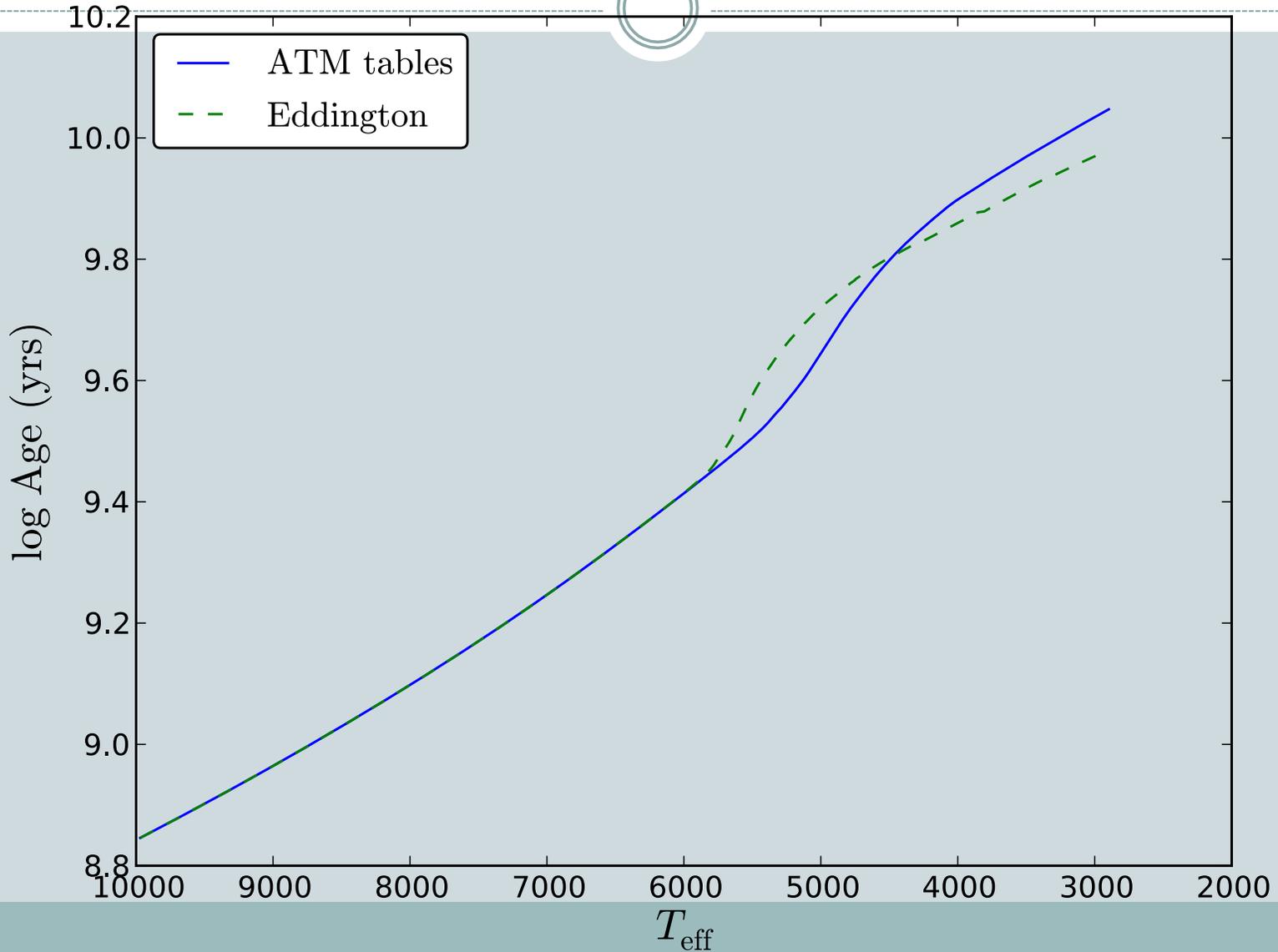
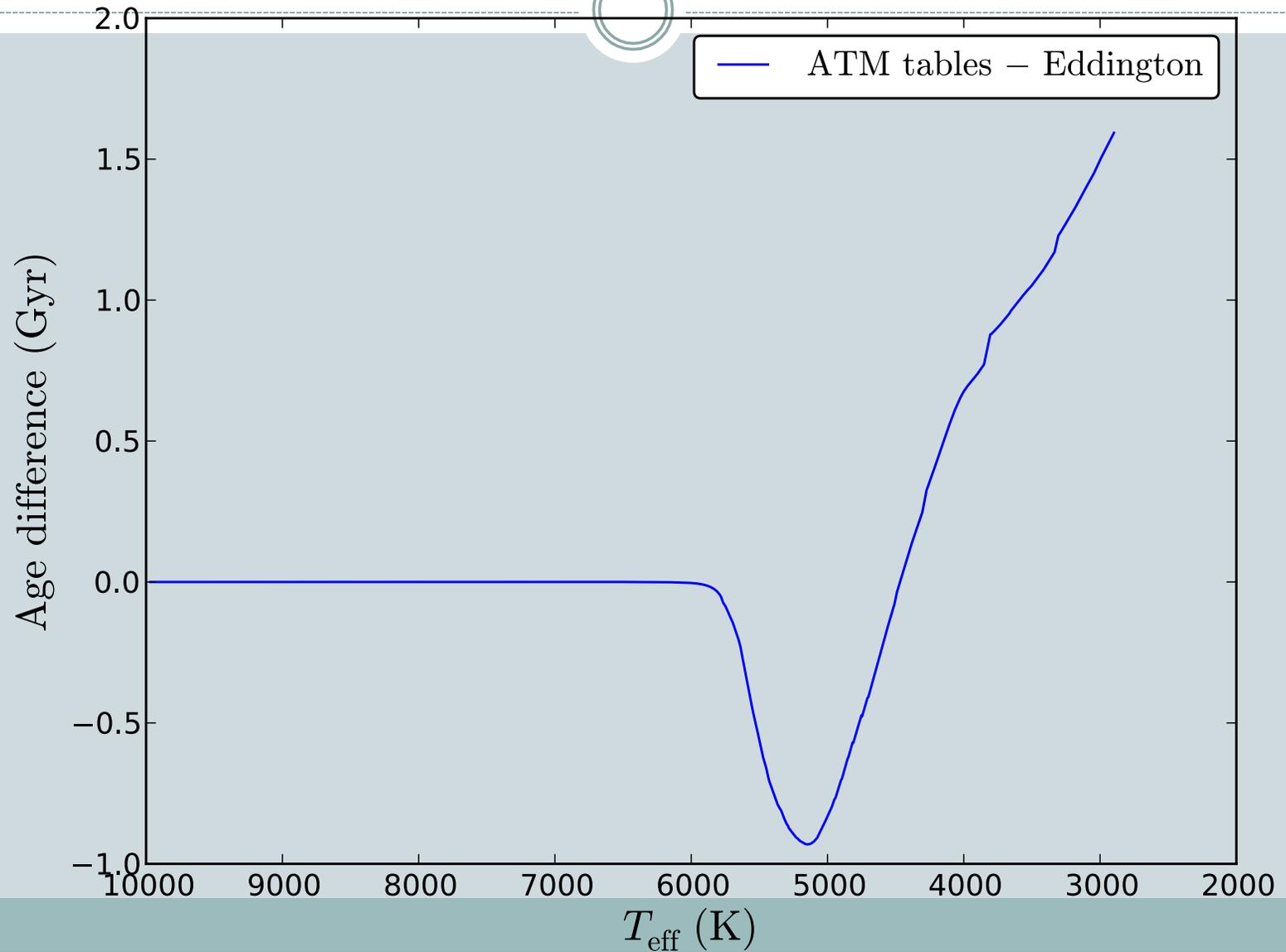


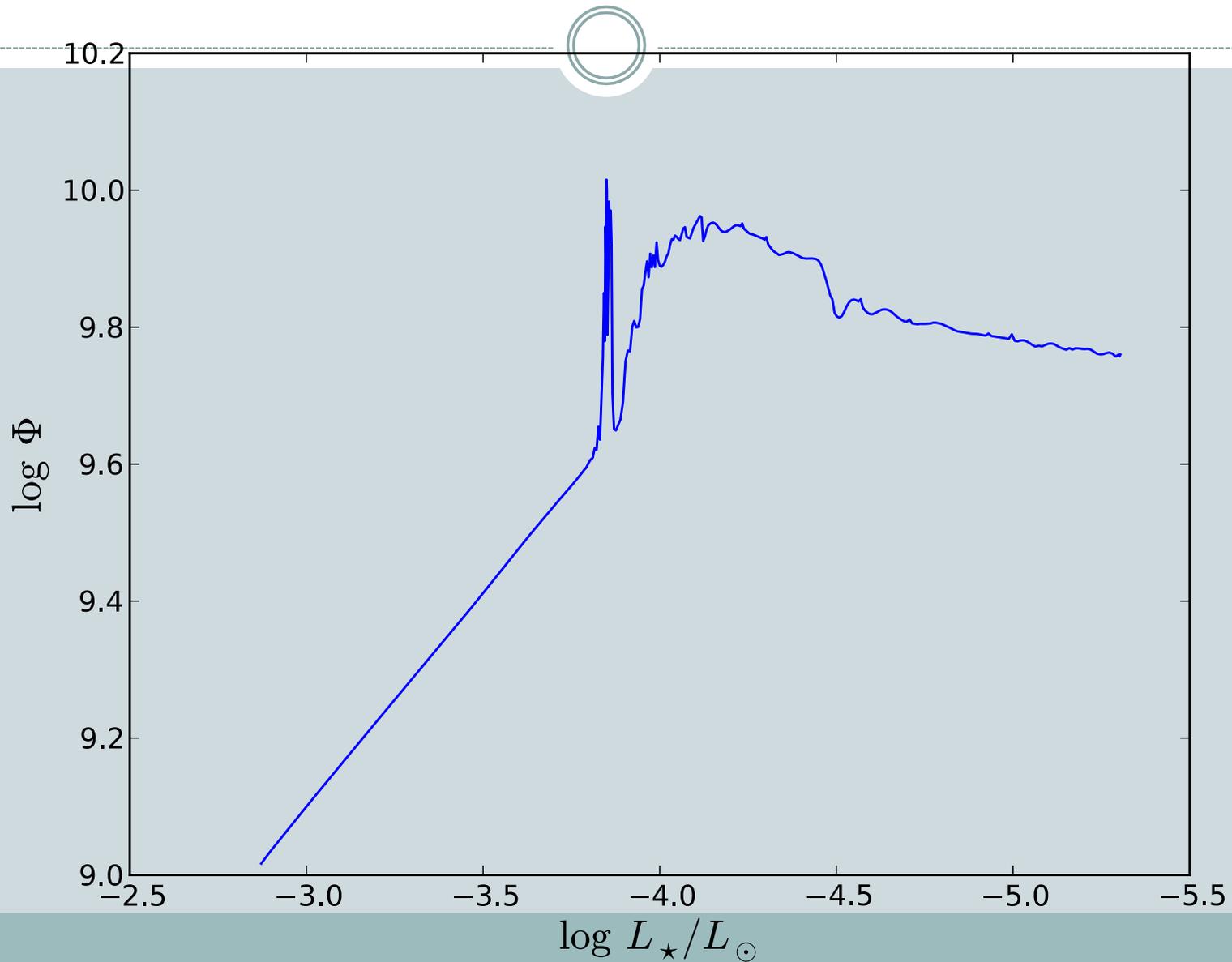
# Review of Long Problem Results



# Review of Long Problem Results



# Review of Long Problem Results



# Review of Long Problem Results



- List of additional models people were able to run:

| Input Model             | Final Teff | Diffusion |
|-------------------------|------------|-----------|
| 0.150_from_1.5_z2m2.mod | 0          | N         |
| 0.200_from_1.5_z2m2.mod | 0          | N         |
| 0.300_from_1.5_z2m2.mod | 0          | N         |
| 0.350_from_1.5_z2m2.mod | 0          | N         |
| 0.400_from_1.5_z2m2.mod | 0          | N         |
| 0.496_from_0.8_z2m2.mod | 0          | N         |
| 0.513_from_0.9_z2m2.mod | 0          | N         |
| 0.522_from_1.0_z2m2.mod | 0          | N         |
| 0.544_from_1.3_z2m2.mod | 0          | N         |
| 0.567_from_2.0_z2m2.mod | 0          | N         |
| 0.604_from_2.3_z2m2.mod | 0          | N         |

# Review of Long Problem Results



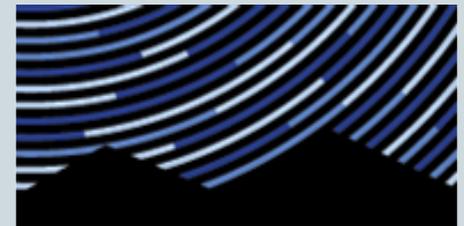
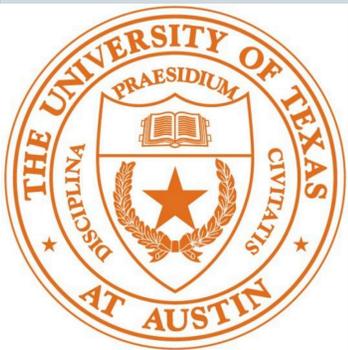
- List of additional models people were able to run:

| Input Model             | Teff | Diffusion |
|-------------------------|------|-----------|
| 0.611_from_2.5_z2m2.mod | 0    | N         |
| 0.639_from_3.0_z2m2.mod | 0    | N         |
| 0.734_from_3.5_z2m2.mod | 0    | N         |
| 0.819_from_4.0_z2m2.mod | 0    | N         |
| 0.856_from_5.0_z2m2.mod | 0    | N         |
| 0.927_from_6.0_z2m2.mod | 0    | N         |
| 1.025_from_7.0_z2m2.mod | 0    | N         |
| 1.259_from_8.0_z2m2.mod | 0    | N         |
| 1.316_from_8.5_z2m2.mod | 0    | N         |
| 1.376_from_8.7_z2m2.mod | 0    | N         |

# The Evolution and Pulsation of White Dwarf Stars II: Extremely Low Mass WD Pulsators



MIKE MONTGOMERY, DON WINGET, **JJ HERMES**,  
ROSS FALCON, SAMUEL HARROLD, KEATON BELL  
AUGUST 17, 2012



McDonald Observatory  
THE UNIVERSITY OF TEXAS AT AUSTIN

# Location of files for talk and problems



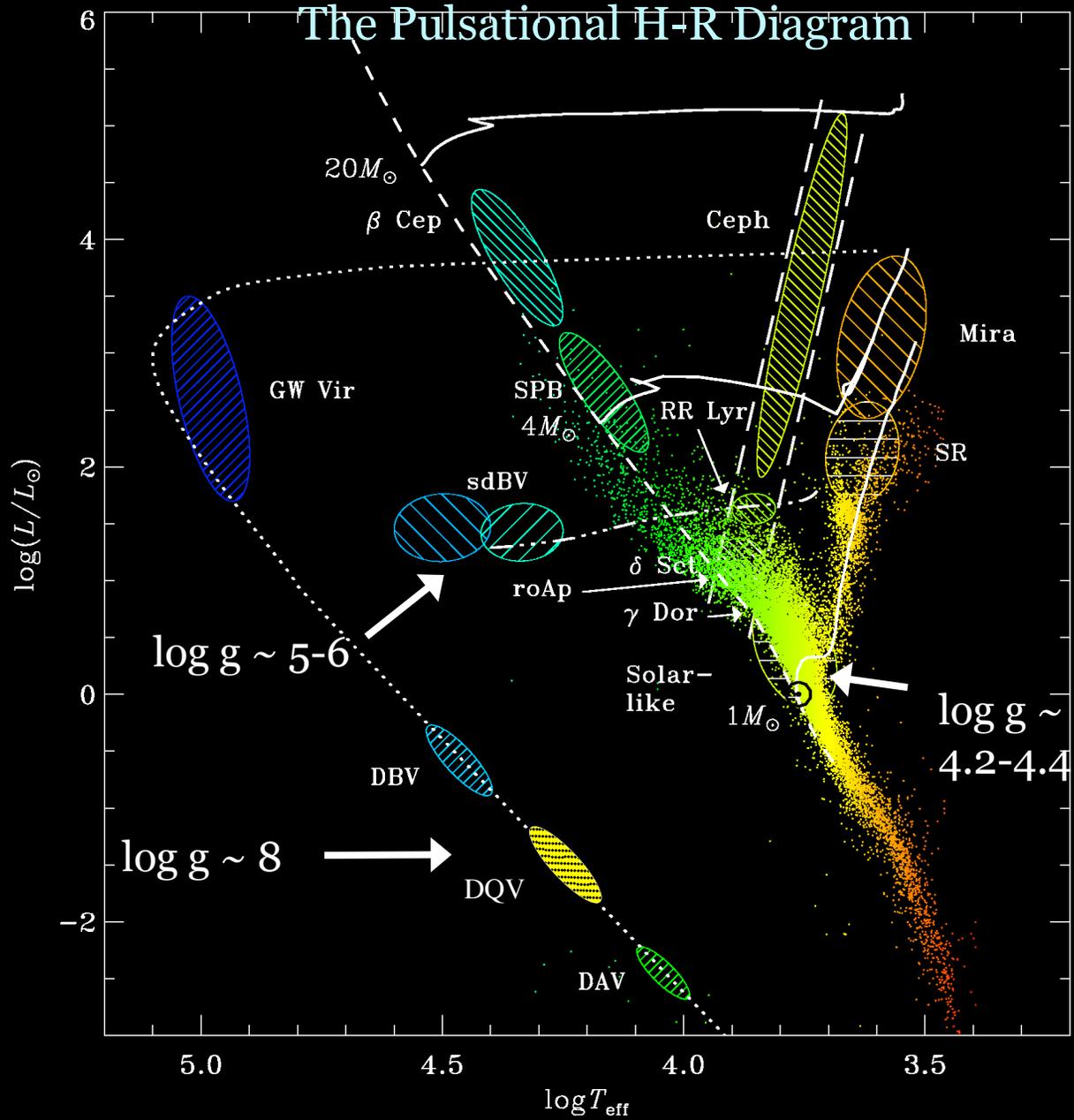
- Download file “wd\_problems2.tar” from mesastar.org -> FAQ -> MESA Summer School 2012 lectures -> Mike Montgomery II

After detarring, you’ll find the lecture in [Montgomery\\_lecture2.pdf](#) and the instructions for the long and short problems in [mesa\\_rapid\\_problem2.pdf](#) and [mesa\\_long2.pdf](#). You will also need the files you saved from the rapid problem.

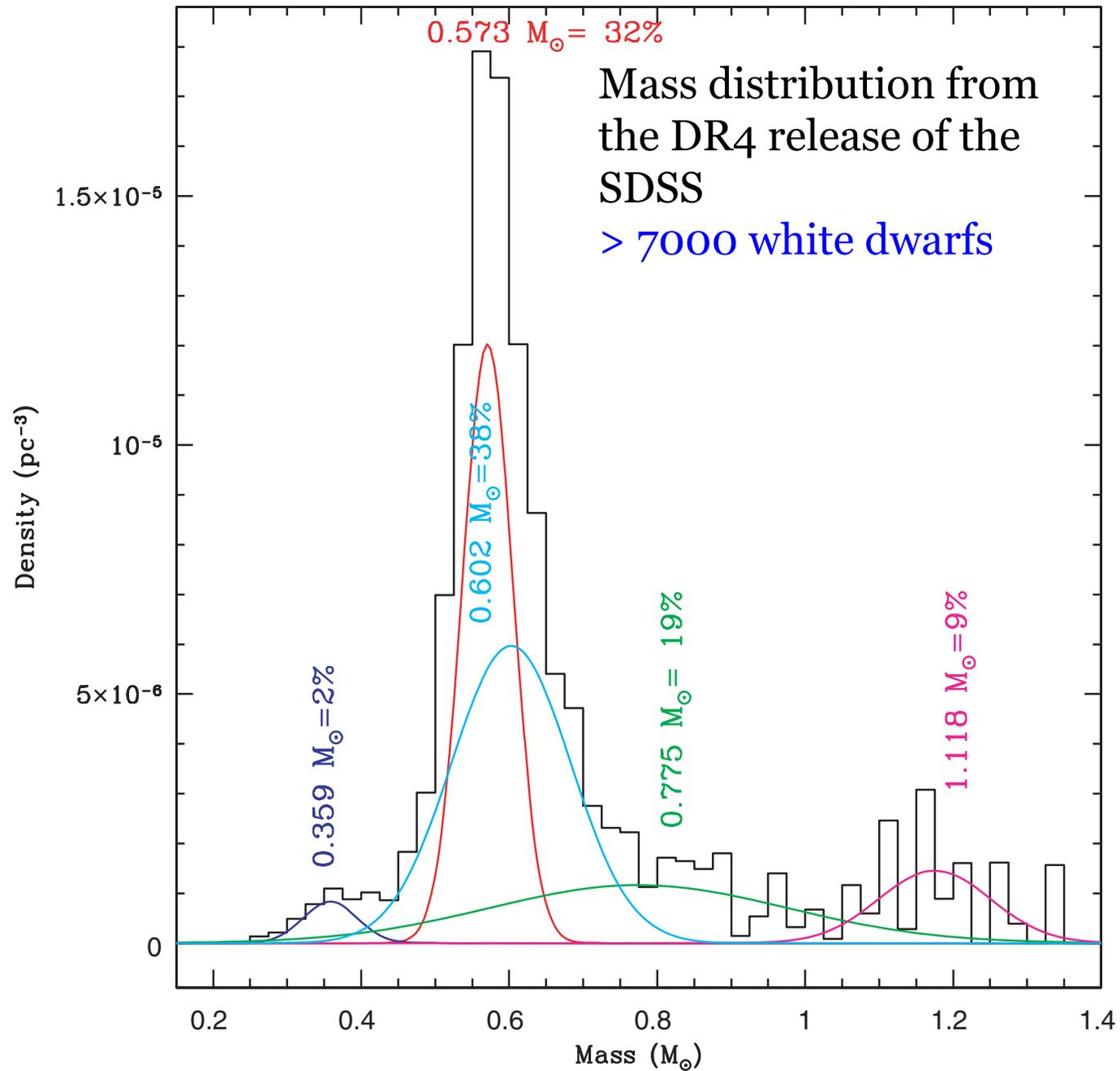
Full web address:

[http://mesastar.org/documentation/mesa-summer-school-2012-lectures/mike-montgomery-ii/wd\\_problems2.tar/view](http://mesastar.org/documentation/mesa-summer-school-2012-lectures/mike-montgomery-ii/wd_problems2.tar/view)

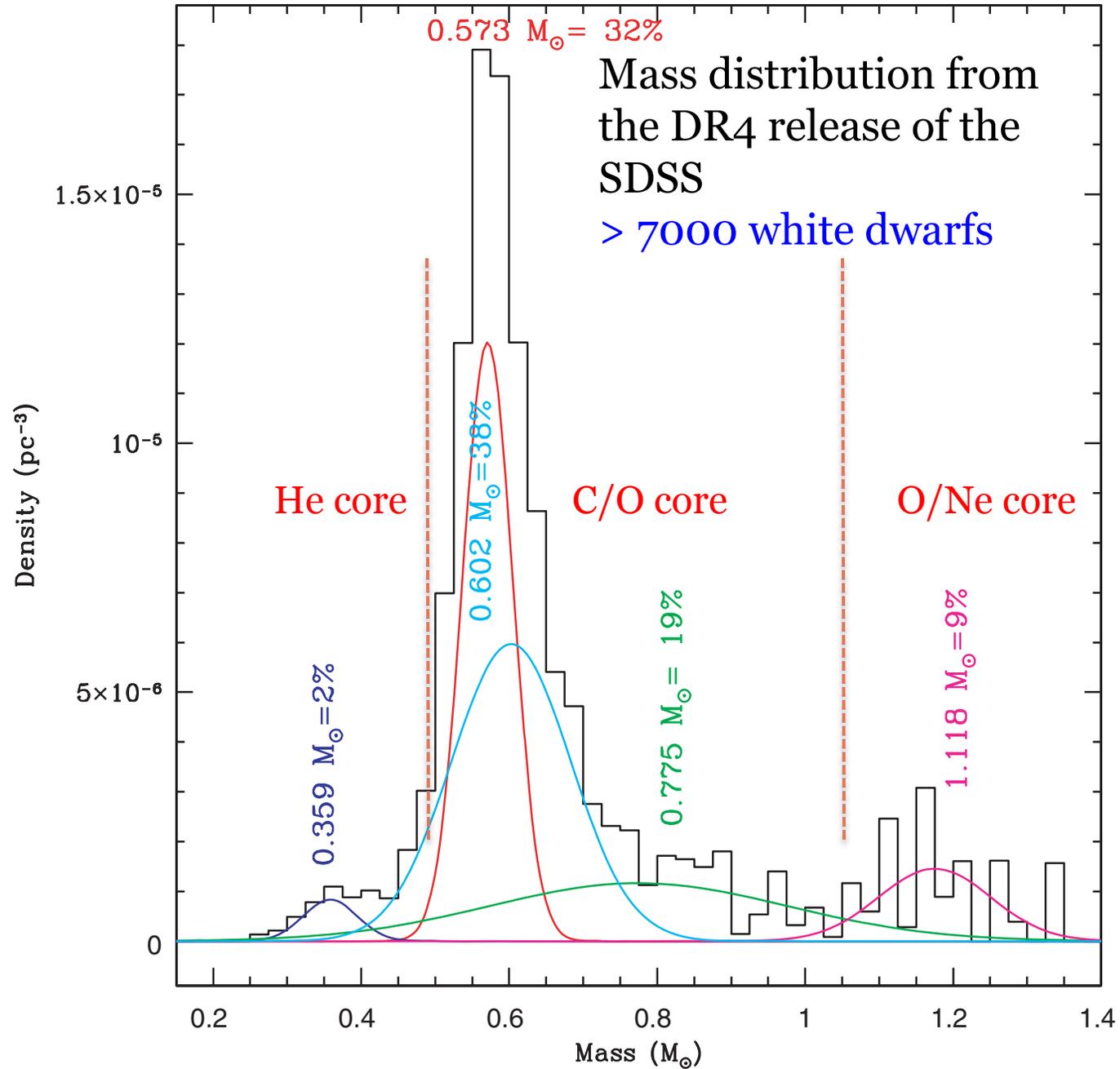
# The Pulsational H-R Diagram



SDSS DR4 DAs  $g < 19$   $T_{\text{eff}} > 12000\text{K}$



SDSS DR4 DAs  $g < 19$   $T_{\text{eff}} > 12000\text{K}$



This motivated Steinfadt et al. (2010) to examine pulsations in these objects to test whether they have He cores...



## PULSATIONS IN HYDROGEN BURNING LOW-MASS HELIUM WHITE DWARFS

JUSTIN D. R. STEINFADT<sup>1</sup>, LARS BILDSTEN<sup>2</sup>, AND PHIL ARRAS<sup>3</sup>

<sup>1</sup> Department of Physics, Broida Hall, University of California, Santa Barbara, CA 93106, USA; [jdrs@physics.ucsb.edu](mailto:jdrs@physics.ucsb.edu)  
<sup>2</sup> Institute for Theoretical Physics and Department of Physics, Kohn Hall, University of California, Santa Barbara, CA 93106, USA; [bildsten@kitp.u](mailto:bildsten@kitp.u)

<sup>3</sup> Department of Astronomy, University of Virginia, P.O. Box 400325, Charlottesville, VA 22904, USA; [arras@virginia.edu](mailto:arras@virginia.edu)

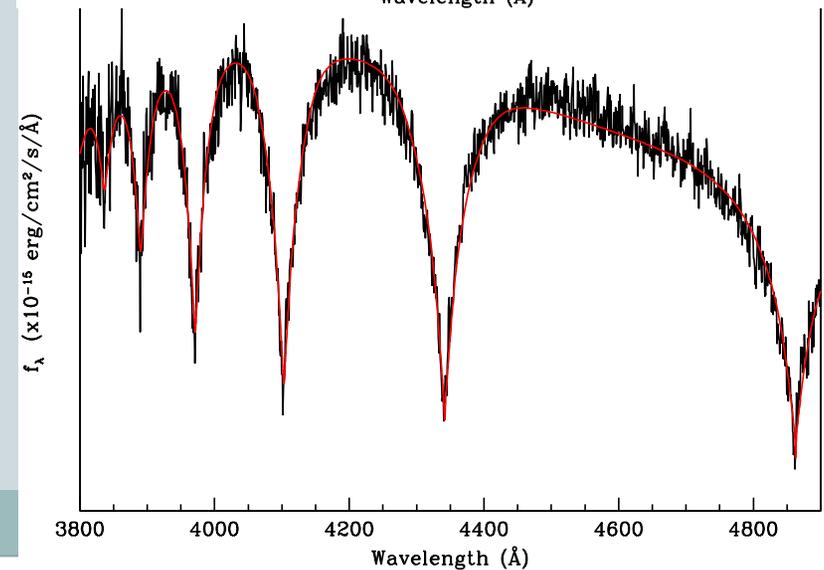
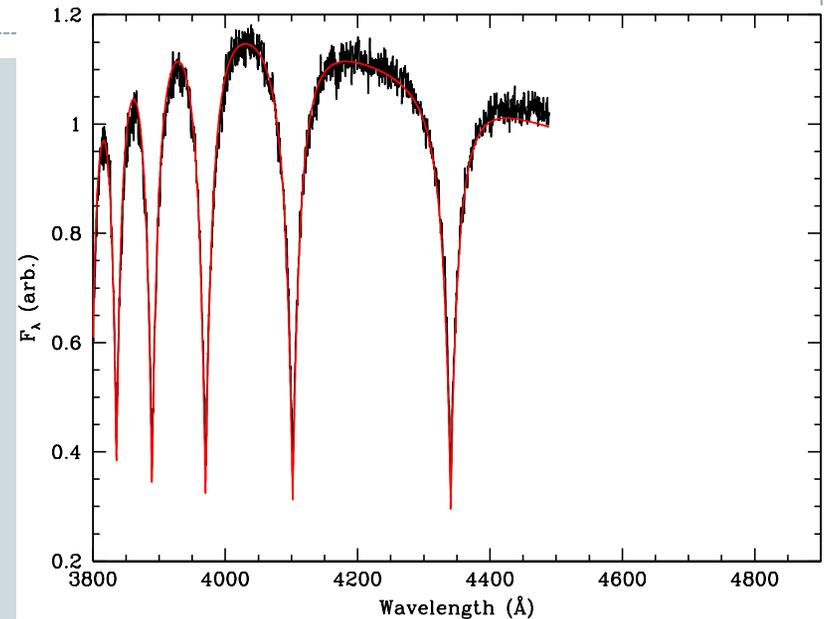
*Received 2009 December 2; accepted 2010 May 28; published 2010 June 30*

### ABSTRACT

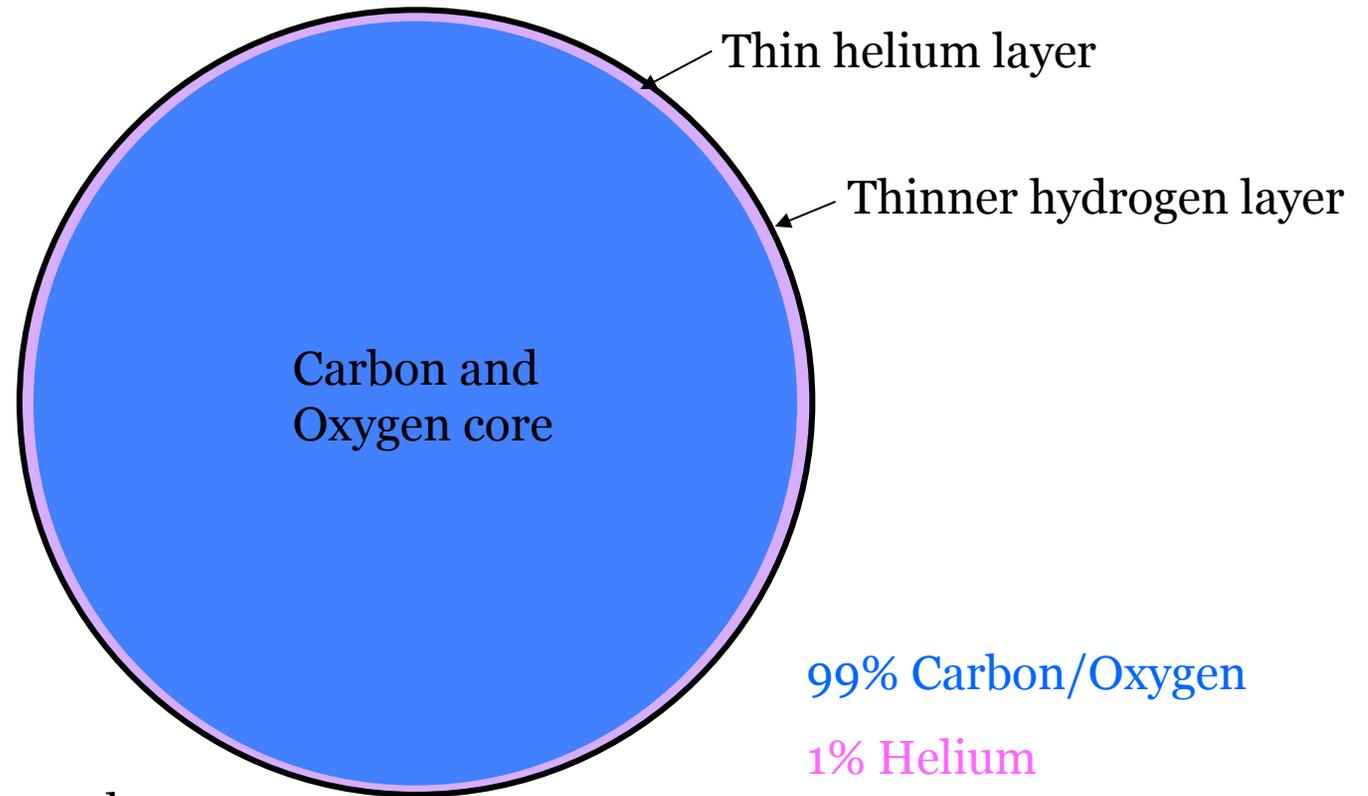
Helium core white dwarfs (WDs) with mass  $M \lesssim 0.20 M_{\odot}$  undergo several Gyr of stable hydrogen burning as they evolve. We show that in a certain range of WD and hydrogen envelope masses, these WDs may exhibit  $g$ -mode pulsations similar to their passively cooling, more massive carbon/oxygen core counterparts, the ZZ Cetus. Our models with stably burning hydrogen envelopes on helium cores yield  $g$ -mode periods and period spacings longer than the canonical ZZ Cetus by nearly a factor of 2. We show that core composition and structure can be probed using seismology since the  $g$ -mode eigenfunctions predominantly reside in the helium core. Though we have not carried out a fully nonadiabatic stability analysis, the scaling of the thermal time in the convective zone with surface gravity highlights several low-mass helium WDs that should be observed in search of pulsations: NLTT 11748, SDSS J0822+2753, and the companion to PSR J1012+5307. Seismological studies of these He core WDs may prove especially fruitful, as their luminosity is related (via stable hydrogen burning) to the hydrogen envelope mass, which eliminates one model parameter.

# What we (think) we know about Extremely Low-Mass (ELM) WDs...

- $M < 0.25 M_{\odot}$
- He-core
  - Stripped of material before much He fusion to C/O can occur
- Identified spectroscopically (hydrogen-atmosphere WDs with narrower lines)
- Must form in binaries
  - Single-star evolution would take too long to form a  $0.2 M_{\odot}$  WD
  - So far, 18 of 18 WDs with masses  $< 0.25 M_{\odot}$  have detected RV companions (Kilic et al. 2011, ApJ 727 3)



# “Normal” White Dwarfs...



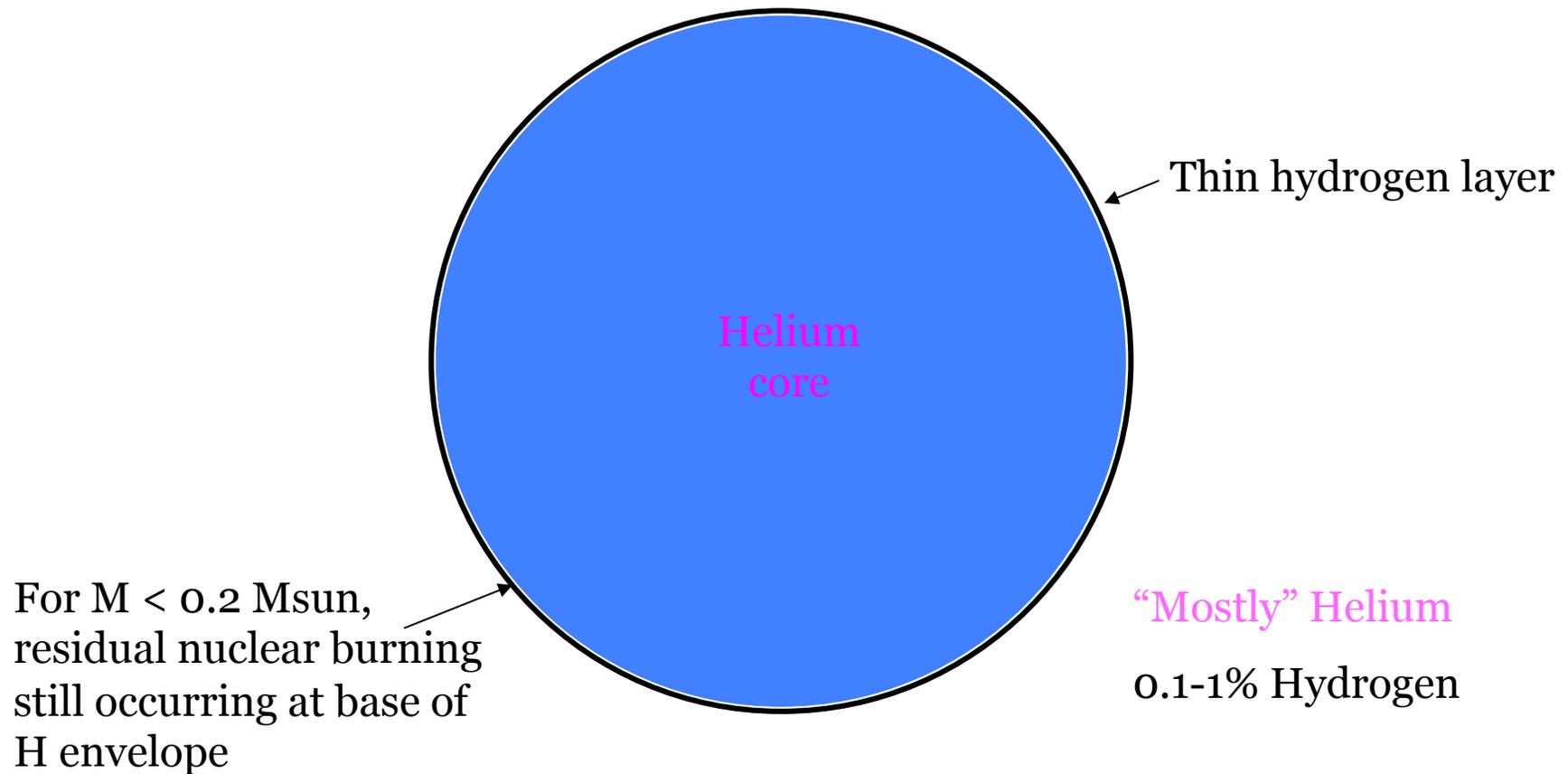
99% Carbon/Oxygen

1% Helium

0.01% Hydrogen

DA= hydrogen atmosphere  
DB= helium atmosphere

# Extremely Low Mass White Dwarfs



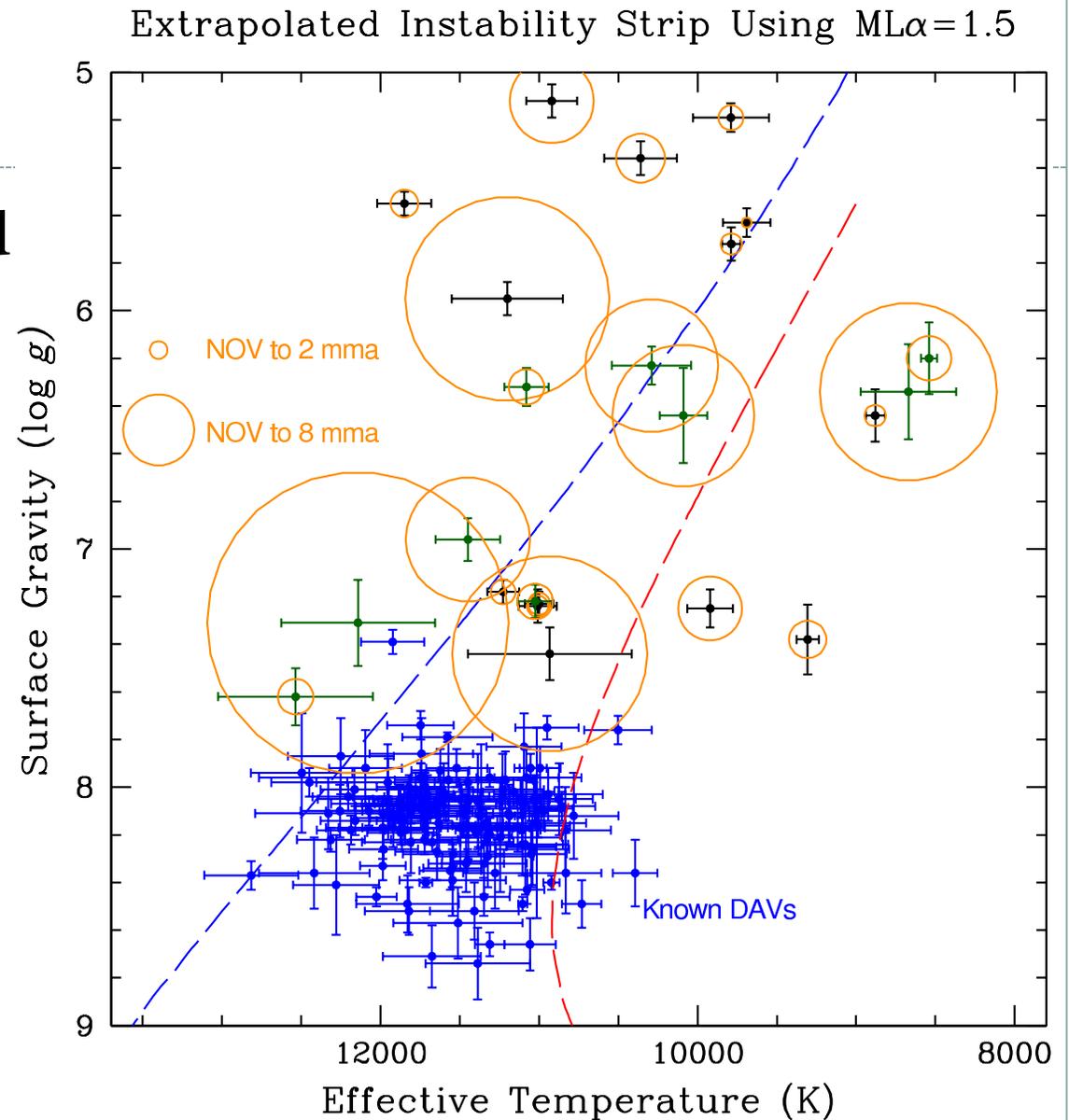
(Panei et al. 2007 , Steinfadt et al. 2010)

# The SDSS

It's good to be faint and  
**blue!**

In the last 9 years the  
number of known  
pulsators has gone  
from  $\sim 35$  to  $\sim 160$

(e.g., Mukadam et al. 2004,  
ApJ, 607, 982; Gianninas,  
Bergeron, & Fontaine 2006,  
AJ, 132, 831; Castanheira et  
al. 2006, A&A, 450, 227;  
Mullally et al. 2005, ApJ, 625,  
966; Nitta et al. 2009, ApJ,  
690, 560)



# THE FIRST PULSATING EXTREMELY LOW MASS WHITE DWARF : SDSS J184037.78+642312.3



## SDSS J184037.78+642312.3: THE FIRST PULSATING EXTREMELY LOW MASS WHITE DWARF

J. J. HERMES<sup>1,2</sup>, M. H. MONTGOMERY<sup>1,2</sup>, D. E. WINGET<sup>1,2</sup>, WARREN R. BROWN<sup>3</sup>, MUKREMIN KILIC<sup>4</sup>, AND SCOTT J. KENYON<sup>3</sup>

<sup>1</sup> Department of Astronomy, University of Texas at Austin, Austin, TX 78712, USA; [jjhermes@astro.as.utexas.edu](mailto:jjhermes@astro.as.utexas.edu)

<sup>2</sup> McDonald Observatory, Fort Davis, TX 79734, USA

<sup>3</sup> Smithsonian Astrophysical Observatory, 60 Garden St, Cambridge, MA 02138, USA

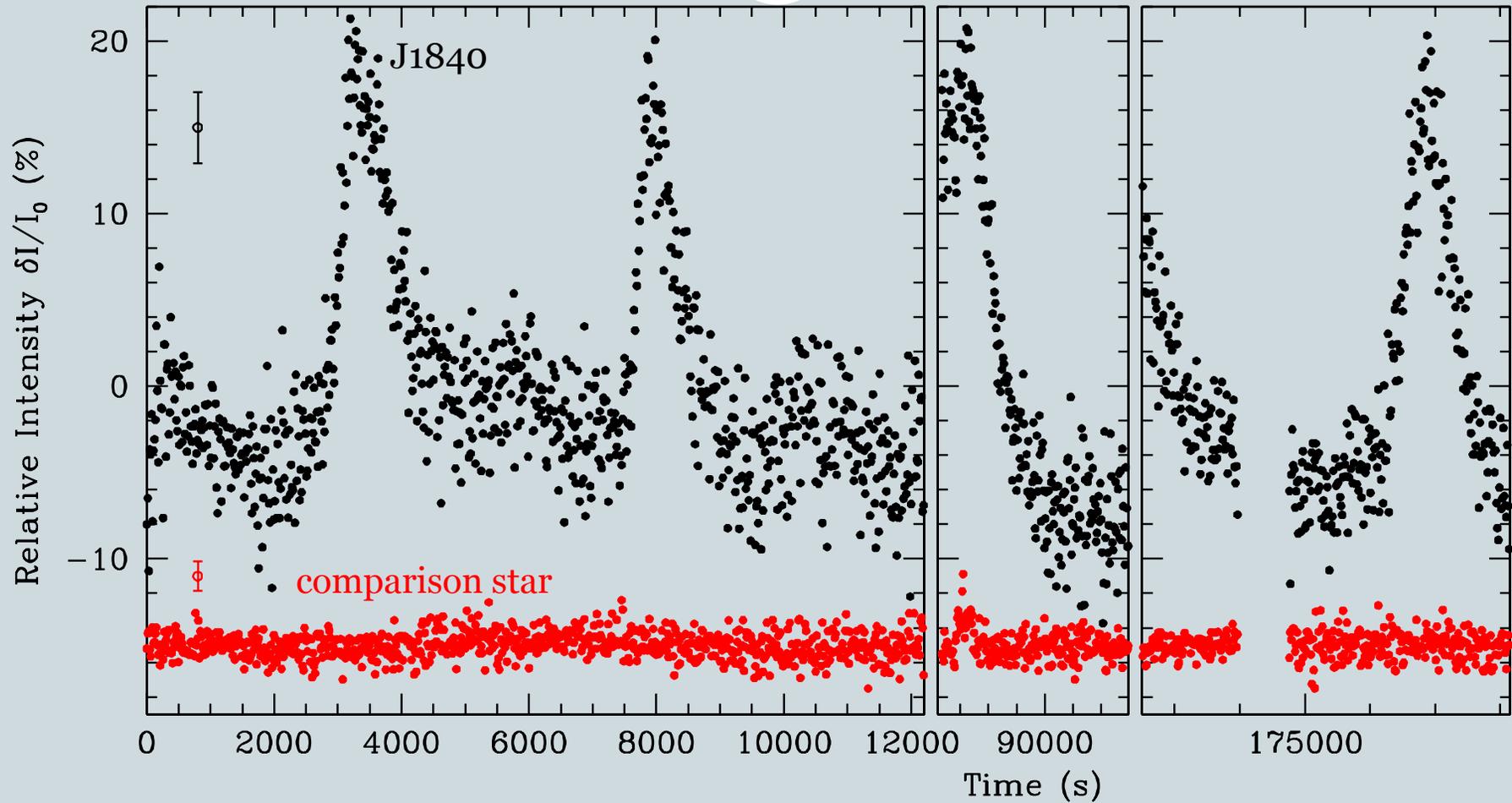
<sup>4</sup> Homer L. Dodge Department of Physics and Astronomy, University of Oklahoma, 440 W. Brooks St., Norman, OK 73019, USA

*Received 2012 March 26; accepted 2012 April 5; published 2012 April 17*

### ABSTRACT

We report the discovery of the first pulsating extremely low mass (ELM) white dwarf (WD), SDSS J184037.78+642312.3 (hereafter J1840). This DA (hydrogen-atmosphere) WD is by far the coolest and the lowest-mass pulsating WD, with  $T_{\text{eff}} = 9100 \pm 170$  K and  $\log g = 6.22 \pm 0.06$ , which corresponds to a mass of  $\sim 0.17 M_{\odot}$ . This low-mass pulsating WD greatly extends the DAV (or ZZ Ceti) instability strip, effectively bridging the  $\log g$  gap between WDs and main-sequence stars. We detect high-amplitude variability in J1840 on timescales exceeding 4000 s, with a non-sinusoidal pulse shape. Our observations also suggest that the variability is multi-periodic. The star is in a 4.6 hr binary with another compact object, most likely another WD. Future, more extensive time-series photometry of this ELM WD offers the first opportunity to probe the interior of a low-mass, presumably He-core WD using the tools of asteroseismology.

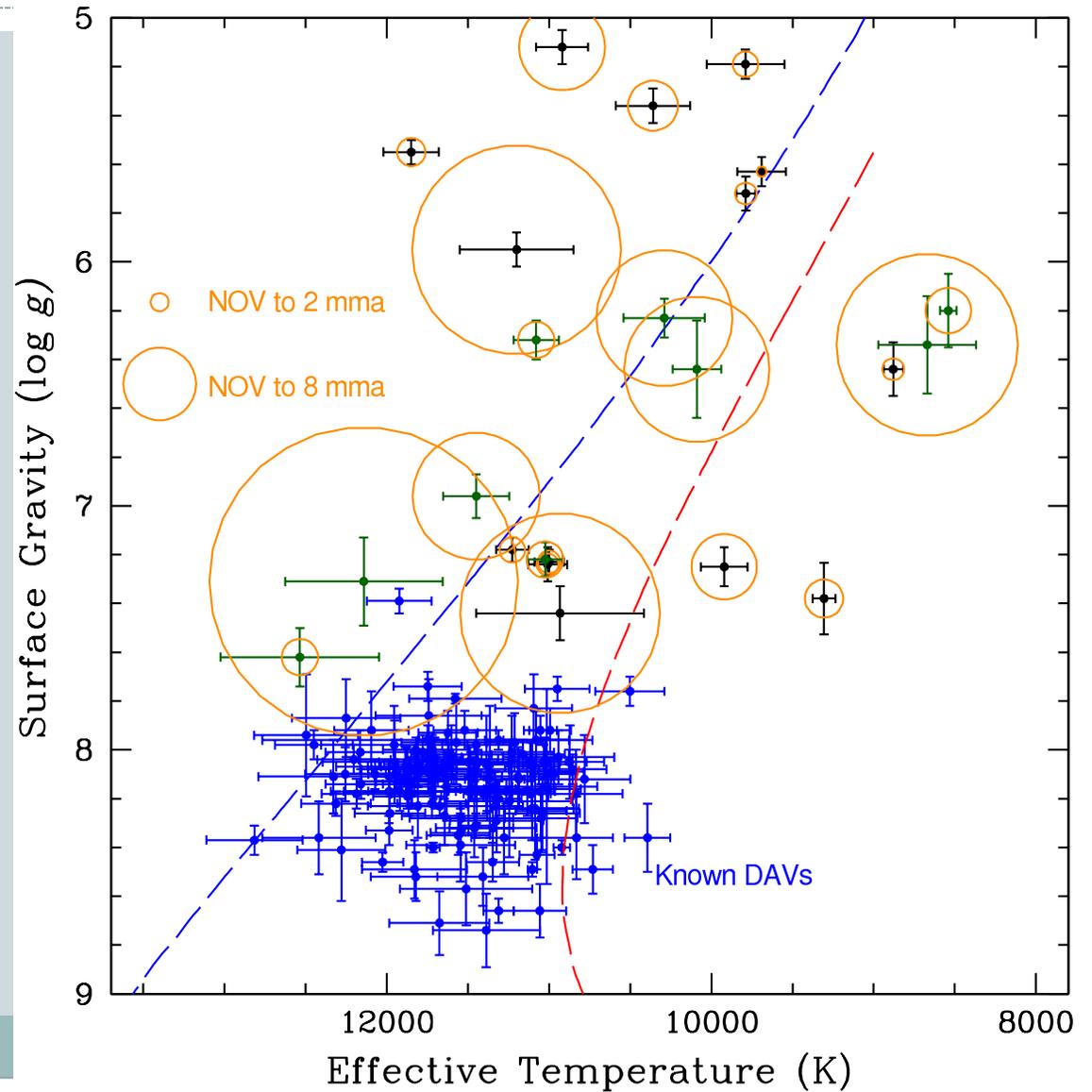
# THE FIRST PULSATING EXTREMELY LOW MASS WHITE DWARF : SDSS J184037.78+642312.3



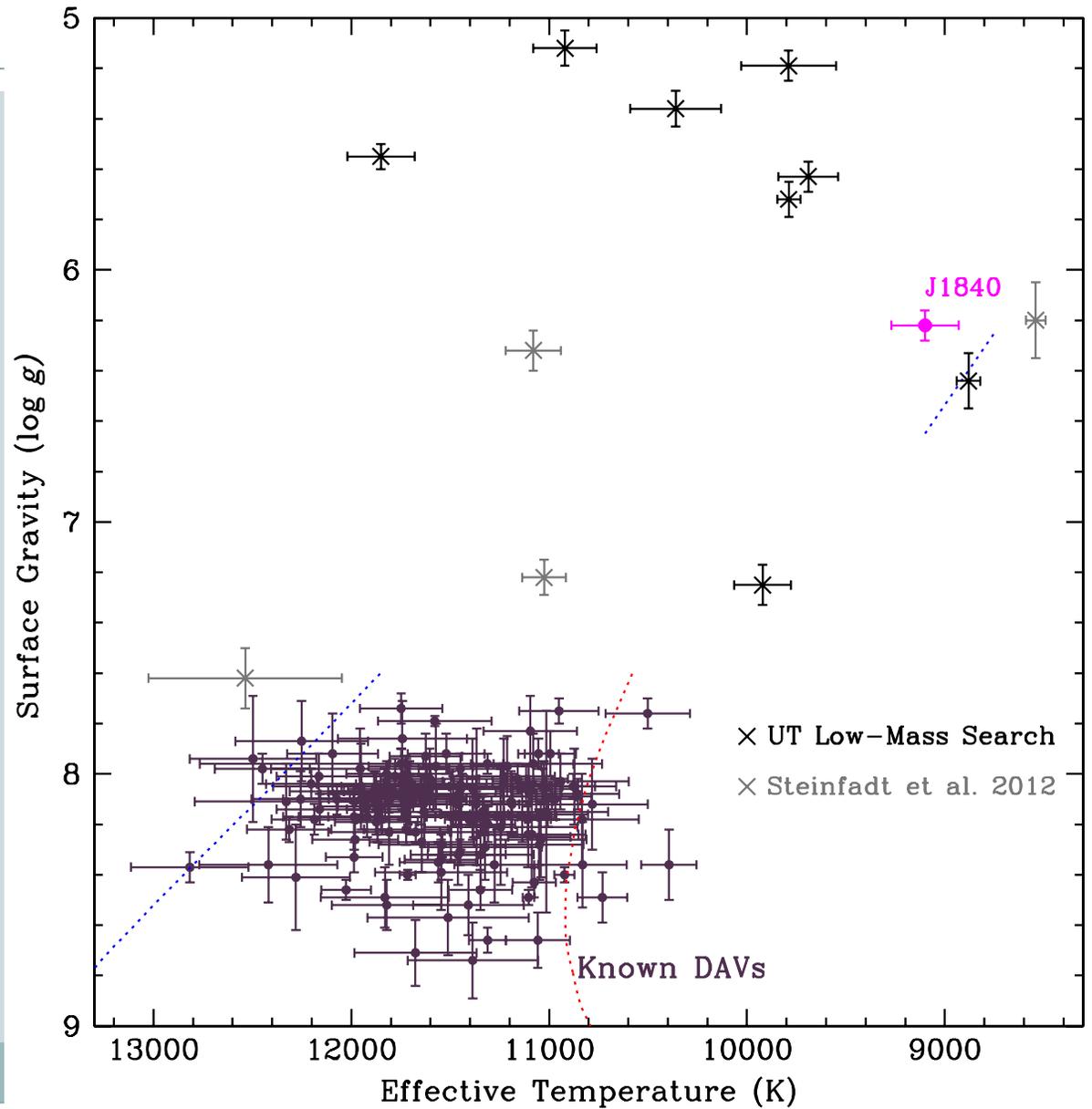
Hermes et al. (2012)

# The search for pulsating ELM WDs

Extrapolated Instability Strip Using  $M\alpha=1.5$

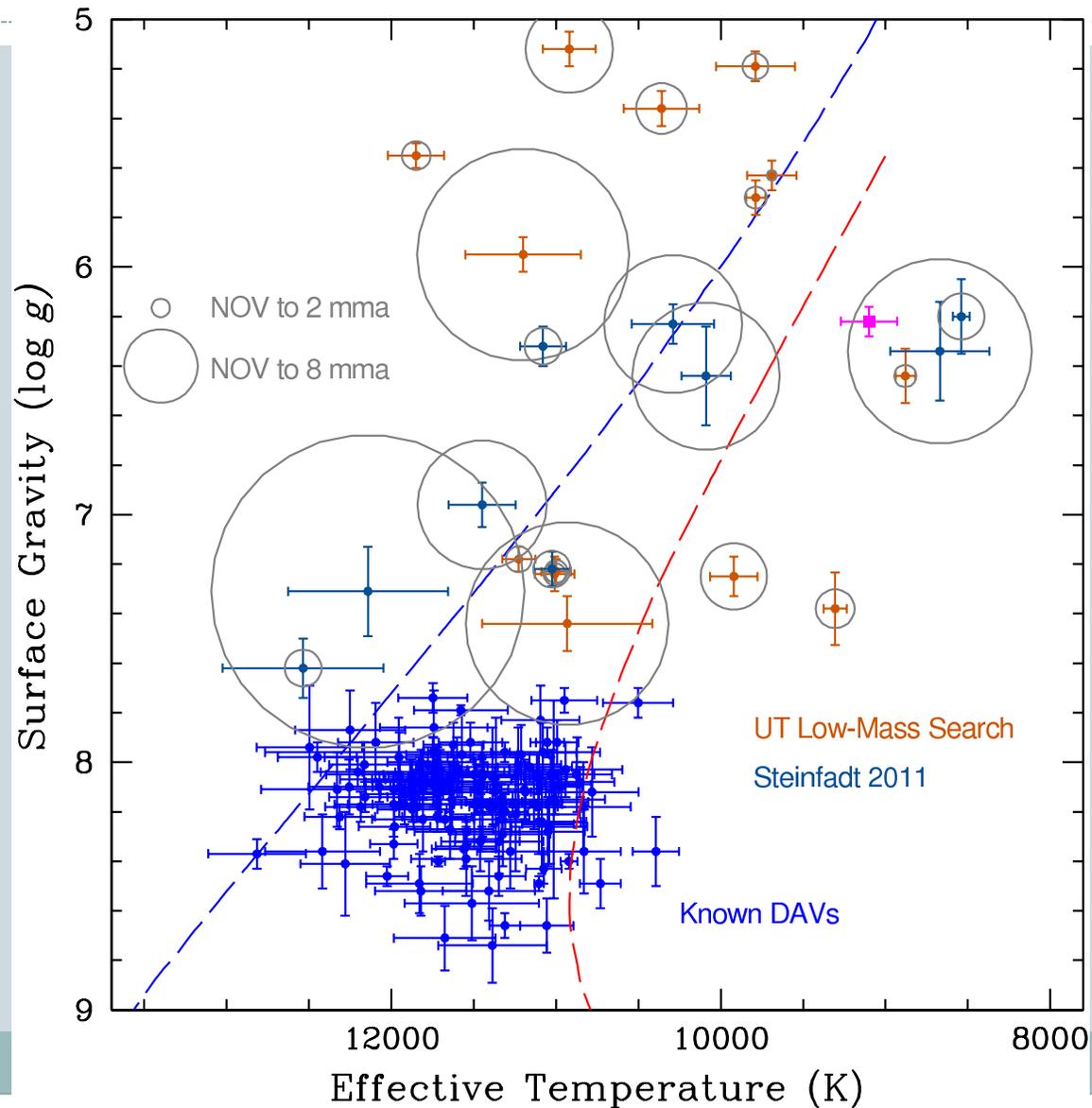


# The search for pulsating ELM WDs



# Its location in the $\log g$ - $T_{\text{eff}}$ plane

Extrapolated Instability Strip Using  $M L \alpha = 1.5$



# MESA Rapid Problem #2



- Download file “wd\_problems2.tar” from mesastar.org -> FAQ ->

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# What to know about WD pulsations



- White dwarfs have been observed to pulsate in non-radial g-modes
  - g-modes are asymptotically evenly spaced in period, not frequency

$$P_n = n \langle \Delta P \rangle_\ell + \epsilon, \quad n = 1, 2, 3 \dots$$

$$\langle \Delta P \rangle_\ell \sim \frac{2\pi^2}{\sqrt{\ell(\ell+1)}} \left( \int_{r_1}^{r_2} dr N/r \right)^{-1}$$

# DBV and DAV driving

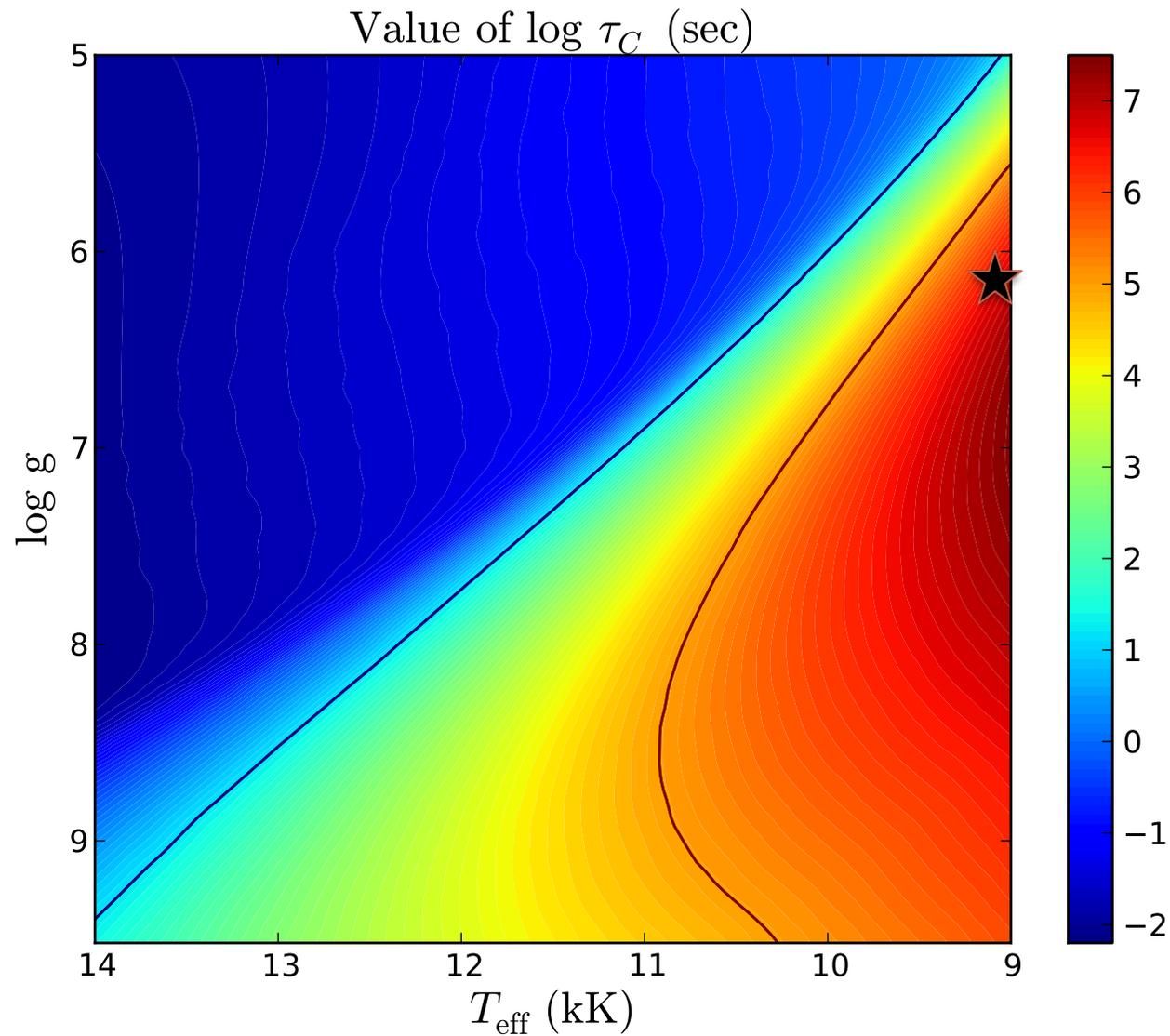


Due to convective driving – the “Brickhill effect”  
(Brickhill 1992, Wu & Goldreich)

- convection zone is associated with the partial ionization of either H or He
- predictions of instability are similar to those of  $\kappa$  mechanism driving in white dwarfs:

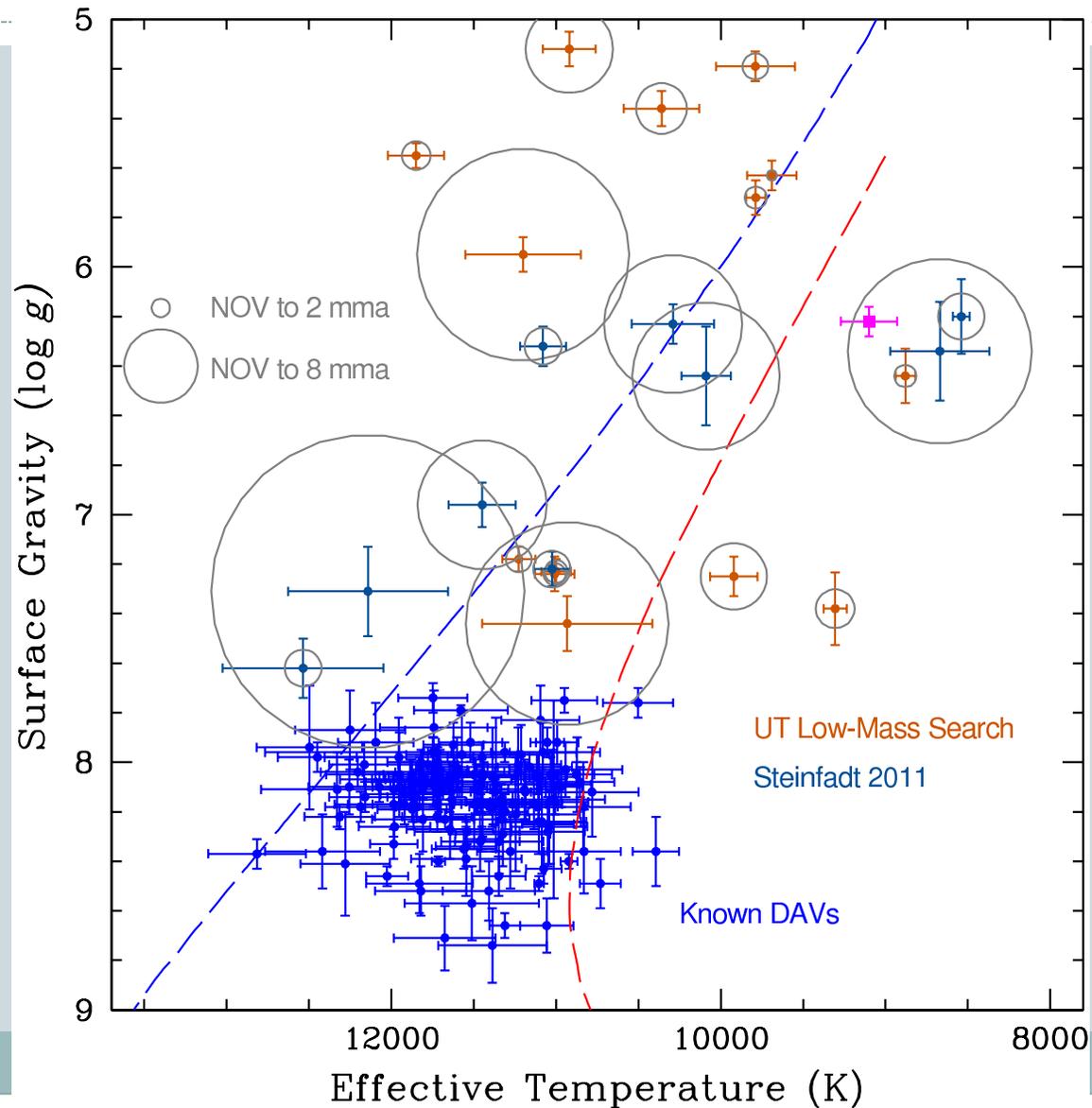
“Blue” (hot ) edge occurs when the  $n=1, l=1$  mode satisfies  $\omega\tau_C \approx 1$ , where  $\tau_C \approx 4 \tau_{\text{thermal}}$  at the base of the convection zone (Wu & Goldreich, late 1990’s)

# Extension of ZZ instability strip to lower $\log g$ 's

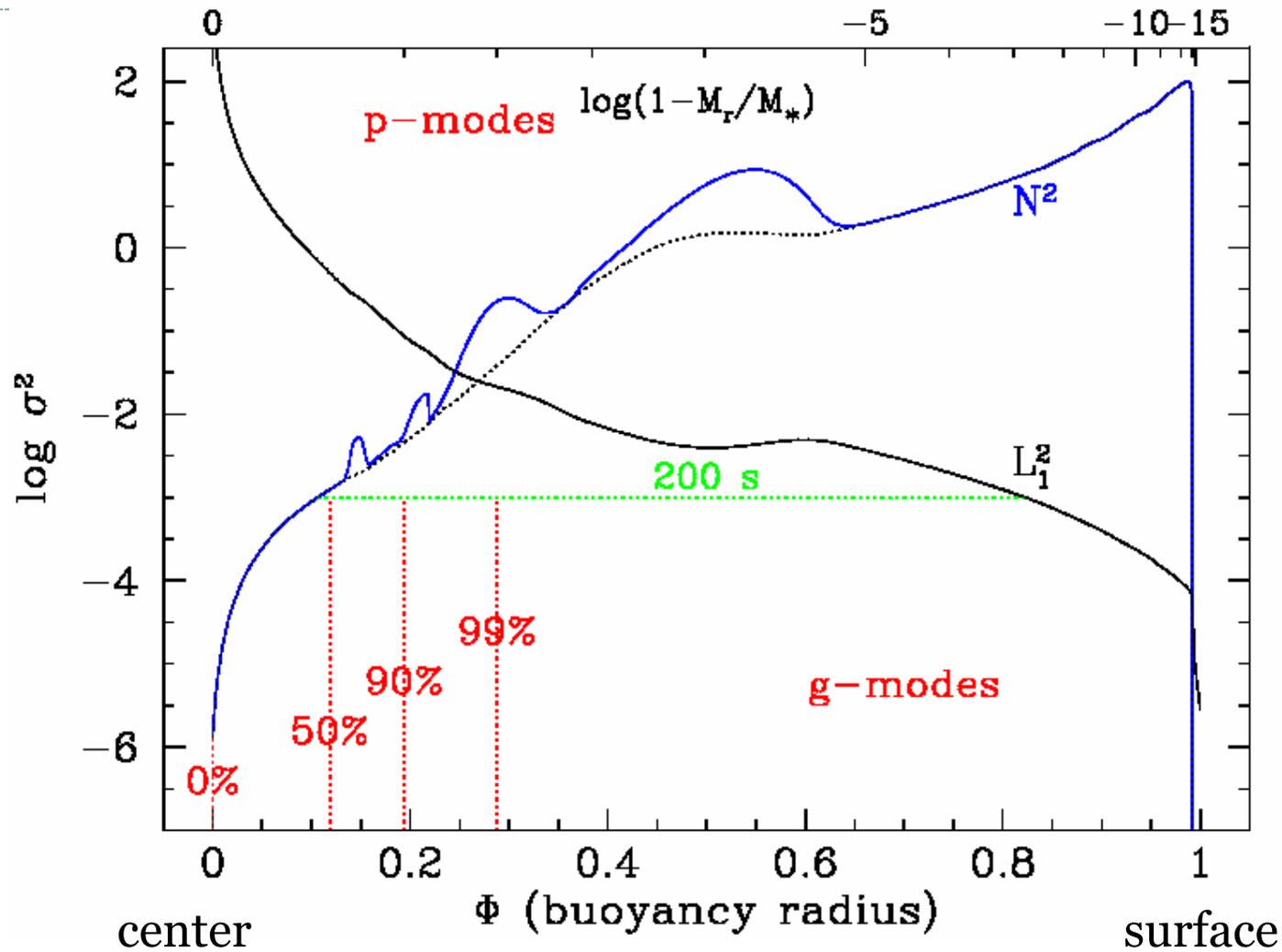


# Its location in the $\log g$ - $T_{\text{eff}}$ plane

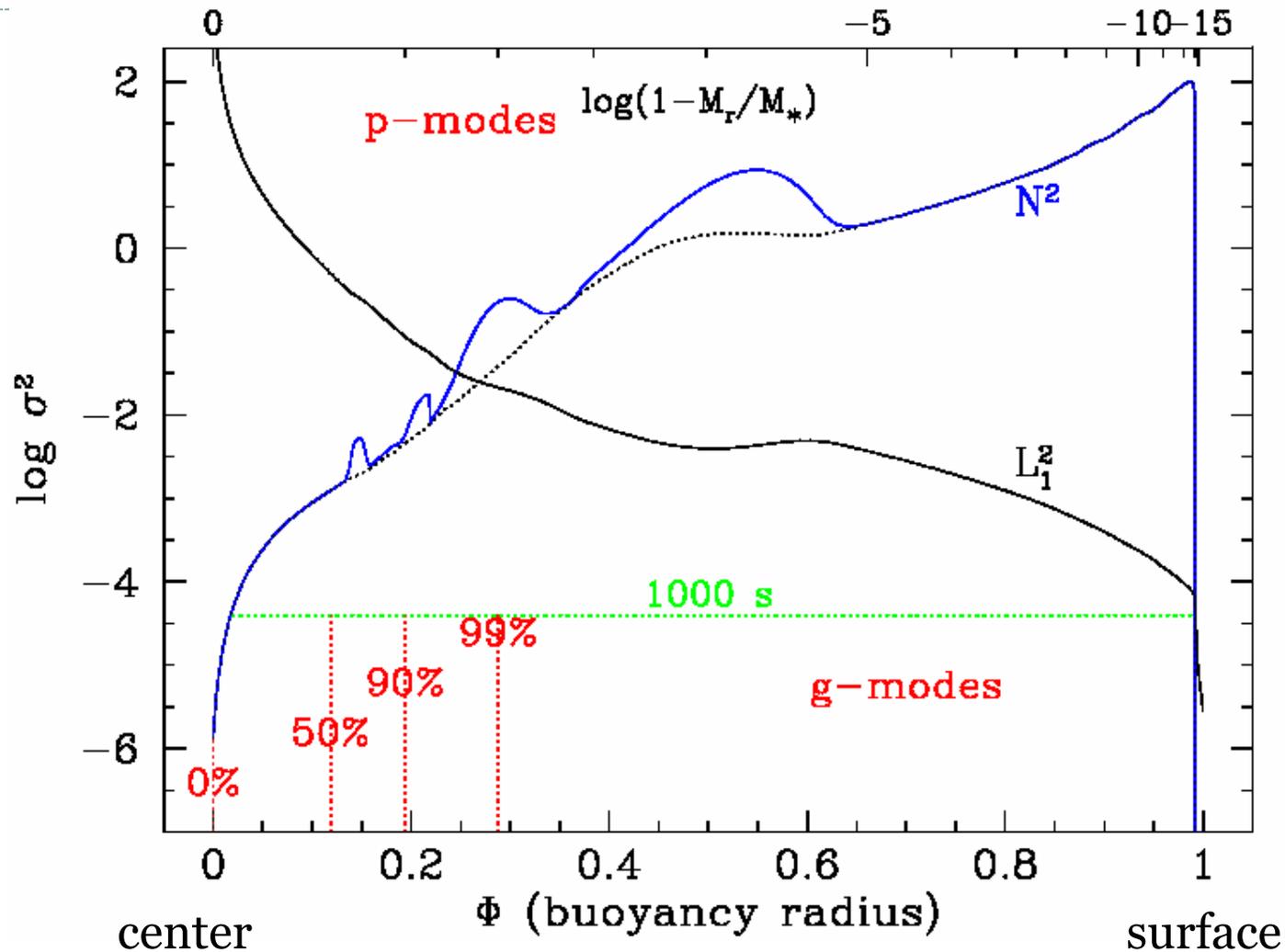
Extrapolated Instability Strip Using  $M L \alpha = 1.5$



# White Dwarf Seismology: a propagation diagram



# White Dwarf Seismology: a propagation diagram



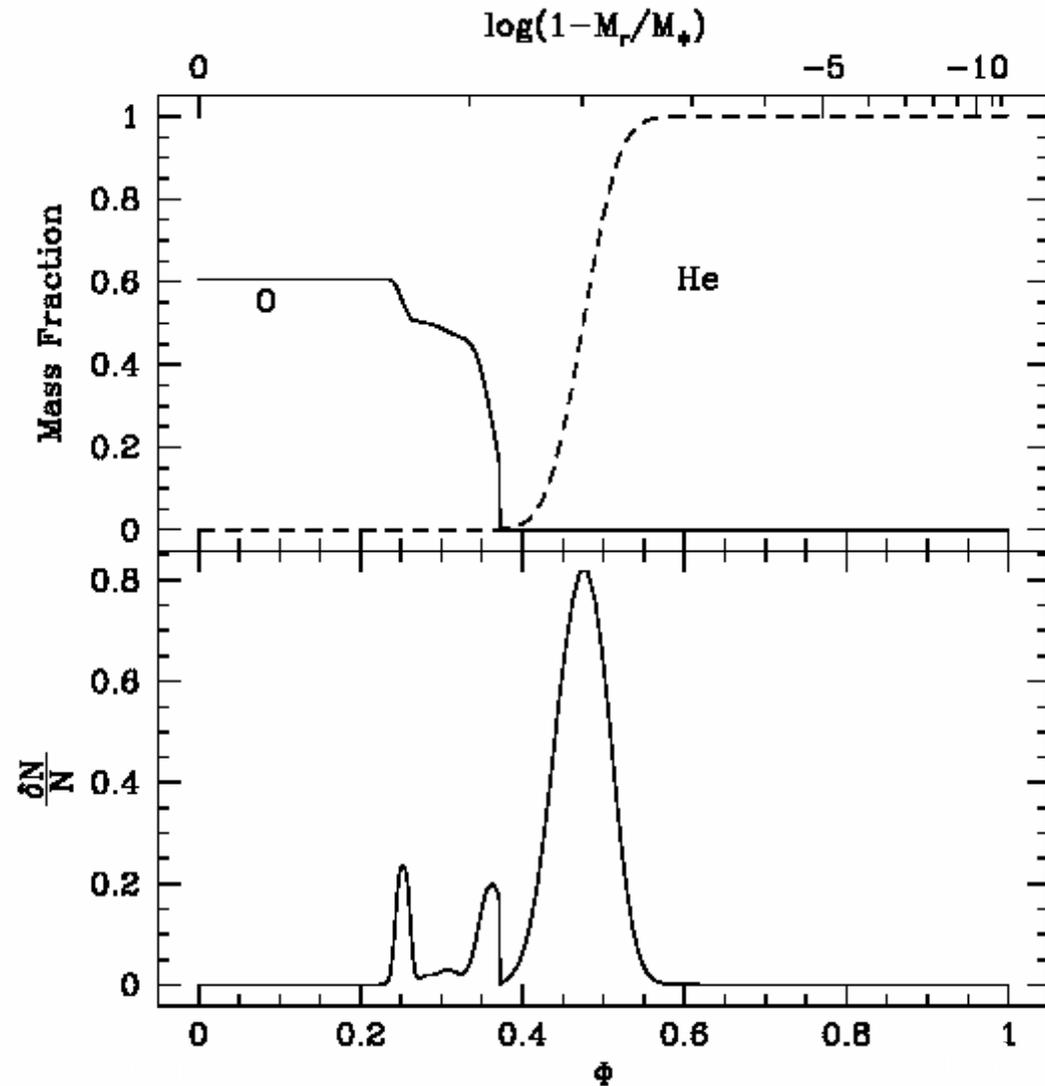
# Chemical Profiles produce bumps in $N$

The composition transition zones produce bumps in  $N$

DBV model

$M = 0.6 M_{\odot}$

$T_{\text{eff}} = 25000 \text{ K}$



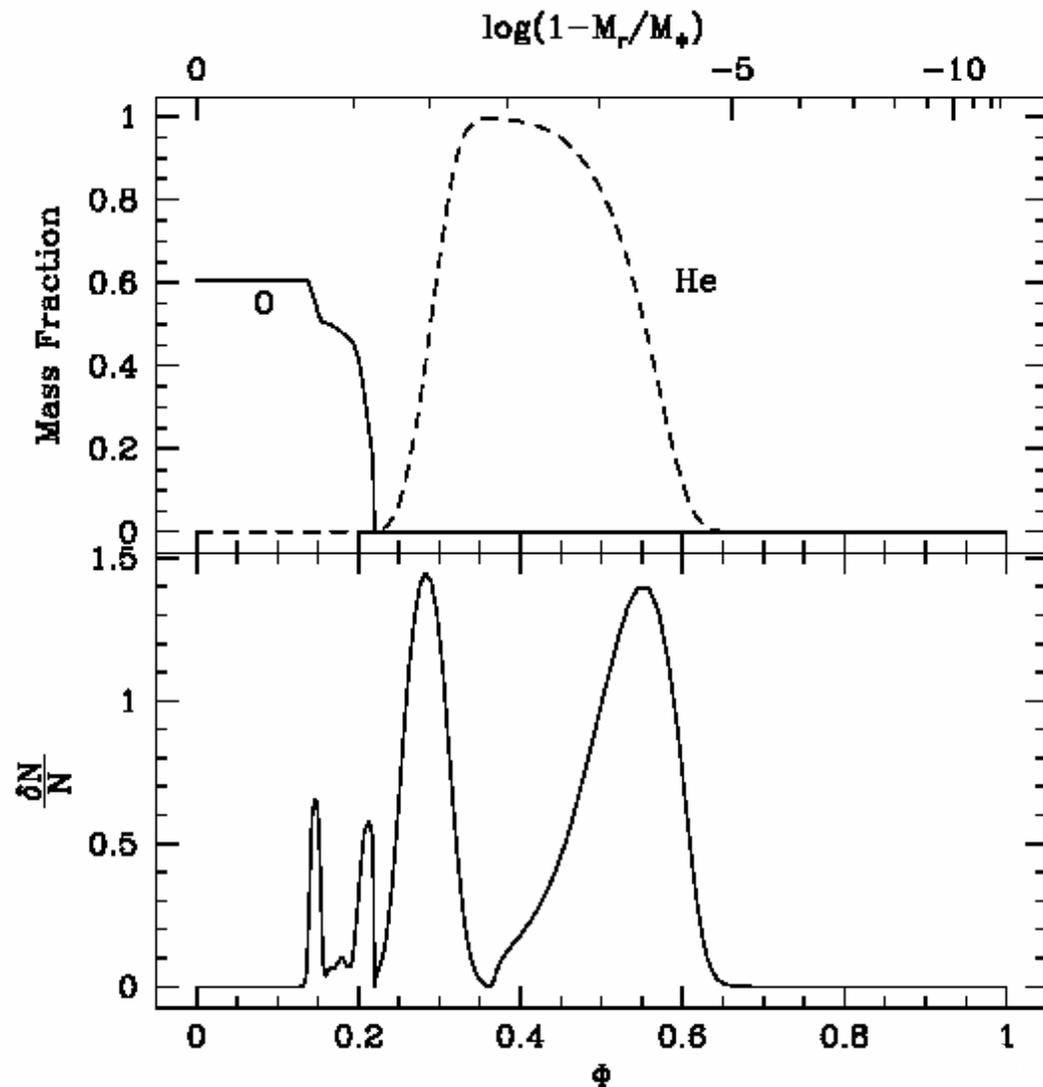
# Chemical Profiles produce bumps in $N$

The composition transition zones produce bumps in  $N$

DAV model

$M = 0.6 M_{\odot}$

$T_{\text{eff}} = 12000 \text{ K}$



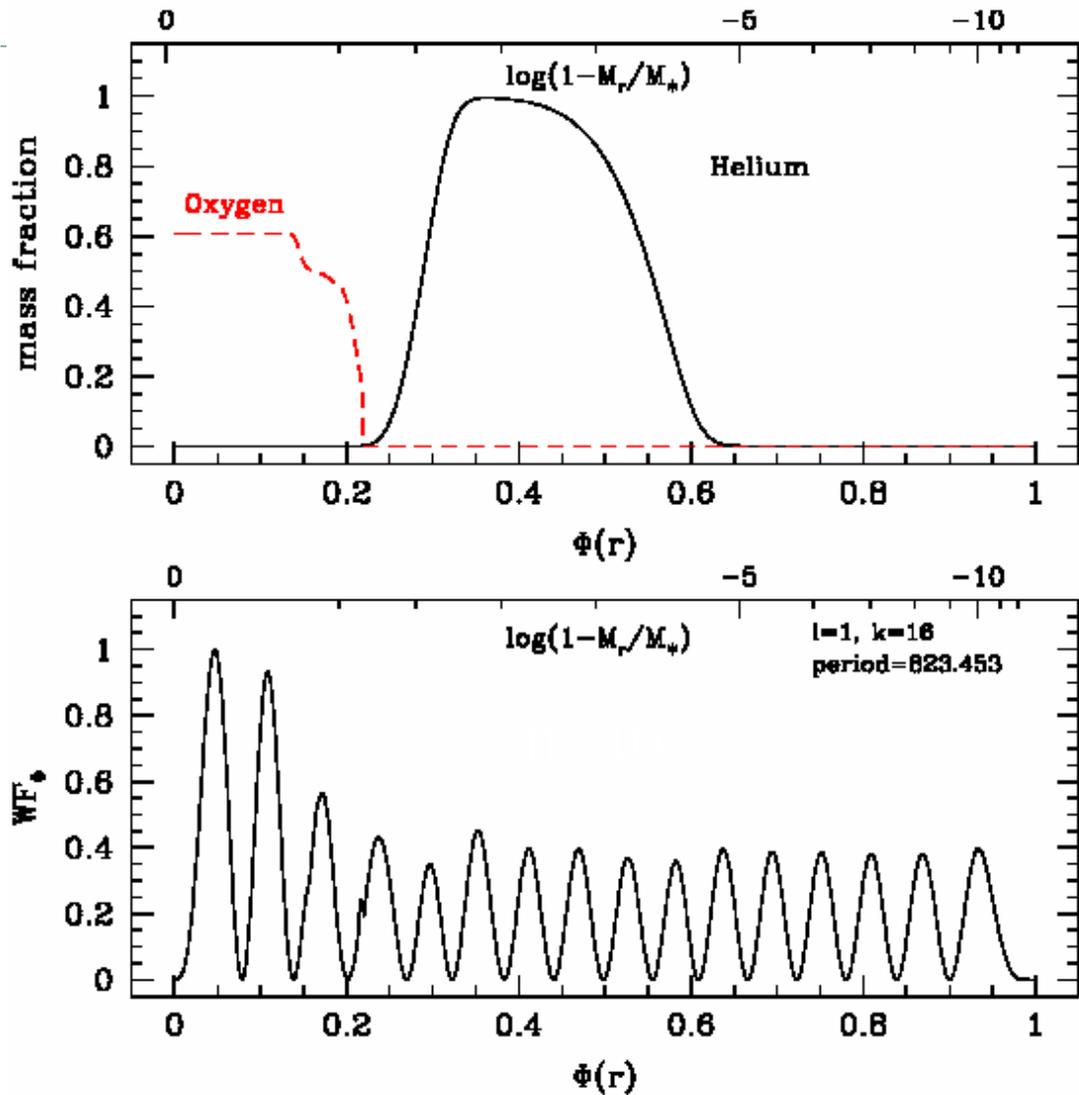
# The bumps can “trap” modes...

Unequal sampling  
produces unequal  
period spacings

DAV model

$M = 0.6 M_{\odot}$

$T_{\text{eff}} = 12000 \text{ K}$



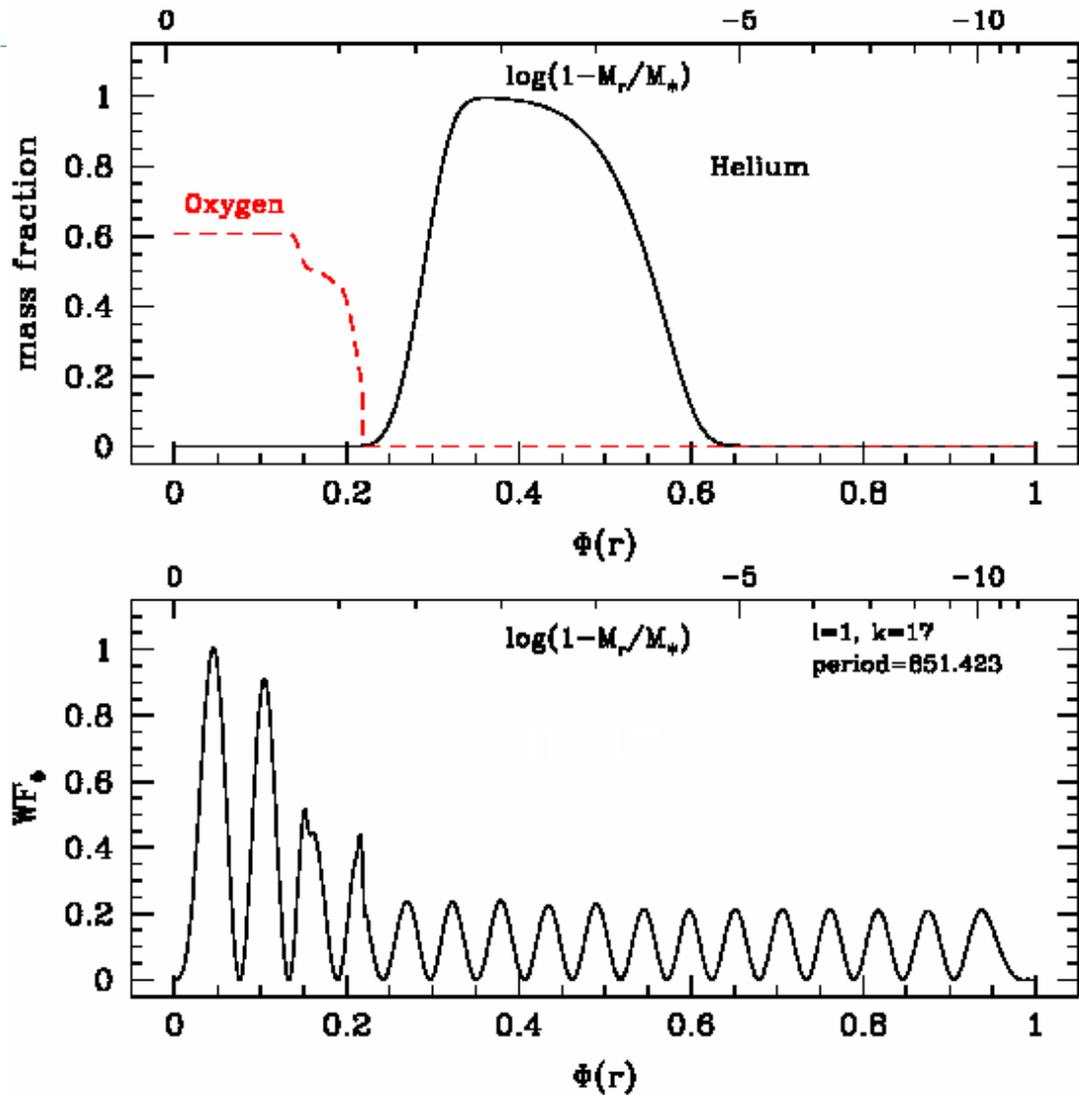
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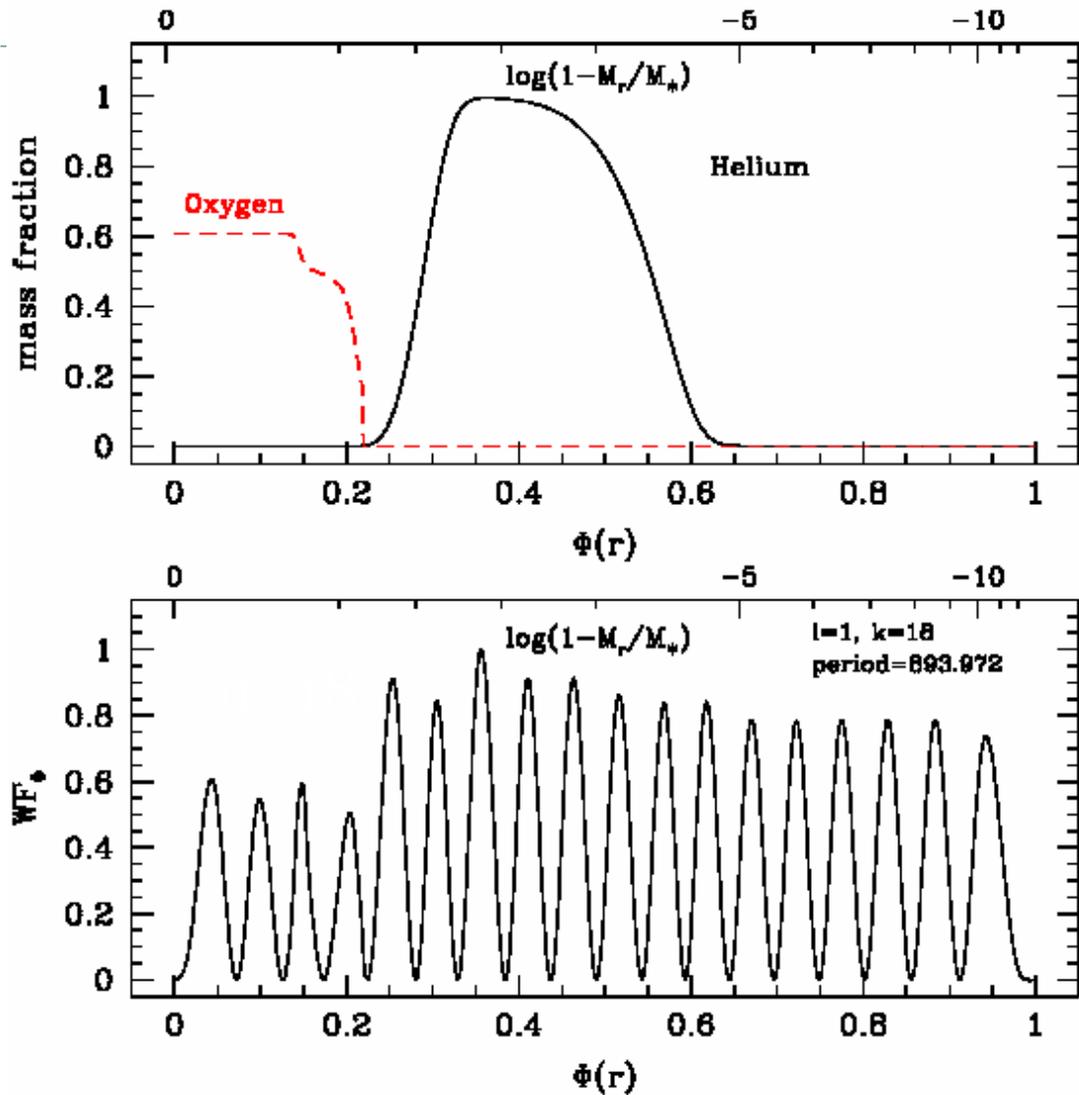
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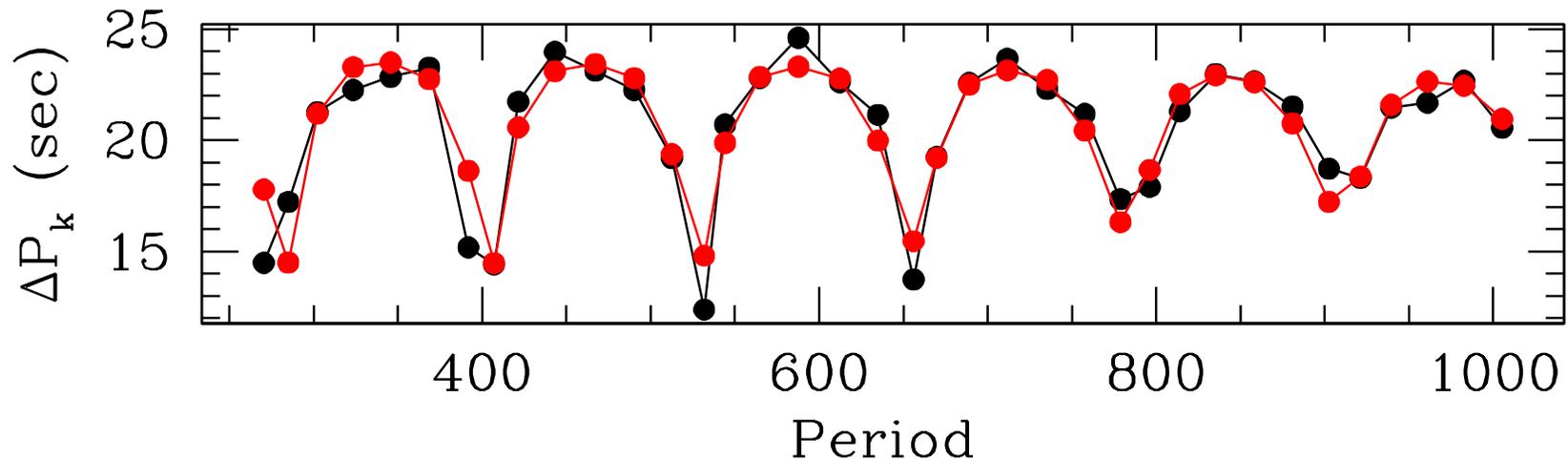


# This information is encoded in the periods...



Variations in the period spacing  $\Delta P_n$  contain information about the structure of the model

$$\Delta P_n \equiv P_{n+1} - P_n$$



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