

# New-Generation Interferometric Polarimetry

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QU-ESO Workshop

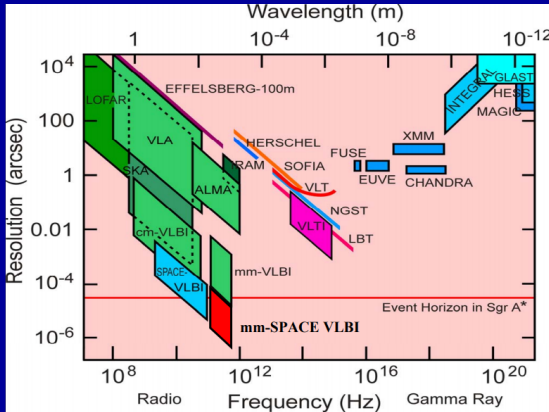
Munich (October 2017)

# Outline



- New Observational Windows.
  - ▶ Wide bandwidths, extreme sensitivity, high frequencies.
- Rotation Measure on the Widest Bandwidths.
  - ▶ RM Synthesis, RM CLEAN, and super-Gaussian modelling.
- Beating the Dynamic Range.
  - ▶ Primary-beam Muller deconvolution.
  - ▶ Rotation-invariant CLEANing.
  - ▶ Calibration artifacts: Dterms and cross-pol gains. Monte Carlo assessment.
- The Highest Sensitivities.
  - ▶ Differential polarimetry.
- The Highest Angular Resolutions.
  - ▶ Limitations of the “classical” pol. calibration.
  - ▶ Fractional polarizations in Fourier domain.
  - ▶ Wide bandwidths (linear polarizers) in VLBI.

# Observational Windows



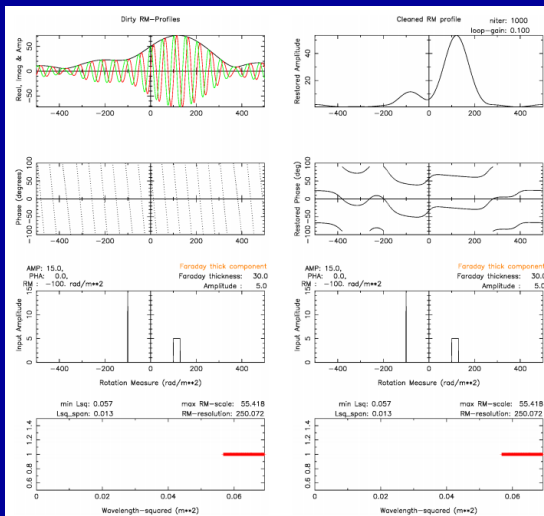
New frequency & resolution windows with high sensitivities & wide BW (e.g., several GHz at ALMA, VLA, VLBI; fract. BW of  $\sim 1$  at LOFAR).



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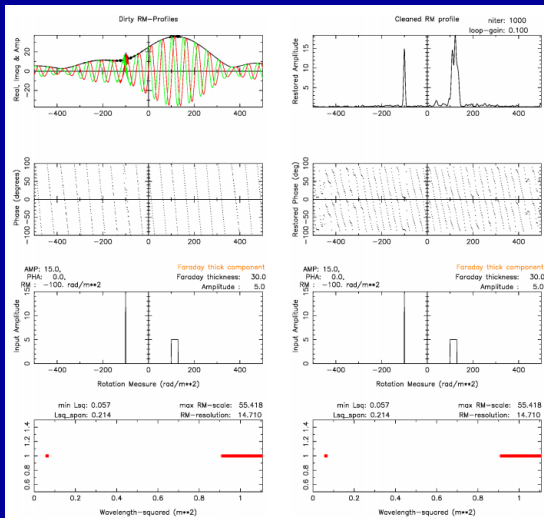
# Wide Bandwidth Polarimetry

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RM Synthesis and RM CLEAN (Raja 2016; based on Brentjens & de Bruyn 2005; Heald 2008).

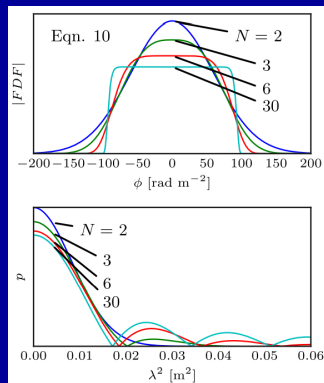
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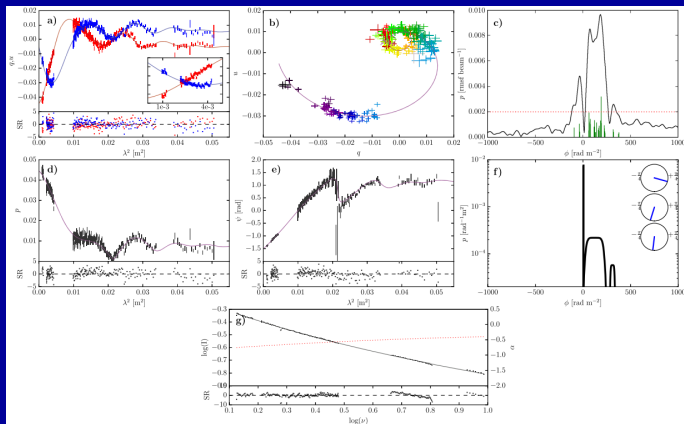
# Wide Bandwidth Polarimetry

$$p(\phi) = -\frac{A}{\sqrt{2\pi}\sigma_\phi} \exp\left(2i\psi_0 + \frac{-|\phi - \phi_{\text{peak}}|^N}{2\sigma_\phi^N}\right)$$



Faraday-thick structures (conceptually similar to MS CLEAN).  
Anderson et al. (2017)

# Wide Bandwidth Polarimetry



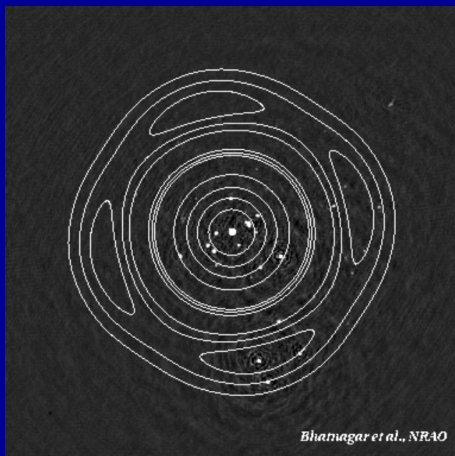
Faraday-depth reconstruction (Anderson et al. 2017)





# High Dynamic Range Polarimetry

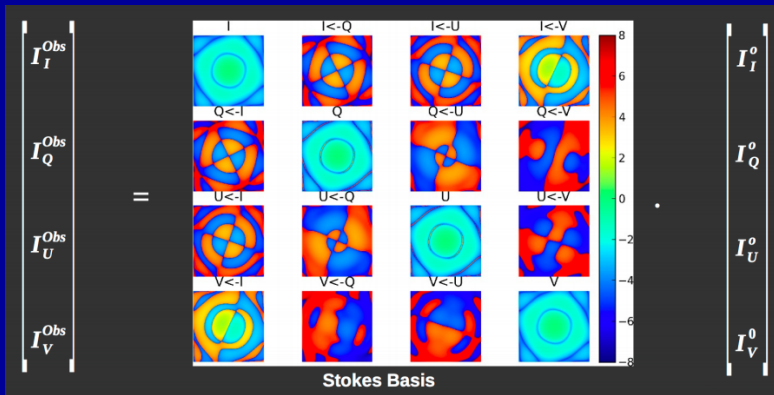
# High Dynamic Ranges: Primary Beam



# High Dynamic Ranges: Primary Beam



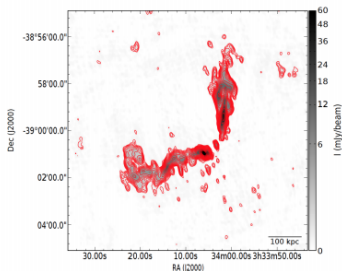
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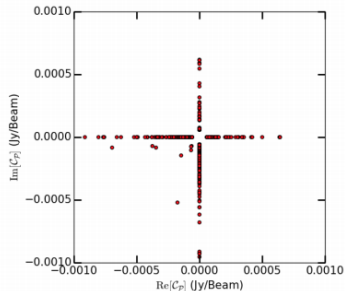
Mueller decomposition of beam response (Bhatnagar 2016).

# High Dynamic Ranges: CLEANing Biases

This is ATCA data of a polarised radio galaxy from (Pratley, Johnston-Hollitt et al. 2013)



This is the CLEAN components for the source on an Argand diagram. Why are the majority of the components along the axes?

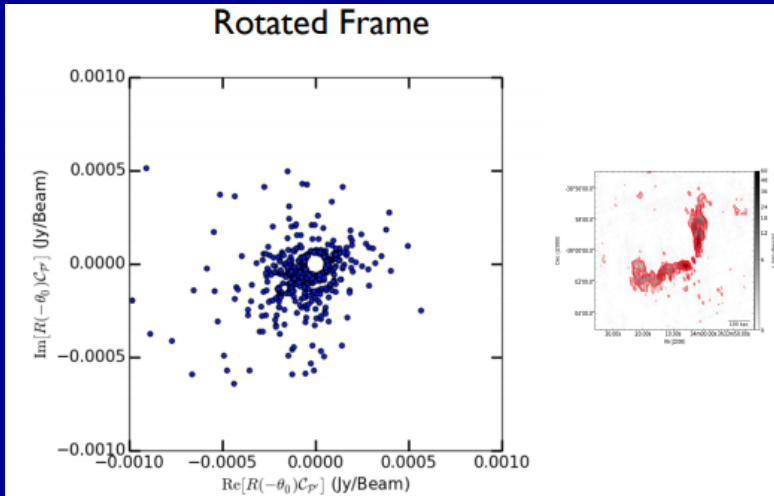


CLEAN in  $IQUV$  space limits the dynamic range of  $m$  (Johnston & Hollitt 2016).

# High Dynamic Ranges: CLEANING Biases



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Rotation-invariant CLEANing (Johnston & Hollitt 2016).



# Intermezzo:

## The Measurement Equation

# The Measurement Equation



- Electric field seen by antenna  $A$ :  $\vec{E}^A$ .
- For baseline  $AB$ , the coherency matrix is  $E^{AB} = \vec{E}^A (\vec{E}^B)^H$
- In the  $\alpha$ - $\beta$  polarization basis, the coherency matrix for baseline  $AB$  is:

$$E^{AB} = \begin{pmatrix} \langle E_\alpha^A (E_\alpha^B)^* \rangle & \langle E_\alpha^A (E_\beta^B)^* \rangle \\ \langle E_\beta^A (E_\alpha^B)^* \rangle & \langle E_\beta^A (E_\beta^B)^* \rangle \end{pmatrix}$$

- The coherency matrix is related to the Fourier transform of the brightness matrix!

$$E^{AB} = \mathcal{F}[S]_{(u,v)}$$

- Brightness matrix: For X-Y polarization basis:

$$E^{AB} = \begin{pmatrix} \langle E_x^A (E_x^B)^* \rangle & \langle E_x^A (E_y^B)^* \rangle \\ \langle E_y^A (E_x^B)^* \rangle & \langle E_y^A (E_y^B)^* \rangle \end{pmatrix} ; S = \begin{pmatrix} I + Q & U + jV \\ U - jV & I - Q \end{pmatrix}$$

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- The coherency matrix is related to the Fourier transform of the brightness matrix!

$$E^{AB} = \mathcal{F}[S]_{(u,v)}$$

- Brightness matrix: For R-L polarization basis:

$$E^{AB} = \begin{pmatrix} \langle E_r^A (E_r^B)^* \rangle & \langle E_r^A (E_l^B)^* \rangle \\ \langle E_l^A (E_r^B)^* \rangle & \langle E_l^A (E_l^B)^* \rangle \end{pmatrix}; S = \begin{pmatrix} I + V & Q + jU \\ Q - jU & I - V \end{pmatrix}$$



# Coherency matrix and Visibility matrix.



- Voltage for antenna  $A$  with an  $\alpha$ - $\beta$  polarizer is:  $\vec{v}^A = J^A \vec{E}^A$ , where  $\vec{E}^A$  is the electric field in the  $\alpha$ - $\beta$  base and  $J^A$  is the Jones matrix that calibrates antenna  $A$ .
- The visibility matrix (i.e., voltage cross-correlations) is:

$$V^{AB} = \vec{v}_A (\vec{v}_B)^H = \begin{pmatrix} \langle v_\alpha^A (v_\alpha^B)^* \rangle & \langle v_\alpha^A (v_\beta^B)^* \rangle \\ \langle v_\beta^A (v_\alpha^B)^* \rangle & \langle v_\beta^A (v_\beta^B)^* \rangle \end{pmatrix}$$

- Since  $\vec{v}_i = J_i \vec{E}_i$ ,

$$V^{AB} = J_A \vec{E}_A (\vec{E}_B)^H J_B^H = J_A \begin{pmatrix} \langle E_\alpha^A (E_\alpha^B)^* \rangle & \langle E_\alpha^A (E_\beta^B)^* \rangle \\ \langle E_\beta^A (E_\alpha^B)^* \rangle & \langle E_\beta^A (E_\beta^B)^* \rangle \end{pmatrix} J_B^H$$



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# Back to HDR Polarimetry

# High Dyn. Ranges: Leakage biases



- Effect of the **D**terms on the  $XY^*$  cross-correlations:

$$XY^* \rightarrow XY^* + D_x^a YY^* + (D_y^b)^* XX^*$$

# High Dyn. Ranges: Leakage biases



- Effect of the **Dterms** on the  $XY^*$  cross-correlations:

$$XY^* \rightarrow XY^* + D_x^a YY^* + (D_y^b)^* XX^*$$

- In terms of the brightness matrix (i.e., assuming a point source):

$$XY^* \rightarrow U_{ant} + jV + D_x^a(I - Q_{ant}) + (D_y^b)^*(I + Q_{ant})$$

- Re-arranging terms:

$$XY^* \rightarrow U_{ant} + Q_{ant} \left( (D_y^b)^* - D_x^a \right) + jV + I(D_x^a + (D_y^b)^*)$$

Symmetries in Dterm distributions may relate to spurious  $V$  and/or  $m$

# High Dyn. Ranges: Leakage biases



- $V^{obs} = D_a X V_{ab}^{true} X^H D_b^H$  ;  $X = \begin{pmatrix} 1 & 0 \\ 0 & e^{j\alpha} \end{pmatrix}$  ;  $D_a = \begin{pmatrix} 1 & D_a^L \\ D_a^R & 1 \end{pmatrix}$

$$RL^* \rightarrow ((D_a^R + (D_b^L)^*) I + m) e^{-j\alpha} + O(D^2)$$

$$LR^* = ((D_a^L + (D_b^R)^*) I + m^*) e^{j\alpha} + O(D^2)$$

- Unpolarized** calibrator:

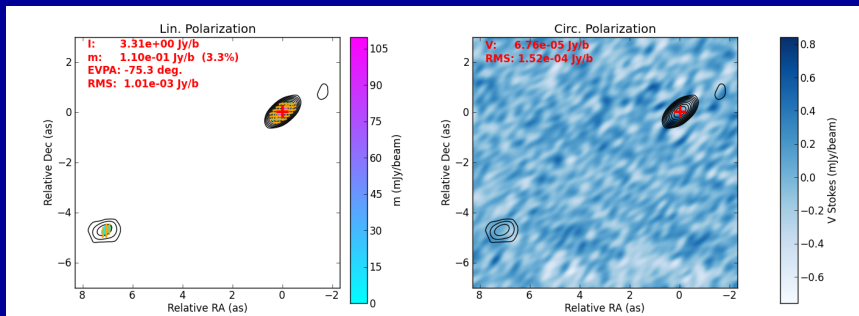
$$(D_a^L, D_a^R, e^{j\alpha}) \rightarrow (D_a^L e^{j\Delta} + jK, D_a^R e^{-j\Delta} + jK, e^{j(\alpha-\Delta)})$$

- Polarized** calibrator:

$$(D_a^L, D_a^R, e^{j\alpha}) \rightarrow (D_a^L + jK, D_a^R + jK, e^{j(\alpha)})$$

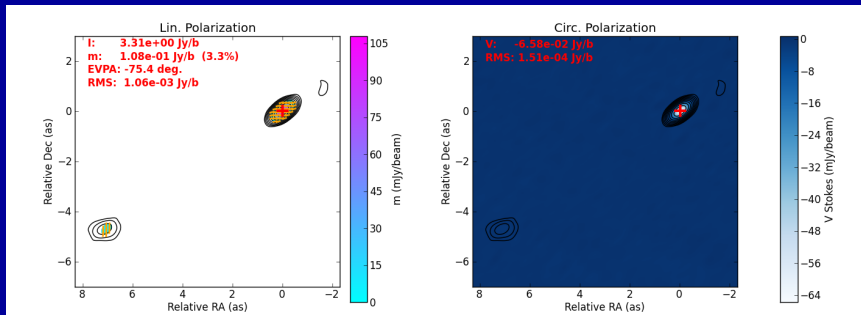
Dterm ambiguities may inject 2nd-order effects in the polarimetry.

# Bias in the D-terms?



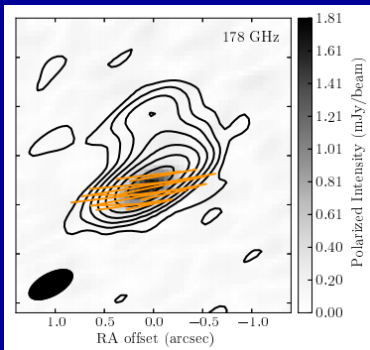
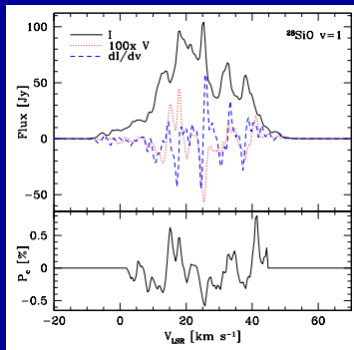
J0522–3627, ALMA Band 5 (172 GHz).  
Original calibration.

# Bias in the D-terms?



J0522–3627, ALMA Band 5 (172 GHz) with  
 $D_x \rightarrow D_x + 0.01j$  and  $D_y \rightarrow D_y - 0.01j$ .

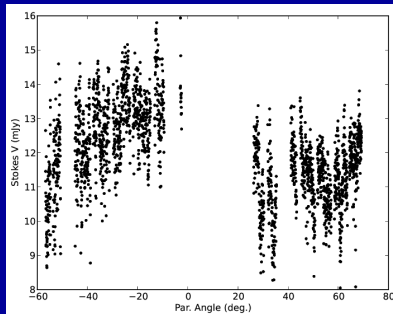
# Bias in the D-terms?



VY CMa, ALMA Band 5 (172 GHz). Spectrum of  $V$  not proportional to  $I$  (Vlemmings et al. 2017).



# High Dyn. Ranges: X-Y phase offset



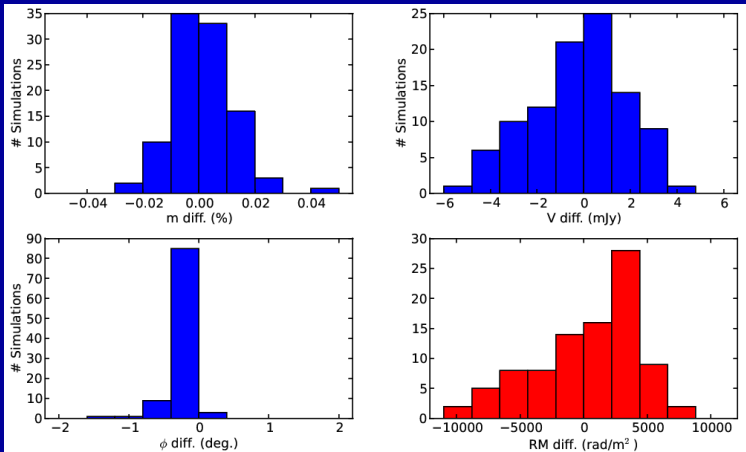
$$V^{spur} \sim V^{true} \cos \Delta + (U \sin(\phi - \psi) + Q \cos(\phi - \psi)) \sin \Delta$$

(e.g., 3C 273 with ALMA @ 1.3 mm; Hovatta et al. in prep.)

# High Dyn. Ranges: X-Y phase offset



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Monte Carlo analysis (e.g.,  $G \rightarrow D$  cross-talk in 3C273 with ALMA)



# High-Sensitivity Polarimetry

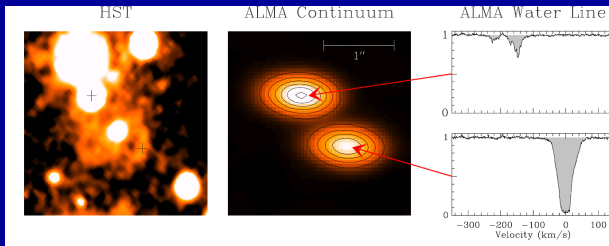
# High Sensitivities: Intra-field Differential Observables



- The relative brightness within the same observed field is a **very precise and accurate** quantity (only limited by *dynamic range*).
- Using the relative brightness, we can improve variability analyses by **several orders of magnitude**.

# High Sensitivities: Intra-field Differential Observables

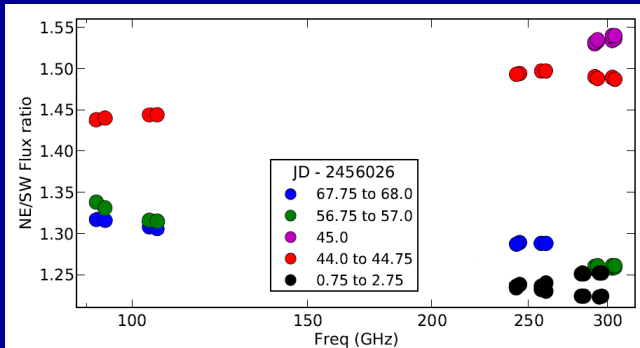
- The relative brightness within the same observed field is a **very precise and accurate** quantity (only limited by *dynamic range*).
- Using the relative brightness, we can improve variability analyses by **several orders of magnitude**.
- We need:
  - ▶ A source with a **resolved structure**.



# Relative brightness NE/SW



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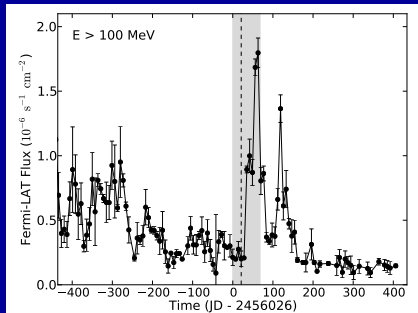


Martí-Vidal et al. (2013)

# ... and a strong $\gamma$ -ray counterpart!



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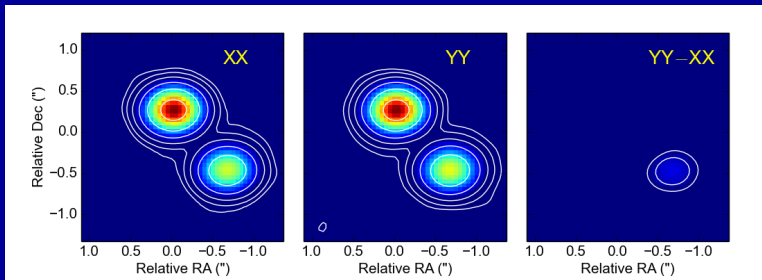






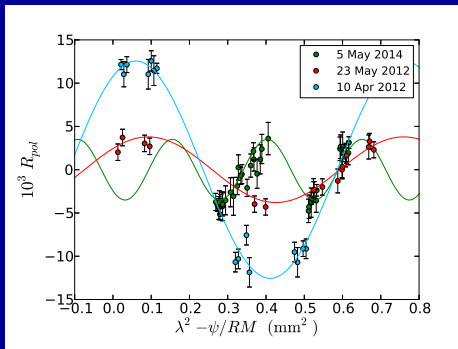
# Dual Differential polarimetry NE/SW

- ALMA observed in two polarizations, **XX** e **YY**.
- **XX** is related to the brightness distribution of  $I + Q$ .  
**YY** is related to  $I - Q$ .
- Studying the relative brightness of the **XX** and **YY** images, we can extract polarimetry information from the observed source.



Martí-Vidal et al. (2015)

# Dual Differential polarimetry NE/SW

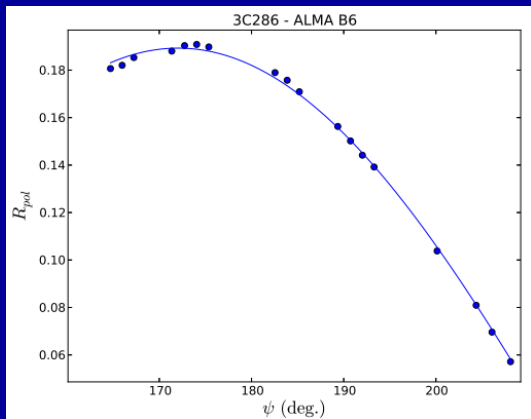


- The largest Faraday rotation so far ( $RM$  of  $3 \times 10^8 \text{ rad m}^{-1}$ ).
- The highest rest frequencies so far (1 THz, corrected for  $z$ ). This corresponds to  $R \sim 0.01 \text{ pc}$  from the jet base.
- Highest  $RM$  measured in other AGN (at lower frequencies):  $\sim 10^6 \text{ rad m}^{-1}$  at 250 GHz (e.g., Plambeck et al. 2014).

# More (ALMA) data. 3C 286 (SV @ B6)



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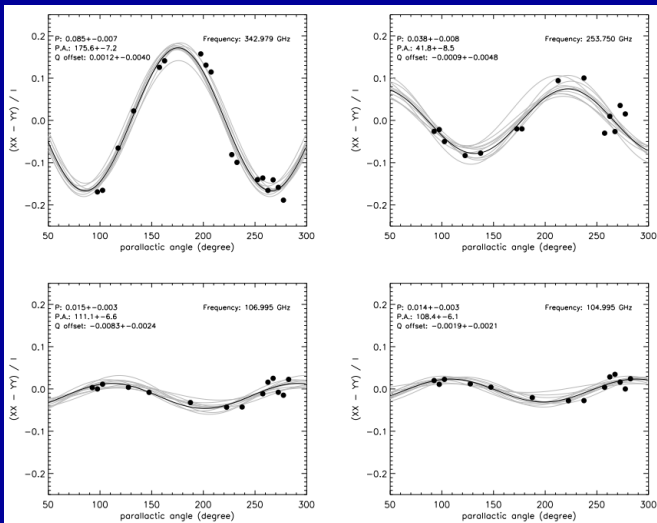
Martí-Vidal et al. *A&A* (2016)

(Result compatible with full-pol calibration: Nagai et al. *ApJ* 2016)

# More (ALMA) data. Sgr A\* (SV @ B3,6,7)



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Baobab et al. *A&A* (2016)



# Polarimetry at the Highest Angular Resolutions

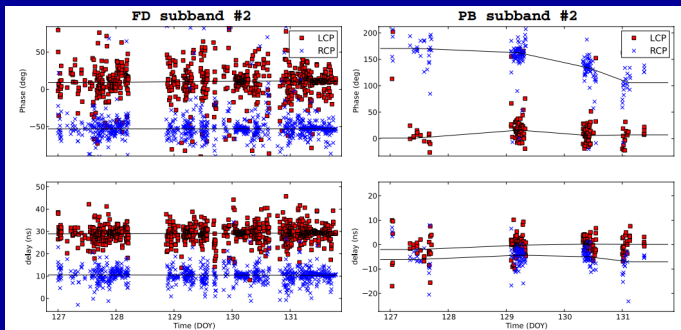
# Highest Angular Resolutions: VLBI



- Limitations of the “Classical” Calibration.
  - ▶ Effects of some basic tenets that may not hold. (Marti-Vidal et al. 2012)
- Fractional polarization in Fourier domain.
  - ▶ Robust observables independent of deconvolution artifacts. (Johnson et al. 2015)
- Use of wide bandwidths for higher sensitivities.
  - ▶ Linear polarizers in VLBI for higher polarization purity (Marti-Vidal et al. 2016).

# Classical VLBI Polarization Calibration

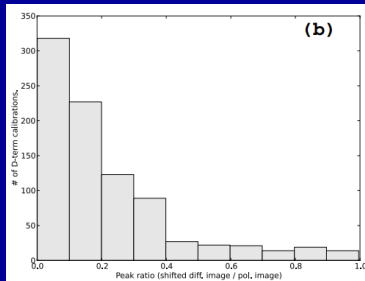
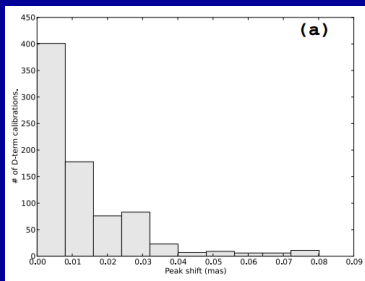
- R-L phase stability is assumed.
- Only first-order D-term effects are considered.
- Absolute EVPA is unknown *per sé*.



Cross-pol. phases can vary on day timescales  
(Marti-Vidal et al. 2012)

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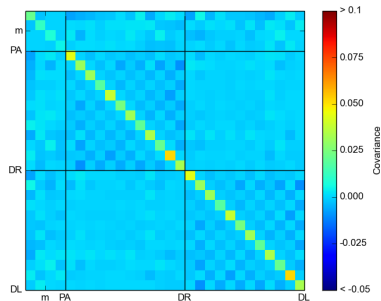
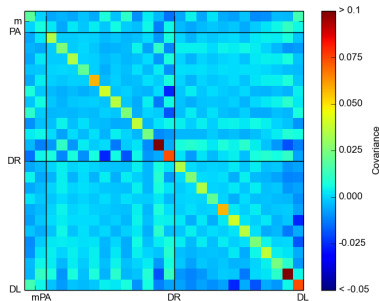


Heavy pol. cutoffs required to deal with residual D-term effects  
(Marti-Vidal et al. 2015)



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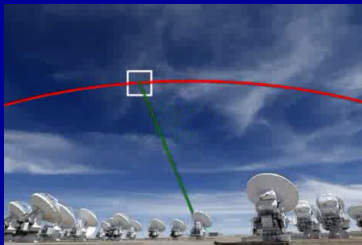


D-term covariance matrix for one calibrator (left) and 2 calibrators (right), with the same total observing time (Martí-Vidal 2016).

# Parallactic angle in VLBI

$$P_{xy} = \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix} \quad P_{rl} = \begin{pmatrix} e^{j\phi} & 0 \\ 0 & e^{-j\phi} \end{pmatrix}$$

- Is the rotation of the antenna mount axis w.r.t. the sky.
- Is **deterministic**. Apply it **before** the phase (and delay/rate) calibration!
- It does **not commute** with the gains for **linear polarizers**.
- In VLBI, it also mixes  $V_{xx}$  and  $V_{yy}$  with  $V_{xy}$  and  $V_{yx}$ .



# PolConvert



- CASA task for linear-circular conversion (Marti-Vidal et al. 2016).
- Works on either **SWIN** (i.e., DiFX) or **FITS-IDI** files.
- Designed for **ALMA-VLBI**, but already tested on other arrays.
- Either **pure linear** or **mixed-polarization** fringes can be handled!

```
CASA <7>: inp
-----> inp()
# polconvert ::
Version 1.2

Converts VLBI visibilities from mixed-polarization basis (i.e.,
linear-to-circular) into circular basis. Works with single VLBI stations
as well as with phased arrays (i.e., phased ALMA).

IDI                = '/media/marti/LaCie_3/DATA/APP/VLBA_B3/MP1FR/' # Input
                  # FITS-IDI file with VLBI
                  # visibilities. It can also be a
                  # directory containing SWIN files from
                  # DiFX.
OUTPUTIDI         = '/media/marti/LaCie_3/DATA/APP/VLBA_B3/MP1FR/' # Output
                  # FITS-IDI file (or SWIN directory).
                  # If equal to IDI, the file(s) will
                  # be overwritten
DiFXinput         = '/media/marti/LaCie_3/DATA/APP/VLBA_B3/MP1FR/bn34a_01.input' # I
                  # f SWIN files are being converted,
                  # this must be the *.input file used
                  # by DiFX.
doIF              = [35] # List of IFs to convert. Default means
                  # all.
LinAntIdx        = [1] # List of indices of the linear-
                  # polarization antennas in the IDI
                  # file
Range            = [1] # Time range to convert (integer list;
                  # AIPS format). Default means all
                  # data
ALMAvis         = '/home/marti/WORKAREA/ARC/ARC_TOOLS/PolConvert/TEST_DATA/VLBA_B3.m
emmap/CONCAT_spw1.ms' # I
                  # f ALMA has been used, this is the
                  # measurement set with the intra-ALMA
                  # visibilities
spw              = 0 # Spectral window in ALMAvis that
                  # contains the VLBI band.
calAPP          = '/home/marti/WORKAREA/ARC/ARC_TOOLS/PolConvert/TEST_DATA/VLBA_B3.m
emmap/CALAPPHASE.tab' # I
                  # f ALMA has been used, this is the
                  # combined ASDM CALAPPHASE table from
                  # the ASDM. The list of measurement
```

```
gains             = ['NONE'] # Gain tables to pre-calibrate the
                  # linear-pol VLBI stations (one list
                  # of gains per linear-pol station).
dterms           = ['NONE'] # D-term tables to pre-calibrate the
                  # linear-pol VLBI stations (one table
                  # per linear-pol station).
XYadd            = [0.0] # Add manually a phase between X and Y
                  # before conversion (in deg.). One
                  # value per linear-pol station.
swapXY           = [False] # Swap X-Y before conversion. One value
                  # per linear-pol VLBI station.
swapRL           = False # Swap R-L of the OTHER antenna(s) when
                  # plotting the fringes.
plotIF          = 35 # IF index to plot. Default means to
                  # NOT plot.
plotRange        = [0, 0, 20, 0, 0, 8, 22, 0] # Time range to plot (integer
                  # list; AIPS format). Default means
                  # to NOT plot
plotAnt         = 2 # Index of the other antenna in the
                  # baseline to plot. Default means to
                  # NOT plot.
doTest          = True # If true, only compute (and eventually
                  # plot), the data, but leave OUTPUTIDI
                  # untouched.

CASA <b>: |
```

# How does PolConvert Work?



- Linear (or mixed) basis:  $V_{+\odot} = \begin{pmatrix} V_{xr} & V_{xl} \\ V_{yr} & V_{yl} \end{pmatrix}$
- Conversion to circular:  $V_{\odot\odot} = C_{\odot+} \times G \times V_{+\odot}$   
 $C_{\odot+}$  is well known. All we need is to know  $G$ !

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- Linear (or mixed) basis:  $V_{+\odot} = \begin{pmatrix} V_{xr} & V_{xl} \\ V_{yr} & V_{yl} \end{pmatrix}$
- Conversion to circular:  $V_{\odot\odot} = C_{\odot+} \times G \times V_{+\odot}$   
 $C_{\odot+}$  is well known. All we need is to know  $G$ !
- How does  $G$  look like?  $\rightarrow G = \begin{pmatrix} 1 & 0 \\ 0 & \rho \end{pmatrix}$   
where  $\rho$  is the cross-polarization gain, i.e.  $G_Y/G_X$ .
- In the basis of circular polarizers:

$$V_{\odot\odot}^{cal} \propto \begin{pmatrix} 1 & D \\ D & 1 \end{pmatrix} \times V_{\odot\odot}^{obs}, \text{ where } D = \frac{1 - \rho}{1 + \rho}$$

# Calibration Approach (non-ALMA)



Global *Cross-Polarization* Fringe Fitting (Martí-Vidal et al. 2016):

$$\min [\chi^2(\vec{\rho})] \text{ with } \chi^2(\vec{\rho}) = \sum_k (RR_k/LL_k - 1)^2 + \lambda \left[ \sum_k (RL_k^2 + LR_k^2) \right]$$

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$$\chi^2 = \chi_{+\odot}^2 + \chi_{\odot\odot}^2 \text{ with } \chi_{+\odot}^2 = \sum_k \omega_k \left[ \frac{V_{xr}^k \rho_+^{-1} - jV_{yr}^k}{V_{xl}^k \rho_+^{-1} + jV_{yl}^k} (e^{i\psi_+})(e^{i\psi_{\odot}})(\rho_{\odot}^{-1})^* - 1 \right]^2$$

# Calibration Approach (non-ALMA)



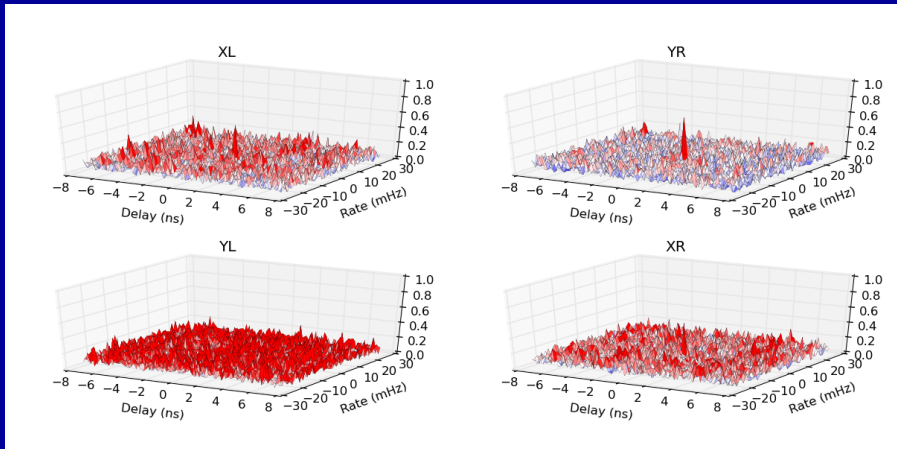
Global *Cross-Polarization* Fringe Fitting (Martí-Vidal et al. 2016):

$$\min [\chi^2(\vec{\rho})] \text{ with } \chi^2(\vec{\rho}) = \sum_k (RR_k/LL_k - 1)^2 + \lambda \left[ \sum_k (RL_k^2 + LR_k^2) \right]$$
$$\chi^2 = \chi_{+\odot}^2 + \chi_{\odot\odot}^2 \text{ with } \chi_{+\odot}^2 = \sum_k \omega_k \left[ \frac{V_{xr}^k \rho_+^{-1} - jV_{yr}^k}{V_{xl}^k \rho_+^{-1} + jV_{yl}^k} (e^{i\psi_+})(e^{i\psi_\odot})^* (\rho_\odot^{-1})^* - 1 \right]^2$$

- The idea is to derive **all** the cross-polarization gain ratios **in one shot** (for both linear and circular polarizers).
- This approach is **independent** of the source structure!
- And you can get the **absolute EVPA** calibration for free!!!

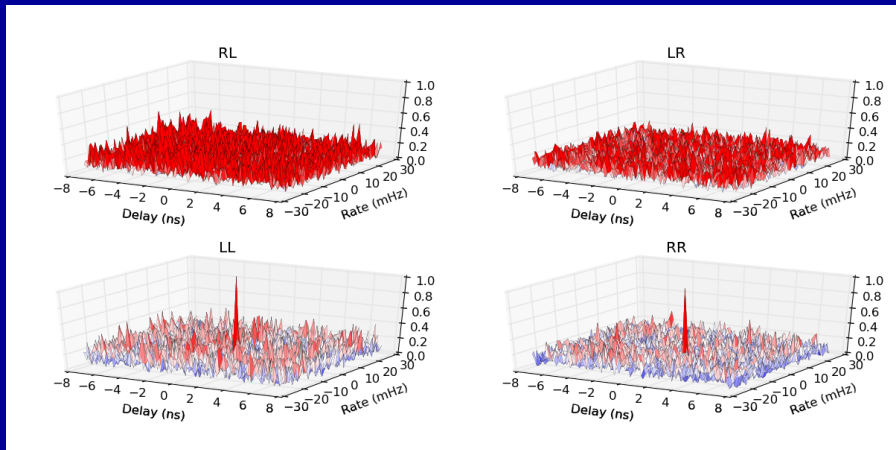


# GMVA (W Band; ON in linear)



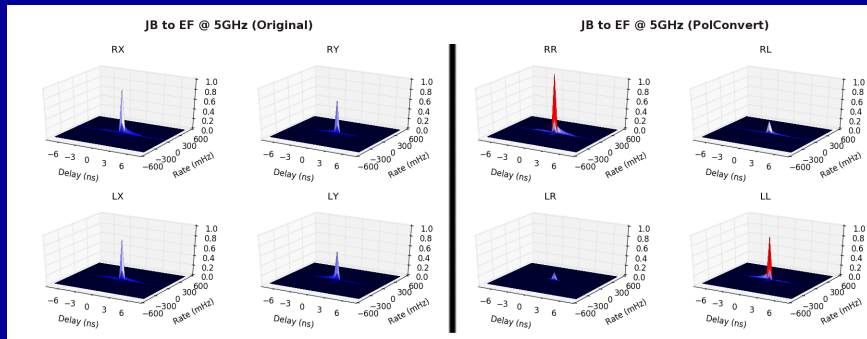
Onsala to Effelsberg (10 sec. on OJ287)

# GMVA (W Band; ON in linear)



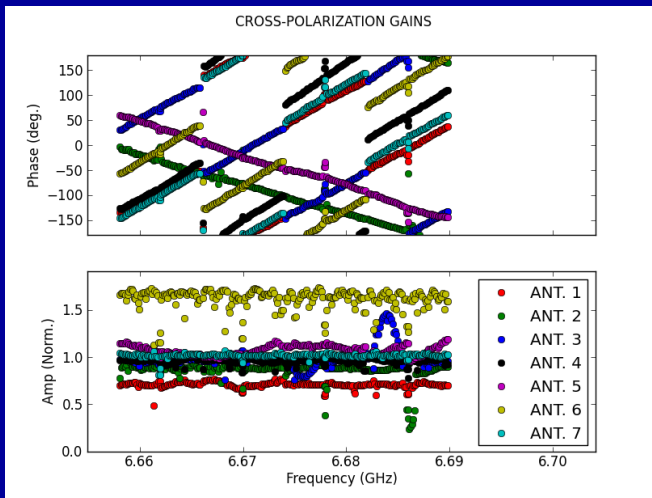
Onsala to Effelsberg (10 sec. on OJ287)

# eEVN (C Band; EB in linear)



(EO014, PI: M. Olech)

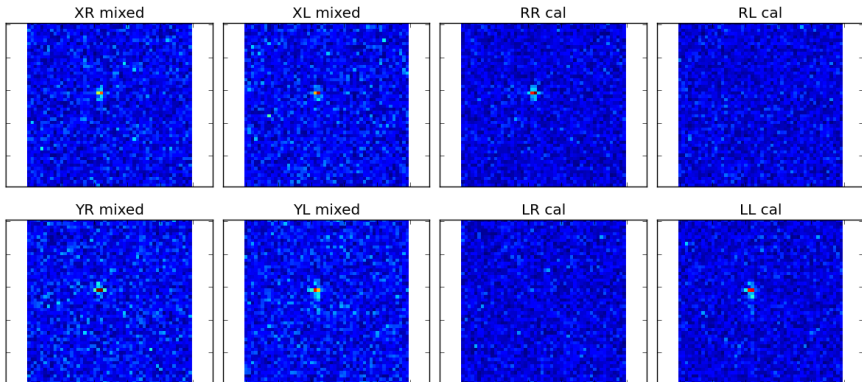
# eEVN (C Band; EB in linear)



GCPFF! Effelsberg (Ant. 2) is in green

# ATCA-KVN (Q/W bands; AT in linear)

DELAY-RATE FRINGE FOR IF 1 (BASELINE TO ANT #3) FROM 0-18:45:00 TO 0-18:49:59

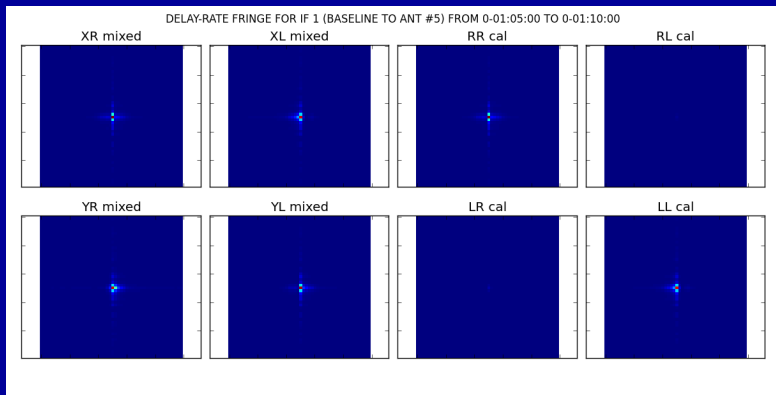


Chanapote (PI of data) & Dodson

# LBA (C Band; AT in linear)

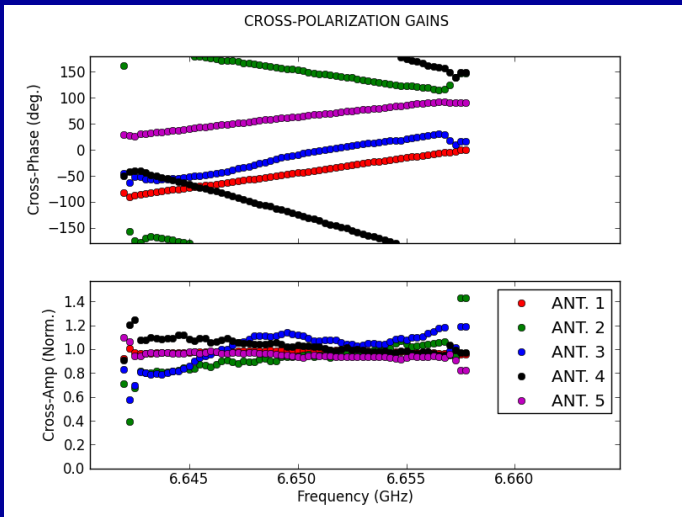


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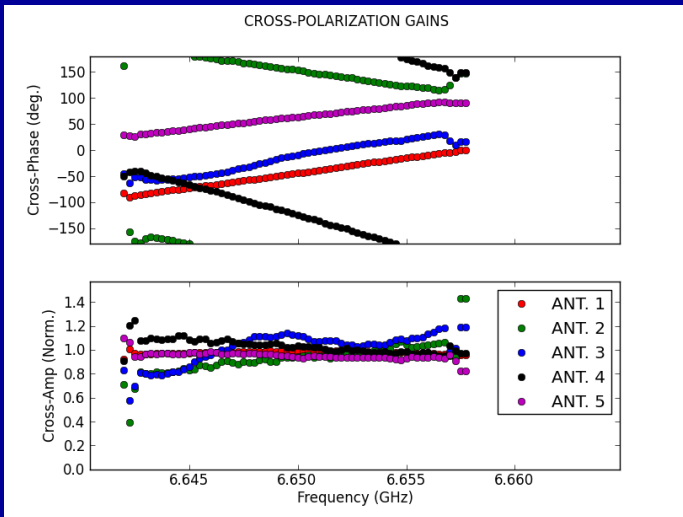
Chanapote (PI of data) & Dodson

# LBA (C Band; AT in linear)



GCPFF! ATCA in red

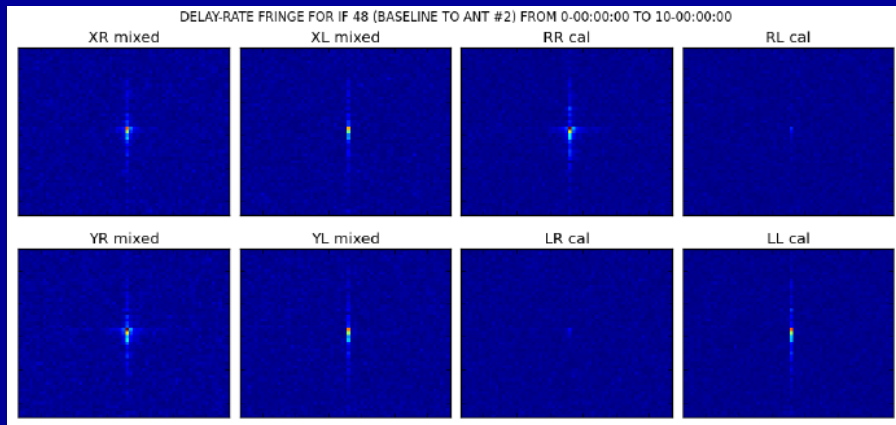
# LBA (C Band; AT in linear)



If used on Mopra → D-terms would lower from 15 – 20% ( $\pi/2$  plates) to 3 – 5%.



# ALMA-LMT @ B6 (230 GHz)



ALMA to LMT (México)

# ALMA-LMT @ B6 (230 GHz)

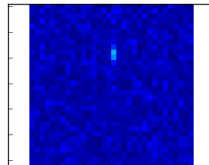
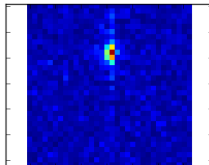
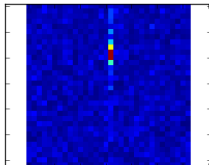
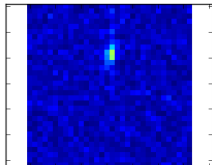
DELAY-RATE FRINGE FOR IF 36 (BASELINE TO ANT #2) FROM 0-00:00:00 TO 14-00:00:00

XR mixed

XL mixed

RR cal

RL cal

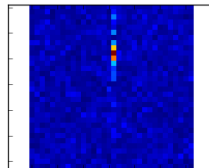
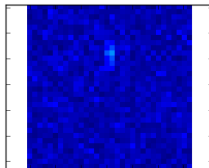
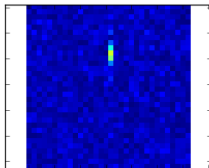
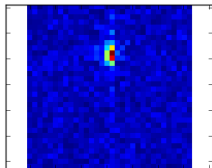


YR mixed

YL mixed

LR cal

LL cal



ALMA to LMT (México)

# Fractional Polarization in UV Domain

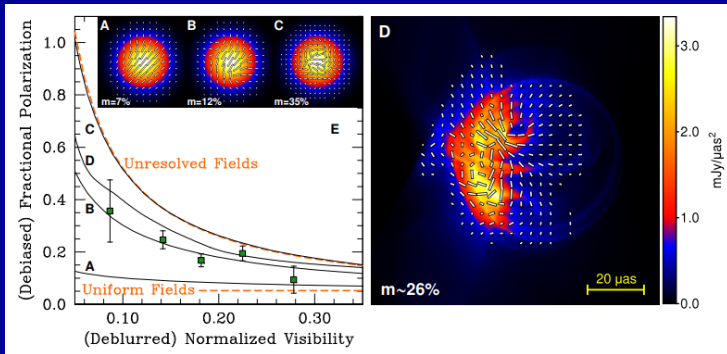


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$$\begin{aligned}\frac{\langle L_1 R_2^* \rangle}{\langle L_1 L_2^* \rangle} &\approx \left( \frac{G_{2,R}}{G_{2,L}} \right)^* [\check{m}^*(-\mathbf{u}_{12})e^{2i\phi_2} + D_{1,L}e^{-2i(\phi_1-\phi_2)} + D_{2,R}^*] \\ \frac{\langle L_1 R_2^* \rangle}{\langle R_1 R_2^* \rangle} &\approx \left( \frac{G_{1,L}}{G_{1,R}} \right) [\check{m}^*(-\mathbf{u}_{12})e^{2i\phi_1} + D_{1,L} + D_{2,R}^*e^{2i(\phi_1-\phi_2)}] \\ \frac{\langle R_1 L_2^* \rangle}{\langle L_1 L_2^* \rangle} &\approx \left( \frac{G_{1,R}}{G_{1,L}} \right) [\check{m}(\mathbf{u}_{12})e^{-2i\phi_1} + D_{1,R} + D_{2,L}^*e^{-2i(\phi_1-\phi_2)}] \\ \frac{\langle R_1 L_2^* \rangle}{\langle R_1 R_2^* \rangle} &\approx \left( \frac{G_{2,L}}{G_{2,R}} \right)^* [\check{m}(\mathbf{u}_{12})e^{-2i\phi_2} + D_{1,R}e^{2i(\phi_1-\phi_2)} + D_{2,L}^*] \\ \frac{\langle R_1 R_2^* \rangle}{\langle L_1 L_2^* \rangle} &\approx \left( \frac{G_{1,R}}{G_{1,L}} \right) \left( \frac{G_{2,R}}{G_{2,L}} \right)^* e^{-2i(\phi_1-\phi_2)}.\end{aligned}$$

Based on cross-polarization visibility ratios. Robust observables  
(Johnson et al. 2015)

# Fractional Polarization in UV Domain



Model-independent quantities related to polarization substructures!  
(Johnson et al. 2015)

# SUMMARY



- New observational windows are opening in interferometry: wider bandwidths, higher sensitivities, and higher image fidelities (dynamic ranges).
- New algorithms are being developed to squeeze the instrumentation capabilities.
- We summarize some examples of advanced algorithms in interferometric polarimetry:
  - ▶ Wide-bandwidth polarimetry → RM reconstruction in Faraday space.
  - ▶ High Dynamic Range → Primary-beam modelling, RI-CLEAN, ...
  - ▶ High Sensitivity → Differential observables.
  - ▶ High Angular Resolution (VLBI) → High-precision D-term estimates from multi-calibrator observations, fractional polarization in UV space, linear polarizers (PolConvert).

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## THANKS