend for the NDL and DL building

262 subsets. In general, the figure shows that the stiffer the horizontal structure is, the better the global
 263 structural behavior for both the NDL and DL data subsets. Furthermore, the damage detected to the
 264 DL buildings was always greater than that in the NDL buildings.



265
 266 **Figure 6:** Mean empirical damage; comparison between the No Damaged by Liquefaction – NDL
 267 and Damaged by Liquefaction – DL data subsets.

268
 269 **Prediction of repair costs**

270 The mean empirical damage is a measure of the global damage detected in a building, but may not be
 271 an adequate measure when it comes to making a prediction of losses, because it does not correlate the
 272 damage caused to each building component with its economic value. Indeed, recent studies
 273 demonstrated that the repair costs are strongly affected by nonstructural components rather than
 274 structural ones (De Martino et al. 2017, Del Vecchio et al. 2018). Consequently, in this section, in
 275 order to focus on the impact of liquefaction in terms of economic losses, a different parameter is used
 276 to compute these losses, in particular a measure that is related to the aftermath of the L’Aquila event
 277 (De Martino et al. 2017). This parameter, named as the damage factor (DF), has been calibrated on
 278 data costs related to the reconstruction process and directly accounts for the real losses computed by
 279 practitioners involved in the estimation of repair costs (Di Ludovico et al. 2016a and b). The DF is
 280 directly computed using the data reported in Section 3 of the AeDES forms, but depends on the D_j
 281 and γ_j values specifically calibrated for loss analyses. Furthermore, a relationship between the DF and
 282 actual repair costs (ARC) induced by damage (or between the DF and an a-dimensional cost ratio
 283 obtained as a ratio between the ARC related to the building and the average building demolition and
 284 reconstruction cost - building repair cost ratio, Cr) is reported in De Martino et al. 2017 and recalled
 285 as follows:

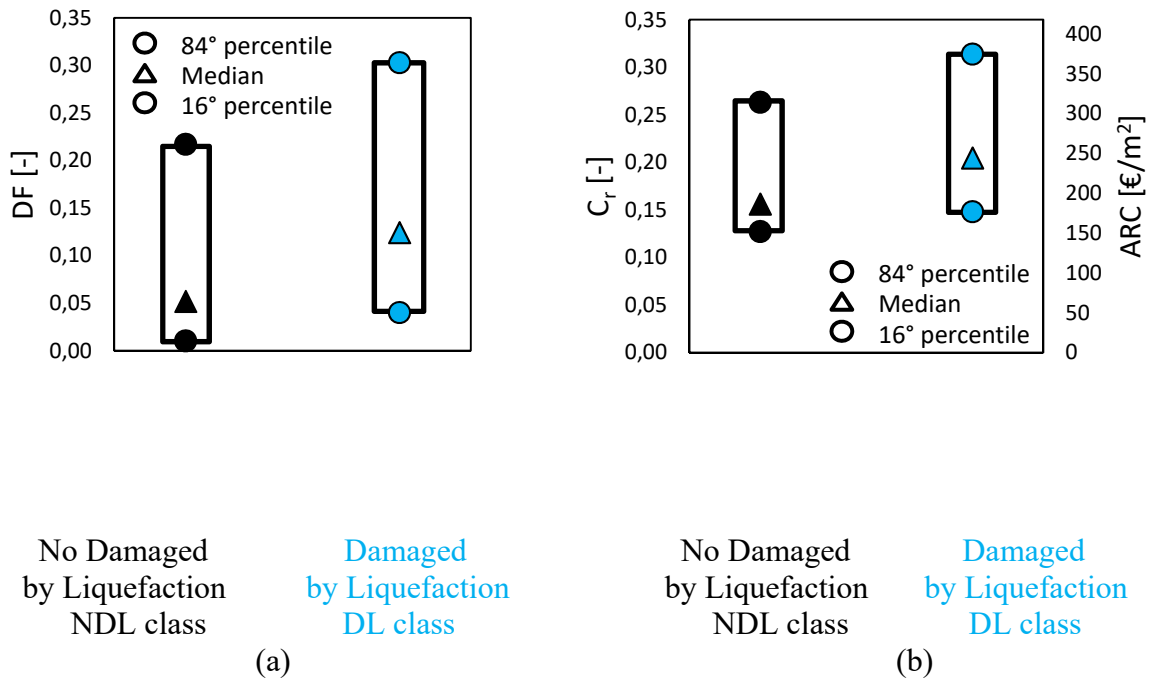
$$ARC = 143 + 849 DF - 277 DF^2 \quad (3)$$

$$C_r = 0.12 + 0.71 DF - 0.23 DF^2$$

286

287 Figures 7a,b report the DF with a median and 16th and 84th percentiles, as well as the relevant ARC
 288 and C_r values for the NDL and DL buildings. The analysis refers to NDL and DL buildings classes
 289 rather than the subsets of data analysed in the previous section because it aims capturing the effects
 290 of liquefaction on costs rather than structural vulnerability parameters on costs.

291 The median DFs are 0.052 and 0.124, corresponding to a median C_r of 0.156 and 0.204 for the NDL
 292 and DL classes, respectively. Accordingly, the effects of liquefaction may lead, based on the
 293 predictions of such a model, to an increase in the repair costs of about 30% in cases where liquefaction
 294 was not observed.



295

296 **Figure 7:** Median, 16th and 84th percentile DFs for the NDL and DL classes (a); building repair cost
 297 ratio C_r and actual repair costs ARC (b) for the NDL and DL classes.

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300 **EMPIRICAL FRAGILITY CURVES**

301 Fragility curves related to seismic events define the exceeding probability of a given damage grade
 302 (DG) as a function of a ground motion intensity measure (IM). The IM may be a macroseismic
 303 parameter or, as commonly adopted in recent studies, is represented by a ground motion intensity
 304 record in terms of various peak ground parameters: acceleration (PGA); velocity (PGV); and
 305 displacement (PGD). A commonly used functional form and regression technique to produce fragility
 306 curves is the lognormal cumulative distribution function:

$$P[DG \geq dg|IM] = \Phi\left(\frac{\ln(IM) - \mu}{\sigma}\right) \quad (4)$$

307 where $\Phi(\cdot)$ is the standard normal cumulative distribution function (CDF), μ is the logarithmic mean
 308 and σ is the logarithmic standard deviation defining the lognormal distribution. This returns values
 309 between 0 and 1 and is particularly suitable for fitting data clustered around low values, as is
 310 commonly the case in fragility analyses (Rossetto et al. 2013). The parameters σ and μ can be
 311 determined according to the nonlinear least squares estimation (LSE) methodology, which aims to
 312 derive the most accurate description of data, or by means of the maximum likelihood estimation
 313 (MLE) approach (e.g., Baker 2015), which is an iterative method to determine the parameters
 314 maximizing the likelihood function:

$$Likelihood = \prod_{j=1}^m \binom{N_j}{n_j} p_j^{n_j} (1 - p_j)^{N_j - n_j} \quad (5)$$

315 where p_j is the probability that n_j number of buildings over N_j shows damage that is greater than or
 316 equal to a threshold DG_i in the j^{th} bin of the IM.

317 Another available functional form used in the literature is the exponential model (Rossetto and
 318 Elnashai 2003, Amiri et al. 2007).

$$P[DG \geq dg|IM] = 1 - e^{-\alpha IM^\beta} \quad (6)$$

319 The parameters α and β can be determined according to the LSE or MLE methodology. In the
 320 following, both functional forms (i.e. lognormal and exponential) are used, along with the nonlinear
 321 LSE and MLE methodologies. In order to produce fragility curves that take into account the
 322 liquefaction phenomenon, it is necessary to define suitable DGs and IMs.

323

324 **Damage grades**

325 The empirical data collected in Section 4 of the AeDES forms (Baggio et al. 2007) were used to
 326 define the buildings' DGs. In particular, the DG of each building was determined by accounting for
 327 the level and extent of the damage to the VS component, and five damage grades were assumed based

328 on the European Macroseismic Scale, EMS-98 (Grünthal 1998). The criterion used to convert the
329 damage levels to DGs was that reported in Dolce et al. 2017 and is summarized in Table 4.

330 **Table 4:** DG (EMS-98) and corresponding damage levels to VSs according to the AEDES survey
331 forms (Baggio et al. 2007).

Vertical structures			
EMS-98 damage		AeDES damage	
Damage grade	Damage description	Damage level	Extent
DG1	<i>Fine cracks in plaster over frame members or in walls at the base.</i>	D1	<1/3 1/3-2/3 >2/3
DG2	<i>Cracks in the columns and beams of frames and in structural walls.</i>	D2-D3	<1/3
		D2-D3 and D1	<1/3 and 1/3-2/3
			<1/3 and >2/3
DG3	<i>Cracks in the columns and beam-column joints of frames at the base and at the joints of coupled walls.</i>	D2-D3 and D1	1/3-2/3 and <1/3
		D2-D3	1/3-2/3 >2/3
		D4-D5	<1/3
		D4-D5 and D1	<1/3 and <1/3
			<1/3 and 1/3-2/3
		D4-D5 and D2-D3	<1/3 and <1/3
D4-D5 and D2-D3 and D1	<1/3		
DG4	<i>Large cracks in structural elements, with a compression failure of the concrete and a fracture of rebars; [...] collapse of a few columns or a single upper floor.</i>	D4-D5 and D2-D3	<1/3 and 1/3-2/3
			<1/3 and >2/3
		D4-D5	1/3-2/3
		D4-D5 and D1	1/3-2/3 and 1/3-2/3
D4-D5 and D2-D3	1/3-2/3 and <1/3		
DG5	<i>Collapse of ground floor or parts of buildings.</i>	D4-D5 and D2-D3	1/3-2/3 and 1/3-2/3
		D4-D5	>2/3
		D4-D5 and D1	>2/3 and <1/3
		D4-D5 and D2-D3	>2/3 and <1/3

332

333 The table shows the corresponding DGs assumed for the building for each damage level and its
334 relevant extent. Note that the AeDES forms allow multiple choices in the selection of the damage
335 level and extent and so different combinations are possible.

336 **Potential liquefaction indices**

337 In this study, a liquefaction potential index was adopted as an IM, in order to correlate the observed
338 building damage due to the occurrence of liquefaction.

339 The assessment of potential liquefaction is still one of the most debated topics in earthquake
340 geotechnical engineering. In common engineering practice, it is usually based on simplified methods
341 which propose empirical relationships between liquefaction evidence observed after strong seismic
342 events and soil liquefaction resistance, as measured with traditional in-situ tests, such as Cone
343 Penetration Tests (CPTs) and Standard Penetration Tests (SPTs) (Boulanger and Idriss 2016). Within
344 this framework, it is possible to calculate a safety factor against liquefaction triggering, F_L , for each
345 of the investigated layers as the ratio between the soil liquefaction capacity, CRR, and the expected
346 seismic demand, CSR. The increased attention paid to the effects on the built environment induced
347 by liquefaction has led over time to the introduction of indices expressing the severity of the effects
348 at ground surface of soil liquefaction occurring in depth. The earliest index was proposed by Iwasaki
349 et al. 1984 as a function of the safety factor F_L against liquefaction and is as follows:

$$LPI = \int_0^{20} F(z) \cdot W(z) dz \quad (7)$$

350 where z is the depth of the midpoint of the soil layer in meters and $F(z)$ and $W(z)$ are:

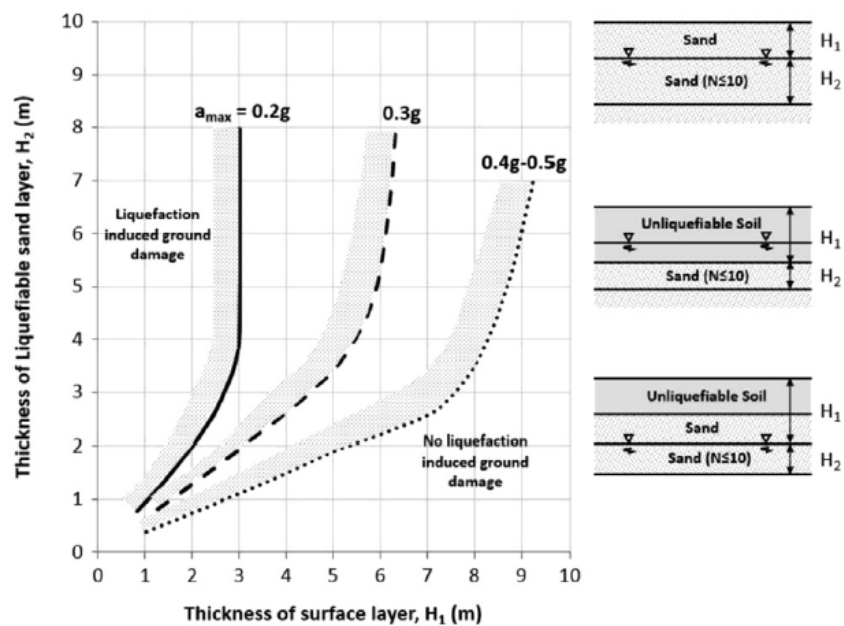
$$F(z) = \begin{cases} 1 - F_L & \text{for } F_L < 1 \\ 0 & \text{for } F_L \geq 1 \end{cases} \quad (8)$$

351

$$W(z) = 10 - 0.5z \quad (9)$$

352 Although it has gained wide popularity worldwide, the LPI only accounts for conditions of full
353 liquefaction ($F_L \leq 1$), while excess pore pressure build-up can induce a significant reduction in
354 stiffness and strength of soil also when liquefaction condition has not been attained. Such excess pore
355 pressure build-up induces settlement, while the reduction of shear strength reduces the bearing
356 capacity safety margins prior to liquefaction triggering. Furthermore, even in these non-liquefied
357 conditions, the post-seismic consolidation process (possible if the stratigraphic conditions allow for
358 drainage) leads to settlement at ground level (Spacagna et al. 2017; Chiaradonna et al. 2018a). Over
359 the years, modifications to the LPI have been proposed by several authors (Sonmez 2003; Sonmez
360 and Gokceoglu 2005; Rashidian and Gillins 2018). Sonmez & Gokceoglu (2005), for instance,
361 introduced a liquefaction probability in the original formulation. However, the threshold value of the
362 safety factor that they introduce in the analysis is still a debated issue.

363 Recently, Van Ballegooy et al. (2014) introduced a new parameter, named liquefaction severity
 364 number (LSN). This parameter is calculated by considering soil volumetric deformation, and has the
 365 advantage of allowing the contribution of unliquefied ($F_L \geq 1$) soil strata to be taken into account,
 366 thus removing one of the shortcomings of LPI. Even though this correlation is easy to use, it has the
 367 major drawback of being based on laboratory test results obtained on a specific sand (Fuji River sand).
 368 A completely different approach to take into account the effect of liquefaction at ground level has
 369 been proposed by Ishihara (1985), who suggests to correlate in a qualitative way to the onset of
 370 damage the thickness of the superficial crust and of the liquefiable layer, as well as the maximum
 371 ground acceleration, using the chart reported in Figure 8.
 372



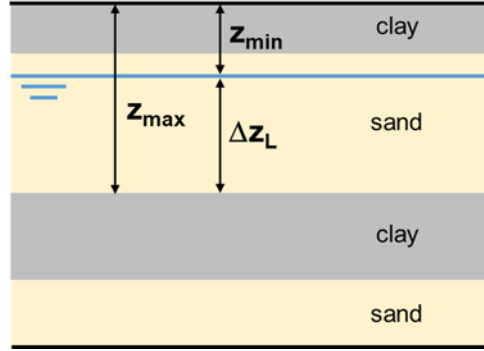
373
 374 **Figure 8:** Relationship between thickness of a liquefying, H_2 (m) and thickness of a non-liquefying
 375 overlying layer, H_1 (m) at sites for which surface manifestation of level-ground liquefaction has
 376 been observed (modified after Ishihara 1985)
 377

378 This approach is intriguing because directly links the observed damage to the most relevant variables
 379 related to liquefaction induced settlements, which should be preferred in the definition of an integral
 380 parameter to the safety factor adopted by the other approaches (LPI, LSN, etc.).

381 Therefore, in this work an estimate of the liquefaction induced settlement has been used to derive an
 382 IM to be adopted for defining the fragility curves. As the effects of sand ejecta (if any) are difficult
 383 to quantify, the post-consolidation settlement was specifically considered. In free-field conditions,
 384 such a settlement can be expressed as:

$$w = \int_{z_{min}}^{z_{max}} \frac{\Delta\sigma'_v(z)}{E_{oed}(z)} dz \quad (10)$$

385 where z_{min} and z_{max} are, respectively, the minimum and maximum depths of the uppermost
 386 saturated, potentially liquefiable, soil layer (Figure 9); $\Delta\sigma'_v$ is the increase of effective vertical stress
 387 induced by the dissipation of the excess pore pressure, Δu ; and E_{oed} is the constrained (oedometric)
 388 modulus.



389

390 **Figure 9:** Minimum, z_{min} , and maximum, z_{max} , depths of the uppermost saturated, potentially
 391 liquefiable, soil layer.

392 A new liquefaction potential index, Induced dAmage Measurement, is then proposed as IM in this work:

$$I_{AM} = \frac{1}{1 + z_{min}} \cdot \int_{z_{min}}^{z_{max}} r_u \cdot dz \quad (11)$$

393 in which r_u is the excess pore pressure ratio (defined as the ratio between the excess pore pressure
 394 induced by the seismic event, Δu , and the initial effective vertical stress in free-field conditions, σ'_{v0}).
 395 This index was adopted because it is strictly related to the volumetric settlement of ground level
 396 induced by liquefaction, as will be shortly discussed in the following. Using the parameter r_u , equation
 397 (10) can be written as:

$$w = \int_{z_{min}}^{z_{max}} \frac{r_u \cdot \sigma'_{v0}(z)}{E_{oed}(z)} dz \quad (12)$$

398 Assuming for $\sigma'_{v0}(z)$ and $E_{oed}(z)$ the mean values $\sigma'_{v0,m}(z = (z_{min} + z_{max})/2)$ and $E_{oed,m}(z =$
 399 $(z_{min} + z_{max})/2)$, eq. (12) can be rearranged as:

$$\frac{w \cdot E_{oed,m}}{\sigma'_{v0,m}} = \int_{z_{min}}^{z_{max}} r_u dz \quad (13)$$

400 In order to make this normalized settlement non-dimensional, and considering that the potential post-
 401 liquefaction settlement is more likely to take place as this layer gets closer to ground level, the desired

402 (and physically based) parameter I_{AM} defined by eq. (11) is finally obtained from eq. (13) dividing it
 403 for $(1+z_{min})$.

404 In a fully liquefied layer ($r_u=1$), the expression of I_{AM} simplifies and becomes:

405

$$I_{AM} = \frac{w \cdot E_{oed,m}}{\sigma'_{v0,m} \cdot (1 + z_{min})} = \frac{\Delta z_L}{1 + z_{min}} \quad (14)$$

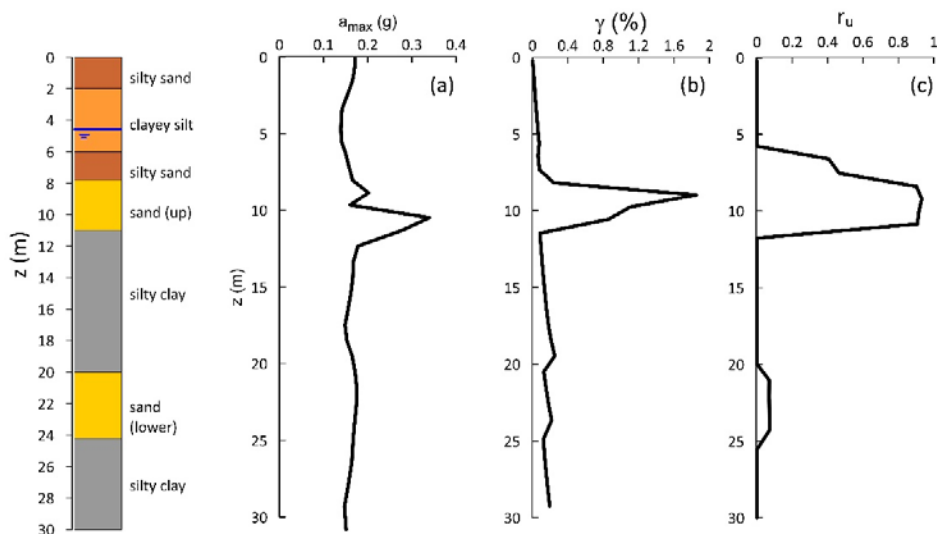
406

407 The simplified expression of I_{AM} (eq. 14) can be simply calculated on the basis of stratigraphic
 408 evidence, and is then best fitted for the investigation of wide areas.

409 The proposed potential index has been computed for both study areas based on the field investigation
 410 database produced by the Emilia Romagna region, which is composed of 166 CPTs and 170 CPTUs.
 411 In this case the simplification $r_u=1$ was based on the results of 1D numerical analyses in effective
 412 stress (using the code SCOSSA, Tropeano et al. 2019) carried out on representative soil profiles for
 413 San Carlo and Mirabello using the seismic input obtained by deconvolution of the Mirandola record
 414 (MRN) of the 20 May 2012 Emilia Earthquake (Chiaradonna et al. 2018b). These results indicate that
 415 full liquefaction of the uppermost liquefiable layer was extensively reached in the paleo-riverbed and
 416 in the paleo-bank (Figure 1) (Caputo et al. 2019), as shown for example in Figure 10.

417 This simplified assumption is realistic, since there was widespread evidence of liquefaction in the
 418 study area (Fioravante et al. 2013; Lai et al. 2015; Papathanassiou et al. 2015).

419



420

421 **Figure 10:** Example of 1D numerical analysis carried out in San Carlo, showing full liquefaction of
 422 the uppermost sand layer (sand(up)) (modified after Caputo et al. 2019).

423

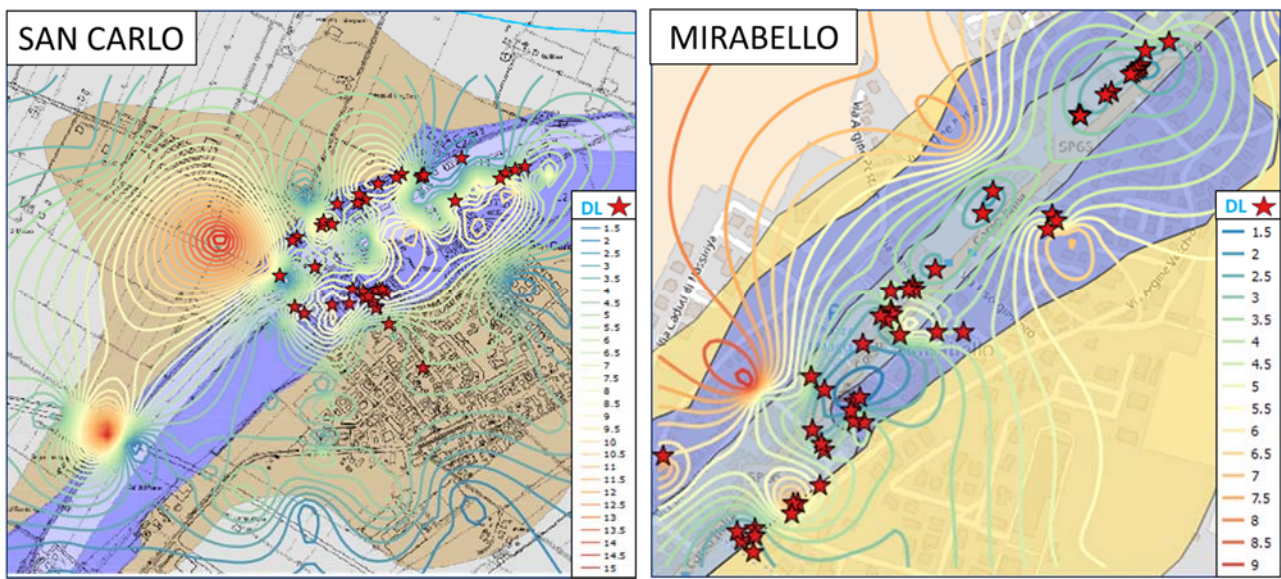
424 Figure 11 shows the minimum depth isolines of the first potentially liquefiable soil layer under the
425 surface, z_{min} (in meters), superimposed on the geological map. The figure highlights that the
426 liquefiable soil deposits are shallowest along the paleochannel and paleobank (depth of 2-3 m on
427 average), while higher depths are observed in the surrounding plain.

428 The spatial distribution of the thickness of the potential liquefiable soil, Δz_L (in meters), is also shown
429 in Figure 12. The thicker liquefiable deposits, 6 m on average, are observed along the paleo-channel
430 and paleo-bank, which are confirmed as the areas that are most susceptible to liquefaction.

431 Finally, Figure 13 reports the spatial distribution of the proposed index, according to eq. (15), which
432 is consistent with the geological setting and the observed damage. As a matter of fact, higher I_{AM}
433 values are calculated along the paleo-channel of the Reno River in both municipalities, where most
434 of the DL buildings are also located.

435 Since the I_{AM} distribution reflects the geological map of the area (Figure 13), a mean I_{AM} value has
436 been assigned to any geological unit, as reported in Figure 14.

437



438

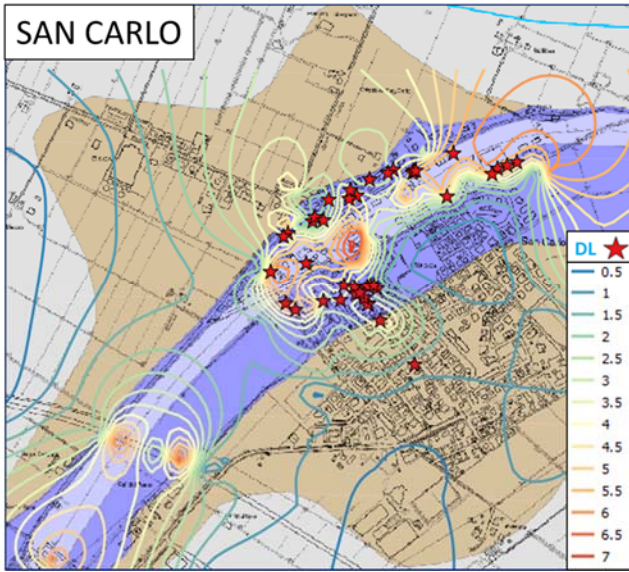
439

(a)

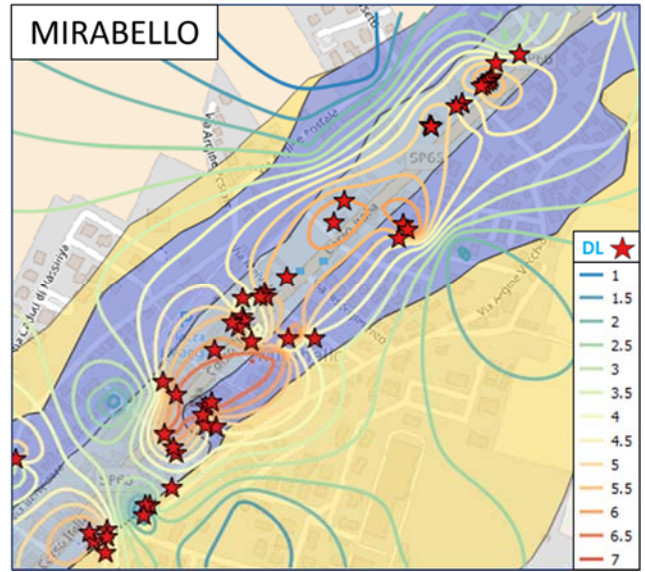
(b)

440 **Figure 11:** Minimum depth isolines of the first potentially liquefiable soil layer under the surface,
441 z_{min} (in meters), superimposed on the geological map, vs. the observed building damage induced by
442 liquefaction (red symbols) in the municipalities of San Carlo (a) and Mirabello (b).

443



(a)

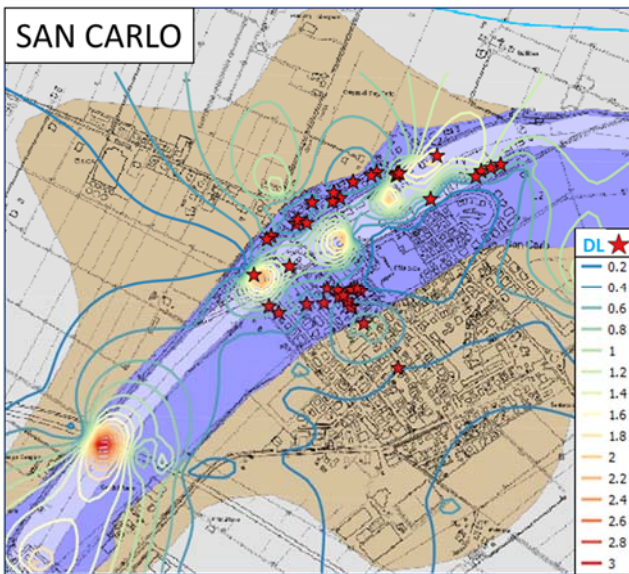


(b)

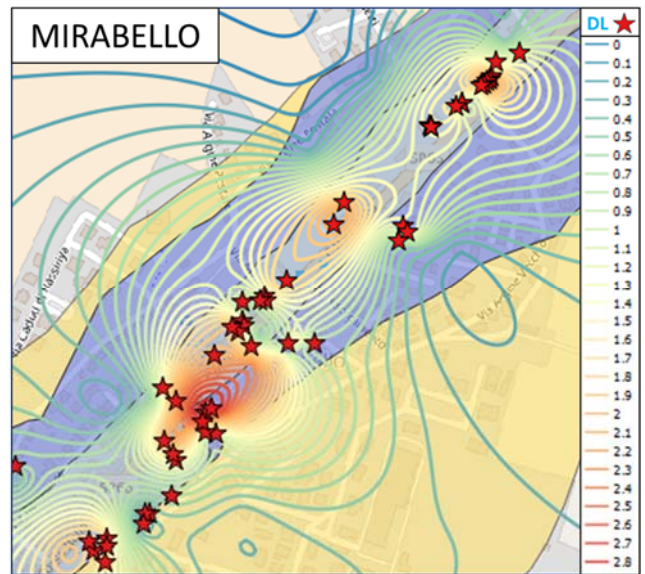
444

445 **Figure 12:** Thickness isolines of the potentially liquefiable soil, Δz_L (in meters), superimposed on
 446 the geological map, vs. the observed building damage induced by liquefaction (red symbols) in the
 447 municipalities of San Carlo (a) and Mirabello (b).

448



(a)

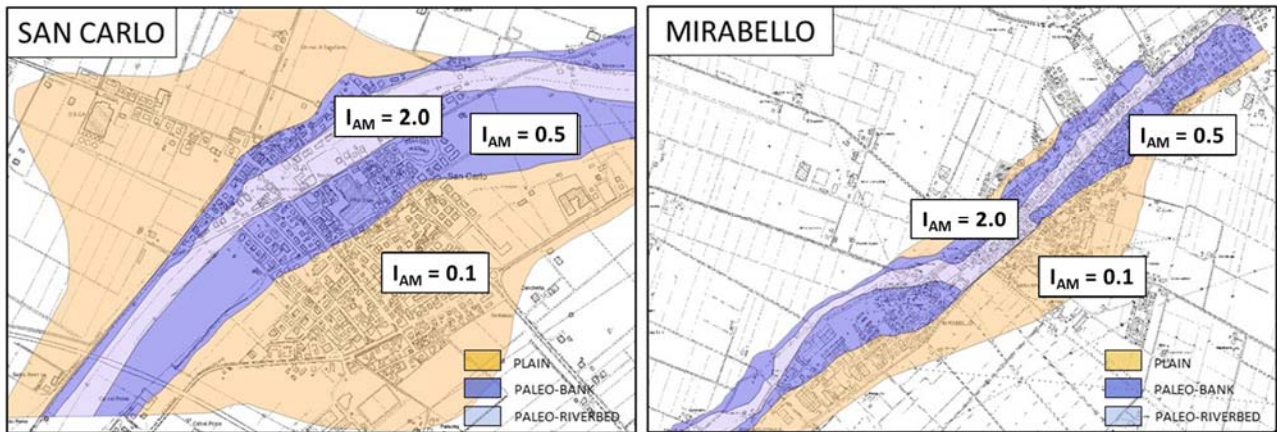


(b)

449

450 **Figure 13:** IAM index isolines superimposed on the geological map, vs. the observed building damage
 451 induced by liquefaction (red symbols) in the municipalities of San Carlo (a) and Mirabello (b).

452



453

454

(a)

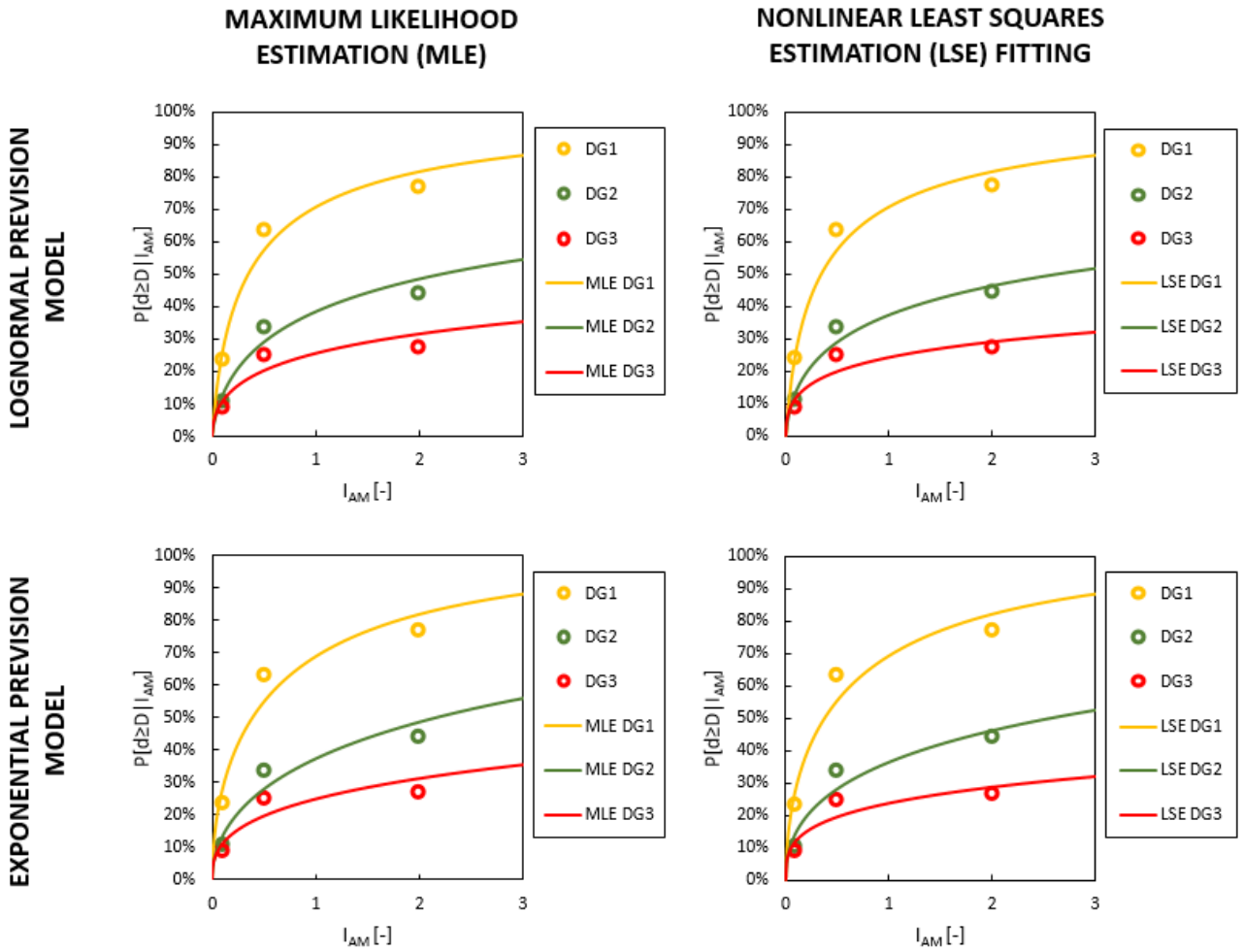
(b)

455 **Figure 14:** Geological map with I_{AM} values adopted for the municipalities of San Carlo (a) and
 456 Mirabello (b).

457

458 **Liquefaction fragility curves**

459 In this section, preliminary liquefaction fragility curves are derived according to the methodologies
 460 described above for the entire dataset of buildings (i.e., about 750 in the NDL and DL classes and
 461 about 350 with no damage). Figure 15 reports the fragility curves for the assumed functional forms
 462 and fitting methodologies. Table 5 sets out the values of the estimated parameters for each fragility
 463 curve. Due to the reduced amount of data, no reliable estimation of the fragility curves at DG4 and
 464 DG5 can be provided.



465

466 **Figure 15:** Lognormal and exponential fragility curves (*solid lines*) at different damage grades (DG)
 467 fitting observed fragility data (*circles*) for all the buildings and the adopted regression techniques
 468 (MLE and LSE).

469 **Table 5:** Lognormal and exponential fragility curve parameters for the damage states considered.

	DG1		DG2		DG3		
	μ	σ	μ	σ	μ	σ	
LSE	-1.07	1.99	0.96	2.99	3.29	4.71	Lognormal
MLE	-1.06	1.96	0.78	2.67	2.57	3.89	

	DG1		DG2		DG3		
	α	β	α	β	α	β	
LSE	1.17	0.53	0.45	0.45	0.27	0.32	Exponential
MLE	1.17	0.54	0.47	0.51	0.29	0.39	

470

471 Figure 15 shows that no significant difference is observed in the lognormal or exponential models.
472 Strictly speaking, the advantages of using a functional form can be evaluated by comparing the values
473 of: a) the weighted sum of the square of the errors in the LSE methodology; and b) the likelihood in
474 the MLE methodology, obtained by adopting the lognormal and exponential models. In both cases,
475 the use of the lognormal model yields slightly better results, i.e. a lower weighted sum of the square
476 of the errors (with the LSE methodology) and a higher likelihood (with the MLE methodology).

477 CONCLUSIONS

478 The 2012 Emilia earthquake highlighted the large extent of the damage caused to structures and
479 infrastructures due to soil liquefaction. The study presented herein investigated the effects of
480 liquefaction on private residential masonry buildings using data on about 1,000 such structures
481 located in several municipalities hit by the earthquake. According to empirical data collected
482 immediately after the seismic event, it was possible to compare the behavior of structures whose soil
483 foundation was not subjected to the liquefaction phenomena (the NDL class of buildings) with that
484 of buildings that were (the DL class of buildings). The analysis of the damage in the DL class of
485 buildings confirmed that, if immediately activated, liquefaction works as a natural isolation system
486 against the transmission of inertial seismic actions on a superstructure; in these cases, the damage is
487 mainly governed by the rigid rotation of buildings or settlements. However, liquefaction is often not
488 immediately activated and this leads to a damage pattern that is characterized by both typical inertial
489 damage (i.e., masonry walls overturning or in-plane cracks) and localized settlements (i.e. rigid
490 rotation or one-way diagonal cracks).

491 The comparative analysis of the damage observed to the NDL and DL building classes has revealed
492 evidence of the impact of soil liquefaction on structures. In particular, the empirical damage detected
493 to the DL class of buildings was generally more severe than that sustained by the NDL class. The
494 macro-parameters influencing the structural vulnerability of masonry buildings to inertial actions
495 were less decisive in the evaluation of the global building damage caused by liquefaction. However,
496 rigid horizontal structures confirmed their crucial role in limiting damage for both building classes.
497 By using a model calibrated empirically to compute losses, the predicted repair costs were about 30%
498 higher in the DL than the NDL buildings.

499 The correlation between structural damage and soil liquefaction allowed to derive empirical fragility
500 curves as functions of a new parameter (I_{AM}), expressing the liquefaction demand because it is related
501 to ground settlement, and therefore to structural damage. Under the simplified hypothesis that the
502 uppermost liquefiable layer is fully liquefied (i.e. $r_u=1$), such a new liquefaction index can be
503 calculated in a very straightforward way. In order to produce fragility curves to determine the

504 probability of exceeding the damage grades defined according to EMS-98, average values of I_{AM} were
505 attributed to different parts of the two analysed villages, based on both in situ tests results and
506 geological characteristics. Because of this simplification, in the next future a more detailed
507 characterization of the villages will be done by carrying out more widespread in situ tests, obtaining
508 therefore a more refined I_{AM} mapping. Although the curves presented herein depend on the local
509 context where the seismic event occurred, and further data from other events are required, they
510 certainly represent a preliminary tool to predict losses in liquefaction-prone areas and to establish
511 priorities and reconstruction policies for use in the aftermath of future earthquakes.

512

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521

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