

**FOKKER-VFW B.V.**

NETHERLANDS AIRCRAFT FACTORIES FOKKER-VFW B.V.

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SUBJECT **Static Directional Stability and Control of Transport Aircraft**

SAMENVATTING  
SUMMARY

An analysis is described of side-force and yawing-moment-in-sideslip of conventional transport aircraft based on available wind tunnel and full-size aircraft data. After a chapter on general design requirements the analysis is divided in a part which describes the tail-off characteristics and a part which describes the contribution of the tail surfaces to side-force and yawing-moment-due-to- sideslip. Particular attention is paid to the different contributions to the sidewash as experienced by the tail surfaces. Also rudder characteristics are discussed.

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## Notation

$A$	Aspect ratio
$A_H$	Horizontal tailplane aspect ratio $b_H^2 / S_H$
$A_V$	Vertical tailplane aspect ratio $b_V^2 / S_V$
$A_W$	Wing aspect ratio $b_W^2 / S_W$
$b_{FL}, b_{fl}$	Wing flap span
$b_H$	Horizontal tailplane span
$b_V$	Vertical tailplane span ( see page I-19 )
$b_W$	Wing span
$C$	Cross force perpendicular to the X-Z plane, positive to the left.
$C_C (= -C_Y)$	Cross force coefficient $C / qS_W$
$c_H$	Horizontal tailplane chord
$C_{L_W}$	Wing ( or tail-off ) lift coefficient $L / qS_W$
$C_{L_{T-O}}, (C_L)_{T-O}$	Tail-off lift coefficient
$c_{l_\alpha}$	2-dimensional lift gradient due to angle-of-attack
$c_{l_\delta}$	2-dimensional lift gradient due to control surface deflection
$C_{l_\beta}$	Rolling-moment-due-to-sideslip derivative
$(C_{l_\beta})_{T-O}$	Tail-off rolling-moment-due-to-sideslip derivative
$(C_{l_\beta})_T$	Contribution to rolling-moment-due-to-sideslip derivative due to wing dihedral
$C_{L\alpha}$	Lift-due-to-angle-of-attack gradient ( Lift curve slope )
$C_{L\alpha_V}$	Vertical tailplane lift-due-to-angle-of-attack gradient ( Also $(C_{L\beta})_V$ )
$C_{L\alpha_{est}}$	Estimated <u>isolated</u> vertical tailplane lift-due-to-angle-of-attack gradient

$C_{L\alpha_{V+H}}$ , $C_{L\alpha_T}$	Vertical tailplane (including horizontal tailplane endplate effect ) lift-due-to-angle-of-attack gradient. ( Also $(C_{L\beta})_{V+H}$ ,)
$C_{L\alpha_{V+Hest}}$	Estimated <u>isolated</u> vertical tailplane (including horizontal tailplane endplate effect ) lift-due-to-angle-of-attack gradient
$C_{L\delta_r}$	Vertical tailplane (including horizontal tailplane endplate effect ) lift-due-to-rudder-deflection gradient
$C_{L\beta}$	Rolling moment coefficient due to sideslip
$(C_{L\beta})_{V+H}$	See $C_{L\alpha_{V+H}}$
$C_l$	Rolling moment coefficient $\mathcal{L} / qS_w b$
$(C_l)_{T-O}$	Tail-off rolling moment coefficient due to sideslip.
$C_n$	Yawing moment coefficient $N / qS_w b$
$C_{n_{30}}$	Yawing moment coefficient with moment reference centre at $x = 0.30\overline{c_w}$ .
$(\Delta C_{n_{30}})_{V+H}$	Tail contribution to yawing moment coefficient with moment reference centre at $x = 0.30\overline{c_w}$ .
$C_{n_\beta}$	Yawing-moment-due-to-sideslip derivative
$(\Delta C_{n_\beta})_{FL}$	Contribution to yawing-moment-due-to-sideslip derivative due to flap deflection
$(C_{n_\beta})_{tail-off}$	Tail-off yawing-moment-due-to-sideslip derivative ( Also $(C_{n_\beta})_{T-O}$ and $(C_{n_\beta})_{WT}$ or $(C_{n_\beta})_{WFN}$ .)
$(\Delta C_{n_\beta})_T$ , $(\Delta C_{n_\beta})_{V+H}$	Tail contribution to yawing-moment-due-to-sideslip derivative (Also $(C_{n_\beta})_T$ )
$C_{n_{\delta_r}}$	Yawing-moment-due-to-rudder-deflection derivative
$c_r$	Rudder chord
$c_{R_V}$	Vertical tailplane root chord
$c_{R_V \text{ exposed}}$	Exposed vertical tailplane root chord ( see page I-53 )

$c_V$	Vertical tailplane chord
$\overline{c_V}$	Vertical tailplane mean aerodynamic chord.
$\overline{c_W}, \overline{c_{ref}}$	Wing mean aerodynamic chord.
$C_Y$	Side force coefficient $Y / qS_W$
$C_{Y\beta}$	Side-force-due-to-sideslip derivative
$(\Delta C_{y\beta})_{est}$	Estimated tail contribution to side-force-due-to-sideslip derivative ( See pages II-1 to II- 65 )
$(C_{y\beta})_{tail-off}$	Tail-off side-force-due-to-sideslip derivative ( Also $(C_{y\beta})_{T-O}$ and $(C_{y\beta})_{WF}$ or $(C_{y\beta})_{WFN}$ ).
$(\Delta C_{y\beta})_{FL}$	Contribution to side-force derivative due to flap deflection
$(\Delta C_{y\beta})_{nac}$	Contribution to side-force derivative due to engine nacelles
$(\Delta C_{y\beta})_T, (\Delta C_{y\beta})_{V+H}$	Tail contribution to side-force-due-to-sideslip derivative (Also $(C_{y\beta})_T$ or $(\Delta C_{y\beta})_{VH}$ ).
$(\Delta C_{y\beta})_\Gamma$	Contribution to side-force-due-to-sideslip derivative due to wing dihedral.
$C_{Y\delta_r}$	Side-force-due-to-rudder-deflection derivative
$(C_{y\delta_r})_{S_V}$	Side-force-due-to-rudder-deflection derivative for a full-vertical-tailplane-span rudder derived from side-force data, $Y_{\delta_r} / q \frac{S_V}{S_W} S_W$
$(C_{y\delta_r}^*)_{S_V}$	Side-force-due-to-rudder-deflection derivative for a full-vertical-tailplane-span rudder derived from yawing moment data, $N_{\delta_r} / q \frac{S_V}{S_W} \frac{l_{VR+(DF)}}{b_W} S_W b_w$
$D_{f_{max}}, D_{fus}, d$	Maximum fuselage diameter
$d_V, D_V$	Fuselage height as defined on page I-19

$\frac{d\sigma}{d\beta}$	Sidewash-angle-to-sideslip-angle ratio
E	Rudder-chord-to-fin-chord ratio $c_r / c_v$
$h_w, \Delta h_w$	Wing root height relative to fuselage centre line. Positive when wing is above the fuselage centre line.
$i_h$	Horizontal tailplane angle-of-incidence.
$i_v$	Vertical tailplane angle-of-incidence
$K_i$	Empirical factor defined on page I-15
$K_N$	Empirical factor defined on page I-16
$K_{FV}$	Fuselage-vertical-tailplane lift carry-over effect
$K_{VH}$	Horizontal-to-vertical tailplane endplate effect
$K_{VH_{est}}$	Estimated horizontal-to-vertical tailplane endplate effect
L	Lift
$l_B$	Fuselage length ( see page I-16 )
$l_V, l_{V_{30}}, l_V^*$	Vertical tailplane yawing moment arm measured from $x = 0.30\overline{c_w}$ . or $x = 0.25\overline{c_w}$ .
$l_{V+dfn}^*$	Effective vertical tailplane yawing moment arm including dorsal fin n. ( n=2,3,4,5 ) For Fokker models measured from $x = 0.30\overline{c_w}$ . (Also $l_{V+DF}$ )
$l_{V_{ref}}$	Vertical tailplane moment arm related to reference (=exposed) vertical tailplane area
£	Rolling moment
N	Yawing moment
$n_{nac}$	Number of engine nacelles
q	Free-stream dynamic pressure $q = \frac{1}{2}\rho V^2$
$q_V$	Average dynamic pressure at the vertical tailplane

$R_{TL}$	Tail moment arm ratio ( Tail length ratio) $R_{TL} = \left( \Delta C_{n_p} \right)_T / - \left( \Delta C_{y_p} \right)_T * \frac{l_V}{b_W}$
$S_{Bs}$	Body side area ( see page I-16 )
$S_{dfn}$	Area of dorsal fin $n$ ( $n = 2, 3, 4, 5$ ) ( Also $S_{DF}$ )
$S_{fus.cross}$	Maximum fuselage cross section.
$S_H$	Horizontal tailplane area
$S_V$	Vertical tailplane area ( see page I-19 )
$S_{V_r}$	Part of vertical tailplane area affected by the rudder ( see page I-19 ).
$S_{V_{ref}}$	Reference (=exposed) vertical tailplane area
$S_W$	Wing area
$S_{W_{ref}}$	Reference wing area
$S_{W_{trap}}$	Wing area of trapezoidal wing
$V$	Free stream velocity
$\overline{V}_{V_{30}}$	Vertical tailplane volume coefficient with moment centre at $x = 0.30 \overline{c}_W$ .
$\overline{y}^*$	Spanwise position of the centroid of span loading as a fraction of the semispan.
$x$	Distance along fuselage centre line from fuselage nose
$x_{ac_V}$	Distance from fuselage nose of vertical tailplane aerodynamic centre including dorsal fin.
$x_{exh}$	Longitudinal position of engine exhausts ( see page I-53 )
$x_{R_V}$	0% $x_{R_V}$ = longitudinal position of vertical tailplane root chord
$Y$	Side force perpendicular to the X-Z plane, positive to the right.
$z_{CL_{nac}}$	Vertical position of engine-nacelle centre line
$z_H$	Vertical position of the horizontal tailplane ( see page I-19 )

$z_w (= -h_w)$	Wing root height relative to fuselage centre line. Positive when wing is below the fuselage centre line ( see page I-15 ).
$\alpha, \alpha_R$	aircraft angle-of-attack
$\alpha_h$	Horizontal tailplane angle-of-attack
$\alpha_h^*$	Horizontal tailplane zero-lift angle-of-attack relative to tailplane reference plane
$\alpha_v$	Effective vertical tailplane angle-of-attack
$\frac{\Delta\alpha_0}{\Delta\delta}$	2-dimensional control surface effectiveness $\frac{c_{l_\delta}}{c_{l_{\alpha_0}}}$ ( see page I-116 )
$\beta$	Sideslip angle
$\Gamma_w$	Wing dihedral angle
$\delta_f$	Flap angle
$\delta_s$	Slat angle
$\delta\sigma / \delta\beta, \frac{\delta\sigma}{\delta\beta}, \frac{d\sigma}{d\beta}$	Sidewash-angle-to-sideslip-angle ratio
$\left(\frac{\delta\sigma}{\delta\beta}\right)_{FV}$	Fuselage-vertical-tailplane interference factor
$\left(\Delta\frac{\delta\sigma}{\delta\beta}\right)_{h_w}$	Effect of relative wing height on the fuselage on the sidewash-angle-to-sideslip-angle ratio
$\left(\Delta\frac{\delta\sigma}{\delta\beta}\right)_\Gamma$	Effect of wing dihedral on the sidewash-angle-to-sideslip-angle ratio
$\left(\Delta\frac{\delta\sigma}{\delta\beta}\right)_{FL}$	Effect of wing flap deflection on the sidewash-angle-to-sideslip-angle ratio.
$\left(\Delta\frac{\delta\sigma}{\delta\beta}\right)_{FL,ldg}$	Effect of wing flap deflection to the landing position on the sidewash-angle-to-sideslip-angle ratio.



$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{CI\beta}$	Effect of rolling moment due to sideslip on the sidewash-angle-to-sideslip-angle ratio.
	the sidewash-angle-to-sideslip-angle ratio
$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{NF}$	Effect of rear-fuselage engine nacelles on the sidewash-angle-to-sideslip-angle ratio
$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{NW}$	Effect of engine-nacelles-on-the-wing on the sidewash-angle-to-sideslip-angle ratio
$\varepsilon$	Downwash angle
$\lambda$	Taper ratio
$\lambda_H$	Horizontal tailplane taper ratio
$\lambda_V$	Vertical tailplane taper ratio
$\lambda_W$	Wing taper ratio
$\Lambda_{\frac{1}{4}c_H}$	Horizontal tailplane quarter-chord sweep angle
$\Lambda_{\frac{1}{4}c_V}$	Vertical tailplane quarter-chord sweep angle
$\Lambda_{\frac{1}{4}c_W}$	Wing quarter-chord sweep angle
$\rho$	air density
$\sigma$	Sidewash angle

#### Model or aircraft components

W, V	wing
F, R	fuselage
N <sub>f</sub> , G	engine nacelles on the rear fuselage
N <sub>w</sub> ,	engine nacelles on the wing
V	vertical tailplane
H	horizontal tailplane
DR	dorsal fin

All dimensions are measured in m, in, m<sup>2</sup> or in<sup>2</sup>.

Unless otherwise indicated all angles are measured in degrees ( deg ).

# Static Directional Stability and Control of Jet Transport Aircraft

## Introduction

Static directional stability and control of transport aircraft is primarily determined by the forward fuselage and the vertical tailplane or fin and the rudder with some secondary effects due to the wing and wing-fuselage interference.

For preliminary design purposes the contribution of the forward fuselage can be determined with the standard design manual methods. However, these manuals do not consider the effect of angle-of-attack or high-lift devices on tail-off side force or yawing moment. This effect is addressed in the present report.

Determining the characteristics of the vertical tail surface and rudder is a more complex process. This is due to the vertical tail being positioned in a flow field affected by all other major aircraft components. In a sideslip the fuselage, wing, engine nacelles and even the horizontal tailplane create all different, often non-linear, cross flows, also depending on their relative position. ( High - or low - wing, engine nacelles on the wing or on the rear – fuselage, high or low horizontal tailplane.) Furthermore modern transport aircraft have swept wings and highly efficient high-lift systems. This tends to produce large variations in the rolling-moment-due to-sideslip at varying angle-of-attack which in turn produces significant variations in cross flow at the tail.

Standard design manuals such as ESDU Data Sheets and the USAF Datcom and the textbooks derived from these sources consider only fuselage cross flow and the effect of the vertical position of the wing on the fuselage and of the wing dihedral on this cross flow , all at zero angle-of-attack.

In the present analysis the different contributions to the cross-flow or sidewash at the tail mentioned above and not covered by the design manuals are discussed in detail. As the analysis is entirely based on experimental data sometimes large variations in flow characteristics are noted on configurations with relatively small variations in geometry. Nevertheless an effort is made to present elementary guidelines for the preliminary design of vertical tail surfaces.

The data compilation in this report took place over the years 1978 – 2013. The text was finished in July 2013.

## Some general guidelines for the analysis of directional stability and control of transport aircraft.

With respect to fin and rudder sizing directional stability and control requirements for transport aircraft refer primarily to steady-state conditions. The two main conditions to be considered are:

Crosswind take-offs and landings with maximum crosswind.  
Maintaining directional control after an engine failure at low airspeeds.

As the information provided in the present report is primarily intended for preliminary design studies, the attention is focused on the low-speed regime.

Tail surfaces perform three functions :

1. They provide static and dynamic STABILITY.
2. They enable aircraft CONTROL.
3. They provide a STATE OF EQUILIBRIUM in each flight condition.

In general the following DESIGN REQUIREMENTS can be formulated for VERTICAL TAIL SURFACES:

1. They shall provide a sufficiently large contribution to static and dynamic directional STABILITY. This determines primarily their lift SLOPE,  $dC_{L_v} / d\alpha_v x S_V$ .
2. They shall provide sufficient CONTROL CAPABILITY  $dC_{L_v} / d\delta_r x S_V$  without flow separation up to high sideslip and rudder deflection angles.
3. Control shall be possible with sufficiently LOW CONTROL FORCES either for manual control or to minimize control system weight.

$$\text{Control Force } F = C_h x^{1/2} \rho v^2 S_c \bar{c}_c .$$

For a constant rudder area the HINGE MOMENT is MINIMISED when the factor

$$S_c \bar{c}_c \approx b_c \bar{c}_c^2 \text{ is minimized.}$$

For all three requirements a MAXIMUM ASPECT RATIO and for HIGH ASPECT RATIOS MINIMUM SWEEP is favourable.

4. The vertical tail surface shall be able to cope with HIGH TAILPLANE ANGLES - OF - ATTACK both with sideslip angle and rudder deflection with equal sign and with opposite sign. In this case a LOW ASPECT RATIO and applying SWEEP is beneficial.
5. The tail surface shall be able to provide a MAXIMUM FORCE sufficiently large to BALANCE the total tail-off forces and moments so that STATIC EQUILIBRIUM is achieved in all flight conditions. This leads to specific requirements on TAIL SURFACE AREAS and on the MAXIMUM LIFT COEFFICIENT of the vertical tail with a varying degree of rudder deflection including the effect of ice roughness.

The RUDDER performs three functions :

1. It provides a means to achieve a STEADY STATE OF EQUILIBRIUM ( TRIM ) either at zero or at non-zero control force.
2. It allows MANOEUVRING up to maximum yaw rates.

3. It provide a means to COUNTERACT DISTURBANCES, both small and large, such as gusts, which might otherwise cause the aircraft to deviate from its intended flight path ( flight path TRACKING ).

In order to obtain a MAXIMUM LIFT FORCE due to rudder deflection the use of a deep rudder may be tempting. However, the resulting maximum force and moment increases far from linearly with rudder depth for the larger rudder-to-fin chord ratio's.

Within the normal range of rudder-to-fin chord ratio's (  $c_R / c_V = 0.20$  to  $0.35$  ) the MAXIMUM SIDE FORCE DUE TO RUDDER DEFLECTION is FAIRLY INDEPENDENT OF FIN SHAPE AND RUDDER DEPTH.

The type of AERODYNAMIC BALANCE on the rudder has a LARGE EFFECT on the DEGREE OF LINEARITY of the variation of the hinge moment due to angle-of-attack and due to rudder deflection. (  $C_h = C_{H_0} + \frac{\delta C_h}{\delta \alpha_V} \alpha_V + \frac{\delta C_h}{\delta \delta_R} \delta_R$  seldom applies at large angles.)

HORN BALANCES and DORSAL FINS IMPROVE LINEARITY OF HINGE MOMENTS. LONG SPAN OVERHANG BALANCES have an ADVERSE EFFECT on this linearity.

LINEARITY of hinge moments is particularly important for RUDDERS because in sideslips the rudder may be deflected to its maximum angle both to the weather side (during  $V_{MC}$ - tests) and to the lee side ( in sideslips and cross-wind take-offs and landings )

#### A special characteristic of vertical tail surfaces

The most stringent design requirement for vertical tail surfaces is the ability to cope with VERY LARGE SIDESLIP ANGLES up to 25 degrees. Therefore vertical tail surfaces have :

- Low aspect ratio's
- Large leading-edge sweep
- sometimes dorsal fins

As shown on page I-21 to I-24 for lifting surfaces with an aspect ratio  $A \leq 1.5$  the lift curve gradient  $C_{L_\alpha} = 0.0274 A$ . As  $A = b^2 / S$  and  $L = C_{L_\alpha} \times \alpha \times \frac{1}{2} \rho V^2 S$  then

$$L = 0.0274 b^2 \times \alpha \times \frac{1}{2} \rho V^2 \quad (\text{Note } \alpha = \alpha_v = -\beta)$$

Thus: The side force gradient on a fin is to a first order independent of the shape and the fin chord but only of the fin span ( fin height ).

Adding a dorsal fin or applying wing sweep does however often increase the maximum lift and the angle-of-attack for maximum lift and improves the linearity of the aerodynamic characteristics. Therefore a dorsal fin and fin sweep are also beneficial for low-speed aircraft.

#### Tail – off side force and yawing moment

On pages I-1 to I-12 the tail-off side force and yawing moment is presented of a number of aircraft models as obtained from wind tunnel tests. Page I-13 shows for one model, F-29 Model 2-5, the raw data and the sideslip derivatives as given in ref. 59. Ref.59 shows the sideslip derivatives in fig.66b which is reproduced as the lower left figure on page I-13. Reconsidering the slope of the raw data produced slightly different derivatives. ( See page I-13 with data from ref.59 figs.34a,b and 35 and the lower left part of page I-12). This illustrates that inaccurate determination of derivatives may lead to confusing conclusions.

The tail-off side force and yawing moment are analyzed in the present report, although in a slightly modified form, according to the method presented in the USAF Datcom and NACA TN D-6946.

In the USAF Datcom the side force is estimated according to the formula :

$$(C_{y_b})_{WFN} = \frac{S_{fus.cross}}{S_W} K_i \frac{2}{57.3} - 0.0001\Gamma - 0.0011 n_{nac}$$

( The latter term is taken from ESDU Data Sheet No. 79006. )

From the data on pages I-8 to I-12 and the lower part of page I-14 it is concluded that flap deflection increases the tail-off side force and decreases the yawing moment and both are slightly affected by angle-of-attack. Although these effects show considerable variations a trend can clearly be observed. Therefore average curves for these changes in tail-off side force and yawing moment due to flap deflection  $(\Delta C_{y_\beta})_{FL}$  and  $(\Delta C_{n_\beta})_{FL}$  are proposed on the upper half of page I-14.

For the models in cruise configuration no unambiguous effect of angle-of- attack on side force or yawing moment could be determined.

The test data of Models SKV-LST-3 (page I-11) and SKV-6 (page I-12) with and without engine nacelles on the wing show on average that fitting engine nacelles on the wing produces an increase in side force  $(\Delta C_{y_\beta})_{nac} = -0.0035$  and in yawing moment  $(\Delta C_{n_\beta})_{nac} = -0.0005$  for two engines.

The test data of Models 8/41 (pages I-8, I-9) and SKV-LST-3 (page I-11) with and without engine nacelles on the rear fuselage show on average that two engine nacelles on the rear fuselage produce an increase in side force  $(\Delta C_{y_\beta})_{nac} = -0.0005$  and no effect on yawing moment  $(\Delta C_{n_\beta})_{nac} = 0$  is observed.

Based on the analysis of the wind tunnel data as described above the tail-off side force formula is modified to :

$(C_{y_b})_{WFN} = \frac{S_{fus.cross}}{S_W} K_i \frac{2}{57.3} - 0.0001\Gamma + (\Delta C_{y_\beta})_{FL} - 0.00175 n_{nac} \text{ ( nacelles on wing )}$		
$- 0.00025 n_{nac} \text{ ( nacelles on fuselage )}$		
For $K_i$ see page I-15	For $(\Delta C_{y_\beta})_{FL}$ see page I-14	( 1 )

The tail-off yawing moment in the USAF Datcom is estimated via :

$$(C_{n_\beta})_{WFN} = -K_N \frac{S_{B_S} l_B}{S_W b_W} \text{ with the factor } K_N \text{ read off a graph presented on page I-16.}$$

The analysis of the wind tunnel data on pages I-8 to I-14 showed the effect of angle-of- attack and flap angle on the tail-off yawing moment and led to the modified formula:

$$(C_{n\beta})_{WFN} = -K_N \frac{S_{B_S} l_B}{S_W b_W} + (\Delta C_{n\beta})_{FL} \quad \text{with } K_N \text{ taken from page I-16} \quad (2)$$

On pages I-17 and I-18 a comparison is presented of the tail-off side force and yawing moment for the models in cruise configuration as estimated with the formula given above and data derived from wind tunnel tests.

## The tail contribution to side force and yawing moment

### Some definitions

On page I-19 some geometrical definitions concerning the vertical tail surface or fin are presented.

Note that in the definition of area and span (height) the tail surface is assumed to continue inside the fuselage up to the fuselage centre line. This is in accordance with the definition used in most NACA publications and differs from the definition used in the ESDU Data Sheet and used by several aircraft manufacturers.

Page I-20 shows some sketches explaining the flow characteristics in front of the vertical tail affecting the contribution of the tail to side force and yawing moment.

### The lift curve slope of isolated lifting surfaces.

On pages I-21 to I-24 lift curve slopes for various lifting surfaces are shown. (3)

These figures clearly show that for low-aspect-ratio surfaces with  $A \leq 1.5$  the actual shape (sweep, taper ratio, tip shape) has hardly any effect on the lift curve slope.

### The effect of a dorsal fin on the lift curve slope and the aerodynamic centre of the vertical tailplane.

Pages I-25 to I-38 show the effect of a dorsal fin on the vertical tail characteristics. Although the main purpose of a dorsal fin is increasing the maximum angle-of-attack of the vertical tailplane before flow separation occurs the tailplane lift gradient is slightly increased and the aerodynamic centre moves forward. These effects can also be seen when leading-edge strakes or leading-edge extensions (LEX) are considered in the wing designs of modern combat aircraft. The data presented are derived from wind tunnel tests performed during the development programmes of both the Fokker F-27 and the F-28.

Page I-35 shows the data derived from the wind tunnel test results of the F-28 Models 8/4 and 8/41.

From the tests on the F-27 tail model only cross force coefficients (= - side force coefficients) were available. (page I-37). The change in lift curve slope due to dorsal fins of different size is indicated in the lower figure on page I-38.

The lower figure on page I-36, taken from test data of a complete F-27 model, shows that for different dorsal fins the yawing moment, at least up to medium yaw angles, is not affected by fin size or shape. This means that the increase in side force due to an increase in fin size is counteracted by a forward movement of the aerodynamic centre. With this in mind this **shift in aerodynamic centre was determined with the data from page I-37. (Upper figure on page I-38)**

Note the similarity between the curves for the two data sets on pages I-35 and I-38.

On pages I-25 to I-34 a collection of available raw wind tunnel data and on page I-35 to I-38 a collection of available dorsal fin aerodynamic data is presented.

( 4 )

The endplate effect of the horizontal tailplane on the vertical tailplane lift curve slope.

Wind tunnel test data of the endplate effect of the horizontal tailplane  $K_{VH}$  is shown on pages I-39 to I-45.

The lower figure on page I-39 shows a graph of the endplate effect of the horizontal tailplane on the lift curve slope of the vertical tailplane as expressed by a change in effective aspect ratio  $A_V$  as presented in the USAF Datcom.

Analysis of all available test data, including wind tunnel data on later transport aircraft produced a slightly modified curve (pages I-41 and I-42), in particular for horizontal tailplanes mounted on the fuselage. (page I-45).

The derivation of the individual data points in the figures on pages I-41, I-42 and I-45 can be found in the second part of this report, pages II-1 to II-68.

These data are rearranged in a separate chapter on pages III-1 to III-14.

The effect of the tailplane area ratio  $S_H / S_V$  on the endplate effect is shown for a number of configurations on page I-43 together with the average curve given in the USAF DATcom.

The endplate effect of the horizontal tailplane on the vertical tailplane can be determined with the aid of the graphs presented on page I-39 to I-45.

( 5 )

The endplate effect of the horizontal tailplane is not only affected by the tailplane relative vertical position and tailplane area ratio but also by the horizontal tailplane effective angle-of-attack or lift coefficient. This is illustrated on page I-44 for a number of model configurations.

It will be clear that a lifting swept horizontal tail surface shows a cross flow above and below the upper and lower surface in a sideslip just as a wing produces a cross-flow and a rolling-moment-due-to-sideslip. It is however not immediately clear what the relation is between the sign of sideslip angle, tailplane lift coefficient and average cross flow direction at the vertical tailplane.

For the average horizontal tailplane the effect of the tail lift on the endplate effect on the vertical tailplane can be expressed as :

$$K_{VH} = (K_{VH})_{\alpha_H=0} \left[ 1 - 0.014(\alpha_H + \alpha^*) \right]$$

( 6 )

Some additional data on the lift curve slope of the vertical tail including the endplate effect of the stabilizer of models SKV-LST-3 and F-29-1-1 are given on pages I-57 and I-58.

Sidewash at the vertical tailplane.

1. Sidewash or cross-flow due to the presence of the fuselage.

Sidewash due to the flow around a fuselage in sideslip is illustrated on page I-20.

On page I-46 a collection of sidewash data for fuselage-tailplane combinations is shown.

The sidewash parameter is defined as the product of the actual sidewash ratio  $(1 + \delta\sigma / \delta\beta)$ , the effective-versus-free-stream dynamic pressure ratio  $q_V / q$  (to take into account the fuselage-boundary-layer effect) and the tailplane-fuselage lift carry-over effect  $K_{FV}$ .

The parameter  $(1 + \delta\sigma / \delta\beta) q_V / q K_{FV}$  is presented as a function of fin-span-to-fuselage-diameter ratio  $b_V / d_V$ . ( See page I-19 for the definition of  $b_V$  and  $d_V$  )

In the upper figure on page I-39 this fuselage-tailplane interference effect is expressed as a ratio between the nominal and effective vertical tailplane aspect ratio  $(A_{V(B)}) / (A)_V$ .

For  $A \leq 1.5$  the lift gradient can be written as  $C_{L\alpha} = 0.0274 A$  and thus the tailplane aspect ratio given above is equivalent to the fuselage-tailplane interference factor  $(1 + \delta\sigma / \delta\beta) q_V / q K_{FV}$ . Therefore the curves on pages I-39 and I-46 show a high degree of similarity.

For estimating the tailplane-fuselage sidewash  $(1 + \delta\sigma / \delta\beta) q_V / q K_{FV}$   
 -----  
 an average curve was drawn in the figure on page I-46. ( 7 )

2. Sidewash due to wing-fuselage interference. ( Rolling moment due to sideslip I. )

The data on pages I-47 and 48 show the effect of the wing position in height on the fuselage on the sidewash-due-to-sideslip derivative.

$$\left( \Delta \frac{d\sigma}{d\beta} \right)_{h_W} \frac{q_V}{q} K_{FV} = -0.40 \frac{h_W}{D_{f_{\max}}} \quad \text{For definition of } h_W \text{ and } D_{f_{\max}} \text{ see page I-19}$$

( 8 )

3. Sidewash due to wing dihedral and sweep. ( Rolling moment due to sideslip II. )

Based on a limited amount of wind tunnel test data ( see page I-49 ) an equation (equation 9) has been found that expresses the relation between sidewash and wing dihedral. Wing dihedral has been substituted by the change in rolling-moment-due-to-sideslip derivative due to wing dihedral  $(\Delta C_{l_\beta})_\Gamma$  to account for both dihedral and wing sweep.



$$\left( \Delta \frac{\delta \sigma}{\delta \beta} \right)_\Gamma \frac{q_V}{q} K_{FV} = + \left( 110 + 50 \frac{h_W}{D_{f_{\max}}} \right) (\Delta C_{i_\beta})_\Gamma \quad (9)$$

#### 4. Direct sidewash measurements on Model SKV-LST-3.

On model SKV-LST-3 with engine nacelles on the rear fuselage direct sidewash measurements were performed by means of a variable-incidence vertical tailplane. By comparing tail-on and tail-off side-force and yawing moment for different tailplane incidences  $i_{vH}$ , under the assumption that when tail-on and tail-off side-force and yawing moment are equal the load on the tailplane is zero and the average vertical-tailplane

angle-of-attack  $\alpha_v = 0$ , the average sidewash can be determined via the equation

$$\alpha_{vH} = 0 = \beta + \sigma + i_{vH} \quad \text{or} \quad \sigma = -\beta - i_{vH}.$$

-----  
 Note that to enable variation of the vertical tailplane incidence  $i_{vH}$  a fin root plug was installed ( see page II-9b ).

Therefore in the analysis two volume coefficients have been used:  $\bar{V} = 0.1443$  for the basic fin including a dorsal fin and  $\bar{V} = 0.1554$  for the fin with rootplug (but without dorsal fin ). The latter configuration was not only used for the tests with variable incidence  $i_{vH}$  but also for tests with varying sideslip angle.

On pages I-57 to I-71 an analysis is presented of the vertical tailplane characteristics as determined according to the method described above

On page 57 a detailed analysis is shown for the configuration with engines on the rear-fuselage with flaps and slats retracted at  $\alpha = 0$ .

On the left hand side of page I-57 the vertical tail lift curve slope (including the horizontal tailplane and dynamic pressure ratio and lift-carry-over effects )  $C_{L_{av+H}} \frac{q_V}{q} K_{FV}$  is

determined by varying the vertical tailplane incidence  $i_{v+H}$  at sideslip angle  $\beta = 0$ . By

comparing this lift curve slope  $C_{L_{av+H}} \frac{q_V}{q} K_{FV} = 0.0290$  with the theoretical value

$$C_{L_{av+H}} = 0.0308 \quad \text{the factor} \quad \frac{q_V}{q} K_{FV} = 0.942 \quad \text{is obtained.}$$

On the right hand side of page I-57 the sidewash is determined, both from the data on the left side for  $\beta = 0$  ( upper right) and by comparing the tail yawing moment contribution

$$\frac{dC_{n_{30vH}}}{d\beta} = 0.0048/0.0053, \quad \text{as found by varying the sideslip angle } \beta \text{ with } i_{v+H} = 0, \text{ with the}$$

yawing moment contribution  $\frac{dC_{n_{30vH}}}{di_{v+H}} = 0.0045$  found with  $\beta = 0$ . In both cases  $\frac{\delta \sigma}{\delta \beta} = 0.13$ .

Page-58 shows some additional vertical tailplane characteristics.

On the upper half of page I-58 the effect of angle-of-attack and flap deflection on the tail

lift curve slope (including stabilizer)  $C_{L_{av+H}}$  of model SKV-LST-3 determined at  $\beta = 0$  is presented. This effect is apparently due to variations in local flow direction at the vertical tail resulting in changes in the factor  $\frac{q_V}{q} K_{FV}$ . This is also indicated on page I-71.

The lower half of page I-58 is discussed under the heading. " The effect of engine\_nacelles on the wing on sidewash".

On page I-59 two more examples are shown of the sidewash as determined from tests with different fin incidences on model SKV-LST-3.

Page I-60 shows the overall sidewash results whereas page I-61 shows the change in yawing moment due to fin incidence variation for all model configurations and angles-of-attack investigated .

On pages I-63 / I-64 and I-65 / I-66 the computed sidewash derivative  $(1+ \delta\sigma / \delta\beta)$  or  $\delta\sigma / \delta\beta$  and the relative effective dynamic pressure ratio combined with the lift carry-over factor  $\frac{q_V}{q} K_{FV}$  are presented in tabular form for both the configuration with the fin

including the root plug ( $\bar{V} = 0.1554$ ) and with the basic fin ( $\bar{V} = 0.1443$ ). On pages I-67 , I-69 / I-70 and I-71 this data is presented in graphical form. Page I-68 contains the tail-off rolling-moment-due-to-sideslip derivative for the wing-fuselage combination to be used in the analysis of the effect of angle-of-attack and flap deflection on sidewash.

#### 5. Sidewash analysis of other aircraft and windtunnel models.

Besides model SKV-LST-3 a number of wind tunnel models and full-scale aircraft have been analysed according to the method described above :

Fokker 100 Model 15-3	F-28 Mk 1000 Model 6-2-3
Fokker 100 Model 15-10	F-28 Mk 1000 Model 8-3
Fokker 100 Model 18-5	Airbus A320
Fokker 70 Model 15-24	Airbus A340 – 300
F-29 Model 1-2	Douglas DC-9-30
F-29 Model 2-5	Airbus A300
F-29 Model 5-3	Boeing 737-100
F-29 Model 1-1	

The results of this analysis are shown on pages I-73 to I-87

#### 6. Sidewash due to rolling-moment-due-to-to-sideslip

On pages I-69, I-70 and I-73 to I-87 the sidewash term  $\frac{d\sigma}{d\beta}$  as a function of angle-of-attack  $\alpha_R$ , is presented for all models and aircraft investigated.

The resulting curves show a large variation in shapes, even when for a given aircraft or model the curves derived from side force and yawing moment data are compared. Although some data sets, such as that for Model F-29-1-2 or F-28 Model 8-3, (page I-77 And I-83) show an opposite trend the majority of the curves clearly show a trend where the sidewash diminishes with increasing  $\alpha_R$ . In most cases the curves show a gradual decrease in sidewash, in particular in the normal operating range of  $\alpha_R$ 's. Only at the

highest  $\alpha_R$ 's do the curves drop sharply, presumably due to the beginning of local flow disturbance. No explanation is offered for the smaller downwash at low angles-of-attack in some cases.

Overall however, it is concluded that for preliminary design purposes and lacking other data the decrease in sidewash with increasing angle-of-attack can be expressed with a straight line with a small negative slope.

This effect is attributed to the sidewash resulting from the non-uniform spanwise lift distribution in a sideslip. The upwind wing producing more lift than the downwind wing causes above the wing upper surface a cross flow towards the upward wing decreasing the overall sidewash. This is illustrated on page I-20.

In particular on swept wings the rolling-moment-due-to-sideslip increases with increasing angle-of-attack. ( An increasing tendency to roll in an anti-clockwise direction with the wind coming from the right.) This is a linear relation as illustrated in the figures on pages I-89 to I-94.

As for transport aircraft the wing aspect ratio lies usually in the range  $A_w = 7.0 - 12.0$  and the wing sweep is mostly  $\Lambda_w \leq 30\text{deg}$  the lift curve slope shows little variation as shown by the table below (complete aircraft).

Aircraft or model	Lift curve gradient	Aircraft or model	Lift curve gradient
Model SKV-LST-3 WF	0.094 / deg	A320	0.093 / deg (AI)
Model SKV-LST-3 WFN <sub>f</sub>	0.095 / deg	A340-300	0.092 / deg (AI)
Model SKV-LST-3 WFN <sub>w</sub>	0.093 / deg	F-29 model 1-2	0.092 / deg
F-28 model 8-3	0.087 / deg	F-29 model 2-5	0.093 / deg
F-28 model 6-2-3	0.087 / deg	Fo 100 model 15-10	0.090 / deg
		F-27	0.092 / deg

As the lifting –line theory clearly shows the rolling-moment-due-t- sideslip is directly connected to lift and consequently the slope or gradient of the rolling-moment-due-to-sideslip as a function of angle-of-attack will also show little variation with aspect ratio and wing sweep. This is clearly shown in the graphs on pages I-89 to I-94 and the lower figure on page I-108.

On pages I-95 to I-100 the tail-off rolling-moment-due- to-sideslip is presented as a function of the tail-off lift-coefficient. As for the configurations considered the lift curve has a constant gradient with little variation the curves on pages I-95 to I-100 are also straight lines with almost constant gradient.

These gradients  $\left( \frac{C_{l\beta}}{C_{L\beta}} \right)$  were computed with equation ( 12 ) and compared with the

measured values on page I-111. Note that apart from the data for the A340 calculated and measured data compare reasonably well.

Assuming the relation between the sidewash and the rolling-moment-due-to-sideslip discussed above and the small variation in the rolling-moment-versus- tail-off-lift-coefficient gradient the relation between sidewash and tail-off lift-coefficient is assumed to be linear with a small negative gradient.

In the figures on pages I-102 to I-107 this relation is indicated as a double straight line as an average between the curves derived from side-force and from yawing-moment data. This relation is also described as equation ( 10 ).

$$\left( \frac{\Delta \delta \sigma}{\delta \beta} \right)_{C_{l\beta}} = -0.50 \left[ (C_{l\beta})_{T-O} - (C_{l\beta})_{T-O, C_L=0} \right] \quad (10)$$

The tail-off rolling-moment-due-to-sideslip is determined with the following equation taken from the USAF Datcom and ref.1 (after some re-writing) :

$$(C_{l\beta})_{T-O} = \left( \frac{C_{l\beta}}{C_{LW}} \right) \frac{C_{LW}}{57.3} + \left( \frac{C_{l\beta}}{\Gamma} \right) \Gamma - \left( 0.042 \frac{Z_W}{D_{fus_{max}}} + 0.0005\Gamma \right) \sqrt{A_w} \left( \frac{D_{fus_{max}}}{b_w} \right)^2 \quad (11)$$

The coefficients which express the effect of wing dihedral and sweep on the rolling-moment-due-to-sideslip  $(C_{l\beta} / C_{LW})$  and  $(C_{l\beta} / \Gamma)$  are given on pages I-51 and I-52.

The lift-dependent tail-off rolling-moment-due-to-sideslip  $(C_{l\beta} / C_{Lw})$  may also be determined with the following equation :

$$\left( \frac{C_{l\beta}}{C_{Lw}} \right) = -\frac{1}{2} \left[ \frac{3}{A_w(1+\lambda)} + y^* \left( \tan \Lambda_{c/4} - \frac{6}{A_w} \frac{1-\lambda}{1+\lambda} \right) \right] + 0.05 \text{ per rad.} \quad (12)$$

The computed rolling-moment-due-to-sideslip are shown on page I-110.

#### 7. Sidewash due to flap deflection in the landing position

The sidewash due to flap deflection in the landing position is derived from the shift in the figures of the average linearized curves for different flap settings. This shift sometimes showed an increase in sidewash and sometimes a decrease. A similar effect was shown by the rolling-moment-due-to-sideslip. It was therefore concluded that this depended on the relative flap span. This relation is shown in the upper figure on page I-107 and also expressed by equation ( 13 ) .

For smaller flap angles a sidewash contribution due to flap deflection is assumed to be proportional to the flap angle.

$$\left( \frac{\Delta \delta \sigma}{\delta \beta} \right)_{FL,ldg} = -0.80 \left( \frac{b_{FL}}{b_w} - 0.67 \right) \quad (13)$$

#### 8. The effect of engine nacelles on the wing on sidewash

On the lower half of page I-58 some tailplane data are given for model F-29-1-1. Note that

at  $\alpha_R = 0$  fitting the low-set wing ( $h_w / D_{f_{max}} = -0.26$ ,  $\Gamma_w = 7.0$  deg) and under-wing engine nacelles onto the fuselage-tail combination increases the sidewash by  $\delta\sigma / \delta\beta \approx 0.100$ . Fitting the low-set wing onto the fuselage, together with the wing dihedral

increases the sidewash with  $\Delta \frac{\delta\sigma}{\delta\beta} = 0.40 \times 0.26 - (110 - 50 \times 0.260) \times 0.00161 =$

$= 0.104 - 0.156 = 0.046$ . See pages I-47, I-49 I-109) and thus on this model fitting two

engine nacelles onto the wings increases the sidewash with  $\left( \Delta \frac{d\sigma}{d\beta} \right)_{NW} \approx 0.145$

This seems unlikely given the small increase in sidewash due to the under-wing engine nacelles on model SKV-LST-3 (page I-70) and the small decrease in rolling-moment – due-to-sideslip on models SKV-6 and SKV-6WN (page I-101). Furthermore the sidewash measured on the fuselage +tailplane combination of model 1-2 (page II-14b) seems unrealistically low. The available test results on these two fuselage-tail combination are suspect. Also, the estimated sidewash data, computed without any effect of the nacelles (page I-110) and compared with measured sidewash data for the configurations with engine nacelles on the wing show relatively minor differences with either sign (+ or -) as shown in this table :

Configuration	$\left( \frac{d\sigma}{d\beta} \right)_{estimated}$	$\left( \frac{d\sigma}{d\beta} \right)_{measured}$
Model SKV-LST-3 (II) WF	0.375	0.450
Model SKV-LST-3 (II) WFN <sub>w</sub>	0.375	0.420
A320	0.350	0.320
A340-300	0.295	0.240
F-29 model 1-2	0.280	0.270
F-29 model 2-5	0.272	0.300

It is suggested to use the following number as contribution to the sidewash due to under-wing nacelles

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{NW} \approx 0 + 0.03 \quad (\text{page I-101 and I-103, lower figure})$$

( 14 )

9. The effect of the horizontal and vertical position of rear-fuselage engine nacelles on the sidewash at the vertical tail.

On pages I-53 and I-54 wind tunnel test data are presented of the effect of engine nacelle position on the sidewash-in-sideslip at the vertical tail. The data show for these tests on F-28 Model 8/41 (ref. 22) a considerable effect of relative small variations in nacelle position. If the effect of the dorsal fin on the effective yawing moment arm is incorporated ( $S_{DF} / S_V = 0.071$  and  $l_{V+DF} = l_V 0.95$  see page I-35) the data on side-force and yawing moment compare very well.

Note that the longitudinal position of the nacelles is defined as the distance between the engine exhaust plane and the 0%-point of the fin root chord, positive when the engine exhaust is behind this 0%-point.

The vertical position is defined by the vertical distance between the engine nacelle centre line and the fuselage centre line, positive when the nacelle centre line is above the fuselage centre line.

With the aid of the test data shown on page I-71 the factor  $\frac{q_v}{q} K_{FV}$  was estimated.

By dividing the total sidewash factor  $(1 + \frac{\delta\sigma}{\delta\beta}) \frac{q_v}{q} K_{FV}$  by  $\frac{q_v}{q} K_{FV}$  the true sidewash factor  $\frac{\delta\sigma}{\delta\beta}$  was found. For the data on pages I-53 and I-54  $\Delta \frac{\delta\sigma}{\delta\beta}$  is given on page I-56.

Generalized curves for estimating the effect of the position of rear-fuselage engine nacelles on sidewash-due-to-sideslip at the vertical tailplane  $\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{NF}$  are given on page 56. ( 15 )

### An analysis of the effective tail moment arm.

In the standard approach in analyzing the yawing moment contribution of the vertical tailplane to the aircraft's yawing moment the tailplane side-force is assumed to apply at the 25% m.a.c.-point of the exposed tailplane area. The distance between this point and the moment reference point is considered to be the yawing-moment arm . The analysis of the effect of a dorsal fin on the relation between tailplane side-force and yawing-moment justified an analysis of this relation for tailplanes without dorsal fin as found from wind tunnel tests and in the data bases of some full-scale airplanes.

On pages IV-1 to IV-36 an overview is presented of the ratio

$R_{TL} = \left( \Delta C_{n\beta} \right)_{V+H} / \left( \Delta C_{Y\beta} \right)_{V+H} * \frac{l_V}{b}$  in tabular form. On pages I- 112 to I-116 this ratio

is shown in graphical form.

Although a large variation occurs in this parameter it may in general be concluded that the ratio  $R_{TL}$  is close to one provided that :

1. The data are obtained at a sufficiently high Re-number
2. No dorsal fin is fitted
3. The rear fuselage is not highly tapered

### Rudder Characteristics

#### Side- force due to rudder deflection

On pages I-117 to I-120 available data are collected on rudder characteristics of ten aircraft and wind tunnel models. In most cases the side force curves show a linear behavior up to  $\delta_R = 25$  deg. In the normal range of rudder-chord-to-tailplane chord ratio

( $c_R / c_V = 0.20-0.35$ ) the maximum side force is reached at  $\delta_R \approx 35$  deg. The maximum side force loss, relative to the linear  $C_{L_V} - vs. - \delta_R$  relation is then  $\Delta C_{L_V} = 10$  to 15 %. The maximum lift (or side force) is  $C_{L_V \max} \approx 0.8$  based on exposed tailplane area or  $C_{L_V \max} \approx 0.6$  based on tailplane reference area.

Note that on model SKV-LST-2 a double-hinged rudder was tested. The data on page I-117 refer to the tests with the forward part deflected with the rear part in the neutral position ( $c_R / c_V = 0.311$ ) and with the rear part deflected ( $c_R / c_V = 0.156$ ).

In order to be able to compare the data of rudders with different relative span the data are normalized to full-span rudders by the ratio  $S_{V_R} / S_V$  (page I-19).

With the equation given below and the equation for the yawing-moment-due-to-rudder-deflection the ratio  $\frac{(C_{y_{\delta_R}})_{S_V}}{C_{L_{\alpha_V + H_{est}}}}$  (both terms related to the tailplane reference area) were

calculated (page I-121). They are presented in graphical form on page I-122. Note the similarity with the data for two-dimensional flow.

$$(C_y)_{\delta_R} = C_{y_{\delta_R}} \times \delta_R = C_{L_{\alpha_V}} \times \frac{q_V}{q} \times K_{FV} \times K_{VH} \times \frac{c_{l\delta}}{c_{l\alpha}} \times \frac{S_{V_R}}{S_W} \times \delta_R \quad (16)$$

#### Yawing moment due to rudder deflection

Rudder yawing moment = Rudder side-force x Rudder moment arm.

The rudder moment arm is longer than the vertical-tailplane moment arm because the centre-of-pressure of the load due to rudder deflection lies behind the  $0.25\overline{c_V}$ -point.

This difference in distance is  $\Delta l_R \approx 0.30\overline{c_V}$  for the usual range of relative rudder chords.

An example is shown on page I-123.

The yawing moment due to rudder deflection can be estimated with equation ( 17 ).

$$(C_n)_{\delta_R} = C_{n_{\delta_R}} \times \delta_R = C_{L_{\alpha_V}} \times \frac{q_V}{q} \times K_{FV} \times K_{VH} \times \frac{c_{l\delta}}{c_{l\alpha}} \times \frac{S_{V_R}}{S_W} \times \frac{l_{V(+DF)} + 0.30\overline{c_V}}{b_V} \times \delta_R$$

With maximum rudder deflection  $(C_{n_{\max}})_{\delta_R} = 0.90 \times C_{n_{\delta_R}} \times \delta_{R_{\max}}$  ( 17 )

#### Aircraft ( Model ) Geometry and Aerodynamic data

On pages II-1a to II-68a detailed geometries are given for all aircraft types and models analyzed in the present report together with the basic available wind tunnel test data

As the analysis of the material in this part of the report took place over a long period due to improved insight small differences may be found between some numbers in this part of the report and in the text which was written at a much later date. This refers in particular to some calculations concerning the endplate effect of the horizontal tailplane the conclusions on which were modified in a later stage. These differences have not affected however the overall conclusions.

### **Compilation of Wind Tunnel Test Data**

On pages V-1 to V-35 a compilation is presented of raw wind tunnel test data together with some computed data of all the model tests discussed in this report.

### **Some final remarks**

1. In the design of transport aircraft the emphasis is on transport capability and thus on performance aerodynamics. In the early phases of the design process the interest is therefore , apart from the fuselage interior arrangement and the loadability, primarily focused on the wing aerodynamics and the airframe-propulsion integration. The interest for the tail surfaces is usually limited to quick estimates of the required volume coefficients for horizontal and vertical tailplanes. This approach may have been adequate when centre-of gravity-ranges were limited and thrust –to-weight ratios were much lower than today but for a modern design with its large c.g.-range, high thrust-to-weight ratio and severe requirements for take-offs and landings with strong cross-winds this approach no longer suffices and a more detailed analysis is required already in an early design stage. The weight but in particular the size of tail surfaces today is such that, in combination with the ever-increasing design range and built-in development potential the role of tailplane sizing in the overall weight and drag prediction is more important than ever.

For horizontal tail surfaces the analysis already goes further than estimating a volume coefficient. With the aid of so-called “scissor plots” the various design requirements for the horizontal tailplane are studied.

The vertical tailplane however, notwithstanding the more complicated flow condition under which the fin has to operate because more airframe components ahead of the fin influence the local flow direction at the fin, has up to now not received the same attention. It is hoped that the present report will help to improve on this unsatisfactory situation.

2. The approach followed in the present report is mainly based on empirical data compilations. As the experience with the USAF Datcom and ESDU data sheets has shown the accuracy of predictions with the information provided in these publications sometimes leaves to be desired. When no wind tunnel data are available only this empirical approach provides the required sizing information. When wind tunnel data are available on a configuration with a reasonable degree of resemblance more accurate information is obtained when both configurations are analyzed with the data in this report and the difference is added to the data of the older model. Although the actual numbers in the present correlations may not always show the required accuracy the general trends seem reliable.



## A summary of equations and graphs discussed in this report

### Tail-off side force

$$(C_{y\beta})_{WFN} = \frac{S_{fus.cross}}{S_W} K_i \frac{2}{57.3} - 0.0001\Gamma + (\Delta C_{y\beta})_{FL} - 0.00175 n_{nac} \text{ (nacelles on wing)} \\ - 0.00025 n_{nac} \text{ (nacelles on fuselage)}$$

For  $K_i$  see page I-15      For  $(\Delta C_{y\beta})_{FL}$  see page I-14      (1)

### Tail-off yawing moment

$$(C_{n\beta})_{WFN} = -K_N \frac{S_{Bs}}{S_W} \frac{l_B}{b_W} + (\Delta C_{n\beta})_{FL} \quad \text{with } K_N \text{ taken from page I-16} \quad (2)$$

### Lift curve slope of isolated lifting surfaces

On pages I-21 to I-24 lift curve slopes for various lifting surfaces are shown.      (3)

### Dorsal fins

On pages I-25 to I-34 a collection of available raw wind tunnel data and on page I-35 to I-38a collection of available dorsal fin aerodynamic data is presented.      (4)

### The endplate effect of the horizontal tailplane on the vertical tailplane

The endplate effect of the horizontal tailplane on the vertical tailplane can be determined with the aid of the graphs presented on page I-39 to I-45.      (5)

For the average horizontal tailplane the effect of the tail lift on the endplate effect on the vertical tailplane can be expressed as :

$$K_{VH} = (K_{VH})_{\alpha_H=0} [1 - 0.014(\alpha_H + \alpha^*)] \quad (6)$$

### Vertical - tailplane - fuselage sidewash

For estimating the tailplane-fuselage sidewash  $(1 + \delta\sigma / \delta\beta) q_V / q K_{FV}$  an average curve was drawn in the figure on page I-46.      (7)

### Sidewash due to wing-fuselage interference

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{h_W} \frac{q_V}{q} K_{FV} = -0.40 \frac{h_W}{D_{f_{\max}}} \quad \text{For definition of } h_W \text{ and } D_{f_{\max}} \text{ see page I-19. (8)}$$

Sidewash due to wing dihedral and wing sweep

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{\Gamma} \frac{q_V}{q} K_{FV} = + \left( 110 + 50 \frac{h_W}{D_{f_{\max}}} \right) (\Delta C_{l_{\beta}})_{\Gamma} \quad (9)$$

Sidewash due to rolling moment due to sideslip

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{C_{l_{\beta}}} = -0.50 \left[ (C_{l_{\beta}})_{T-O} - (C_{l_{\beta}})_{T-O, C_L=0} \right] \quad (10)$$

Rolling moment due to sideslip

$$(C_{l_{\beta}})_{T-O} = \left( \frac{C_{l_{\beta}}}{C_{LW}} \right) \frac{C_{LW}}{57.3} + \left( \frac{C_{l_{\beta}}}{\Gamma} \right) \Gamma - \left( 0.042 \frac{Z_W}{D_{fus_{\max}}} + 0.0005\Gamma \right) \sqrt{A_w} \left( \frac{D_{fus_{\max}}}{b_W} \right)^2 \quad (11)$$

Lift dependent rolling moment due to sideslip

$$\left( \frac{C_{l_{\beta}}}{C_{LW}} \right) = -\frac{1}{2} \left[ \frac{3}{A_w(1+\lambda)} + y^* \left( \tan \Lambda_{c/4} - \frac{6}{A_w} \frac{1-\lambda}{1+\lambda} \right) \right] + 0.05 \quad \text{per rad} \quad (12)$$

Sidewash due to flap deflection to the landing position

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{FL,ldg} = -0.80 \left( \frac{b_{FL}}{b_W} - 0.67 \right) \quad (13)$$

The effect of engine nacelles on the wing on sidewash

$$\left( \Delta \frac{\delta\sigma}{\delta\beta} \right)_{NW} \approx 0 - 0.04 \quad (\text{page I-100 and I-101}) \quad (14)$$

The effect of rear-fuselage engine position on sidewash

Generalized curves for estimating the effect of the position of rear-fuselage engine nacelles on sidewash-due-to-sideslip at the vertical tailplane  $\left(\Delta \frac{\delta\sigma}{\delta\beta}\right)_{NF}$  are given on page 56. (15)

Side force due to rudder deflection

$$(C_y)_{\delta_R} = C_{y_{\delta_R}} x \delta_R = C_{L\alpha_V} x K_{FV} \frac{q_V}{q} x K_{VH} x \frac{c_{l\delta}}{c_{l\alpha}} x \frac{S_{V_R}}{S_W} x \delta_R$$

With maximum rudder deflection  $(C_{y_{\max}})_{\delta_R} = 0.90 x C_{y_{\delta_R}} x \delta_{R_{\max}}$  (16)

Yawing moment due to rudder deflection

$$(C_n)_{\delta_R} = C_{n_{\delta_R}} x \delta_R = C_{L\alpha_V} x K_{FV} \frac{q_V}{q} x K_{VH} x \frac{c_{l\delta}}{c_{l\alpha}} x \frac{S_{V_R}}{S_W} x \frac{l_{V(+DF)} + 0.30 \overline{c_V}}{b_V} x \delta_R$$

With maximum rudder deflection  $(C_{n_{\max}})_{\delta_R} = 0.90 x C_{n_{\delta_R}} x \delta_{R_{\max}}$  (17)

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