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THE SUCCESS OF PRIMARY SCHOOL 4th GRADE STUDENTS IN THE "DIGIT SYSTEM" CONCEPT IN NATURAL NUMBERS

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Abstract:

The purpose of the present study was to examine the success of fourth grade primary school students in the "digit system "concept in natural numbers. The research was conducted with a mixed model. A total of 300 students who attended the fourth grades of two primary schools in Elazig city center, Turkey participated in the study. A test that consisted of 28 questions that were developed by examining the relevant literature and the mathematics curriculum of 2018 were used in the study. The reliability of the test was calculated by using the KR-20 formula, and the Reliability Coefficient was calculated to be .885. The data that were collected were analyzed by employing descriptive statistical methods together with the Content Analysis method. The results showed that 4th grade students had serious difficulties in understanding the "digit system" concept and that they had misconceptions in this respect. The overall success level of the students was found as 58%. The sub-learning area in which students had the highest difficulty levels was determined as "Subtraction in Natural Numbers", and the sub-learning area in which they were most successful was determined to be "Multiplication in Natural Numbers". The students reached the correct result at the highest level by using the calculation strategy and at the lowest level by using the estimation strategy. Again, the students had difficulty at the highest level in "writing the numbers given in an unusual way". Again, according to these findings, the highest mistake type was detected in the questions on the "digit system" (9 different mistakes), and the least error type was detected in the questions about showing the numbers using symbols and models (2 different mistakes). Depending on the results obtained from the study, suggestions were made to better teach the concept of the "digit system", which can be considered as the basis of mathematics education.

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1. Introduction

A full understanding of the "digit system" concept develops during the primary and secondary school processes (Van De Walle, Karp & Bay-Williams, 2014: 187). The "digit system" or the "digit value", which enables students to read and write very large and very small numbers with symbols with ease, is one of the most important features, and is also among the most abstract concepts of the number system and arithmetic we use in which a number takes its value according to its position in the numbers set. The "digit system", or the "digit value" can be defined as the value taken by the numbers according to their location in a number set (Tosun, 2011: 24). Thompson (2000) reported that most children could think of the "digit system" concept at a very early age; however, confusion on this issue continued for many years. Garlikov (2000), on the other hand, examined the studies conducted on the "digit system" concept and reported that children in America did not learn the "digit system" concept in an effective way. Again, Thompson and Bramald (2002) asked a question on kilometers to the students, and asked them to tell how many kilometers would be covered in case the indicator showed 06142 at first and then 06299. A total of only 24% of the 144 students (2nd, 3rd and 4th graders) were able to answer this question correctly.

According to Dinc, Artut and Tarim (2006), the teaching of the "digit system" concept during teaching numbers and operations is one of the biggest difficulties that children ever face. Ross (1985) conducted a study and examined the development of the "digit system" concept in 2nd-5th graders. They conducted the study with 60 students, and each student was asked about the similarity between the numbers in a two-digit number set and the amount of objects. It was observed that although most of the students in the study knew that 25 represented twenty-five objects, they did not know that "2" represented "20" and "5" represented the remaining "five objects". As a result, it was concluded that students should have knowledge of the "number" concept and of the relationship between "piece and whole" to understand the "digit system" concept. According to the results obtained in the study that was conducted by Kamii (1988), the rate of students who said that "1" meant "10" in 16 was 0% in the 2nd grade, 33% in the 4th grade, and 50% in the 5th grade. This shows that students have difficulties in distinguishing the "number" and "digit" value of the number set.

Rusch (1997) conducted a study to evaluate the understanding of the digit value concept of teacher candidates. A means of assessment was developed to be used in this study, and was used to obtain information on digit values unlike the operational skill. In the study, teacher candidates participated in a course, and the means of assessment was applied to them before and after this course. The results showed that many of the teacher candidates started the course with a superficial digit value approach, and completed it by realizing that this superficial understanding was far from the understanding they needed. Dinc, Artut and Tarım (2006) tried to determine how well 1st-5th grade students could learn the digit value concept, and what kind of mistakes

were made by those who could not learn it. The data they obtained showed that only 1.5% of the students could show 10 counting bars for "1" in the decimal digit of the number "16". They also observed that 98.5% of the students could not show this number correctly in the first stage; however, after a clue was given, 46.2% corrected the error and gave correct answers. In terms of gender, on the other hand, the difficulties were found to be similar. The representation of "zero" by children occurs relatively later than other representations in the number system. It is not difficult for children to represent the concept "nothing" with "0"but it is difficult to use "0"as a digit value (Sharma, 1993). Many children think that when it is used to represent a zero digit, zero means nothing. For example, "zero" represents "nothing" or an empty set alone but the zero in number "10"shows that there is no "1". The "zero" in the number "108"shows that there are no decimals (Olkun & Ucar, 2007: 94).

A total of seven students from 8th grade students participated in the study conducted by Kaplan (2008) to examine the perceptions of students on digit and digit values as separate concepts for each student. The results of the study showed that many of the students thought that the digit value was a place, and the concept of the digit value was the product of a multiplication. In addition, it was also observed that when the students explained their ideas about the digit concept and digit value in a number system that is different from the decimal number system, they continued their habits that came from the decimal number system. Macdonald (2008) conducted a study and examined the misconceptions of 7th grade students on digit values in decimal numbers. In this study, it was seen that a 7th grade student answered the question "What is the digit value of 8 in 6.781?" as "one tenth". The student, who thought that the structure of whole numbers was also valid for decimal numbers, explained the first digit after the comma as "one in first". According to the study, this stems from the fact that students do not understand that the digits of the decimal part in a number should be staged as "one tenth", "one hundredth", "one thousandth", etc.

In this study, the purpose was to examine the success status of 4th grade students in terms of digit values in natural numbers. For this purpose, the success levels of primary school 4th grade students in the digit value concept, and how they solved questions regarding the digit value concept, were examined.

2. Method

The study was conducted in two public schools in the city center of Elazig, Turkey. The research group was selected with the Purposeful Sampling method and the Convenient Sampling method by considering the number of students and teachers of the schools. All of the 4th grade students were invited to participate in the present study, and 300 students agreed to participate in the study voluntarily with their parental consents.

A success test for the digit value concept in natural numbers was developed to collect the data in the study. The preparation of the questions in the test was based on the mistakes of students emphasized in relevant literature considering the 17 acquisitions mentioned in the Primary School 4th grade mathematics curriculum of 2018.

Although according to the curriculum the digit concept is taught as of the 1st grade of primary school, there are several reasons for the selection of 4th grade primary school students in the study. Firstly, the acquisitions and skills of the digit concept are taught from the 1st grade in primary school according to the Elementary School Mathematics Teaching Program (2018). However, the researcher aimed to see the general development of the primary students by selecting the 4th grade students as participants because the learning objectives become more specific and detailed when 4th grade begins. Finally, 4th grade students were thought to be the most appropriate group for primary school level study because they would act better in thinking and problem solving compared to younger students.

In the test, there were four acquisitions on the digit concept in the natural numbers sub-learning area. In addition to these acquisitions, the researcher added the following acquisitions to the natural numbers sub-learning area; "The student shows the four-digit numbers by using the model"; "s/he expresses how many decimals are obtained from how many units, and how many hundreds are obtained from how many decimals"; and "s/he notices the relations between the numbers and patterns in the hundreds' table". The reason why these acquisitions were added was that these acquisitions were included in the Primary School 1st, 2nd and 3rd grade mathematics curriculum showing digits with models and expresses them in different ways. Similarly, two acquisitions were included in the sub-learning area of natural numbers in addition operations; two acquisitions were included in the subtraction operations in the natural numbers sub-learning area; two acquisitions were included in the multiplication operations in the natural numbers sub-learning area; and four acquisitions were included in the division in natural numbers sub-learning area in the draft achievement test. Examples of the questions in the test are given in Appendix 1. Necessary information was given to the primary school 4th grade teachers in the selected schools after the necessary permissions were obtained from the Directorate of National Education. The study was conducted by classroom teachers under the supervision of the researcher in all classes at the same time in the Spring Semester of the 2018-2019 Academic Year. The Achievement Test was applied as 14+14 questions with 10-minute intervals in two class hours considering the number of the problems that fourth graders could solve in one class hour. The application lasted 80 minutes in total. The students were asked to solve each problem by writing or drawing.

Expert opinions, relevant literature and the acquisitions in the digit concept in the 4th grade natural numbers curriculum of primary schools were made use of to ensure the content validity of the test. To ensure content validity, the developed test was presented to one professor and two associate professors working in the Class Teachers Education Department, and to two doctorate instructors working in the Education Programs and Teaching Department for expert opinion. The reliability of the test was calculated by using the KR-20 formula, and the Reliability Coefficient was calculated to be .885. Data analysis was carried out according to an answer key that was prepared together with the researcher and a field expert. The data were analyzed with the ITEMAN Program by scoring each correct answer with 1, and each false and empty answer with 0. Then, the correct and wrong solutions of the students were examined. In this way, it was determined which strategies students used to reach the correct answer and what mistakes they had made if the solution was wrong.

3. Findings

In this section, the results that were obtained from the Achievement Test, which was applied to 300 students to determine the achievement levels of primary school 4th grade students in terms of the digit concept, are given in line with the sub-themes determined by the researcher.

3.1 Findings on the problems on reading and writing numbers

There were 28 questions in the test intended to determine the level of understanding of the digit concept in natural numbers of primary school 4th grade students. Problems 1 and 2 were intended to test reading and writing. The students were asked to solve and also to explain each problem. The frequency and percentage values of the answers that were given by the students are given in Table 1. In this respect, 89% of students were able to read and write a five-digit number and the digits of a six-digit number, and also to determine and analyze the digits in the first question; and 87% of the students were successful in doing these in the second question.

	to the prob	olems on rea	iding and wi	riting numbe	rs	
	Correct	answer	Incorrec	ct answer	Empty	answer
	f	%	f	%	f	%
1 st Problem	267	89	33	11	0	0
2 nd Problem	261	87	39	13	0	0

Table 1: Frequency and percentage distributions of the answers given

The examples of correct and incorrect/inadequate answers that were given by the fourth grade students to the problems on reading and writing numbers are given in Table 2.

Question 1: Our teache	er has written in	Question2: What is the num	ber that has 9 in the hundreds
words the reading of a nu	umber on the board	of thousands digit, 8 in the	thousands digit, 2 in the
below. Write this number	below.	decimals digit, 7 in the units	s digit, and that is 0 in the sum
		of the decimals of thousand	s and hundreds digits? Show
Elli Bin Bir 🔍 🦦		it to Murat by writing it on	the dotted line below.
The answer accepted as	Students'	The answer accepted as	Students' strategies
correct	strategies	correct	
50.001	Naming	908.027	Naming
	(Naming a verbal		(Naming a number whose
	statement by		digits are given by writing
	writing it in		it in correct digits)

 Table 2: Sample student answer

	numbers)		
Answers that were	Students'	Answers that were accepted	Students' mistakes
accepted as	mistakes	as incorrect/insufficient	
incorrect/insufficient			
5000001	Expansion of the	9780627	Defining both the digit
510001	number		number incorrectly and
	(Expansion of the		placing the numbers in
	number as a		incorrect digits.
	result of using 0		
	and 1 more)		
5001	Reducing the	98027	Reducing the number
	number		(Reducing the number as a
	(Reducing the		result of using 0
	number as a		insufficiently)
	result of using 0	900827	Placing the numbers in
	insufficiently)		incorrect digits

All of the students who answered the questions on reading and writing numbers in a correct way answered the question by using the Naming Strategy. The students made two different mistakes in the first question, and three different mistakes in the second question. The common mistake of the students in both questions was to reduce the number as a result of using 0 in a misplaced way.

3.2 Findings on showing the numbers by using symbols and models

In the test, questions 3 and 6 were intended to measure the ability of students in representing the numbers using symbols and models. The frequency and percentage values of the answers given by the students are displayed in Table 3. According to these data, 51% of the students were successful in showing the digit values of the numbers by using some models and in showing the patterns and relations in the hundreds tables in the 3rd and 6th questions.

	Correct	answer	Incorrec	t answer	Empty	answer
	f	%	f	%	f	%
3 rd question	153	51	147	49	0	0
6 th question	153	51	135	45	12	4

Table 3: Frequency and percentage distributions of the answers givento the questions on showing numbers by using symbols and models

The examples of the answers that were accepted as correct and as incorrect/insufficient given by primary school 4th graders to the questions on showing numbers using symbols and models are presented in Table 4.

	Table 4: Sample	student answer		
Question 3.		Question 6.In the following h	undreds tables;	
How do you complete the nur	nber above given in	represents the number = 35. H	How do we find the	
the hundreds' blocks by using	the hundred and ten	result of 35+ 28 by moving the ball to the right, left,		
blocks? Show below by drawi	ng.	up and down? Show it on the	e table by drawing.	
The answer accepted as	Students' strategies	The answer accepted as	Students' strategies	
correct		correct		
10 x + = 1010 To obtain 1010, it is necessary to use ten 100's blocksandone 10's block.	Representing - Calculating (Expressing the given natural number by using standard representations and by making use of the four operations)	If I go down 1 square, it becomes 45; if I go down 1 square more, it becomes 55. Then I move towards right for 8 squares in 8 units, and it becomes 63.	Representation (Reaching the result by making use of the patterns and connections indicated by the given representation.)	
Answers that were accepted	Students' mistakes	Answers that were	Students' mistakes	
as incorrect/insufficient		accepted as		
		incorrect/insufficient		
If I add one hundred's block and one ten's block, it makes 1010.	Confusing the models (Thinking as if the hundred's block were the thousand's block)	1 90 11 90 13 90 14 90 15 90 11 90 12 90 13 90 14 90 15 90 16 70 17 20 18 90 19 90 10 90 11 90		
I draw 10 hundreds block, and then I draw 10 decimal blocks If I draw ten from 10's block, I find the result.	Confusing the models (Thinking as if the decimal block were unit block) Missing modeling (Not using decimals blocks)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Not knowing the patterns in the hundred's table	

Table 1. Sample student answer

The students who gave correct answers to the questions on showing numbers by using symbols and models did so by using representation and calculation strategies. The students made two different mistakes in the in the 3rd question. However, all of the students who gave incorrect answers in the 6th question did so because they did not know the patterns in the hundred's tables.

3.3 Findings on the questions on understanding the relationship between digits

In the test, questions 4, 5, 7, 8 and 9 were on understanding the relation between the digits. The frequency and percentage values of the answers of the students given to

these questions are given in Table 5. According to these data, 45% of the students succeeded in rounding numbers to the nearest decimal, sorting numbers using big/small symbols, and stating numbers in different ways as units, decimals and hundreds in question 4; 51% succeeded in doing these in question 5; 76% students in question 7; 42% students in question 8; and 58% students in question 9.

	Correct a	nswer	Incorrect	answer	Empty	answer
	f	%	f	%	f	%
4 th question	135	45	135	45	30	10
5 th question	153	51	129	43	18	6
7 th question	228	76	72	24	0	0
8 th question	126	42	165	55	9	3
9 th question	174	58	120	40	6	2

Table 5: Distributions of the frequency and percentage of the answers to the questions on the relationship between digits

The examples of the answers of the fourth graders that were accepted as correct or incorrect/insufficient given to the questions on the relationship between the digits are presented in Table 6.

Table 6: Sample student answer

Question 4. If I am 341, and if I have 22 decimals, how many hundreds do I have left? Show it on the dotted area below by writing.

hundred, 2 decimals, and300 units2 thousands in 121.3 4 1- 2 2unusual way	Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
	- 2 0 2 2 1 1 22 decimals make 220, if I subtract 220 from 341, I find 121, and there are 1 hundred, 2 decimals, and	(Finding the result	divide 341 by 100,I find 3. 3 4 1 + 2 2 3 6 3 300 units 3 4 1 - 2 2	data in the operation (not considering 22 decimals) Not being able to write the number given in an unusual way (writing 22 decimals as

Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
$ \begin{array}{c cccc} 658 & 10 \\ 60 & 65 \\ \hline 058 \\ -50 \\ \hline 8 \\ \hline I divide 658 by 10 to find \end{array} $	Calculation (Finding the result by dividing)	There are maximum 58 decimals in 658	Not analyzing the number (Thinking as if the number were given in decimals by
how many 10s are there			combining the units and decimals digit)

in 658.the result was 65.		There are maximum 60 decimals in 658 because. 6	Not including all data in the operation
		hundreds means 60.	(Considering only the
		There are maximum 5	hundreds digit)
		decimals in 658. Because,	
		there is 5 in the decimals	
		digit.	
Question 7. Round 59099 to	the nearest decimal c	ligit. Write your answer to the	dotted area below.
Sample answer that was	Students'	Sample answer that was	Students' mistakes
accepted as correct	strategies	accepted as	
	Prediction	incorrect/insufficient	
59.100 In case the number	(Applying the	60.000	Not knowing the
in the units digit is	"Rounding Rule")		"Rounding Rule"
0,1,2,3,4, and if the			(Considering the
number is 5 and over, it is			biggest digit when
rounded to an upper			rounding, or rounding
number, I did this for this			to the nearest hundred
reason.			digit instead of the
			nearest decimal digit)
		59.000	Not knowing the
			"Rounding Rule"
			(Rounding to the next
			lower hundredth)
		590100	Not knowing the
			"Rounding Rule"
			Writing the nearest
			decimal value directly

Ayse uses Road A on her way to school, and Road B on her way back home from school. Ayse describes the length of Road A as "1 hundred + 22 decimals "meters; and describes the length of Road B as "32 decimals + 5 units" meters. Which road is longer for Ayse, the departure road or the return road? Explain it by writing to the dotted place below.

Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
A=100+ 22 x 10 + 0 = 320	Re-naming-	Road A 1220	Not being able to write
makes 1 hundred (100). 22	Comparison	Road B is longer than road	the number given in an
decimals make 220, we	(Finding two	325 A.	unusual way
add them, the result is	numbers given in		(writing 1 hundred digit
320,I mean, road A is 320	an unusual way		as 1 thousand digit)
m long.	according to their	Road A, because there is a	Not including all the
B=32 x 10 + 5 = 325. Here,	being big or small)	hundred.	data to the operation
there are 32 decimals,			(Considering the
which makes 320. If I add			number values in the
units to it, it makes 325m.			digits in an
I mean, road B is longer.			independent manner)

Because, 325 is bigger		A= 122	Not including all the
than 320 by 5 units.		B=37	data to the operation
2			(writing 32 decimals as
			32 units)
Question 9. Which of the ab	ove numbers is smalle	er than 2 decimals and 54 units	s? Circle these numbers
and write why they are sma	all.		
Sample answer that was	Students'	Sample answer that was	Students' mistakes
accepted as correct	strategies	accepted as	
		incorrect/insufficient	
12, 41 and 52;since the	Re-naming-	54+2 = 56 →	Not being able to write
numbers in the decimals	Comparison	56>12,41,52	the number given in an
digit here are smaller	(Finding the two		unusual way
than 7, 74> 12, 41, 5274<89	numbers given in		(writing 2 decimals as 2
	an unusual way		units)
	being big or small)	20+54=74	Not knowing the digit
	2 decimals + 54	There are 4 decimals in 74.	value
	units =74	However, since there are 2	(Confusing the place of
		units and 2 decimals in 12,	units and decimals)
		41, 52, 74>12,41,52	,
		Since it says54 units, 12, 41	Not knowing the
		and 52's units are smaller	"Comparison Rule"
		than 4.	(Not knowing what to
		54>12,41,52	consider when
			comparing the numbers
			as small/big)

Fourth graders answered the questions on the relationship between the digits correctly by using calculation, re-naming, comparison and prediction strategies. The students used the same strategies when they solved the 4th, 5th, 8th and 9th questions. The students made two different mistakes in the 4th, 5th and 8th questions; one different mistake in the 7th question, and three different mistakes in the 9th question. In general, most of the mistakes of the students in the questions on the relationship between the digits were mostly not including all data in the operation, not being able to write the number given in an unusual way, not analyzing the number, not knowing the "Rounding Rule", not knowing the digit value and not knowing the comparison rule.

3.4 Findings on the questions on four operations in natural numbers

Questions 10, 15, 19, 21, 22, 23, 24 and 25 in the test were about four operations in natural numbers. The frequency and percentage values of the answers of the students for these questions are given in Table 6. As seen in Table 6, 87% of the students gave correct answers in the 10th question; 64% of them gave correct answers in the 15th and 25th questions; 62% of them gave correct answers in the 19th question; 56% of them gave correct answers in the 21st question; and 60% of them gave correct answers in the 22nd, 23rd and 24th questions.

Based on this finding, it is possible to argue that students are successful in adding and subtracting two four-digit numbers, multiplying a three-digit number by a two-digit number, dividing a three-digit number by a two-digit number, dividing a

four-digit number by a one-digit number, and dividing a five-digit number with the last digit being 0 by 10 and the multiples of 10.

	Correct answer		Incorrect	answer	Empty answer	
	f	%	f	%	f	%
10 th question	261	87	30	10	9	3
15 th question	192	64	105	35	3	1
19 th question	186	62	105	35	9	3
21 st question	168	56	120	40	12	4
22 nd question	180	60	120	40	0	0
23 rd question	180	60	117	39	3	1
24 th question	180	60	114	38	6	2
25 th question	162	64	120	30	18	6

Table 7: Frequency and percentage distributions of the answers of the students given to the questions on four operations in natural numbers

The examples of the answers that were accepted as correct and the answers that were accepted as incorrect/insufficient of primary school 4th graders on four operations in natural numbers are presented in Table 8.

Table 8: Sample student answer				
Question 10. $\frac{^{1358}}{^{+1276}}$ Solve the a	addition given he	ere, and explain how it is solved.		
Sample answer that was	Students'	Sample answer that was accepted	Students'	
accepted as correct	strategies	as incorrect/insufficient	mistakes	
1358 +1276 2634 I start on the right and add towards the left. Since8+6=14, I write 4 from 14 to the units digit, and transfer 1 decimal to the decimals digit. 5+7=12, here, there were ten waiting, It made 13. I write 3. decimals to the decimals digit. I transfer the 10 decimals as 1 hundreds to the hundred digit.	Calculation (Finding the result by adding)	1358 +1276 2624 $8+6=14$, I write 4 from 14. I write 2 from 12 in 5+7=12. There was 1 waiting in 3+2=5. If I add 1 to it, it makes 6. 1+1=2. The result is 2624. 1358 +1276 2644 $8+6=14$, here, I write 4 from 14. 5+7=12, here, there is 2 waiting, it makes 14. 3+2=5, here, there was 1 waiting. It makes 6. 1+1=2. The result is 2644. 1358 +1276 3634 $8+6=14$. In 14,I have 1 waiting. 5+7=12, here, if I add 1, it makes 13. I write 3 from 13. Again, I have 1 waiting here. 3+2=5, here, I have 1 waiting. It makes 6. 1+1=2, and I have 1 waiting. The result is 3634.	Not knowing how to make the operation (Transferring missing decimals) Not knowing how to make the operation (Transferring excessive decimals)	

Table Q. Commole stude

Question 15. 6000 -3009

Solve the subtraction given here, and explain how you solve to Ahmet by writing.

Sample answer that was	Students'	Sample answer that was accepted	Students'
accepted as correct	strategies	as incorrect/insufficient	mistakes
10-9=1 9 0-9 9 0-9 5-3=2 2991 The bigger number cannot be subtracted from a smaller number, so, I take 1 decimal from the decimals digit. If it is not possible, I take a hundred from the	Calculation (Finding the result by subtracting)	6000 <u>-3009</u> <u>3091</u> We cannot subtract 9 from 0. We take a decimal from the neighbor. If we subtract 9 from 10, we have 1. We have 9 here. If we subtract 0 from 9, we have 9. If we subtract 0 from 0, again, we have 0. If we subtract 3 from 6, we have 3. <u>6000</u>	Not knowing how to make the operation (Transferring a decimal to the units digit from the thousands digit) Not knowing how
hundreds digit, if it is not possible, I take a thousand from the thousands digit.		$\frac{-3009}{2001}$ It is not possible to subtract 9 from 0. I go to the neighbor, but, since they are 0, I go to 6. If we subtract 9 from 10, we have 1. There was 5 here. If we subtract 3 from 5, we have 2. The result is 2001	to make the operation (Transferring decimals to the units digit from the units digit by ignoring the hundreds and decimals digits)
		6000 <u>-3009</u> 2891 It is not possible to subtract 9 from 0. We need to go to the neighbor and take a decimal. Since there are 0 in the decimals and hundreds digits, we go to the thousands digit. We take from the thousands digit and give it to the hundreds digit. Then we take it from there, and give it to the decimals digit. We take it from there and give it to the units digit. We have 10-9=1. There is 9 left in the decimals digit. There is 8 left in the hundreds digit. If we subtract 3 from 5, we have 2. The result is 2891.	Not knowing how to make the operation (Subtracting two hundreds from the hundreds digit in the subtracting operation)
890 X 99			
		left, and explain how you solve by writir	
Sample answer that was	Students'	Sample answer that was accepted	Students'

Sample answer that was	Students'	Sample answer that was accepted	Students'
accepted as correct	strategies	as incorrect/insufficient	mistakes

8 9 0	Calculation	8 9 0 X 9 9	Not knowing how
	(Finding the		to make the
8 0 1 0	result by	7 3 8 8	operation
8 8 1 1 0	multiplying)	7 3 8 9 0 9x0=0, 9x9=81, 81;	-
		here, I write 1. 9x8=72, 72; here, I	
		write 2. Then, I go to the other side.	
		9x9=81; here, I had 7 waiting, and it	
		became88. 9x8=72; here, we had 1	
		waiting, it made 73. When we add	
		them, it is 73890.	
		8 9 0 X 9 9	Not knowing how
			to make the
		8 0 1 0	operation
		1 6 0 2 0 9x0=0, 9x9=81; here,	(Not knowing
		we write 1. 9x8=72 becomes 80 when	digit transfer in
		added 8. Since all numbers are the	multiplication)
		same, here it becomes 8010. When	
		we add them, we find 16020.	
		8 9 0	Not knowing how
		1 6 2 8 0	to make the
		9x0=0, 9x9=81, 81;	operation
		here, I write 8. 9x8=72; here, I write 2	(Writing the
		from 72. I multiply8 by 2, and obtain	results obtained
		16. The result is 16280.	side by side)

333 11

Question 21. Solve the division on the side, and explain how you solved it to Ali.

Sample answer that was	Students'	Sample answer that was accepted	Students'
accepted as correct	strategies	as incorrect/insufficient	mistakes
333 11 -33 30 003 Since we start division from the left, firstly, since there is no 11 in 3, I look into 33. Since there are 3 times of 11 in 33, we obtain 3x11, 33 and 33-33=0. Since there are no11 in 0, we take 3 below, and since there are no 11 in 3, I add 0 to the division section.	Calculation (Finding the result by dividing)	There are no 11 in 33. We find 3 when we divide 33 by 11. 331 333 332 333 332 333 332 333 332 333 332 333 332 333 332 333 332 333 332 333 332 333 332	Not knowing how to do the operation (When the small number is not divided by the bigger number, not knowing how to continue the operation) Not knowing how to make the operation (Not knowing when to put 0 and comma to the division section)

		There are 3 times 1 in 3. If we subtract 3 from 3, we have 0. We take 3 down. We should always do the same operation.	Not knowing how to make the operation (Dividing each digit separately)
Question 24. 11000÷110 Exp	lain how this oper	ration can be solved in a short way by so	olving it.
Sample answer that was	Students'	Sample answer that was accepted	Students'
accepted as correct	strategies	as incorrect/insufficient	mistakes
11000÷ 110= 100	Calculation (Finding the result by the	11000 ÷ 110= 1100 11000÷ 110= 10	Not knowing how to make the operation
	rule of deleting 0)	11000÷110= 110	(Not knowing how to divide 10 and 10s in a short way)
Question25 Explain	how this operati	on can be solved in a short way by solvi	ng it.
Sample answer that was	Students'	Sample answer that was accepted	Students'
accepted as correct	strategies	as incorrect/insufficient	mistakes
$\begin{array}{c c} 9306 & 6 \\ -6 & 1551 \\ -30 \\ -30 \\ 006 \\ -6 \\ 00 \end{array}$ There are one 6 in 9. We write 1 to the division section. 1x6=6. If we subtract 6 from 9, we have 3. Since there are no 6 in 3, we take the other 3 down. There are 5 times 6 in 23	Calculation (Finding the result by dividing)	$\begin{array}{c c} 9306 & 6 \\ \hline 156 \\ \hline 33 \\ \hline -30 \\ \hline 036 \\ \hline -36 \\ \hline 00 \\ \end{array}$ If we divide 9 by 6, we have 1. We have 1x6=6. If we subtract 6 from 9, we have 3. We take the other 3 down. There are 5 times 6 in 33. We subtract again, we will have 3 again. We take 6 down again. There are 6 times 6 in 36. $\begin{array}{c} 9306 & 6 \\ \hline 9306 & 6 \end{array}$	Not including some numbers in the operation (Forgetting the 0 in the decimals digit of 9306)
There are 5 times 6 in 33. The operation goes on like this.		$\begin{array}{c} \begin{array}{c} -6 \\ \hline 33 \\ \hline 33 \\ \hline 30 \\ \hline 00 \\ \hline 00 \\ \hline \end{array}$ We find 1 if we divide 9 by 6.We have 1x6=6. If we subtract 6 from 9, we have 3.We take the other 3 down. There are 5 times 6 in 33. 5 times 6 is 30. When we subtract it, we have 3 again. 0 goes down, and we have 5 times 6 in 30. We write 6 here.	Not including some numbers in the operation (Writing the 6 in the unit digit of 9306 to the division section without including it in the operation)

9306 6 -6 15 33 -30 03	Not including some numbers in the operation
If we divide 9 by 6, we have 1. We	(Not including the
have 1x6=6. If we subtract 6 from 9,	units and decimals
we have 3. We take the other 3	digits of 9306 in
down. There are 5 times 6 in 33. We	the operation)
have 5x6=30. We subtract 30 from	_
33, and have 3.	

According to the findings in Table 8, all of the students who gave correct answers to the questions on four operations in natural numbers reached correct results by using the calculation strategy. Again, fourth graders gave incorrect answers to the questions because they did not know how to do four operations, and also, they did not include some numbers of the given number.

3.5 Findings on solving problems on the digit concept

Questions 11, 12, 13, 14, 16, 17, 18, 20, 26, 27 and 28 in the test were regarding the digit concept. The frequency and percentage values of the answers given by the students to these questions are given in Table 9. According to the findings given in Table 8, the correct answers provided by the students are as follows: 53% of 4th graders gave correct answers in the 11th and 16th questions, 49% in the 12th question, 57% in the 13th question, 58% in the 14th question, 42% in the 17th and 26th questions, 38% in the 18th question, 62% in the 20th and 28th questions, and 45% in the 27th question. Based on these findings, it is possible to argue that primary school 4th grade students are successful in solving problems that require addition, subtraction, multiplication and division in natural numbers.

	given by the students to these questions					
	Correct	Correct answer		t answer	Empty answer	
	f	%	f	%	f	%
11 th question	159	53	138	46	3	1
12 th question	147	49	150	50	3	1
13 th question	171	57	120	40	9	3
14 th question	174	58	126	42	0	0
16 th question	159	53	135	45	6	2
17 th question	126	42	165	55	9	3
18 th question	114	38	180	60	6	2
20 th question	186	62	105	35	9	3
26 th question	126	42	165	55	9	3
27 th question	135	45	165	55	0	0
28 th question	186	62	114	38	0	0

Table 9: The frequency and percentage values of the answers given by the students to these questions

The examples of the answers of primary school 4th grade students that were accepted as correct or incorrect/insufficient for problems related to the digit concept are presented in Table 10.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as incorrect/insufficient	mistakes
87404	Calculation	We must add 50	Confusing the
- 87354	(Finding the	decimals.	multiplication
	result by		value and the
00050	subtraction)		digit value.
I start the operation from the right			
side with the unit's digit. Since 4-4 is		87404	Not knowing
0, and it is not possible to subtract 5		-87354	how to make the
from 0 in the decimals digit, I take 1		09050	operation
hundred from 4 in the hundreds digit			(Erroneous
and transfer it to the decimals digit.			decimals
Since there are 1 hundred and 10			analysis)
decimals, we have 5 decimals when		87404	Not knowing
we subtract 5 decimals from 10		-87354	how to do the
decimals. Since there are 3 hundreds		00100	operation
in the hundreds digit, it we subtract 3			(Not reducing
hundred from 3 hundred, we have 0.			decimals from
We have 0 if we subtract 7 thousand			the hundreds
from 7 thousand and 8 ten-thousand			digit)
from 8 ten-thousand. The result is 5			-
decimals.			

Table 10: Sample student answer

Question 11. How many decimals will make Ali obtain 87404 by adding to 87354? Show it by solving in

Question 12. 8a3a is a four-digit number. If the sum of digit values of "a "sis 202, what is the number value of "a"? Explain this operation by solving it.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as incorrect/insufficient	mistakes
100 x a + 1 x a = 101 x a =202 a =2 8 x1000+ a x 100+ 3x 10+a 8000+100a+30+a=100a+a=2 x100+ 2a=2	Re-naming (Finding the result by analyzing the number)	$\begin{array}{c} 2022\\ 2101a = 101\\ 002\\ -2\\ 0\\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	Not being able to define the number value.

Question 13. The li	ist of some products and their prices in a market	are as follows.
Product	Price	
ALLS	4 decimals 11 units TL	
	50 units TL	
1	1 decimals 3 units TL	

In this context, how much will a person who buys 1 a clutch of eggs, 1 kg yogurt and 1 package flour will pay? Explain the operation by solving it below.

Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
Eggs 4x10+11= 51	Re-naming-	1 a clutch of eggs 411,1	Not being able to
Flour =50	Calculation	package of flour 50, 1	write the number
Yogurt =1 x10 +3 =13 we add them	(Finding the	kg yogurt 13411+50+13=	given in an
together.	result by adding	474	unusual way
50+51+13=114	the numbers		(Considering 4
	given in usual		decimals as 4
	and unusual		hundreds)
	way)	Eggs 51, Flour500,	Not being able to
		Yogurt 13	write the number
		500+51+13=564	given in an
			unusual way
			(Writing 50 units
			as 50 decimals)
		4,11	Not being able to
		5,0	write the number
		+ 1,3	given in an
		10, 41	unusual way
			(Confusing with
			decimals)

Question 14. For which two of the above products will Ayşe pay more to the market? Explain it by solving this problem below

Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
Eggs 4 decimals + 11 units=51 Flour 50 units=5051+50=101. For this	Re-naming- Calculation	Eggs 51 and yogurt 13.	Insufficient answer
reason, if I buy these two products, I will pay more.	(Finding the result by adding two numbers given in an unusual way)	4.11+1.03=5.14 Eggs and yogurt	Not being able to write the number given in an unusual way (Confusing with decimals)

114+51+50=215	Not being able to write the number
	given in an
	unusual way
	(Writing 4
	decimals and 11
	units as 11
	decimals and 4
	units)

Question 16. Ahmet has 426 liras. He gave 13 ten liras and 6 one Liras. How much money does Ahmet left? Explain it by solving.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as	mistakes
		incorrect/insufficient	
13x10= 130, 130+6=136, 426-136=290	Re-naming-	426 413	Not being able to
13 ten Liras makes 130 Liras. And oh,	Calculation	-13 - 6	write the number
there is also 6 thousand Liras. If I add	(Finding the	413 407	given in an
them, it makes 136 Liras. If I subtract	number given in		unusual way
this from Ahmet's money, I will find	an unusual way,		(Writing in the
how much money he has left. The	finding the result		form of 13
result is 290 Liras.	with operations)		decimals and 13
			units)
		26-13=13	Not including all
		If we subtract 13	of the numbers
		decimals from 26	in the operation.
		decimals, we have	
		13decimals. We also	
		subtract 3 units from 6	
		units.	
		6-3=3	
		There are 40 decimals in	Not analyzing
		426.	the number
		40-13=27	(Not including
		27-6=23	the decimal in
			the decimals
			digit)

Question 17. If the decimal and hundred digits of 1896 change, how does the value of the number change? Explain this by solving below.

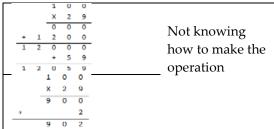
Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as incorrect/insufficient	Students' mistakes
There is 9 in the decimals digit, and there is 8 in the hundreds digit. If we replace them, we have 1986. 1986- 1896=90 Here, we have a reduction.	Calculation (Finding the result by subtracting)	1896-1698=198	Confusing the place of the digits (Replacing the units digit and hundreds digit)
		1986-1896=100	Not knowing
		1986-1896= 80 Here, we have an increase.	how to make the operation

Question 18. My father bought a refrigerator and a television to our house, and paid6541 Liras. Since he
paid 1 thousand and 13 hundreds to the seller as the price of the television, how much is the price of the
refrigerator? Explain it by solving.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as	mistakes
		incorrect/insufficient	
1 thousand= 1000	Re-naming-	1000+130=1130 I add 1	Not being able to
1 hundreds= 100	Calculation	thousand and 13	write the number
100x 13=1300	(Finding the	hundreds. If I subtract	given in an
1300+1000=2300	number given in	6541,I find the price of	unusual way
6541-2300= 4241	an unusual way,	the refrigerator.	(Writing 13
	and finding the	6541-1130=5411	hundreds as 13
	result with		decimals)
	operation)	1000+13=1013 Since the	Not being able to
		price of the television is	write the numbe
		1 thousand and 13	given in an
		hundreds, I add them	unusual way
		together.	(Writing 13
		6541-1013=5528 Then, if	hundreds as if it
		I subtract it from 6541,I	were 13 units)
		find the result.	
		6541-1013=5428	Not being able to
		Since there are 1	write the numbe
		thousand and 13	given in an
		hundreds, which makes	unusual way and
		1013 Liras, I subtract	making mistake
		1013 from 6541.	in the operation
			(Writing 13
			hundreds as 13
			units, and
			reducing
			decimals in the
			hundreds digit
			more than
			necessary)

Question 20. There are a total of 30 boxes in the greengrocery of Ali. Although there are 100 apples in 29 of these boxes, there are 59 apples in the 30th box. How many apples are there in the greengrocery of Ali? Explain it by solving below.

Sample answer that was accepted as correct	Students' strategies	Sample answer that was accepted as	Students' mistakes
		incorrect/insufficient	
29 x100=2900	Calculation	29 x 100= 290	Not knowing
Since there are 59 in the last box, I add	(Finding the	Since there are 100	how to make the
59 to 2900.	result by	apples in 29 boxes, I	operation
2900+59=2959	multiplication	multiply by 100 and	(Not knowing
	and addition)	then, add 59. Because	how to multiply
		there are 59 apples in 1	by 100 in a short
		box.	way)
		290+59=349	



Question 26. A grandfather wants to divide 3207 liras evenly to his 3 children. How should this grandfather do this sharing? Explain it by solving below.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as	mistakes
$\frac{3207}{-3} \frac{3}{1069}$ There are 1 three in 3. 1 times 3 is 3. I subtract, and have 0. There is no 3 in 0. There is no 3 in 2. For this reason, I leave 0 here. Then, if I bring the 0 above, I have 20, and then I divide it by 20.	Calculation (Finding the result by dividing)	$\begin{array}{c c} incorrect/insufficient \\ \hline 3207 & 3 \\ \hline -3 & 169 \\ \hline 020 & -18 \\ \hline 27 & -27 \\ \hline 00 \\ \hline I divided by 3 because there are 3 classes. \\ \hline 3207 & 3 \\ \hline -3 & -161 \\ \hline 020 & -18 \\ \hline -27 & -21 \\ \hline -6 \\ \hline 3207 & 3 \\ \hline -3 & -161 \\ \hline 020 & -18 \\ \hline -27 & -21 \\ \hline -6 \\ \hline 3207 & 3 \\ \hline -3 & -161 \\ \hline 020 & -18 \\ \hline -27 & -27 \\ \hline 00 \\ \hline \end{array}$	Not knowing how to make the operation (Not knowing when to add 0 to the division section)

Question 27. Ali grouped the eggs firstly in tens and obtained 500 boxes. Then he realized that the number of the boxes was too much, and decided to group the boxes in 100s. How many boxes will Ali have now? Explain the operation by solving.

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as	mistakes
		incorrect/insufficient	
10 x 500= 5000		500÷100= 5. 500 If I	Not including all
5000 ÷ 100= 50	Calculation	divide the box by 100,	data in the
	(Multiplication	how many boxes can I	operation
	and finding the	have? The result is 5	
	result by	500 x 10= 5000	Not knowing
	dividing)	5000÷100= 500	how to make the
			operation
			(Not knowing
			how to make
			division shortly
			with 100)
		10 ÷ 5= 2	Insufficient
			answer
Question 28. We want to distribute 125	books we have to th	e classes as 2 decimals and	l 5 units. To how
many classes can we distribute these be	ooks? Explain it by so	olving.	
Sample answer that was accorted as	Students'	Sample answer that	Students'

Sample answer that was accepted as	Students'	Sample answer that	Students'
correct	strategies	was accepted as	mistakes
		incorrect/insufficient	

125 25 -125 5 000	2 decimals and 5 units=25	Re-naming- Calculation (Finding the	125 5 -125 50 000	Not including all data in the operation
		number given in the usual way, and finding the result with	125 25 -120 6 000	Not knowing how to make the operation
		proper operation)	$ \begin{array}{c} 125 & 7 \\ -7 & 17 \\ 55 \\ -49 \\ \hline 6 & 2 \text{ decimal} + 5 \\ \text{units} = 7 \end{array} $	Not being able to write the number given in an unusual way (Writing 2 decimalsas2 units)

According to the findings in Table 10, primary school 4th grade students gave correct answers on the questions that were related to digit values by using calculation and renaming strategies. Students gave incorrect answers to the questions due to the following reasons: Not being able to write the number given in an unusual way, not knowing how to do four operations, confusing multiplicity and number values, not knowing the value of the number, not including all the digits of the given number in the operation, confusing the places of the number, including the data that are not given in the question, not analyzing the number given, and insufficient answers.

4. Result and Discussion

Although this study, in which the level of knowledge of primary school fourth grade students on the digit concept in natural numbers and the ways of solving the questions were examined, was limited with the findings obtained from the sampling and data collection tool, it yielded very important results. When the correct answer rates of the students on the digit concept in natural numbers are considered, it may be argued that more than half (58%) of the students have good knowledge on the digit concept in natural numbers. However, when the correct answer rates of the acquisitions are examined in terms of 75% learning level in the study, it is seen that primary school 4th grade students have not achieved many acquisitions. The achievements that had a correct answer rate of 75% or more were K1 (89%), K2 (87%), K3 (76%) and K8 (87%). Although K1, K2 and K3 acquisitions are in the Natural Numbers sub-learning domain, K8 acquisition is in the Addition in Natural Numbers sub-learning domain. When this finding is considered, it is seen that primary school fourth grade students have serious difficulties in understanding and using the digit concept in natural numbers in an effective way in operations. Kamii (1988) investigated grades 1, 3 and 4 reporting that none of the 1st grades, 33% of the 3rd grades, and only 50% of the 4th grades could give correct answers to the digit concept. The results of our study are in line with the results reported by Kamii (1988). In their study, Thompson ve Bramald (2002) concluded that 4

students were very good at their step value, 14 students were good, 28 students were middle and 46 students were above middle.

When the correct answer percentages are accepted as the success rates, the sublearning area in which the students were successful at the highest rate was Multiplication in Natural Numbers with an average correct answer rate of 62% (f=186). The sub-learning area in which primary school fourth grade students had the most difficulty with an average correct answer rate of 49% (f=147),was the Subtraction Operation in Natural Numbers The average correct answer percentages of Natural Numbers and Addition in Natural Numbers are the same (61%; f=183). Again, the average correct answer of students in the Division in Natural Numbers is 56% (f=168).

In general, the most successful achievement of primary school fourth grade students was the K1 acquisition, with an 89% (f=267) correct answer percentage. The most difficult acquisition was K11 with a correct answer percentage of 44% (f=132). Again, the question in which the students were successful at the highest rate was the 1st question with a correct answer percentage of 89% (f=267). The question the students had the highest difficulty was the 8th, 17th and 26th questions with a correct answer percentage of 42% (f=126). Dinc, Artut and Tarım (2006) reported that only 1.5% of 728 primary school fourth grade students could show 10 counting bars for "1" in the decimals digit of 16.

When the solution methods in the correct answers given by primary school 4th grade students to the questions in the success test were examined, it was seen that these were naming, re-naming, representation, prediction, comparison and calculation. Although students achieved the correct result mostly by using a single strategy in the question, they reached the correct result by using two strategies together in some questions. While the most commonly used strategy by the students was the calculation strategy, the least used strategy was the prediction strategy. When the strategies that were used by the students were examined in terms of the sub-learning domains, it was seen that the primary school fourth grade students mostly used the naming strategy in the Natural Numbers sub-learning domain, they had the correct result by using the calculation strategy in Addition, Subtraction, Multiplication in Natural Numbers and Division in Natural Numbers sub-learning domains.

Again, it is possible to argue that the correct forms of answers given by primary school 4th grade students to the The Achievement Test questions were mostly based on the usual rules taught at school (rounding rule, big/small rule, etc.). The students mostly found the correct answer by using a single and similar strategy, and the students applied the rules based on the digits that were taught at school rather than using student-invented strategies.

When the wrong ways of solving the questions in The Achievement Test of the 4th grade students are examined, it is seen that the students gave incorrect answers to the questions because of seventeen different mistakes. The students made more than one mistake in each question. The students had difficulty mostly in "writing the number given in an unusual way". According to these findings, again, the highest error type was detected in the questions that were on the digit concept (9 different mistakes),

and the lowest error type was detected in the questions that required showing numbers by using symbols and models (2 different mistakes). Engelhardt (1977) identified eight different errors in his study in which he administered 84 arithmetic tests to 194 students. Students have difficulty with concepts 0 and 1 when calculating at an early age (Engelhardt, 1977). This is much more so in transactions involving the concept of 0 (Cockburn & Parslow-Williams, 2008). Children with zero and one concepts also frequently cause conceptual difficulties (Bamberger, Oberdorf and Schultz Ferrell 2010; Cockburn and Litter, 2008; Engelhardt, 1977; Van de Walle, Karp and Williams, 2014). Önal (2017) stated that the error made at the highest level within the mistakes made by the students was the error of "placing the digits in the wrong place" by 19.75%. When the mistakes made by the students according to the sub-learning domains were examined, it was seen that students had difficulties mostly in "writing a number that is given in an unusual way" in the Natural Numbers, Addition in Natural Numbers and Subtraction in Natural Numbers sub-learning domains. However, students gave incorrect answers to the questions that were related to "not being able to do four operations" in the Multiplication in Natural Numbers and Division in Natural Numbers sub-learning domains. Yorulmaz and Önal (2017) studies revealed that students made more mistakes in adding the eldest in the picking process, breaking the tenner in the subtraction process, scrolling the digits in the multiplication process, and assigning zero to the division in the splitting process.

Kubanç and Varol (2017) in their study, second and third grade students 'multiplication process; subtraction instead of multiplication, addition instead of multiplication, aggregate and subtraction rules to multiply generalization, continuous processing without scrolling steps and 0 and 1 with the multiplication rule to understand the most common misconceptions in questions that require multiplication. Varol and Kubanç (2015) in their study, the second and third grade students started the splitting process by generalizing the right-to-Start Process Rule, which is valid in addition to the addition, subtraction, and multiplication processes, and the splitting process by generalizing the right-to-start process, as in the addition and subtraction process, and generalizing. Erbaş, Çetinkaya and Ersoy (2009) stated that students' mistakes were mostly arithmetic or transactional. In his study of 140 students, Wallece (1984) stated that the most common mistakes were: not dominating basic addition and multiplication events; not understanding digit value and numbering, and confusion about subtraction and renaming. Again, Brown and Burton (1978) addition and subtraction students in the process of the mistakes they made; in total, the columns independent of each other, thinking the application to the properties of the extraction process the collection process, to attach the value of the zero digit, add the digits to the end of the collection process as in the production process, aggregate production process and at the same time as you add digits to the end of the process to the next column to the total ones ignore digits, the numbers in the figure as assessment, to be issued the number from the left alignment, the biggest steps from borrowing, expressed in the form of borrowing from scratch. The results of the study support the results of the earlier study.

Based on all these findings, when the wrong solution methods of the 4th grade students given to the questions in The Achievement Test are examined, it is seen that the students made similar mistakes. All of the mistakes that students made were caused by not understanding the digit concept. Considering these results, the following recommendations can be made on the things that must to be done in teaching environments. Firstly, teachers must examine the methods and techniques that may be used to explain the digit concept more effectively. Then, they must also determine the mistakes and deficiencies of students in this subject by using appropriate measurement tools. Finally, students must be encouraged to use more than one strategy to solve questions.

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