Figured Magic Squares of Order 28 Using Bordered Magic Rectangles: A Systematic Procedure

Inder J. Taneja¹

Abstract

Recently, author constructed even order magic squares from orders 6 to 20 with different styles and models, for examples the order 20 is with 1616 magic squares, order 18 with 810 magic squares, etc. These can be seen at [31, 32, 33, 33, 34, 35, 36, 37]. The aim is to proceed for the further orders of magic squares. In this work there are few examples of magic squares given as figures of order 28. A systematic procedure to construct these magic squares is given. It is based on the magic squares of orders 4, 6, 8 etc. at corners and small blocks of **bordered magic rectangles** forming external borders. Then the internal borders are filled with previous known magic squares. The presentations is in figures instead of numbers. The readers can find replies in numbers from references given above. For the orders multiples of 4, we can always write magic squares with equal sums blocks of magic squares of order 4. This procedure is very helpful for the orders of type 2p, where **p** is a prime number, for examples, 14, 22, 26, 34, 38, etc. For the orders like 18, 30, etc. we can make good external blocks with order 4, and for orders like 16, 20, 28, 32, etc. we can make good external borders of order 6, and so on.

¹Formerly, Professor of Mathematics, Federal University of Santa Catarina, Florianópolis, SC, Brazil (1978-2012). Also worked at Delhi University, India (1976-1978).

E-mail: ijtaneja@gmail.com; Web-sites: http://inderjtaneja.com; http://numbers-magic.com; Twitter: @IJTANEJA; Instagram: @crazynumbers.

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1 Introduction

The magic sums of order *n* of consecutive numbers from 1 to n^2 is given by

$$S_{n \times n} := \frac{n \times (1 + n^2)}{2}, n \ge 3.$$
 (1)

Recently, the author [31, 32, 33, 34, 35, 36, 37] constructed magic squares of even orders from 8 to 20 using **bordered magic rectangles**. This construction is based on two aspects:

- (i) Using magic rectangles or bordered magic rectangles.
- (ii) Using algebraic formula like $(\mathbf{a} + \mathbf{b})^2$, $\mathbf{a} \neq \mathbf{b}$.

For the above magic squares no construction procedure is explained. The aim is to proceed further orders of magic squares. In this work, a systematic procedure to construct these magic squares is given. It is based on the magic squares and bordered magic rectangles (BMR) of orders 4, 6, 8 etc forming external borders. Then the internal borders are filled with previous known magic squares. For the orders multiples of 4, we can always write magic squares with equal sums blocks of magic squares of order 4. This procedure is very helpful for the orders of type **2p**, where **p** is a prime number, for examples, 14, 22, 26, 34, 38, etc. For the orders like 18, 30, etc.,we can make good external blocks with order 4, and for orders like 16, 20, 28, 32, etc. we can make good external borders of order 6, and so on. There is no explainations for the orders 6, 8, 10 and 12. The real construction starts from the order 14.

The whole the work is done manually, without use of any programming language, except for the constructions of small blocks of **bordered magic rectangles**. This construction is based on the software due to H. While. Later, these BRMs are readopted according to distribution of each magic square. The distribution of **magic squares** or **bordered magic rectangles** is based on **halfsequential** numbers. By **half-sequential** numbers we understand that the total numbers in each case are divided in two equal parts. The first part is one sequence and the second part is another sequence. Due to **half-sequential** numbers, it is not possible to construct all orders **bordered magic rectangles**. In Appendix 3, there are tables showing the existence of these **bordered magic rectangles** for **half-sequential**. For simplicity, we shall write **BMR** as **bordered magic rectangle**. This work is for order 28. The previous works can be seen at [38, 39, 40, 41, 42]. The further work on order 30 can be seen at [44].

Remark 1. The **bordered magic squares** and **bordered magic rectangles** are with the property that if we remove external borders in each case, still we are left with **bordered magic squares** and **bordered magic rectangles** respectively with sequential number entries. The whole work is in figures instead of numbers. In the same magic square the **small equal figures** represents equal sums **magic squares** and/or equal sums **bordered magic rectangles**. The whole work is done manually

2 Magic Squares of Order 28

This section brings in figures (without numbers) magic squares of order 28. In some cases, the idea of constructions are explained. It is based on **cornered magic squares**.

2.1 Block-Wise and Bordered Square of Order 28

Below are magic squares of order 28 already known in the literature. For more details refer author's work [22, 24].

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2.2 Magic Squares of Order 28 With BMRs

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2.3 Cornered Magic Squares of Order 4

Let's consider an external border, where there are 4 magic squares of order 4 at the corners. Let's make an external border by putting 2 BMR of order 4×10 in each row and column. In the middle we are left with block of order 20. Writing this middle blocks with different types of magic squares of order 20, we get magic squares of order 28. See below few examples:

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2.4 Closed Border of Order 4

The external border is made with 4 BMRs of order 4×14 and 4 BMRs of order 4×10 . We are left with internal block of order 20. Writing this middle blocks with different types of magic squares of order 20, we get magic squares of order 28. See below few examples:

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The Figures 58, 59, 60 and 61 can also be considered as blocks of order 10.

2.5 Cornered Magic Squares of Order 6

Let's consider an external border, where there are 4 magic squares of order 6 and 4 BMRs of order 6×16 . This gives us an external border with cornered magic squares of order 6. In the middle we are left with block of order 16. Writing this middle blocks with different types of magic squares of order 16, we get magic squares of order 28. See below few examples:

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2.6 Closed Border of Order 6

Let's write a closed external border formed by 2 equal sums BMR's of order 6×28 and 2 of order 6×16 . In the middle we are left with block of order 16. Writing this middle blocks with different types of magic squares of order 16, we get magic squares of order 28. See below few examples:

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2.7 Cornered Magic Squares of Order 8

Let's consider an external border, where there are 4 magic squares of order 8 at the corners. Let's make an external border by putting 2 BMRs of order 6×8 in each row and column. In the middle we are left with blocks of order 12. Writing this middle blocks with different types of magic squares of order 12, we get magic squares of order 28. See below few examples:

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2.8 Closed Border of Order 8

Let's consider an external border, where there are 8 BMRs of order 8×10 . Putting them in rows and columns, we get a closed border of order 8. In the middle we are left with blocks of order 12. Writing this middle blocks with different types of magic squares of order 12, we get magic squares of order 28. See below few examples:

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2.9 Cornered Magic Squares of Order 10

Let's consider an external border, where there are 4 magic squares of order 10 at the corners. Let's make an external border by putting BMRs of order 8×10 in each row and column. In the middle we are left with blocks of order 8. Writing this middle blocks with different types of magic squares of order 8, we get magic squares of order 28. See below few examples:

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2.10 Cornered Magic Squares of Order 12

Let's consider an external border, where there are 4 magic squares of order 12 at the corners. Let's make an external border by putting 2 BMRs of order 4×6 in each row and column. In the middle we are left with blocks of order 4. Writing magic squares of order 12 in different ways, we get magic squares of order 28. See below few examples:

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2.11 Closed Border of Order 12

Let's consider an external border with 8 BMRs of order 6×16 . In the middle we are left with blocks of order 4. It gives us a magic square of order 28. See below a single example:

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2.12 Blocks of Order 14

Let's consider 4 equal sums blocks of order 14. It gives magic squares of order 28. See below few examples:

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2.13 Consecutive BMRs of Orders 12×14 and 12×14

Let's consider consecutive BMRs of orders 12×14 and 12×14 . It gives us a following magic square of order 28:

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3 Appendix

Below are tables giving the existence of **bordered magic rectangles** for **half-sequential** numbers.

Order of Magic Square	Bordered Magic Rectangles
6	4 imes 6
8	6×8
10	4 imes 10,8 imes 10
12	6 imes 12, 10 imes 12
14	4 imes 14, $8 imes 14$, $12 imes 14$
16	6 imes 16, 10 imes 16, 14 imes 16
18	4 imes18,8 imes18,12 imes18
20	$6 \times 20, 10 \times 20, 14 \times 20, 18 \times 20$
22	$4 \times 22, 8 \times 22, 12 \times 22,$
	16 imes22, 20 $ imes$ 22
24	6 imes 24, $10 imes 24$, $14 imes 24$,
	18 imes 24, $22 imes 24$
26	4 imes26, $8 imes$ 26, $12 imes$ 26,
	16 imes 26, 20 imes 26, 24 imes 26
28	6 imes 28, 10 imes 28, 14 imes 28,
	18 imes28, 22 imes28, 26 imes28
30	$4 \times 30, 8 \times 30, 12 \times 30, 16 \times 30,$
	20 imes 30, 24 imes 30, 28 imes 30
32	$6 \times 32, 10 \times 32, 14 \times 32, 18 \times 32,$
	$22 \times 32, 26 \times 32, 30 \times 32$
34	4×34 , 8×34 , 12×34 , 16×34 ,
	$20 \times 34, 24 \times 34, 28 \times 34, 32 \times 34$

Order of Magic Square	Bordered Magic Rectangles
36	6 imes 36, 10 imes 36, 14 imes 36, 18 imes 36,
	$22 \times 36, 26 \times 36, 30 \times 36, 34 \times 36$
38	4 imes 38, $8 imes 38$, $12 imes 38$, $16 imes 38$, $20 imes 38$,
	24 imes38, $28 imes38$, $32 imes38$, $36 imes38$
40	6 imes 40, 10 imes 40, 14 imes 40, 18 imes 40, 22 imes 40,
	26 imes 40, 30 imes 40, 34 imes 40, 38 imes 40
42	4 imes 42, $8 imes 42$, $12 imes 42$, $16 imes 42$, $20 imes 42$,
	24 imes 42, $28 imes 42$, $32 imes 42$, $36 imes 42$, $40 imes 42$
44	$6 \times 44, 10 \times 44, 14 \times 44, 18 \times 44, 22 \times 44, 26 \times 44,$
	30 imes 44, $34 imes 44$, $38 imes 44$, $42 imes 44$
46	$4 \times 46, 8 \times 46, 12 \times 46, 16 \times 46, 20 \times 46, 24 \times 46,$
	28 imes 46, $32 imes 46$, $36 imes 46$, $40 imes 46$, $44 imes 46$
48	$6 \times 48, 10 \times 48, 14 \times 48, 18 \times 48, 22 \times 48, 26 \times 48,$
	30 imes 48, $34 imes 48$, $38 imes 48$, $42 imes 48$, $46 imes 48$
50	$4 \times 50, 8 \times 50, 12 \times 50, 16 \times 50, 20 \times 50, 24 \times 50,$
	$28 \times 50, 32 \times 50, 36 \times 50, 40 \times 50, 44 \times 50, 48 \times 50$

4 Author's Contribution to Magic Squares and Recreation Numbers

For author's contribution to **magic squares** and **recreation numbers** please see the links below:

- Inder J. Taneja, Magic Squares, https://inderjtaneja.com/2019/06/27/publications-magic-squares/
- Inder J. Taneja, Recreation of Numbers, *https://inderjtaneja.com/2019/06/27/publications-recreation-of-numbers/*

Acknowledgement

The **bordered magic rectangles** are constructed based on the software produced by H. White [1]. The author is thankful to H. White for their valuable help.

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