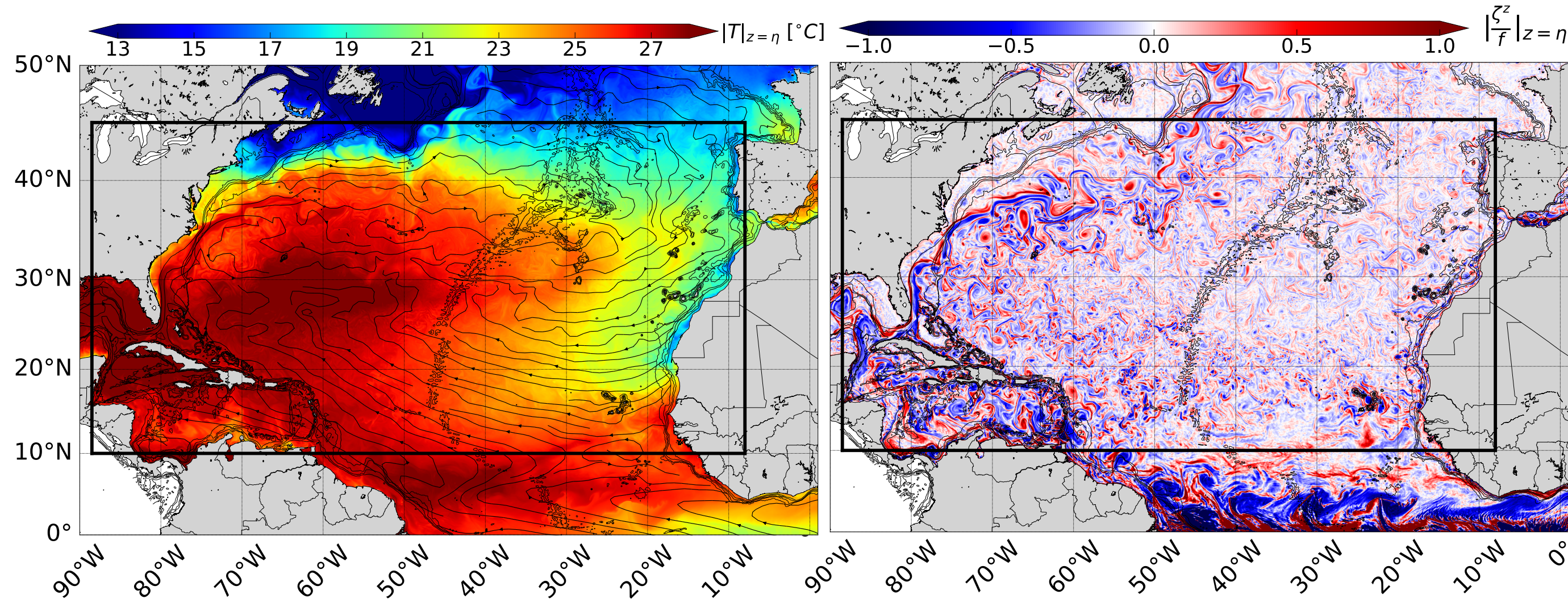


1. Context

What is the leading-order energy balance of the subtropical gyre of the North Atlantic?
Which flows does it rely on, and how does it vary in space?



- The North Atlantic is a key region in the global ocean circulation and plays a central role in regulating our climate (Ganachaud and Wunsch, 2000).
- Its response to climate change is constrained by energy transfers between basin-scale time-averaged currents and smaller-scale (hundreds to the order of a kilometer) time-varying currents, including low-frequency mesoscale and submesoscale currents and high-frequency internal waves.
- Although understanding the energy pathways of North Atlantic's subtropical gyre is crucial for accurately representing its role in climate models, we lack (1) a description of energy pathways at the basin-scale (2) based on a dataset simultaneously resolving the different time-varying flows.

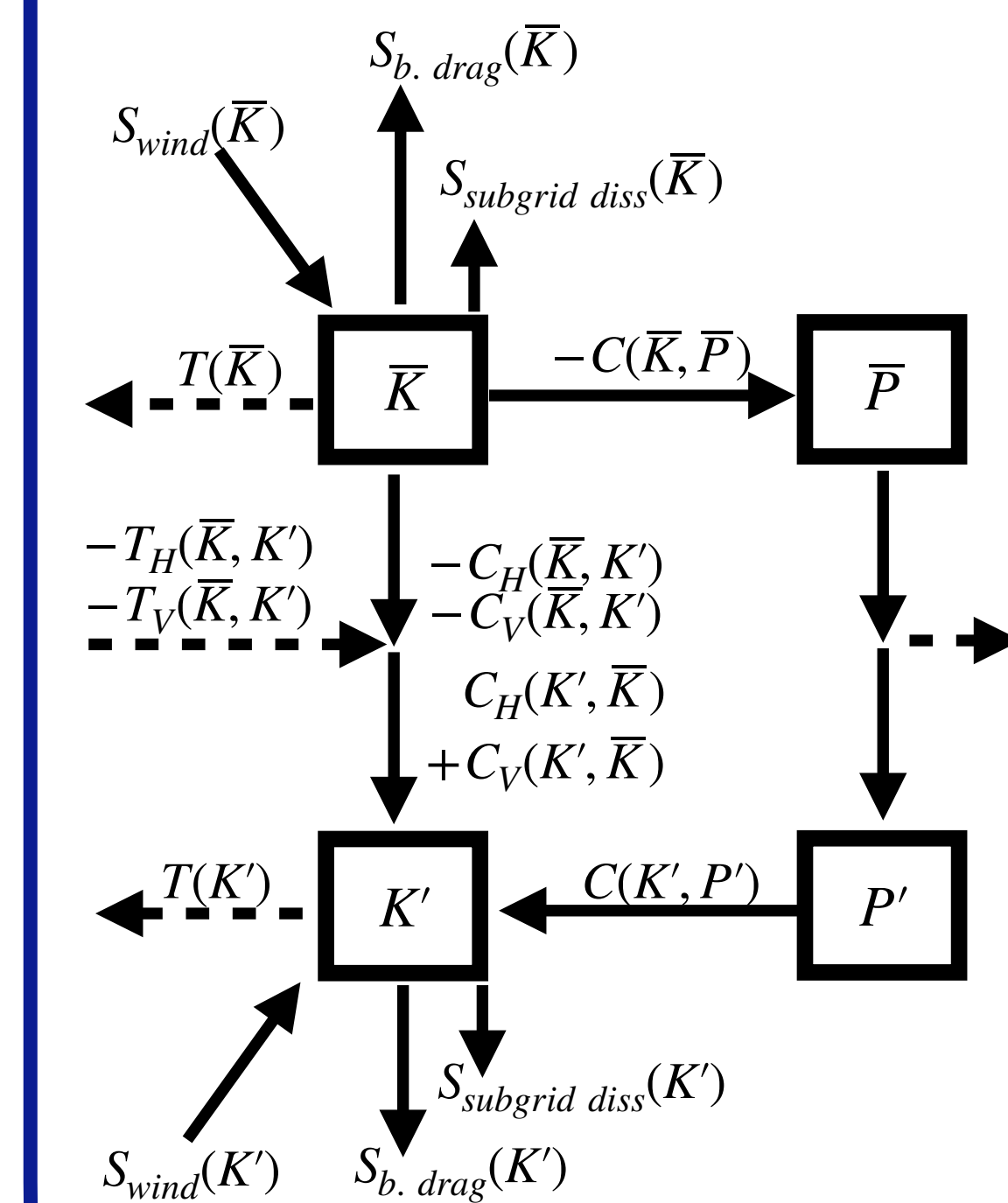
2. Theory

Our energy analysis uses the concept of **energy separation in a time-mean (\bar{K}) and time-varying (K') component:**

$$\bar{K} = \frac{1}{2} \rho_0 (\bar{u}^2 + \bar{v}^2) \text{ and } K' = \frac{1}{2} \rho_0 (u'^2 + v'^2)$$

with (u, v) the horizontal velocity components, ρ_0 the reference density, $(\bar{\cdot})$ a 4-year average, and (\cdot') deviation from this average.

The steady-state balance of \bar{K} and K' reservoirs is analyzed with a regional formulation of the **Lorenz Energy Cycle** (Lorenz, 1955):



Energy rates of change related to:

- $S(\cdot)$: wind stress, bottom drag, subgrid dissipation.
- $T(\cdot)$: non-local effects being spatial redistribution due to pressure work and advection.
- $C(\dots)$: conversion between energy reservoirs.
- $-C(\bar{K}, K')$; $C(K', \bar{K})$: local and non-local eddy-mean energy conversions.
- $C(\bar{K}, \bar{P})$; $C(K', P')$: energy conversions related to buoyancy flux.

Scheme of ocean energy pathways as described by the Lorenz Energy Cycle (Lorenz, 1955). Dashed arrows denote non-local effects. Terms are defined positive in the direction of the arrow. Adapted from Capo et al., (2018).

5. Take home messages

\bar{K} and K' budgets:

- \bar{K} and K' budgets have the same order of magnitude.
- \bar{K} and K' budgets spatially vary, from leading-order energy balances to contributions from time-varying flows.
- The leading-order \bar{K} source in the interior is the wind, and it is the spatial redistribution in other regions.
- Regions of net K' sources (western and eastern boundaries) are hotspots of mean-to-eddy energy conversion.

Impact of tidal forcing on \bar{K} and K' budgets:

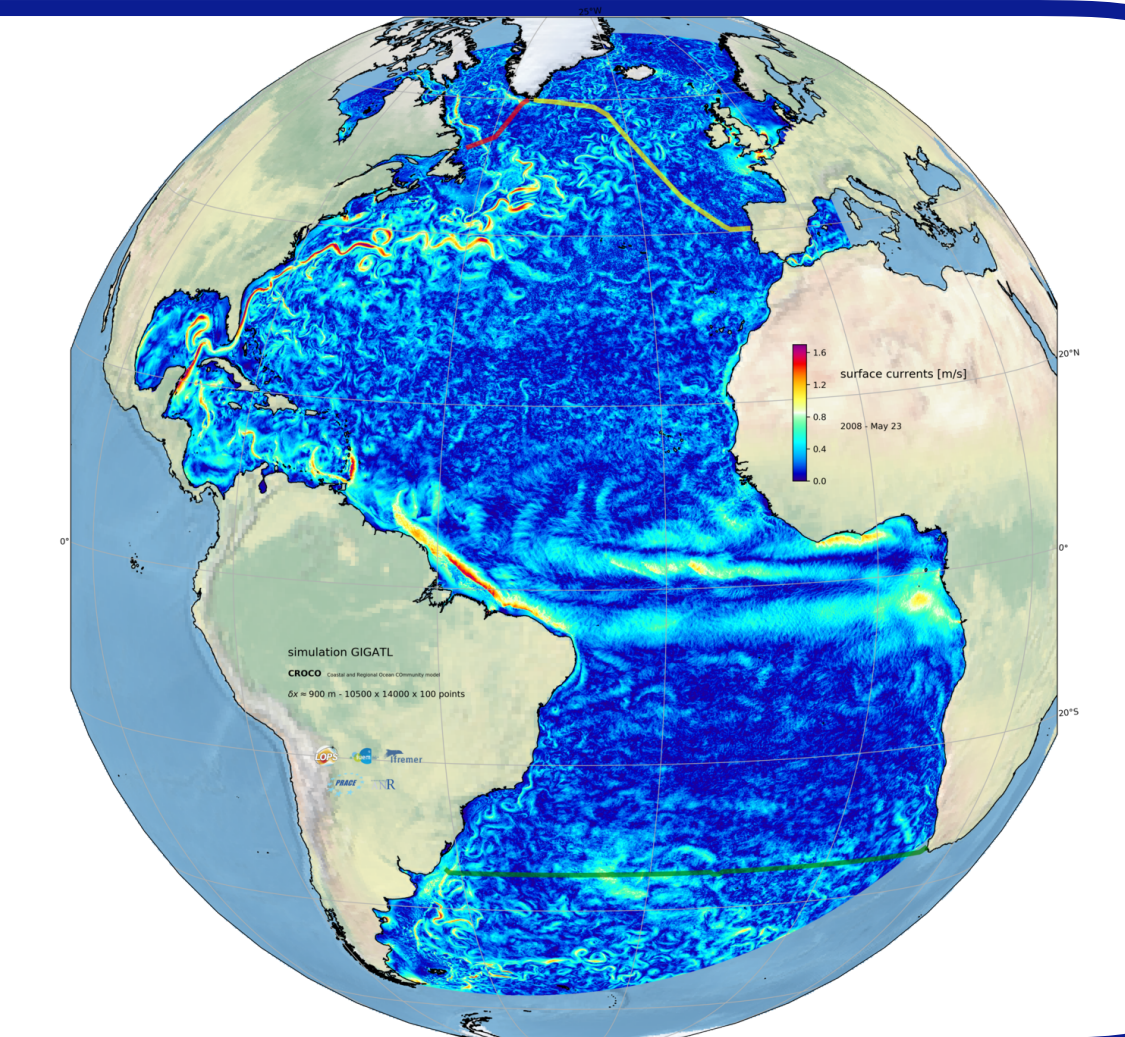
- Tidal forcing adds a K' source, increases mean-to-eddy energy conversion driven by shear processes and energy spatial redistribution.
- The impact of tidal forcing on energy budgets is the largest east of the basin.
- The impact of internal tides on the time-mean circulation should be represented, together with those of mesoscale and submesoscale currents, in ocean models.

Lorenz, E. N. (1955). Available potential energy and the maintenance of the general circulation. *Tellus*, 7(2), 157-167.
Capo, E., Orfila, A., Mason, E., & Ruiz, S. (2019). Energy conversion routes in the Western Mediterranean Sea estimated from eddy-mean flow interactions. *Journal of Physical Oceanography*, 49(1), 247-267.
Ganachaud, A., & Wunsch, C. (2000). Improved estimates of global ocean circulation, heat transport and mixing from hydrographic data. *Nature*, 408(6811), 453-457.

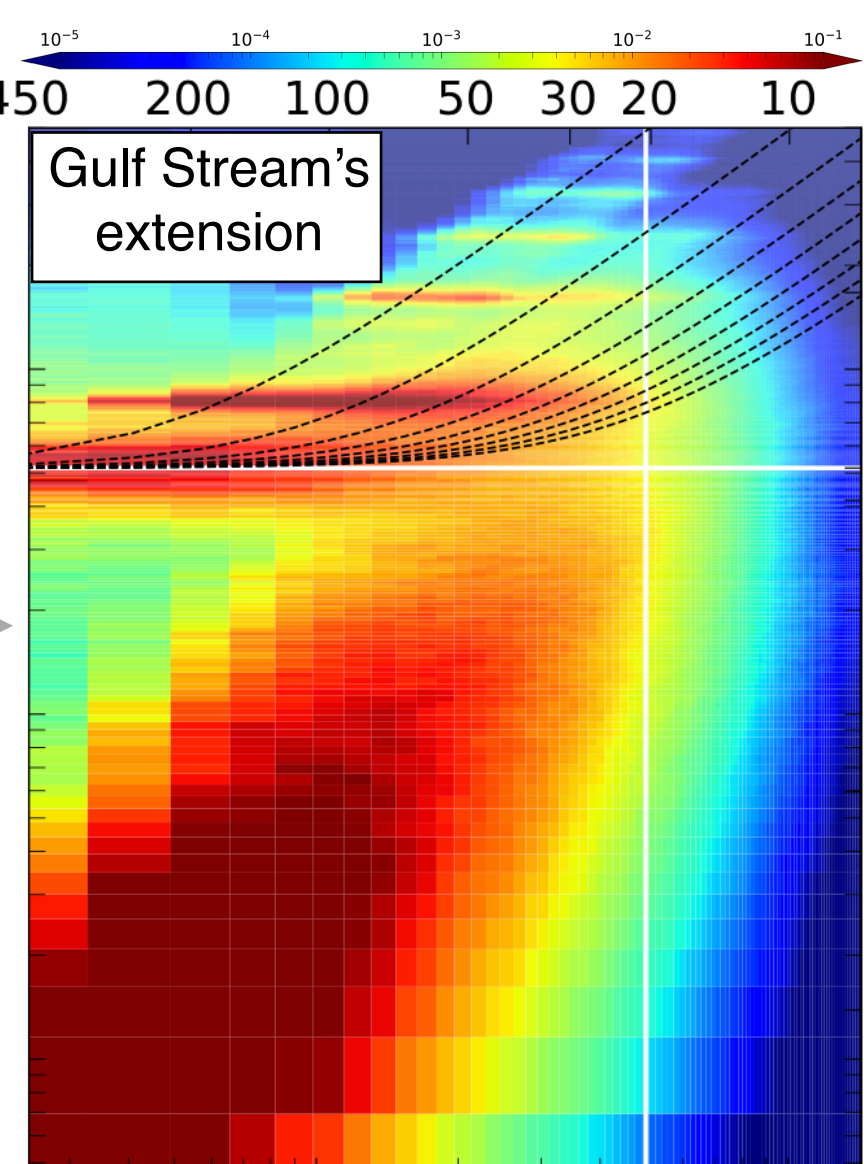
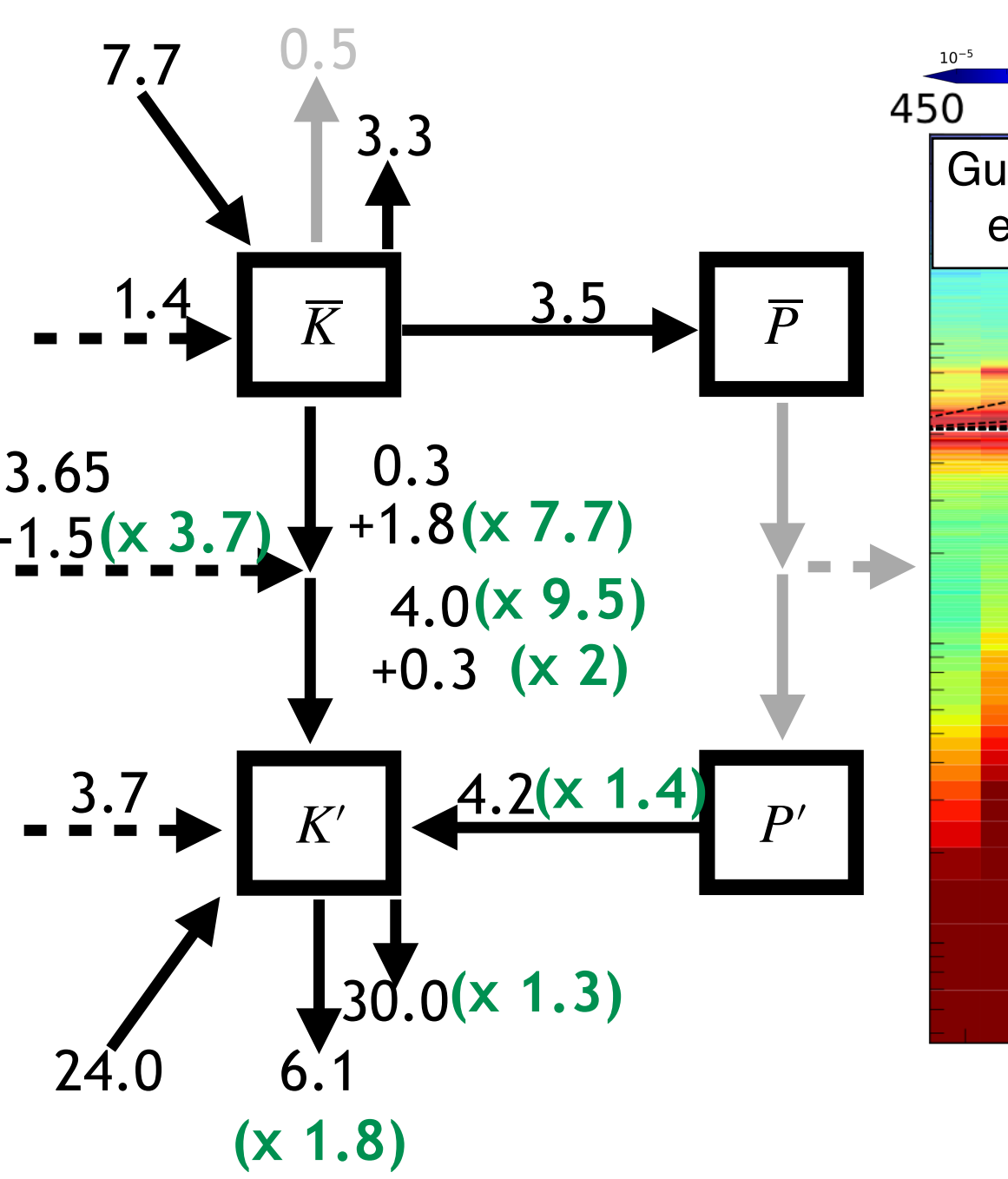
3. Numerical simulation

- State-of-the-art numerical simulations of the Atlantic performed using the CROCO model with realistic forcings (<https://github.com/Mesharou/GIGATL>).
- Two simulations at 3 km resolution including 1-hour atmospheric forcing, one without and with tidal forcing.
- Outputs: hourly 3-dimensional variables (u, v, w, b, η) and 5-day averages of online diagnostics of kinetic energy and momentum budgets and quadratic terms $(uu, vv, uv, uw, vw, bb, ub, vb, wb)$.

Snapshot of surface currents performed as modelled by a dx=1km simulation of the Atlantic (<https://github.com/Mesharou/GIGATL>).

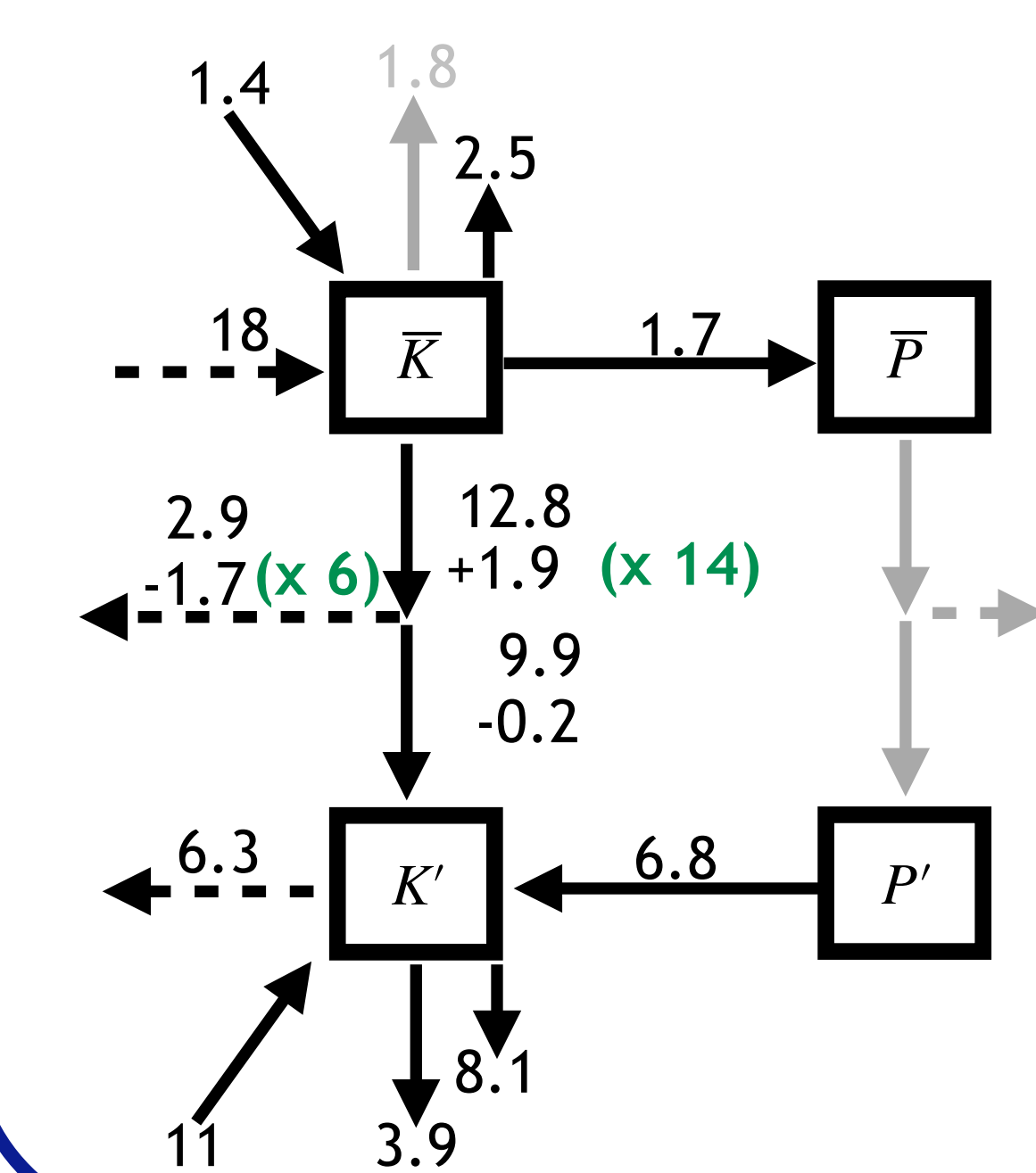


4. \bar{K} (time-mean) and K' (time-varying) budgets for tidal scenario



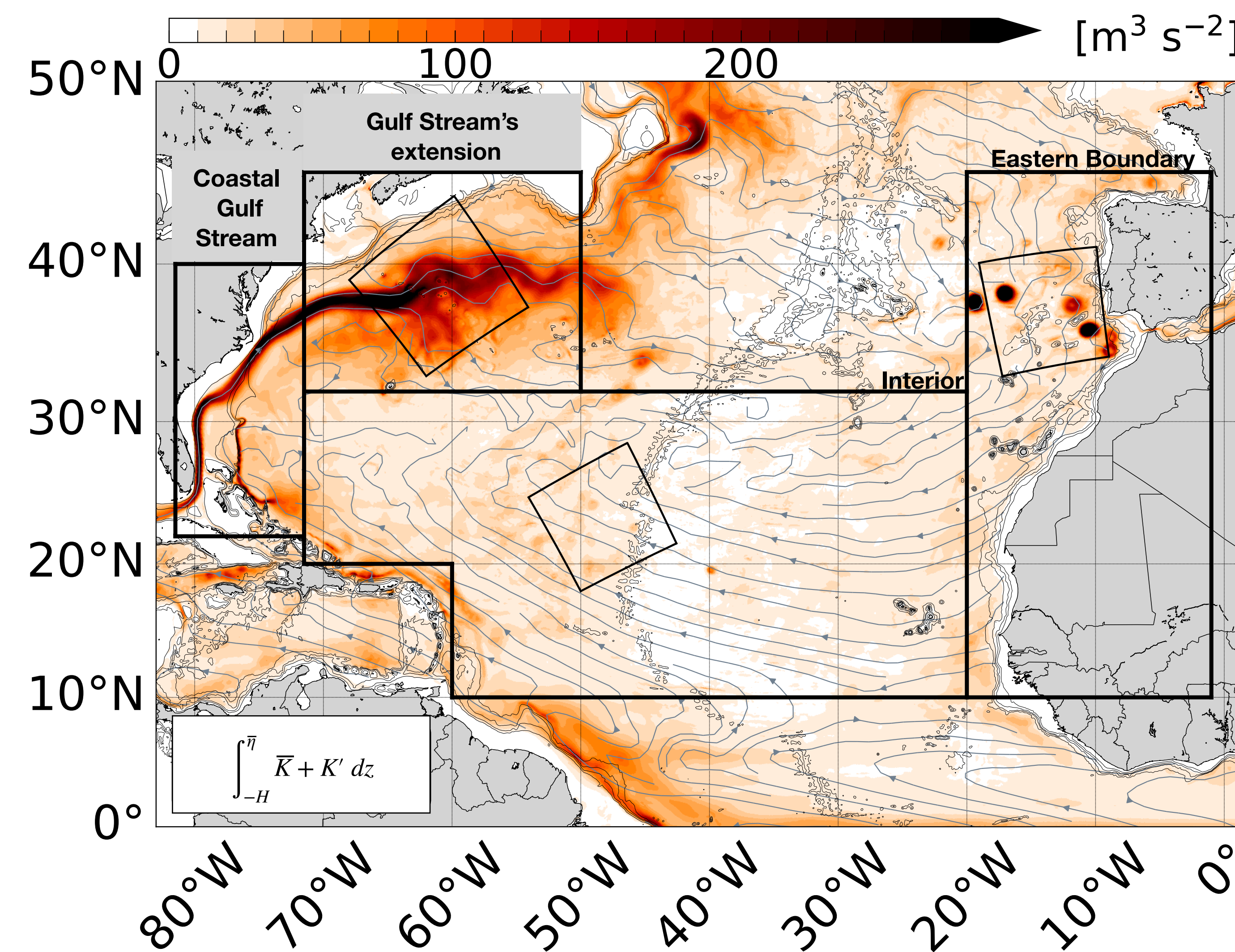
Western Boundary: Gulf Stream's extension

- K' is larger than \bar{K} reservoir by a factor of 3. K' reservoir is dominated by mesoscale, submesoscale currents, and internal waves.
- \bar{K} and K' budgets are sensitive to tidal forcing.
- Net \bar{K} and K' budgets denote local energy sinks.
- \bar{K} is advected within the region, energised by wind, and lost to non-local mean-to-eddy conversion and dissipative processes.
- K' is transported within the region from the coastal Gulf Stream and lost to dissipative processes (although wind and mean-to-eddy conversion are intense K' inputs).



Western Boundary: Coastal Gulf Stream and separation

- \bar{K} and K' reservoirs have comparable magnitudes.
- \bar{K} and K' budgets are insensitive to tidal forcing.
- net \bar{K} budget denotes a local \bar{K} sink, and net K' budget denotes a local K' source.
- \bar{K} is transported within the region (by pressure work) and locally lost to mean-to-eddy conversion and dissipative processes.
- K' is energized by wind, mean-to-eddy conversion, and baroclinic instability and exported to the Gulf Stream's extension.

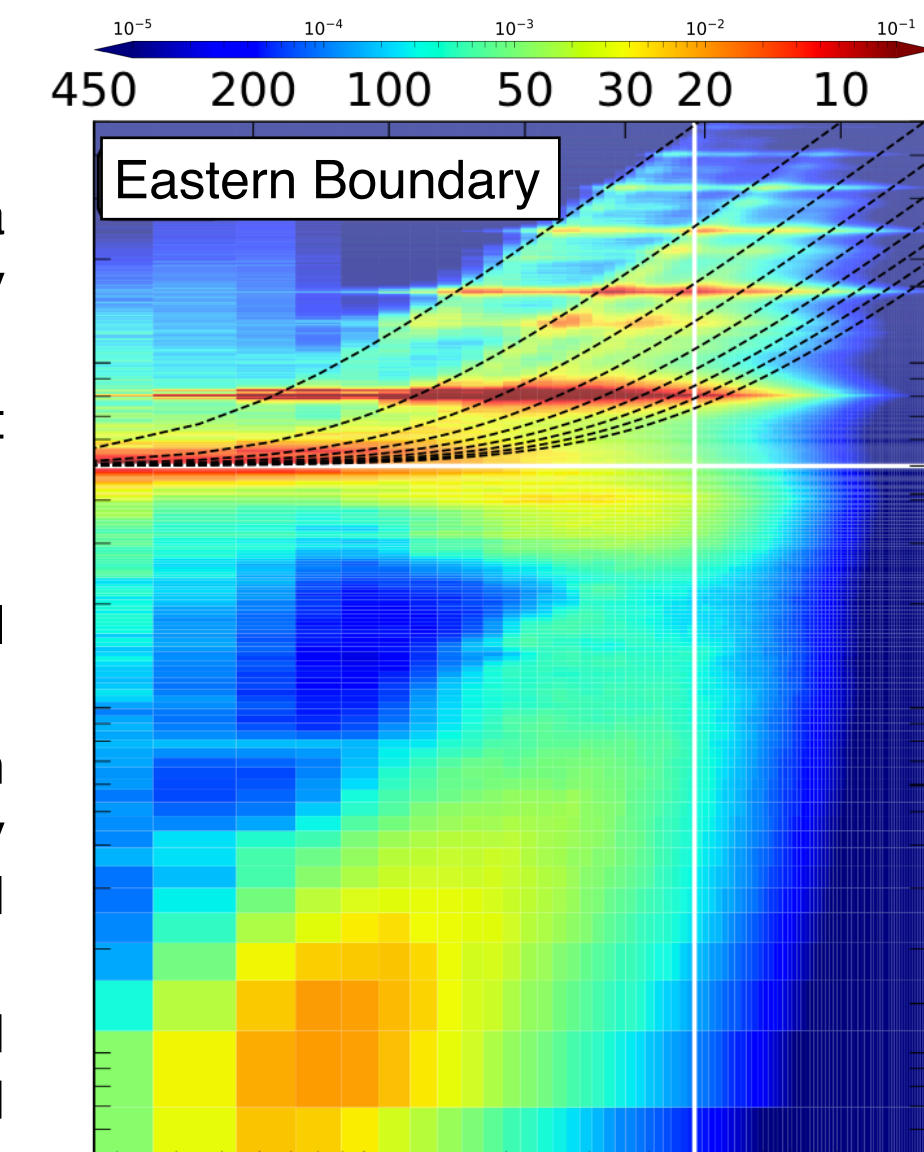


(Top) Vertically-integrated $\bar{K} + K'$ averaged over a 4-year period. The four sub-regions: Coastal Gulf Stream and separation, Gulf stream's extension, Interior and Eastern boundary are shown as squared areas. Streamlines show 4-year averaged surface currents. (Left and right) Frequency-wavenumber K' spectra and scheme of ocean energy pathways for the four sub-regions. In the schemes, amounts have been computed from time-averaged and vertically-integrated terms and then horizontally-averaged [$10^3 \text{ m}^3 \text{ s}^{-2}$].

→: main energy balances
→: weak energy pathways
(x < >): ratio between net contributions in tidal and non-tidal scenarios

Eastern Boundary:

- K' is larger than the \bar{K} reservoir by a factor of 2.5 and is dominated by internal waves.
- \bar{K} and K' budgets are the most sensitive to tidal forcing.
- net \bar{K} and K' budgets denote local energy sinks.
- \bar{K} is transported within the region and lost to non-local mean-to-eddy conversion driven by horizontal and vertical shear processes.
- K' is advected within the region and lost to dissipative processes and bottom drag.



Subtropical gyre's interior

- K' is larger than the \bar{K} reservoir by a factor of 6 and is dominated by submesoscale currents and internal waves.
- \bar{K} and K' budgets are insensitive to tidal forcing.
- \bar{K} budget follows a Sverdrup-like balance: only region with a net \bar{K} export provided by the wind.
- K' reservoir is mainly energized by wind and tides.

