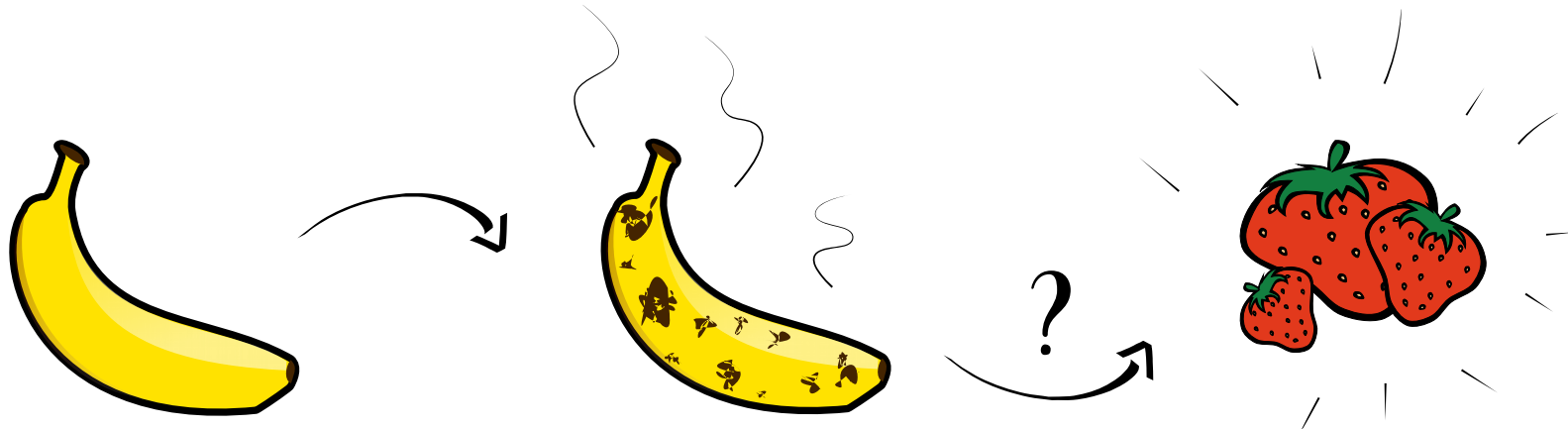


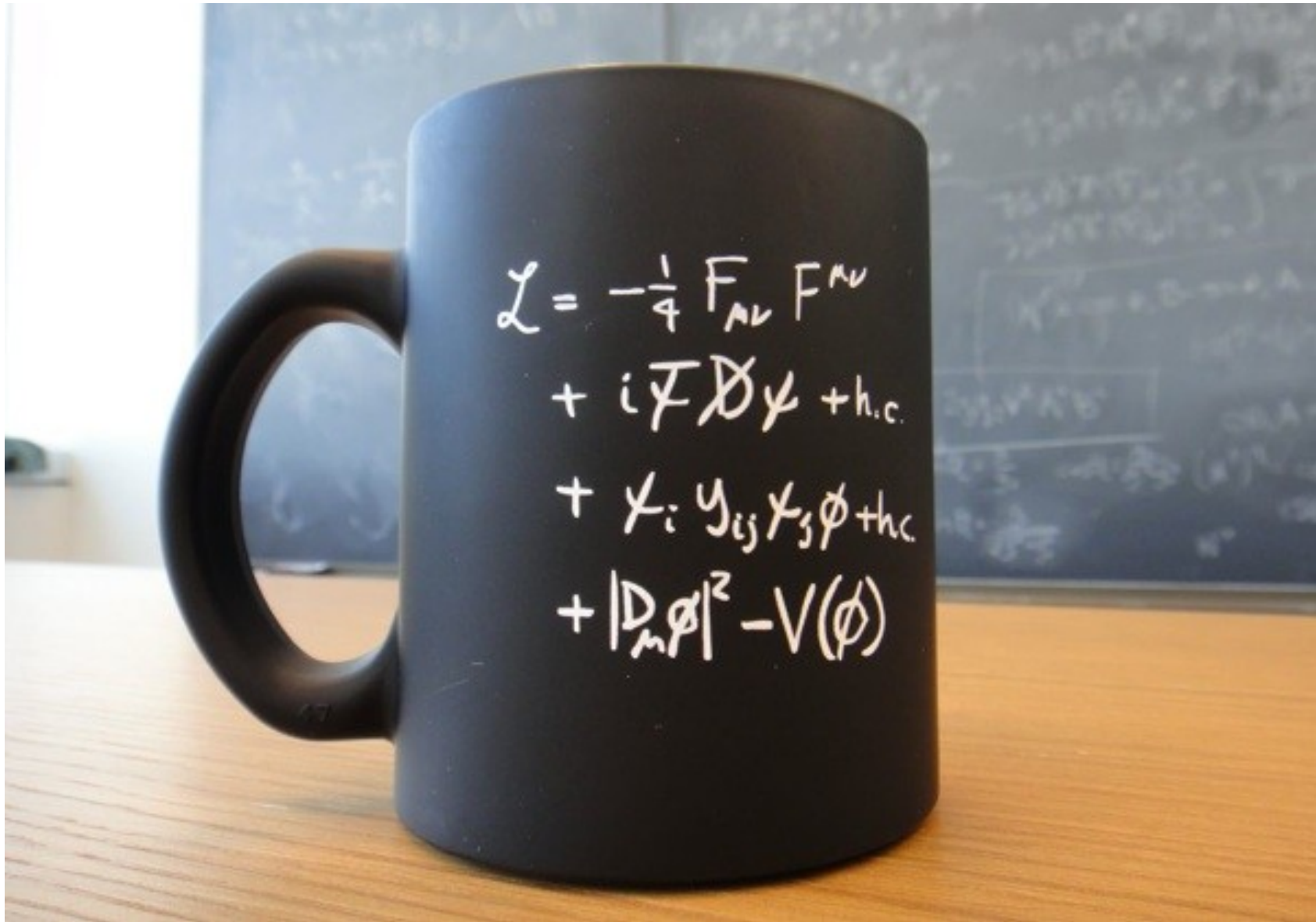
Rare decays with flavor



Julian Heeck

June 8, 2018 @ Neutrino 2018, Heidelberg

The Standard Model



www.quantumdiaries.org, Flip Tanedo

Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned} &U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\ &= \\ &U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_\mu-L_\tau} \times U(1)_{L_\mu+L_\tau-2L_e} . \end{aligned}$$

Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} =$$

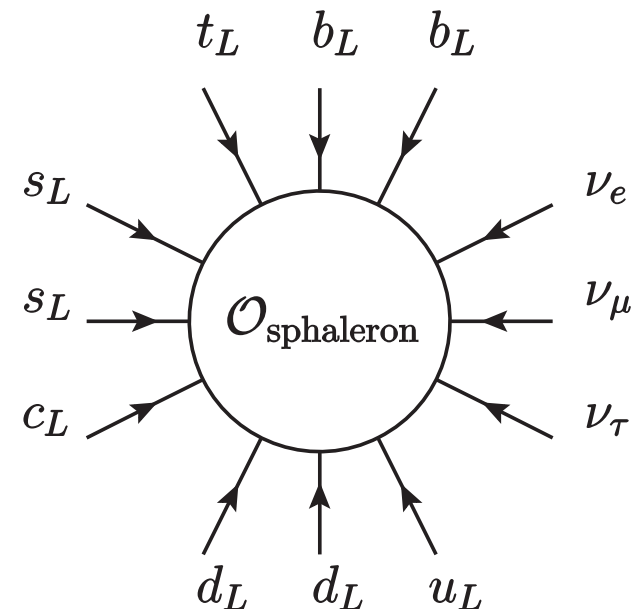
$$\underbrace{U(1)_{B+L}}_{\text{crossed out}} \times U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}.$$

- B+L broken** non-perturbatively,

$$\Delta B = 3 \wedge \Delta L_e = \Delta L_\mu = \Delta L_\tau = 1,$$

but unobservably suppressed at low temperatures by

$$e^{-2\pi/\alpha_w} \sim 10^{-173}. \quad [\text{'t Hooft '76}]$$



Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned}
 &U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\
 &= \\
 &\cancel{U(1)_{B+L}} \times \underbrace{U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}}
 \end{aligned}$$

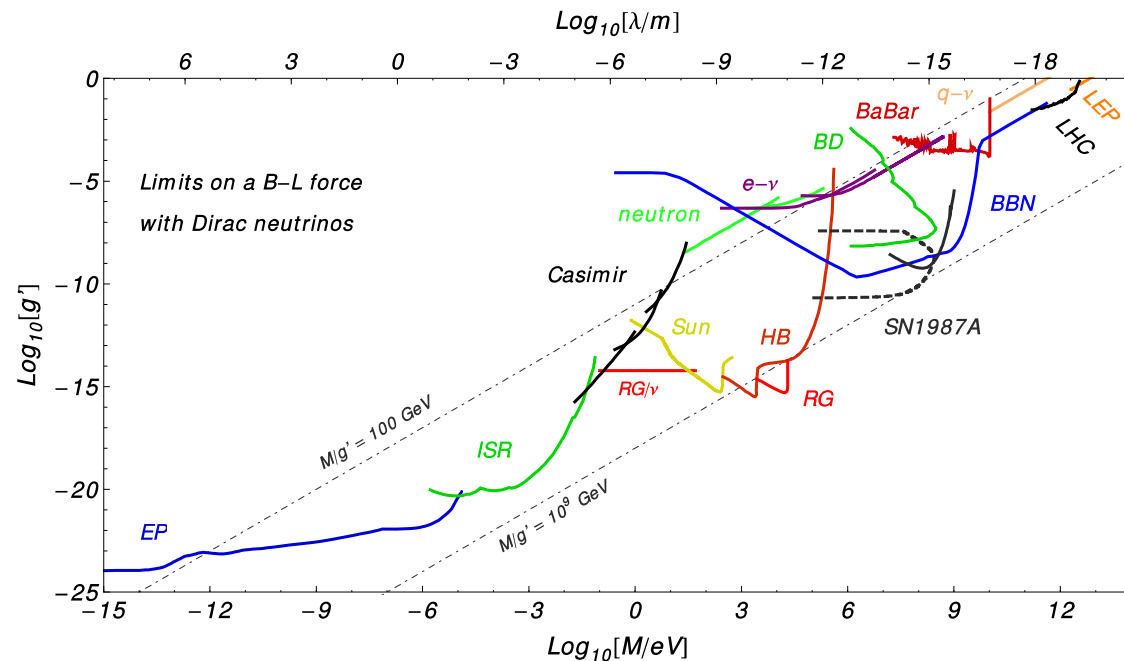
- $B - L$ could be conserved if neutrinos are Dirac.

[Heeck, 1408.6845]

- No $0\nu\beta\beta$.

- Dirac leptogenesis.

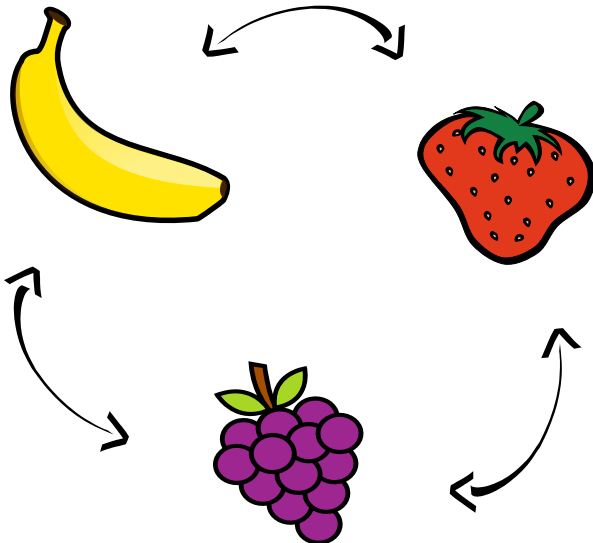
[Dick, Lindner, Ratz, Wright, '00]



Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned}
 &U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\
 &= \\
 &\cancel{U(1)_{B+L}} \times U(1)_{B-L} \times \underbrace{\cancel{U(1)_{L_\mu-L_\tau}} \times \cancel{U(1)_{L_\mu+L_\tau-2L_e}}}_{\cdot}
 \end{aligned}$$



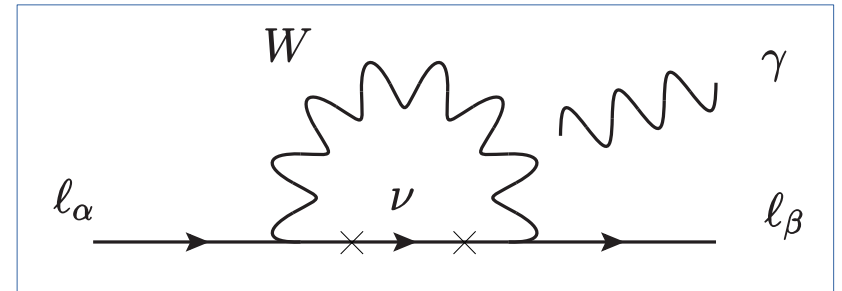
- Broken by $\nu_\alpha \rightarrow \nu_\beta$:

$$\Delta(L_\alpha - L_\beta) = 2.$$

- Charged* lepton flavor violation suppressed by M_ν .

Neutrino mass \Rightarrow charged LFV?

- SM + Dirac neutrinos:
all LFV is GIM suppressed!



$$\frac{\Gamma(l_\alpha \rightarrow l_\beta \gamma)}{\Gamma(l_\alpha \rightarrow l_\beta \nu_\alpha \bar{\nu}_\beta)} = \frac{3\alpha_{\text{EM}}}{32\pi} \left| \sum_{j=2,3} U_{\alpha j} \frac{\Delta m_{j1}^2}{M_W^2} U_{j\beta}^\dagger \right|^2 < 5 \times 10^{-53}.$$

- SM + heavy seesaw neutrinos:

$$\frac{\Gamma(l_\alpha \rightarrow l_\beta \gamma)}{\Gamma(l_\alpha \rightarrow l_\beta \nu_\alpha \bar{\nu}_\beta)} \simeq \frac{3\alpha_{\text{EM}}}{8\pi} \underbrace{|(m_D M_R^{-2} m_D^\dagger)_{\alpha\beta}|^2}_{M_\nu^2 / M_R^2}$$

Not true with fine-tuning or structure in m_D .

[1977: Petcov; Bilenky, Petcov, Pontecorvo; Marciano, Sanda; Lee, Pakvasa, Shrock, Sugawara; Lee, Shrock]

Neutrino mass \Rightarrow charged LFV!

- Neutrino-mass induced charged LFV is **unobservable**.

Observation of CLFV \rightarrow beyond SM *and* beyond M_ν !

- (Only exception: $0\nu\beta\beta$ can probe LFV ($\Delta L_e = 2$) via M_ν .)
- arXiv: many ν -mass models *can* actually give large LFV:
 - Low-scale/inverse/linear/SUSY/type-II seesaw;
 - Radiative seesaw (Zee-Babu, Ma,...). [\[Cai++, 1706.08524\]](#)
- $M_\nu \Leftrightarrow$ LFV connection possible but not necessary.

Symmetries of the Standard Model

- Rephasing lepton and quark fields:

$$\begin{aligned}
 &U(1)_B \times U(1)_{L_e} \times U(1)_{L_\mu} \times U(1)_{L_\tau} \\
 &= \\
 &\underbrace{\cancel{U(1)_{B+L}} \times U(1)_{B-L} \times \cancel{U(1)_{L_\mu-L_\tau}} \times \cancel{U(1)_{L_\mu+L_\tau-2L_e}}}_{\text{approximate symmetry}}
 \end{aligned}$$

Still amazing **approximate symmetry** for charged leptons!

(SM + 3 N_R : $U(1)_{B-L} \times U(1)_{L_\mu-L_\tau} \times U(1)_{L_\mu+L_\tau-2L_e}$ anomaly free.)

[Araki, Heeck, Kubo, 1203.4951. Without N_R just L_i-L_j , He, Joshi, Lew, Volkas, '91]

Charged lepton flavor violation

=

The violation of

$$U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$$

in neutrinoless decays

$$l \rightarrow l' \gamma, l \rightarrow l' l'' l''', \mu \rightarrow e \text{ conv.}, h \rightarrow ll', \text{had} \rightarrow ll', \dots^*$$

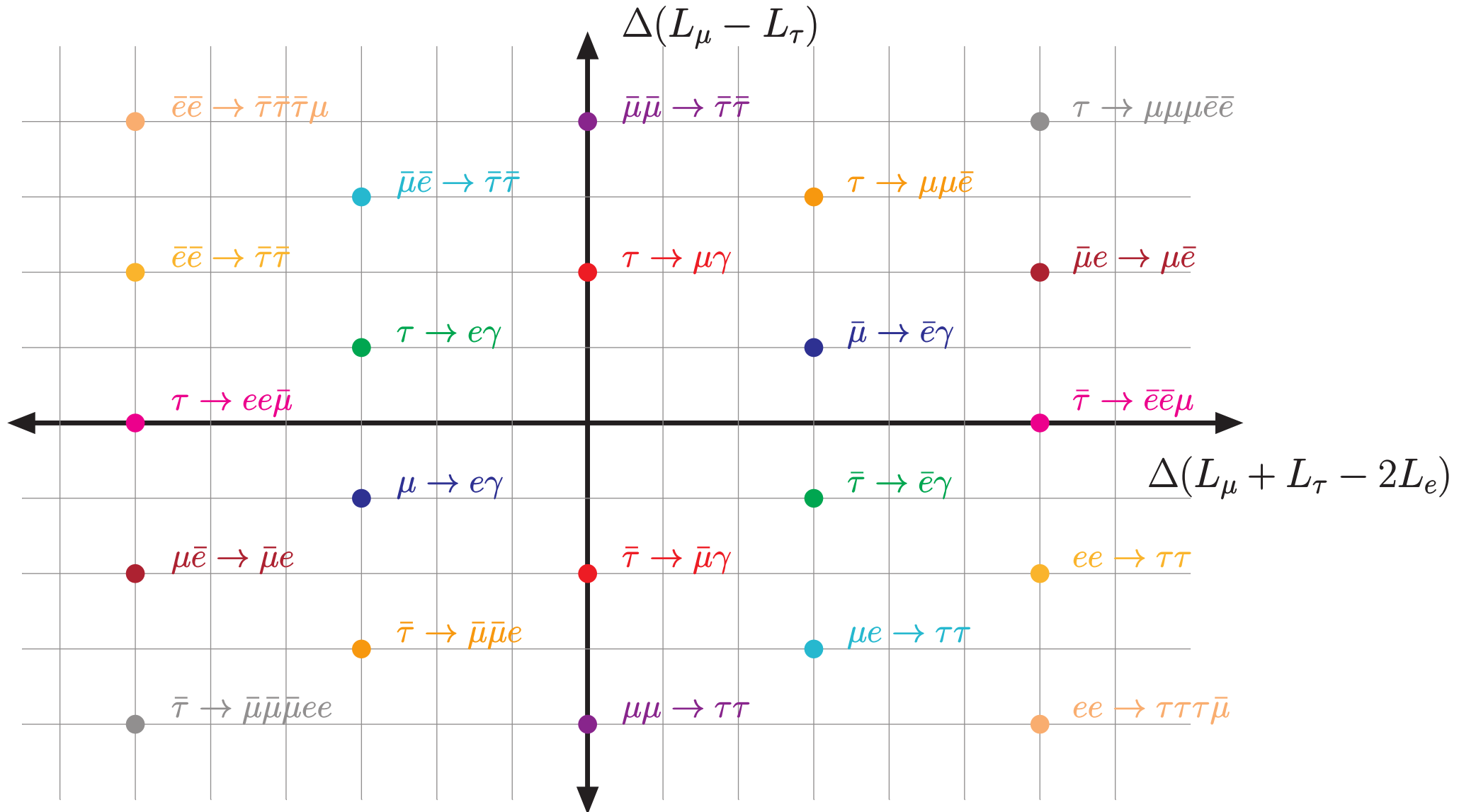
*Assuming *heavy* new physics.

[recent review: Lindner, Platscher, Queiroz, 1610.06587]

$$\Delta B = \Delta L = 0$$

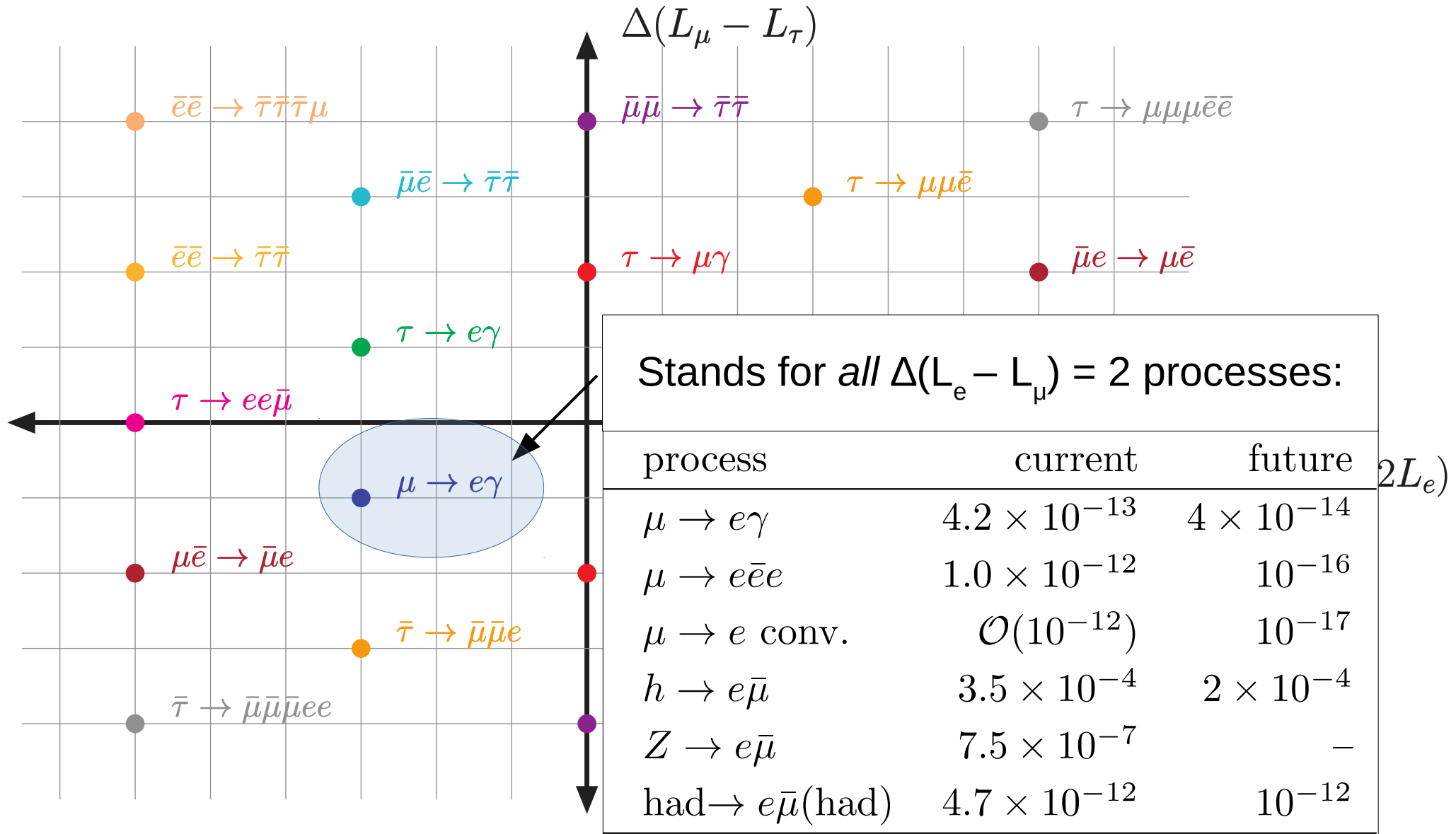
[Heeck, 1610.07623]

[Lew, Volkas, 9410277]



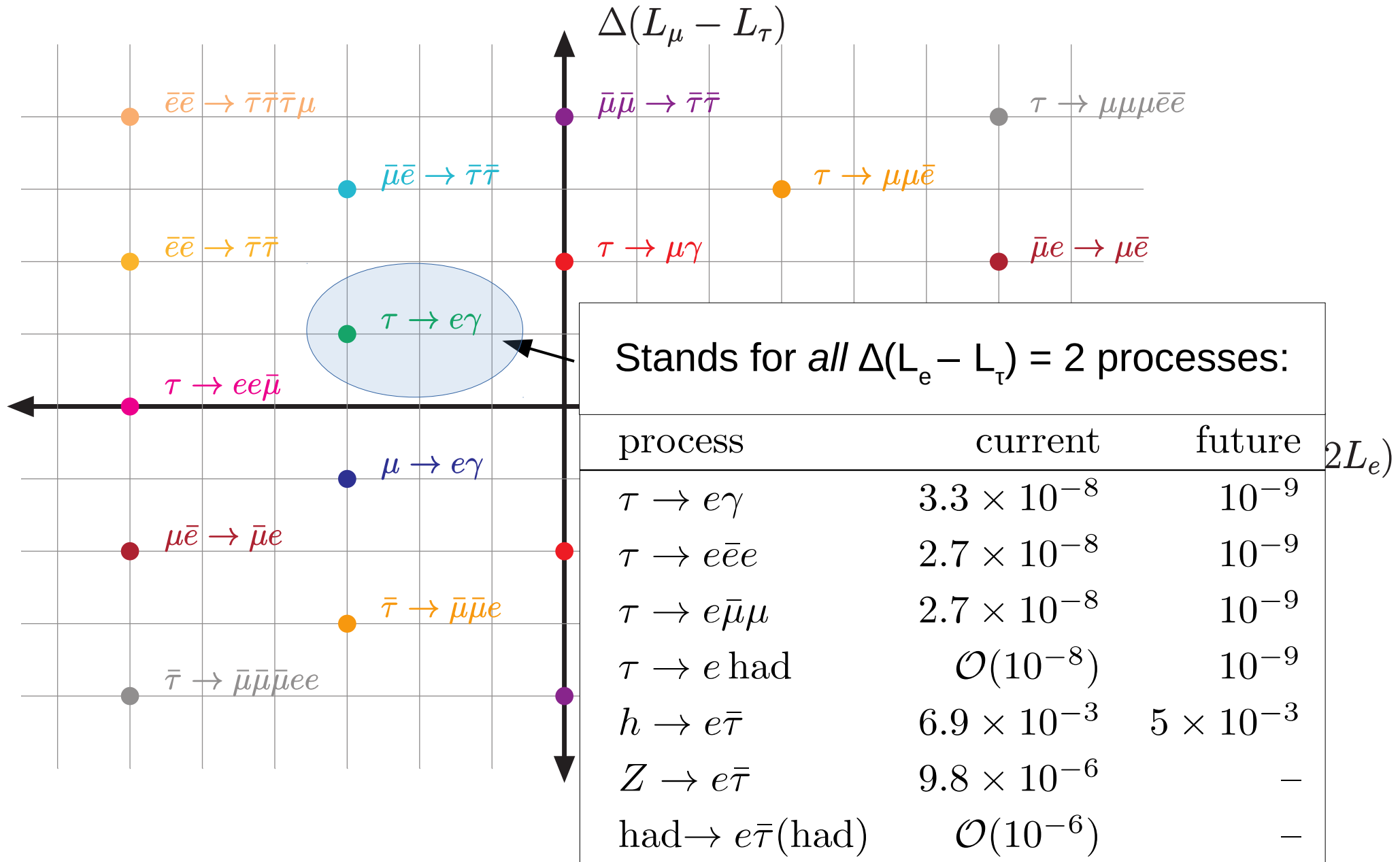
$$\Delta B = \Delta L = 0$$

[Heeck, 1610.07623]
[Lew, Volkas, 9410277]



$$\Delta B = \Delta L = 0$$

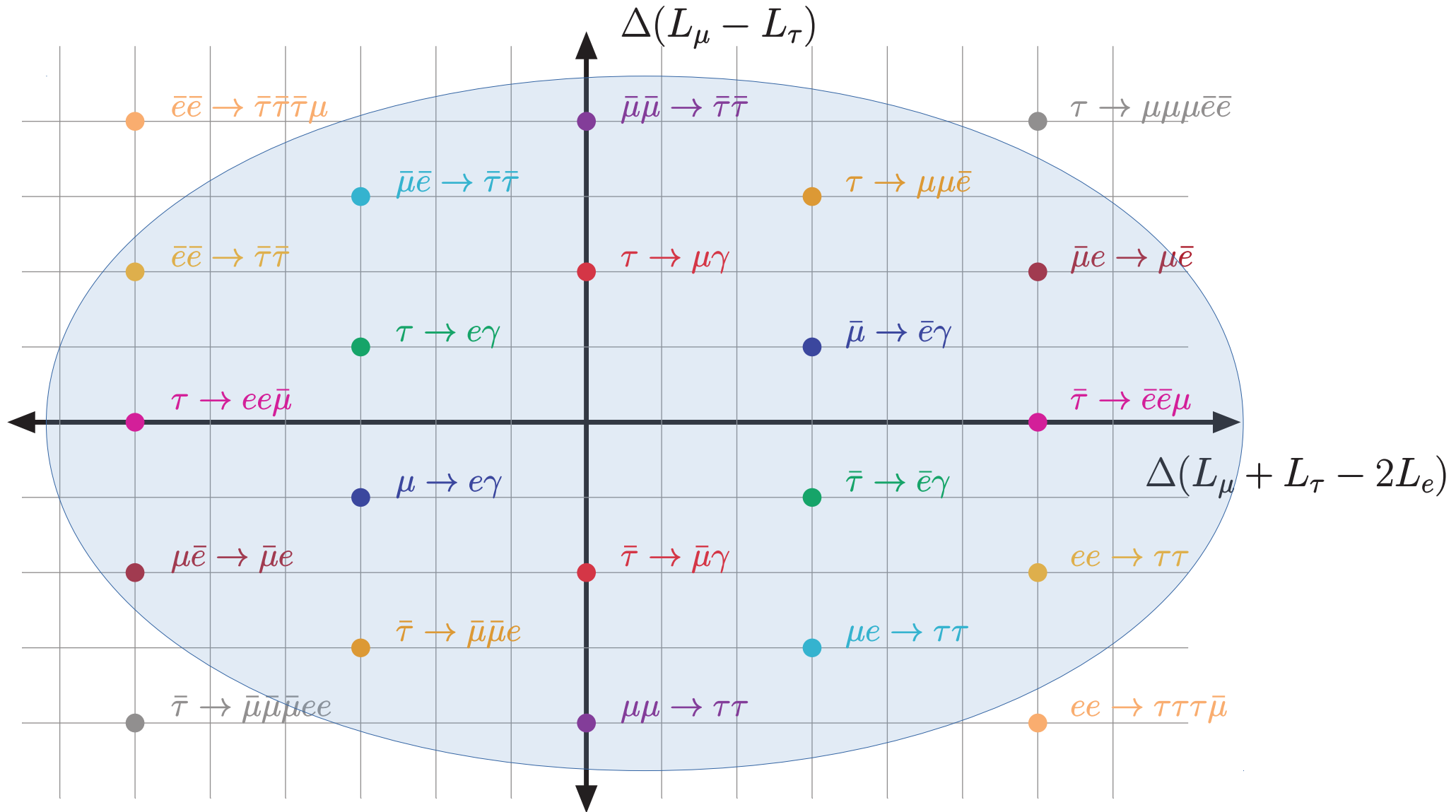
[Heeck, 1610.07623]
[Lew, Volkas, 9410277]



Dimension 6 operators

[Heeck, 1610.07623]

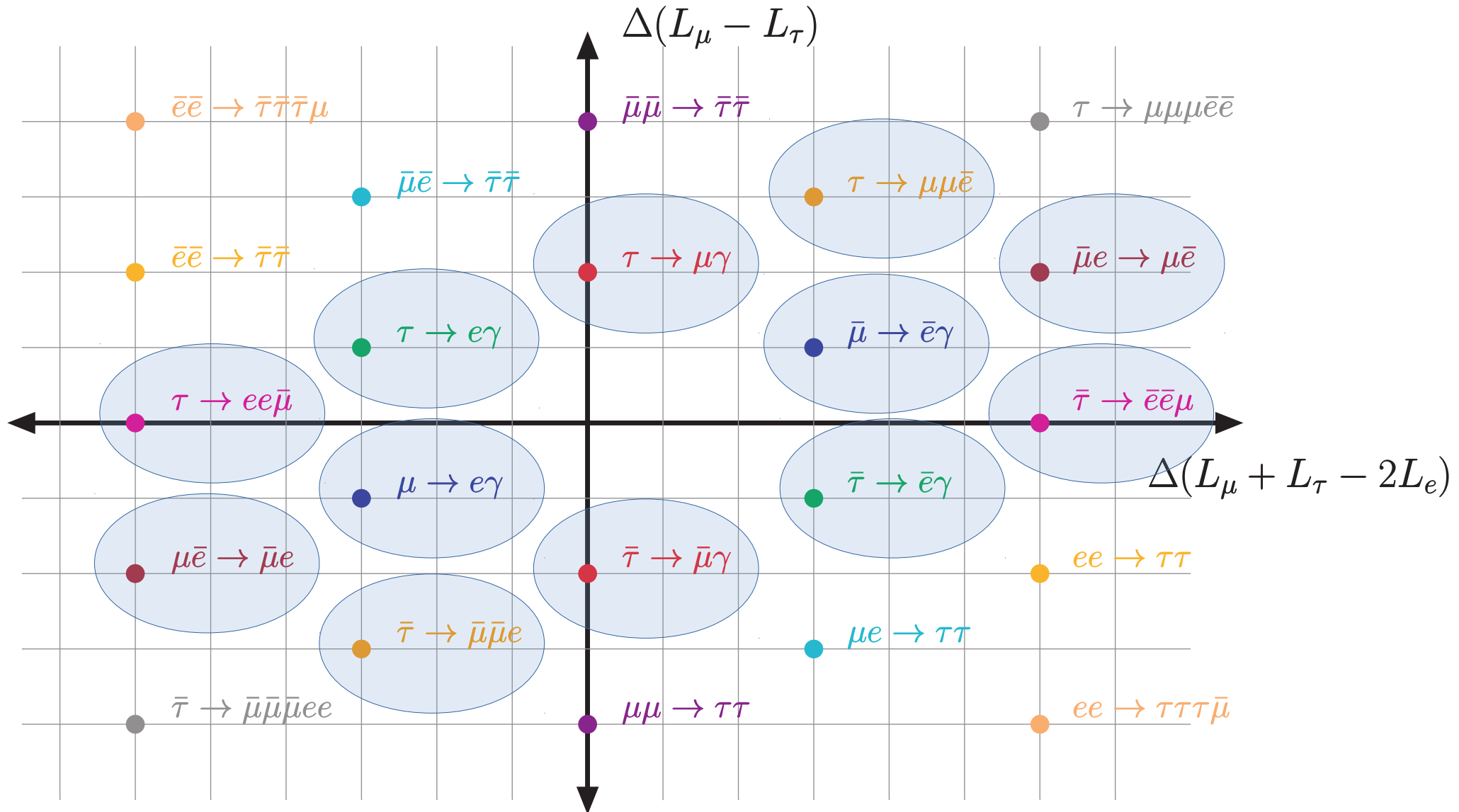
[Lew, Volkas, 9410277]



Currently being probed.

[Heeck, 1610.07623]

[Lew, Volkas, 9410277]



Interpretation of LFV

$$U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$$

Observation of charged lepton flavor violation

\Rightarrow

Remaining symmetry

$$\Delta(L_\alpha - L_\beta) = 2$$

$$U(1)_{L_\alpha + L_\beta - 2L_\gamma}$$

$$\Delta(L_\alpha + L_\beta - 2L_\gamma) = 6$$

$$U(1)_{L_\alpha - L_\beta}$$

$$\Delta(L_\alpha + L_\beta - 2L_\gamma) = 6 \text{ and } \Delta(L_\alpha - L_\beta) = 2$$

$$\mathbb{Z}_2: \ell_\gamma \rightarrow -\ell_\gamma$$

$$\Delta(L_\alpha + L_\beta - 2L_\gamma) = 6 \text{ and } \Delta(L_\alpha + L_\gamma - 2L_\beta) = 6$$

$$\mathbb{Z}_3: (\ell_\alpha, \ell_\beta, \ell_\gamma) \sim (0, 1, 2)$$

$$\Delta(L_\alpha - L_\beta) = 2 \text{ and } \Delta(L_\alpha - L_\gamma) = 2$$

–

$$\Delta(L_\alpha - L_\beta) = 2 \text{ and } \Delta(L_\alpha + L_\gamma - 2L_\beta) = 6$$

–

- *At least* two orthogonal channels required for *full* LFV.
- Flavor violation by higher units more challenging.
- Easy to build models that single out certain channels, e.g. $\tau \rightarrow \mu\gamma$ or $\tau \rightarrow e^-e^+\mu^+$.

Example: $\tau^- \rightarrow e^- e^- \mu^+$

- Conserves $L_\mu - L_\tau$, so impose this!
- Simplest UV model:

	$U(1)_Y$	$U(1)_{L_\mu - L_\tau}$
k^{++}	+2	0
S	0	+1
$N_{e,\mu,\tau}$	0	0, +1, -1

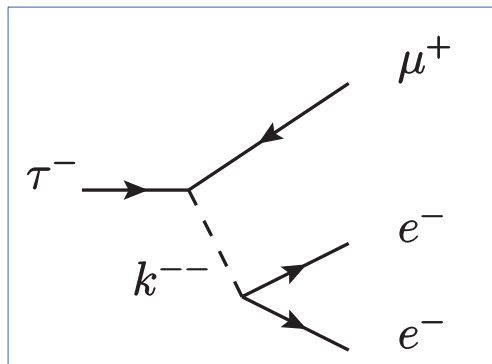
$$(g_{\mu\tau} \bar{\mu}_R^c \tau_R + g_{ee} \bar{e}_R^c e_R) k^{++} + y \bar{L} H N_R + \frac{1}{2} \bar{N}_R^c (M_R^{\text{sym}} + y_S S) N_R.$$

Example: $\tau^- \rightarrow e^- e^- \mu^+$

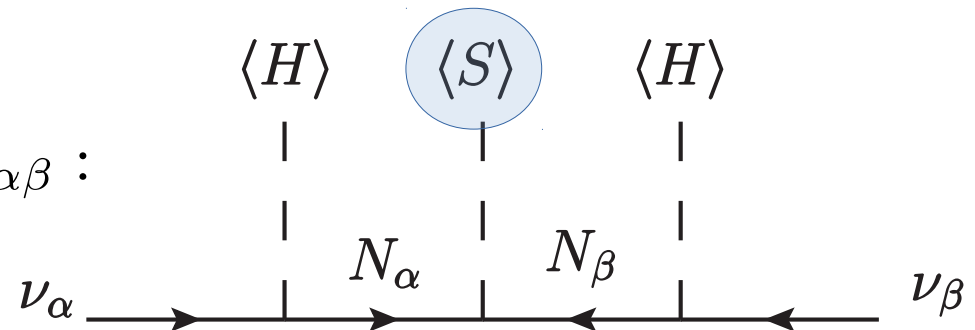
	$U(1)_Y$	$U(1)_{L_\mu - L_\tau}$
k^{++}	+2	0
S	0	+1
$N_{e,\mu,\tau}$	0	0, +1, -1

- Conserves $L_\mu - L_\tau$, so impose this!
- Simplest UV model:

$$(\mathbf{g}_{\mu\tau} \bar{\mu}_R^c \tau_R + \mathbf{g}_{ee} \bar{e}_R^c e_R) k^{++} + y \bar{L} H N_R + \frac{1}{2} \bar{N}_R^c (M_R^{\text{sym}} + y_S \langle S \rangle) N_R.$$



$(M_\nu)_{\alpha\beta} :$



- Only $\tau^- \rightarrow e^- e^- \mu^+$ is unsuppressed by M_ν .

ν oscillations but approximate symmetry in ℓ^- sector.



Baryon number violation

=

The violation of

$$U(1)_B \quad \left[\times U(1)_L \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} \right]$$

in processes

$p \rightarrow \text{leptons} + \text{had}$, $n-\bar{n}$ osc, $pp \rightarrow \ell^+ \ell^{+'}$, $nn \rightarrow \text{had}$, ...*

*Assuming *heavy* new physics.

[Weinberg, '79 & '80]

Baryon number violation

=

The violation of

$$U(1)_B \quad \left[\times U(1)_L \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e} \right]$$

in processes

$p \rightarrow \text{leptons} + \text{had}$, $n-\bar{n}$ osc, $pp \rightarrow \ell^+ \ell^{+'}$, $nn \rightarrow \text{had}$, ...*

*Assuming *heavy* new physics.

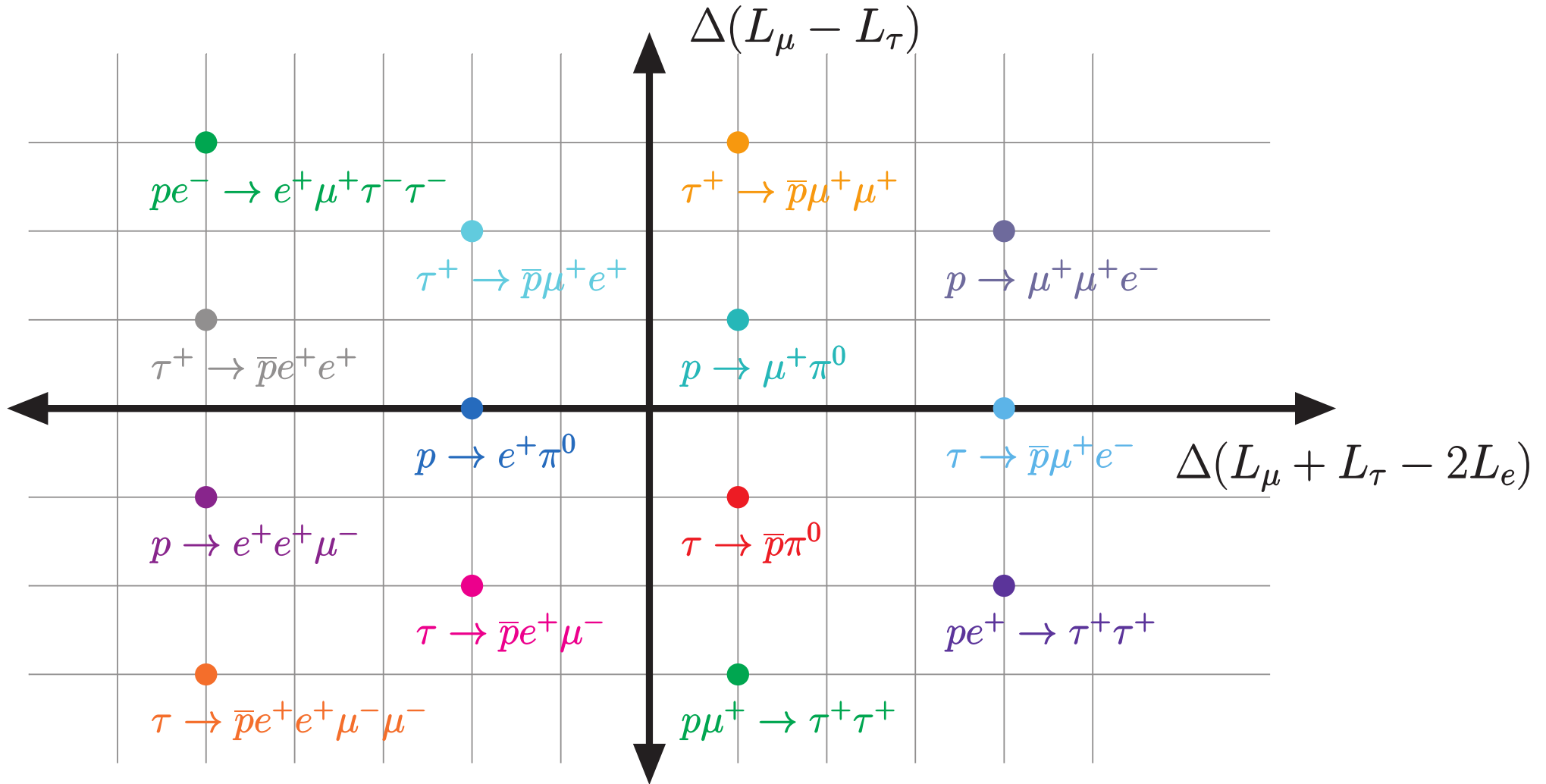
$$\Delta B = 1 \quad \text{and} \quad \Delta L = 1, 3, \dots$$

[Weinberg, '79 & '80]

[Hambye, Heeck, 1712.04871]

[Fonseca, Hirsch, Srivastava, 1802.04814]

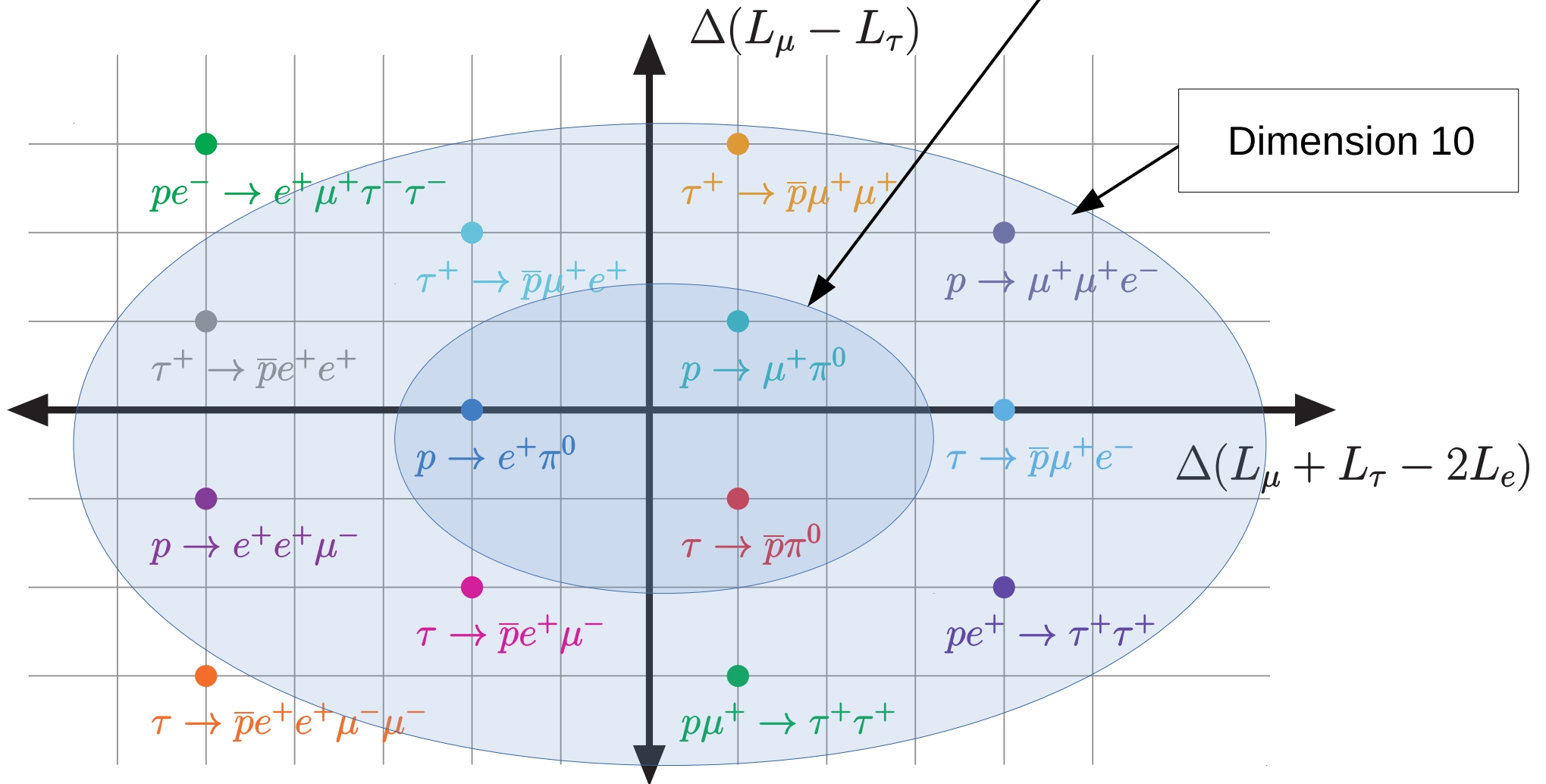
$$\Delta B = \Delta L = 1$$



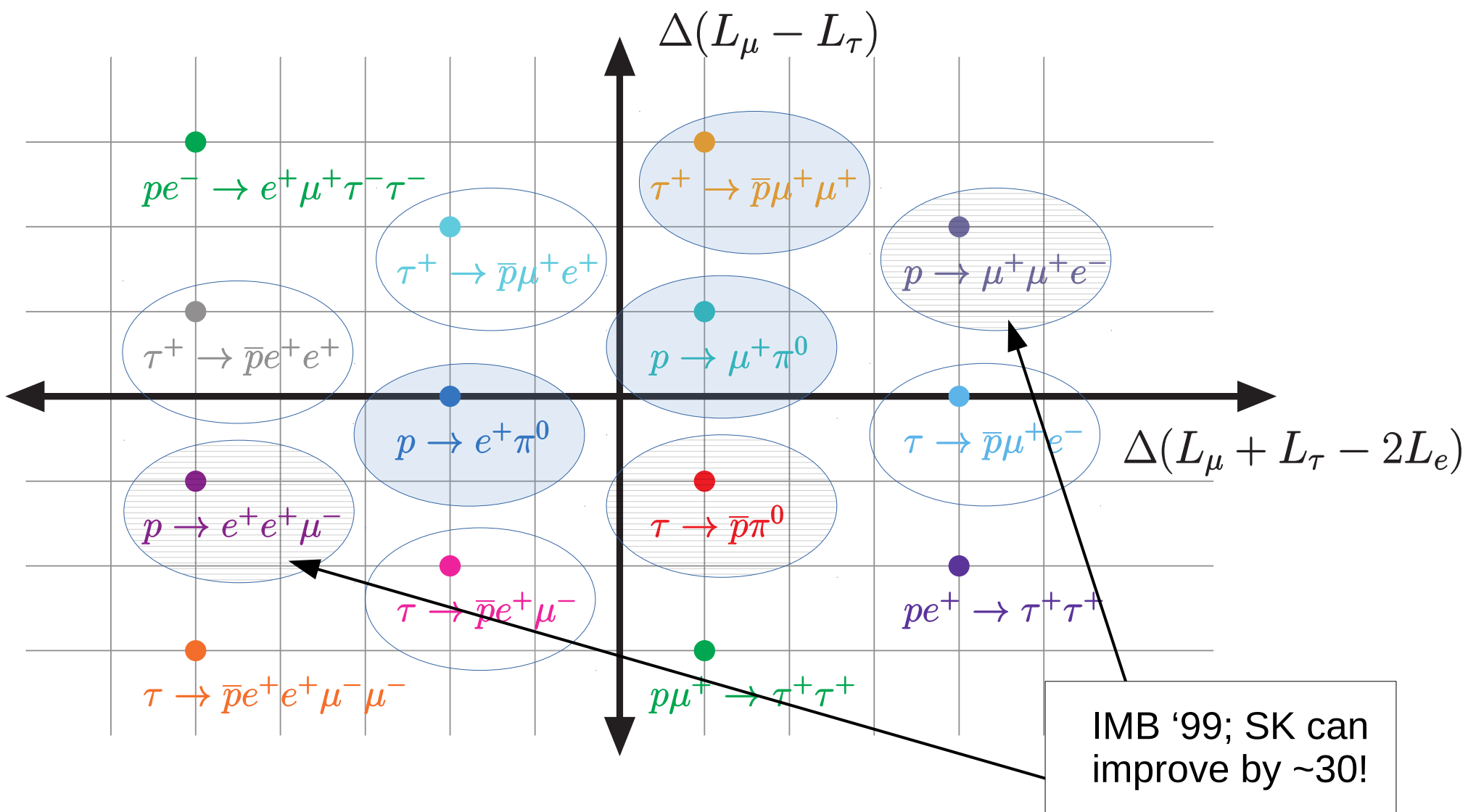
$$\Delta B = \Delta L = 1$$

Dimension 6 operators

Dimension 10



Currently being probed: Old results: Doable:



Lepton-flavored proton decay

- The decay $p \rightarrow e^+e^+\mu^-$ (or $p \rightarrow \mu^+\mu^+e^-$) could be dominant!
- Conserves $B-L$, L_τ , and $L_e+2L_\mu-3L_\tau$ (or $L_\mu+2L_e-3L_\tau$).
- 35 $d=10$ operators of the form $QQQL\bar{L}H\ell/\Lambda^6$.
- Rate suppressed:

$$\Gamma \propto \langle H \rangle^2 \frac{m_p^{11}}{\Lambda^{12}} \sim (10^{33} \text{ yr})^{-1} (100 \text{ TeV}/\Lambda)^{12} .$$

- Easy channels, Super-K can probe 10^{34} yrs!
- UV completion @ 100 TeV could show up in flavor physics.
- Other channels, e.g. $p \rightarrow e^+ \pi^0$, suppressed by ν mass.

[Hambye, Heeck, 1712.04871, PRL]

$$p \rightarrow \mu^+ \mu^+ e^-$$

- Minimal scalar leptoquark example,

$$L_\mu(\phi_1) = 1, L_e(\phi_2) = -1.$$

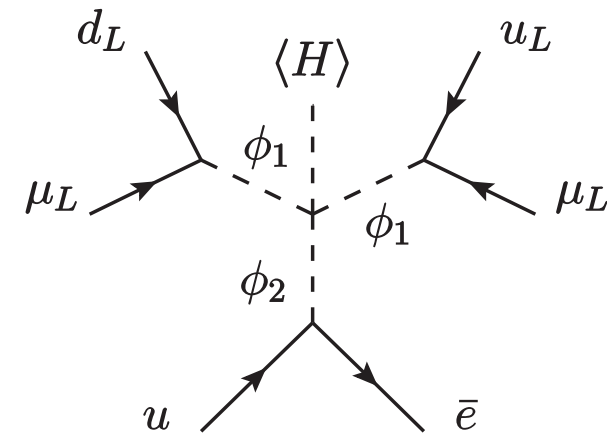
- $L_\mu + 2L_e - 3L_\tau$ ensures simple structure:

$$y_j \bar{L}_\mu \phi_1 Q_j^c + f_j \bar{u}_j \phi_2 L_e + \lambda \phi_1^2 \phi_2 H.$$

$$\phi_1 \sim (\mathbf{3}, \mathbf{3}, -2/3)$$

$$\phi_2 \sim (\mathbf{3}, \mathbf{2}, 7/3)$$

$$\frac{1}{\Lambda^6} \sim \frac{\lambda y_1^2 f_1}{m_{\phi_1}^4 m_{\phi_2}^2}$$



- B-L and lepton flavor conserved: only $p \rightarrow \mu^+ \mu^+ e^-$!

$$p \rightarrow \mu^+ \mu^+ e^-$$

- Minimal scalar leptoquark example,

$$L_\mu(\phi_1) = 1, L_e(\phi_2) = -1.$$

$$\phi_1 \sim (\mathbf{3}, \mathbf{3}, -2/3)$$

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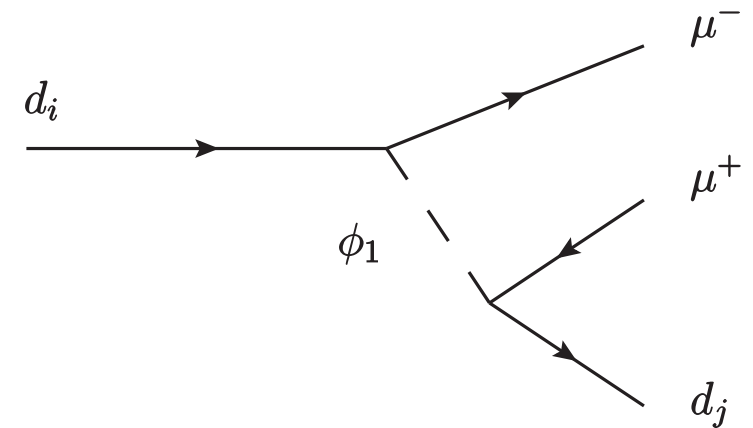
- $L_\mu + 2L_e - 3L_\tau$ ensures simple structure:

$$y_j \bar{L}_\mu \phi_1 Q_j^c + f_j \bar{u}_j \phi_2 L_e + \lambda \phi_1^2 \phi_2 H.$$

- $d = 6$ operators:

$$\frac{y_j \bar{y}_i}{m_{\phi_1}^2} (\bar{L}_\mu Q_j^c)(Q_i L_\mu) + \frac{f_j \bar{f}_i}{m_{\phi_2}^2} (\bar{L}_e u_j)(\bar{u}_i L_e).$$

⇒ Lepton universality violation!



Lepton universality violation

=

The violation of

$SU(3)_\ell$

(in SM broken down to $U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$ by m_ℓ)

in processes

$$Z \rightarrow \ell^- \ell^+, B \rightarrow K^{(*)} \ell^- \ell^+, W \rightarrow \ell \bar{\nu}_\ell, B \rightarrow D^{(*)} \ell \bar{\nu}_\ell, \dots^\dagger$$

[†]Assuming *heavy* new physics.

Lepton universality violation

=

The violation of

$SU(3)_\ell$

(in SM broken down to $U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$ by m_ℓ)

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[†]Assuming *heavy* new physics.

$b \rightarrow s \mu \mu$

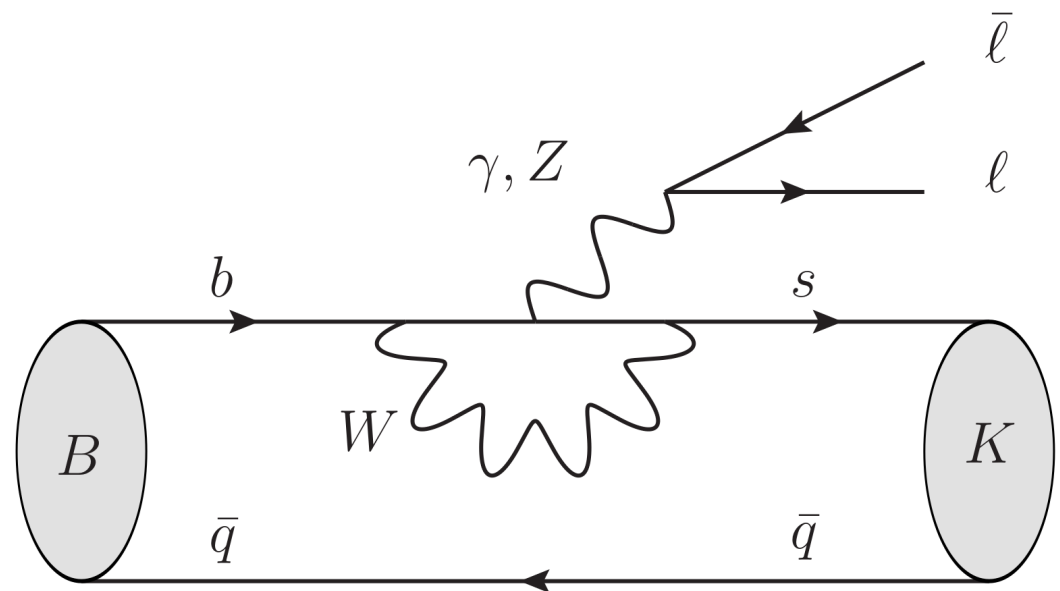
- Hints for **lepton flavor non-universality** in

$$R(K^{(*)}) = \frac{B \rightarrow K^{(*)} \mu^+ \mu^-}{B \rightarrow K^{(*)} e^+ e^-}.$$

- LHCb: $R(K) \sim 0.75$,
 $R(K^*) \sim 0.67$.
- 4-6 σ** improvement with

$$- \frac{1}{(30 \text{ TeV})^2} (\bar{b} \gamma^\alpha P_L s) (\bar{\mu} \gamma_\alpha P_L \mu).$$

- Also explains anomalies in other $b \rightarrow s \mu \mu$ observables.
- Resolution via Z' or leptoquarks.



$b \rightarrow s\mu\mu$

- Hints for **lepton flavor non-universality** in

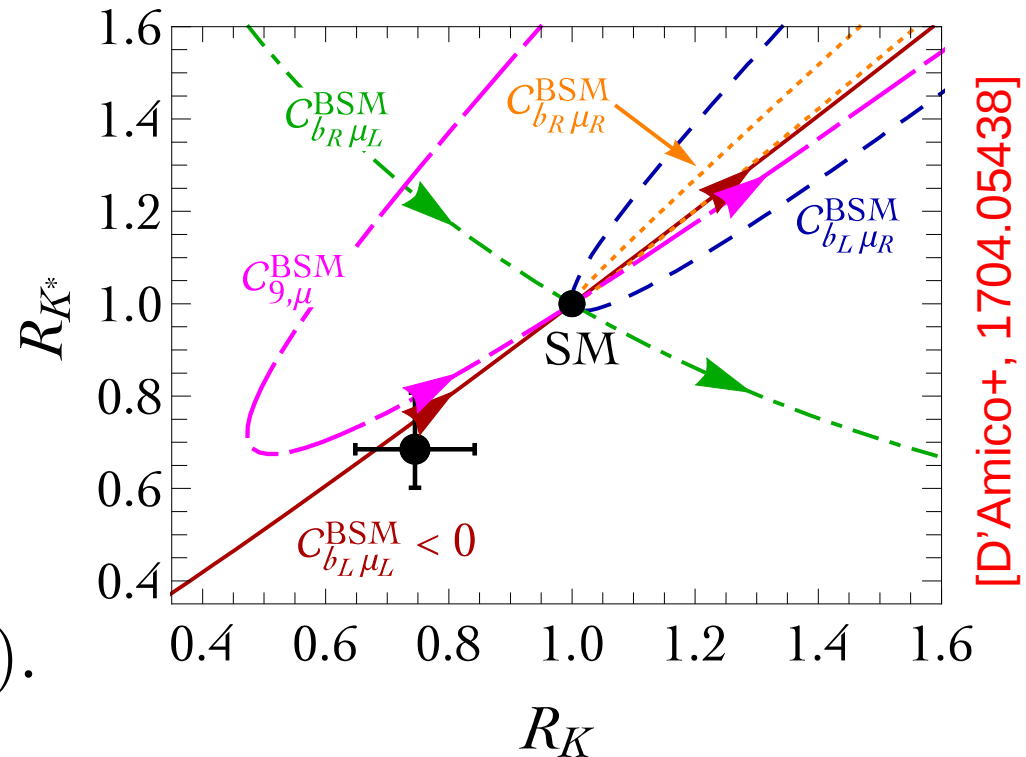
$$R(K^{(*)}) = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}.$$

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- Also explains anomalies in other $b \rightarrow s\mu\mu$ observables.
- Resolution via Z' or leptoquarks.

New physics in μ



Triplet leptoquark and $b \rightarrow s\mu\mu$

- Assume $m_{\phi_1} \ll m_{\phi_2}$, $\phi_1 \sim (\mathbf{3}, \mathbf{3}, -2/3)$, $\phi_2 \sim (\mathbf{3}, \mathbf{2}, 7/3)$.

- $L_\mu + 2L_e - 3L_\tau$ ensures simple structure

$$\mathcal{L} \propto \frac{y_j \bar{y}_i}{m_{\phi_1}^2} (\bar{L}_\mu Q_j^c)(Q_i L_\mu) \propto \frac{y_j \bar{y}_i}{m_{\phi_1}^2} (\bar{L}_\mu \gamma_\alpha P_L L_\mu)(\bar{Q}_j \gamma^\alpha P_L Q_i).$$

- Generates $C_{9,LL}^\mu$ operator preferred by $b \rightarrow s\mu\mu$:

$$m_{\phi_1} \simeq 30 \text{ TeV} \sqrt{y_2 y_3} \quad \text{improves fit by } 4\text{-}6\sigma.$$

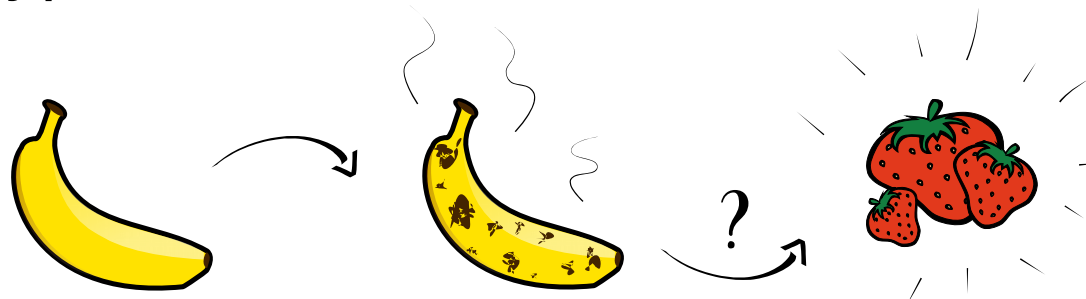
[Alok+, 1703.09247; Dorsner+, 1706.07779; Capdevila+, 1704.05340]

- Flavor symmetry ensures lepton non-universality and kills coupling $QQ\phi_1$ that would lead to d=6 proton decay.

[Hambye, Heeck, 1712.04871, PRL]

Summary

- Charged LFV gives info *complementary* to ν oscillations.
- Is $U(1)_{B+L} \times U(1)_{B-L} \times U(1)_{L_\mu-L_\tau} \times U(1)_{L_\mu+L_\tau-2L_e}$ broken in ℓ^- sector?
 - ⇒ Need to **probe all possible channels!**
- Non-trivial breaking: $\tau \rightarrow ee\bar{\mu}$, $\tau \rightarrow \mu\mu\bar{e}$, $\rho \rightarrow e\bar{\mu}\mu$, $\rho \rightarrow \mu\bar{e}e$,...
- $R(K^{(*)})$ hint at **lepton non-universality**.
- Wait for Mu3e, MEG-II, Belle-II, Mu2e, COMET, DeeMe, LHC(b), Hyper-K,...



Backup

Upcoming CLFV

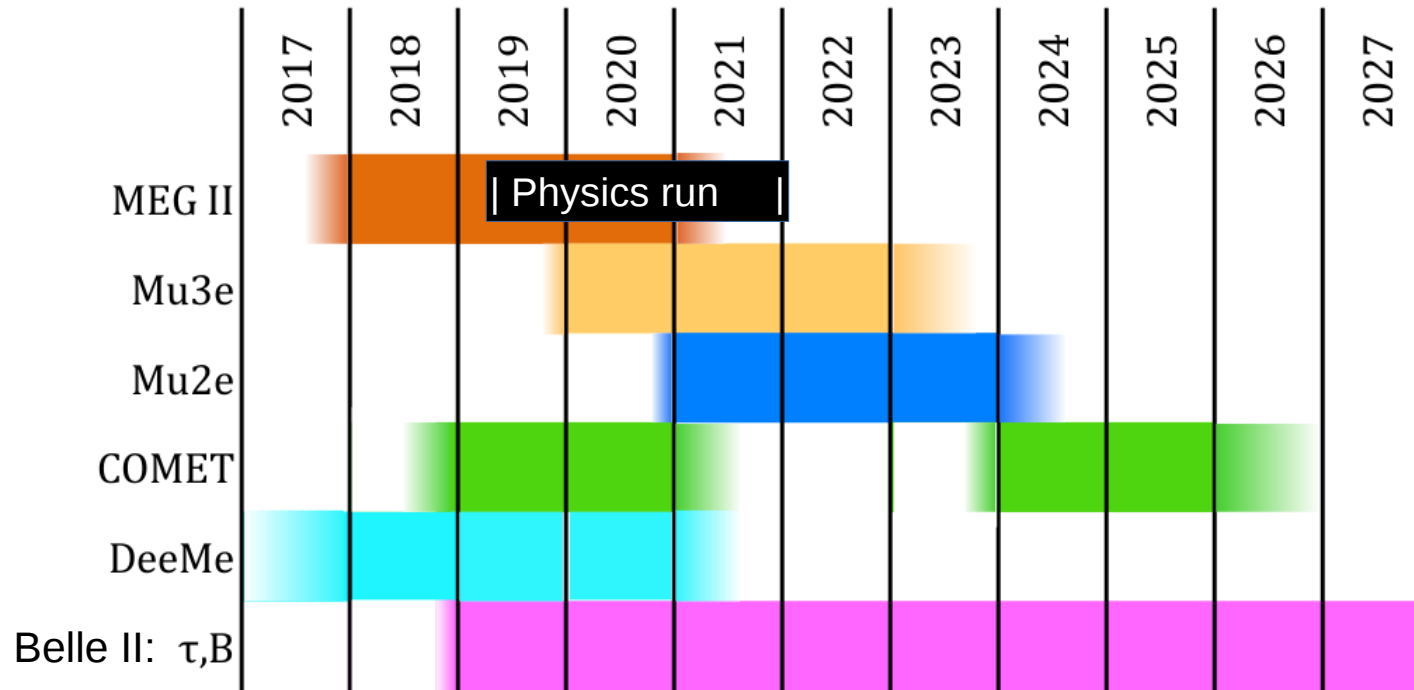


Figure 47. – Projected time lines for different projects searching for CLFV decays. MEG II is expected to start data taking in 2018 after an engineering run in 2017; Mu3e magnet and detectors are expected at the end of 2019; Mu2e foresees three years of data taking starting in 2021; COMET Phase-I is expected to start commissioning and data taking in 2018 for two-three years, followed by a stop to develop and deploy the beamline and detectors for Phase-II; DeeMe is expected to start soon and take data with graphite and silicon carbide targets in sequence; Belle II is scheduled to start data taking at end 2018.

[Calibbi & Signorelli, 1709.00294]

Effective field theory view

- SM symmetry: $G = U(1)_{B-L} \times U(1)_{L_\mu - L_\tau} \times U(1)_{L_\mu + L_\tau - 2L_e}$.
- Effective field theory with Majorana ν :

$$L = L_{\text{SM}} + \frac{\overbrace{\text{LLHH}}^{M_\nu}}{\Lambda} + \underbrace{\sum_j \frac{\mathcal{O}_j}{\Lambda^2} + \sum_j \frac{\mathcal{O}'_j}{\Lambda^3} + \sum_j \frac{\mathcal{O}''_j}{\Lambda^4} + \dots}_{\text{could conserve } G \text{ or subgroup} \Rightarrow \text{'weird' channels dominate!?!}}$$

conserves G ↑ violates G

Scales probed by LFV

LFV channel	Example operator	Coefficient limit	
$\mu \rightarrow e\gamma$	$\bar{L}_\mu \sigma^{\alpha\beta} e_R H B_{\alpha\beta}$	$(6 \times 10^4 \text{ TeV})^{-2}$	
$\mu \rightarrow ee\bar{e}$	$\bar{e}_R \gamma^\alpha \mu_R \bar{e}_R \gamma_\alpha e_R$	$(200 \text{ TeV})^{-2}$	
$\tau \rightarrow ee\bar{\mu}$	$\bar{e}_R \gamma^\alpha \tau_R \bar{e}_R \gamma_\alpha \mu_R$	$(10 \text{ TeV})^{-2}$	
$K_L \rightarrow \bar{\mu}e$	$\bar{s}_L \gamma^\alpha d_L \bar{\mu}_R \gamma_\alpha e_R$	$(460 \text{ TeV})^{-2}$	
$0\nu\beta\beta$	$L_e H H L_e$	$(10^{11} \text{ TeV})^{-1}$	$\Delta L = 2$
$p \rightarrow \bar{e}\pi^0$	$QQQL_e$	$(3 \times 10^{12} \text{ TeV})^{-2}$	$\Delta L = 1$
$p \rightarrow \bar{e}\bar{e}\mu$	$QQQL_e \bar{L}_\mu H e_R$	$(100 \text{ TeV})^{-6}$	$\Delta B = 1$

$b \rightarrow c \ell \bar{\nu}$

- Hints for **lepton flavor non-universality** in

$$R(D^{(*)}) = \frac{\overline{B} \rightarrow D^{(*)} \tau \bar{\nu}}{\overline{B} \rightarrow D^{(*)} \ell \bar{\nu}}.$$

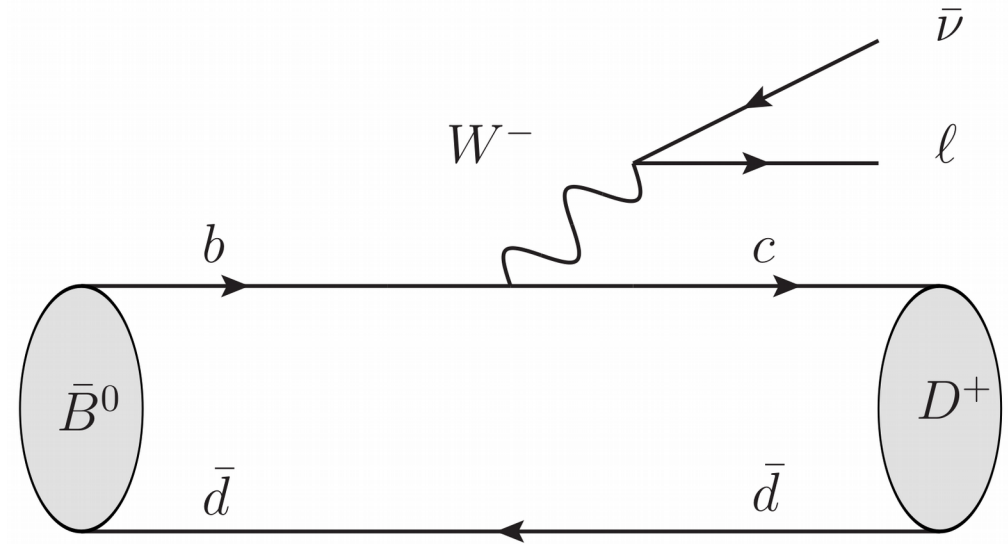
- Belle, **BaBar**, LHCb:

$$R(D^{(*)}) \sim 1.2 R(D^{(*)})_{\text{SM}}.$$

- 4 σ** improvement with

$$\frac{1}{(2 \text{ TeV})^2} (\bar{c} \gamma^\alpha P_L b) (\bar{\tau} \gamma_\alpha P_L \nu).$$

- Strong constraints from $pp \rightarrow \tau\tau, B_c \rightarrow \tau\nu$. [e.g. Alonso, Grinstein, Martin Camalich, PRL '16]
- Resolution via leptoquarks.



$b \rightarrow c \ell \bar{\nu}$

- Hints for **lepton flavor non-universality** in

$$R(D^{(*)}) = \frac{\overline{B} \rightarrow D^{(*)} \tau \bar{\nu}}{\overline{B} \rightarrow D^{(*)} \ell \bar{\nu}}.$$

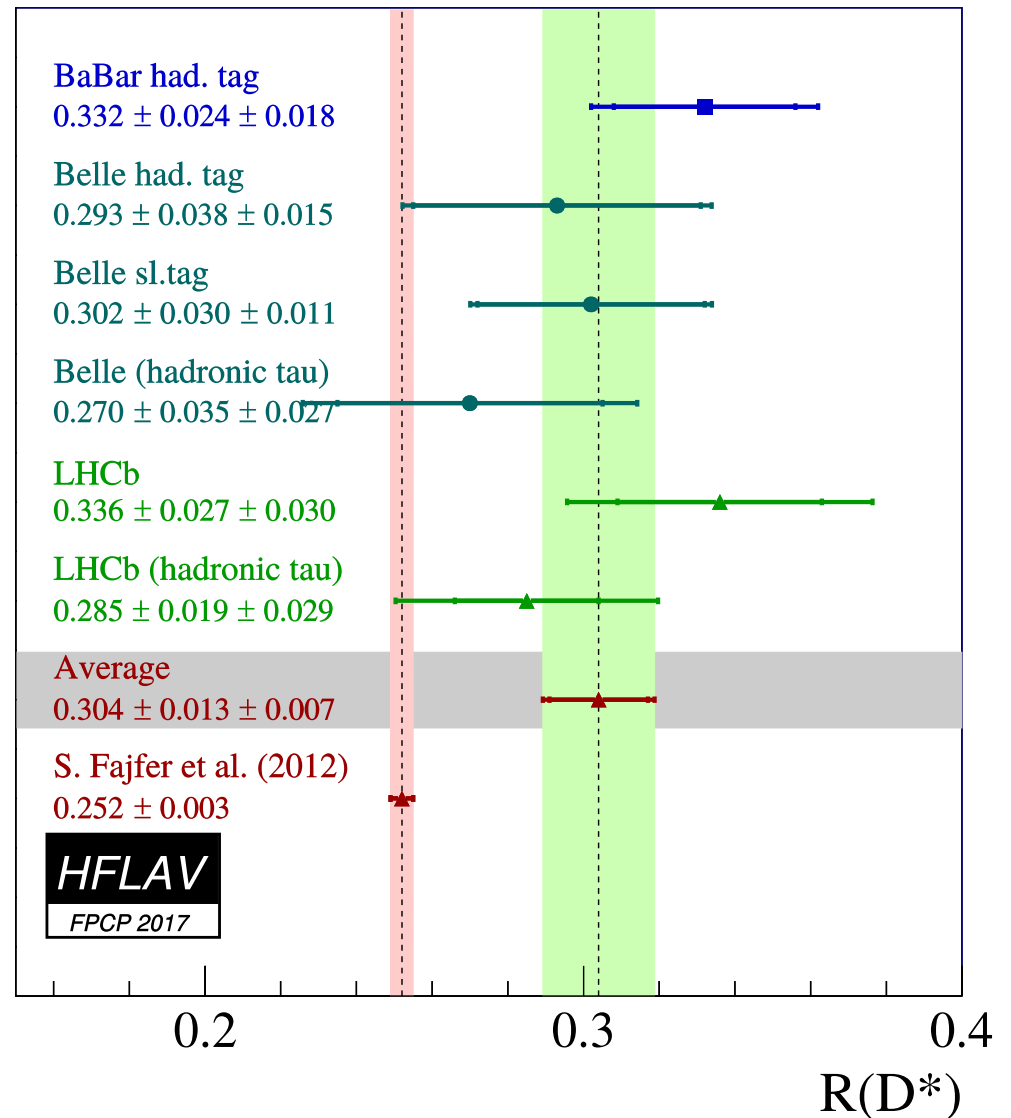
- Belle, **BaBar**, LHCb:
 $R(D^{(*)}) \sim 1.2 R(D^{(*)})_{\text{SM}}$.

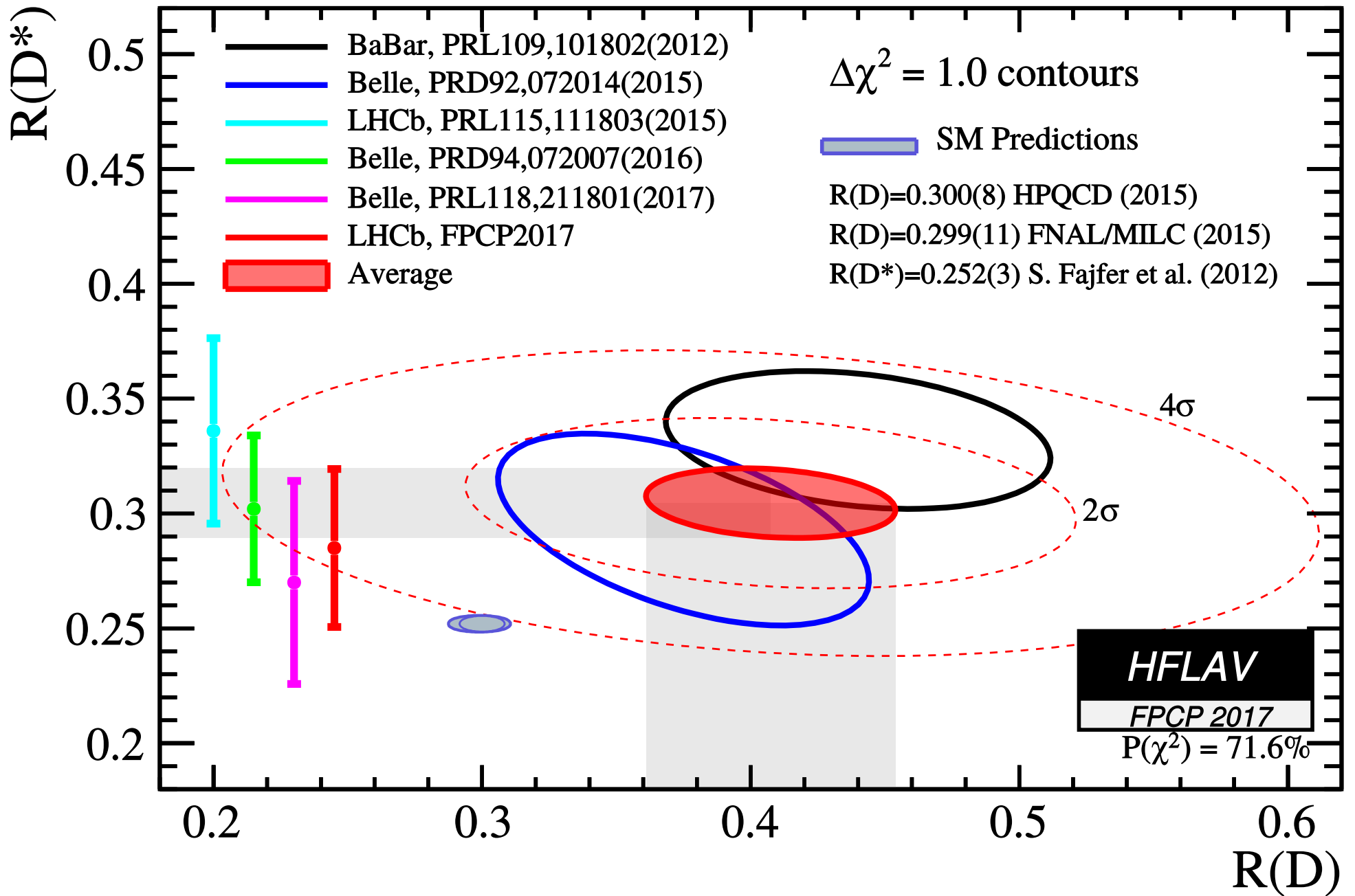
- 4 σ** improvement with

$$\frac{1}{(2 \text{ TeV})^2} (\bar{c} \gamma^\alpha P_L b) (\bar{\tau} \gamma_\alpha P_L \nu).$$

- Strong constraints from $pp \rightarrow \tau\tau, B_c \rightarrow \tau\nu$.
- Resolution via leptoquarks.

[e.g. Alonso, Grinstein, Martin Camalich, PRL '16]





Neutrino oscillation parameters

NuFIT 3.2 (2018)

	Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 4.14$)		Any Ordering
	bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range	3σ range
$\sin^2 \theta_{12}$	$0.307^{+0.013}_{-0.012}$	$0.272 \rightarrow 0.346$	$0.307^{+0.013}_{-0.012}$	$0.272 \rightarrow 0.346$	$0.272 \rightarrow 0.346$
$\theta_{12}/^\circ$	$33.62^{+0.78}_{-0.76}$	$31.42 \rightarrow 36.05$	$33.62^{+0.78}_{-0.76}$	$31.43 \rightarrow 36.06$	$31.42 \rightarrow 36.05$
$\sin^2 \theta_{23}$	$0.538^{+0.033}_{-0.069}$	$0.418 \rightarrow 0.613$	$0.554^{+0.023}_{-0.033}$	$0.435 \rightarrow 0.616$	$0.418 \rightarrow 0.613$
$\theta_{23}/^\circ$	$47.2^{+1.9}_{-3.9}$	$40.3 \rightarrow 51.5$	$48.1^{+1.4}_{-1.9}$	$41.3 \rightarrow 51.7$	$40.3 \rightarrow 51.5$
$\sin^2 \theta_{13}$	$0.02206^{+0.00075}_{-0.00075}$	$0.01981 \rightarrow 0.02436$	$0.02227^{+0.00074}_{-0.00074}$	$0.02006 \rightarrow 0.02452$	$0.01981 \rightarrow 0.02436$
$\theta_{13}/^\circ$	$8.54^{+0.15}_{-0.15}$	$8.09 \rightarrow 8.98$	$8.58^{+0.14}_{-0.14}$	$8.14 \rightarrow 9.01$	$8.09 \rightarrow 8.98$
$\delta_{CP}/^\circ$	234^{+43}_{-31}	$144 \rightarrow 374$	278^{+26}_{-29}	$192 \rightarrow 354$	$144 \rightarrow 374$
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.40^{+0.21}_{-0.20}$	$6.80 \rightarrow 8.02$	$7.40^{+0.21}_{-0.20}$	$6.80 \rightarrow 8.02$	$6.80 \rightarrow 8.02$
$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.494^{+0.033}_{-0.031}$	$+2.399 \rightarrow +2.593$	$-2.465^{+0.032}_{-0.031}$	$-2.562 \rightarrow -2.369$	$\left[+2.399 \rightarrow +2.593 \right]$ $\left[-2.536 \rightarrow -2.395 \right]$

[JHEP 01 (2017) 087 [arXiv:1611.01514], see www.nu-fit.org]

Limits on CLFV

Group	Process	Current	Future
$\Delta(L_e - L_\mu) = 2$	$\mu \rightarrow e\gamma$	4.2×10^{-13} [15]	4×10^{-14} [16]
	$\mu \rightarrow e\bar{e}e$	1.0×10^{-12} [17]	10^{-16} [18]
	$\mu \rightarrow e$ conv.	$\mathcal{O}(10^{-12})$ [19]	10^{-17} [20] [21]
	$h \rightarrow e\bar{\mu}$	3.5×10^{-4} [22]	2×10^{-4} [23]
	$Z \rightarrow e\bar{\mu}$	7.5×10^{-7} [24]	–
	had $\rightarrow e\bar{\mu}$ (had)	4.7×10^{-12} [25]	10^{-12} [26]
$\Delta(L_e - L_\tau) = 2$	$\tau \rightarrow e\gamma$	3.3×10^{-8} [27]	10^{-9} [28]
	$\tau \rightarrow e\bar{e}e$	2.7×10^{-8} [29]	10^{-9} [28]
	$\tau \rightarrow e\bar{\mu}\mu$	2.7×10^{-8} [29]	10^{-9} [28]
	$\tau \rightarrow e$ had	$\mathcal{O}(10^{-8})$ [30]	10^{-9} [28]
	$h \rightarrow e\bar{\tau}$	6.9×10^{-3} [22]	5×10^{-3} [23]
	$Z \rightarrow e\bar{\tau}$	9.8×10^{-6} [31]	–
	had $\rightarrow e\bar{\tau}$ (had)	$\mathcal{O}(10^{-6})$ [32] [33]	–
$\Delta(L_\mu - L_\tau) = 2$	$\tau \rightarrow \mu\gamma$	4.4×10^{-8} [27]	10^{-9} [28]
	$\tau \rightarrow \mu\bar{e}e$	1.8×10^{-8} [29]	10^{-9} [28]
	$\tau \rightarrow \mu\bar{\mu}\mu$	2.1×10^{-8} [29]	10^{-9} [28]
	$\tau \rightarrow \mu$ had	$\mathcal{O}(10^{-8})$ [30]	10^{-9} [28]
	$h \rightarrow \mu\bar{\tau}$	1.2×10^{-2} [7]	5×10^{-3} [23]
	$Z \rightarrow \mu\bar{\tau}$	1.2×10^{-5} [34]	–
		had $\rightarrow \mu\bar{\tau}$ (had)	$\mathcal{O}(10^{-6})$ [32] [33]

TABLE I: CLFV with conserved L and B , omitting CP conjugate processes. Current limits on the branching ratios are at 90% C.L. (h/Z decays at 95% C.L.). A full list of CLFV involving hadrons (had) can be found in the PDG [30].

Group	Process	Current	Future
$\Delta(L_\mu + L_\tau - 2L_e) = 6$	$\tau \rightarrow ee\bar{\mu}$	1.5×10^{-8} [29]	10^{-9} [28]
$\Delta(L_\tau + L_e - 2L_\mu) = 6$	$\tau \rightarrow \mu\mu\bar{e}$	1.7×10^{-8} [29]	10^{-9} [28]
$\Delta(L_e + L_\mu - 2L_\tau) = 6$	$\mu e \rightarrow \tau\tau$	–	–

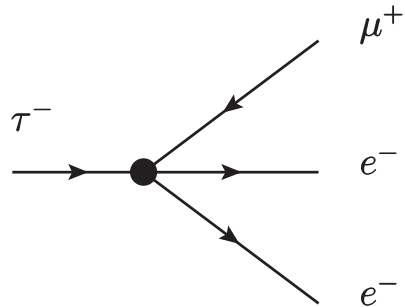
TABLE II: CLFV with conserved L and B , omitting CP conjugate processes. Current limits at 90% C.L.

Group	Process	Current	Future
$\Delta L_e = 2$	$0\nu\beta\beta$	$\mathcal{O}(10^{25}$ yr) [44]	10^{26} yr [44]
	had $\rightarrow ee$ had	6.4×10^{-10} [45]	10^{-12} [26]
$\Delta L_\mu = 2$	had $\rightarrow \mu\mu$ had	8.6×10^{-11} [46]	10^{-12} [26]
$\Delta L_\tau = 2$	had $\rightarrow \tau\tau$ had	–	–
$\Delta(L_e + L_\mu) = 2$	$\mu \rightarrow \bar{e}$ conv.	3.6×10^{-11} [47]	$\ll 10^{-11}$ [48]
	had $\rightarrow \mu e$ had	5.0×10^{-10} [45]	10^{-12} [26]
$\Delta(L_e + L_\tau) = 2$	$\tau \rightarrow \bar{e}$ had	2.0×10^{-8} [49]	10^{-9} [28]
	had $\rightarrow \tau e$ had	–	–
$\Delta(L_\mu + L_\tau) = 2$	$\tau \rightarrow \bar{\mu}$ had	3.9×10^{-8} [49]	10^{-9} [28]
	had $\rightarrow \tau\mu$ had	–	–

TABLE IV: Processes violating total lepton number L by two units (90% C.L. limits), assuming conserved baryon number.

[Heeck, 1610.07623]

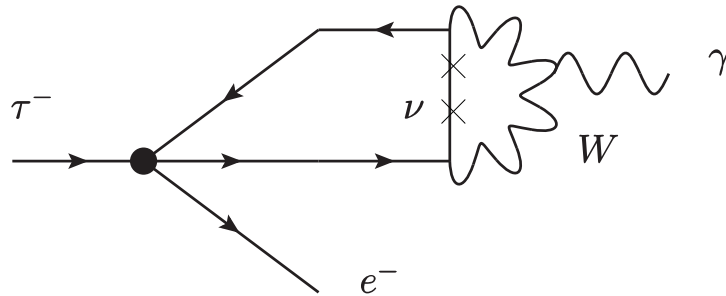
$\tau^- \rightarrow e^- e^- \mu^+$ plus M_ν breaks U(1)



$$\propto \frac{1}{\Lambda^2}$$



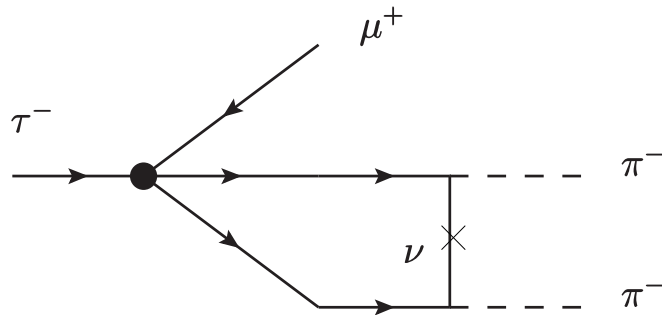
Conserves $L_\mu - L_\tau$



$$\propto \frac{1}{\Lambda^2} \propto \frac{\Delta m_\nu^2}{M_W^2}$$

Additional suppression factors from **loops**, **phase space** and **lepton mass flips** depending on actual operator.

\Rightarrow All heavily **suppressed!**



$$\propto \frac{1}{\Lambda^2} \frac{(m_\nu)_{ee}}{m_e}$$

Baryon number violation

- Can also do LFV with $\Delta B \neq 0$!
- Example: proton decay ($\Delta B = 1$).
- Super-K limits on $p \rightarrow e^+\pi^0, \mu^+\pi^0$ are 10^{34} yrs!
- More interesting for flavor: $p \rightarrow \bar{\ell}\ell\ell$:

channel	$(\Delta L_e, \Delta L_\mu)$	limit/years
$p \rightarrow e^+e^+e^-$	(1, 0)	793×10^{30}
$p \rightarrow e^+\mu^+\mu^-$	(1, 0)	359×10^{30}
$p \rightarrow \mu^+e^+e^-$	(0, 1)	529×10^{30}
$p \rightarrow \mu^+\mu^+\mu^-$	(0, 1)	675×10^{30}
$p \rightarrow \mu^+\mu^+e^-$	(-1, 2)	359×10^{30}
$p \rightarrow e^+e^+\mu^-$	(2, -1)	529×10^{30}

IMB '99; SK can improve by ~30!

Different flavor from $p \rightarrow \ell^+\pi^0$!

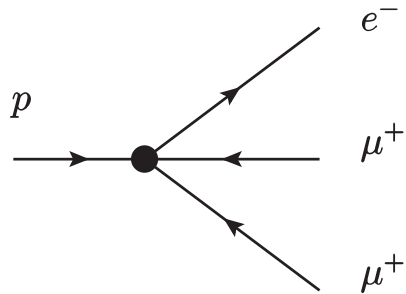
d=10 operators for $p \rightarrow \bar{\ell}\ell\ell$

$$\begin{aligned}
 \mathcal{O}_{1,2}^{10} &= (QQ)_{1,1} (QL)_{1,3} (\bar{L}\ell\bar{H})_{1,3}, \\
 \mathcal{O}_{3,4}^{10} &= (QQ)_{1,1} (QL)_{1,3} (\bar{\ell}LH)_{1,3}, \\
 \mathcal{O}_5^{10} &= (QQ)_1 (LL)_3 (\bar{\ell}QH)_{1,3}, \\
 \mathcal{O}_6^{10} &= (QQ)_1 (\ell\ell)_1 (\bar{\ell}Q\bar{H})_1, \\
 \mathcal{O}_7^{10} &= (QQ)_1 (LL)_3 (\bar{L}uH)_{1,3}, \\
 \mathcal{O}_8^{10} &= (QQ)_1 (\ell\ell)_1 (\bar{L}u\bar{H})_1, \\
 \mathcal{O}_9^{10} &= (QQ)_1 (u\ell)_1 (\bar{L}\ell\bar{H})_1, \\
 \mathcal{O}_{10}^{10} &= (QQ)_1 (u\ell)_1 (\bar{\ell}LH)_{1,3}, \\
 \mathcal{O}_{11,12}^{10} &= (QL)_{1,3} (QL)_{3,3} (\bar{\ell}QH)_{3,3}, \\
 \mathcal{O}_{13,14}^{10} &= (QL)_{1,3} (QL)_{3,3} (\bar{L}uH)_{3,3}, \\
 \mathcal{O}_{15,16}^{10} &= (QL)_{1,3} (u\ell)_{1,1} (\bar{\ell}QH)_{1,3}, \\
 \mathcal{O}_{17,18}^{10} &= (QL)_{1,3} (d\ell)_{1,1} (\bar{\ell}Q\bar{H})_{1,3}, \\
 \mathcal{O}_{19}^{10} &= (QL)_3 (u\ell)_1 (\bar{L}uH)_{1,3}, \\
 \mathcal{O}_{20,21}^{10} &= (QL)_{1,3} (d\ell)_{1,1} (\bar{L}u\bar{H})_{1,3},
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{O}_{22,23}^{10} &= (QL)_{1,3} (u\ell)_{1,1} (\bar{L}d\bar{H})_{1,3}, \\
 \mathcal{O}_{24,25}^{10} &= (QL)_{1,3} (ud)_{1,1} (\bar{L}\ell\bar{H})_{1,3}, \\
 \mathcal{O}_{26,27}^{10} &= (QL)_{1,3} (ud)_{1,1} (\bar{\ell}LH)_{1,3}, \\
 \mathcal{O}_{28}^{10} &= (LL)_3 (ud)_1 (\bar{\ell}QH)_{1,3}, \\
 \mathcal{O}_{29}^{10} &= (ud)_1 (\ell\ell)_1 (\bar{\ell}Q\bar{H})_1, \\
 \mathcal{O}_{30}^{10} &= (u\ell)_1 (d\ell)_1 (\bar{\ell}Q\bar{H})_1, \\
 \mathcal{O}_{31}^{10} &= (LL)_3 (ud)_1 (\bar{L}uH)_{1,3}, \\
 \mathcal{O}_{32}^{10} &= (ud)_1 (u\ell)_1 (\bar{L}\ell\bar{H})_1, \\
 \mathcal{O}_{33}^{10} &= (ud)_1 (\ell\ell)_1 (\bar{L}u\bar{H})_1, \\
 \mathcal{O}_{34}^{10} &= (u\ell)_1 (d\ell)_1 (\bar{L}u\bar{H})_1, \\
 \mathcal{O}_{35}^{10} &= (ud)_1 (u\ell)_1 (\bar{\ell}LH)_{1,3}, \\
 \mathcal{O}_{36,37}^{10} &= (QL)_{1,3} (QL)_{1,3} (\bar{\ell}QH)_{1,1}, \\
 \mathcal{O}_{38,39,40}^{10} &= (QL)_{1,1,3} (QL)_{1,3,3} (\bar{L}d\bar{H})_{1,3,1}, \\
 \mathcal{O}_{41}^{10} &= (u\ell)_1 (u\ell)_1 (\bar{\ell}QH)_{1,3}, \\
 \mathcal{O}_{42}^{10} &= (u\ell)_1 (u\ell)_1 (\bar{L}d\bar{H})_{1,3},
 \end{aligned}$$

[Hambye, Heeck, 1712.04871, PRL]

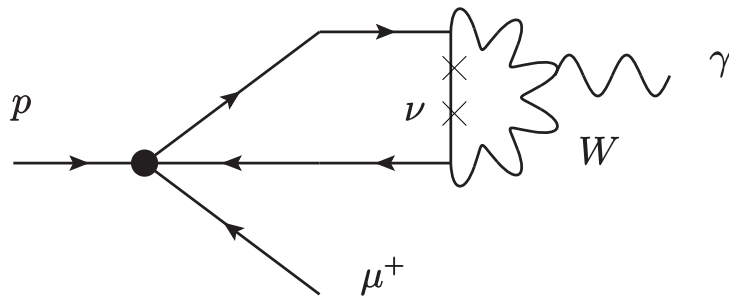
$p \rightarrow \mu^+ \mu^+ e^-$ plus M_ν breaks U(1)



$$\Delta B = \Delta L = 1, d = 10 :$$

$$\mathcal{A}_{10} \propto \frac{\langle H \rangle}{\Lambda^6}$$

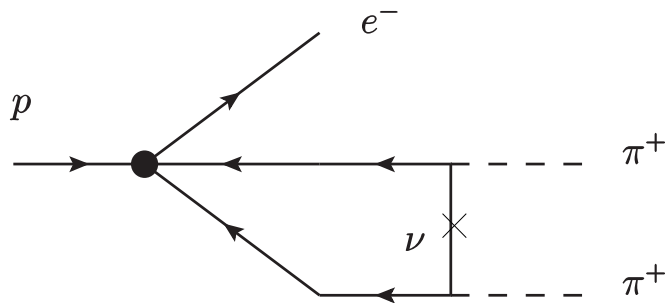
Conserves
U(1)



$$\Delta B = \Delta L = 1, d = 6 :$$

$$\mathcal{A}_6 \propto \frac{\langle H \rangle m_p}{\Lambda^6} \alpha \frac{\Delta m_\nu^2}{16\pi^2}$$

GIM: Not
dangerous



$$\Delta B = -\Delta L = 1, d = 7 :$$

$$\mathcal{A}_7 \propto \frac{\langle H \rangle m_p}{\Lambda^6} \frac{(m_\nu)_{\mu\mu}}{16\pi^2}$$

Small
enough!

Effective operators

- $\Delta B = 1$ **proton decay** operators:
 - $QQQL$: $d=6$, $\Delta L = 1$, e.g. $p \rightarrow e^+ \pi^0$.
 - $QQ\bar{L}Hd$: $d=7$, $\Delta L = -1$, e.g. $p \rightarrow e^- \pi^+ K^+$.
 - $\bar{L}\bar{L}\ell udd$: $d=9$, $\Delta L = -1$, e.g. $p \rightarrow \nu e^- e^+ K^+$.
 - $QQQL\bar{L}H\ell$: $d=10$, $\Delta L = 1$, e.g. $p \rightarrow e^+ e^- e^+$.
 - $ddd\bar{L}\bar{L}\bar{L}H$: $d=10$, $\Delta L = -3$, e.g. $p \rightarrow e^- \nu \nu \pi^+ \pi^+$.
 - $Qu d\bar{L}\bar{L}\bar{L}H\bar{H}$: $d=11$, $\Delta L = 3$, e.g. $p \rightarrow e^+ \bar{\nu}\bar{\nu}$.

[Weinberg, '79 & '80]

Different symmetry properties

But what if new physics is light?

Simple example: majoron

- 3 singlets N_R + new scalar $\sigma = (f + \sigma^0 + iJ)/\sqrt{2}$.

B – L breaking scale

Heavy scalar
(inflaton?)

Goldstone boson:
majoron

[Chikashige, Mohapatra, Peccei, '81; Schechter, Valle, '82]

- Break $U(1)_{B-L}$ spontaneously: $\mathcal{L} = -\bar{L}yHN_R - \frac{1}{2}\bar{N}_R^c \underbrace{\lambda\sigma N_R}_{M_R} + h.c.$

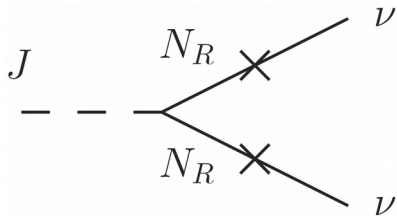
$$M_R = \frac{\lambda f}{\sqrt{2}}$$

- For $M_R \gg m_D$: $M_\nu \simeq -m_D M_R^{-1} m_D^T$

$$\simeq 1\text{eV} \left(\frac{m_D}{100\text{GeV}} \right)^2 \left(\frac{10^{13}\text{GeV}}{M_R} \right).$$

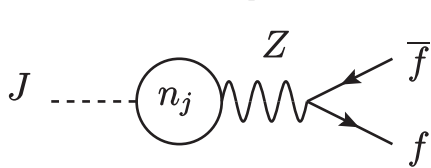
Majoron couplings

- Tree level coupling only to neutrinos:



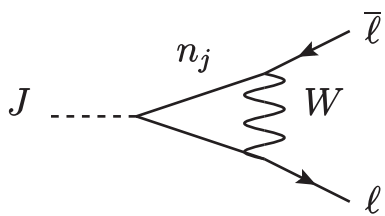
$$\frac{iJ}{2f} \bar{\nu}_\alpha^c \gamma_5 (m_D^* M_R^{-1} m_D^\dagger)_{\alpha\beta} \nu_\beta = -\frac{iJ}{2f} \sum_k \bar{\nu}_k \gamma_5 m_k \nu_k$$

- One loop:



$$\frac{iJ}{f} \bar{f} \gamma_5 f \frac{m_f T_3^f}{8\pi^2 v^2} \text{tr} (m_D m_D^\dagger)$$

Off-diagonal!



$$\frac{iJ}{f} \bar{l}_\alpha \left(\frac{m_\beta}{8\pi^2 v^2} P_R - \frac{m_\alpha}{8\pi^2 v^2} P_L \right) l_\beta (m_D m_D^\dagger)_{\alpha\beta}$$

- Two loop: $\Gamma(J \rightarrow \gamma\gamma) \simeq \frac{\alpha^2 \text{tr} (m_D m_D^\dagger)^2}{4096\pi^7} \frac{m_J^3}{v^4 f^2} \left| \sum_f N_c^f T_3^f Q_f^2 g \left(\frac{m_J^2}{4m_f^2} \right) \right|^2$

[Heeck, Camilo Garcia-Cely, 1701.07209; see also Pilaftsis '94]

Properties

- Crucial observation: the two matrices are independent!

$$\{m_D, M_R\} \leftrightarrow \{M_\nu, m_D m_D^\dagger\}.$$

[Davidson, Ibarra, hep-ph/0104076]

- $J\bar{\ell}\ell'$ coupling can be *large* and of **arbitrary structure**.

- Similar couplings arise for familons or flavor Z'.

[Wilczek, '82; Reiss, '82; Grinstein, Preskill, Wise, 85; ...]

- Boson not necessarily massless: *pseudo*-Goldstone.

- Experimental signature depends on decay channel:

$$\ell \rightarrow \ell' J, \quad J \rightarrow \text{inv}, \ell'' \ell''', \gamma\gamma.$$

$\ell \rightarrow \ell' J$ with $J \rightarrow$ invisible

- Standard LFV in seesaw:

$$\frac{\Gamma(\ell \rightarrow \ell' \gamma)}{\Gamma(\ell \rightarrow \ell' \nu_\ell \bar{\nu}_{\ell'})} \simeq \frac{3\alpha}{8\pi} |(m_D M_R^{-2} m_D^\dagger)_{\ell\ell'}|^2.$$

- Great signature, but requires light N_R .
- With majoron: look for **mono-energetic** lepton:

[Pilaftsis, '94; Feng, Moroi, Murayama, Schnapka, '98; Hirsch, Vicente, Meyer, Porod, '09]

$$\frac{\Gamma(\ell \rightarrow \ell' J)}{\Gamma(\ell \rightarrow \ell' \nu_\ell \bar{\nu}_{\ell'})} \simeq \frac{3}{16\pi^2} \frac{1}{m_\ell^2 f^2} |(m_D m_D^\dagger)_{\ell\ell'}|^2.$$

- If $M_R = \text{diag}(M)$: $\frac{\Gamma(\ell \rightarrow \ell' \gamma)}{\Gamma(\ell \rightarrow \ell' J)} \simeq 2\pi\alpha \frac{m_\ell^2}{M^2} \frac{f^2}{M^2} \begin{cases} \gg 1 & \text{for } M \ll f, \\ \ll 1 & \text{for } M \sim f \gg m_\ell. \end{cases}$

$\mu \rightarrow e J$ with $J \rightarrow$ invisible

- TWIST, '15: limits on different anisotropies.
- Chiral coupling $\bar{\mu} P_L e J$ suppresses sensitivity!

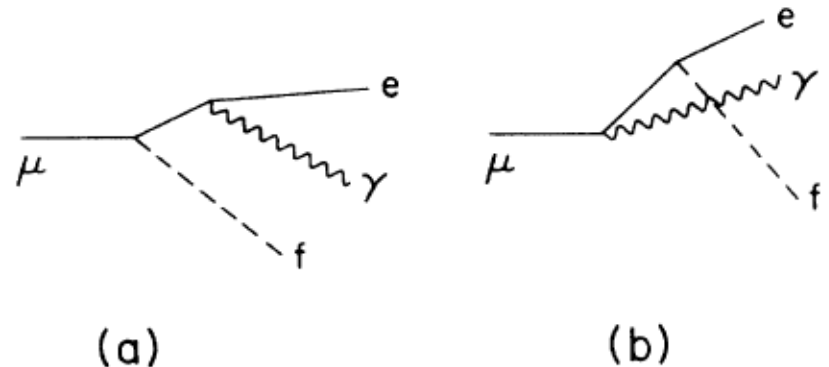
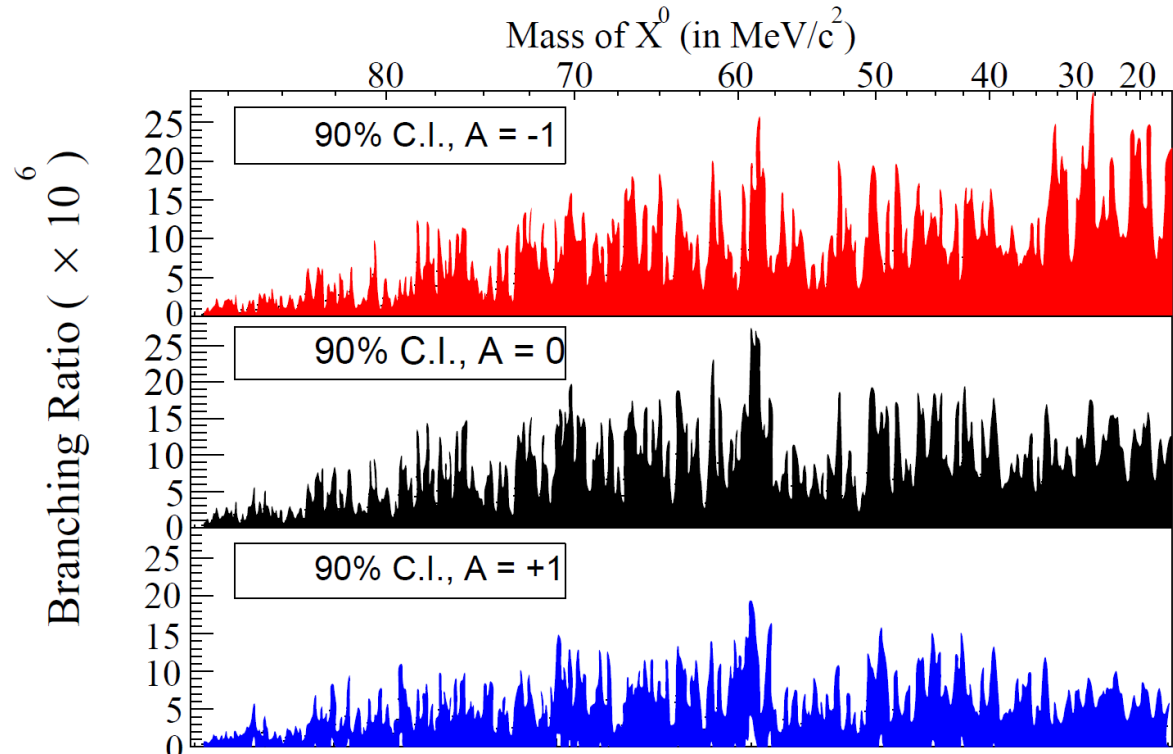
[Heeck, Garcia-Cely, 1701.07209]

- Bremsstrahlung is competitive: $\mu \rightarrow e J \gamma$.

[Goldman et al, '87]

- Approximate limit

$$\frac{|(m_D m_D^\dagger)_{\mu e}|}{v f} \lesssim 10^{-5}.$$



$\mu \rightarrow e J$ with $J \rightarrow$ invisible

- TWIST, '15: limits on different anisotropies.
- Chiral coupling $\bar{\mu} P_L e J$ suppresses sensitivity!

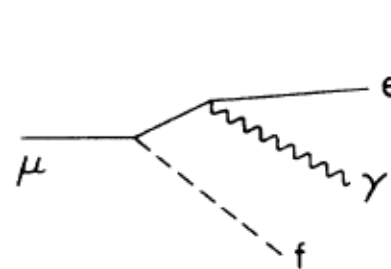
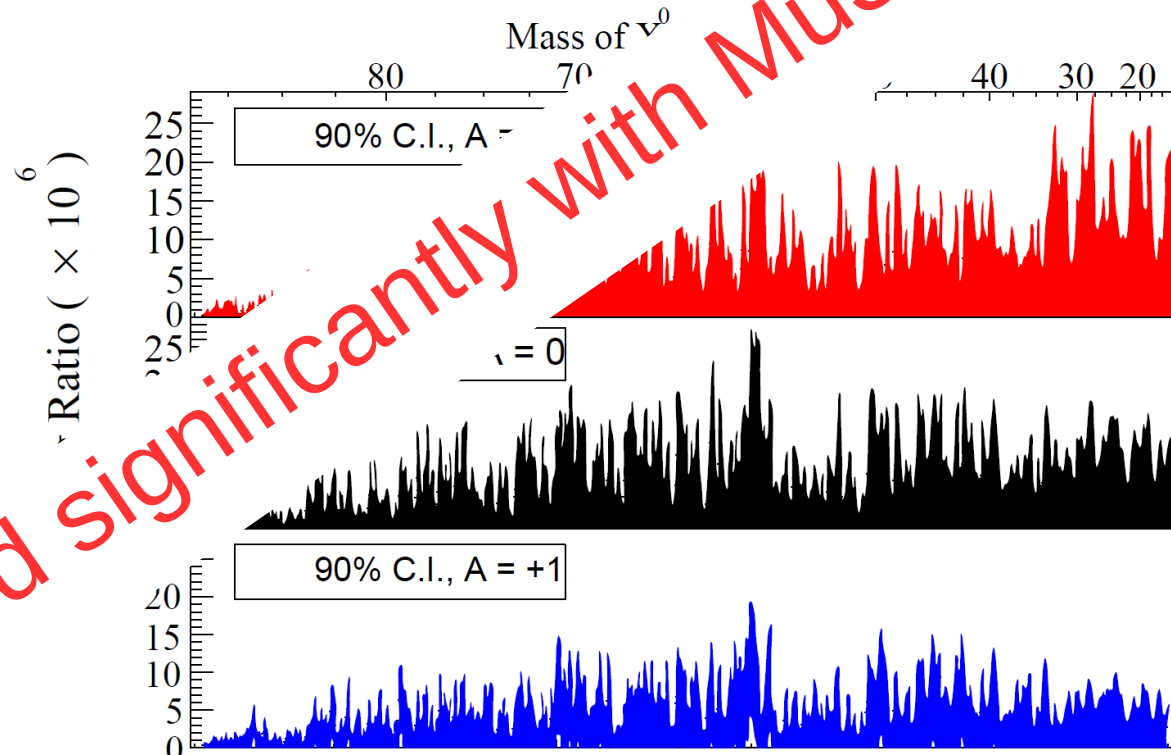
[Heeck, Garcia-Cely, 1701.07206]

- Bremsstrahlung competitive

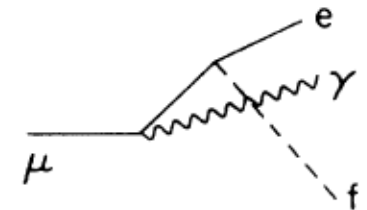
[Goldman et al.]

- Approximate limit

$$\left| \frac{D m_D^\dagger}{v f} \right|_{\mu e} \lesssim 10^{-5}.$$



(a)



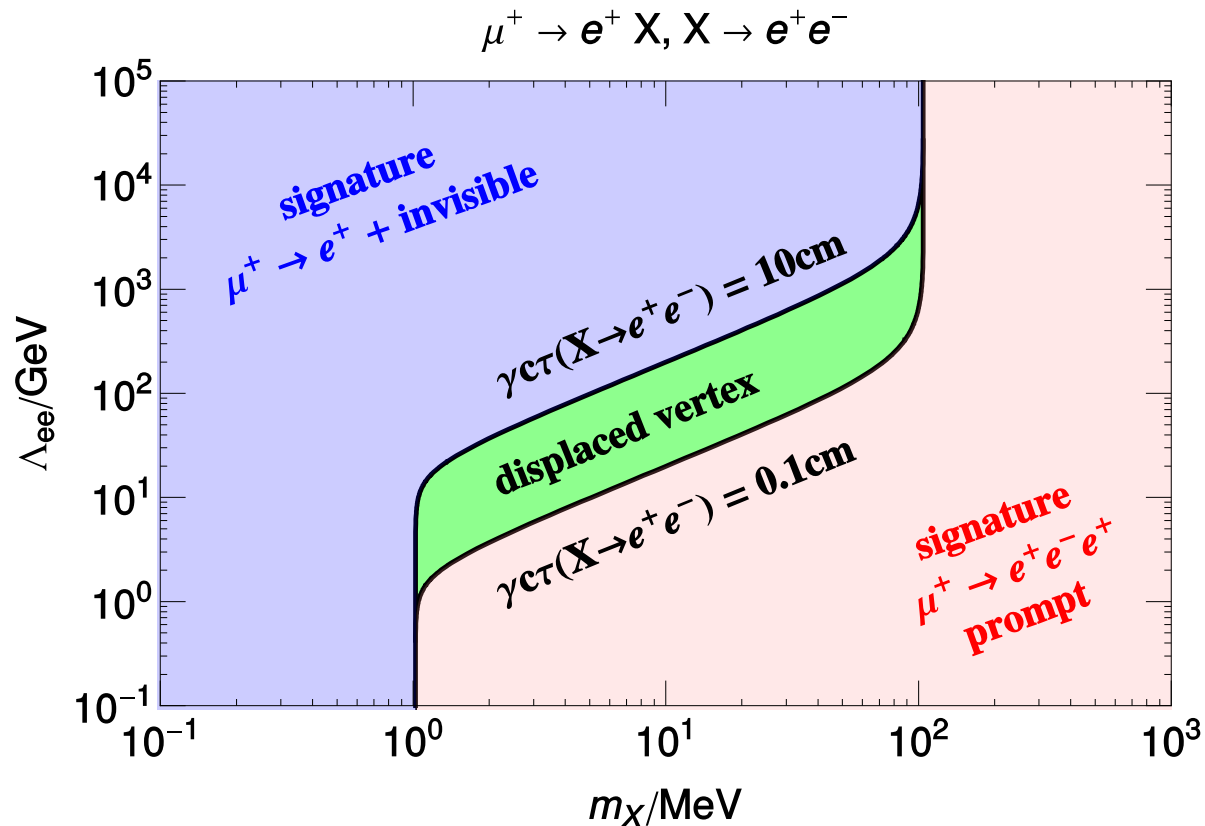
(b)

$\mu \rightarrow e X$ with $X \rightarrow$ visible

- Take $X \bar{e} y_5 e m_e / \Lambda_{ee}$.
- Decay length determines signature.
- Displaced vertex gives new observable.
[Heeck, Rodejohann, 1710.02062]

- Muon at rest:

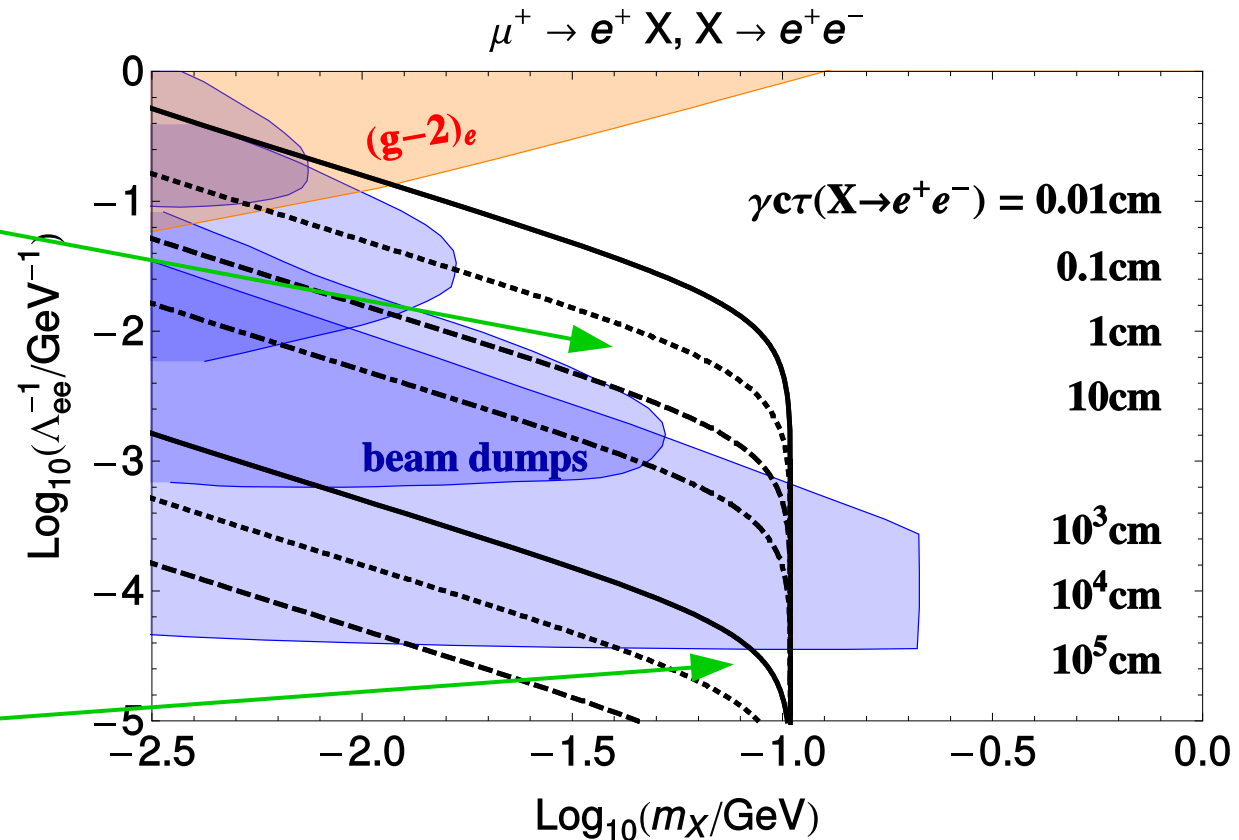
$$\gamma c \tau \simeq \frac{\pi m_\mu \Lambda_{ee}^2}{m_e^2 m_X^2} \simeq 2.5 \text{ cm} \left(\frac{\Lambda_{ee}}{100 \text{ GeV}} \right)^2 \left(\frac{10 \text{ MeV}}{m_X} \right)^2.$$



Sub-GeV X with ee coupling allowed?

$\mu \rightarrow e X$ with $X \rightarrow e\bar{e}$

- Decay length typically below cm. => looks prompt.
- Below beam dump: $\Lambda_{ee} > 30$ TeV; mostly invisible, but some DV!



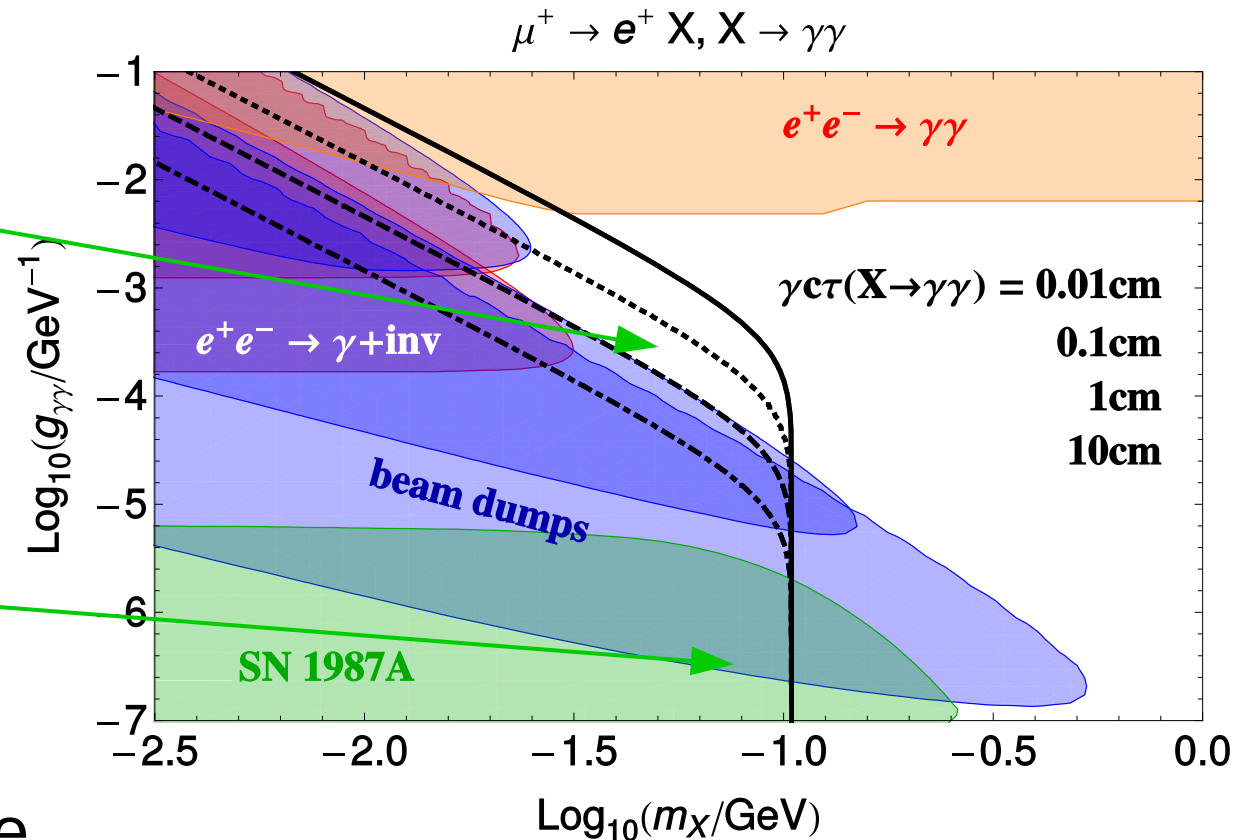
$$\text{BR}(\mu \rightarrow eX) \text{BR}(X \rightarrow ee) (1 - P(l_{\text{dec}}))$$

$$\simeq \text{BR}(\mu \rightarrow eX) \frac{l_{\text{dec}}}{\gamma c\tau}$$

Possible in
Mu3e!

$\mu \rightarrow e X$ with $X \rightarrow \gamma\gamma$

- Decay length always below cm. \Rightarrow looks prompt.
- Below beam dump: supernova constraints!
- Prompt channel still interesting, maybe MEG(II) or Mu3e extension?

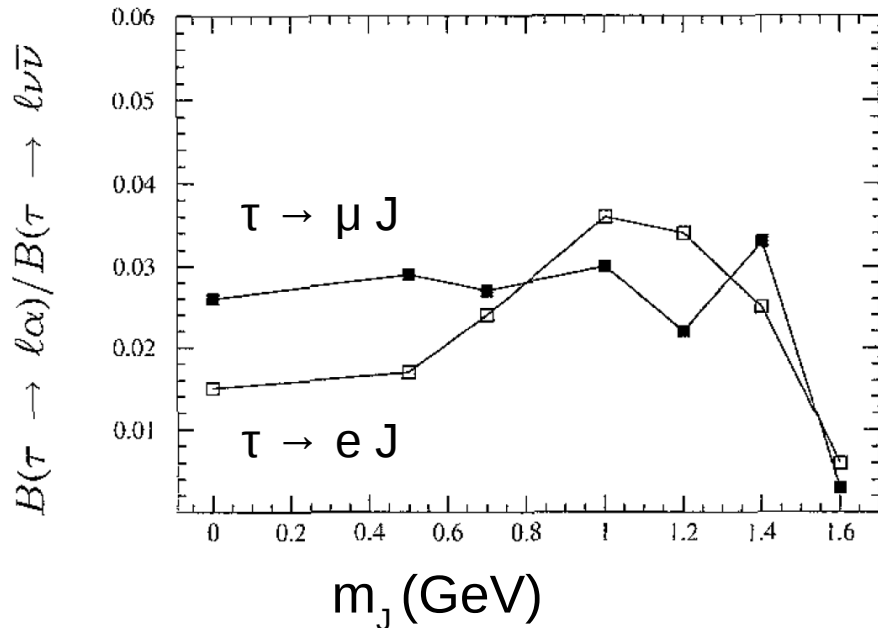


[Recent limits: Dolan et al, 1709.00009]

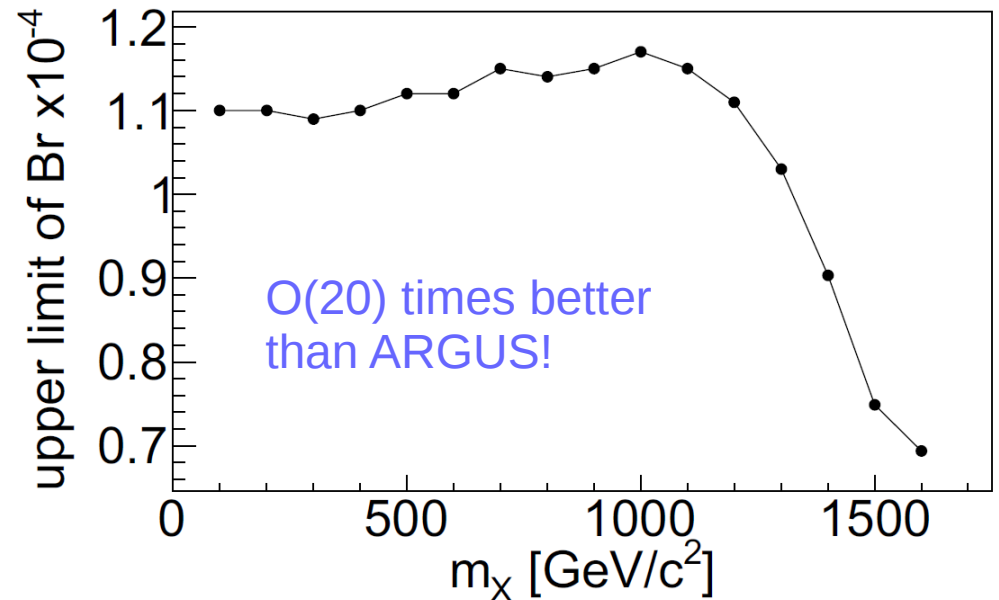
Muons difficult, taus easier.

$\tau \rightarrow \ell J$ with $J \rightarrow$ invisible

- ARGUS, '95; $5e5$ taus.



- Belle, '16 prelim.; $1e9$ taus.



- Also interesting for LFV Z'.

[Foot, He, Lew, Volkas, '94; Heeck, 1602.03810; Altmannshofer et al, 1607.06832]

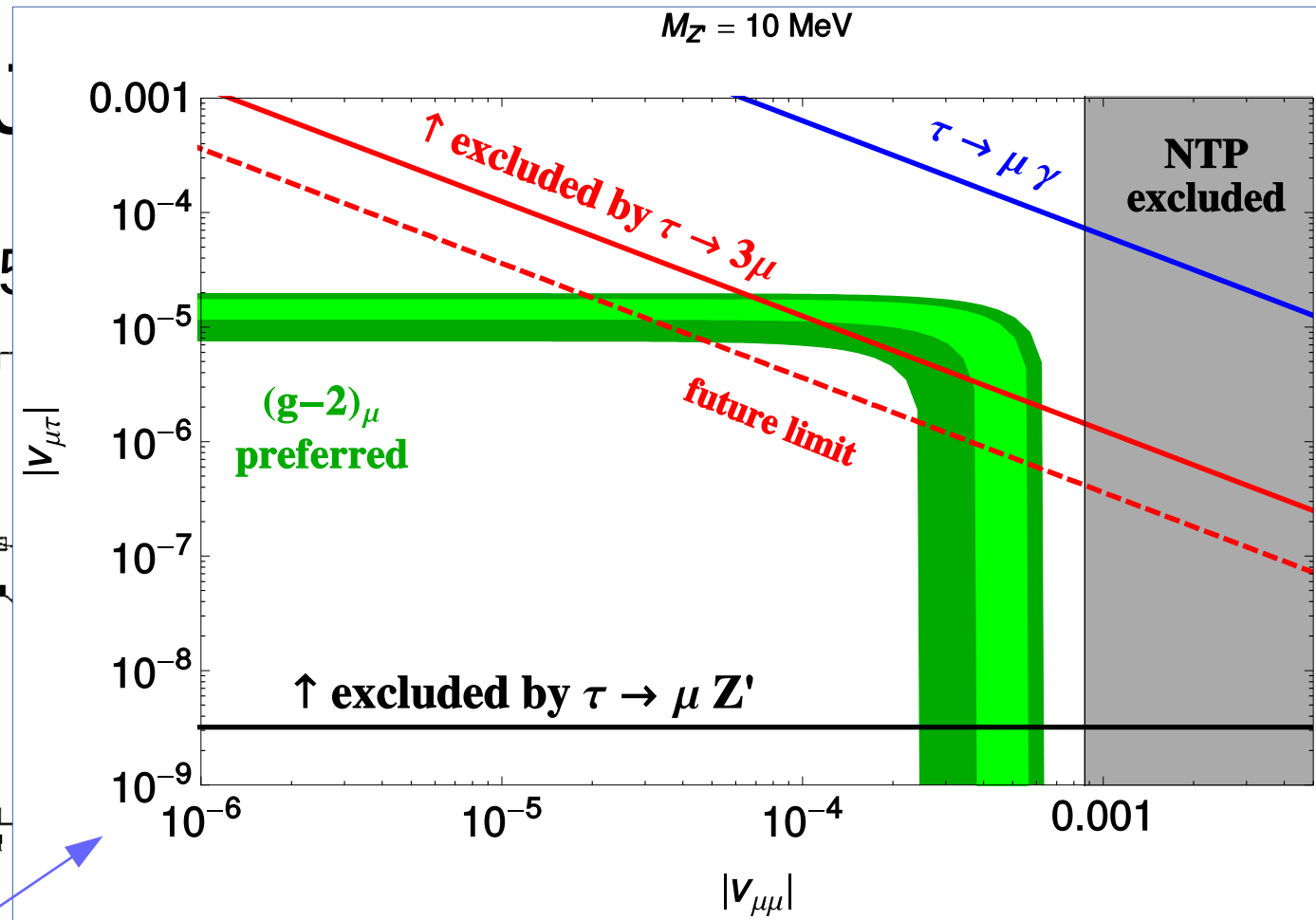
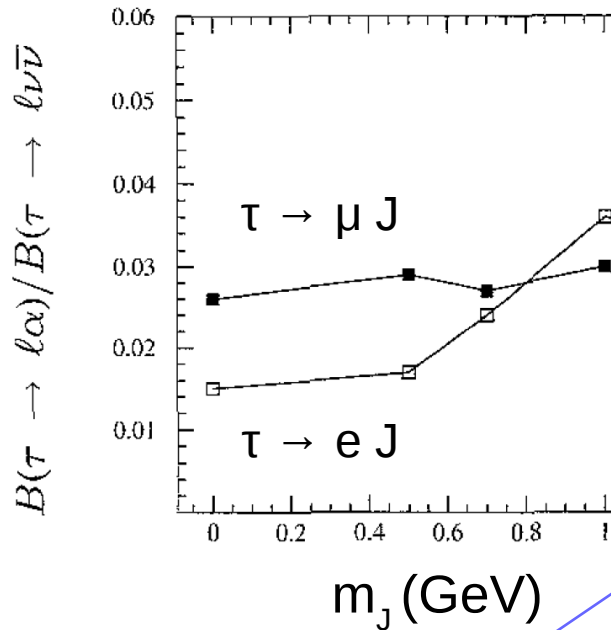
- Improvement with Belle-II.

$$\frac{|(m_D m_D^\dagger)_{\tau e}|}{v f} \lesssim 6 \times 10^{-3},$$

$$\frac{|(m_D m_D^\dagger)_{\tau \mu}|}{v f} \lesssim 10^{-3}.$$

$\tau \rightarrow \ell J$ with J

- ARGUS, '95; 5e5



- Also interesting for LFV Z' .

[Foot, He, Lew, Volkas, '94; Heeck, 1602.03810; Altmannshofer et al, 1607.06832]

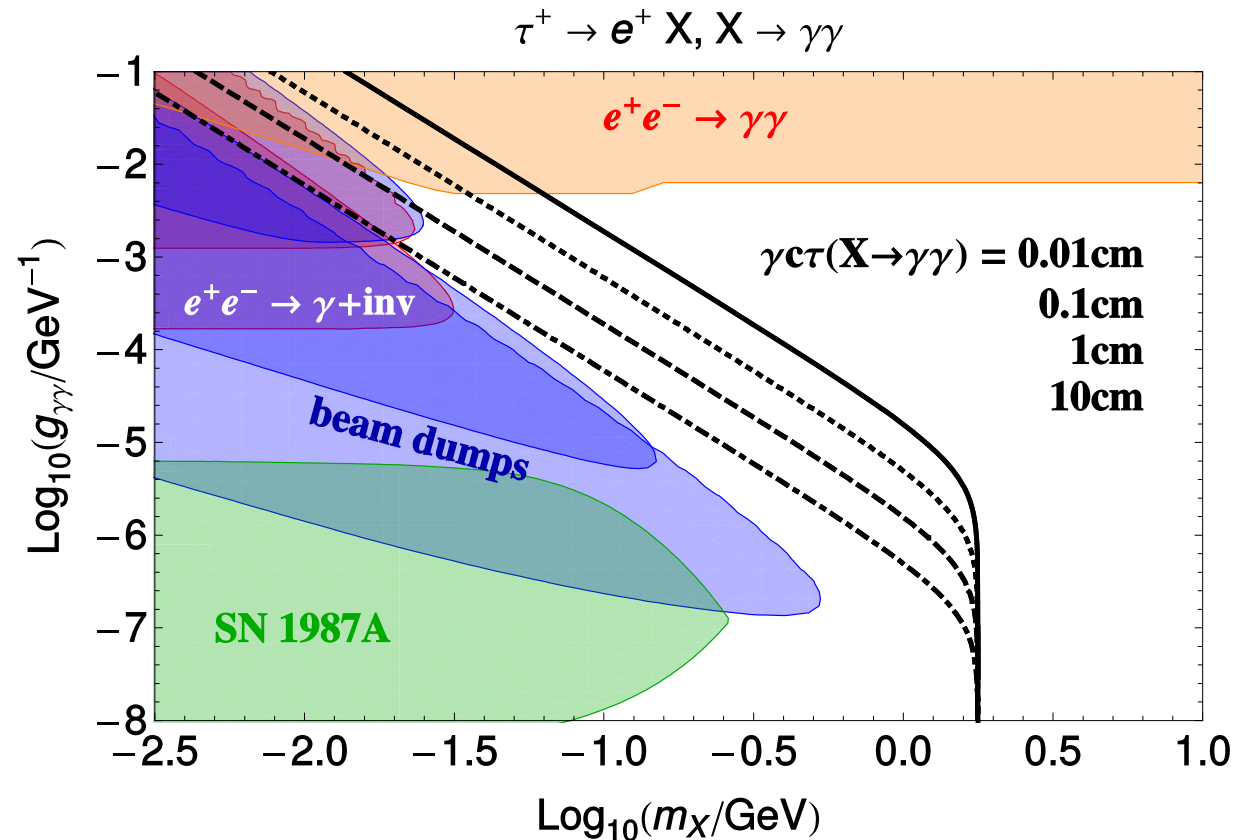
- Improvement with Belle-II.

$$\frac{|(m_D m_D^\dagger)_{\tau e}|}{v f} \lesssim 6 \times 10^{-3},$$

$$\frac{|(m_D m_D^\dagger)_{\tau \mu}|}{v f} \lesssim 10^{-3}.$$

$\tau \rightarrow e X$ with $X \rightarrow$ visible

- Tau at rest, higher X boost.
- Arbitrary decay lengths possible.
- Similar for $X \rightarrow ee, \mu\mu, \mu e$.
- Worthwhile in LHCb and Belle (II).



[Recent limits: Dolan et al, 1709.00009]

Muons difficult, taus easier...