



anses

- **MU ESTIMATION FROM TECHNICAL, MATRIX AND DISTRIBUTIONAL UNCERTAINTIES**
- **MU EXPRESSION IN TEST REPORTS**

EURLs *Campylobacter*, CPS & *Lm* webinar on MU  
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Bertrand LOMBARD

Senior Project Manager, Reference activities

Anses-Research and Reference Division – Strategy and Programmes Department, Maisons-Alfort

bertrand.lombard@anses.fr, mobile +33 6 15 54 19 94

**INVESTIGATE, EVALUATE, PROTECT**

# Combined and Expanded Standard Uncertainty



# Combined standard uncertainty

- 2 options provided in ISO 19036 (8.1.3)
  - Option 1: A combination of separately estimated:
    - ✓ technical standard uncertainty
    - ✓ matrix standard uncertainty
    - ✓ distributional standard uncertainties
  - Option 2: reproducibility standard deviation alone (technical standard uncertainty)
- Recommendation of EURs guide (2.1):  
**to use option 1 and not option 2**
  - ↶ Values of matrix uncertainty are provided

# Combined standard uncertainty based on separate technical, matrix and distributional standard uncertainties (option 1) (1)

- Estimate technical uncertainty as a reproducibility standard deviation
  - $U_{\text{tech}} = S_R$
- Estimate matrix uncertainty
  - $U_{\text{matrix}} = S_r$

# Combined standard uncertainty based on separate technical, matrix and distributional standard uncertainties (option 1) (2)

- Estimate any relevant distributional uncertainties from the data underlying the reported results
- Derive the **combined standard uncertainty  $u_c(y)$**

$$u_c(y) = \sqrt{u_{tech}^2 + u_{matrix}^2 + u_{Poisson}^2 + u_{conf}^2} \quad (\text{example})$$

- For a given method, not all the terms will be included in the calculation of combined standard uncertainty

E.g., a CCT without partial confirmation:  $u_c(y) = \sqrt{u_{tech}^2 + u_{matrix}^2 + u_{Poisson}^2}$

# Expanded uncertainty

- Calculate the **expanded uncertainty  $U$**  from the combined standard uncertainty  $u_c(y)$ , with a coverage factor  $k$ :

$$U = k \times u_c(y)$$

- In ISO 19036 ,  $k$  is chosen as a value of 2
  - To correspond approximately to a confidence level of 95%
  - Therefore

$$U = 2u_c(y)$$

# Expression of Measurement Uncertainty in test reports

Several decorative orange leaf-like shapes are scattered across the slide, primarily in the right half, behind the main title text.

# Reporting Measurement Uncertainty (1)

- MU reported in same unit as test result
- Number of figures in reported MU
  - To reflect practical measurement capability
  - And the same than for the test result
    - It is recommended that expanded uncertainty be rounded to **2 significant figures**



# Reporting Measurement Uncertainty (2)

Three options to express MU in test report:

- Using  $\log_{10}$  scale
  - Option 1:  $\log_{10}$  result  $\pm U$  :  $y \pm U \log_{10}$  cfu/g
  - Option 2:  $\log_{10}$  result with limits :  $y \log_{10}$  cfu/g [ $y - U$ ;  $y + U$ ]
- Using natural values (anti-log)
  - Option 3: natural result value with limits :  $x$  cfu/g [ $10^{y-U}$ ;  $10^{y+U}$ ]

# Example

Result (x) =  $1,00 \times 10^5$  cfu/g, therefore  $y = \log_{10}$  result (x) = 5,00, and  $U = 0,31 \log_{10}$

- Report using  $\log_{10}$  scale
  - $\log_{10}$  result  $\pm U$  :  $y \pm U \log_{10}$  cfu/g  
 $5,00 \pm 0,31 \log_{10}$  cfu/g
  - $\log_{10}$  result with limits :  $y \log_{10}$  cfu/g [ $y - U$  ;  $y + U$ ]  
 $y - U = 5,00 - 0,31 = 4,69$   
 $y + U = 5,00 + 0,31 = 5,31$   
 $5,00 \log_{10}$  cfu/g [4,69; 5,31]
- Report using natural values (anti-log)
  - Natural result value with limits :  $x$  cfu/g [ $10^{y-U}$  ;  $10^{y+U}$ ]  
 $10^{y-U} = 10^{4,69} = 48977$  (rounded to  $4,90 \times 10^4$ )  
 $10^{y+U} = 10^{5,31} = 204173$  (rounded to  $2,04 \times 10^5$ )  
 $1,00 \times 10^5$  cfu/g [ $4,90 \times 10^4$  ;  $2,04 \times 10^5$ ]

# Results below Limit of Quantification (LOQ)

- Can arise:
  - for a CCT, when the number of counted colonies is zero,  $\Sigma C = 0$
  - for a CCT with partial confirmation, when the number of confirmed colonies is zero,  $n_c = 0$
- Not covered today, see ISO 19036, clause 9.2, including examples

# Reporting Measurement Uncertainty

Include in the test report an explicit statement:

- the indicated MU is an expanded uncertainty
- the confidence level (95%)
- MU has been estimated in accordance with EN ISO 19036

“The reported expanded measurement uncertainty has been estimated in accordance with ISO 19036 and is based on a standard uncertainty multiplied by a coverage factor of  $k = 2$ , providing a level of confidence of approximately 95 %.”