

Preoperative Atelectasis

Part 4: Outcomes

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2024-04-08

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Setup

Packages used

```

if (!require("pacman", quietly = TRUE)) {
  install.packages("pacman")
}

pacman::p_load(
  tidyverse, # Used for basic data handling and visualization.
  table1, #Used to add labels to variables.
  RColorBrewer, #Color palettes for data visualization.
  gridExtra, #Used to arrange multiple ggplots in a grid.
  grid, #Used to arrange multiple ggplots in a grid.
  mgcv, #Used to model non-linear relationships with a general additive model.
  ggmosaic, #Used to create mosaic plots.
  car, #Used to assess distribution of continuous variables (stacked Q-Q plots).
  simpleboot, boot, # Used to calculate mean atelectasis coverage and
    # 95%CI through bootstrapping.
  gt, #Used to present tables in html format.
  report #Used to cite packages used in this session.
)

```

Session and package dependencies

R version 4.3.3 (2024-02-29 ucrt)
 Platform: x86_64-w64-mingw32/x64 (64-bit)
 Running under: Windows 11 x64 (build 22631)

Matrix products: default

locale:
 [1] LC_COLLATE=Spanish_Mexico.utf8 LC_CTYPE=Spanish_Mexico.utf8
 [3] LC_MONETARY=Spanish_Mexico.utf8 LC_NUMERIC=C
 [5] LC_TIME=Spanish_Mexico.utf8

time zone: Europe/Berlin
 tzcode source: internal

attached base packages:
 [1] grid stats graphics grDevices datasets utils methods
 [8] base

other attached packages:

```
[1] report_0.5.8      gt_0.10.1          boot_1.3-30        simpleboot_1.1-7
[5] car_3.1-2          carData_3.0-5      ggmosaic_0.3.3     mgcv_1.9-1
[9] nlme_3.1-164       gridExtra_2.3      RColorBrewer_1.1-3 table1_1.4.3
[13] lubridate_1.9.3    forcats_1.0.0      stringr_1.5.1      dplyr_1.1.4
[17] purrr_1.0.2        readr_2.1.5        tidyr_1.3.1        tibble_3.2.1
[21] ggplot2_3.5.0      tidyverse_2.0.0    pacman_0.5.1
```

Set seed (for reproducibility of bootstrapping) as the current year 2023:

```
seed <- 2023
```

Outcome variable

Corroborate that atelectasis(Yes/No) matches atelectasis percent equal or different to 0%:

	atelectasis_percent								
atelectasis	0	2.5	5	7.5	10	12.5	15	17.5	27.5
Yes	0	11	14	33	6	1	4	7	1
No	159	0	0	0	0	0	0	0	0

Yes, these do match.

Prevalence of atelectasis

	Yes	No
frequencies	77.0	159.0
percent	32.6	67.4

Prevalence of atelectasis with 95% confidence interval

1-sample proportions test without continuity correction

```
data: frequencies, null probability 0.5
X-squared = 28.492, df = 1, p-value = 9.411e-08
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
 0.2696526 0.3884549
sample estimates:
```

p
0.3262712

The prevalence of atelectasis was **32.6 (95%CI: 26.97, 38.85)**.

Atelectasis - obesity class

Mean expected frequency:

	mean_expected_freq
1	39.33333

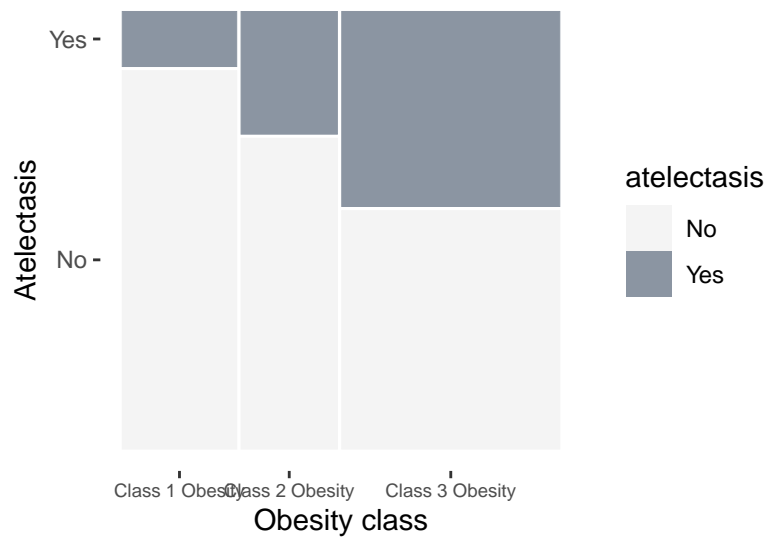
Frequencies:

type_obesity		atelectasis	
		Yes	No
Class 1 Obesity		8	55
Class 2 Obesity		15	38
Class 3 Obesity		54	66

Percentage:

type_obesity		atelectasis	
		Yes	No
Class 1 Obesity		12.7	87.3
Class 2 Obesity		28.3	71.7
Class 3 Obesity		45.0	55.0

Mosaic Plot



Pearson's Chi-squared test

```
data: frequencies
X-squared = 20.191, df = 2, p-value = 4.127e-05
```

Atelectasis location by obesity class

Mean expected frequency:

```
mean_expected_freq
1          12.83333
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

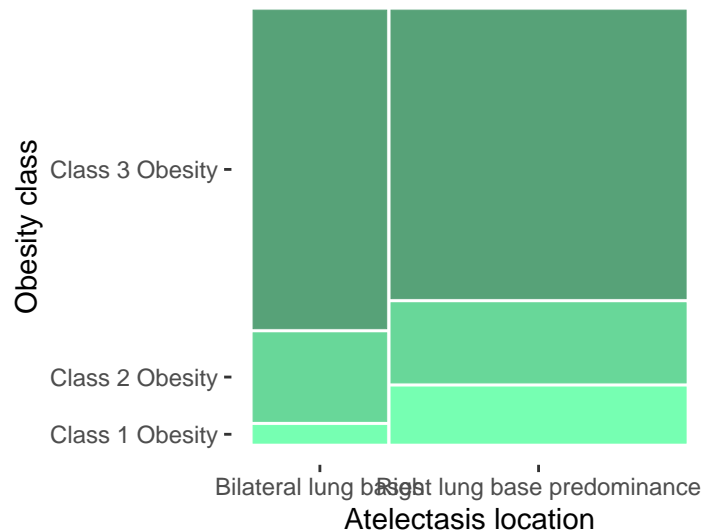
Frequencies:

	atelectasis_location	
type_obesity	Bilateral lung bases	Right lung base predominance
Class 1 Obesity	1	7
Class 2 Obesity	5	10
Class 3 Obesity	18	36

Percentage:

	atelectasis_location	
type_obesity	Bilateral lung bases	Right lung base predominance
Class 1 Obesity	12.50	87.50
Class 2 Obesity	33.33	66.67
Class 3 Obesity	33.33	66.67

Mosaic Plot



Pearson's Chi-squared test

data: frequencies
X-squared = 1.4503, df = 2, p-value = 0.4843

Prevalence of atelectasis with 95% confidence intervals calculated with sourced script ***Prevalence_atelectasis.R***

The prevalence of atelectasis was greater in higher obesity classes: class 1, n=8 (12.7%, 95%CI:6.03 - 24.04); class 2, n=15 (28.3%, 95%CI:17.2 - 42.56); and class 3, n=54 (45%, 95%CI:36 - 54.33) (p<0.001).

Of those who had atelectasis, the most frequent presentation was the right lung base predominance n=, compared to bilateral lung bases n=. When examining this by obesity class, the observed distribution was not significantly different for those with class 1, 2, and 3 obesity categories (n=, n=, and n=, respectively) (p=0.484).

Atelectasis Percent

Mean atelectasis percentage

The following would be the mean atelectasis percentage coverage if a normal distribution were assumed, which is what has been done in some prior studies:

```
      mean      sd
1 2.658898 4.687145
```

And by obesity class:

```
# A tibble: 3 x 3
  type_obesity    mean    sd
  <fct>          <dbl> <dbl>
1 Class 1 Obesity 0.913  2.89
2 Class 2 Obesity 1.56   3.15
3 Class 3 Obesity 4.06   5.53
```

As is evident from these numbers, assuming normality causes standard deviation to capture negative values, which is impossible in reality for this variable.

Thus, bootstrapping the mean and 95%CI is expected to lead to more appropriate estimates.

Mean by bootstrapping for the total sample:

```
[1] 2.656468
```

Bootstrap 95% confidence intervals:

```
BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
Based on 10000 bootstrap replicates
```

```
CALL :
boot.ci(boot.out = boot_atel)
```

```
Intervals :
Level      Normal              Basic
95%    ( 2.064,  3.259 )    ( 2.055,  3.242 )
```

```
Level      Percentile          BCa
95%    ( 2.076,  3.263 )    ( 2.066,  3.263 )
Calculations and Intervals on Original Scale
```

The bias-corrected and accelerated (BCa) bootstrap interval is known to lead to more stable intervals with better coverage. Will report this. However, it is a good thing that here 95%CI through different methods do not lead to widely different results.

Now, I will calculate this for different BMI categories:

Class 1

Mean:

```
[1] 0.9109484
```

95% CI:

BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS

Based on 10000 bootstrap replicates

CALL :

```
boot.ci(boot.out = boot_class1)
```

Intervals :

Level	Normal	Basic
95%	(0.2120, 1.6169)	(0.1587, 1.5476)

Level	Percentile	BCa
95%	(0.2778, 1.6667)	(0.3175, 1.7063)

Calculations and Intervals on Original Scale

Class 2

Mean:

```
[1] 1.552184
```

95% CI:

BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS

Based on 10000 bootstrap replicates

CALL :

```
boot.ci(boot.out = boot_class2)
```

```

Intervals :
Level      Normal      Basic
95%   ( 0.730,  2.393 )   ( 0.660,  2.358 )

Level      Percentile      BCa
95%   ( 0.755,  2.453 )   ( 0.755,  2.453 )
Calculations and Intervals on Original Scale

```

Class 3

Mean:

```
[1] 4.056177
```

95% CI:

```

BOOTSTRAP CONFIDENCE INTERVAL CALCULATIONS
Based on 10000 bootstrap replicates

```

```

CALL :
boot.ci(boot.out = boot_class3)

```

```

Intervals :
Level      Normal      Basic
95%   ( 3.081,  5.057 )   ( 3.042,  5.021 )

Level      Percentile      BCa
95%   ( 3.104,  5.083 )   ( 3.104,  5.083 )
Calculations and Intervals on Original Scale

```

The mean atelectasis percentage coverage in the sample was 2.66% (95%CI:2.07-3.26) and according to obesity categories: class 1 (0.91%, 95%CI:0.32-1.71), class 2 (1.55%, 95%CI:0.75-2.45), and class 3 (4.06%, 95%CI:3.1-5.08).

What could happen if I took random subsamples between $n=20$ and $n=30$ similar to what has been done in other studies and calculate mean BMI and mean atelectasis percentage assuming normal distributions?

Random sample

```

      mean_BMI mean_atelectasis
1  39.1345      1.5

```

```

      mean_BMI mean_atelectasis
1  39.3644          2.1

```

```

      mean_BMI mean_atelectasis
1 39.36633      2.083333

```

Atelectasis percentage by obesity class

Now, I will continue assessing atelectasis percentage if assumed to be categorical ordinal:

Mean expected frequency:

```

      mean_expected_freq
1          8.740741

```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

Frequencies:

```

              type_obesity
atelectasis_percent Class 1 Obesity Class 2 Obesity Class 3 Obesity
0                   55          38          66
2.5                  2           7           2
5                    1           2          11
7.5                  4           4          25
10                   0           1           5
12.5                 0           0           1
15                   0           1           3
17.5                 1           0           6
27.5                 0           0           1

```

Percentage by obesity class

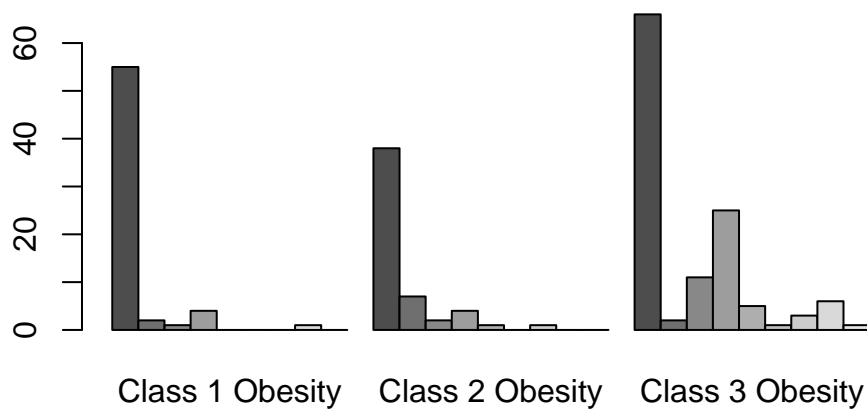
```

              type_obesity
atelectasis_percent Class 1 Obesity Class 2 Obesity Class 3 Obesity
0                   87.30       71.70       55.00
2.5                  3.17       13.21        1.67
5                    1.59        3.77        9.17
7.5                  6.35        7.55       20.83
10                   0.00        1.89        4.17
12.5                 0.00        0.00        0.83

```

15	0.00	1.89	2.50
17.5	1.59	0.00	5.00
27.5	0.00	0.00	0.83

Barplot of absolute frequencies:

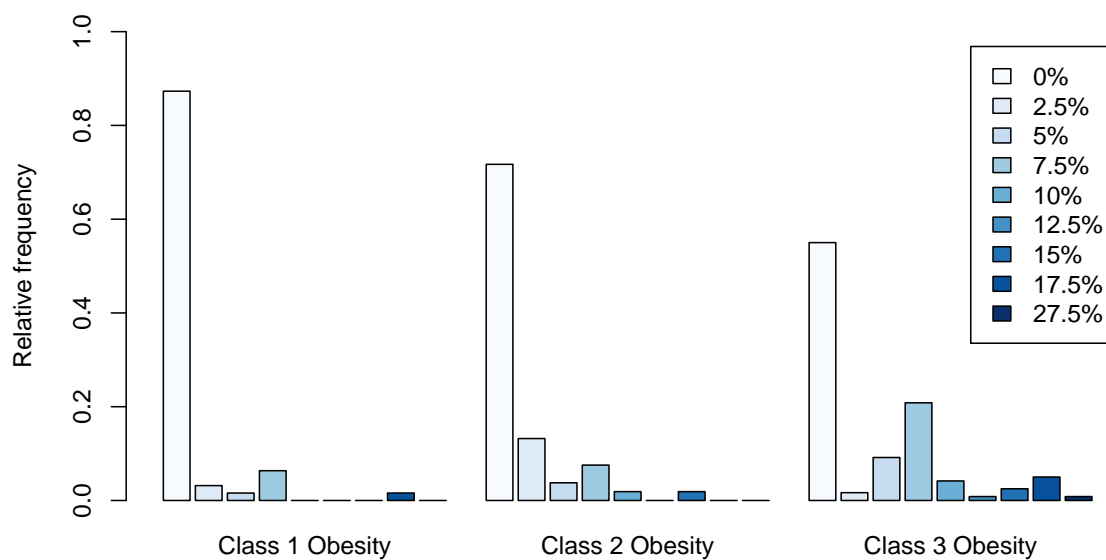


Pearson's Chi-squared test

data: frequencies

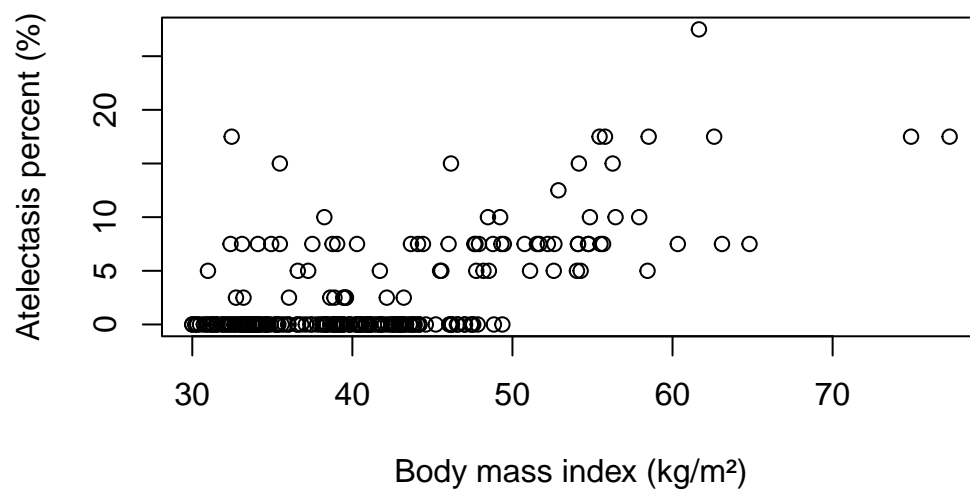
X-squared = 40.318, df = 16, p-value = 0.0006995

Barplot of atelectasis percentage by obesity class category



Smooth term?

Scatterplot



Atelectasis percent seems to increase as BMI increases. However, relationship is not linear.

Models evaluated with the accompanying sourced script ***nonlinear_BMI_Atelectasis.R***

All models are significantly better than linear. Thus, using a smooth term for BMI to predict atelectasis percent is better than modelling a linear relationship.

Best AIC:

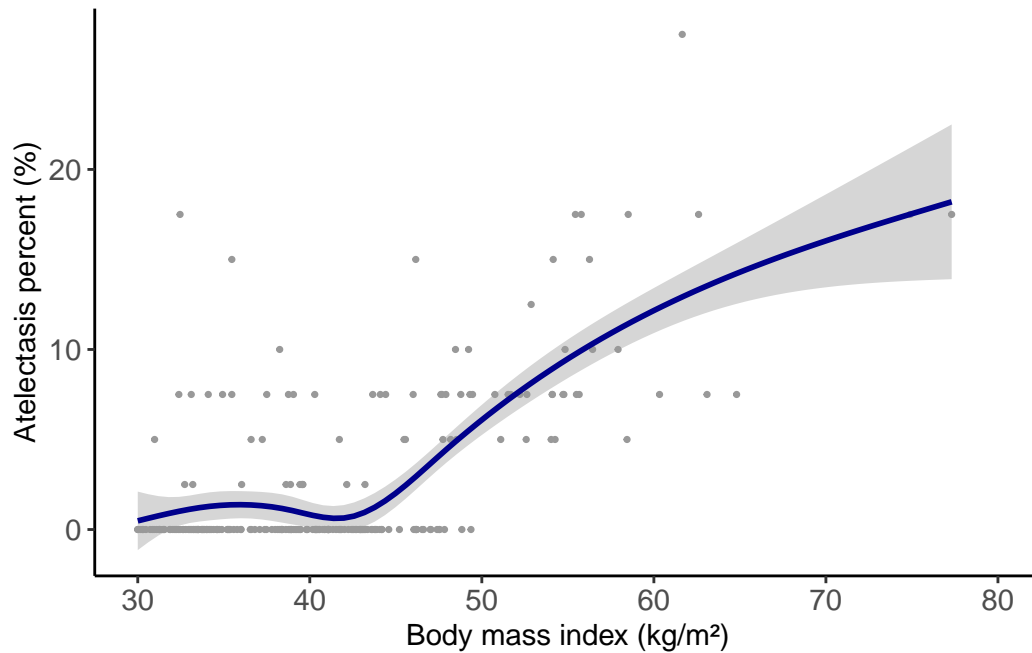
model	AIC
k=2	1259.7
k=4	1237.6
k=6	1232.3
k=8	1233.6

Regarding AIC, greatest improvement in AIC is k=6. Will model with k=5 and k=7 to compare

Best AIC:

model	AIC
k=5	1235.7
k=6	1232.3
k=7	1233.2

k=6 offers the lowest AIC. Will keep k=6 to model.



Positive non-monotonic relationship since atelectasis increases as BMI increases only after ~BMI equal to 42.

Will assess Spearman's correlation again only to have a rough idea (will not report this in the paper since the relationship is not monotonic):

Spearman's rank correlation rho

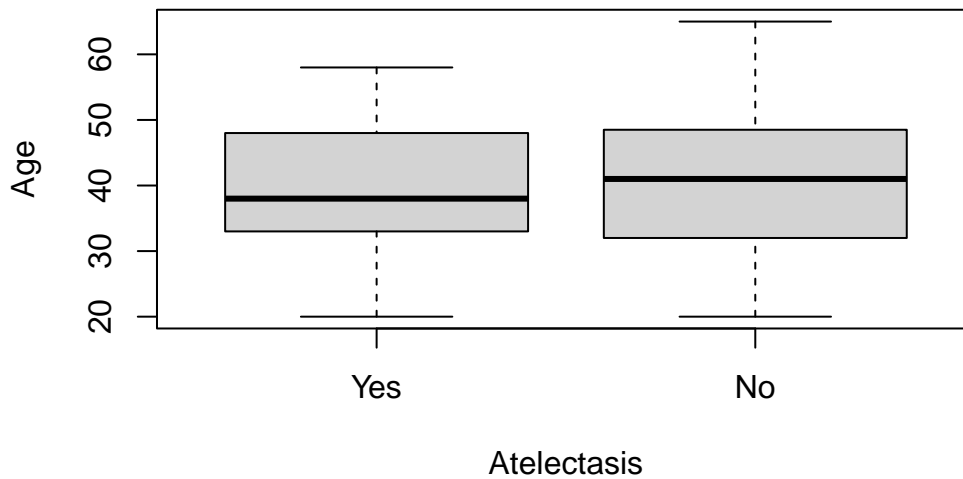
```
data:  spo2_VP0 and atelectasis_percent
S = 3883525, p-value < 2.2e-16
alternative hypothesis: true rho is not equal to 0
sample estimates:
      rho
-0.7727568
```

Atelectasis percent exhibited a negative non-linear non-monotonic relationship with SpO2 (**Figure 1A**, rho= -0.773, p<0.001).

Note that this p-value refers to the smooth term vs linear as assessed in GAM models.

Interestingly, this figure is almost a mirror image of the priorly created plot for SpO2 ~ BMI.

Atelectasis - age



Assess distribution of age by atelectasis (yes/no):

Distribution near-normal, will assess mean and variance for further testing:

Atelectasis	n	age_mean	sd	variance
Yes	77	39.65	9.30	86.5728
No	159	40.55	10.14	102.8816

Variances near-similar, but group sizes differ. Welch's t-test more suitable:

Welch Two Sample t-test

```
data: age by atelectasis
```

```
t = -0.67931, df = 162.72, p-value = 0.4979
```

```
alternative hypothesis: true difference in means between group Yes and group No is not equal
```

```
95 percent confidence interval:
```

```
-3.532230  1.724013
```

```
sample estimates:
```

```
mean in group Yes  mean in group No
      39.64935      40.55346
```

Age was similarly distributed among patients without atelectasis (40.5, sd:10.1) and those with atelectasis (39.6, sd:9.3) ($p=0.498$).

Atelectasis - sex

Mean expected frequency:

```

      mean_expected_freq
1                59

```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

Frequencies:

```

      atelectasis
sex    Yes  No
Woman  67 147
Man    10  12

```

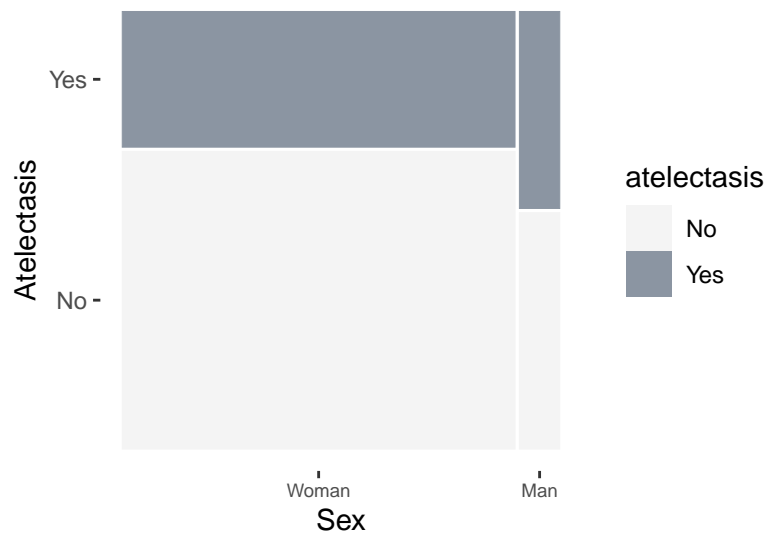
Percentage:

```

      atelectasis
sex    Yes    No
Woman 31.31 68.69
Man   45.45 54.55

```

Mosaic Plot



Pearson's Chi-squared test

```
data: frequencies
X-squared = 1.8161, df = 1, p-value = 0.1778
```

There were no significant differences in atelectasis occurrence between men (45.5%) and women (31.3%) ($p=0.178$).

Atelectasis - OSA

Mean expected frequency:

```
mean_expected_freq
1                59
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

Frequencies:

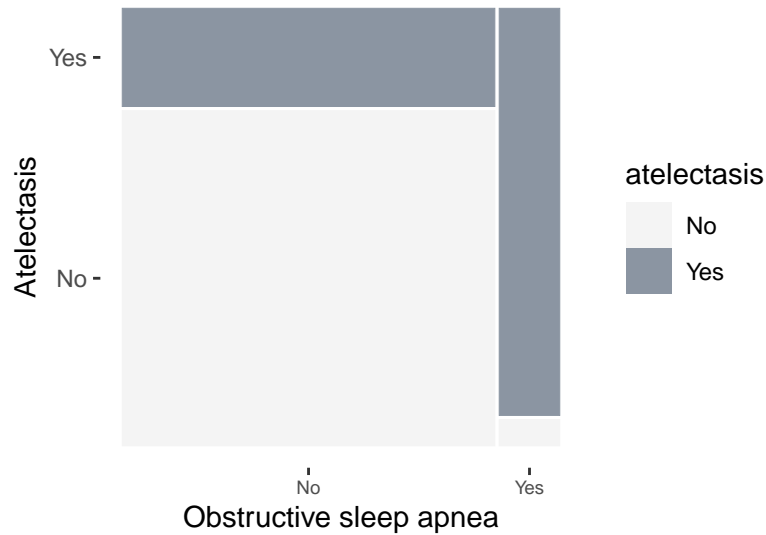
```

      atelectasis
sleep_apnea Yes  No
No         46 157
Yes        31   2
```

Percentage:

		atelectasis	
sleep_apnea	Yes	No	
	No	22.66	77.34
	Yes	93.94	6.06

Mosaic Plot



Pearson's Chi-squared test

data: frequencies
X-squared = 65.609, df = 1, p-value = 5.5e-16

Patients with a diagnosis of obstructive sleep apnea had atelectasis more frequently (93.9%) than those without the diagnosis (22.7%) ($p < 0.001$).

Atelectasis location by OSA

Mean expected frequency:

	mean_expected_freq
1	19.25

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

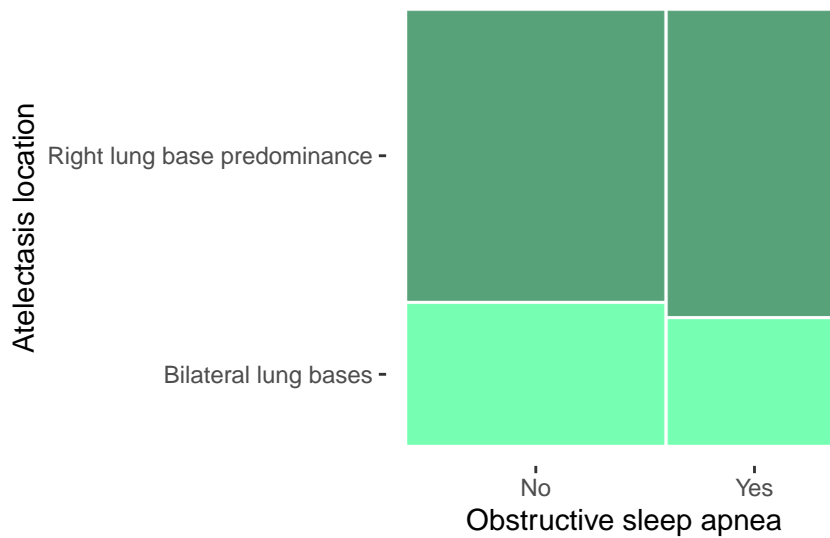
Frequencies:

		atelectasis_location	
sleep_apnea		Bilateral lung bases	Right lung base predominance
No		15	31
Yes		9	22

Percentage:

		atelectasis_location	
sleep_apnea		Bilateral lung bases	Right lung base predominance
No		32.61	67.39
Yes		29.03	70.97

Mosaic Plot



Pearson's Chi-squared test

data: frequencies

X-squared = 0.11041, df = 1, p-value = 0.7397

The location of atelectasis was not different among patients with and without OSA (p=0.74).

Atelectasis - Asthma

Mean expected frequency:

```
mean_expected_freq
1                59
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

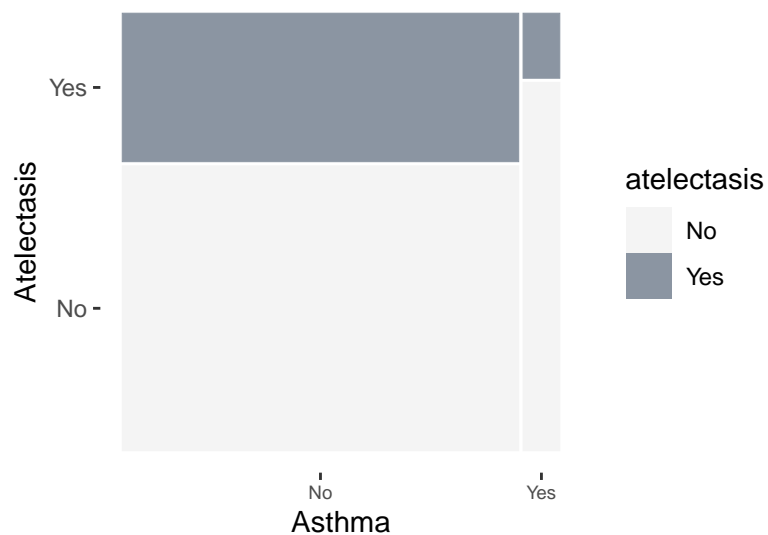
Frequencies:

```
      atelectasis
asthma Yes  No
No      74 142
Yes      3  17
```

Percentage:

```
      atelectasis
asthma  Yes   No
No    34.26 65.74
Yes   15.00 85.00
```

Mosaic Plot



Pearson's Chi-squared test

data: frequencies

X-squared = 3.0888, df = 1, p-value = 0.07883

Patients with a diagnosis of asthma did not have atelectasis more frequently (15%) than those without the diagnosis (34.3%) (p=0.079).

Atelectasis location by asthma status

Mean expected frequency:

	mean_expected_freq
1	19.25

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

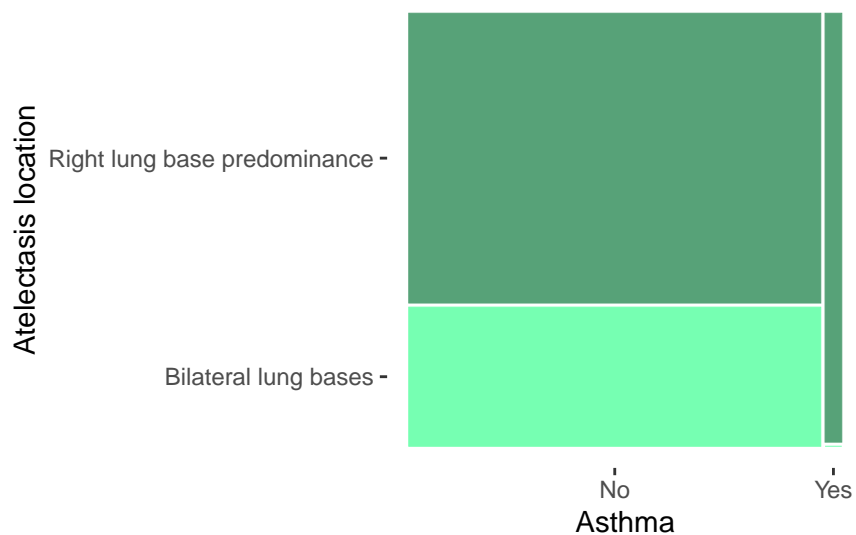
Frequencies:

	atelectasis_location	
asthma	Bilateral lung bases	Right lung base predominance
No	24	50
Yes	0	3

Percentage:

	atelectasis_location	
asthma	Bilateral lung bases	Right lung base predominance
No	32.43	67.57
Yes	0.00	100.00

Mosaic Plot



Pearson's Chi-squared test

```
data: frequencies
X-squared = 1.4136, df = 1, p-value = 0.2345
```

The location of atelectasis was not different among patients with and without asthma ($p=0.234$).

Atelectasis - COPD

Mean expected frequency:

```
mean_expected_freq
1                59
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

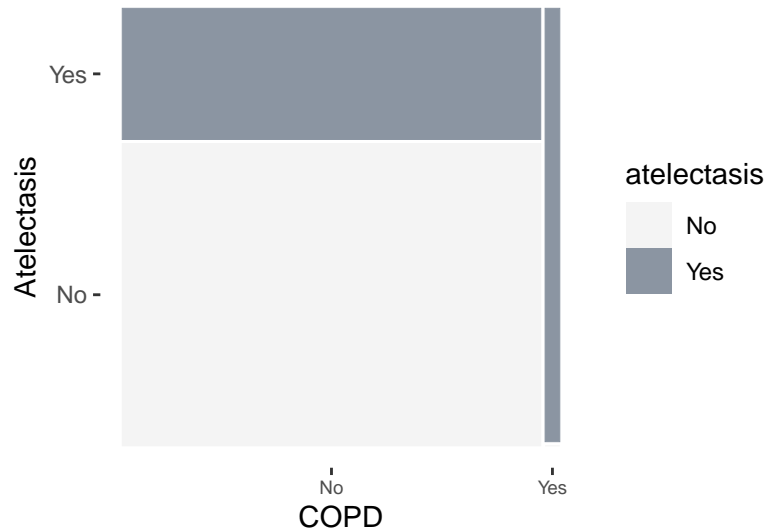
Frequencies:

```
atelectasis
COPD  Yes  No
No    69 159
Yes    8   0
```

Percentage:

atelectasis		
COPD	Yes	No
No	30.26	69.74
Yes	100.00	0.00

Mosaic Plot



Pearson's Chi-squared test

data: frequencies
X-squared = 17.099, df = 1, p-value = 3.548e-05

Patients with a diagnosis of COPD had atelectasis more frequently (100%) than those without the diagnosis (30.3%) ($p < 0.001$).

Atelectasis location by COPD

Mean expected frequency:

	mean_expected_freq
1	19.25

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

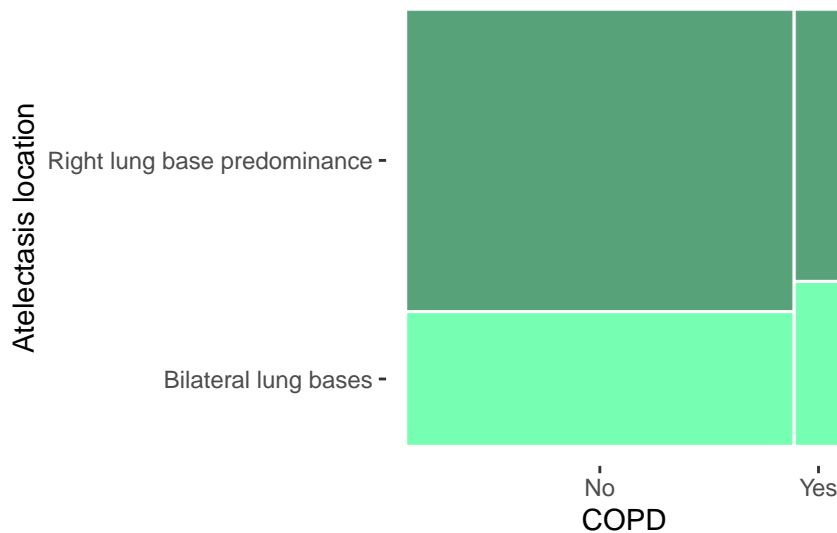
Frequencies:

	atelectasis_location	
COPD	Bilateral lung bases	Right lung base predominance
No	21	48
Yes	3	5

Percentage:

	atelectasis_location	
COPD	Bilateral lung bases	Right lung base predominance
No	30.43	69.57
Yes	37.50	62.50

Mosaic Plot



Pearson's Chi-squared test

data: frequencies

X-squared = 0.1668, df = 1, p-value = 0.683

The location of atelectasis was not different among patients with and without COPD (p=0.683).

Atelectasis - Oxygen use

Mean expected frequency:

```
mean_expected_freq
1                59
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

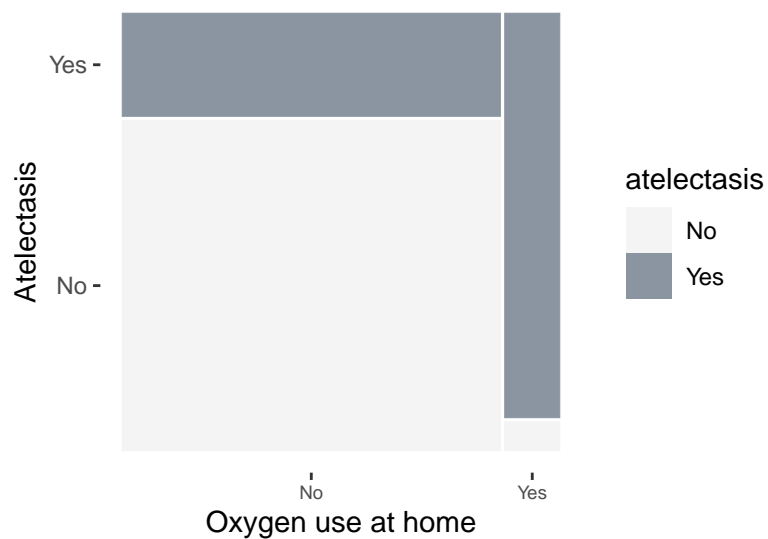
Frequencies:

```
      atelectasis
oxygen_use Yes  No
No       49 157
Yes      28   2
```

Percentage:

```
      atelectasis
oxygen_use  Yes   No
No      23.79 76.21
Yes     93.33  6.67
```

Mosaic Plot



Pearson's Chi-squared test

data: frequencies

X-squared = 57.619, df = 1, p-value = 3.181e-14

Patients who used oxygen at home had atelectasis more frequently (93.3%) than those who did not (23.8%) ($p < 0.001$).

Atelectasis location by OSA

Mean expected frequency:

```
mean_expected_freq
1                19.25
```

Mean expected frequency is greater than 5.0, so chi-squared without continuity correction is adequate.

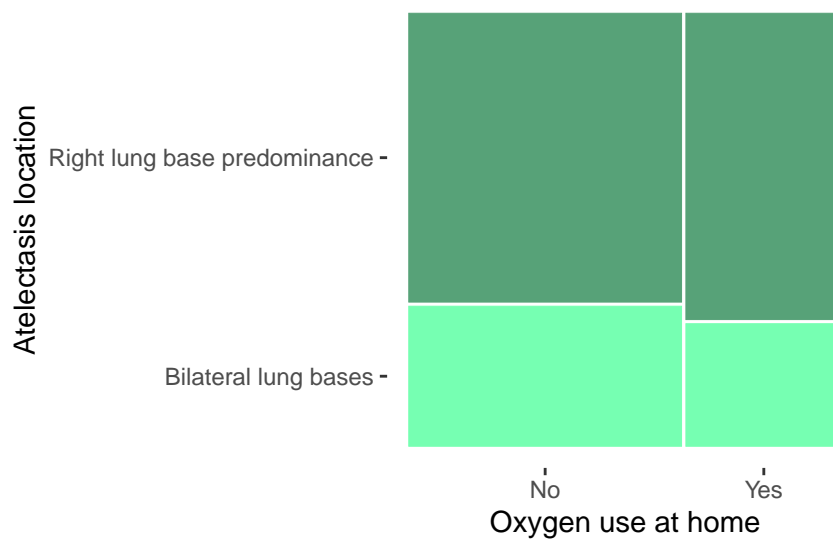
Frequencies:

	atelectasis_location	
oxygen_use	Bilateral lung bases	Right lung base predominance
No	16	33
Yes	8	20

Percentage:

	atelectasis_location	
oxygen_use	Bilateral lung bases	Right lung base predominance
No	32.65	67.35
Yes	28.57	71.43

Mosaic Plot



Pearson's Chi-squared test

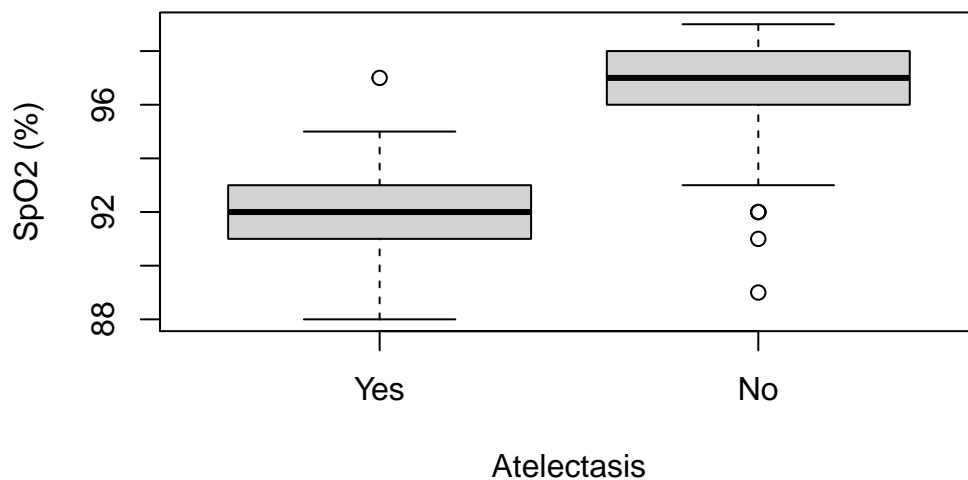
data: frequencies

X-squared = 0.13836, df = 1, p-value = 0.7099

The location of atelectasis was not different according to oxygen use status (p=0.71).

Atelectasis - SpO2

Atelectasis	n	spo2_median	Q1	Q3	min	max
Yes	77	92	91	93	88	97
No	159	97	96	98	89	99



Distribution not normal and influential outliers. Will assess non-parametrically.

Wilcoxon rank sum test with continuity correction

data: spo2_VP0 by atelectasis

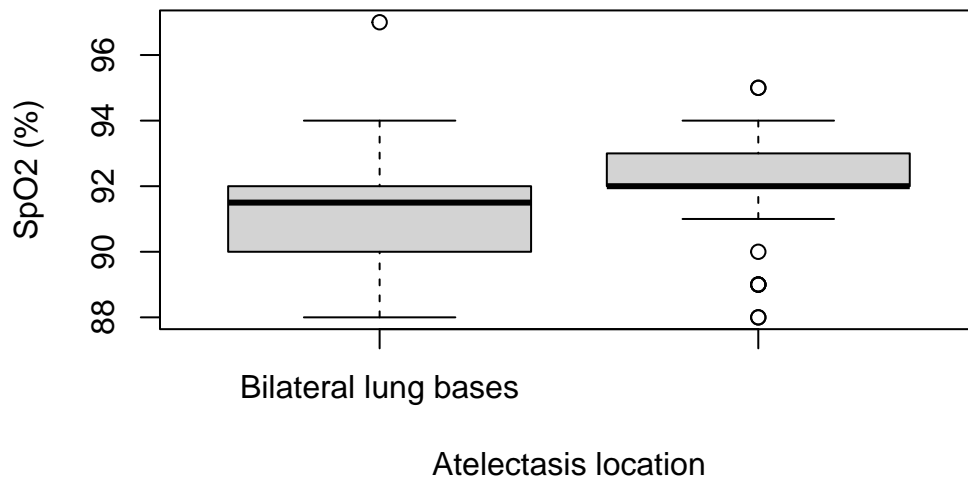
W = 465.5, p-value < 2.2e-16

alternative hypothesis: true location shift is not equal to 0

The median SpO2 was significantly lower in patients with atelectasis (92, IQR: 91-93) compared to those without (97, IQR: 96-98) ($p < 0.001$).

Atelectasis location - SpO2

Atelectasis location	n	spo2_median	Q1	Q3	min	max
Bilateral lung bases	24	91.5	90	92	88	97
Right lung base predominance	53	92.0	92	93	88	95



Distribution not normal and likely influential outliers. Will assess non-parametrically.

Wilcoxon rank sum test with continuity correction

data: spo2_VP0 by atelectasis_location

W = 393, p-value = 0.006227

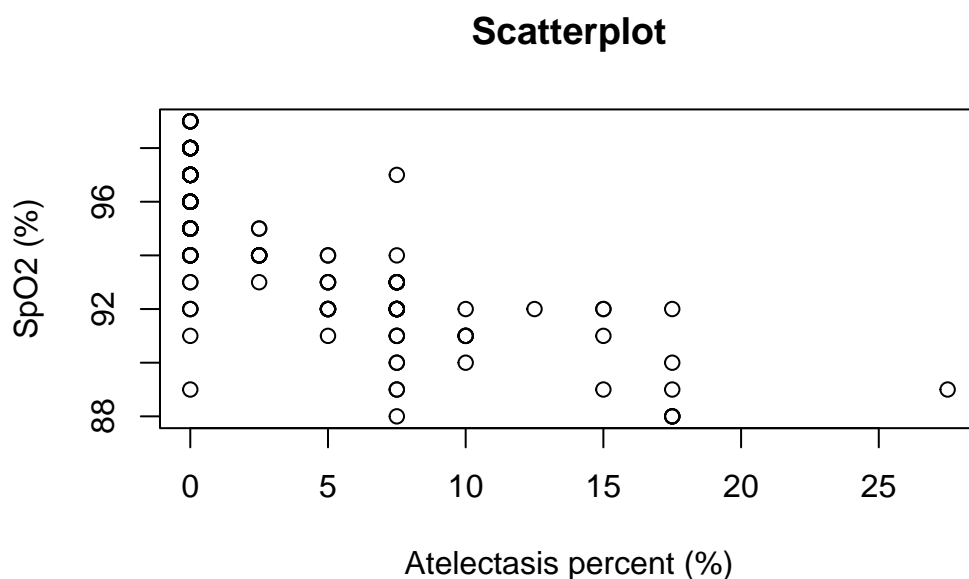
alternative hypothesis: true location shift is not equal to 0

The median SpO2 was significantly lower in patients with bilateral atelectasis (92, IQR: 92-93) compared to those with unilateral atelectasis (91.5, IQR: 90-92) (p=0.006).

Atelectasis percent - SpO2

Smooth term?

Scatterplot



Decreasing SpO2 as atelectasis percent increases.

Would a smooth term be more useful to model SpO2?

Models evaluated with the accompanying sourced script ***nonlinear_Atelectasis_SpO2.R***

All models are significantly better than linear. Thus, using a smooth term for atelectasis percent is better than modelling a linear relationship.

Best AIC:

model	AIC
k=2	892.1
k=4	888.6
k=6	885.8
k=8	885.8

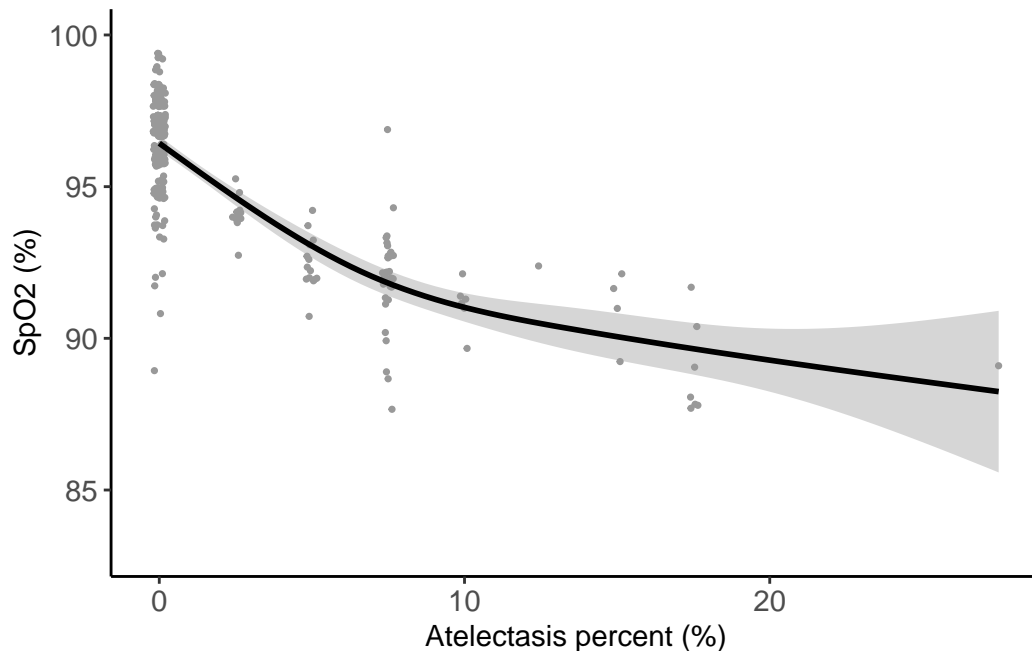
Regarding AIC, no model offers greater improvement in AIC than k=6. Will try a model with k=5.

Best AIC:

model	AIC
k=4	888.6

k=5	885.1
k=6	885.8

There is a drop in AIC for k=5, which also offers the best k-index. Nonetheless, one problem with this is that the extra knot is explaining a clump around 12.%, for which there was only one single observation. Thus, it is likely that this clump and additional knot is only explaining noise in the data, and would thus not be a good representation of the trend in the variable. Thus, will keep k=4 to model as this model offers the best visual representation of the trend in all categories.



Negative monotonic relationship since SpO2 decreases as BMI increases. Will assess Spearman's correlation coefficient to report in paper:

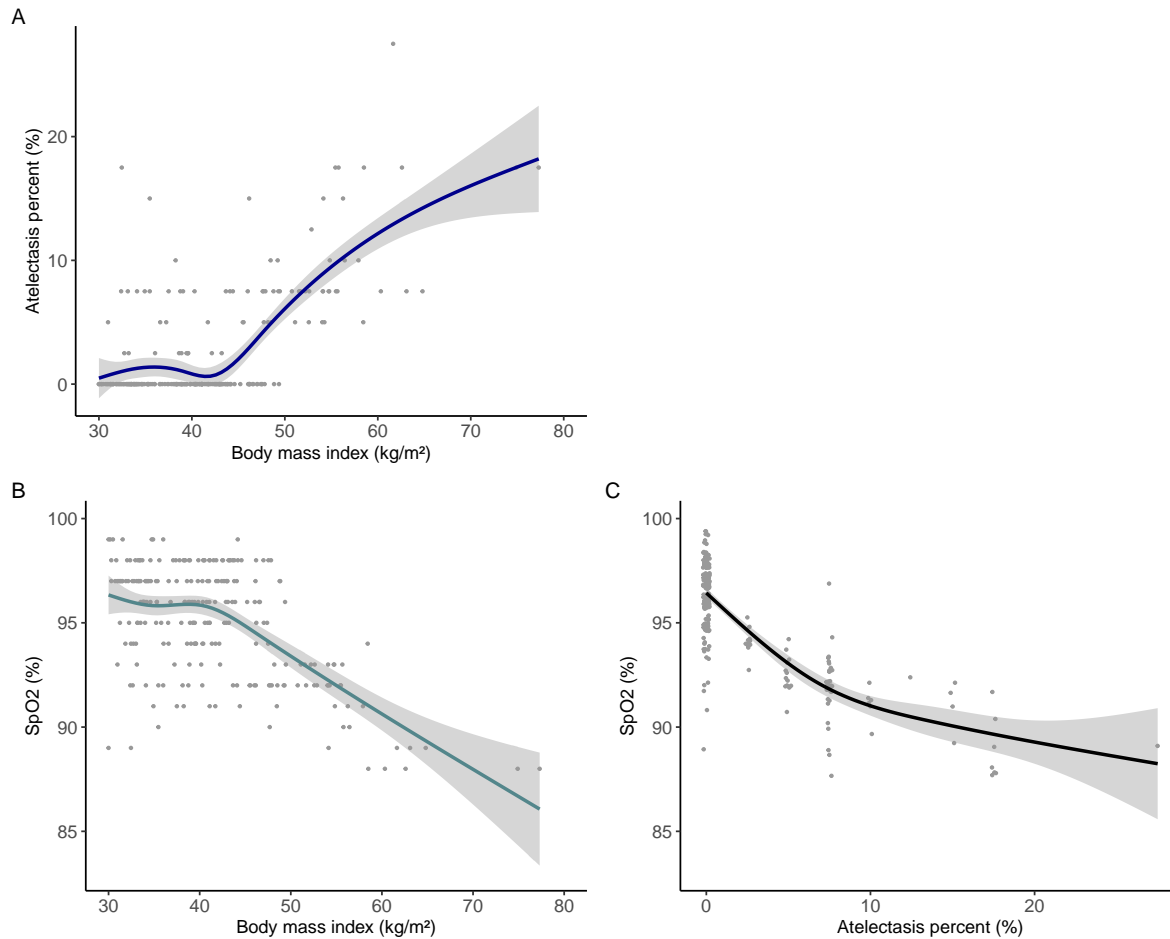
Spearman's rank correlation rho

```
data: spo2_VP0 and atelectasis_percent
S = 3883525, p-value < 2.2e-16
alternative hypothesis: true rho is not equal to 0
sample estimates:
rho
-0.7727568
```

Atelectasis percent exhibited a negative non-linear monotonic relationship with SpO2 (**Figure 1C**, rho= -0.773, p<0.001).

Figure 1

Created with the accompanying sourced script *Figure1.R*



Ordinal variable

Since there is only one participant in the 30% category, will collapse with the 20 category for further analyses:

0%	2.5%	5%	7.5%	10%	12.5%	15%	17.5%
159	11	14	33	6	1	4	8

Distribution not normal, group sizes are different and there are outliers in both directions, depending where you are located. Thus, will proceed with non-parametric assessment:

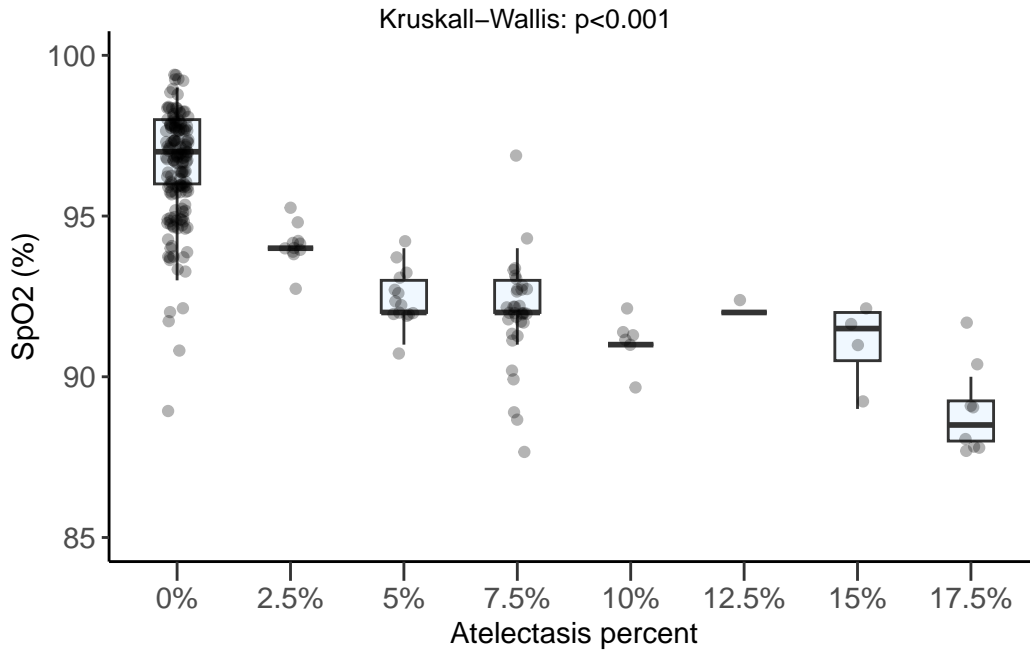
atelectasis_percent	n	spo2_median	Q1	Q3	min	max
0%	159	97.0	96.0	98.00	89	99
2.5%	11	94.0	94.0	94.00	93	95
5%	14	92.0	92.0	93.00	91	94
7.5%	33	92.0	92.0	93.00	88	97
10%	6	91.0	91.0	91.00	90	92
12.5%	1	92.0	92.0	92.00	92	92
15%	4	91.5	90.5	92.00	89	92
17.5%	8	88.5	88.0	89.25	88	92

Kruskal-Wallis rank sum test

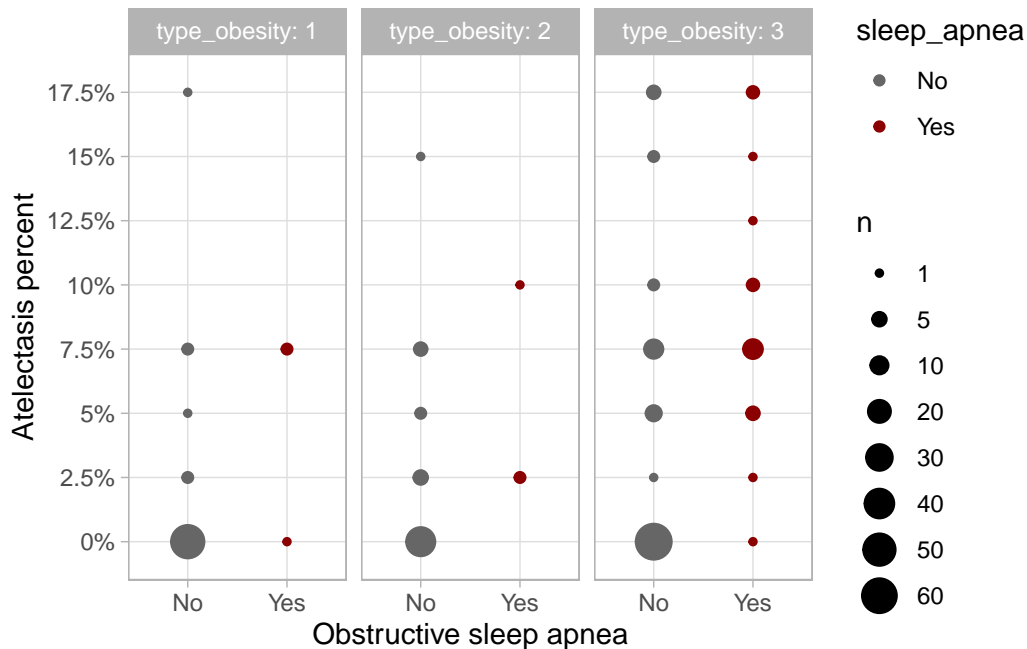
data: spo2_VP0 by atelectasis_percent

Kruskal-Wallis chi-squared = 141.19, df = 7, p-value < 2.2e-16

There was a decreasing trend in median SpO2 with higher atelectasis percentage extension ($p < 0.001$).



Relationship between OSA, obesity type and atelectasis percent:



Sleep apnea was more common with higher BMI categories and also with higher atelectasis percentage. Atelectasis percent increases at higher obesity classes.

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