

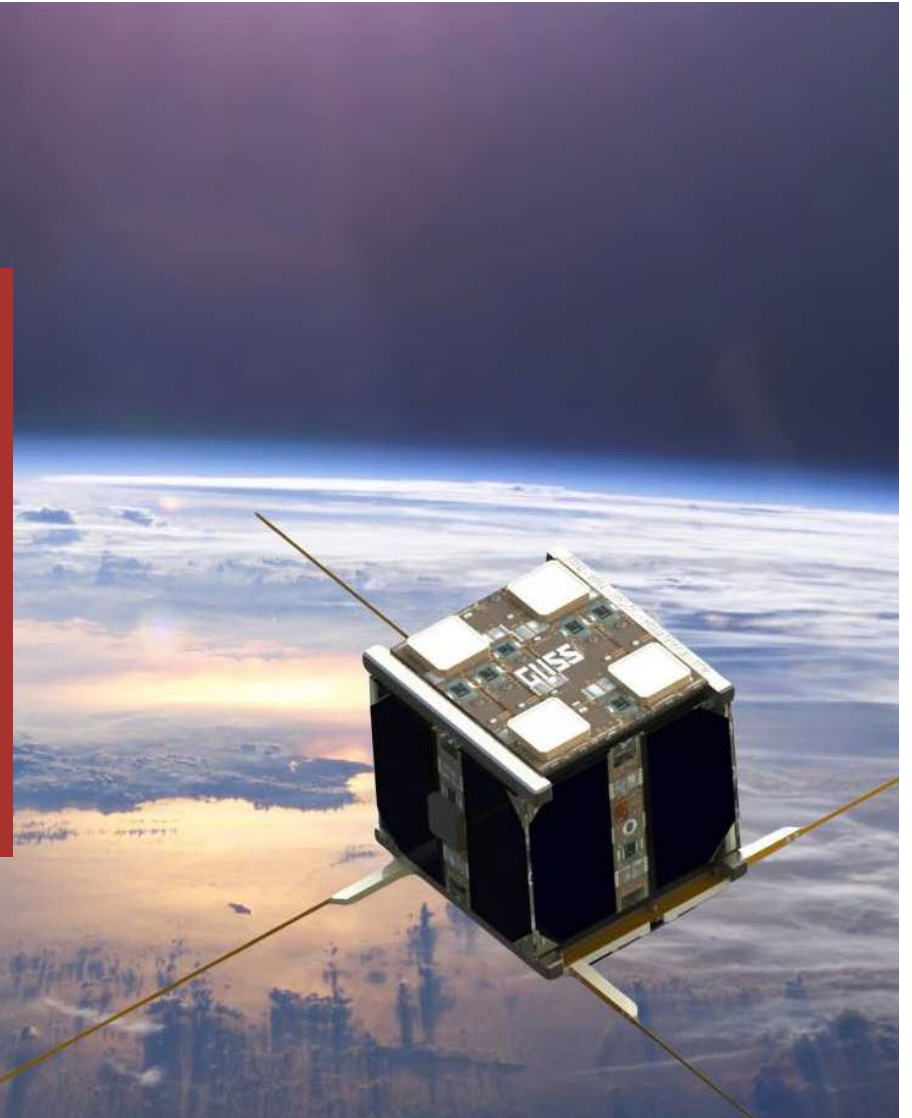
Nanosatellites: The next big chapter in atmospheric tomography

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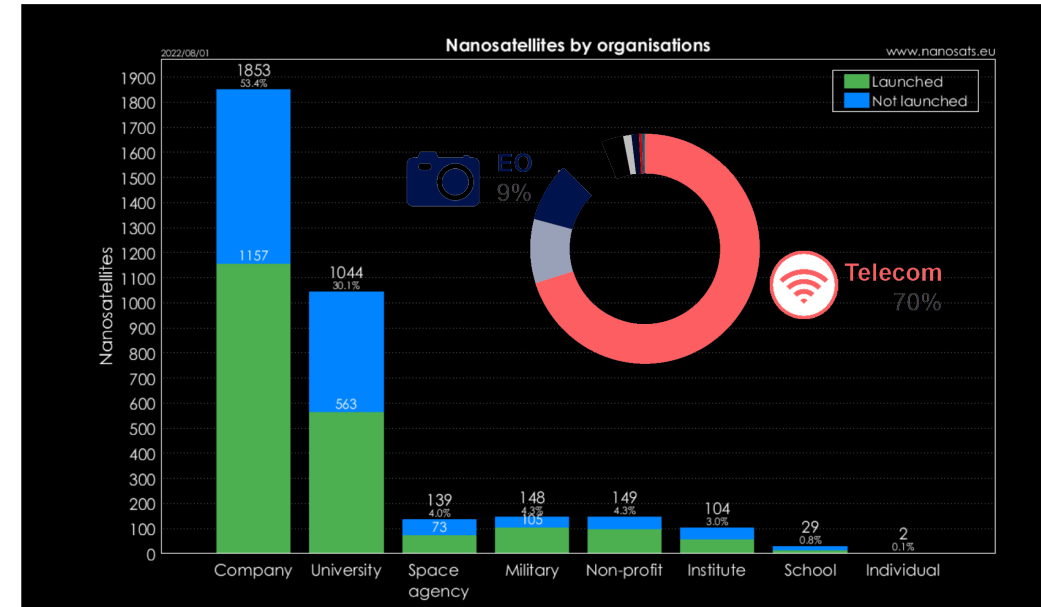
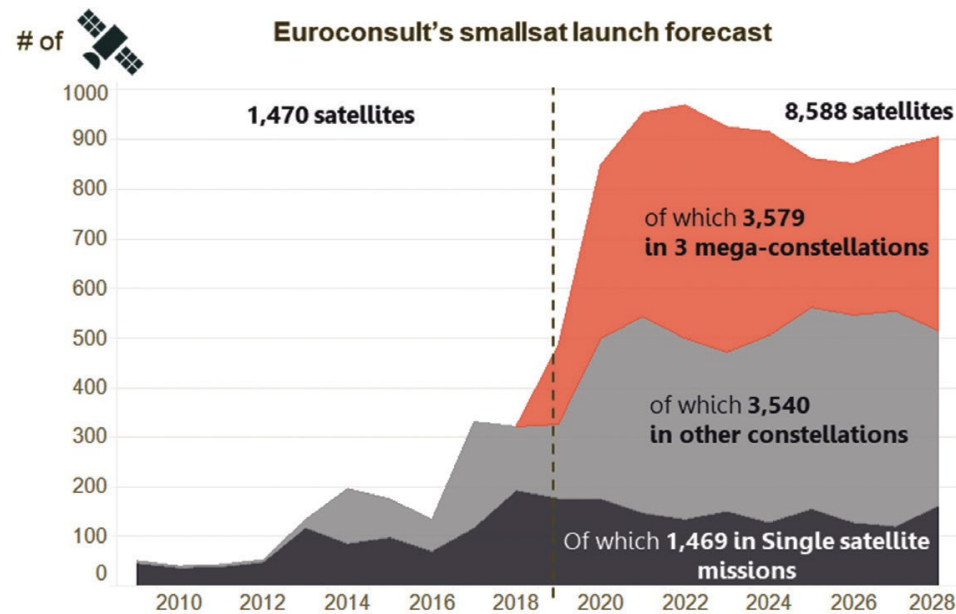


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2. Multi-signal combination
 - a) The concept of GNSS tomography
 - b) Results from a case study
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3. Summary

Concept of a dense nanosatellite formation

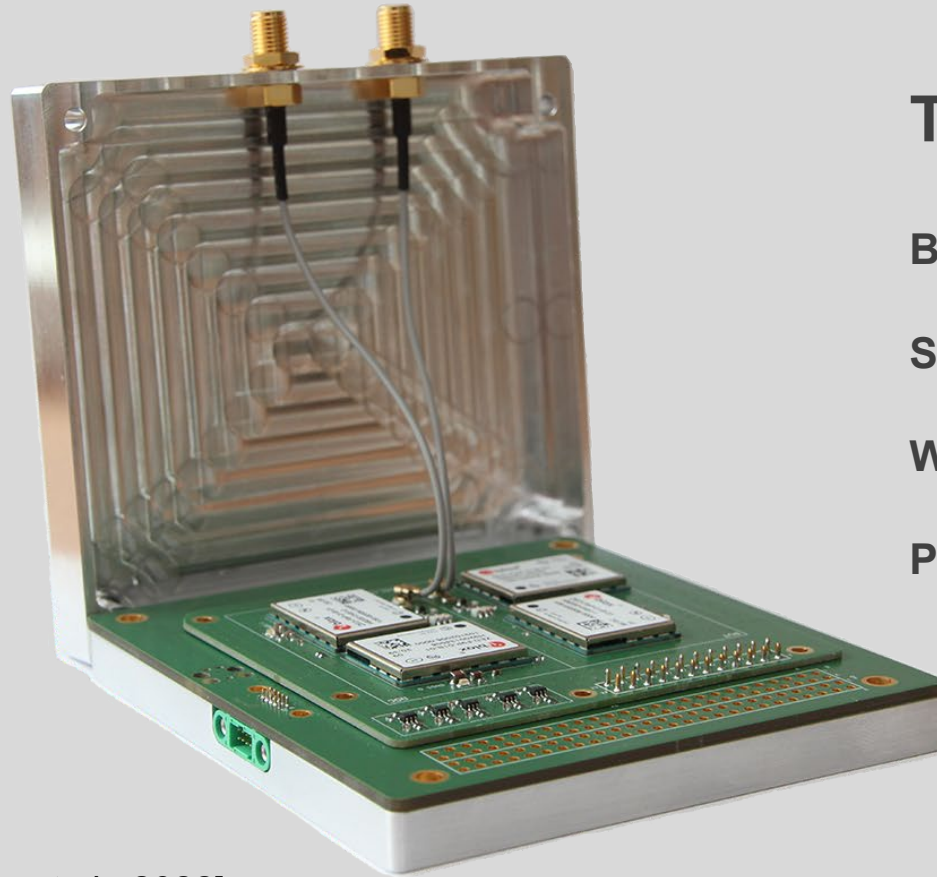
SmallSat Launches



- In the next decade, 4-5 times more SmallSat launches are expected
- Average costs per nanosatellite launch: <500k €

Concept of a dense nanosatellite formation

In-house developed GNSS payload board for nanosatellite missions



The GNSS payload board

Based on the u-blox ZED-F9P multi-GNSS chip

Size: 96 x 90 x 11 mm

Weight: 65 g

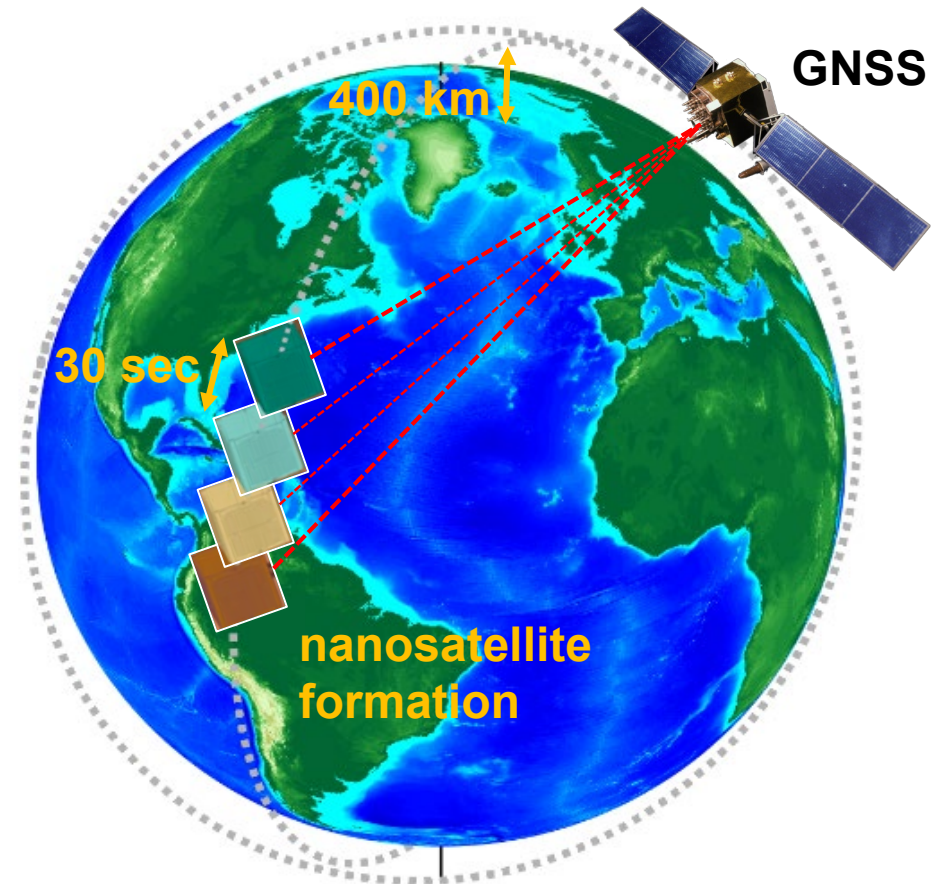
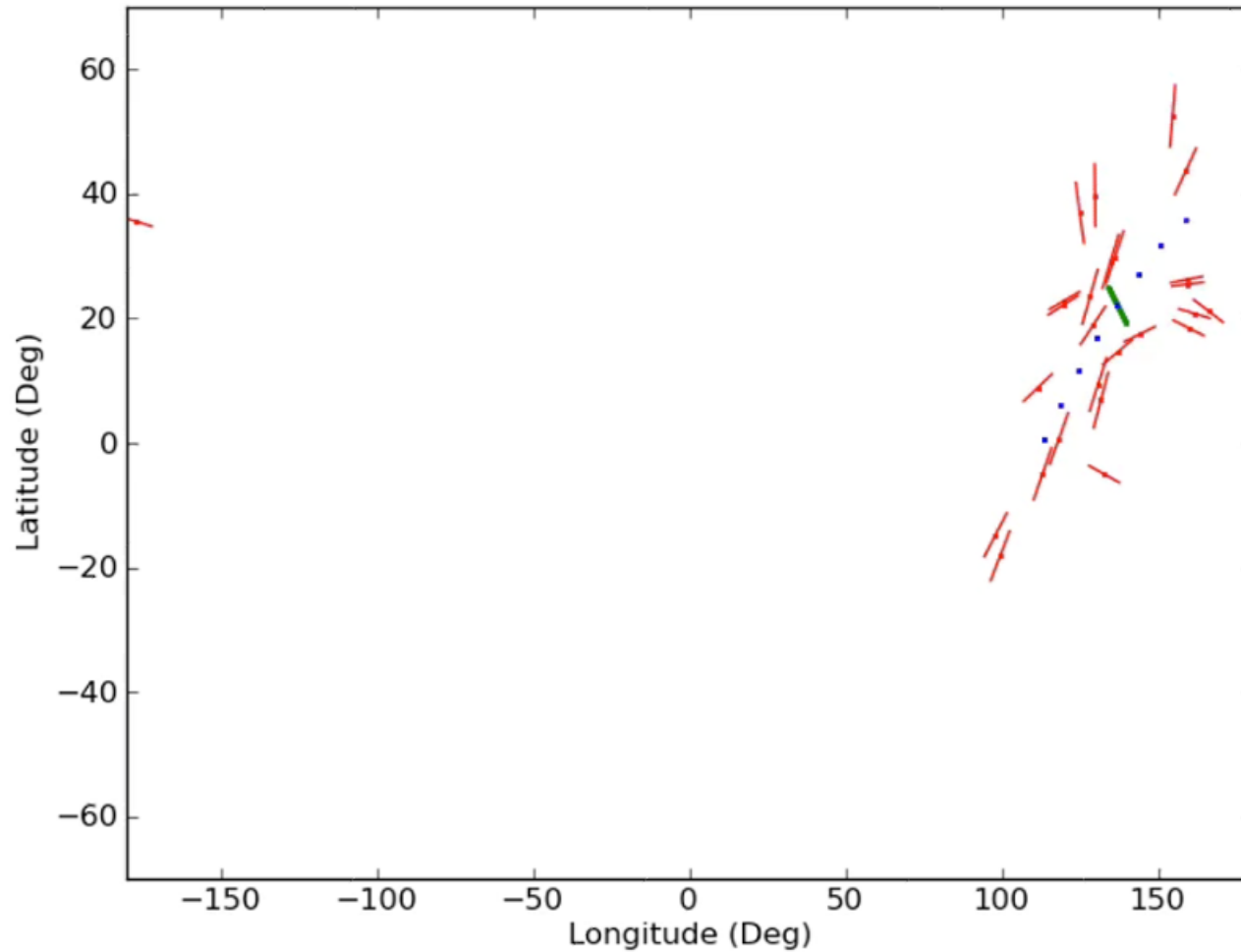
Power consumption: \emptyset 0.5 W

Applications: Precise orbit determination,
RO & Space Weather monitoring

[Moeller et al., 2022]

Concept of a dense nanosatellite formation

Nanosatellite formation for highly detailed atmospheric structure monitoring

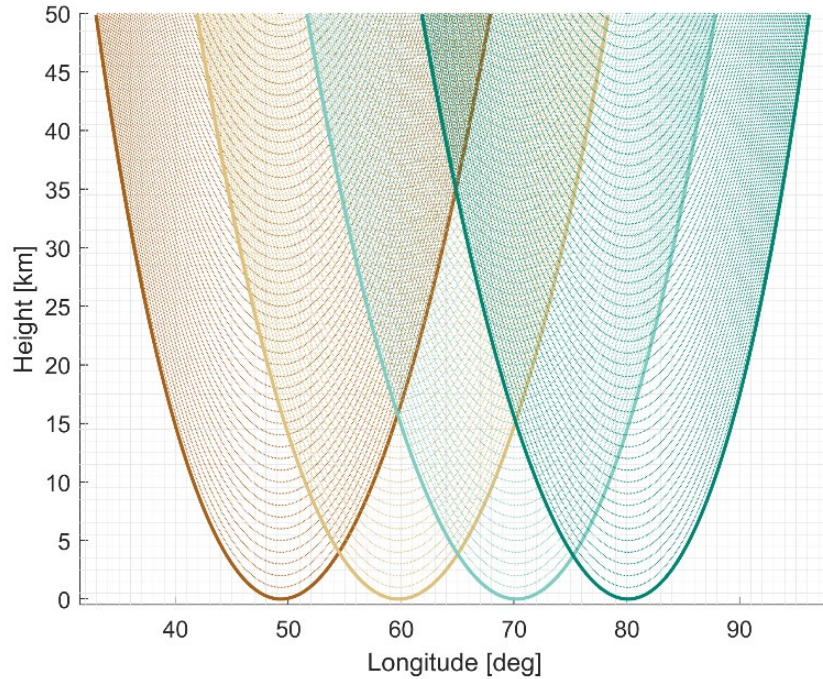


[Turk F. J. et al., 2019]

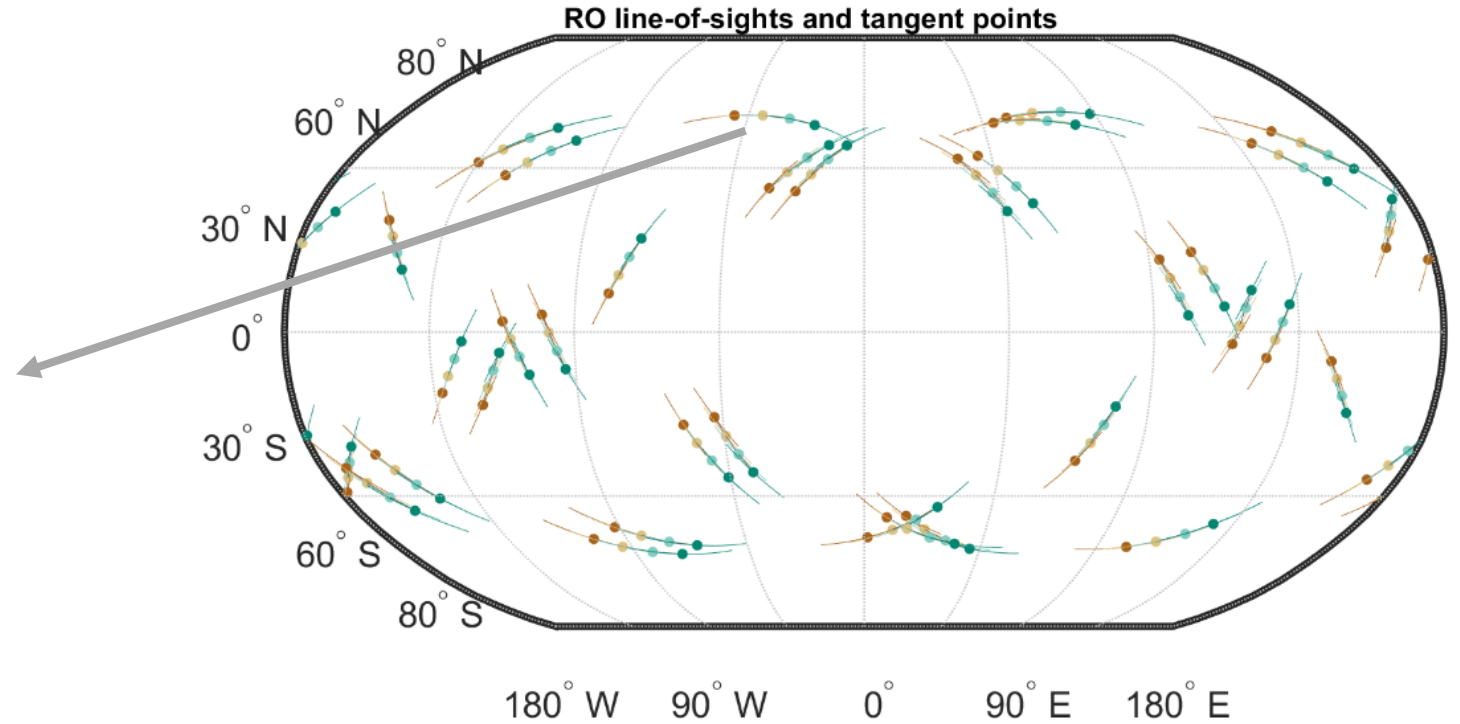
Concept of a dense nanosatellite formation

Cross-link occultation geometry between four nanosatellites and one GNSS satellite

Ray-path geometry through the lower 50 km of the atmosphere



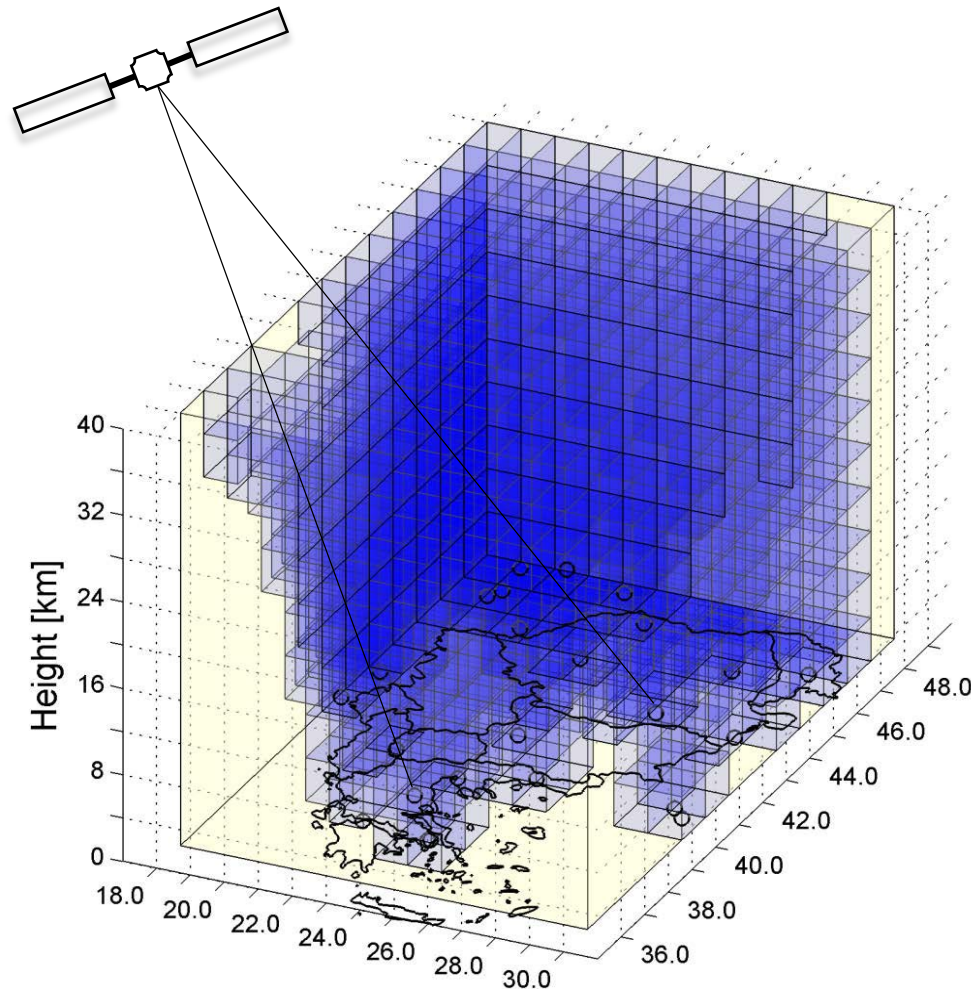
Time between RO observations: <1 min



Observation geometry suited for **tomographic processing**.

Multi-signal combination

The concept of GNSS tomography (exemplary for water vapor density ρ_w)



Basic function of GNSS tomography

$$N = \boxed{A^{-1}} \cdot AEP \ggg \rho_w = \boxed{A^{-1}} \cdot PIWV$$

- Setup tomography model (grid/voxel-based or node-based)
- Ray-trace signal paths and determine components of design matrix A

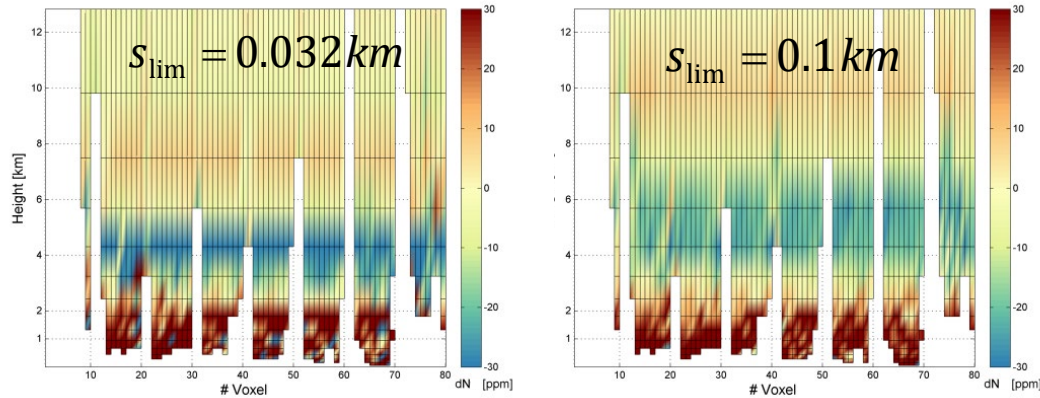
Solution of inverse problem

- Pseudo inverse A^+ $\ggg A = U \cdot \boxed{S} \cdot V^T$
- Truncated singular value decomposition (TSVD)

Multi-signal combination

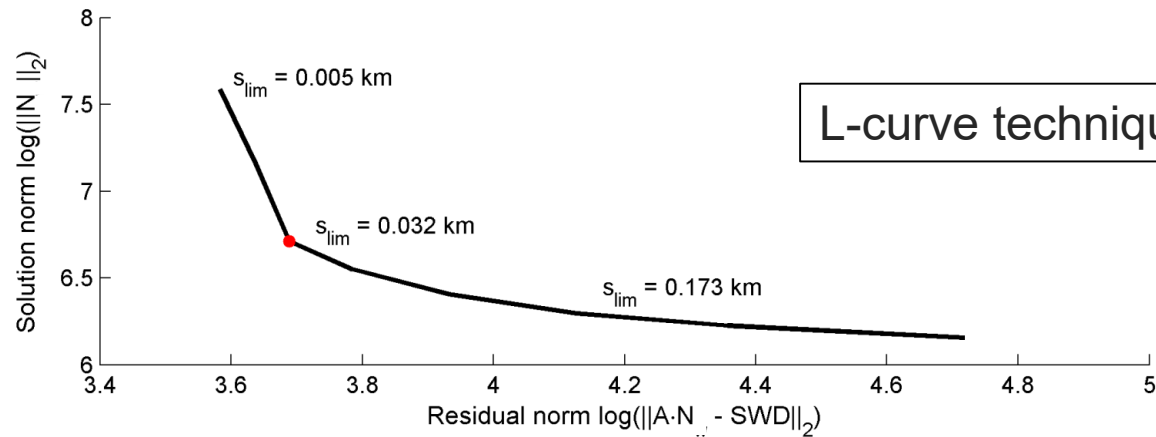
The concept of GNSS tomography (exemplary for water vapor density)

- Impact of the singular value threshold (s_{lim}) on the tomography solution



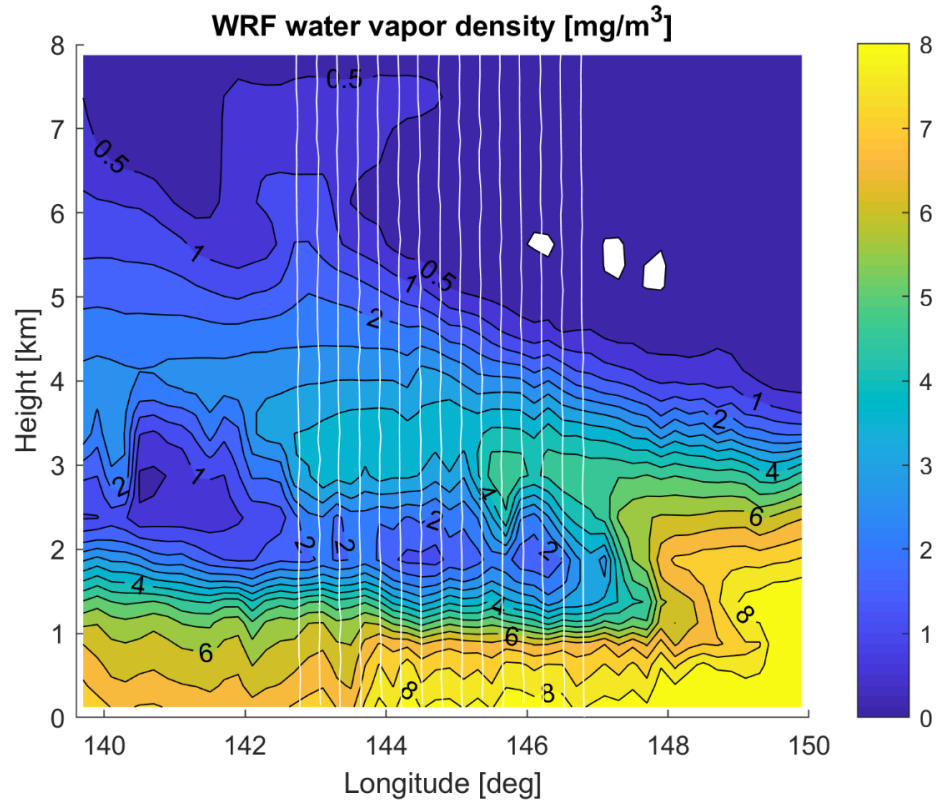
Differences in N between reference solution and synthetic tomography solution

- Goal: Find trade-off between ill-conditioning and over-smoothing

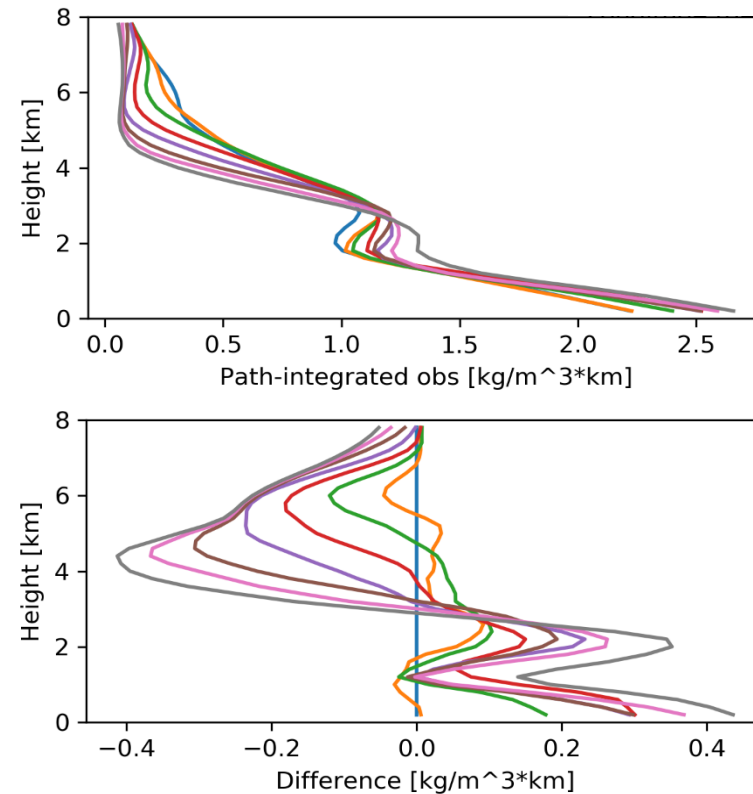


Multi-signal combination

Case study: Water vapor inversion layer between 2-4 km altitude



WRF (reference) water vapor density (ρ_w) field + tangent points of the straight-line RO ray paths through the atmosphere (white lines) - assuming **15 nanosatellite** in one orbit separated by 30 s



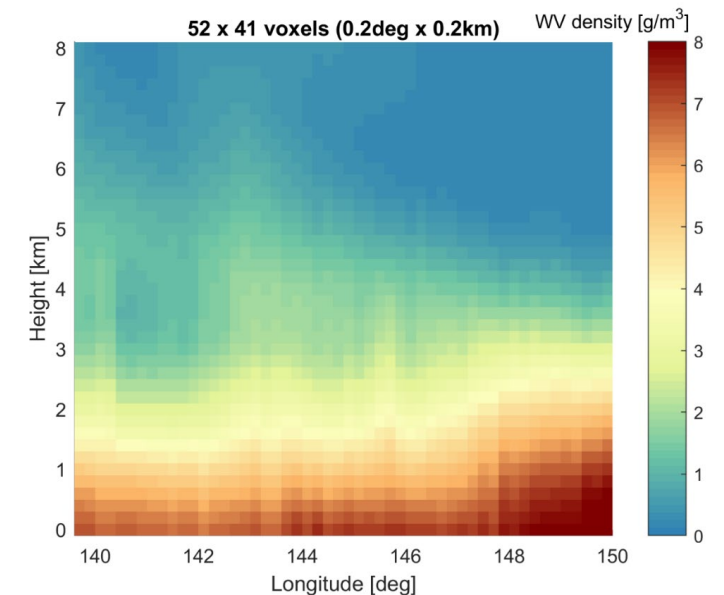
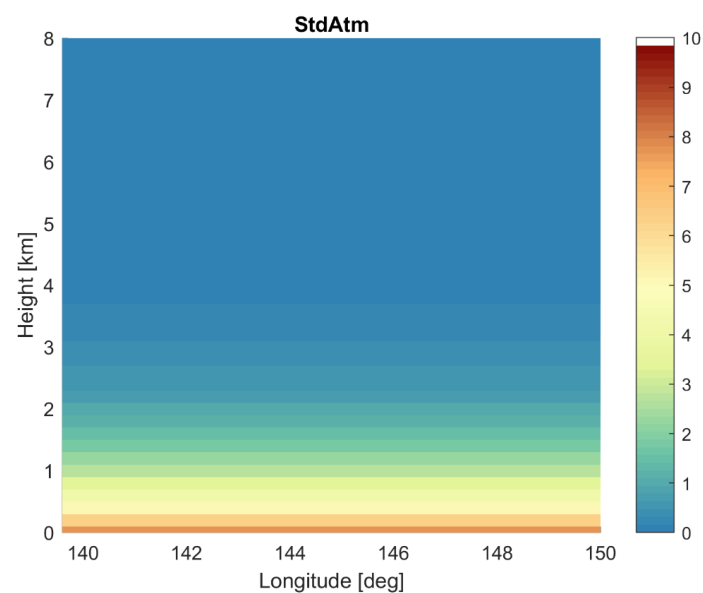
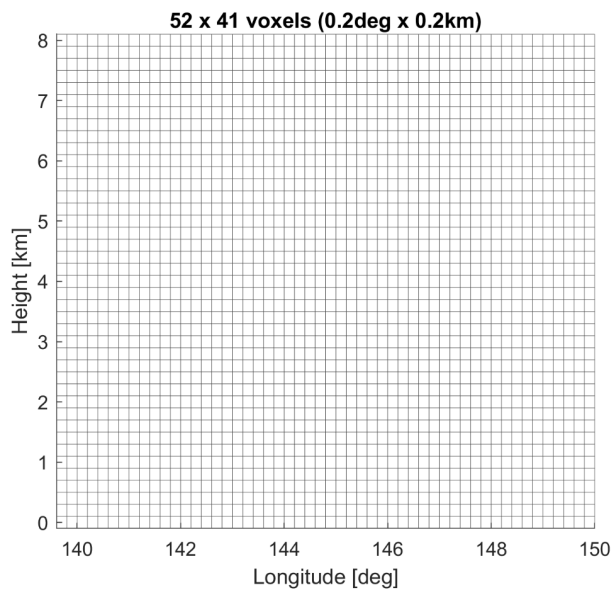
Ray-traced **path-integrated water vapour (PIWV)** (visualized for 8 (every 2nd) nanosatellites)

Multi-signal combination

Tomography solution – A priori field

	#Voxels	First guess	#CubeSats	σ_{RO}	σ_{apr}
Test1a	52 x 41	No	8 (0s,60s,...,420s)	1	—
Test1b	52 x 41	StdAtm	8 (0s,60s,...,420s)	$0.01g/m^3 km$	$0.2wvd$
Test1c	52 x 41	SmoothWRF	8 (0s,60s,...,420s)	$0.01g/m^3 km$	$0.2wvd$

How sensitive is the tomography solution on the quality of the a priori field?

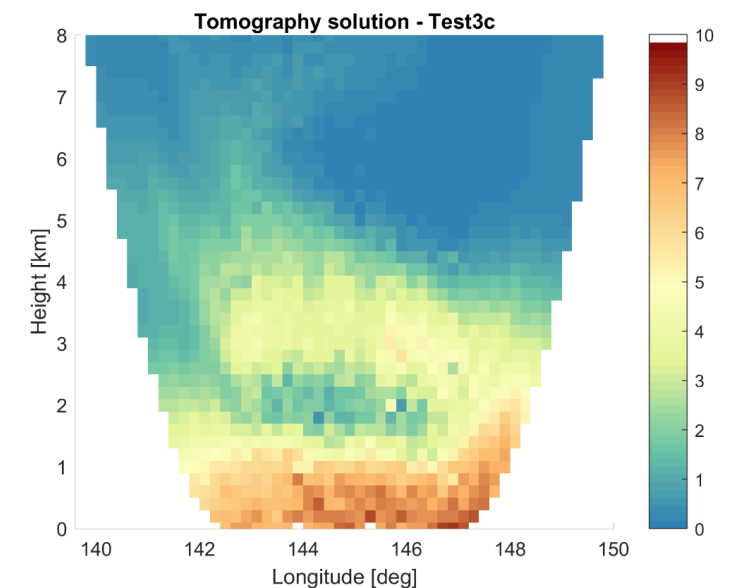
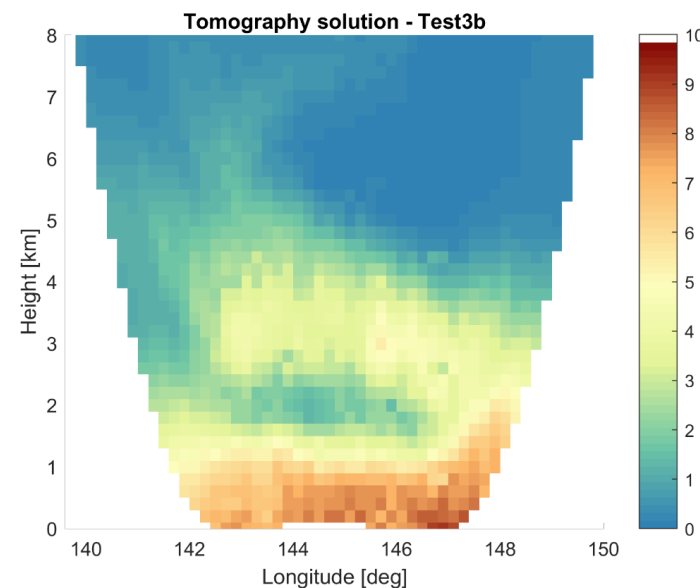
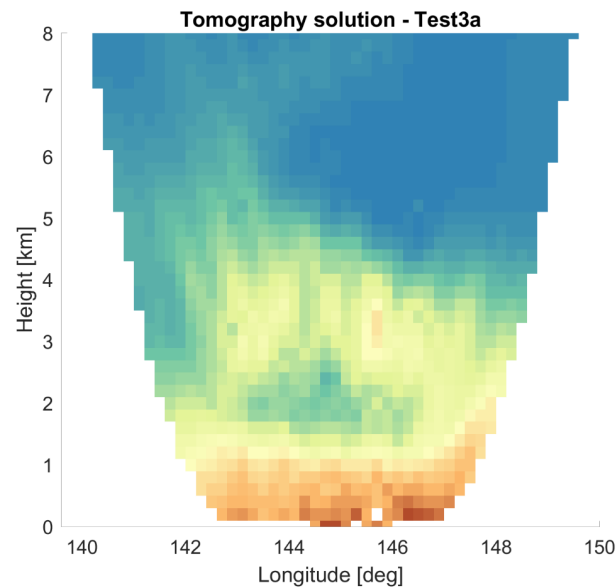


Multi-signal combination

Tomography solution – Number of satellites

	#Voxels	First guess	#CubeSats	σ_{RO}	σ_{apr}
Test3a	52 x 41	SmoothWRF	5 (30s,120s,...,390s)	$0.01g/m^3 km$	$0.2wvd$
Test3b	52 x 41	SmoothWRF	8 (0s,60s,...,420s)	$0.01g/m^3 km$	$0.2wvd$
Test3c	52 x 41	SmoothWRF	15 (0s,30s,...,420s)	$0.01g/m^3 km$	$0.2wvd$

How much depends the tomography solution on the number of satellites?

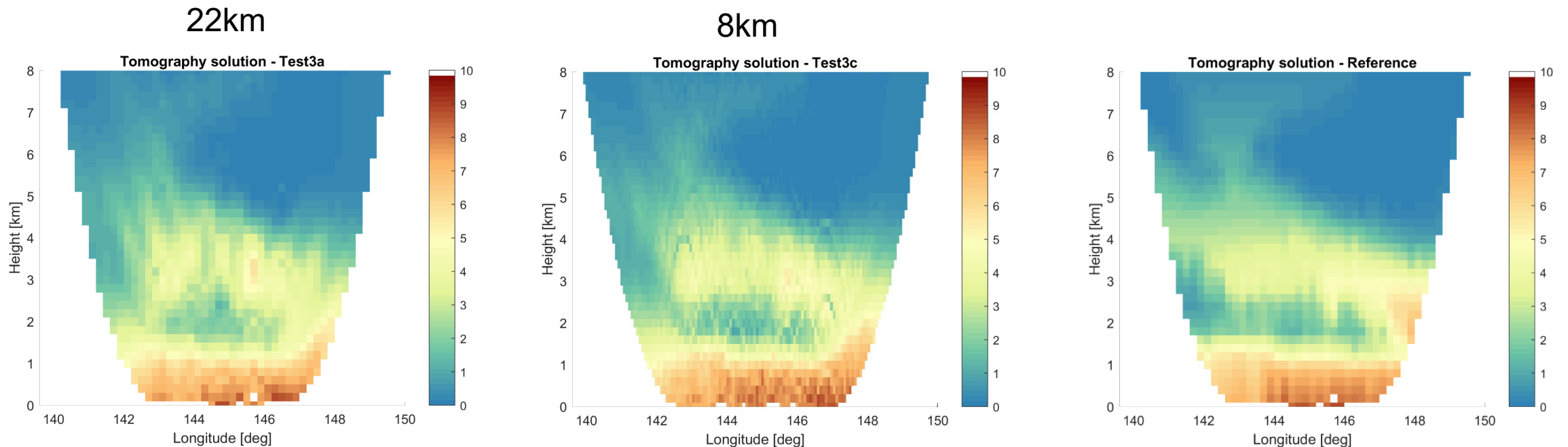


Multi-signal combination

Tomography solution – Spatial resolution

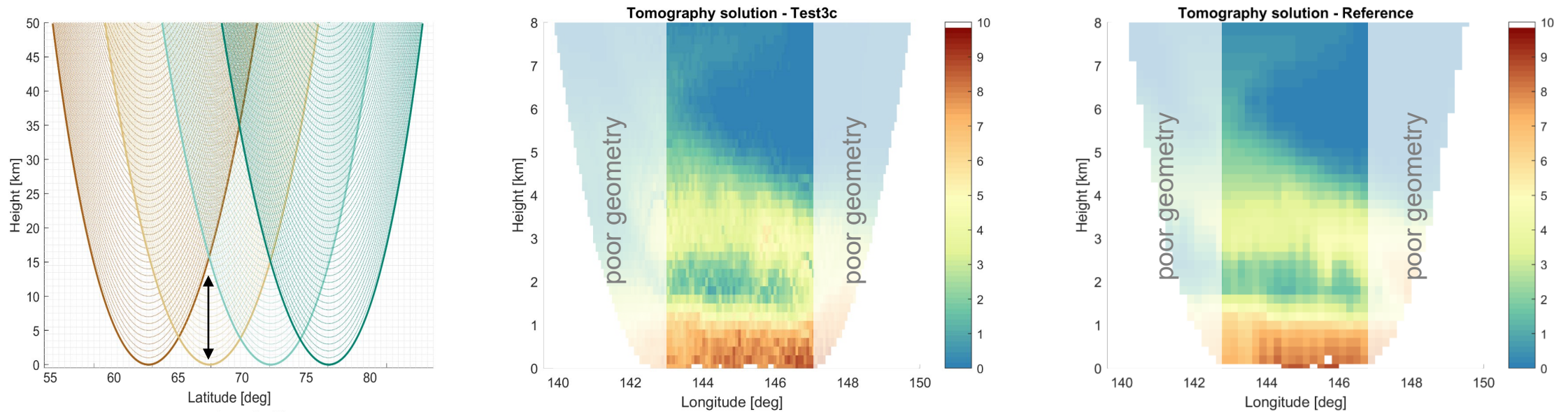
	#Voxels	First guess	#CubeSats	σ_{RO}	σ_{apr}
Test3a	52 x 41	SmoothWRF	5 (30s,120s,...,390s)	$0.01g/m^3km$	$0.2wvd$
Test3c	137 x 41	SmoothWRF	5 (0s,60s,...,420s)	$0.01g/m^3km$	$0.2wvd$

How good is the spatial resolution of the tomography solution?



Multi-signal combination

Tomography solution – Satellite spacing



Satellite spacing defines: a) the number of overlapping observations, b) horizontal resolution, c) temporal resolution, d) height of the lowest layers resolved and e) the area covered

Summary

- Nanosatellite technology opens up new possibilities for Earth observation
- Now available: A high-precision GNSS payload board for nanosatellite PNT
- Observation geometry of a dense satellite formation suited for tomographic processing
 - + not dependent on symmetry assumptions
 - + increased horizontal resolution (> 8 km)
- New quality in the reconstruction of atmospheric structures (demonstrated for water vapor distribution)

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- Moeller G., Sonnenberg F., Wolf A., Rothacher M., A high-precision commercial off-the-shelf GNSS payload board for nanosatellite orbit determination and timing, Proceedings of the 44th COSPAR Scientific Assembly 2022, Athens, Greece
- Turk F.J., Padullés R., Ao C.O., Juárez M.d.I.T., Wang K.-N., Franklin G.W., Lowe S.T., Hristova-Veleva S.M., Fetzer E.J., Cardellach E., Kuo Y.-H., Neelin J.D., Benefits of a Closely-Spaced Satellite Constellation of Atmospheric Polarimetric Radio Occultation Measurements. *Remote Sens.* **2019**, *11*, 2399.
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