

# fda.usc Reference Card

March 27, 2019

*Only main arguments are shown*

## fdata class objects

`fdata(mdata, argvals=NULL, ...)` (class `fdata`) uses the evaluations at the discretization points and converts object of class: `fd`, `fds`, `fts`, `sfts`, vector, matrix, `data.frame` to an object of class `fdata`  
`plot.fdata(x, type, main, ...)` plots functional data class object

## Basic operations

Group Math: `abs()`, `sqrt()`, `floor()`, `ceiling()`, `trunc()`, `round()`, `signif()`, `exp()`, `log()`, `cos()`, `sin()`, `tan()`

Group Summary: `all()`, `any()`, `sum()`, `prod()`, `min()`, `max()`, `range()`

Other S3 methods for class 'fdata': `[]`, `==`, `!=`, `+`, `-`, `*`, `/`, `^`, `is.fdata()`, `c()`, `dim()`, `ncol()`, `nrow()`, `NCOL()`, `NROW()`, `anyNA`, `count.na()`, `order.fdata(y, fdataobj, ...)`

## Create Basis Set for Functional Data

`create.fdata.basis(fdataobj, l=1:5, maxl, type.basis, ...)` computes fixed basis for FD

`create.pc.basis(fdataobj, l=1:5, ...)` computes PCA basis for FD  
`create.pls.basis(fdataobj, y, l = 1:5, ...)` computes PCA basis for FD

## PCA and PLS for Functional Data

`fdata2pc(fdataobj, ncomp = 2, ...)` computes (penalized) principal components (PC) for functional data

`fdata2pls(fdataobj, y, ncomp = 2, ...)` computes penalized partial least squares (PLS) components for functional data

## Tools for Functional Data

`fdata2fd(fdataobj, type.basis=NULL, nbasis=NULL, ...)` converts fdata object to fd object (using the basis representation)

`fdata.deriv(fdataobj, nderiv=1, method="bspline", ...)` computes the derivative of functional data.

`fdata.bootstrap(fdataobj, statistic=func.mean, ...)` bootstrap samples for functional data.

## Functional Smoothing

`S.basis(tt, basis, lambda=0, ...)` provides the smoothing matrix with roughness penalties by fixed basis representation

`S.LLR(tt, h, Ker = Ker.norm, ...)` provides the smoothing matrix for the discretization points by Local Linear Regression

`S.NW(tt, h, Ker = Ker.norm, ...)` provides the smoothing matrix for the discretization points by Nadaraya-Watson kernel estimator

`S.KNN(tt, h=NULL, Ker = Ker.unif, ...)` provides the smoothing matrix for the discretization points by K nearest neighbors estimator

`min.basis()` computes a smooth functional data with a roughness penalty and number of basis representation selection by validation criteria

`min.np()` computes a smooth functional data with a kernel band-

width selection by validation criteria for bandwidth selection  
`CV.S()` computes the leave-one-out cross-validation (CV) score  
`GCV.S()` computes the generalized correlated cross-validation (GCV) score

## Inner product and norm for FD

`inprod.fdata(fdata1, fdata2=NULL, w = 1, ...)` computes a inner products of functional data (fdata object)

`norm.fdata(fdataobj, metric=metric.lp, ...)` approximates  $L_p$ -norm for functional data (fdata object)

`norm.fd(fdobj)` approximates  $L_2$ -norm for fd class object

## Distance between functional elements

`metric.lp(fdata1, fdata2=NULL, lp=2, ...)` for  $L_p$ -metric

`metric.hausdorff(fdata1, fdata2 = fdata1)` for Hausdorff distances between two sets of curves

`metric.kl(fdata1, fdata2 = NULL, symm=TRUE, ...)` for Kullback Leibler distance between two groups of densities

`metric.dist(x, y = NULL, method = "euclidean", ...)` for distances between the rows of a data matrix (wrapper of `dist()`)

`semimetric.basis(fdata1, fdata2 = fdata1, nderiv=0, ...)` for distances based on fixed basis

`semimetric.deriv(fdata1, fdata2=fdata1, nderiv=1, ...)` for distances between derivatives of the curves based on B-spline basis

`semimetric.fourier(fdata1, fdata2=fdata1, nderiv=0, ...)` distance between the curves based on Fourier basis

`semimetric.hshift(fdata1, fdata2, ...)` computes distance between curves taking into account an horizontal shift effect

`semimetric.mplsr(fdata1, fdata2=fdata1, q=2, class1, ...)` computes distance between curves based on the PLS

`semimetric.pca(fdata1, fdata2=fdata1, q=1, ...)` computes distance between curves based on PCA

## Functional Univariate Data Depth

`depth.FM(fdataobj, fdataori = fdataobj, trim=0.25, ...)` computes Fraiman and Muniz (FM) depth

`depth.mode(fdataobj, fdataori = fdataobj, trim=0.25, ...)` computes modal depth

`depth.RT(fdataobj, fdataori = fdataobj, trim = 0.25, ...)` computes random tukey (RT) depth

`depth.RP(fdataobj, fdataori = fdataobj, trim=0.25, ...)` computes random project (RP) depth

`depth.RPD(fdataobj, fdataori = fdataobj, nproj=50, ...)` double random project depth (RPD) depth

`depth.FSD(fdataobj, fdataori = fdataobj, trim = 0.25, ...)` computes Functional Spatial depth

`depth.KFSD(fdataobj, fdataori = fdataobj, trim = 0.25, ...)` computes Kernelized Functional Spatial depth

## Functional Multivariate Data Depth

`depth.FMp(lfdata, lfdataref = lfdata, trim = 0.25, ...)` computes Fraiman-Muniz depth

`depth.RPp(lfdata, lfdataref = lfdata, nproj = 50, ...)` computes Random Projections depth

`depth.modep(lfdata, lfdataref = lfdata, h = NULL, ...)` computes Modal depth

## Multivariate Data Depth

`mdepth.MhD(x, xx=x, ...)` computes Mahalanobis depth (Mean)

`mdepth.HS(x, xx=x, ...)` computes Halfspace depth, also known as Tukey Depth (Median)

`mdepth.SD(x, xx = NULL, ...)` computes Simplicial depth

`mdepth.LD(x, xx=x, ...)` computes Likelihood depth (Mode)

## Functional Outlier Detection

`outliers.thres.lrt(fdataobj, nb=200, smo=0.05, ...)` procedure for detecting functional outliers by likelihood ratio test

`outliers.depth.trim(fdataobj, nb=200, smo=0.05, ...)` procedure for detecting functional outliers using trimmed data according to depth

`outliers.depth.pond(fdataobj, nb=200, smo=0.05, ...)` procedure for detecting functional outliers using weights the data according to depth

## Functional Data Generation

`rproc2fdata(n, t=NULL, ...)` generates curves from different processes: Ornstein Uhlenbeck, Brownian, Fractional Brownian, Gaussian or Exponential variogram

`gridfdata(coef, fdataobj, mu)` generates curves as lineal combination of the original curves plus a functional trend

`rcombffdata(n = 10, fdataobj, mu, ...)` generates random combinations of the curves plus a functional trend

## Functional Linear Models

`fregre.lm(formula, data, basis.x=NULL, ...)` computes LM model between functional (and non functional) explanatory variables and scalar response using (fixed or data-driven) basis representation

`fregre.basis(fdataobj, y, basis.x=NULL, ...)` computes LM model between functional predictor and scalar response using fixed basis representation

`fregre.basis.cv(fdataobj, y, basis.x=NULL, ...)` cross-validation functional regression with scalar response using basis representation

`fregre.pc(fdataobj, y, l = NULL, ...)` computes functional (ridge or penalized) regression using PCA

`fregre.pc.cv(fdataobj, y, kmax=8, ...)` computes functional (ridge or penalized) regression using selection of number of PC components

`fregre.pls(fdataobj, y=NULL, l = NULL, ...)` computes functional linear regression using penalized PLS

`fregre.pls.cv(fdataobj, y, kmax=8, ...)` computes functional linear regression using selection of number of PLS components

## Goodness-of-fit test for the FLM

`flm.Ftest(X.fdata, Y, B=5000, verbose=TRUE)` tests the null hypothesis of no interaction between a functional covariate and a scalar response inside the Functional Linear Model

`flm.test(X.fdata, Y, beta0.fdata = NULL, ...)` tests the composite null hypothesis of a FLM with scalar response

## Model fitting

`summary(object, ...)` summarizes information from fitted models such as: `fregre.pc`, `fregre.basis`, `fregre.pls`, `fregre.np`,

and `fregre.plm`  
`predict(object,...)` predictions from object fitted such as:  
`fregre.pc`, `fregre.basis`, `fregre.pls`, `fregre.np`, and  
`fregre.plm`  
`influence.fdata(model,...)` computes influence measures from  
FLM  
`fregre.bootstrap(model, nb = 500, wild = TRUE,...)` estimate  
the beta parameter by wild or smoothed bootstrap procedure

## Functional Non-Linear Models

`fregre.np(fdataobj,y,h=NULL,...)` computes functional regression  
between functional explanatory variables and scalar response  
using kernel estimation  
`fregre.np.cv(fdataobj, y, h=NULL,...)` computes functional  
regression between functional explanatory variables and scalar  
response using kernel estimation by cross-validation method  
`fregre.plm(formula, data, h=NULL,...)` compute semi-  
functional partially linear model with scalar response using  
kernel estimation of functional predictor

## Generalized Regression Models

`fregre.glm(formula,family = gaussian(), data,...)` fits functional  
GLM model  
`fregre.gsam(formula, family = gaussian(), data,...)` fits  
functional GAM model with integrated Smoothness estimation  
and basis representation  
`fregre.gkam(formula, family = gaussian(),data,...)` fits  
functional GAM model with Kernel estimation

## Functional Response Model

`fregre.basis.fr(x,y, basis.s=NULL,...)` fits functional response  
models using basis representation

## Models for Dependent Data

`fregre.gls(formula, data, correlation = NULL,...)` fits functional  
generalized least squares (GLS) model  
`fregre.igls(formula, data, basis.x=NULL,...)` fits functional  
generalized least squares (GLS) model iteratively  
`GCCV.S(y, S, criteria="GCCV1",...)` generalized correlated  
cross-validation (GCV) score  
`predict.fregre.gls(object, newx = NULL, type =  
"response",...)` predictions from a functional gls object  
`predict.fregre.igls(object, new.fdataobj = NULL,  
data,...)` predictions from a functional iterative gls object

## Variable and Impact Points Selection

`fregre.gsam.vs(data, y, x, alpha, type.basis = "pc", ...)`  
fits functional GAM model by selecting the model variables  
(between functional, scalar, factors,...)  
`LMDC.select(y, covar, data,...)` selects impact points of functional  
predictor using local maxima distance correlation  
(LMDC) for a scalar response given  
`LMDC.regre(y, covar, data, newdata,...)` fits a multivariate  
regression method using the selected impact points like covariates  
for a scalar response

## Functional Classification

`classif.glm(formula, data, family = binomial(),...)` computes  
functional classification using functional (and non functional)  
explanatory variables by basis representation  
`classif.knn(group, fdataobj, knn=NULL,...)` fits kNN Supervised  
Classification for Functional Data.  
`classif.kernel(group, fdataobj,h=NULL,...)` fits Nonparametric  
(Kernel) Supervised Classification for Functional Data.  
`classif.gsam(formula,data, family = binomial(),...)` computes  
functional classification using functional (and non functional)  
explanatory variables by basis representation  
`classif.gkam(formula, family = binomial(), data,...)` computes  
functional classification using functional explanatory  
variables using backfitting algorithm  
`classif.tree(formula, data, basis.x=NULL,...)` computes  
functional classification by Recursive Partitioning and Regression  
Trees (see `rpart`)

## Functional Depth Classification

`classif.depth(group,fdataobj,newfdataobj,...)` classification  
of functional data using maximum depth  
`classif.DD(group, fdataobj, depth="FM", classif="glm",...)`  
fits nonparametric classification procedure based on DD-plot  
(depth-versus-depth plot) for G dimensions

## Functional Non-Supervised Classification

`kmeans.fd(fdataobj, ncl = 2, metric = metric.l,...)` allows  
the estimation of the groups in a functional data set `fdata`  
class by k-means method

## Functional ANOVA

`anova.hetero(object = NULL, formula, pr = FALSE,...)` fits a  
univariate analysis of variance model for heteroscedastic data  
and allows calculate special contrasts defined by the user  
`anova.onefactor(object, group, nboot=100,...)` contrasts the  
null hypothesis of equality of mean functions of functional data  
based on the an asymptotic version of the anova F-test  
`anova.RPm(object, formula, data.fac,...)` tests ANOVA models  
for functional data with continuous covariates based on the  
analysis of randomly chosen one-dimensional projections

## Conditional Distribution Function

`cond.F(fdata0, y0, fdataobj,...)` calculates the conditional  
distribution function of a scalar response with functional data.

## Datasets

`aemet` contains geographic information of 73 Spanish weather station  
and the average for the period 1980-2009 of daily temperature,  
precipitation and wind speed. Meteorological State Agency of Spain  
(AEMET), <http://www.aemet.es/>  
`MCO` The mitochondrial calcium overload (MCO) was measured in two  
groups (control -original cells - and treatment - permeabilized  
cells-) every 10 seconds during an hour in isolated mouse cardiac  
cells.  
`phoneme` contains 250 learning curves and 250 test curves discretized  
in 150 log-periodograms points corresponding to 5 class membership  
(five phonemes): "sh" 1, "iy" 2, "dcl" 3, "aa" 4 and

"ao" 5 (50 by class level).  
`poblenou` NOx levels measured every hour by a control station in  
Poblenou in Barcelona (Spain). The dataset starts on 23 February  
and ends on 26 June, in 2005.  
`tecator` contains the Water, Fat and Protein content of 215 meat  
samples and the 215 absorbance curves recorded in the wavelength  
range 850 - 1050 nm.

## Documentation

Created by Manuel Oviedo de la Fuente, website <http://eio.usc.es/pub/moviedo> and by Manuel Febrero Bande, website <http://eio.usc.es/pub/febrero>, feel free to contact us for contributions.

## Links

fda.usc R package <http://cran.r-project.org/web/packages/fda.usc>  
JSS paper <http://www.jstatsoft.org/article/view/v051i04>  
fda.usc R Manual <https://cran.r-project.org/web/packages/fda.usc/fda.usc.pdf>  
CRAN Task View <https://cran.r-project.org/web/views/FunctionalData.html>

## RPubs document

Installation and Descriptive Statistics <http://rpubs.com/moviedo/fda.usc.introduction>  
Functional Regression <http://rpubs.com/moviedo/fda.usc.regression>  
Functional Classification and ANOVA <http://rpubs.com/moviedo/fda.usc.classification>  
HTML reference card <http://rpubs.com/moviedo/fda.usc.rcard>