

decoherence_times2rates(tau)

Decoherence rates from decoherence times. Zero decoherence rate for the exactly degenerate states and for the self-decoherence (diagonal elements)

$$r_{ij} = \begin{cases} \frac{1}{\tau_{ij}}, & \text{if } \tau_{ij} > 0 \\ 0, & \text{otherwise} \end{cases}$$

energy_gaps(Hvib)

Absolute values of energy gaps for a single trajectory at every timestep.

$$\Delta E_{ij}(t) = |Hvib_{ii}(t) - Hvib_{jj}(t)|$$

energy_gaps_ave(Hvib, itimes, nsteps)

Absolute values of energy gaps averaged over multiple trajectories at every timestep.

$$\Delta E_{ij}(t) = \frac{1}{N_{it}N_{tr}} \sum_{k=1}^{N_{it}} \sum_{n=1}^{N_{tr}} |Hvib_{ii}^n(t_k + t) - Hvib_{jj}^n(t_k + t)|$$

N_{it} – the number of starting times (initial conditions)

N_{tr} - the number of nuclear trajectories (datasets)

decoherence_times(Hvib, verbosity=0)

Decoherence times and rates for a single trajectory

$$\tau_{ij} = \begin{cases} \sqrt{\frac{12}{5} \frac{1}{\delta E_{ij}}}, & \delta E_{ij} > 0 \\ 10^{10}, & \text{otherwise} \end{cases} \quad r_{ij} = \begin{cases} \frac{1}{\tau_{ij}}, & \text{if } \tau_{ij} > 0 \\ 0, & \text{otherwise} \end{cases}$$

Here,

$$\delta E_{ij} = \sqrt{\frac{1}{N_{steps}} \sum_{p=1}^{N_{steps}} (\Delta E_{ij}(t_p) - \langle \Delta E_{ij} \rangle)^2},$$

$$\langle \Delta E_{ij} \rangle = \frac{1}{N_{steps}} \sum_{p=1}^{N_{steps}} \Delta E_{ij}(t_p),$$

$$\Delta E_{ij}(t_p) = |Hvib_{ii}(t_p) - Hvib_{jj}(t_p)|.$$

N_{steps} – the number of MD steps in this single trajectory

$t_p = p\Delta t$ – are the time-points along the MD trajectory, indexed by the integer subscript for clarity in practical implementation.

decoherence_times_ave_old(Hvib, itimes, nsteps, verbosity=0)

WARNING: this function should not be replaced by the next one!

Decoherence times and rates based on the averaged energy gap fluctuations (averaged by the magnitude)

$$\tau_{ij} = \begin{cases} \sqrt{\frac{12}{5}} \frac{1}{\delta E_{ij}} & , \delta E_{ij} > 0 \\ 10^{10}, & otherwise \end{cases} \quad r_{ij} = \begin{cases} \frac{1}{\tau_{ij}}, & if \tau_{ij} > 0 \\ 0, & otherwise \end{cases}$$

Here,

$$\delta E_{ij} = \sqrt{\frac{1}{N_{steps}} \sum_{p=1}^{N_{steps}} (\Delta E_{ij}(t_p) - \langle \Delta E_{ij} \rangle)^2},$$

$$\langle \Delta E_{ij} \rangle = \frac{1}{N_{steps}} \sum_{p=1}^{N_{steps}} \Delta E_{ij}(t_p),$$

$$\Delta E_{ij}(t_p) = \frac{1}{N_{it} N_{tr}} \sum_{k=1}^{N_{it}} \sum_{n=1}^{N_{tr}} |Hvib_{ii}^n(t_k + t_p) - Hvib_{jj}^n(t_k + t_p)|.$$

N_{it} – the number of starting times (initial conditions)

N_{tr} – the number of nuclear trajectories (datasets)

N_{steps} – the number of MD steps in this single trajectory

$t_p = p\Delta t$ – are the time-points along the MD trajectory, indexed by the integer subscript for clarity in practical implementation.

t_k – are the starting time-points of the MD trajectory.

decoherence_times_ave(Hvib, itimes, nsteps, verbosity=0)

Decoherence times and rates based on the averaged energy gap fluctuations (averaged by the magnitude).

$$\tau_{ij} = \begin{cases} \sqrt{\frac{12}{5}} \frac{1}{\delta E_{ij}} & , \delta E_{ij} > 0 \\ 10^{10}, & otherwise \end{cases} \quad r_{ij} = \begin{cases} \frac{1}{\tau_{ij}}, & if \tau_{ij} > 0 \\ 0, & otherwise \end{cases}$$

Here,

$$\delta E_{ij} = \sqrt{\frac{1}{N_{steps}N_{it}N_{tr}} \sum_{p=1}^{N_{steps}} \sum_{k=1}^{N_{it}} \sum_{n=1}^{N_{tr}} (\Delta E_{ij}^n(t_k + t_p) - \langle \Delta E_{ij} \rangle)^2},$$

$$\langle \Delta E_{ij} \rangle = \frac{1}{N_{steps}N_{it}N_{tr}} \sum_{p=1}^{N_{steps}} \sum_{k=1}^{N_{it}} \sum_{n=1}^{N_{tr}} \Delta E_{ij}^n(t_k + t_p),$$

$$\Delta E_{ij}^n(t_k + t_p) = |Hvib_{ii}^n(t_k + t_p) - Hvib_{jj}^n(t_k + t_p)|.$$

N_{it} – the number of starting times (initial conditions)

N_{tr} - the number of nuclear trajectories (datasets)

N_{steps} – the number of MD steps in this single trajectory

$t_p = p\Delta t$ – are the time-points along the MD trajectory, indexed by the integer subscript for clarity in practical implementation.

t_k – are the starting time-points of the MD trajectory.