# Concrete mixed mode fracture test CARPIUC Benchmark Test 1 

doi: 10.5281/zenodo. 1477016

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November 2, 2018

The proposed benchmark consists in simulating crack propagation tests performed on mortar, with any type of adequate material model or numerical method. Two crack propagation tests are proposed, inspired to some extent by the well-known Nooru-Mohamed [1] tests. They present initiation, propagation, reorientation, link-up and branching. The goal is to compare your simulation results with the measured crack paths and forcedisplacement curves.
The input data consists in specimen geometry, experimentally determined material properties (Young modulus, tensile strength, compressive strength and fracture energy) and the measured boundary conditions.

## 1- Test description

## Specimens

The specimens are $50 \times 200 \times 200 \mathrm{~mm}$ mortar parallelepipeds. For the $1^{\text {st }}$ test only one 25 mm long, 5 mm wide notch is sawed on one side (Fig. 1 (a)). For the $2^{\text {nd }}$ test two 40 mm long, 5 mm wide notches are sawed at mid height of the specimen.


Fig. 1 The experimental geometry types

The mortar is composed of cement, $0-4 \mathrm{~mm}$ sand and plasticizer :

| Effective water <br> $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ | Cement <br> $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ | Sand 0/4 <br> $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ | Plasticizer <br> $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ |
| :---: | :---: | :---: | :---: |
| 319 | 611 | 1235 | 5.25 |

All the specimen were stored in the same water basin at room temperature and taken out 3 to 7 days before each test. Both crack-propagation tests were performed a week apart. 3-point flexural tests performed on $40 \times 40 \times 160 \mathrm{~mm}$ specimens and compressive tests performed on the resulting broken parts of the specimens (196-1 NFEN norm [2]) give the following main characteristics:

| Young modulus | $20.03 \pm 0.005 \mathrm{GPa}$ |
| :---: | :---: |
| Tensile strength | $4.1 \pm 0.4 \mathrm{MPa}$ |
| Compressive strength | $79.94 \pm 2.9 \mathrm{MPa}$ |

The Young modulus was assessed using the elastic slope of the tests, to the NFEN procedure. The Poisson ratio was not identified. The fracture energy $\mathrm{Gf}_{\mathrm{f}}$ is obtained from 6 3-point flexural tests performed on $70 \times 70 \times 280 \mathrm{~mm}$ specimens (following the recommendation of [3]). It is equal to $114.6 \pm 18.8 \mathrm{~N} / \mathrm{m}$. Force-displacement curves of these tests are available. For more details, see A. Carpiuc-Prisacari PhD manuscript [4].

## Loadings

The test loadings consist of proportional and non-proportional combinations of three elementary displacements of the upper face of the specimen while the bottom face is fixed:

- a global tension (i.e. vertical translation)
- a global shear (i.e. horizontal translation)
- a gradient of vertical displacement (i.e. in-plane rotation)


Fig. 2 The 3 elementary loadings: (1) global tension, (2) global shear, (3) gradient of vertical displacement
The crack evolution is controlled by Digital Image Correlation [5], with a computation performed every 10 images to detect the advancement of the crack. When the crack is considered sufficiently propagated the loading is changed to reorient/branch the crack.

Roughly speaking, the displacement rate is $0.01 \mu \mathrm{~m} / \mathrm{s}$, corresponding to quasi-static loading conditions. The stable propagation(s) lasts several hours, so only the final unstable crack propagation is a dynamic event. Precise loading paths will be found in the available data.

One may summarize the two tests as:

- for the first test, an initiation of the crack, followed by several reorientations and a branching of the crack
- For the second test, an initiation of the crack from one notch, then on the other, and a final link-up between the two propagated cracks


## Testing machine

The tests are performed on a 6 -axis hexapod testing machine. The load capacities are roughly $120 \mathrm{kN} \& 70 \mathrm{kN} . \mathrm{m}$ along Z and $50 \mathrm{kN} \& 45 \mathrm{kN} . \mathrm{m}$ in the $\mathrm{X}-\mathrm{Y}$ plane. The displacement range is around $\pm 250 \mathrm{~mm} \& \pm 22^{\circ}$ along $\mathrm{X}, \mathrm{Y}$ and Z . Its displacement error is less than 1 micrometre when the displacement range is limited to few hundreds of micrometres.
A small passive hexapod with legs equipped with strain gages is placed under the large one, in order to measure the forces and torques applied to the specimen. Its measurement uncertainties are equal to $80 \mathrm{~N} \& 20$ N.m.


Fig. 3 The 6-axes testing machine : (1) base, (2) actuators, (3) moving platform, (4) upper end-effector, (5) room for specimen, (6) optical setup in close configuration with two cameras, (7) passive hexapod.

## Instrumentation

Displacement measurements are performed with a $2048 \times 2048$ pix. camera placed on each side of the specimen, recording images of the $200 \times 200 \mathrm{~mm}$ faces and the plates to which the specimen are glued. Images are synchronized and taken every 5 s.


Fig. 4 Example of an image taken by a camera during a test, and used for DIC measurements. Top and bottom plates on which the specimen is glued are visible.

The available displacement fields are obtained with a Digital Image Correlation algorithm (Correli RT3, see [5]) with a mesh size equal to 15 pixels and a pixel equal to $130 \mu \mathrm{~m}$. The displacement uncertainty of these kinematic field are 1.3 (resp. 2.4) $\mu \mathrm{m}$ along Z (resp. Y ) direction.

## 2- Results

## First test results presentation

For the $1^{\text {st }}$ test the loading path is chosen to generate several reorientations and the branching of the crack. It consists of a series of different combinations of tension, rotation and shear steps (Fig. 2) that leads to initiation, propagation and reorientation of a crack following a zigzagged path. The reorientation is obtained by changing the shear sign while keeping the tension constant (steps $n^{\circ} 2,4$ and 6 ). The evolution of the crack at the end of each propagation step is given in Fig 5. The forces and torques measured during the test are presented in Fig. 6.
During the test the closure of the crack is observed. One may consider the crack closure to be nearly negligible because simulations performed with a non-local damage model [6] with and without stiffness recovery give good results in terms of crack path prediction in both cases. However, the force-displacement curves obtained with the model considering the stiffness recovery are closer to the experimental data than the ones obtained without any crack closure formulation (For more details, see A. Carpiuc-Prisacari PhD manuscript [4]).


Fig. 5 Vertical displ. fields given in micrometers showing the crack advancement for the $1^{\text {st }}$ test after each propagation step


Fig. 6 Forces (a) and torques (b) measured during the $1^{\text {st }}$ test and expressed at point $\boldsymbol{O}_{\text {sup }}^{\text {spe }}$.Steps 0 to 7 respectively correspond to elastic pre-test, initiation-propagation, reorientation, propagation, reorientation, propagation, branching, propagation.

## Second test results presentation

The $2^{\text {nd }}$ test addresses phenomena such as successive crack initiation and propagation, crack closure and friction and crack coalescence. The chosen geometry is the one with two notches (Fig. 1b). The test can be divided into four loading steps composed of combinations of elementary loading paths like tension, shear and in-plane rotation (Fig. 2). More precisely the test starts by applying positive in-plane rotation combined with a positive shear force to initiate and propagate a crack upward. Afterward, the system is unloaded and reloaded by coupling a negative in-plane rotation with a positive shear force leading to the closure of the crack and the initiation of a second crack on the opposite notch. After a second unloading, the final step is a proportional tensile - negative shear loading that reorients both cracks and links them up. The evolution of the crack after each propagation step is given in Fig. 7 and the evolution of the measured forces and torques is given in Fig. 8.
Even though during the propagation of the second crack, the first one is submitted to a small compressive displacement, when comparing the crack paths predicted by a non-local damage model [6] considering crack closure with those predicted without the crack closure formulation, almost no difference is noted. The forces and torques are also close for both formulations (for more details, see A. Carpiuc-Prisacari PhD manuscript [4]). Therefore, the data can be simulated with models that do not consider the stiffness recovery.


Fig. 7 Vertical displ. fields given in micrometers showing the crack advancement for the $2^{\text {nd }}$ test after each propagation step (for the last time step the calculation is not fully converged, hence the noisy field in the upper part).


Fig. 8 Forces (a) and torques (b) measured during the $2^{\text {nd }}$ test part 2 and expressed at point $\boldsymbol{O}_{\text {sup }}^{\text {spe }}$

## 3-Data

- Kinematic boundary conditions:
- Test1_Face_1_BC_bottom.txt (resp. Test2_Face_1_BC_bottom.txt)
- Test1_Face_1_BC_top.txt (resp. Test2_Face_1_BC_top.txt)
- Test1_Face_2_BC_bottom.txt (resp. Test2_Face_2_BC_bottom.txt)
- Test1_Face_2_BC_top.txt (resp. Test2_Face_2_BC_top.txt)

The given boundary conditions and the crack path evolution are given for one face of the sample and are suited for 2D numerical simulations, the data from the second face will be provided in order to be able, if desired, to perform 3D numerical simulations.

Data are not restricted to some key moments of the tests, but are on the contrary available for a very large number of time steps from the beginning to the end of the loading.
In order to exclude any issues when modeling the loading plates and the glue layer, the DIC mesh node displacements corresponding to a resized sample of $200 \times 150 \mathrm{~mm}$ are extracted and applied to the finite element model on its boundaries (Fig. 9). Therefore, the numerical geometry must be $200 \times 150 \mathrm{~mm}$ (respectively $50 \times 200 \times 150 \mathrm{~mm}$ for 3D simulations).


Fig. 9 The full-field boundary conditions extracted from DIC measurements that will be used to perform 2D numerical simulations

For each face of the sample two "Boundary conditions" files will be provided for different timestep, one containing the displacements to be applied to the lower boundary of the sample and the other one containing the displacements for the upper one. Each "BoundaryConditions" file will be structured in 3 columns:

Column 1: The width coordinate (y axes) corresponding to the displacements values, given [mm] for a coordinate system that has the origin in the centre of the sample Column 2: The horizontal displacement (Uy) [mm]
Column 3: The vertical displacement (Uz) [mm]
Example of boundary conditions data:

| Coord_Y | UY | UZ |
| :---: | :---: | :---: |
| -94.821924 | 0.001203 | 0.000514 |
| -90.945574 | 0.001145 | 0.000602 |
| -85.124886 | 0.001027 | 0.000607 |
| -81.243314 | 0.000923 | 0.000541 |
| -77.358421 | 0.000811 | 0.000424 |
| -73.470135 | 0.000747 | 0.000331 |

Since measured BCs are used, they are not necessarily very smooth, and even small global perturbations can create local stress concentrations, therefore damage localization.

In order to avoid any damage localisation near the upper and lower surface of the sample, it is recommended to consider in the sample's geometry two layers of higher strength and rigidity on the upper and lower ends of the sample (Fig. 9 Undamageable area).
The given kinematic fields unity is the micrometre, and the spatial unity in mm .

- Static boundary conditions:
- Test1_Forces.txt (resp. Test2_Forces.txt)
- Test1_Torques.txt (resp. Test2_Torques.txt)

The full measurements of the 6 effort components are provided. Forces and torques will be given as functions of time. The considered point for torques is located in the center of the upper face of the specimen (point $\boldsymbol{O}_{\boldsymbol{s u p}}^{\text {spe }}$ ).

- Crack path:
- Test1_DIC_paths_face1.pdf (resp. Test2_DIC_paths_face1.pdf)
- Test1_DIC_paths_face2.pdf (resp. Test2_DIC_paths_face2.pdf)
- Test1_Reorientation_branching_crack.gif (resp. Test2_Closing_linking_cracks.gif)
Measured crack paths are given to help users to understand the test scenari.
- Raw results of fracture test (3 point bending tests of the same batch) are also given for 6 notch specimens:
- Specimen_RawData_ep3.csv
- Specimen_RawData_ep4.csv
- Specimen_RawData_ep5.csv
- Specimen_RawData_ep6.csv
- Specimen_RawData_ep7.csv
- Specimen_RawData_ep20.csv


## 4-References

[1] Nooru-Mohamed, M.B. (1992). "Mixed-mode fracture of concrete: an experimental approach". PhD thesis, Technische Universteit Delft
[2] AFNOR (2006). Méthodes d'essais des ciments - Partie 1 : détermination des résistances mécaniques (NF EN 196-1).
[3] R. TCS (1985) Determination of the fracture energy of mortar and concrete by means of three-point bend tests on notched beams, Materials and Structures 18 (106) 285-290
[4] Carpiuc, A. (2015). "Innovative tests for characterizingmixed-mode fracture of concrete: from pre-defined to interactive and hybrid tests". PhD thesis, University of Paris-Saclay.
[5] Tomicevc, Z., Hild, F., and Roux, S. (2013). Mechanics-aided digital image correlation. The Journal of Strain Analysis for Engineering Design, 48(5):330-343.
[6] Lorentz, E. (2015). A nonlocal damage model for plain concrete consistent with cohesive fracture. Submitted.

