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# CKM Physics in $e^+e^-$ Colliders

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KEK

CKM 2018 @ Heidelberg

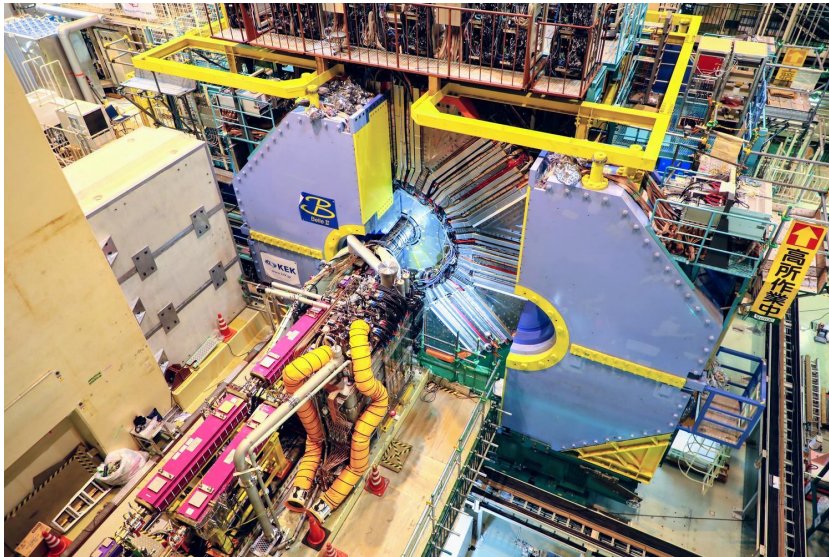
Sep. 17, 2018

# Contents

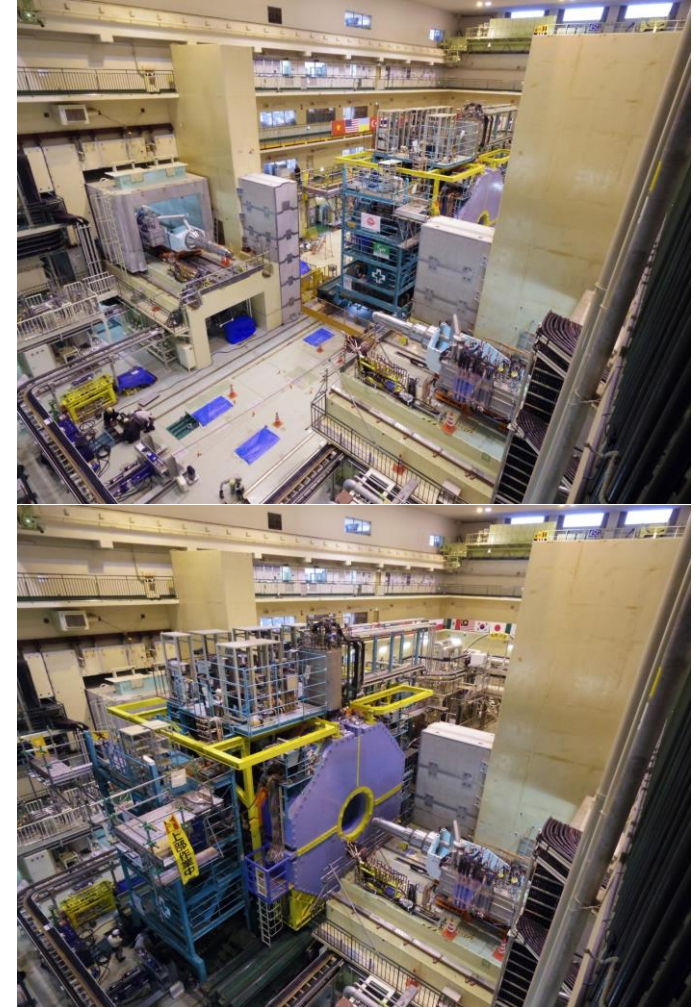


- Status of Belle II experiment.
- Results from BaBar and Belle.

Belle II before Phase 2 (2018 Mar)



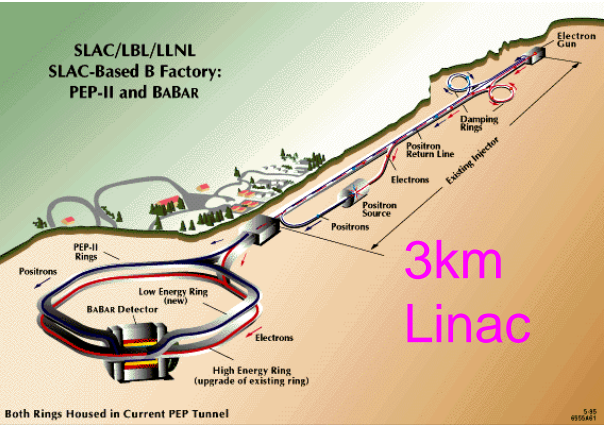
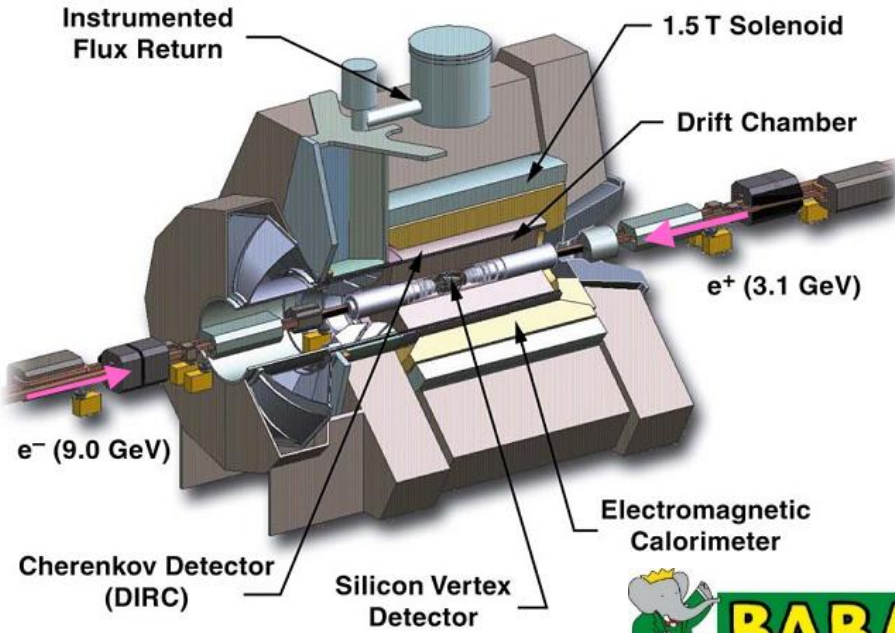
Belle II go to beamline (2017/4/11)





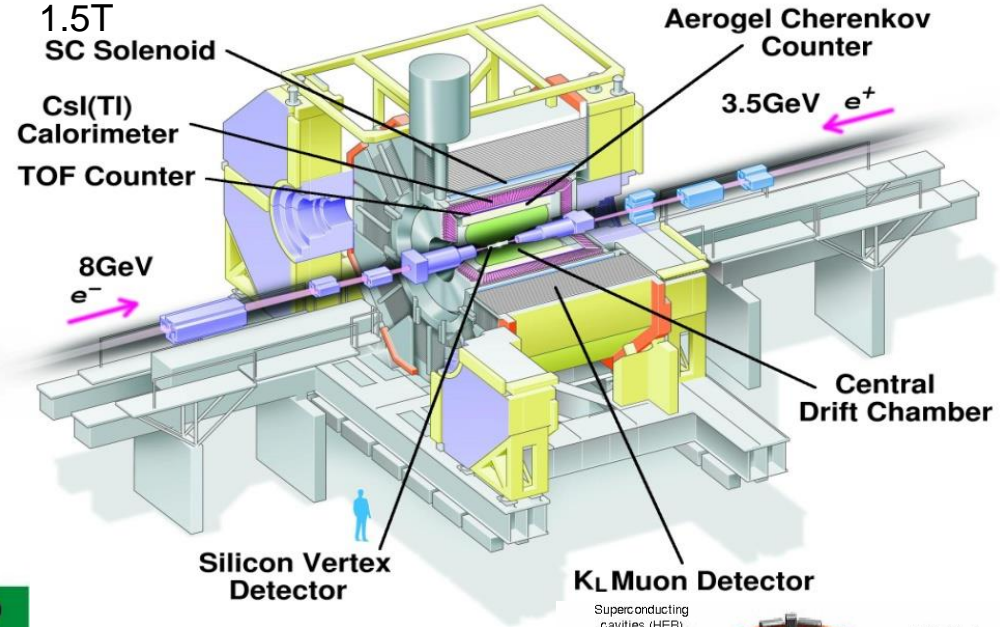


# Two B Factories



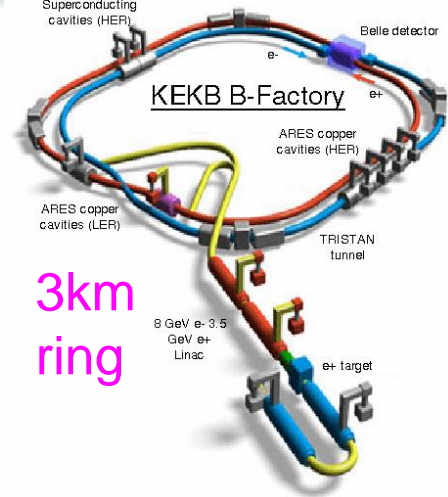
BaBar @ PEP-II

9 GeV  $e^-$  +  
3.1 GeV  $e^+$



Belle @ KEKB

8 GeV  $e^-$  +  
3.5 GeV  $e^+$

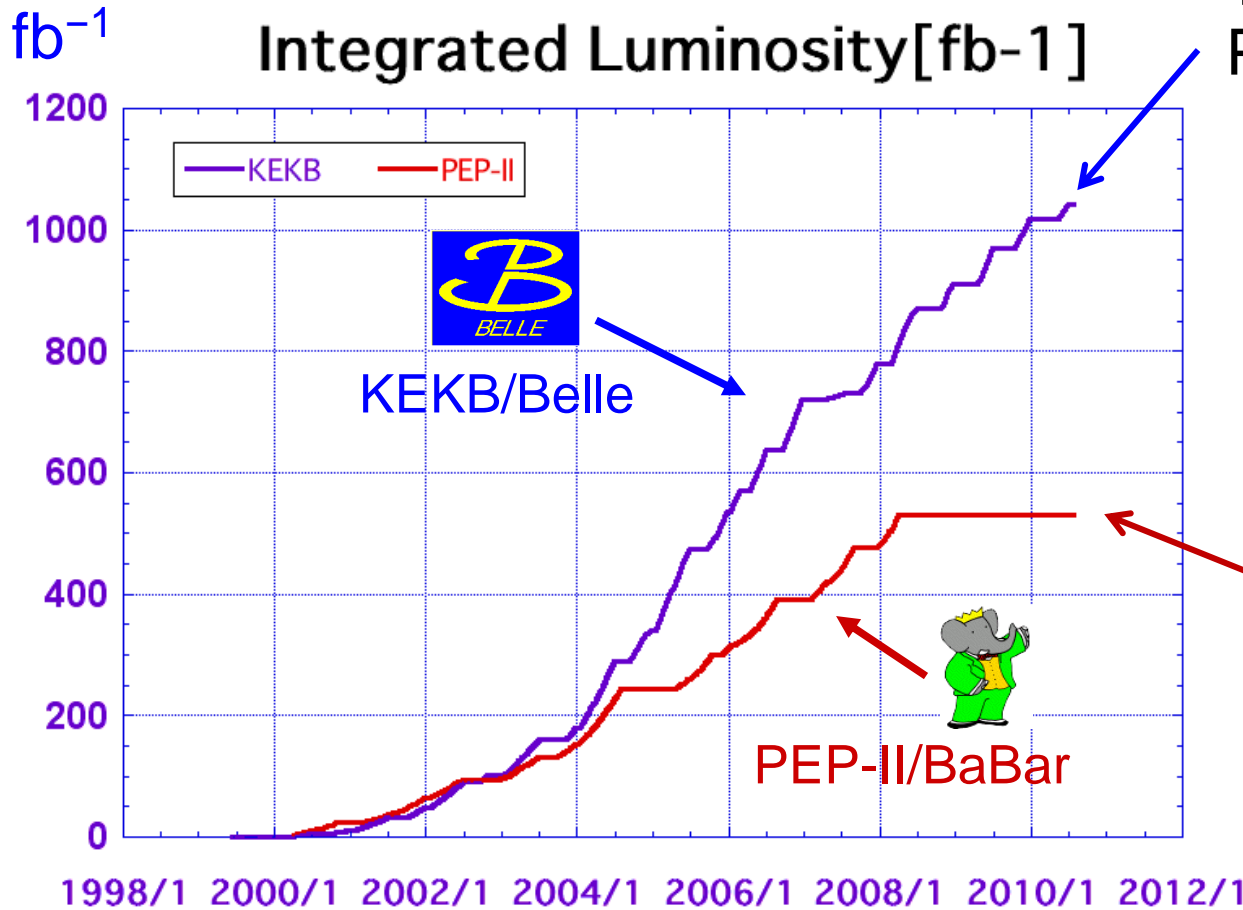


# Luminosity



$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B} \quad (\sigma=1.1\text{nb})$$

$1 \text{ fb}^{-1} \sim 10^6 B\bar{B} @ \Upsilon(4S)$   
 Total  $\sim 1040 \text{ fb}^{-1}$   
 Peak  $2.11 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



On resonance:

$\Upsilon(5S)$ : 121 fb<sup>-1</sup>

$\Upsilon(4S)$ : 711 fb<sup>-1</sup>

$\Upsilon(3S)$ : 3 fb<sup>-1</sup>

$\Upsilon(2S)$ : 24 fb<sup>-1</sup>

$\Upsilon(1S)$ : 6 fb<sup>-1</sup>

Off resonance, scan:  
 $\sim 100 \text{ fb}^{-1}$

$B_s$

Total  $550 \text{ fb}^{-1}$

Peak  $1.21 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

On resonance:

$\Upsilon(4S)$ : 433 fb<sup>-1</sup>

$\Upsilon(3S)$ : 30 fb<sup>-1</sup>

$\Upsilon(2S)$ : 14 fb<sup>-1</sup>

Off resonance:  
 $\sim 54 \text{ fb}^{-1}$

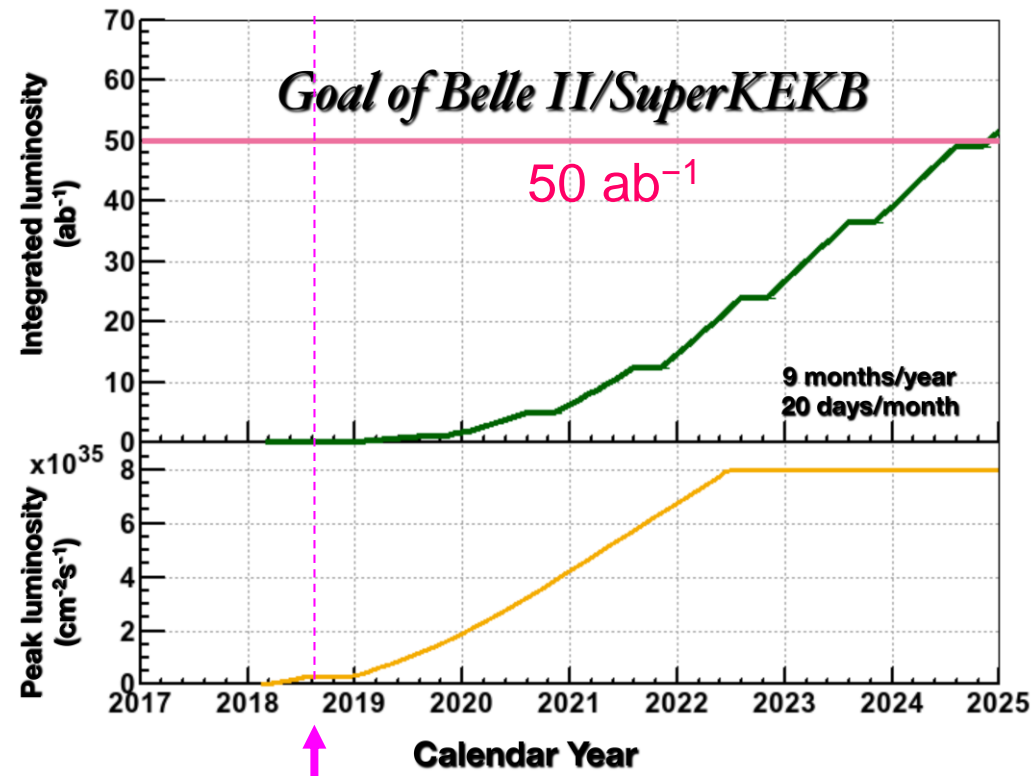
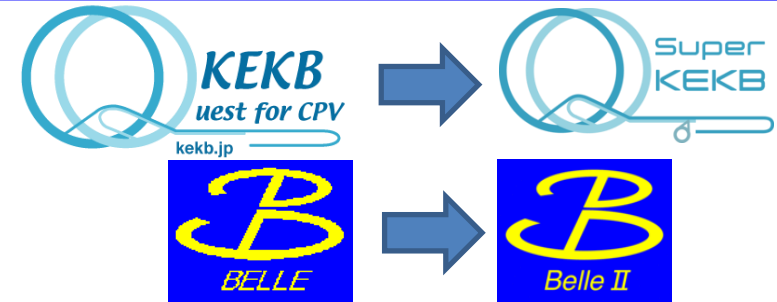
These data are taken till 2010.

# Belle II Experiment



Belle II experiment with SuperKEKB started!

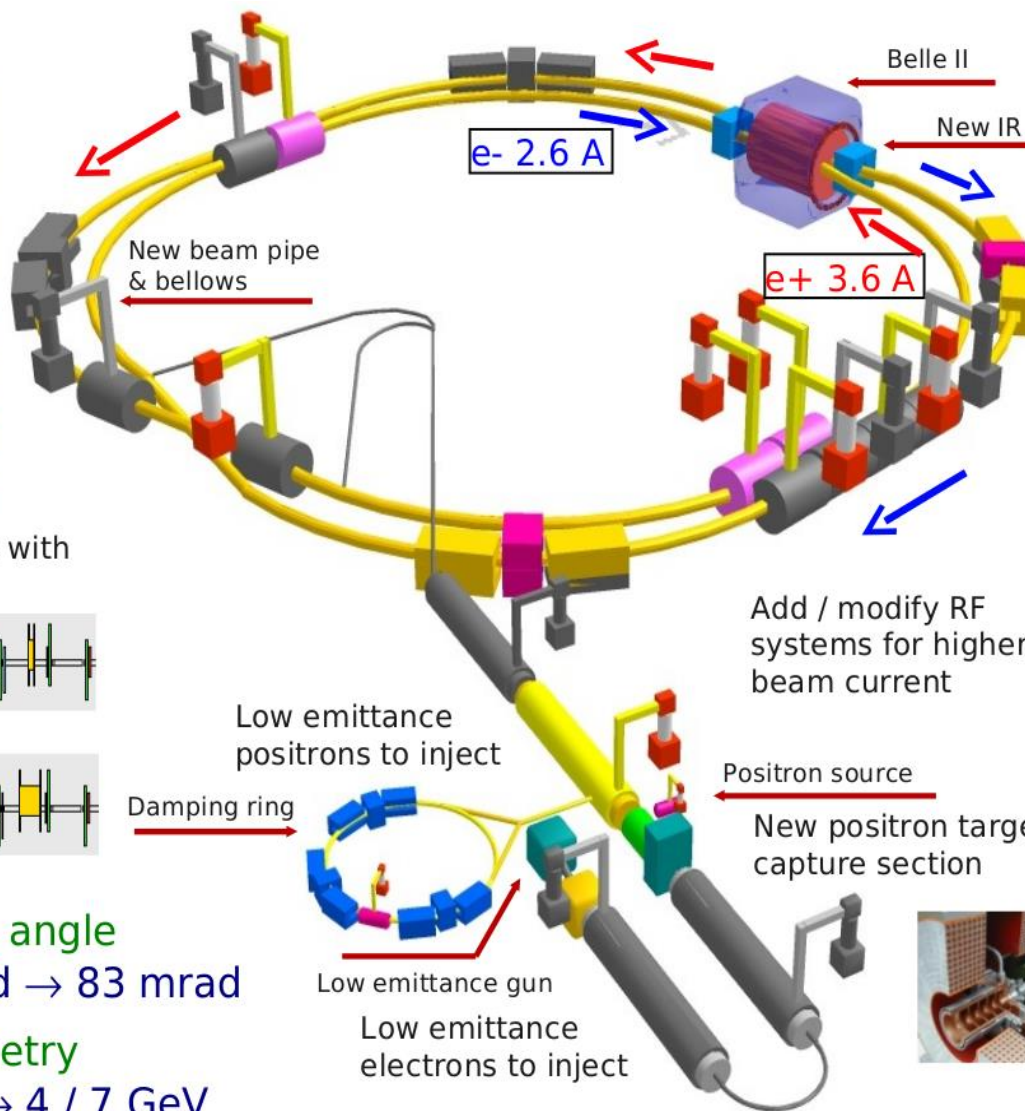
- SuperKEKB targeting  $8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$  ( $\times 40$  of Belle)
  - ✓ “Nano beam scheme”:
    - $\times 1/20$  beam size ( $\sim 50\text{nm}$ )
    - $\times 2$  beam current (2-3 A)
- Belle II spectrometer.
  - ✓ New type of vertex and PID detector.
- Phase 2 Operation in 2018.



Phase 1 (2016)	without Belle II
Phase 2 (2018)	with Belle II (no VXD)
Phase 3 (2019-)	with full Belle II



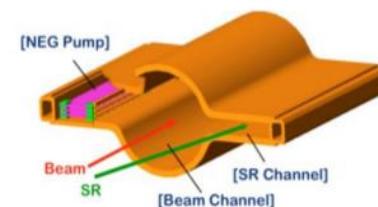
# SuperKEKB



New superconducting / permanent final focusing quads near the IP



TiN-coated beam pipe with antechambers

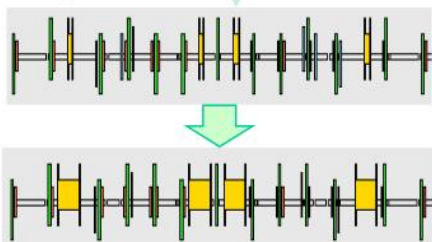


Add / modify RF systems for higher beam current

Redesign the lattices of HER & LER to squeeze the emittance



Replace short dipoles with longer ones (LER)



Larger crossing angle

$$2\phi = 22 \text{ mrad} \rightarrow 83 \text{ mrad}$$

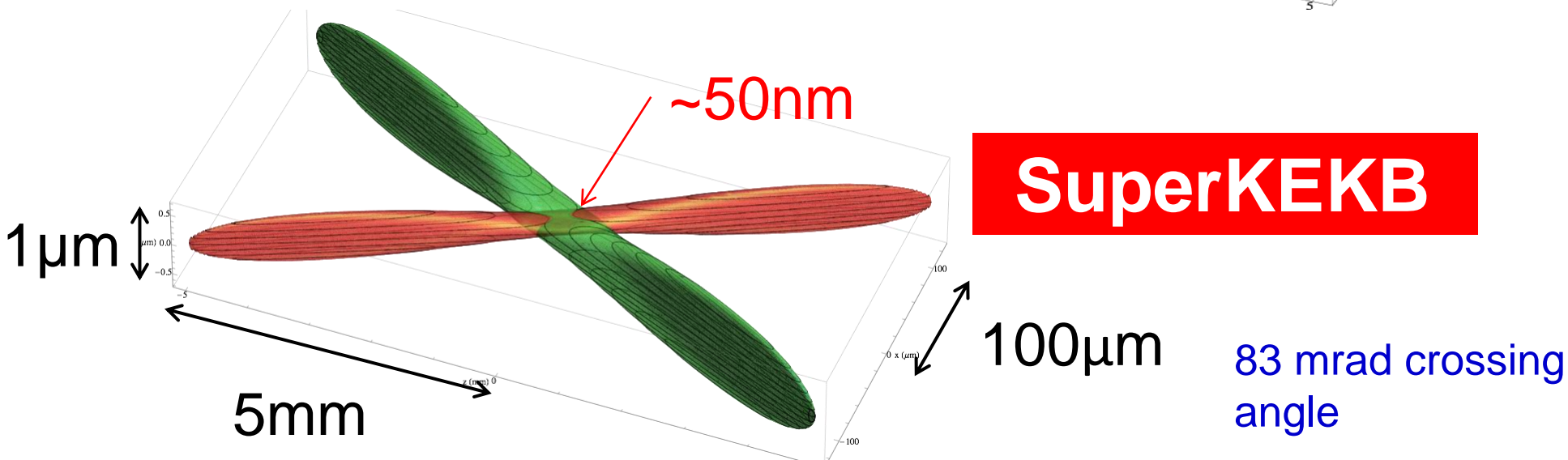
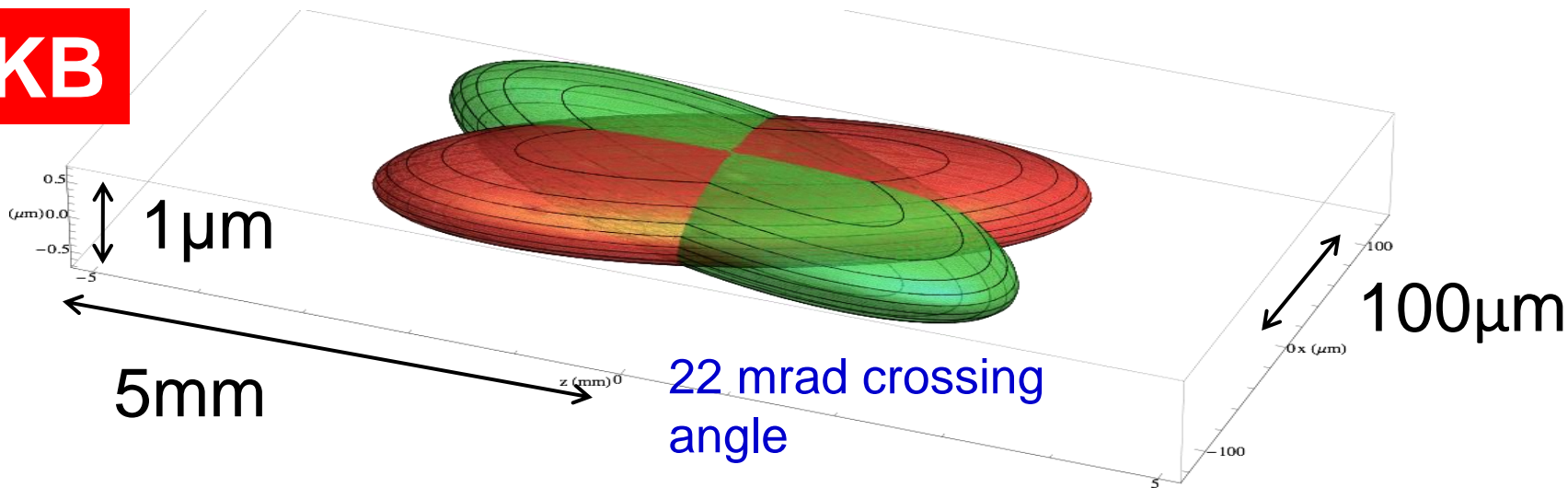
Smaller asymmetry

$$3.5 / 8 \text{ GeV} \rightarrow 4 / 7 \text{ GeV}$$

# SuperKEKB

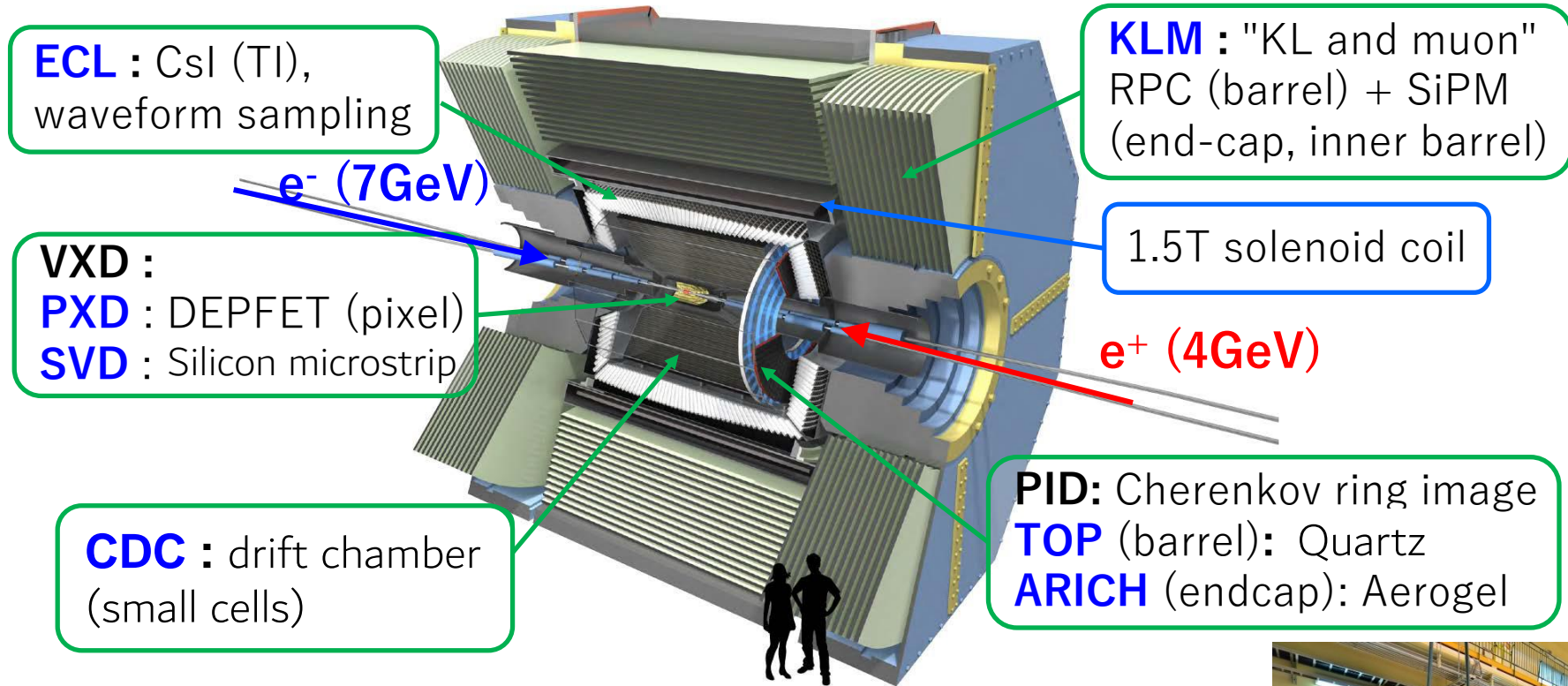


**KEKB**



**SuperKEKB**

# Belle II Spectrometer



- Operation at higher luminosity (background)
- New type of Vertex and PID detector.

ARICH (during construction)

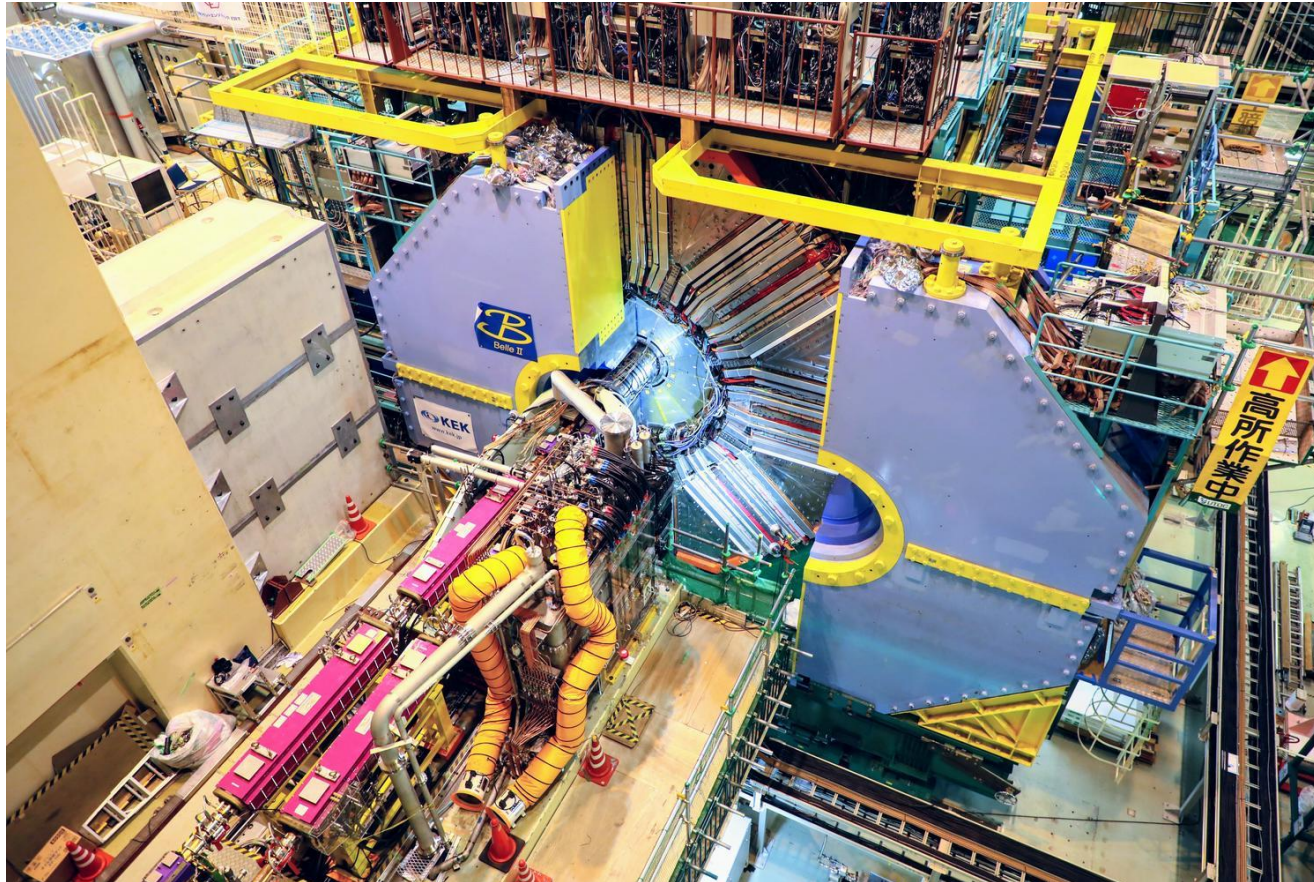




# Phase II Operation



- The construction of SuperKEKB was completed.
- Belle II detector without vertex detectors.
- Phase II operation: Mar-Jul, 2018.

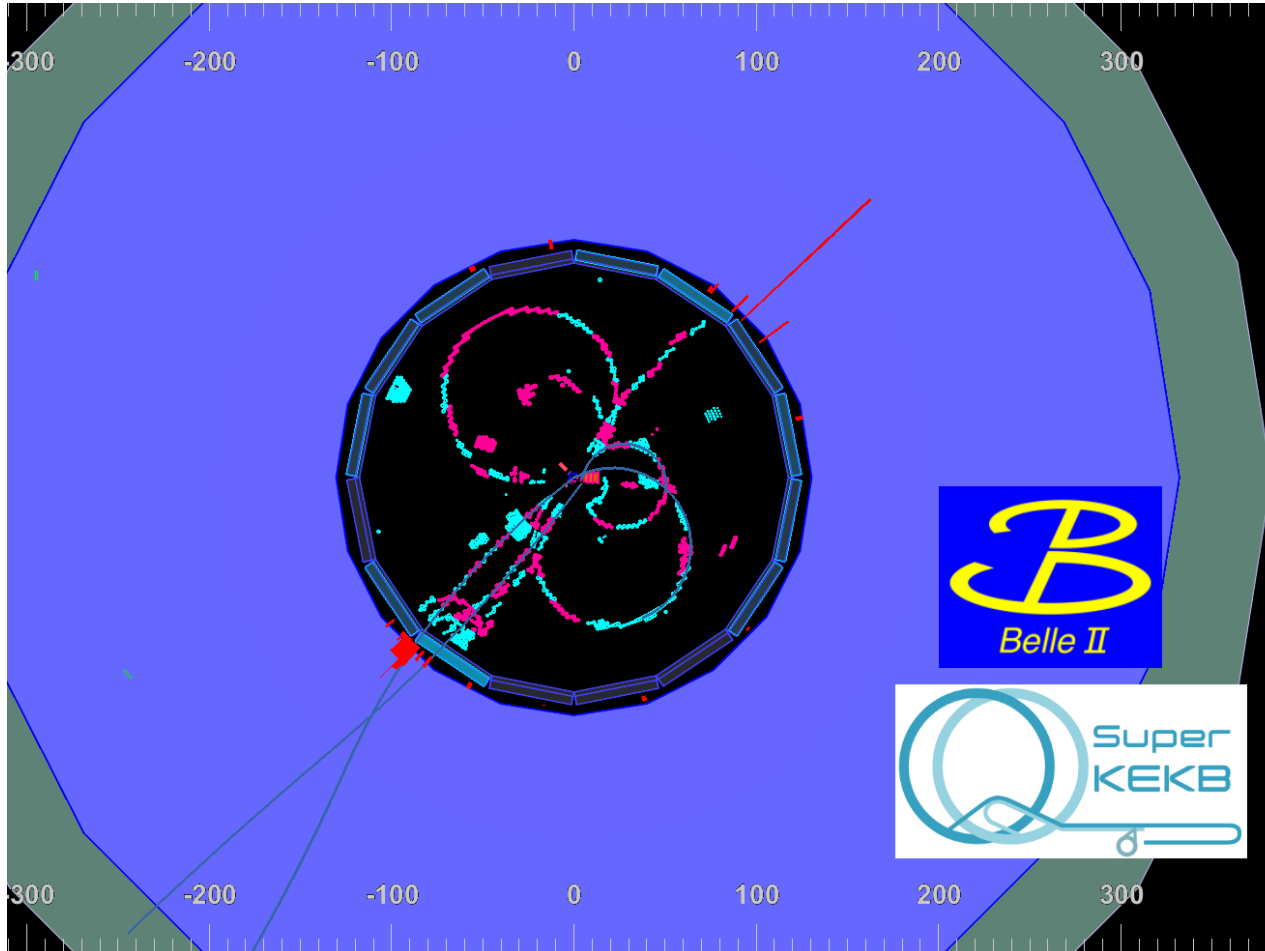


(Mar. 2018)

# Belle II First Collision



Belle II first collision at 0:46 on Apr. 26, 2018

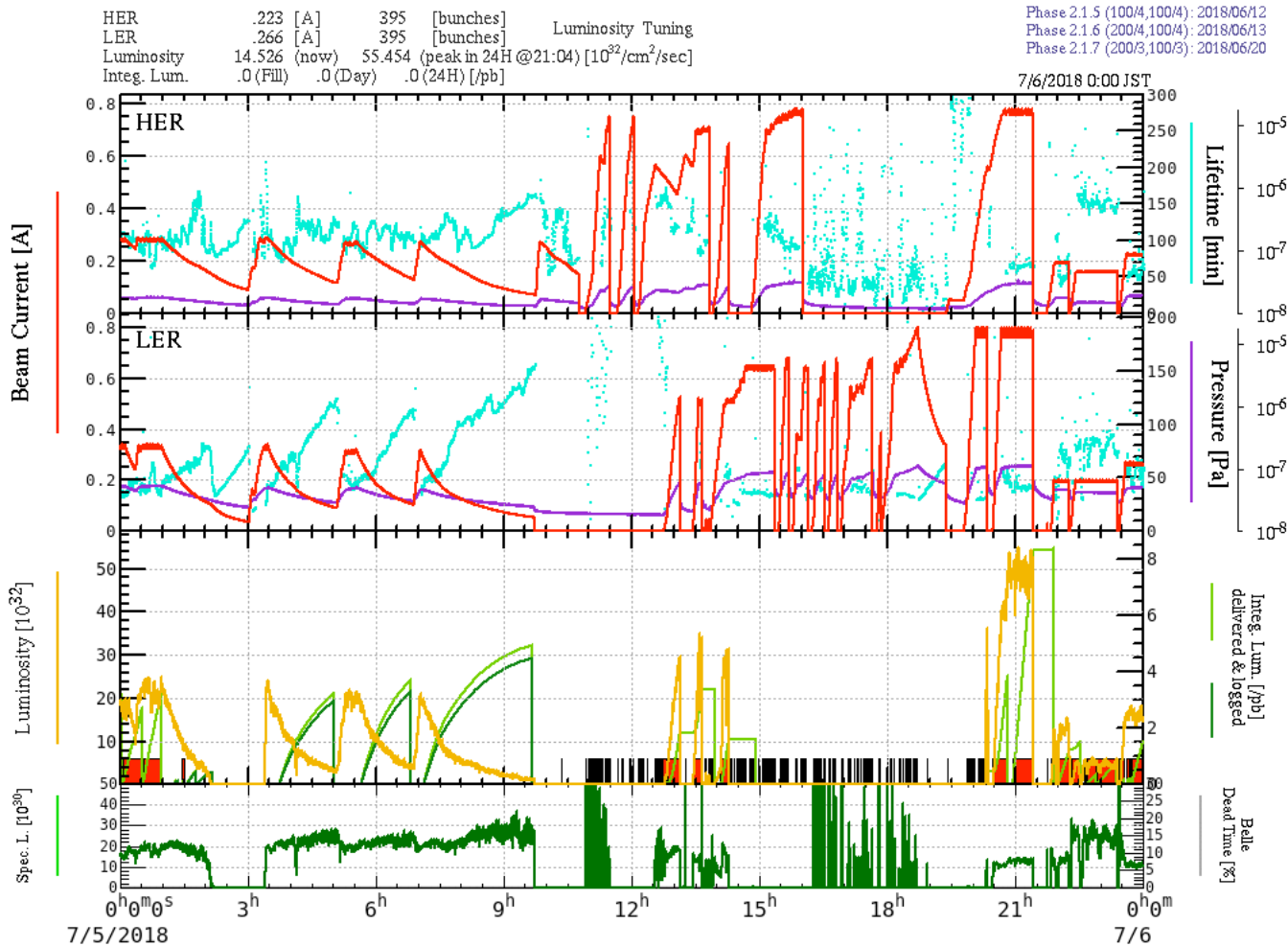




# Phase 2 Operation



## One day history of SuperKEKB (Jul 5, 2018)



- Mostly accelerator tuning.
- Physics run (in the midnight).
- Maximum luminosity  $5.5 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  (during accelerator study).
  - ✓  $1\text{-}2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  during physics run

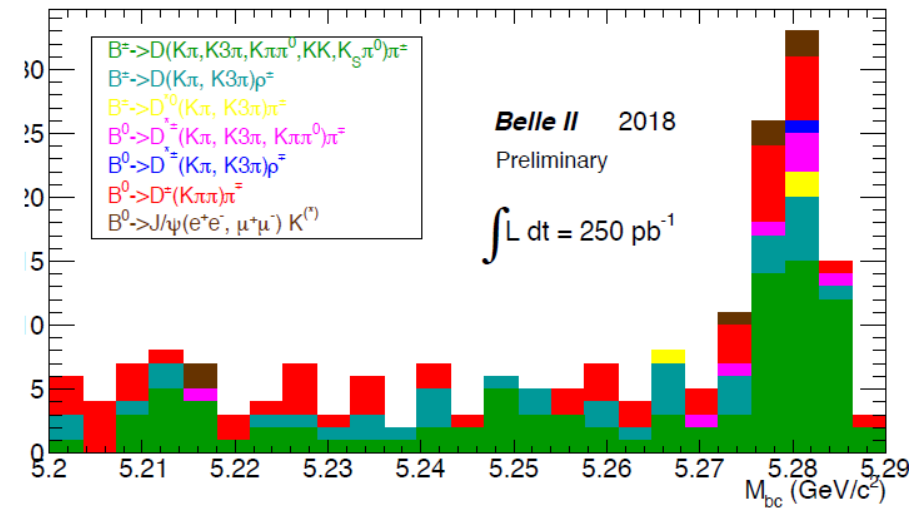
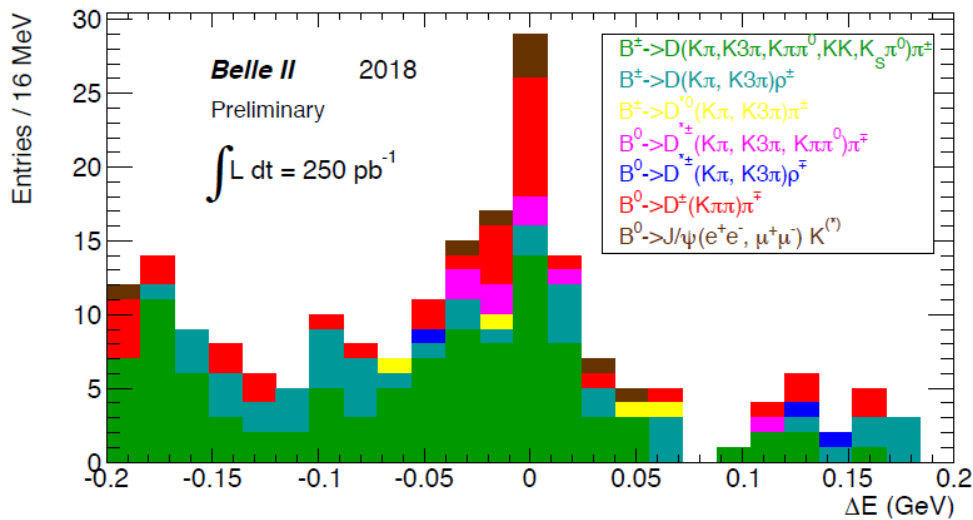
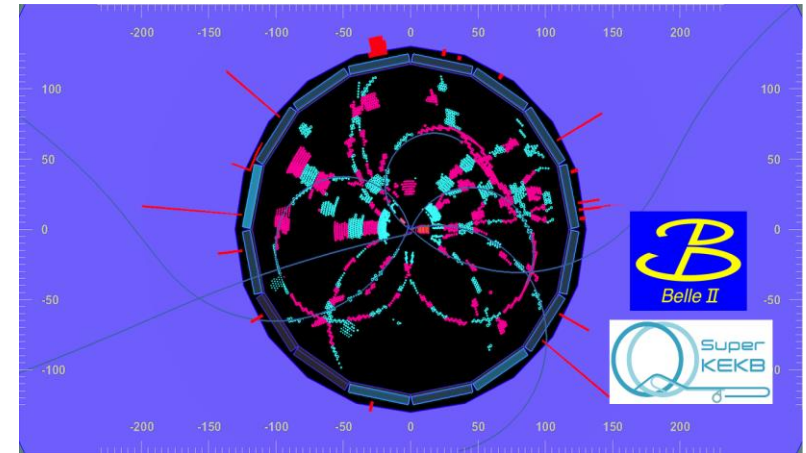


# Phase 2 Operation



- The main purpose of Phase II operation was the accelerator tuning and the study of nano beam scheme.
- Physics data were also taken: total data size  $0.5 \text{ fb}^{-1}$ 
  - ✓ Understanding of the detector.
  - ✓ B mesons are reconstructed.

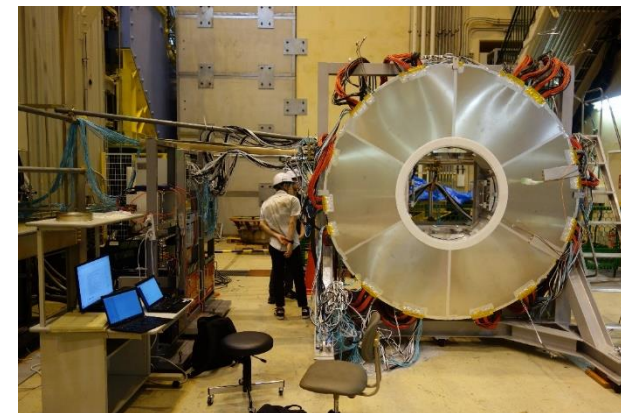
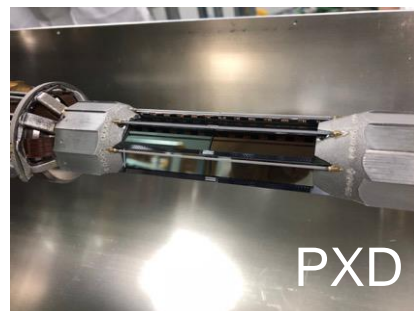
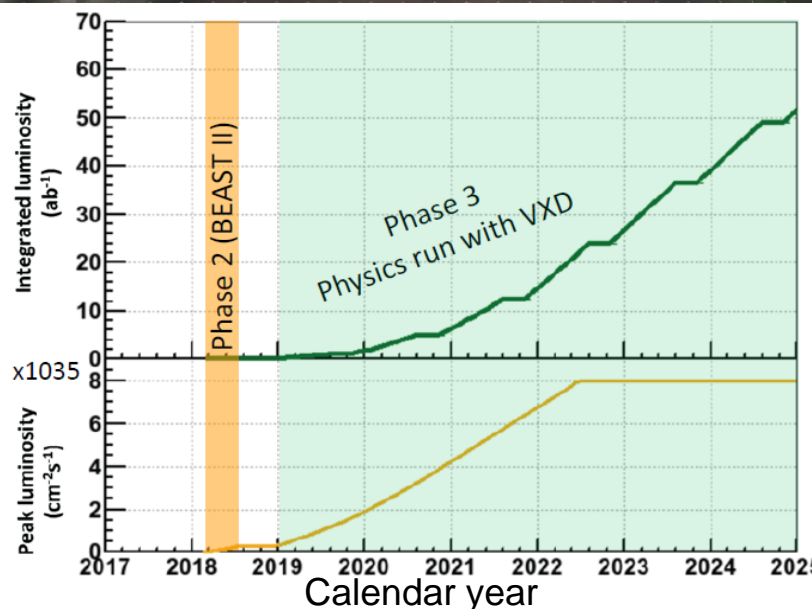
potential  $B\bar{B}$  candidate



# Toward Phase 3



- The construction of SVD (inner vertex detector) is finished. Under commissioning outside Belle II.
- Will be installed to Belle II together with PXD (innermost pixel detector) towards the end of this year.
- Other maintenance, repair work is going on.



Phase III operation (physics run) starts in early 2019.

## Let's go back to BaBar and Belle



**BABAR**

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- Data were taken till 2008/2010.
- But the analysis is still active, and we have new results.



# B Tagging Technique



- Reconstruction of B decay modes with one or more neutrinos in the final states.
- **B mesons are produced in pair** → **Reconstruct or tag the other B.**
  - ✓ **Full reconstruction:** reconstruct the other B with hadronic modes.
  - ✓ **Semi-leptonic tag:** tag the other B with semi-leptonic decays.
  - ✓ **Inclusive:** reconstruct signal B and check if the rests are consistent with B.
  - ✓ **Untagged:** do not tag the other B (applicable in case of one neutrino)
- In general, a method with high purity has low efficiency. Typical full reconstruction efficiency is  $O(0.1\%)$ .
- Effort to improve the performance, which directly affects the analysis sensitivity.



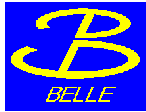
FEI (Full Event Interpretation)



[arXiv:1807.08680]

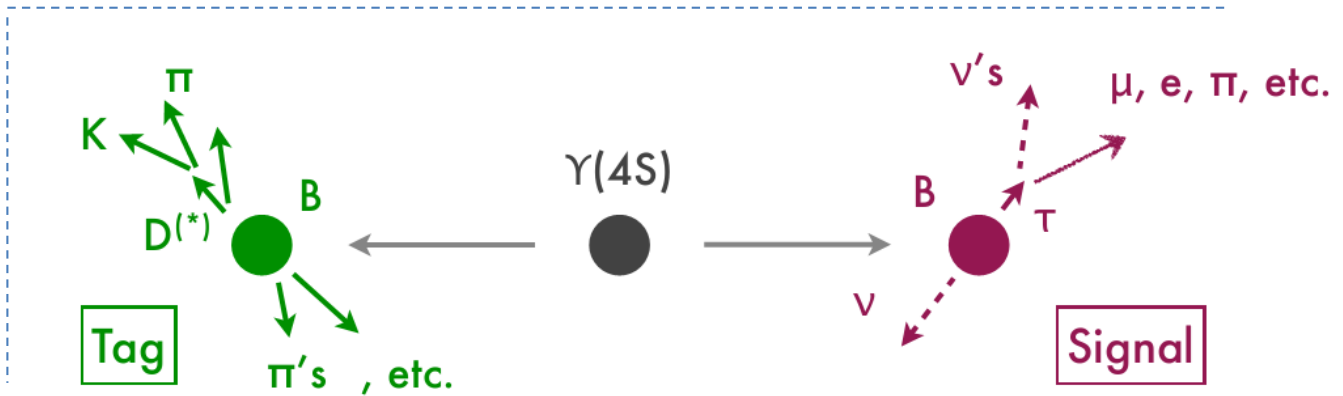
Talk by R. Van Tonder (WG1)

**New Result**



$B \rightarrow \ell \nu \gamma$  by Belle  
(first result w/ FEI)

Talk by M. Gelb (WG2)



# $B \rightarrow D^{(*)}\tau\nu$

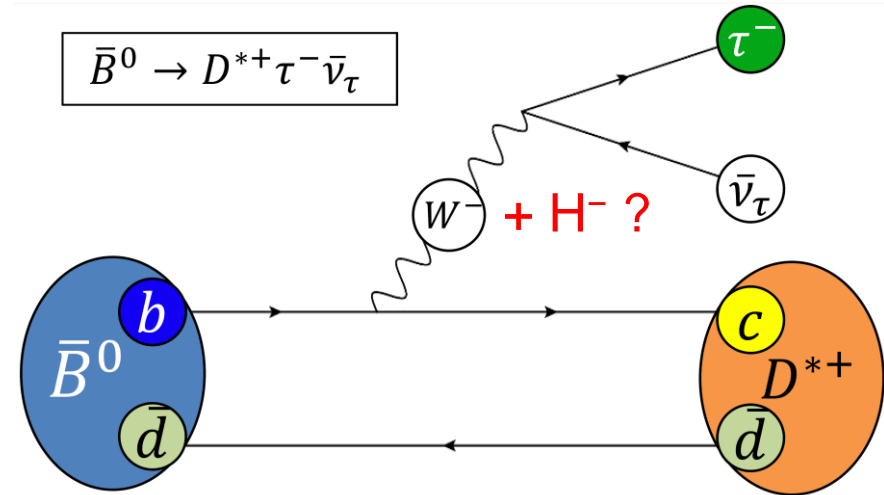


- NP contribution is tree diagram?
  - ✓ Sensitive to charged Higgs.
- Measure the branching ratio

$$R(D^{(*)}) = \frac{BF(\bar{B} \rightarrow D^{(*)}\tau^{-}\bar{\nu}_{\tau})}{BF(\bar{B} \rightarrow D^{(*)}l^{-}\bar{\nu}_{l})}$$

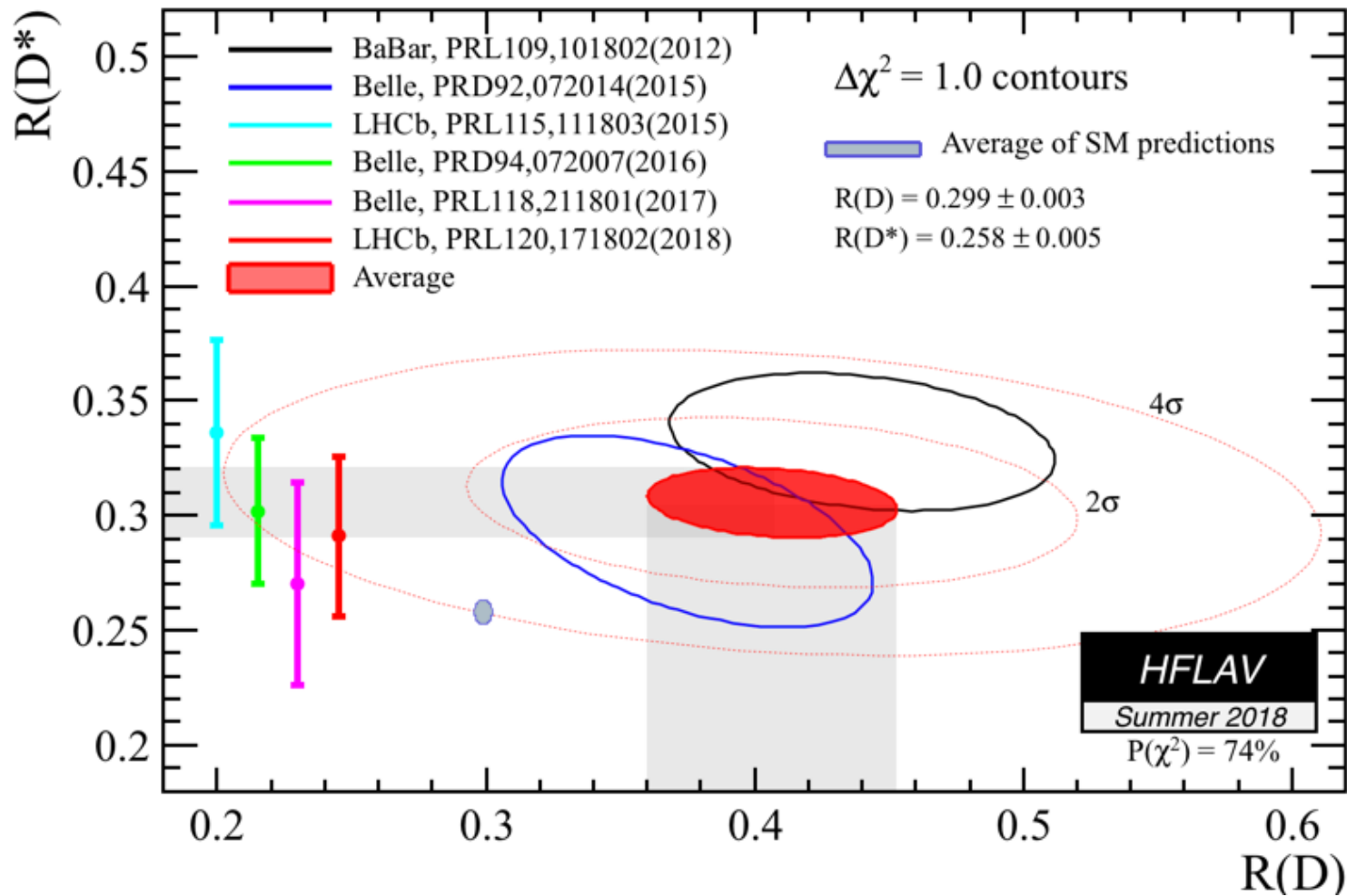
$(l^{-} = e^{-}, \mu^{-})$

- ✓ Cancel form factors.
- ✓ Cancel experimental systematics



- Several measurements from Belle and BaBar
  - ✓ With different B tagging method → Independent sample

# $B \rightarrow D^{(*)}\tau\nu$



- 3.8  $\sigma$  deviation from the SM
- 2.3  $\sigma$  in  $R(D)$
- 3.0  $\sigma$  in  $R(D^*)$



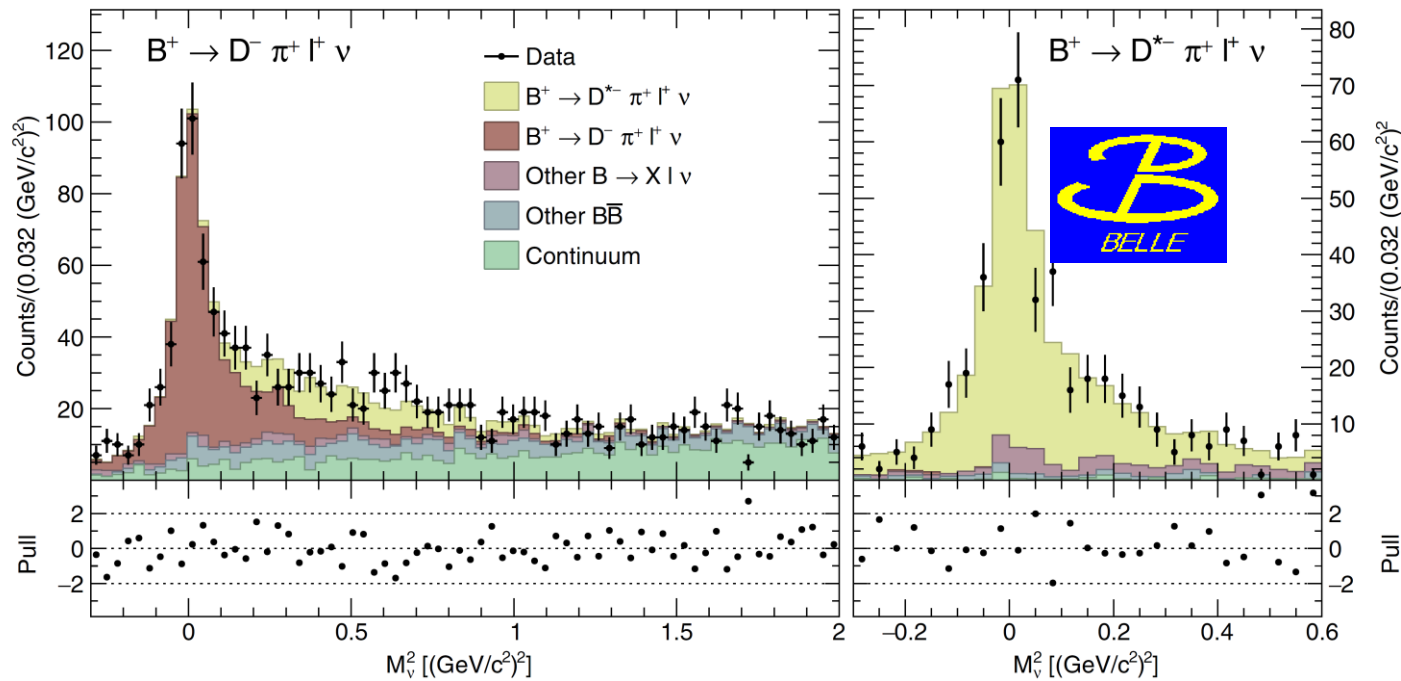
- More precise
- Other observables (polarization)



## For more precise measurement of $B \rightarrow D^{(*)}\tau\nu$

- More statistics  $\rightarrow$  Belle II
- Better understanding of the systematics
  - ✓ Dominant systematic error : the uncertainty of  $B \rightarrow D^{**}\ell\nu$  ( $D^{**}\tau\nu$ ).

## Measurement of $B \rightarrow D^{(*)}\pi\ell\nu$ at Belle



[PRD98, 012005 (2018)]

- Hadronic tag.
- Simultaneous fit on  $B \rightarrow D\pi\ell\nu$  and  $B \rightarrow D^*\pi\ell\nu$ .

# $B \rightarrow D^{(*)}\pi\ell\nu$



	Results	HFLAV2016
$B^+ \rightarrow D^- \pi^+ \ell^+ \nu$	$(4.55 \pm 0.27 \pm 0.39) \times 10^{-3}$	$(4.1 \pm 0.5) \times 10^{-3}$
$B^0 \rightarrow D^0 \pi^- \ell^+ \nu$	$(4.05 \pm 0.36 \pm 0.41) \times 10^{-3}$	$(4.2 \pm 0.6) \times 10^{-3}$
$B^+ \rightarrow D^{*-} \pi^+ \ell^+ \nu$	$(6.03 \pm 0.43 \pm 0.38) \times 10^{-3}$	$(6.0 \pm 0.6) \times 10^{-3}$
$B^0 \rightarrow D^0 \pi^- \ell^+ \nu$	$(6.46 \pm 0.53 \pm 0.52) \times 10^{-3}$	$(4.7 \pm 0.8) \times 10^{-3}$

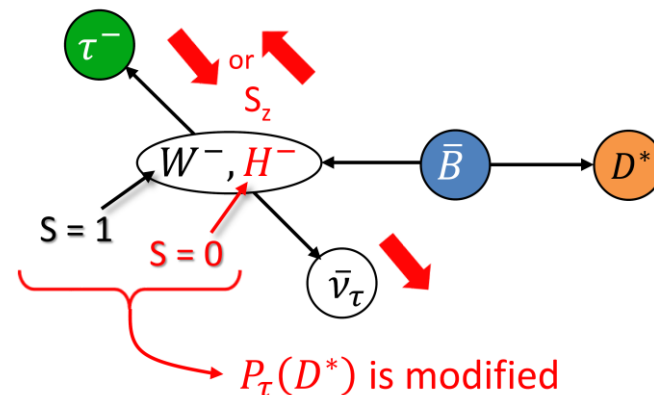
- Consistent with HFLAV.
- Precision is similar or slightly better compared to HFLAV2016.
- Main source of systematic errors are tag efficiency for charged modes, and PID, tracking efficiency for neutral modes.
  - ✓ Can be improved with luminosity (but not an easy work).

# $\tau$ Polarization in $B \rightarrow D^* \tau \nu$

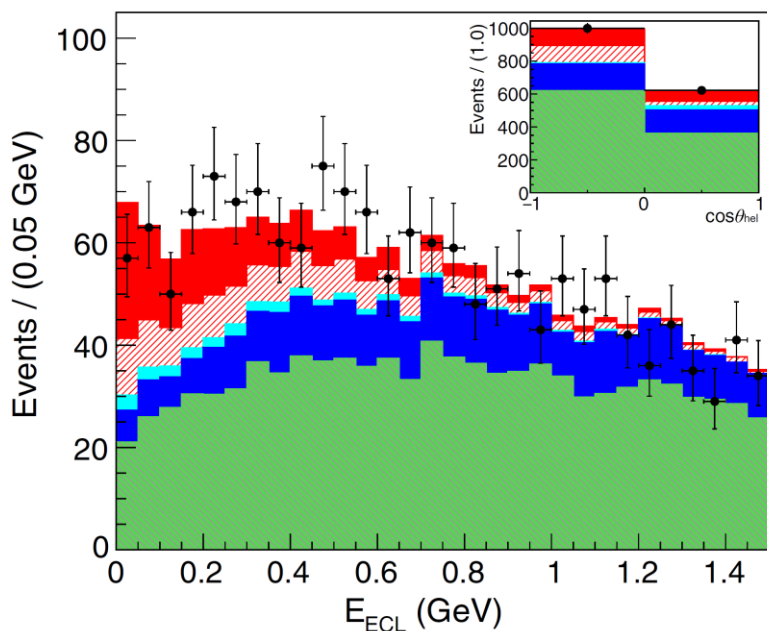


- Effect of the NP can appear in the polarization.
- Belle measured  $\tau$  polarization in  $B \rightarrow D^* \tau \nu$ 
  - ✓ Hadronic tag (full reconstruction)
  - ✓ Hadronic  $\tau$  decays.
  - ✓ 2 bins of  $\cos(\theta_{\text{hel}})$

[PRL 119, 211801 (2017);  
PRD 97, 012004 (2017)]

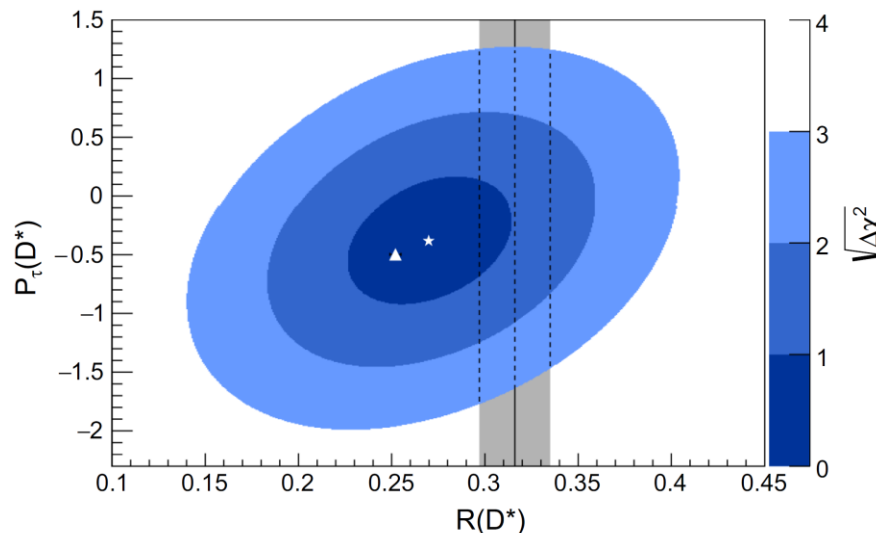


■ Signal     ■  $\bar{B} \rightarrow D^* \bar{\nu}_\tau$      ■ Fake  $D^*$  and  $q\bar{q}$   
▨  $\tau$  cross feed     ■  $\bar{B} \rightarrow D^{**} \bar{\nu}_\tau$  and Hadronic  $B$      ● Data



$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat.})^{+0.21}_{-0.16}(\text{syst.})$$

$$\text{SM} : P_\tau(D^*) = -0.497 \pm 0.013$$



Consistent  
with the SM  
at  $0.6\sigma$



# D\* Polarization in $B \rightarrow D^* \tau \nu$

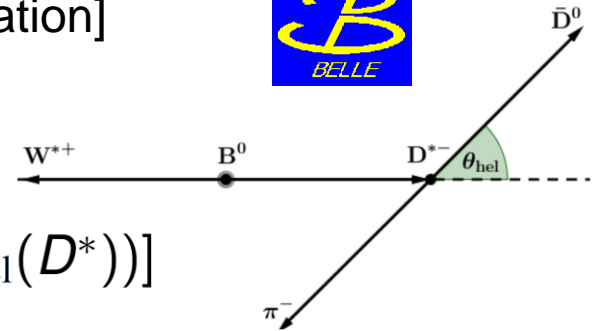


**New Result**

[BELLE-CONF-1805 in preparation]

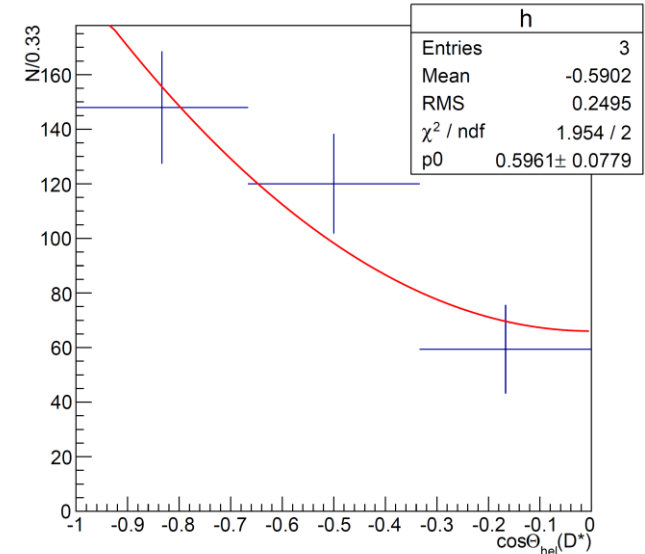


D\* polarization in  $B \rightarrow D^* \tau \nu$



$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}(D^*)} = \frac{3}{4} [2F_L^{D^*} \cos^2(\theta_{\text{hel}}(D^*)) + (1 - F_L^{D^*}) \sin^2(\theta_{\text{hel}}(D^*))]$$

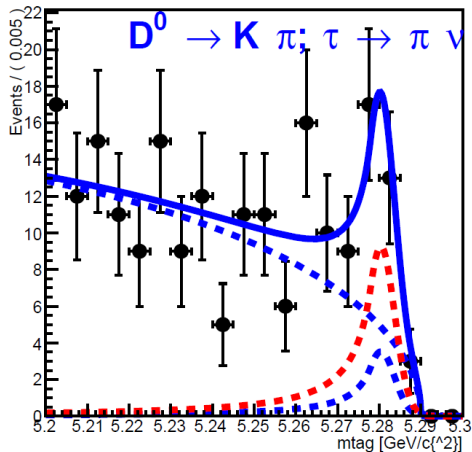
- Inclusive reconstruction
- All  $\tau$  decays can be used.
- Efficiency highly depends on  $\cos \theta_{\text{hel}}(D^*)$ .
- 3 bins of  $\cos \theta_{\text{hel}}(D^*)$ .



$$F_L^{D^*} = 0.60 \pm 0.08 \pm 0.03$$

Consistent with SM  
(~0.45) within  $2\sigma$

M(tag) for one mode with  
 $-0.67 < \cos \theta_{\text{hel}}(D^*) < 0.33$ .



Talk by K. Adamczyk (WG2)

# EW Penguin B Decays

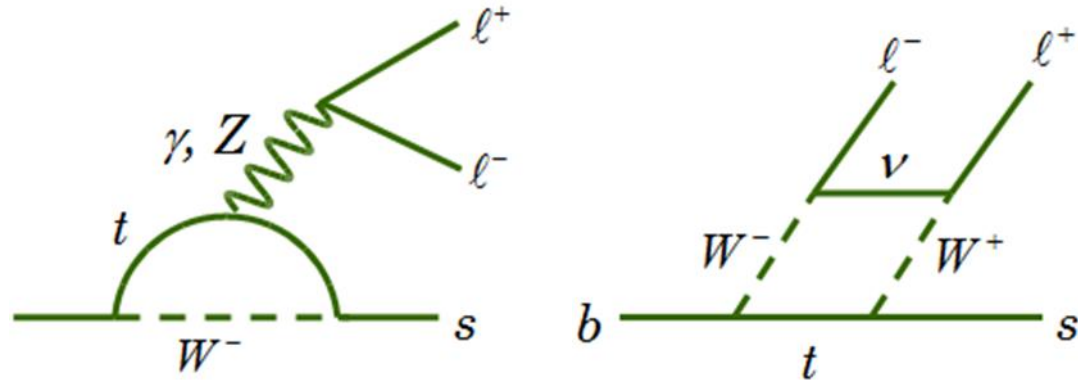


- $b \rightarrow s \ell^+ \ell^-$  : Electroweak penguin (or box) diagram.

✓ Sensitive to  $C_7, C_9, C_{10}$  .

- “Anomalies” seen:

- ✓ Lepton Flavour Universality.
- ✓ Angular variable



LHCb, JHEP08(2017)055

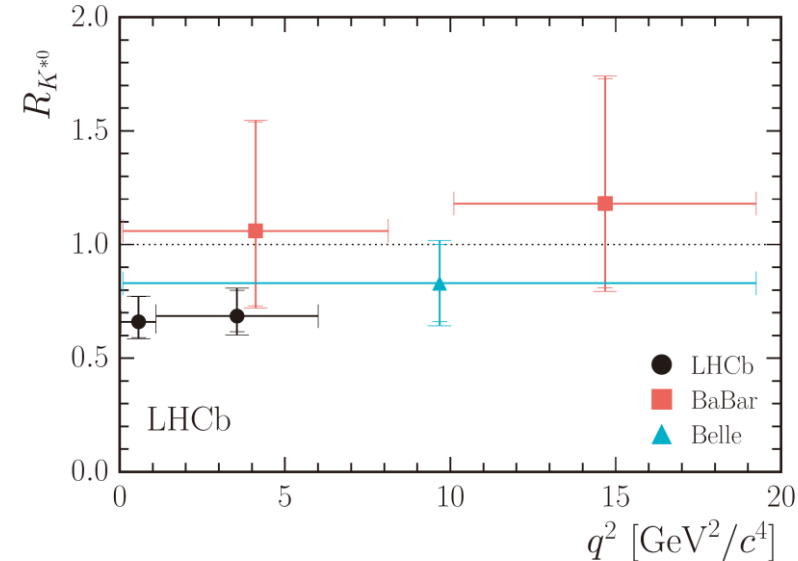
$$R_K \equiv \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu \mu)}{\mathcal{B}(B^+ \rightarrow K^+ e e)}$$

LHCb result

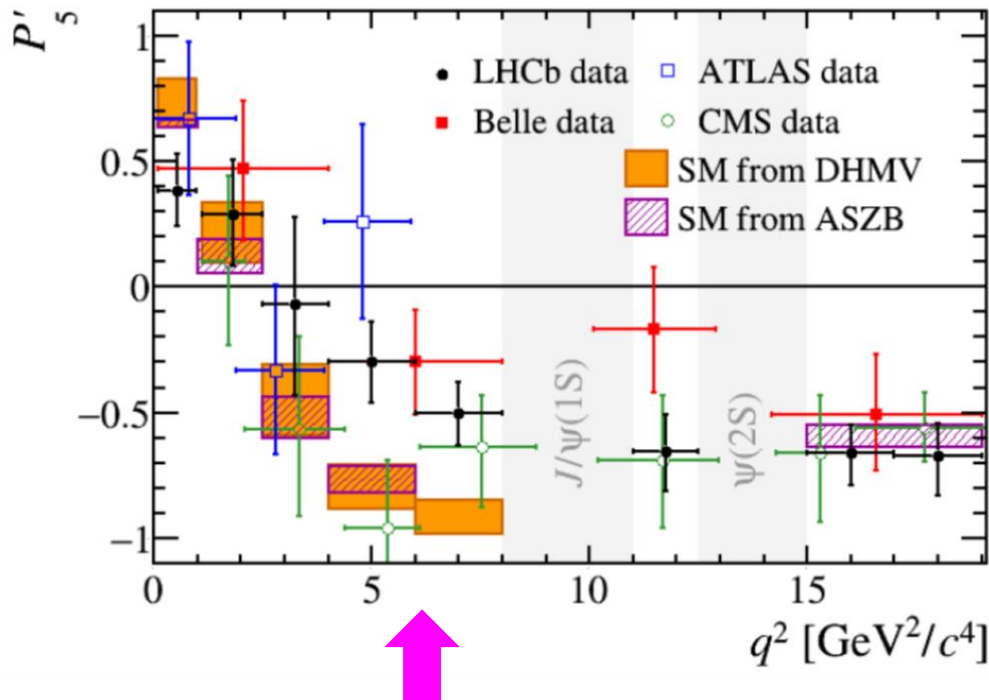
$$R_K = 0.745^{+0.090}_{-0.074} \pm 0.036 \quad (2.6\sigma \text{ from SM})$$

[PRL 113 (2014) 151601]

$R_{K^*}$  : 2.1-2.4 $\sigma$  deviation from SM.  $\longrightarrow$

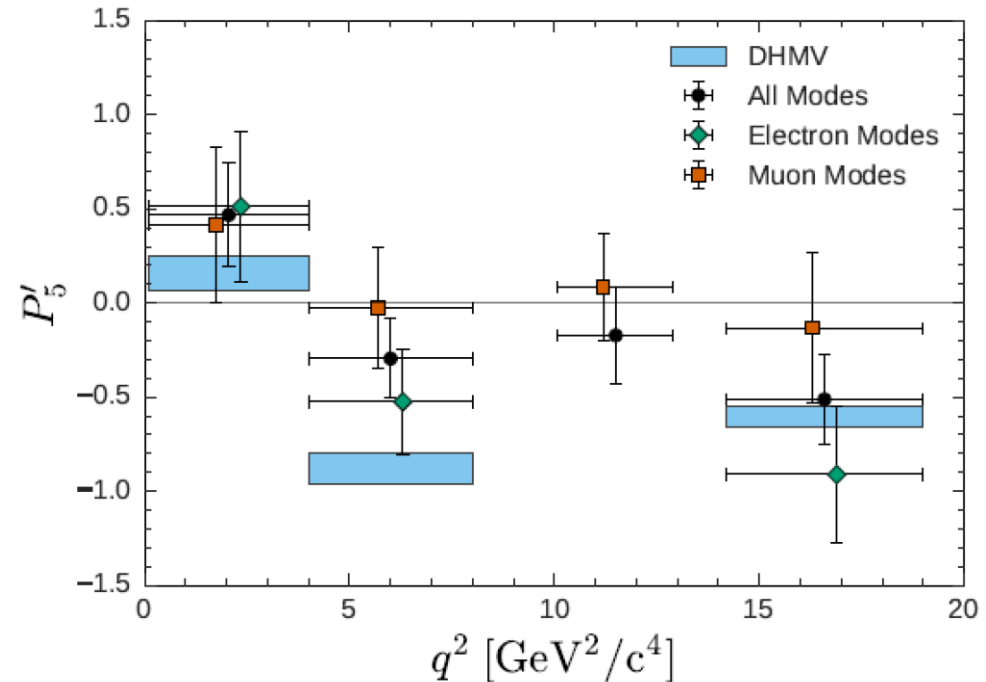


# EW Penguin B Decays



- $\sim 3\sigma$  deviation
- LHCb/ATLAS/CMS results from muon modes.

Belle measured  $P'_5$  separately for muon and electron modes.



- $2.6\sigma$  deviation in the muon mode.
- $1.1\sigma$  in the electron mode.

[PRL 118, 11801 (2017)]



# EW Penguin B Decays

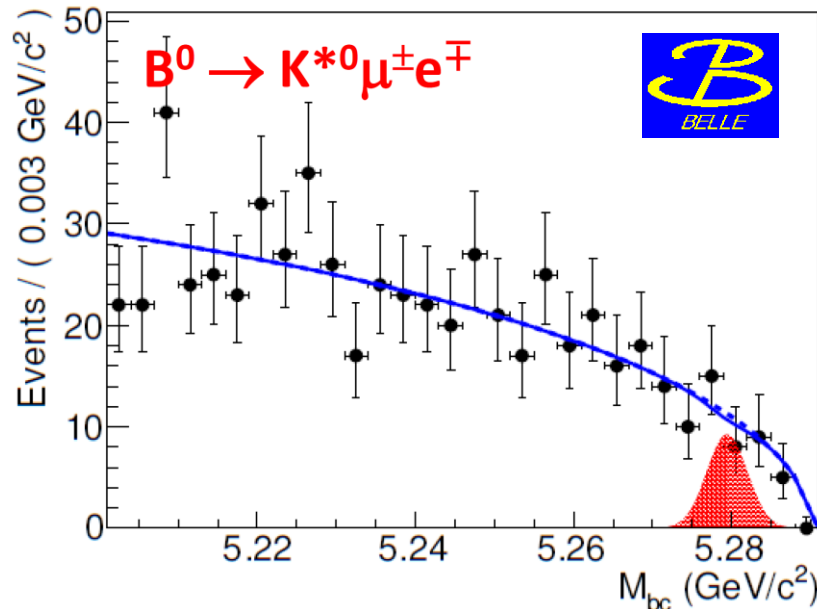


New results in a few more related modes.

Talk by T.Gershon (WG3)

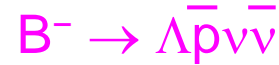


- Deviation in  $R(K)$ ,  $R(K^*)$  by LHCb.
- LFU violation  $\rightarrow$  LFV

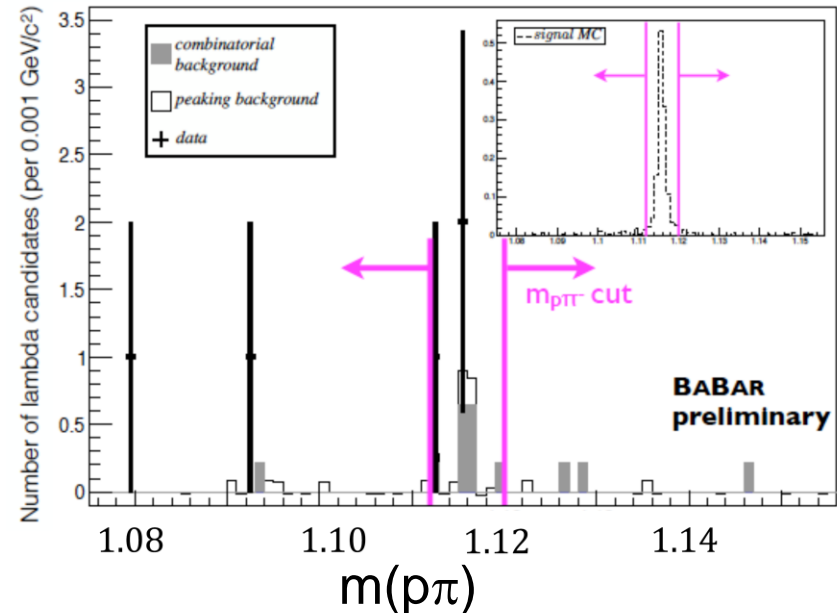


$B(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 1.8 \times 10^{-7}$

[arXiv:1807.03267, submitted to PRD]



- $b \rightarrow s \nu \bar{\nu}$  : FCNC process
- SM :  $B = (7.9 \pm 1.9) \times 10^{-7}$
- Hadronic B tag



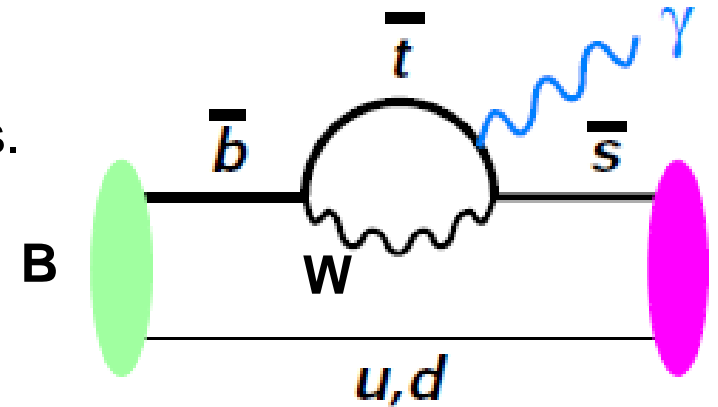
$B(B^- \rightarrow \Lambda \bar{p} \nu \bar{\nu}) < 3.0 \times 10^{-5}$

# $B \rightarrow X_s \gamma$



## Radiative B Decay ( $b \rightarrow s \gamma$ )

- Penguin diagram (FCNC process).
- Good agreement between theory and experiments.
  - ✓ Strong constraint to New Physics



$$B(B \rightarrow X_s \gamma; E_\gamma > 1.6 \text{ GeV})$$

$$= (3.32 \pm 0.15) \times 10^{-4} \text{ [HFLAV2018]}$$

$$= (3.36 \pm 0.23) \times 10^{-4} \text{ [Misiak 2015]†}$$

† Misiak et al, PRL 114, 221801, (2015)

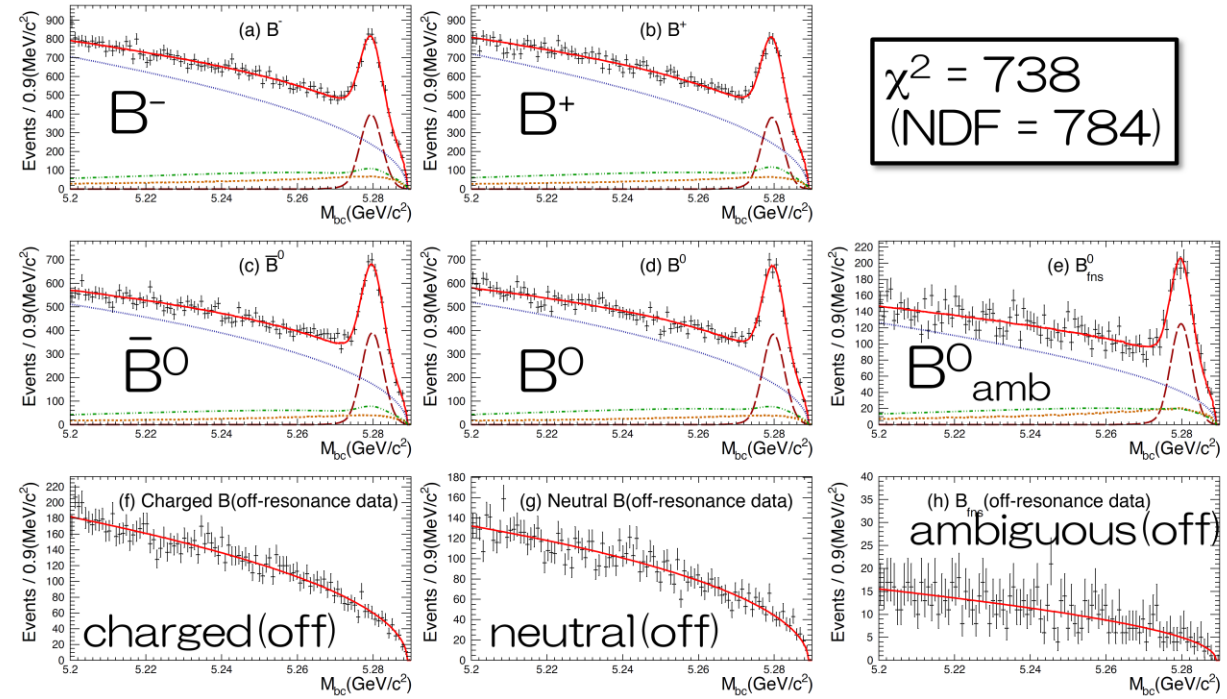
- $A_{CP}$  of  $B \rightarrow X_s \gamma$  is an interesting probe for NP, but has small ( $\sim 2\%$ ) theoretical uncertainty.
- $\Delta A_{CP}$  (difference of  $A_{CP}$  between charged and neutral B) is a cleaner probe.

$$\Delta A_{CP}(B \rightarrow X_s \gamma) \equiv A_{CP}(B^+ \rightarrow X_s^+ \gamma) - A_{CP}(B^0 \rightarrow X_s^0 \gamma)$$

# $B \rightarrow X_s \gamma$

[BELLE-CONF-1801, arXiv:1807.04236]

- Sum of 38  $X_s$  modes with  $M(X_s) < 2.8$  GeV.
  - ✓ 11 of them are flavour non specific modes.
- 8  $M_{bc}$  distributions (including 3 from off-resonance) are simultaneously fitted.



$$\Delta_{0-} = (+1.70 \pm 1.39 \pm 0.87 \pm 1.15)\%$$

$$\Delta A_{CP} = (+1.26 \pm 2.40 \pm 0.67)\%$$

Constraint NP :  $\Delta A_{CP} \approx 4\pi^2 \alpha_s \frac{\tilde{\Lambda}_{78}}{m_b} \text{Im} \left( \frac{C_8}{C_7} \right)$

→ reduce uncertainty for B.F.





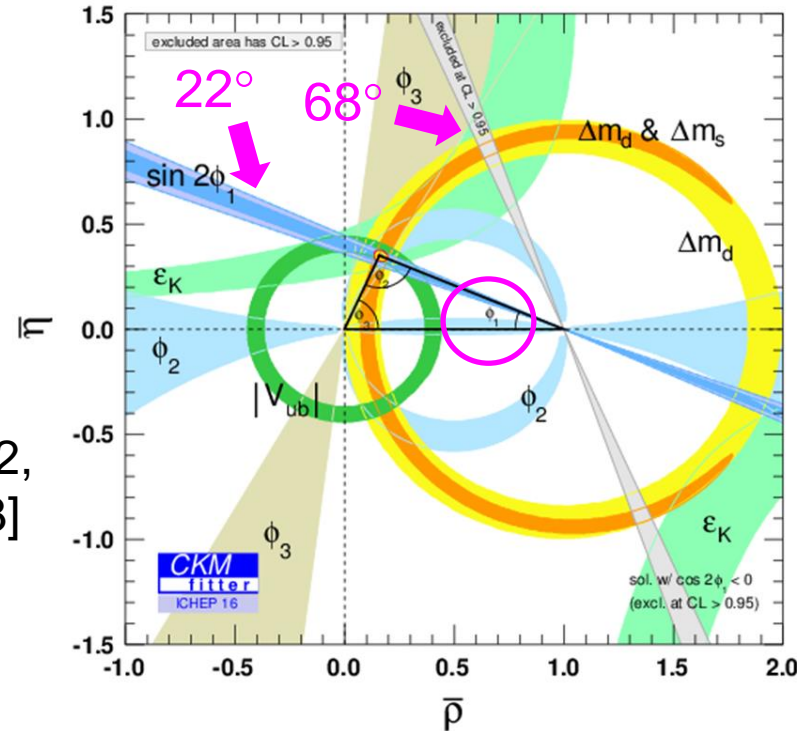
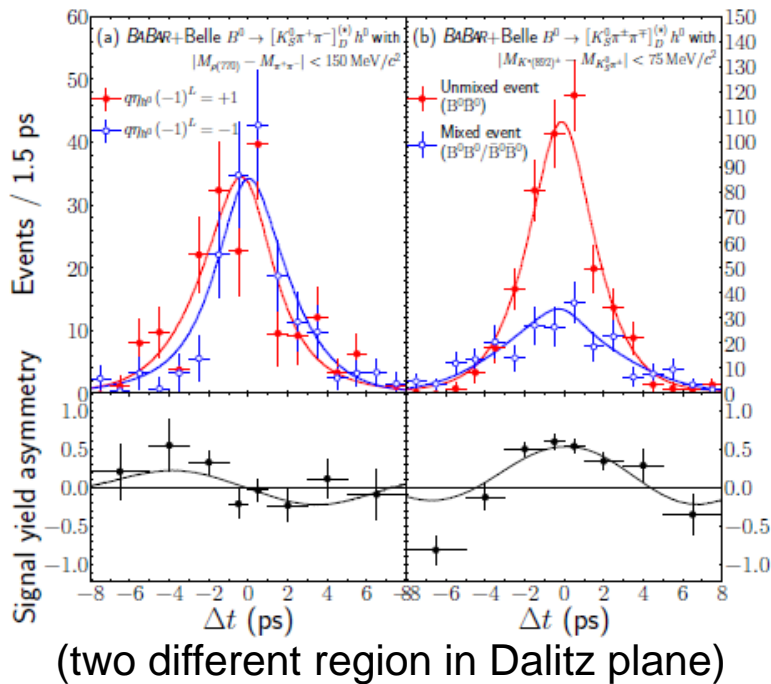
# cos(2β) in B → D(\*)h<sup>0</sup>



- sin2β is precisely measured, but trigonometric ambiguity exists for β.
- Time-dependent Dalitz analysis of B → D(\*)h<sup>0</sup>, D → K<sub>S</sub>π<sup>+</sup>π<sup>-</sup> (h = π<sup>0</sup>, η, ω) can resolve it.
- Joint Babar + Belle analysis. ✓ 471 + 772 M B $\bar{B}$



[arXiv:1804.06152, arXiv:1804.06153]



$$\sin(2\beta) = 0.80 \pm 0.14 \text{ (stat.)} \pm 0.06 \text{ (syst.)} \pm 0.03 \text{ (model)}$$

$$\cos(2\beta) = 0.91 \pm 0.22 \text{ (stat.)} \pm 0.09 \text{ (syst.)} \pm 0.07 \text{ (model)}$$

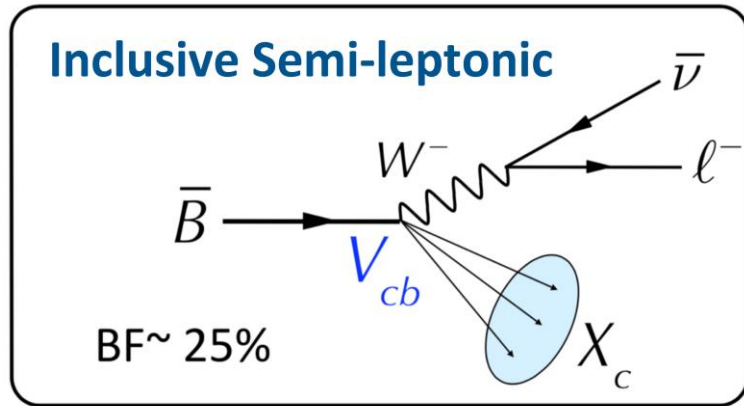
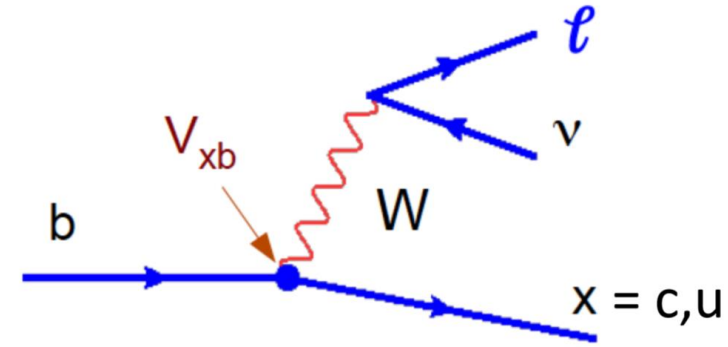
$$\beta = (22.5 \pm 4.4 \text{ (stat.)} \pm 1.2 \text{ (syst.)} \pm 0.6 \text{ (model)})^{\circ}$$

- First evidence of cos2β > 0.

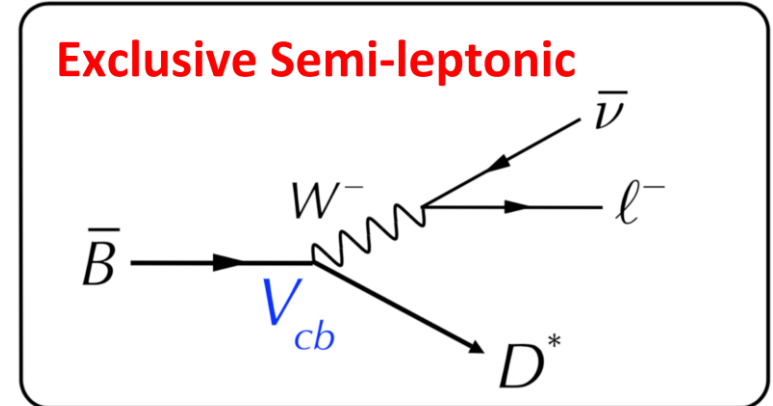
Talk by B.Pal (WG4)

# $|V_{ub}|$ and $|V_{cb}|$

- $|V_{ub}|$  and  $|V_{cb}|$  measurements are done using semi-leptonic decays  $b \rightarrow u\bar{\nu}, c\bar{\nu}$ .
- Two approaches: **inclusive** and **exclusive**



do not specify hadron state



specify hadrons (experimentally clean)

- QCD corrections to parton level decay rate
- Operator Product Expansion (OPE) in  $\alpha_s$  and  $\Lambda/m_b$

- QCD contributions parametrized in form factors
- Lattice QCD (high  $q^2$ ) or LCSR (low  $q^2$ )

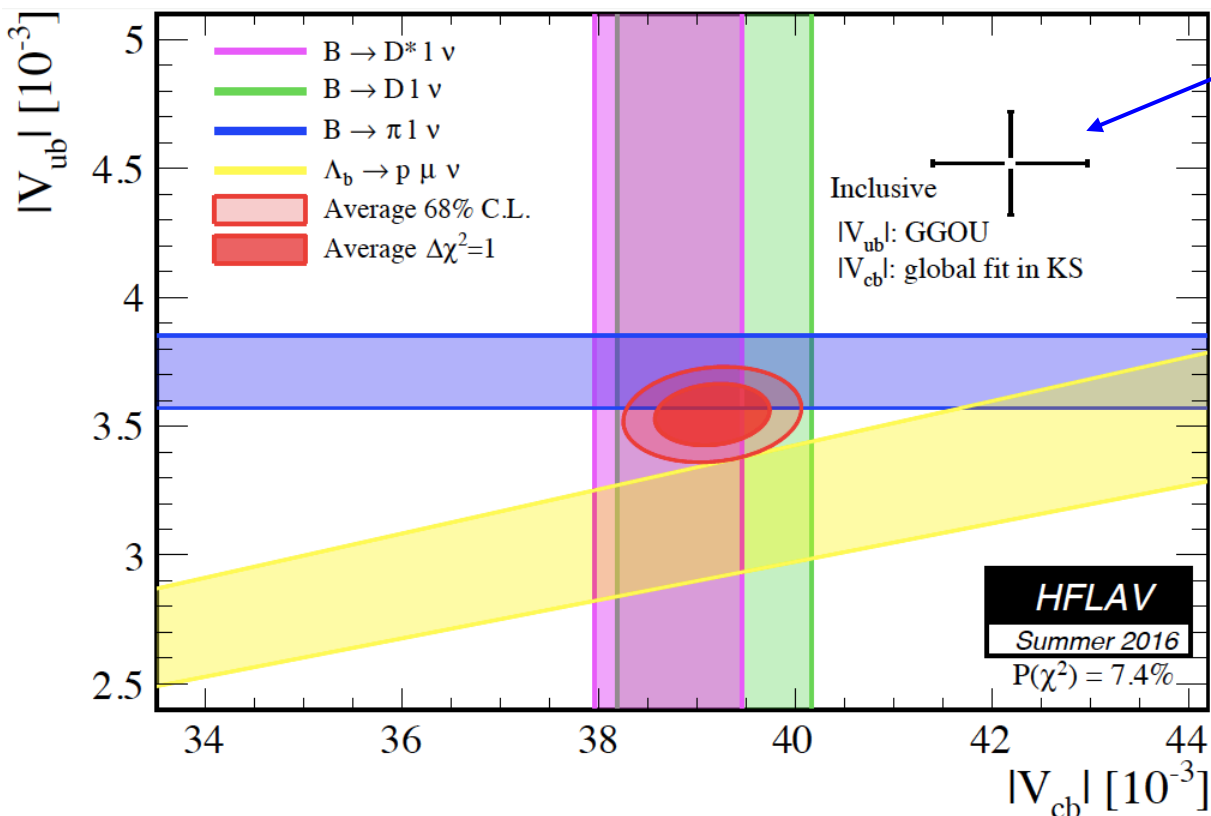


# $|V_{ub}|$ and $|V_{cb}|$



Discrepancy between **inclusive** and **exclusive**

exclusive measurements



average for inclusive

$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.2 \pm 0.7) \times 10^{-3} \quad (\text{exclusive})$$

$$|V_{ub}| = (4.49 \pm 0.16 \begin{smallmatrix} +0.16 \\ -0.18 \end{smallmatrix}) \times 10^{-3} \quad (\text{inclusive})$$

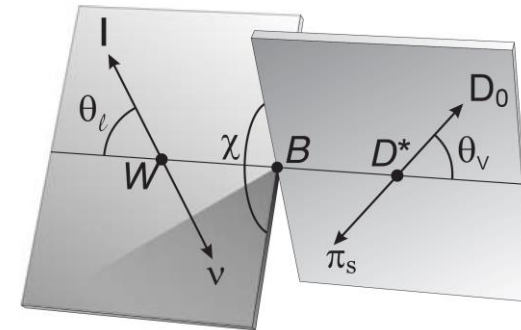
$$|V_{ub}| = (3.72 \pm 0.19) \times 10^{-3} \quad (\text{exclusive})$$

# Untagged $B \rightarrow D^* \ell \nu$



- New result of untagged analysis of  $B \rightarrow D^* \ell \nu$  was presented at ICHEP.
- Simultaneous fit to  $\cos\theta_\ell$ ,  $\cos\theta_\nu$ ,  $\chi$ ,  $w$  (hadronic recoil) to extract form factors and  $F(1) |V_{cb}|$ .
- Two form factor parametrization, CLN [NPB530, 153 (1998)] and BGL [PRL74, 463 (1995)] are used.
  - ✓ CLN was mainly used in previous measurements.

[BELLE-CONF-1803, arXiv:1809.03290]

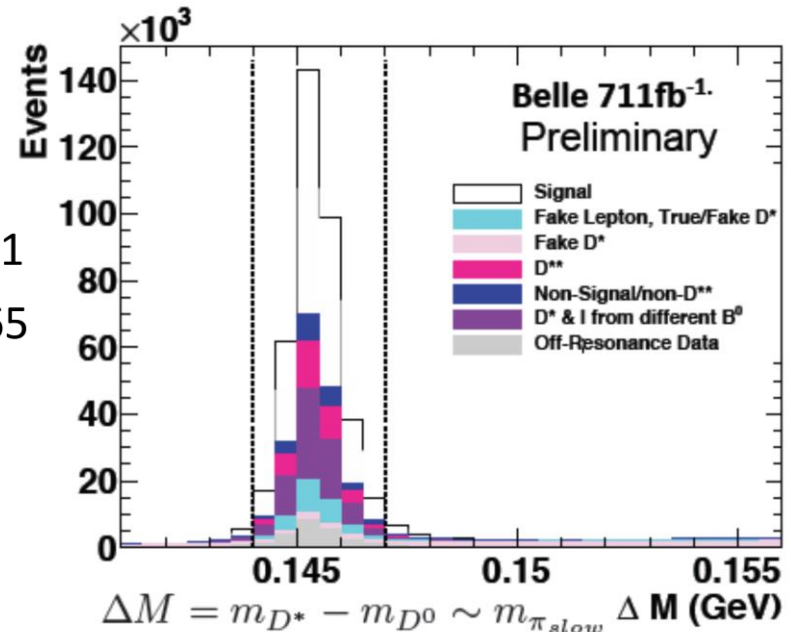


$$N(B \rightarrow D^* e \nu) = 91381$$

$$N(B \rightarrow D^* \mu \nu) = 89965$$

## Bonus: Lepton Flavor Universality test

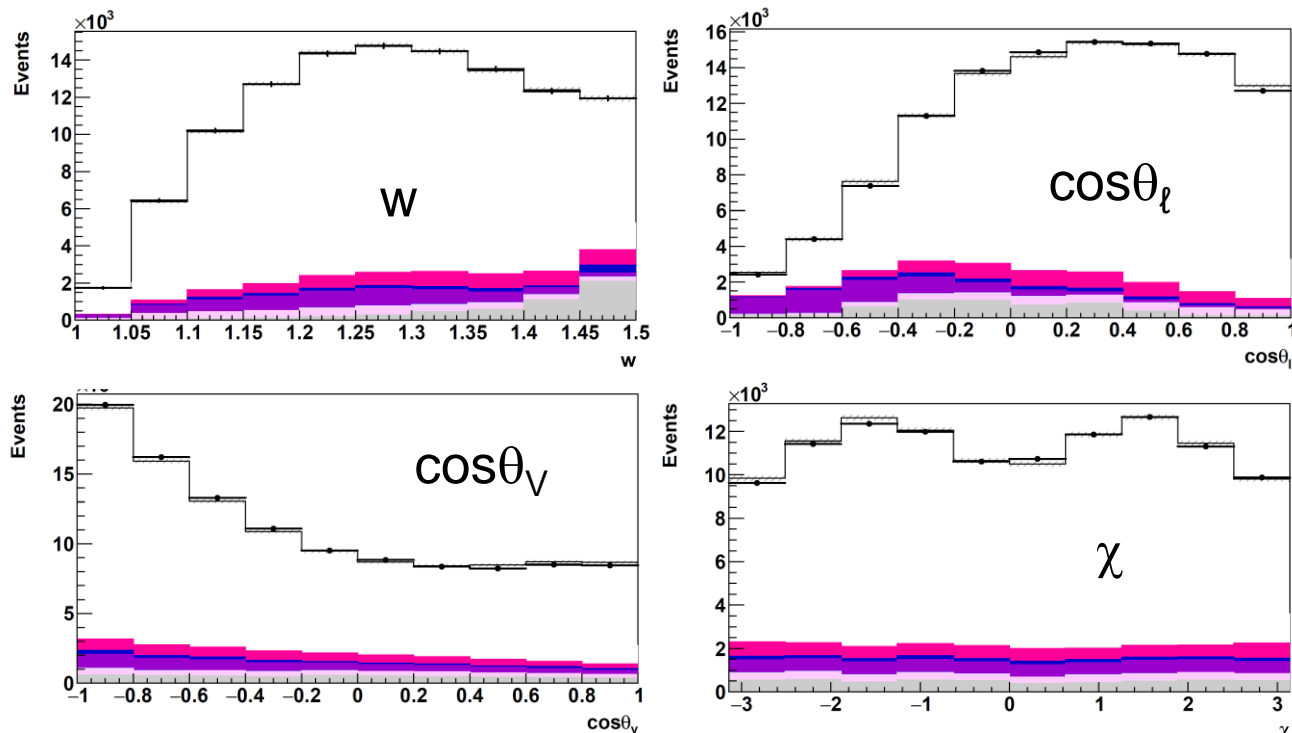
$$\frac{\mathcal{B}(B^0 \rightarrow D^{*-} e^+ \nu)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu)} = 1.01 \pm 0.01 \pm 0.03$$



# Untagged $B \rightarrow D^* \ell \nu$



Fit for BGL parametrizations for  $B \rightarrow D^* \mu \nu$



Talk by K. Lieret (WG2)  
and C. Schwanda (WG2)

world average

$$|V_{cb}| = (42.2 \pm 0.8) \times 10^{-3} \quad (\text{inclusive})$$

$$|V_{cb}| = (39.2 \pm 0.7) \times 10^{-3} \quad (\text{exclusive})$$

CLN:  $|V_{cb}| = (38.4 \pm 0.2 \pm 0.6 \pm 0.6) \times 10^{-3}$

BGL:  $|V_{cb}| = (42.5 \pm 0.3 \pm 0.7 \pm 0.6) \times 10^{-3}$





some hint of inclusive/exclusive discrepancy?

consistent with  
previous (exclusive)  
results

consistent with  
inclusive result

# More Results, Talks



- $B \rightarrow \mu\nu$  (untagged) [PRL 121, 031801 (2018)]  Talk by A. Sibidanov (WG2)
- $B \rightarrow \ell\nu\gamma$  (hadronic tag with Full Event Interpretation)  **New Result** Talk by M. Gelb (WG2)
- CPV of  $B \rightarrow J/\psi\pi^0$ ,  $B \rightarrow K_S\pi^0\pi^0$   Talk by B.Pal (WG4)
- Inclusive  $B \rightarrow X_u\ell\nu$  (electron energy endpoint) [PRD 95, 072001 (2017)] 
- Charmless B decays,  $\gamma(=\phi_3)$ , .....

and

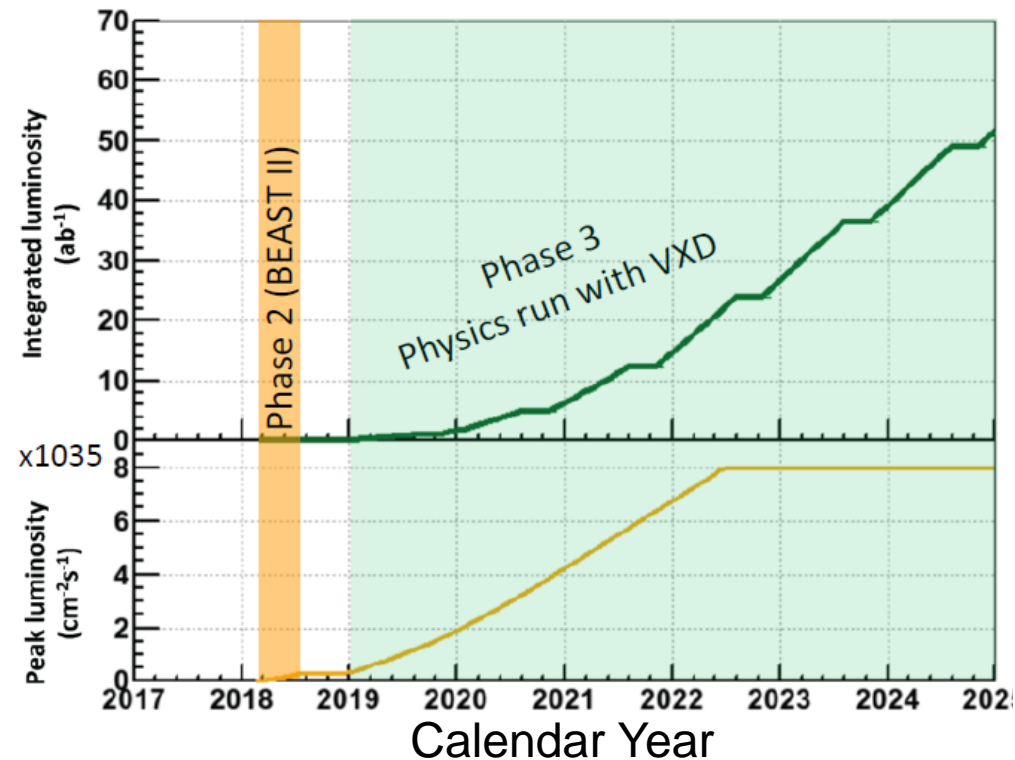
- Prospects for Belle II



# Summary



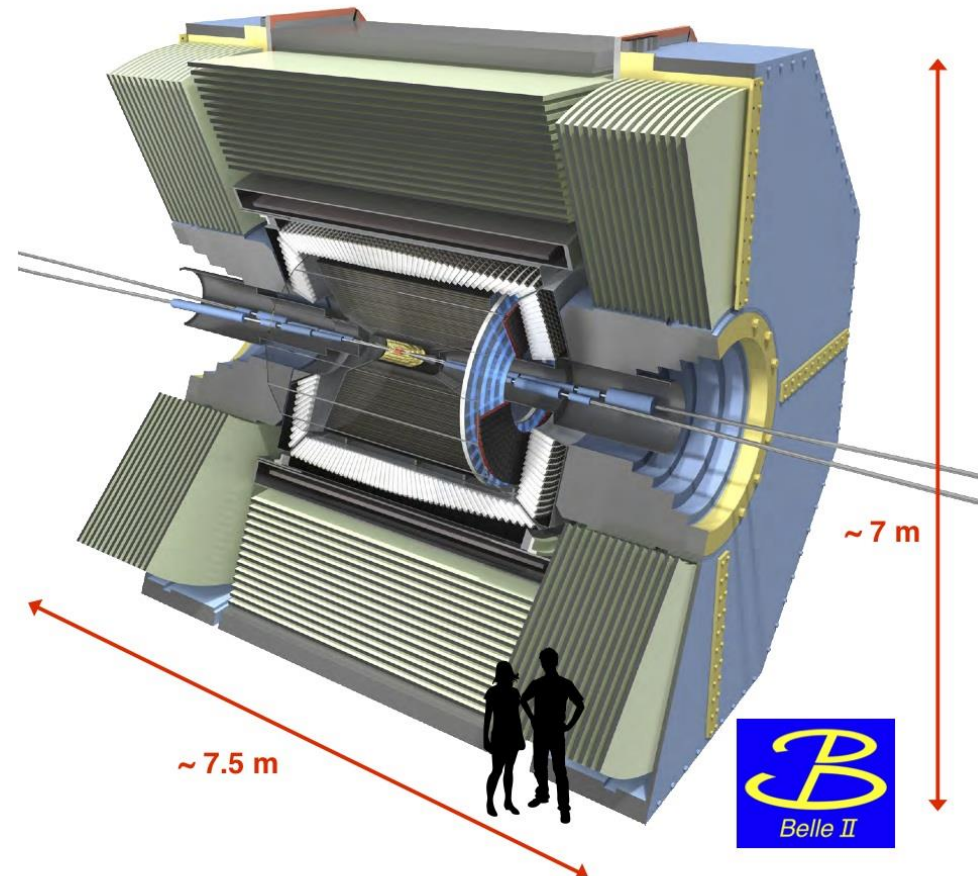
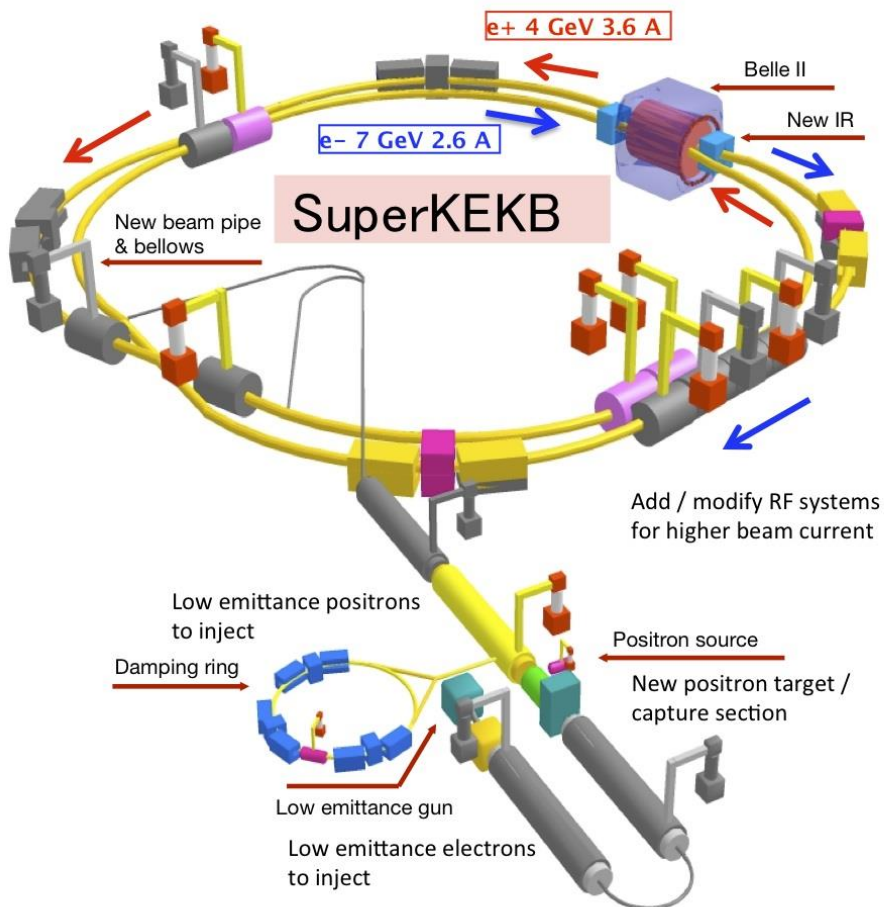
- Belle II started. Phase 2 operation completed this year.
  - ✓ First collision.
  - ✓ Accelerator study, but some physics data are taken.
  - ✓ B mesons are reconstructed.
- New results from BaBar and Belle.
  - ✓  $D^*$  polarization in  $B \rightarrow D^* \tau \nu$ .
  - ✓  $\cos(2\beta)$  in  $B \rightarrow D^{(*)} h^0$
  - ✓  $|V_{cb}|$  from  $B \rightarrow D^* \ell \nu$
  - ✓ .....
- Belle II Phase 3 (physics run) starts next year, and we expect first physics results soon. Stay tuned.





# Backup

# SuperKEKB and Belle II



# SuperKEKB Parameter



parameters		KEKB		SuperKEKB		units
		LER	HER	LER	HER	
Beam energy	$E_b$	3.5	8	4	7	GeV
Half crossing angle	$\phi$	11		41.5		mrad
Horizontal emittance	$\epsilon_x$	18	24	3.2	5.0	nm
Emittance ratio	$\kappa$	0.88	0.66	0.27	0.25	%
Beta functions at IP	$\beta_x^*/\beta_y^*$	1200/5.9		32/0.27	25/0.31	mm
Beam currents	$I_b$	1.64	1.19	3.60	2.60	A
beam-beam parameter	$\xi_y$	0.129	0.090	0.0886	0.0830	
<b>Luminosity</b>	<b>L</b>	<b><math>2.1 \times 10^{34}</math></b>		<b><math>8 \times 10^{35}</math></b>		<b><math>\text{cm}^{-2}\text{s}^{-1}</math></b>

- **Small beam size & high current** to increase luminosity
- **Large crossing angle**
- **Change beam energies** to solve the problem of LER short lifetime

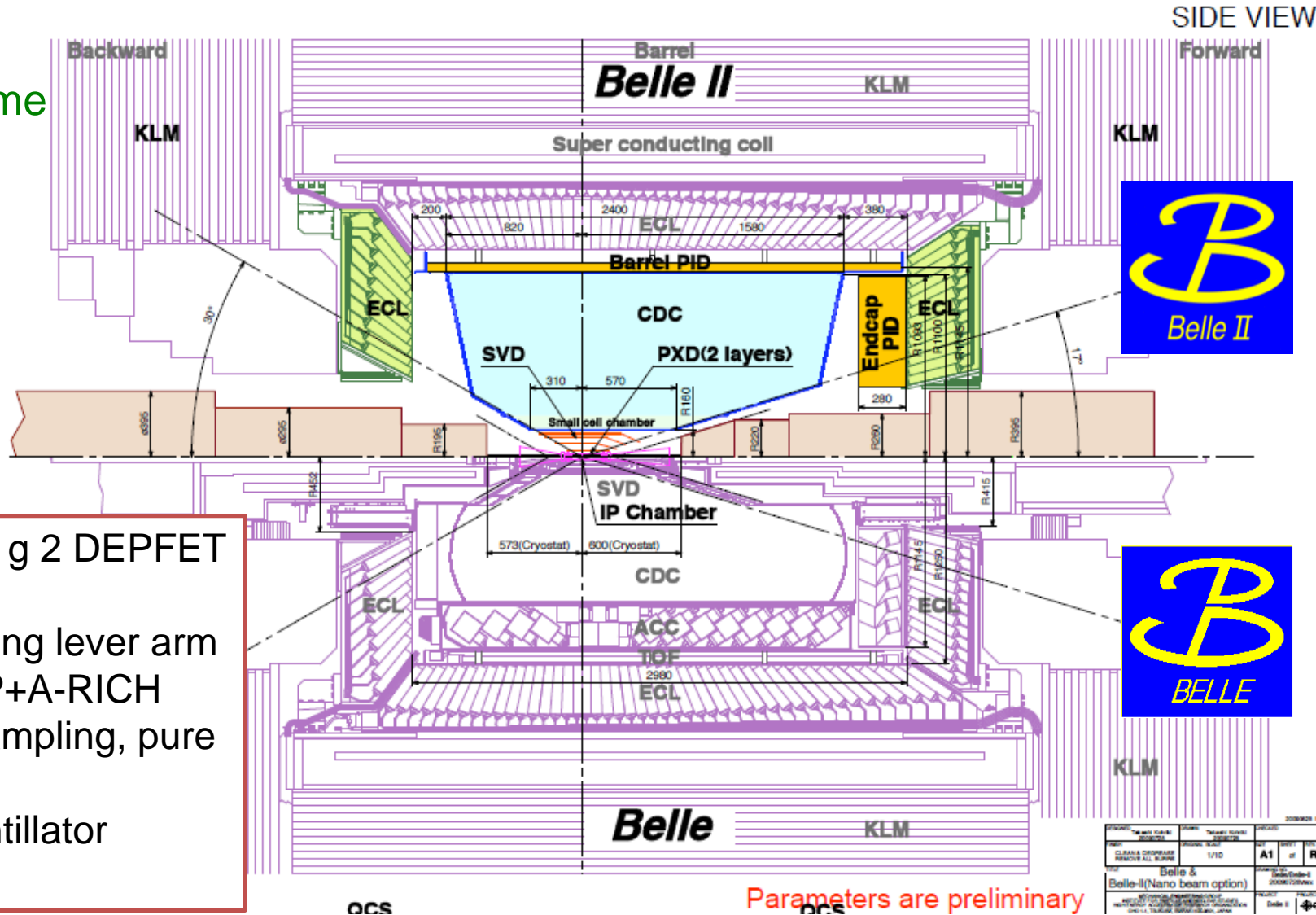


# From Belle to Belle 2



## Belle II

- At least, the same performance as Belle in higher luminosity.
- Better performance if important for physics



SVD: 4 DSSD lyrs g 2 DEPFET lyrs + 4 DSSD lyrs  
 CDC: small cell, long lever arm  
 ACC+TOF → TOP+A-RICH  
 ECL: waveform sampling, pure CsI for end-caps  
 KLM: RPC → Scintillator +SiPM (end-caps)

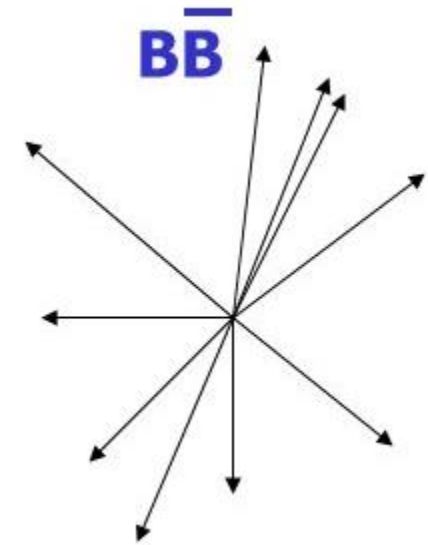
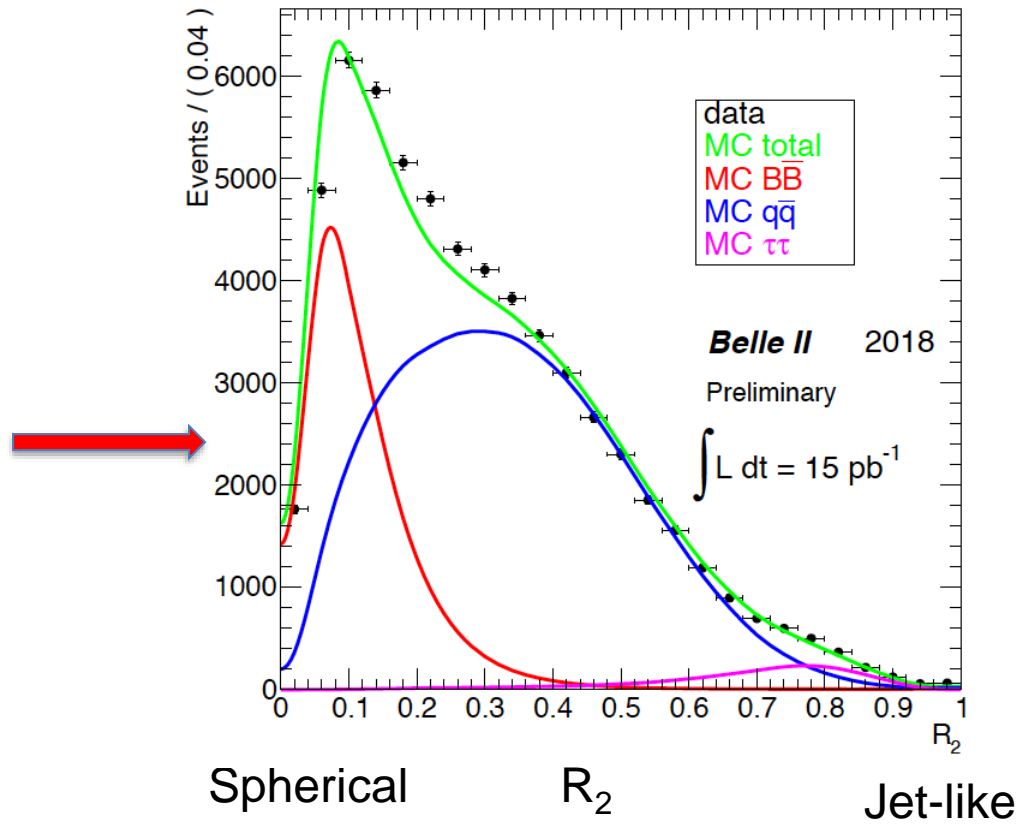
Parameters are preliminary

NO.	REVISION	DATE	BY	CHKD	APPD	REASON
1	1/10		A1			

Belle & Belle-II(Nano beam option)

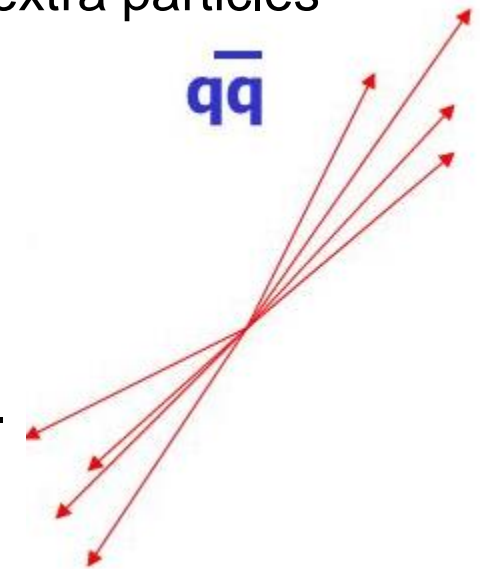


# Event Topology tells us we are seeing B's



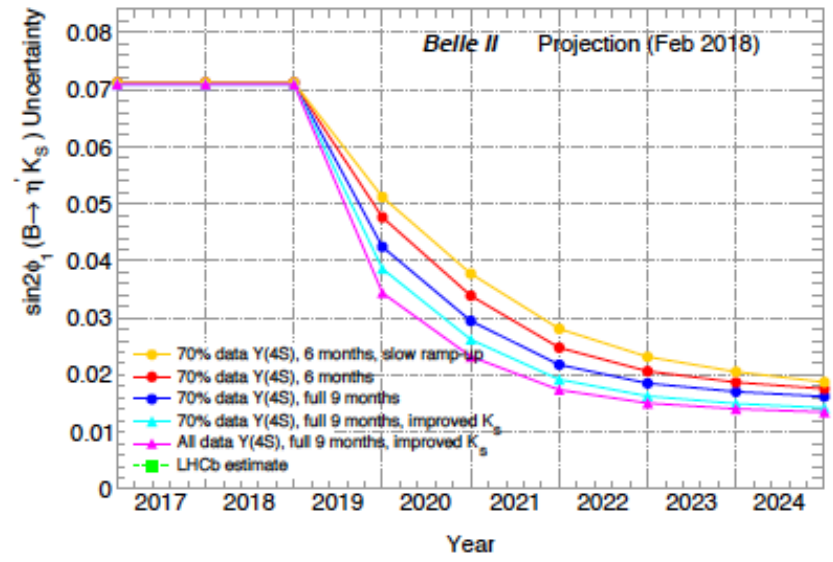
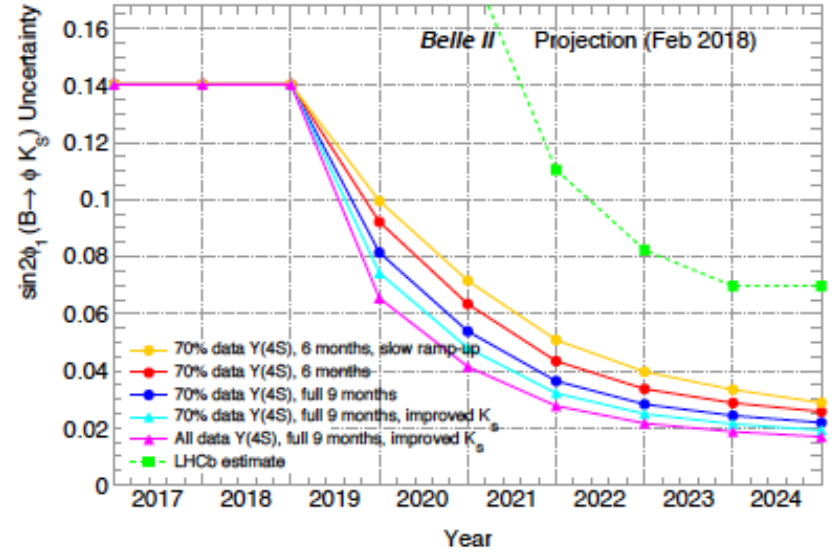
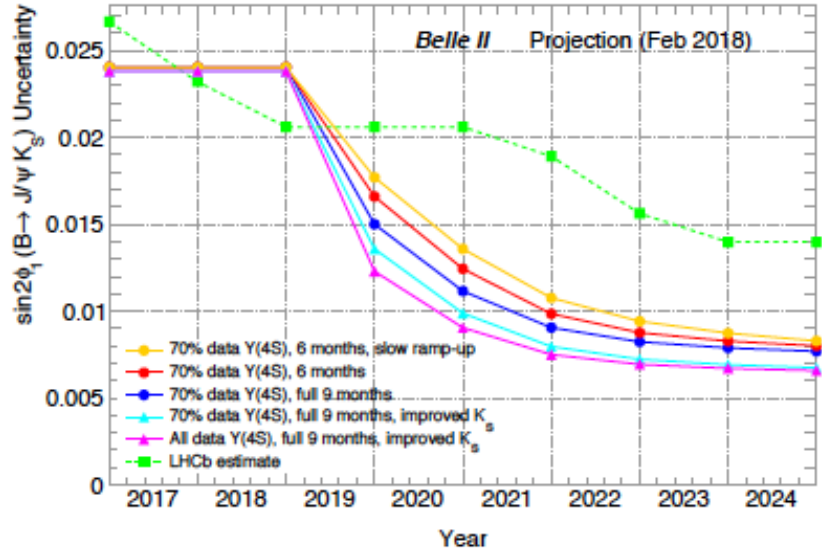
B pairs produced at rest in the CM with no extra particles

$q\bar{q}$



We are on the  $Y(4S)$  resonance and recording B anti-B pairs with  $\sim 99\%$  efficiency.

# Examples of Physics Competition and Complementarity



Use publicly available LHCb projections.



# Angular Analysis of $B \rightarrow K^* \ell^+ \ell^-$



Angular distribution in  $B \rightarrow K^* \ell^+ \ell^-$  ( $K^* \rightarrow K\pi$ )

$$q^2 = M(\ell^+ \ell^-)^2$$

$$\frac{1}{d\Gamma/dq^2 d \cos \theta_\ell d \cos \theta_K d\phi dq^2} d^4\Gamma$$

$$= \frac{9}{32\pi} \left[ \frac{3}{4} (1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right.$$

$$+ \frac{1}{4} (1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell$$

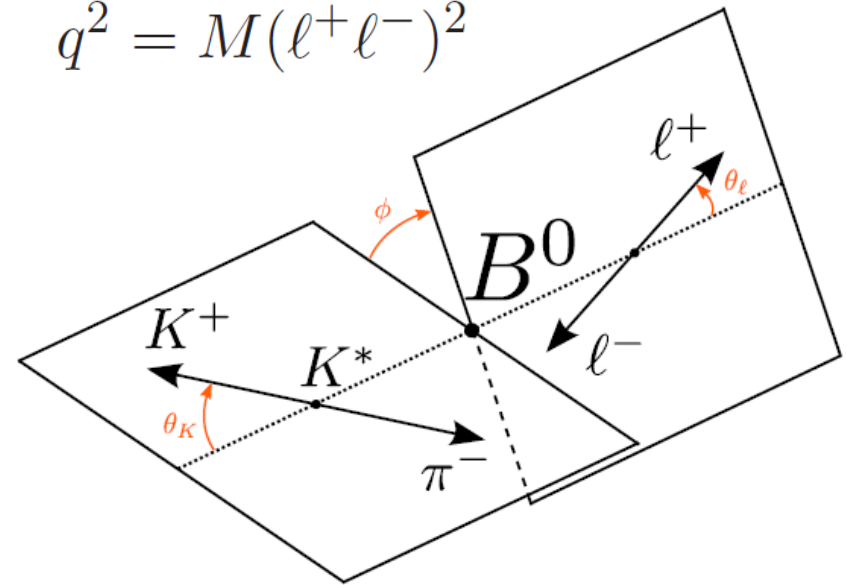
$$- F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi$$

$$+ S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi$$

$$+ S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$$

$$\left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

- 8 variables:  $F_L$  (longitudinal polarization of  $K^*$ )  
and  $S_j$  ( $j=3,4,5,6,7,8,9$ )  
✓ function of  $q^2$



$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$