



CWTS Leiden Ranking 2019
Meaningful metrics

Methodology



Universiteit
Leiden

Data

The CWTS Leiden Ranking 2019 is based on bibliographic data from the Web of Science database produced by Clarivate Analytics. Below we discuss the Web of Science data that is used in the Leiden Ranking. We also discuss the enrichments made to this data by CWTS.

Web of Science

The Web of Science database consists of a number of citation indices. The Leiden Ranking uses data from the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. The Leiden Ranking is based on Web of Science data because Web of Science offers a good coverage of the international scientific literature and generally provides high quality data.

The Leiden Ranking does not take into account conference proceedings publications and book publications. This is an important limitation in certain research fields, especially in computer science, engineering, and the social sciences and humanities.

Enriched data

CWTS enriches Web of Science data in a number of ways. First of all, CWTS performs its own citation matching (i.e., matching of cited references to the publications they refer to). Furthermore, in order to calculate the various indicators included in the Leiden Ranking, CWTS identifies publications by industrial organizations in Web of Science, CWTS performs geocoding of the addresses listed in publications, CWTS assigns open access labels (gold, hybrid, bronze, green) to publications, and CWTS disambiguates authors and attempts to determine their gender. Most importantly, CWTS puts a lot of effort in assigning publications to universities in a consistent and accurate way. This is by no means a trivial issue. Universities may be referred to using many different name variants, and the definition and delimitation of universities is not obvious at all. The methodology employed in the Leiden Ranking to assign publications to universities is discussed below.

More information

More information on the citation matching that is performed by CWTS is provided in a paper by Olensky, Schmidt, and Van Eck (2016). For more information on the geocoding of addresses, we refer to a paper by Waltman, Tijssen, and Van Eck

(2011). The author disambiguation algorithm used by CWTS is documented in a paper by Caron and Van Eck (2014).

Caron E., & Van Eck, N.J. (2014). Large scale author name disambiguations using rule-based scoring and clustering. In E. Noyons, editor, *Proceedings of the 19th International Conference on Science and Technology Indicators* (pp. 79-86).

Olensky, M., Schmidt, M., & Van Eck, N.J. (2016). Evaluation of the citation matching algorithms of CWTS and iFQ in comparison to Web of Science. *Journal of the Association for Information Science and Technology*, 67(10), 2550–2564. [doi:10.1002/asi.23590](https://doi.org/10.1002/asi.23590).

Waltman, L., Tijssen, R.J.W., & Van Eck, N.J. (2011). Globalisation of science in kilometres. *Journal of Informetrics*, 5(4), 574–582. [doi:10.1016/j.joi.2011.05.003](https://doi.org/10.1016/j.joi.2011.05.003).

Universities

The CWTS Leiden Ranking 2019 includes 963 universities worldwide. These universities have been selected based on their number of Web of Science indexed publications in the period 2014–2017. As discussed below, a sophisticated data collection methodology is employed to assign publications to universities.

Identification of universities

Identifying universities is challenging due to the lack of clear internationally accepted criteria that define universities. Typically, a university is characterized by a combination of education and research tasks in conjunction with a doctorate-granting authority. However, these characteristics do not mean that universities are particularly homogeneous entities that allow for international comparison on every aspect. As a result of its focus on scientific research, the Leiden Ranking presents a list of institutions that have a high degree of research intensity in common. Nevertheless, the ranking scores for each institution should be evaluated in the context of its particular mission and responsibilities, which are strongly linked to national and regional academic systems. Academic systems - and the role of universities therein - differ substantially between countries and are constantly changing. Inevitably, the outcomes of the Leiden Ranking reflect these differences and changes.

The international variety in the organization of academic systems also poses difficulties in terms of identifying the proper unit of analysis. In many countries, there are collegiate universities, university systems, or federal universities. Instead of applying formal criteria, whenever possible we follow common practice based on the way these institutions are perceived locally. Consequently, we treat the University of Cambridge and the University of Oxford as entities, whereas in the case of the University of London we distinguish between the constituent colleges. For the United States, university systems (e.g. the University of California) are split up into separate universities. The higher education sector in France, like in many other countries, has gone through several reorganizations in recent years. Many French institutions of higher education have been grouped together in *Communautés d'Universités et Etablissements* (COMUEs), succeeding the earlier *Pôles de Recherche et*

d'Enseignement Supérieur (PRES). Except in the case of full mergers, the Leiden Ranking still distinguishes between the different constituent institutions.

Publications are assigned to universities based on their recent configuration. Changes in the organizational structures of universities up to 2018 have been taken into account.

Affiliated institutions

A key challenge in the compilation of a university ranking is the handling of publications originating from research institutes and hospitals affiliated with universities. Among academic systems, a wide variety exists in the types of relations maintained by universities with these affiliated institutions. Usually, these relationships are shaped by local regulations and practices affecting the comparability of universities on a global scale. As there is no easy solution for this issue, it is important that producers of university rankings employ a transparent methodology in their treatment of affiliated institutions.

CWTS distinguishes three different types of affiliated institutions:

1. Component
2. Joint research facility or organization
3. Associated organization

In the case of a *component*, the affiliated institution is actually part of or controlled by the university. Universitaire Ziekenhuizen Leuven is an example of a component, since it is part of the legal entity of Katholieke Universiteit Leuven.

A *joint research facility or organization* is the identical to a component except that it is administered by more than one organization. The Brighton & Sussex Medical School (the joint medical faculty of the University of Brighton and the University of Sussex) and Charité (the medical school of both the Humboldt University and the Freie Universität Berlin) are examples of this type of affiliated institution.

The third type of affiliated institution is the *associated organization*, which is more loosely connected to a university. This organization is an autonomous institution that collaborates with one or more universities based on a joint purpose but at the same time has separate missions and tasks. In many countries, hospitals that operate as teaching or university hospitals fall into this category. The Massachusetts General Hospital, one of the teaching hospitals of the Harvard Medical School, is an example of an associated organization.

The Leiden Ranking 2019 counts a publication as output of a university if at least one of the affiliations in the publication explicitly mentions either the university or one of its components or joint research facilities. In a limited number of cases, affiliations with academic hospitals that are not controlled or owned by the university are also treated as if they were mentioning the university itself. The rationale for this is that in some cases academic hospitals – although formally being distinct legal entities – are so tightly integrated with the university that they are commonly perceived as being a component or extension of that university. Examples of this situation include the university medical centers in the Netherlands and some of the academic health science systems in the United States and other countries. In these cases, universities have actually delegated their medical research and teaching activities to the academic hospitals and universities may even no longer act as the formal employer of the medical researchers involved. In other cases, tight integration between a university and an academic hospital may manifest itself by an extensive overlap in staff. In this situation, researchers may not always mention explicitly their affiliation with the university. An example of this tight integration is the relation between the University Hospital Zurich and the University of Zurich.

Affiliated organizations that are not classified as a component or a joint research facility or treated as such are labeled as associated organizations. In the case of publications with affiliations from associated organizations, a distinction is made between publications from associated organizations that also mention the university and publications from associated organizations that do not include a university affiliation. In the latter case, a publication is not considered to originate from the university. On the other hand, if a publication includes an affiliation from a particular university as well as an affiliation from an associated organization, both affiliations are considered to represent that particular university. The effect of this procedure depends on the counting method that is used in the calculation of bibliometric indicators. The procedure influences results obtained using the fractional counting method, but it has no effect on results obtained using the full counting method.

Selection of universities

The Leiden Ranking 2019 includes 963 universities from 56 different countries. These are all universities worldwide that have produced at least 1000 Web of Science indexed publications in the period 2014–2017. Only so-called core publications are counted, which are publications in international scientific journals. Also, only research articles and review articles are taken into account. Other types of

publications are not considered. Furthermore, collaborative publications are counted fractionally. For instance, if a publication includes five authors of which two belong to a particular university, the publication is counted with a weight of $2 / 5 = 0.4$ for that university.

It is important to note that universities do not need to apply to be included in the Leiden Ranking. The universities included in the Leiden Ranking are selected by CWTS according to the procedure described above. Universities do not need to provide any input themselves.

Data quality

The assignment of publications to universities is not free of errors, and it is important to emphasize that in general universities do not verify and approve the results of the Leiden Ranking data collection methodology. Two types of errors are possible. On the one hand, there may be false positives, which are publications that have been assigned to a university when in fact they do not belong to the university. On the other hand, there may be false negatives, which are publications that have not been assigned to a university when in fact they do belong to the university. The data collection methodology of the Leiden Ranking can be expected to yield substantially more false negatives than false positives. In practice, it turns out to be infeasible to manually check all addresses occurring in Web of Science. Because of this, many of the 5% least frequently occurring addresses in Web of Science have not been manually checked. This can be considered a reasonable upper bound for errors, since most likely the majority of these addresses do not belong to universities.

Main fields

The CWTS Leiden Ranking 2019 provides statistics not only at the level of science as a whole but also at the level of the following five main fields of science:

1. Biomedical and health sciences
2. Life and earth sciences
3. Mathematics and computer science
4. Physical sciences and engineering
5. Social sciences and humanities

As discussed below, these five main fields are defined based on large number of micro-level fields.

Algorithmically defined fields

Each publication of a university belongs to one, or sometimes to more than one, of the above main fields. If a publication belongs to more than one main field, the publication is assigned fractionally to each of the main fields. For instance, a publication belonging to two main fields is assigned to each of the two fields with a weight of $1 / 2 = 0.5$.

Publications are assigned to the five main fields using an algorithmic approach. Traditionally, fields of science are defined by sets of related journals. This approach is problematic especially in the case of multidisciplinary journals such as *Nature*, *PLOS ONE*, *PNAS*, and *Science*, which do not belong to one specific scientific field. The five main fields listed above are defined at the level of individual publications rather than at the journal level. In this way, publications in multidisciplinary journals can be properly assigned to a field.

Publications are assigned to main fields in the following three steps:

1. We start with 4535 micro-level fields of science. These fields are constructed algorithmically. Using a computer algorithm, each publication in Web of Science is assigned to one of the 4535 fields. This is done based on a large-scale analysis of hundreds of millions of citation relations between publications.

2. We then determine for each of the 4535 micro-level fields the overlap with each of the 249 journal subject categories defined in Web of Science (excluding the *Multidisciplinary Sciences* subject category).
3. Each subject category in Web of Science has been linked to one of the five main fields. Based on the link between subject categories and main fields, we assign each of the 4535 micro-level fields to one or more of the five main fields. A micro-level field is assigned to a main field if at least 25% of the publications in the micro-level field belong to subject categories linked to the main field.

After the above steps have been taken, each publication in Web of Science has an assignment to a micro-level field, and each micro-level field in turn has an assignment to at least one main field. Combining these results, we obtain for each publication an assignment to one or more main fields.

More information

For more information on the methodology for the algorithmic construction of the micro-level fields, we refer to a paper by Waltman and Van Eck (2012). The methodology makes use of the Leiden algorithm. This algorithm is documented in a paper by Traag et al. (2019).

Waltman, L., & Van Eck, N.J. (2012). A new methodology for constructing a publication-level classification system of science. *Journal of the American Society for Information Science and Technology*, 63(12), 2378–2392. [doi:10.1002/asi.22748](https://doi.org/10.1002/asi.22748).

Traag, V.A., Waltman, L., & Van Eck, N.J. (2019). From Louvain to Leiden: Guaranteeing well-connected communities. *Scientific Reports*, 9, 5233. [doi:10.1038/s41598-019-41695-z](https://doi.org/10.1038/s41598-019-41695-z).

Indicators

The CWTS Leiden Ranking 2019 offers a sophisticated set of bibliometric indicators that provide statistics at the level of universities on scientific impact, collaboration, open access publishing, and gender diversity. The indicators available in the Leiden Ranking are discussed in detail below.

Publications

The Leiden Ranking is based on publications in the Web of Science database produced by Clarivate Analytics. The most up-to-date statistics made available in the Leiden Ranking are based on publications in the period 2014–2017, but statistics are also provided for earlier periods. Web of Science includes a number of citation indices. The Leiden Ranking uses the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. Only publications of the Web of Science document types *article* and *review* are taken into account. The Leiden Ranking does not consider book publications, publications in conference proceedings, and publications in journals not indexed in the above-mentioned citation indices of Web of Science.

The Leiden Ranking takes into account only a subset of the publications in the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. We refer to the publications in this subset as core publications. Core publications are publications in international scientific journals in fields that are suitable for citation analysis. In order to be classified as a core publication, a publication must satisfy the following criteria:

- The publication has been written in English.
- The publication has one or more authors. (Anonymous publications are not allowed.)
- The publication has not been retracted.
- The publication has appeared in a core journal.

The last criterion is a very important one. In the Leiden Ranking, a journal is considered a core journal if it meets the following conditions:

- The journal has an international scope, as reflected by the countries in which researchers publishing in the journal and citing to the journal are located.
- The journal has a sufficiently large number of references to other core journals, indicating that the journal is situated in a field that is suitable for citation analysis. Many journals in the arts and humanities do not meet this condition. The same applies to trade journals and popular magazines.

In the calculation of the Leiden Ranking indicators, only core publications are taken into account. Excluding non-core publications ensures that the Leiden Ranking is based on a relatively homogeneous set of publications, namely publications in international scientific journals in fields that are suitable for citation analysis. The use of such a relatively homogeneous set of publications enhances the international comparability of universities. It should be emphasized that non-core publications are excluded not because they are considered less important than core publications. Non-core publications may have an important scientific value. About one-sixth of the publications in Web of Science are excluded because they have been classified as non-core publications.

Our concept of core publications should not be confused with the Web of Science Core Collection. The Web of Science Core Collection represents a subset of the citation indices available in Web of Science. As explained above, the core publications on which the Leiden Ranking is based represent a subset of the publications in the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index.

Size-dependent vs. size-independent indicators

Indicators included in the Leiden Ranking have two variants: A size-dependent and a size-independent variant. In general, size-dependent indicators are obtained by counting the absolute number of publications of a university that have a certain property, while size-independent indicators are obtained by calculating the proportion of the publications of a university with a certain property. For instance, the number of highly cited publications of a university and the number of publications of a university co-authored with other organizations are size-dependent indicators. The proportion of the publications of a university that are highly cited and the proportion of a university's publications co-authored with other organizations are size-independent indicators. In the case of size-dependent indicators, universities with a larger publication output tend to perform better than universities with a

smaller publication output. Size-independent indicators have been corrected for the size of the publication output of a university. Hence, when size-independent indicators are used, both larger and smaller universities may perform well.

Scientific impact indicators

The Leiden Ranking provides the following indicators of scientific impact:

- *P*. Total number of publications of a university.
- *P(top 1%) and PP(top 1%)*. The number and the proportion of a university's publications that, compared with other publications in the same field and in the same year, belong to the top 1% most frequently cited.
- *P(top 5%) and PP(top 5%)*. The number and the proportion of a university's publications that, compared with other publications in the same field and in the same year, belong to the top 5% most frequently cited.
- *P(top 10%) and PP(top 10%)*. The number and the proportion of a university's publications that, compared with other publications in the same field and in the same year, belong to the top 10% most frequently cited.
- *P(top 50%) and PP(top 50%)*. The number and the proportion of a university's publications that, compared with other publications in the same field and in the same year, belong to the top 50% most frequently cited.
- *TCS and MCS*. The total and the average number of citations of the publications of a university.
- *TNCS and MNCS*. The total and the average number of citations of the publications of a university, normalized for field and publication year. An MNCS value of two for instance means that the publications of a university have been cited twice above the average of their field and publication year.

Citations are counted until the end of 2018 in the calculation of the above indicators. Author self-citations are excluded. All indicators except for TCS and MCS are normalized for differences in citation patterns between scientific fields. For the purpose of this field normalization, about 4500 fields are distinguished. These fields are defined at the level of individual publications. Using a computer algorithm, each publication in Web of Science is assigned to a field based on its citation relations with other publications.

The TCS, MCS, TNCS, and MNCS indicators are not available on the main ranking page. These indicators can be accessed by clicking on the name of a university. An overview of all bibliometric statistics available for the university will then be presented. This overview also includes the TCS, MCS, TNCS, and MNCS indicators.

Collaboration indicators

The Leiden Ranking provides the following indicators of collaboration:

- *P*. Total number of publications of a university.
- *P(collab)* and *PP(collab)*. The number and the proportion of a university's publications that have been co-authored with one or more other organizations.
- *P(int collab)* and *PP(int collab)*. The number and the proportion of a university's publications that have been co-authored by two or more countries.
- *P(industry)* and *PP(industry)*. The number and the proportion of a university's publications that have been co-authored with one or more industrial organizations. All private sector for profit business enterprises, covering all manufacturing and services sectors, are regarded as industrial organizations. This includes research institutes and other corporate R&D laboratories that are fully funded or owned by for profit business enterprises. Organizations in the private education sector and private medical/health sector (including hospitals and clinics) are not classified as industrial organizations.
- *P(<100 km)* and *pp(<100 km)*. The number and the proportion of a university's publications with a geographical collaboration distance of less than 100 km. The geographical collaboration distance of a publication equals the largest geographical distance between two addresses mentioned in the publication's address list.
- *P(>5000 km)* and *PP(>5000 km)*. The number and the proportion of a university's publications with a geographical collaboration distance of more than 5000 km.

Some limitations of the above indicators need to be mentioned. In the case of the *P(industry)* and *PP(industry)* indicators, we have made an effort to identify industrial organizations as accurately as possible. Inevitably, however, there will be inaccuracies and omissions in the identification of industrial organizations. In the

case of the $P(<100 \text{ km})$, $pp(<100 \text{ km})$, $P(>5000 \text{ km})$, and $PP(>5000 \text{ km})$ indicators, we rely on geocoding of addresses listed in Web of Science. There may be some inaccuracies in the geocoding that we have performed, and for addresses that are used infrequently no geocodes may be available. In general, we expect these inaccuracies and omissions to have only a small effect on the indicators.

Open access indicators

The Leiden Ranking provides the following indicators of open access publishing:

- P . Total number of publications of a university.
- $P(OA)$ and $PP(OA)$. The number and the proportion of open access publications of a university.
- $P(\text{gold OA})$ and $PP(\text{gold OA})$. The number and the proportion of gold open access publications of a university. Gold open access publications are publications in an open access journal.
- $P(\text{hybrid OA})$ and $PP(\text{hybrid OA})$. The number and the proportion of hybrid open access publications of a university. Hybrid open access publications are publications in a subscription journal that are open access.
- $P(\text{bronze OA})$ and $PP(\text{bronze OA})$. The number and the proportion of bronze open access publications of a university. Bronze open access publications are publications in a journal that are open access without a license.
- $P(\text{green OA})$ and $PP(\text{green OA})$. The number and the proportion of green open access publications of a university. Green open access publications are publications in a journal that are also available in an open access repository.
- $P(OA \text{ unknown})$ and $PP(OA \text{ unknown})$. The number and the proportion of a university's publications for which the open access status is unknown. These publications typically do not have a DOI in the Web of Science database.

The different types of open access are partially overlapping. A publication can be both green open access and gold, hybrid, or bronze open access. In the calculation of the $P(OA)$ and $PP(OA)$ indicators, a publication is considered open access if it is green open access and/or gold, hybrid, or bronze open access.

The open access status of a publication is determined based on Unpaywall¹ data.

¹ <https://unpaywall.org>

Gender indicators

The Leiden Ranking provides the following indicators of gender diversity:

- A . The total number of authorships of a university. Consider for instance a publication that has five authors, of which three report university X as their affiliation and two report university Y as their affiliation. This publication then yields three authorships for university X and two authorships for university Y.
- $A(MF)$. The number of male and female authorships of a university, that is, a university's number of authorships for which the gender is known.
- $A(unknown)$ and $PA(unknown)$. The number of authorships of a university for which the gender is unknown and the number of authorships for which the gender is unknown as a proportion of a university's total number of authorships.
- $A(M)$, $PA(M)$, and $PA(M/MF)$. The number of male authorships of a university, the number of male authorships as a proportion of a university's total number of authorships, and the number of male authorships as a proportion of a university's number of male and female authorships.
- $A(F)$, $PA(F)$, and $PA(F/MF)$. The number of female authorships of a university, the number of female authorships as a proportion of a university's total number of authorships, and the number of female authorships as a proportion of a university's number of male and female authorships.

For each authorship of a university, the gender is determined using the following four-step procedure:

1. *Author disambiguation*. Using an author disambiguation algorithm developed by CWTS, authorships are linked to authors. If there is sufficient evidence to assume that different publications have been authored by the same individual, the algorithm links the corresponding authorships to the same author.
2. *Author-country linking*. Each author is linked to one or more countries. If the country of the author's first publication is the same as the country occurring most often in the author's publications, the author is linked to this country. Otherwise, the author is linked to all countries occurring in his or her publications.

3. *Retrieval of gender statistics.* For each author, gender statistics are collected from three sources: Gender API², Genderize.io³, and Gender Guesser⁴. Gender statistics are obtained based on the first name of an author and the countries to which the author is linked.
4. *Gender assignment.* For each author, a gender (male or female) is assigned if Gender API is able to determine the gender with a reported accuracy of more than 90%. If Gender API does not recognize the first name of an author, Gender Guesser and Genderize.io are used. If none of these sources is able to determine the gender of an author with sufficient accuracy, the gender is considered unknown.

Using the above procedure, the gender can be determined for about 70% of all authorships of universities included in the Leiden Ranking. For the remaining authorships, the gender is unknown.

Counting method

The scientific impact indicators in the Leiden Ranking can be calculated using either a full counting or a fractional counting method. The full counting method gives a full weight of one to each publication of a university. The fractional counting method gives less weight to collaborative publications than to non-collaborative ones. For instance, if a publication has been co-authored by five researchers and two of these researchers are affiliated with a particular university, the publication has a weight of $2 / 5 = 0.4$ in the calculation of the scientific impact indicators for this university. The fractional counting method leads to a more proper field normalization of scientific impact indicators and therefore to fairer comparisons between universities active in different fields. For this reason, fractional counting is the preferred counting method for the scientific impact indicators in the Leiden Ranking.

Collaboration, open access, and gender indicators are always calculated using the full counting method.

² <https://gender-api.com>

³ <https://genderize.io>

⁴ <https://pypi.org/project/gender-guesser/0.4.0/>

Trend analysis

To facilitate trend analyses, the Leiden Ranking provides statistics not only based on publications from the period 2014–2017, but also based on publications from earlier periods: 2006–2009, 2007–2010, ..., 2013–2016. The statistics for the different periods are calculated in a fully consistent way. For each period, citations are counted until the end of the first year after the period has ended. For instance, in the case of the period 2006–2009 citations are counted until the end of 2010, while in the case of the period 2014–2017 citations are counted until the end of 2018.

Stability intervals

Stability intervals provide some insight into the uncertainty in bibliometric statistics. A stability interval indicates a range of values of an indicator that are likely to be observed when the underlying set of publications changes. For instance, the PP(top 10%) indicator may be equal to 15.3% for a particular university, with a stability interval ranging from 14.1% to 16.5%. This means that the PP(top 10%) indicator equals 15.3% for this university, but that changes in the set of publications of the university may relatively easily lead to PP(top 10%) values in the range from 14.1% to 16.5%. The Leiden Ranking employs 95% stability intervals constructed using a statistical technique known as bootstrapping.

More information

More information on the indicators available in the Leiden Ranking can be found in a number of papers published by CWTS researchers. A detailed discussion of the Leiden Ranking is presented by Waltman et al. (2012). This paper relates to the 2011/2012 edition of the Leiden Ranking. Although the paper is not up-to-date anymore, it still provides relevant information on the Leiden Ranking. Field normalization of scientific impact indicators based on algorithmically defined fields is studied by Ruiz-Castillo and Waltman (2014). The methodology adopted in the Leiden Ranking for identifying core publications and core journals is outlined by Waltman and Van Eck (2013a, 2013b). Finally, the importance of using fractional rather than full counting in the calculation of field-normalized scientific impact indicators is explained by Waltman and Van Eck (2015).

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Ruiz-Castillo, J., & Waltman, L. (2015). Field-normalized citation impact indicators using algorithmically constructed classification systems of science. *Journal of Informetrics*, 9(1), 102-117. [doi:10.1016/j.joi.2014.11.010](https://doi.org/10.1016/j.joi.2014.11.010).

Waltman, L., & Van Eck, N.J. (2015). Field-normalized citation impact indicators and the choice of an appropriate counting method. *Journal of Informetrics*, 9(4), 872-894. [doi:10.1016/j.joi.2015.08.001](https://doi.org/10.1016/j.joi.2015.08.001).