# Anti-Hebbian learning with Hebbian spike timing dependent plasticity.

Conor Houghton

CS, U Bristol

Neuroplasticity, July 2018

# Just So



#### How the Elephant Got His Trunk.

https://en.wikipedia.org/wiki/Just\_So\_Stories

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## Hebb's rule

When an axon of cell A is near enough to excite a cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased.

Photo from http://www.cambridgemedicine.org/node/81

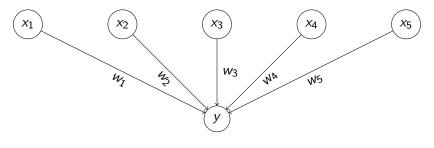
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# Plasticity in AI - perceptron

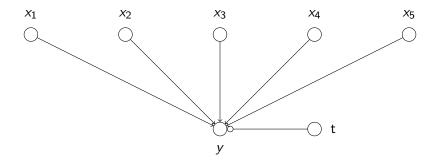
'the embryo of an electronic computer that [the Navy] expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence.'( $^*$ )



 $\Delta w_i = \eta x_i (t-y)$ 

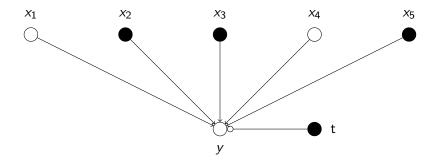
(\*) Frank Rosenblatt

### Plasticity in AI - perceptron - naïve



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## Plasticity in AI - perceptron - training



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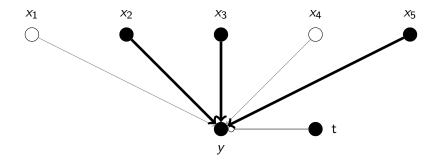
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# Plasticity in AI - perceptron - training

$$\Delta w_i = \eta x_i (t - y)$$

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# Plasticity in AI - perceptron - trained



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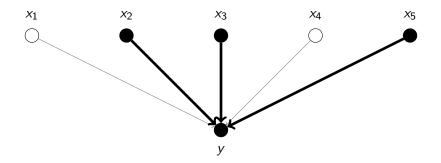
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#### Plasticity in AI - perceptron - recognition

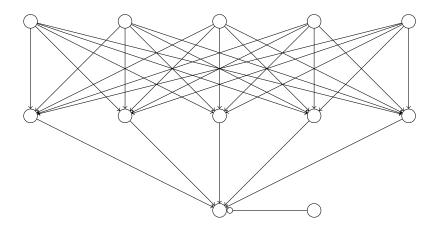


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# Plasticity in AI - back propagation



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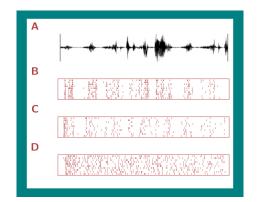
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This is not Hebbian plasticity!

$$\Delta w_i = \eta x_i (t - y)$$

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#### Also neurons have spikes!



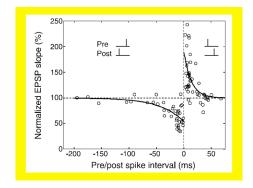
#### Spikes from neurons in the auditory forebrain of zebra finch

Data from Kamal Sen, picture from Houghton and Victor (2012)

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# Spike timing dependent plasticity

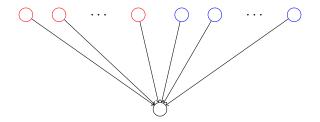


Bi and Poo 1998

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## STDP - learning correlations



Song and Abbott (2000)

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## STDP - correlations

 $x_i = 10(1 + 0.3\xi_i + 0.3\zeta)$ 

with  $\xi_i$  and  $\zeta$  both from  $\mathcal{N}(0,1)$  with inputs constant on intervals drawn from an exponential distribution with mean 20 ms.

Song and Abbott (2000)

## STDP - details

$$\tau_+ \frac{dx_i}{dt} = -x_i + \sum \delta(t - t_i^f)$$

and

$$\tau_{-}\frac{dy}{dt} = -y + \sum \delta(t - t^{n})$$

with

$$\frac{dw_i}{dt} = \eta_+ x_i(t) \sum_n \delta(t - t^n) - \eta_- y(t) \sum_f \delta(t - t_i^f)$$

and hard lower and upper bounds on  $w_i$ :

 $0 \le w_i \le w^{max}$ 

Song and Abbott (2000) ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( ) < ( )

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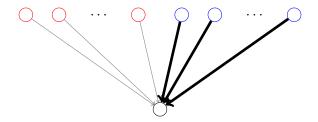
#### STDP - more down than up

$$B = \frac{\eta_-\tau_-}{\eta_+\tau_+} = 1.05$$

Song and Abbott (2000)

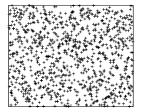
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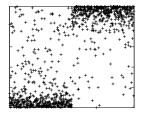
## STDP - correlations learned 1



Song and Abbott (2000)

## STDP - correlations and synapses



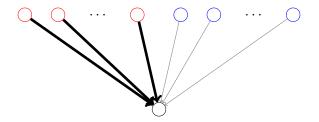


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#### STDP - correlations learned 2



Song and Abbott (2000)

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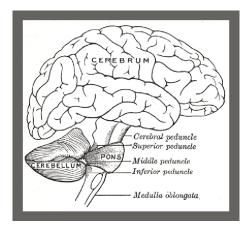
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## Cerebellum



#### Gray's Anatomy (1918)

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## Cerebellum - function - historical view

'Dr Gall was led to the discovery of the function of this organ in the following manner. He was physician to a widow of irreproachable character, who was seized with nervous affections, to which succeeded severe nymphomania. In the violence of a paroxysm, he supported her head, and was struck with the great size and heat of the neck. She stated, that heat and tension of these parts always preceded a paroxysm. He followed out, by numerous observations, the idea, suggested by this occurrence, of connexion between the amative propensity and the cerebellum, and he soon established the point to his own satisfaction.'

George Combe's A System of Phrenology (1853)

## Cerebellum - function



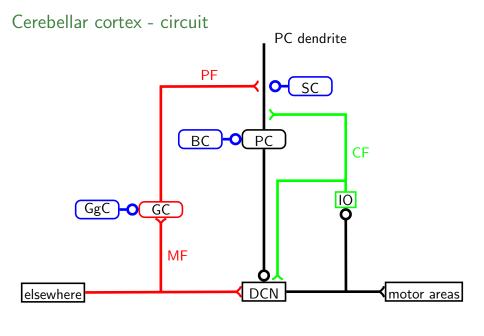
#### Cerebellar Functions by André Thomas (1912)

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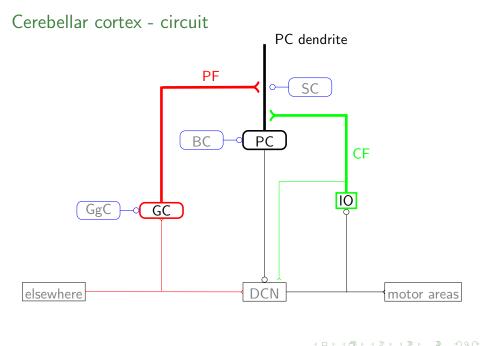


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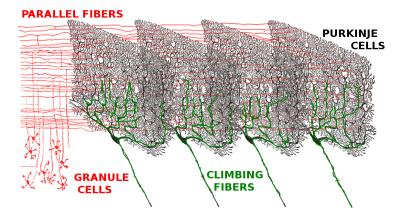


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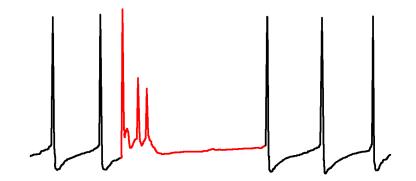
#### Cerebellar cortex - form



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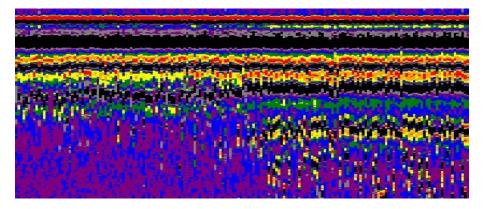
## Complex spike



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## Optogram



By Amelia Burroughs

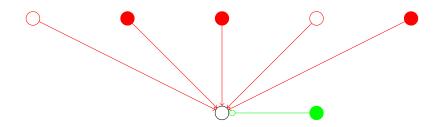
http://www.bristol.ac.uk/neural-dynamics/programme-details/gallery

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#### Cerebellar cortex as a perceptron

This viewpoint can be traced back to David Marr.



## Cerebellar cortex as a perceptron

How does the complex spike supervise the learning?

• Special calcium dependent learning rules.

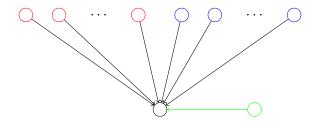
or

• IDEA: normal STDP but with the pauses causing depression of acausal spikes!

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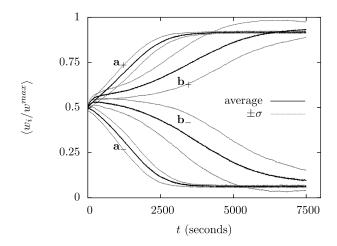
#### Houghton (PLoS ONE, 2014)

# STDP - supervized learning



#### Houghton (PLoS ONE 2014)

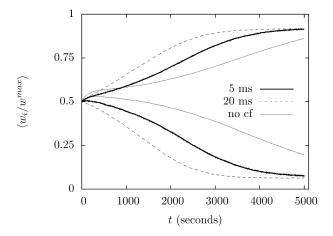
## It works!



#### Houghton (PLoS ONE 2014)

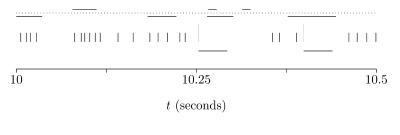
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#### It isn't super sensitive to parameters!



#### Houghton (PLoS ONE 2014)

## More granule cell like behaviour



 $x_i = \lambda_a + \sigma_a \xi_i$ 

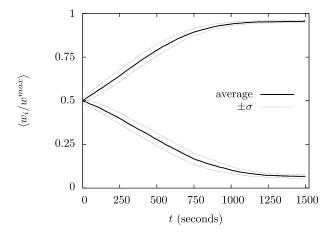
Houghton (PLoS ONE 2014)

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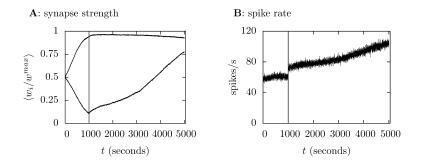
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### It works even better!



#### Houghton (PLoS ONE 2014)

## Switching off the climbing fibre



#### Houghton (PLoS ONE 2014)

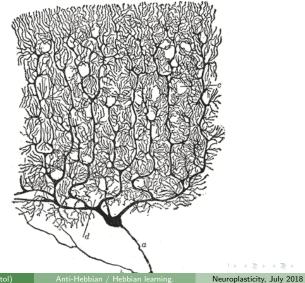
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## Is it true?

Maybe not! It is unlikely that STDP in Purkinje cells is supported by back-propagation of the somatic spike!



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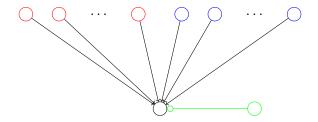
## Is it useful?

Perhaps

- Useful in Al?
- Inhibition might allow supervision in other circuits.

 $\exists \rightarrow$ 

### Inhibition - supervized learning



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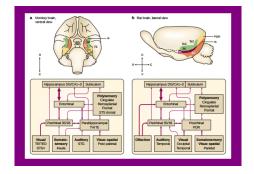
## Is it useful?

Perhaps

Recognition memory

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### Perirhinal cortex



#### MW Brown, JP Aggleton (Nature Reviews Neuroscience, 2001)

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## Recognition memory

TABLE I Mean errors in recognition test, Experiment I (standard deviations in parentheses).											
S 20		T	Vivid pictures			Material Normal pictures			Words		
		20	0	(0)	20	0'2	(0.42)	19.6	2.0	(1.2)	16
40		40	0	(o)	40	1.8	(1.1)	36.4	5.6	(1.3)	28.8
100		80	1.0	(0.0)	96	4.0	(2.2)	90	12	(1.0)	70
200		80	2.0	(2.0)	100	6.8	(1.3)	166	16.8	(4.5)	116
400	•	80	1.0	(3.0)	381	11.4	(5.8)	286	16.6	(7.1)	234
1000		80	4-8	(3.3)	880	0.5	(3.0)	770	15.4	(5.5)	615
4000		160 —			30.2	(16.4)	2490	-54 (5575			
0000		160 —			27.2	(6.1)	6600	_			

(M). Each cell is based on 5 subjects (10 for Vivid pictures)

#### L Standing (The Quarterly journal of experimental psychology, 1973)

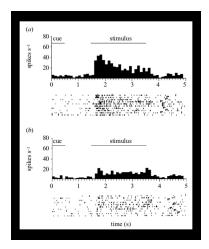
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## Déjà vu

For a few precarious seconds, the chaplain tingled with a weird, occult sensation of having experienced the identical situation before in some prior time or existence. He endeavored to trap and nourish the impression in order to predict, and perhaps even control, what incident would occur next, but the afflatus melted away unproductively, as he had known beforehand it would. *Déjà vu*. The subtle recurring confusion between illusion and reality that was characteristic of paramnesia fascinated the chaplain, and he knew a number of things about it. He knew, for example, that it was called paramnesia

Joseph Heller: Catch 22

### Recognition neurons



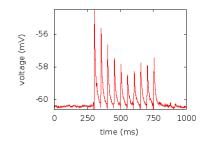
Brown and Bashir 2002

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### Short term depression



From Ola Bykowska

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### Short term depression

Synapse strength is  $w_i u_i$  with

$$\tau_d \frac{du_i}{dt} = 1 - u_i$$

and

 $u_i \rightarrow \lambda_d u_i$ 

at spikes.

Tsodyks and Markram

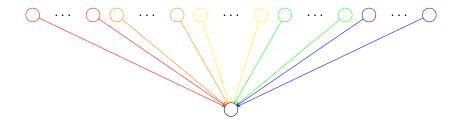
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# STDP / STD - supervised learning

IDEA:

- Lots of potential things to recognize.
- When something is seen the relevant inputs to the recognition neurons fire strongly.
- At first the recognition neuron responds strongly.
- Then STD reduces the input from the synapses.
- However the input continues and this cases depression.
- Next time the same things is seen the recognition neuron doesn't fire.

### STDP / STD - model

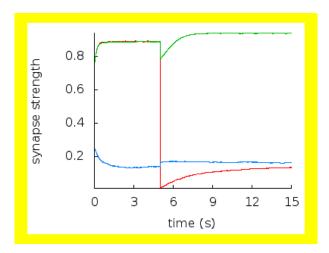


#### Houghton with Luke Milton and Andreas Georgiou

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### It works!



Houghton with Luke Milton and Andreas Georgiou  $(\Box \rightarrow (\Box) + (\Box) \rightarrow (\Xi) \rightarrow$ 

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### THE END

Thanks to the James S McDonnell Foundation for support through a scholar award in cognitive science

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