Electronic Structure and Stability of Cs_2TiX_6 and Cs_2ZrX_6 (X = Br, I) Vacancy Ordered Double Perovskites.

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Vacancy ordered halide perovskites have been extensively investigated as promising lead-free alternatives to halide perovskites for various opto-electronic applications. Among these Cs_2TiBr_6 has been reported as a stable absorber with interesting electronic and optical properties, such as a band-gap in the visible, and long carrier diffusion lengths. Yet, a thorough theoretical analysis of the exhibited properties is still missing in order to further assess its application potential from a materials design point of view. In this letter, we perform a detailed analysis for the established Ti-based compounds and investigate the less-known materials based on Zr. We discuss in details their electronic properties and band symmetries, highlight the similarity between the materials in terms of properties, and reveal limits for tuning electronic and optical properties within this family of vacancy ordered double perovskites that share the same electron configuration. We also show the challenges to compute accurate and meaningful quasi-particle corrections at GW level. Furthermore, we address their chemical stability against different decomposition reaction pathways, identifying stable regions for the formation of all materials, while probing their mechanical stability employing phonon calculations. We predict that Cs_2ZrI_6, a material practically unexplored to-date, shall exhibit a quasi-direct electronic band-gap well within the visible range, the smallest charge carrier effective masses within the Cs_2BX_6 (B=Ti,Zr; X=Br, I) compounds, and a good chemical stability.

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Over the past decade lead-based halide perovskites have revolutionized the field of emerging photovoltaic technologies, reaching record-breaking power conversion efficiencies (PCE) certified at above 25%[1,2]. To-date, these perovskites have also found a wide range of opto-electronic applications in various devices such as highly-efficient light-emitters[3], photo-catalysts[4], and X-ray detectors[5]. In terms of materials, there have been important efforts to increase the exhibited stability while at the same time replacing the non-environmentally friendly lead atoms, which led to the exploration of different candidate perovskite materials[6]. For example, within the $APbX_3$ corner-sharing octahedra lattice it is possible to retain the oxidation state at the metallic site by replacing Pb^{2+} with Sn^{2+}[7,8]. Sn^{2+} based perovskite materials exhibit similar electronic and optical properties than lead halide perovskites, yet, $ASnX_3$ perovskites have a poor stability and degrade fast[9,10] due to the rapid oxidation of Sn^{2+} into Sn^{4+}. Another strategy is to replace Pb^{2+} using atoms at different oxidation states, and hence increase significantly the materials search space[6]. The combination of monovalent and trivalent atoms at the B-site lead to the formation of the $A_2BB'X_6$ halide double perovskites, such as $Cs_2BiAgBr_6$[11,12] and $Cs_2InAgCl_6$[13]. Using trivalent atoms lead to the formation of $A_3B_2X_9$ structures like $Cs_3Bi_2I_9$[14,15], while employing tetravalent atoms can lead to the so-called vacancy ordered double perovskite (VODP) A_2BX_6 lattices like Cs_2SnI_6. In fact, oxidation of Sn^{2+} in $CsSnI_3$ due to exposure to air, can lead to a structural transformation to Cs_2SnI_6[16] with Sn^{4+}.

The crystal lattice of such VODP can be derived from the standard $A_2BB'X_6$ double perovskite lattice by periodically introducing vacancies at the B' site. The final A_2BX_6 structure consists on a checkerboard like pattern between vacancies and isolated BX_6 octahedra. VODP materials can be synthesized with various tetravalent metals at the B-site including Pd[17], Te[18], Pt[19], Ti[20] and the aforementioned group 14 atoms: Pb[21] and Sn[22]. Many of these materials are non-toxic, stable and with tunable electronic and optical properties, making them promising candidates for various optoelectronic applications[23,24]. Cs_2SnI_6 for example is found to be more stable than corner-sharing $CsSnI_3$ and is the first A_2BX_6 material employed in solar cell devices[16]. Ti-based compounds Cs_2TiX_6 (X=Br, I) have been successfully synthesized and exhibit band-gaps of 1.02-2.00 eV[20,23,25]. Photovoltaic devices using Cs_2TiBr_6 have achieved PCE of up to 3.3% in a planar-heterojunction architecture with C_{60}, exhibiting open-circuit voltages (V_{oc}) of 1.0 V and also a short-circuit current (J_{sc}) of 5.69 mA.cm^{-2} [20]. The relatively poor PCE of the photovoltaic devices has been attributed to low absorption, indirect nature of the band-gap and the intrinsic instability of the material under ambient conditions[25]. Finally, Zr-based compounds Cs_2ZrX_6 (X=Cl, Br)

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have been recently synthesized by Abfalterer *et al.*[26] in nanocrystals form, and it was shown that these are stable and interesting light-emitters. We also highlight two reports of the early eighties, where Cs_2ZrI_6 has been reportedly synthesized[27,28], though has since remained unexplored.

In this letter, we perform a thorough analysis of the electronic structure, mechanical and chemical stability, and optical properties, of the class of photo-active Cs_2BX_6 VODP materials with B-site cations Ti^{+4} and Zr^{+4}, hence with d^0 valency at the B-site. Doing so, we explore the potential tunability limits of this family of materials, extend the existing understanding of the well-established Cs_2TiX_6; X=Br, I, and investigate the less known Zr-based compounds Cs_2ZrX_6, X=Br, I. We address the electronic and optical properties of these materials by means of density functional theory calculations, where we perform a complete symmetry analysis of the band structures and reveal its consequences on important physical properties like the exhibited band-gaps and charge carrier effective masses. Furthermore, we follow different decomposition reaction pathways and show the relative stability of the VODP materials with respect to competing compounds, and finally we address their mechanical stability by means of phonon dispersion calculations. Throughout this work we will discuss several aspects regarding both Ti and Zr based materials, and as the physical and chemical properties are very similar between these, in the main text we include the results for the known stable Cs_2TiBr_6 and the newly proposed Cs_2ZrI_6, while the results for the other materials are shown in the SI.
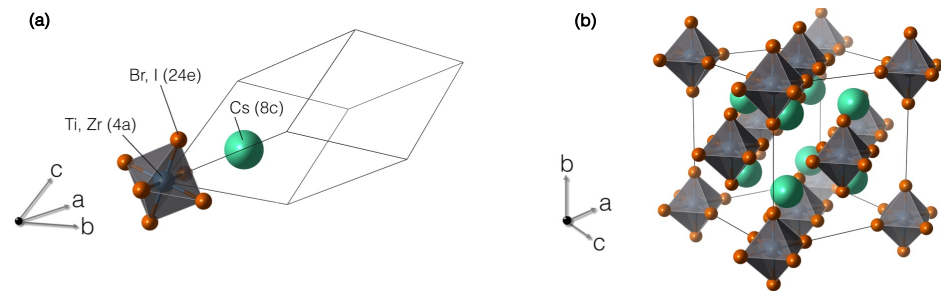

FIG. 1. (a) Primitive unit cell of the VODP family with corresponding Wyckoff positions. (b) Conventional unit cell showing the rock-salt arrangement between BX_6 octahedra and vacancies

Vacancy ordered double perovskites crystallize in a $Fm\bar{3}m$ face-centered cubic lattice (space group: 225), that can be considered as a rock-salt arrangement of BX_6 and ΔX_6 octahedra, with Δ a vacancy site. The primitive and conventional unit cells are shown in Fig. 1(a) and (b), respectively.

To begin, we fully optimize the four compounds Cs_2BX_6 (B=Ti,Zr; X=Br, I) within DFT-PBE (computational details are in the Supplementary Material - SI). Similar to standard perovskites, bromides have smaller lattice constants compared to the respective iodides. The calculated lattice parameters for Cs_2TiBr_6 and Cs_2ZrBr_6 are 10.92 Å and 11.24 Å, respectively. For the iodides Cs_2TiI_6 and Cs_2ZrI_6 we obtain larger lattice constants of 11.75 Å and 12.00 Å. These are in good agreement with experimental values of 10.57-10.92 Å for Cs_2TiBr_6[23,25,29], and 11.67 Å for Cs_2TiI_6[23]. The B-X bond-lengths follow the same trend, but interestingly the size of the vacancy doesn't seem to be significantly affected by the ionic radii of the B-site atom. We can quantify the size of the vacancy site as half the distance between two halogens that bound to a vacancy (i.e., X-Δ-X), and find 2.96 Å, 2.97 Å, 3.10 Å, 3.12 Å, for Cs_2TiBr_6, Cs_2ZrBr_6, Cs_2TiI_6, and Cs_2ZrI_6 respectively. This is in fact consistent with the fact that only halogens surround the vacant site, hence their interactions define the size of this ΔX_6 octahedron.

Next, we look at the electronic properties and symmetry of the VODPs. To do so, we employ and discuss below three levels of theory: standard DFT-PBE, HSE06 hybrid functional[30] (DFT-HSE), and finally G_oW_o (GW) calculations. Figure 2(a) shows the electronic band structures of Cs_2TiBr_6 and Cs_2ZrI_6, with and without spin-orbit coupling (SOC) effects. We also include the irreducible representations close to the band edges. The band structures of the two compounds share similar features, with the Cs_2ZrI_6 exhibiting slightly larger bandwidths. Not surprisingly, the electronic structure of the VODP is dictated by the valency of the B^{4+}-site and its interaction with X-site p-orbitals, which is in fact similar to the case of single[31] and double perovskites[32–34]. Here, the conduction and valence band edges are comprised of d-orbitals from the B-site atoms and p-orbitals from the halogens (projection of the orbitals on the bands are shown in Fig. 2(a) and Fig. S1). The electronic band-gaps are indirect with the conduction band minimum (cbm) at the X-point of the FCC Brillouin zone, and the valence band maxima (vbm) at the Γ point. The pseudo-charge density plots are shown in Fig. 2(b). Within DFT-HSE, we calculate electronic band-gaps of 2.68 eV and 2.58 eV for Cs_2TiBr_6 and Cs_2ZrI_6, respectively (see Table S1 for all compounds). Smaller halogens exhibit larger band-gaps, and the smaller the B-site atom the smaller the band-gap. This is consistent with previous reports for A_2BX_6 (A=Cs,K,Rb; B=Sn,Pt,Te; X=Cl,Br,I)[35] and Cs_2SbX_6 (X=Cl,Br)[36]. Comparing Cs_2TiBr_6 and Cs_2ZrI_6 we note that although Cs_2TiBr_6 exhibit a smaller band-gap than Cs_2ZrI_6 at DFT-PBE level, the opposite is observed at DFT-HSE level. This is due to the larger exchange correction for the bromide materials with respect to the one for iodides in the hybrid xc-functional calculations. Overall, comparing the accuracy of
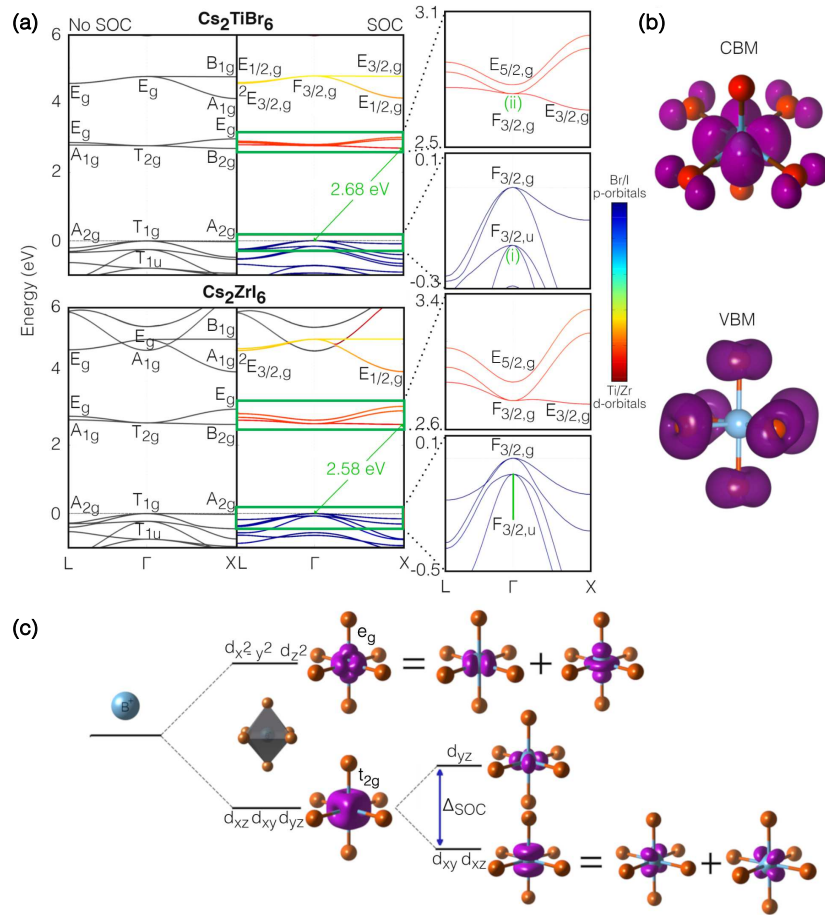
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FIG. 2. (a) Electronic band structure and symmetry analysis with and without spin-orbit coupling (SOC) for Cs_2TiBr_6 and Cs_2ZrI_6. Valence band maximum is set to zero, conduction bands are rigidly shifted to match the DFT-HSE level. Colors on the SOC electronic band structures denote the projection of the halogen p-orbitals (blue) and B-site atoms d-orbitals (red) to the respective state. The complete character table and the notation for the irreducible representations are in Table S3. (b) Pseudo-charge density for the valence band maximum (VBM) and conduction band minimum (CBM). (c) Splitting of Ti/Zr d-states due to octahedral coordination and Δ_{SOC} split.

the DFT-HSE calculations with the experimental reports one can observe a significant band-gap overestimation for Cs_2TiBr_6 and Cs_2TiI_6. On the other hand, for the case of Cs_2ZrBr_6 DFT-HSE

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predicts an electronic band-gap just 0.12 eV above the measured optical gap of the Cs_2ZrBr_6 nanocrystals[26]. These differences can relate to either the direct comparison between measured optical band-gaps with the calculated electronic band-gaps (e.g. no excitonic effects), or to the presence of defects in the samples used for the measurements. In fact, regarding the presence of bound excitons, the confined nature of the isolated octahedra in these materials may lead to large binding energies, thus significantly lowering optical band-gaps. Regarding defects, Maughan *et al.*[24] have shown that for example Cs_2TiI_6 is defect-intolerant, in the sense that defects states form well within its band-gap. Such types of defects, could clearly affect the measurements, and explain the lower experimental band-gaps for the Ti-based compound. To address these effects, further thorough experimental work needs to be carried alongside an ab-initio study including electron-hole interactions.

The calculated GW quasi-particle gaps are summarized in Table S1. For Cs_2TiBr_6 the predicted 3.87 eV quasi-particle gap overestimates more than two times the experimentally measured optical band-gap of 1.78-2.00 eV [20,23,25], and is significantly larger than our HSE calculation value of 2.68 eV. In fact, GW significantly overestimates the band-gaps of all three materials, for which experimental data are available (see Table S1). Such overestimation, can be attributed to the DFT starting point of our GW calculation and the presence of localized *d*-orbitals at the band edges with strong correlation effects, which standard DFT xc-functionals fail to describe. Employing self-consistent approaches that only update the eigenvalues like the evGW[37] leads to even larger band-gaps (e.g. 5.28 eV for Cs_2TiBr_6). This effect can be clearly shown by comparing our GW and HSE interpolated band structures (Fig. S2), where it is clear that there are practically no differences for the description of the halogens *p*-orbitals and the *Cs s*-orbitals. However, the same is not true for the relative position of Ti/Zr *d*-states indicating that indeed a careful treatment needs to be done in order to compute accurate quasi-particle band-gap for these materials. In fact, this is a well-known limitation, and to overcome it one can for example employ the auto-consistent DFT+U-GW method proposed by Patrick and Giustino[38]. Its application on TiO_2, another system for which Ti *d*-orbitals are critical for the electronic structure, corrected the DFT-GW overestimated electronic band-gap of 3.7 eV, to 3.27 eV. In our case, since the dispersion of the electronic band structures within PBE, HSE and GW does not change significantly (Fig. S2 and S3) we employ the PBE xc-functional, shifting the conduction band states rigidly to match the DFT-HSE band-gap.

The cbm of the VODP is made of d_{xy} of the Ti or Zr atoms, that interact with the p-orbitals of the halogens. As diagrammatically shown in Fig. 2(c) the split of the *d*-orbitals due to an octahedral
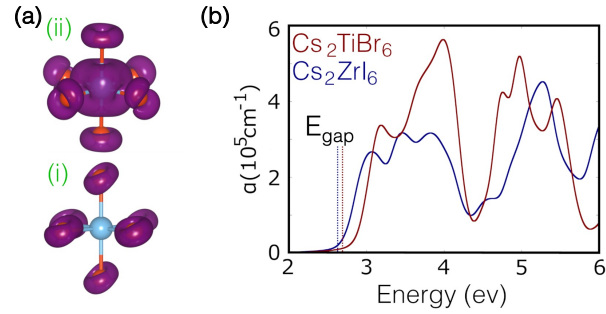
FIG. 3. (a) Pseudo-charge density for the first symmetry allowed transition between points (i) to (ii) as shown in Fig. 2(a). (b) Calculated absorption coefficient with the DFT-HSE electronic band-gap at the dotted lines.

coordination lead to an e_g double degenerated $d_{x^2-y^2}$ and d_{z^2} state and a t_{2g} triple degenerated orbitals d_{xy}, d_{xz}, d_{yz} state, exactly as we find at the Γ point in the VODP band structures without SOC. On the same figure the charge density plots of these points are shown to be consistent with a simple superposition of the aforementioned states, in agreement with the pseudo-charge density plots of Cs_2TiBr_6 and Cs_2ZrI_6. Inclusion of the SOC interactions is important for the conduction band of the VODP compounds and leads to a second splitting of t_{2g} states at the cbm at Γ. We can further look at this splitting; for Cs_2TiBr_6 and Cs_2ZrI_6 the splits are 22 meV and 85 meV respectively, within DFT-HSE. Δ_{SOC} increases going from Ti to Zr, which is consistent with the position of the atomic reference levels for Ti and Zr d-orbitals, shown in Table S2. On the other hand, the vbm of all VODP materials is comprised exclusively from p-orbitals from the halogens, which arrange around the vacant site as shown in Fig. S4.

The lowest direct band-to-band transition is in fact forbidden by symmetry (both at Γ and at X-point). However, few meV below the vbm, 161 meV (67 meV) Cs_2TiBr_6 (Cs_2ZrI_6), we find the irreducible representation $F_{3/2,u}$, which comprises the first symmetry allowed transition to the $F_{3/2,g}$ representation at the conduction band. The charge density corresponding for these states are shown in Fig. 3(a). We note here, that inclusion of SOC is also important for the fine description of the optically active transitions of these VODP, since the irreducible representation related to the first symmetry allowed band-to-band transition without taking into account SOC is at 250 meV and 220 meV below the vbm for Cs_2TiBr_6 and Cs_2ZrI_6, respectively. Figure 3(b) shows

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the calculated absorption coefficient for these materials at RPA level. Here the absorption was obtained using DFT-PBE including SOC with a dense k-point grid of $16\times16\times16$ and applying a scissor operator to match the HSE calculated gap. To verify this approach, in Fig. S3 we compare the electronic structure of the scissor shifted PBE calculation with the HSE hybrid functional bands. It is clear that the features of the bands are well described so, one can expect that optical properties (i.e., only considering inter-band transitions) calculated from a scissor shifted DFT-PBE are in close agreement with hybrid functional optics. One can observe a small shift at the onset of the absorption coefficient spectra with respect to the position of the DFT-HSE band-gap [dotted lines in Fig. 3(b)], which is consistent with the symmetry forbidden direct transition at Γ.

To probe the potential transport properties of these compounds we calculate the charge carrier effective masses at the band edges, which are summarized on the Table I. Looking at the valence band, all materials exhibit heavy and light holes at Γ. Clearly, iodine-based materials exhibit lower effective masses overall, while hole masses are practically the same between bromides and iodides. This is consistent with the projection of the vbm to solely halogen orbitals, shown in Fig. S1. At the conduction band, Zr-based compounds exhibit lower electron effective masses, hence, halogens affect both electron and hole masses, and B-site atoms affect only the electron mass. The conduction edge at the X high-symmetry point exhibits two in-plane light effective masses (fast direction) and a heavy mass (slow direction) orthogonal to these as shown in the effective mass tensor of Fig. S5. The directions of the masses are highlighted with colored arrows in Fig. S6, with the fast component expanding through the charge density lobes (blue lines). The in-plane expansion of the charge density, is in fact 3-fold degenerate along the symmetry equivalent planes due to the cubic lattice of our systems, yet it could allow confining the fast carriers to a two-dimensional plane by introducing small octahedral distortions that would break the crystal symmetry[39].

Having established the electronic structure of this family of VODP, and since we identify Cs_2ZrI_6 as a potential good candidate material, we move on to explore its stability. In an effort to understand the conditions for the formation of the material and compare with the rest of the VODP family, we first investigate their stability with respect to different decomposition reaction pathways. Following the procedure previously described by Persson et $al.$[40], firstly we imposed that the atomic chemical potentials μ_i of atom i must be less or equal to its solid phase μ_i^{solid} in order to assure that there will be no precipitation of these, that is:

$$\mu_i \leq \mu_i^{solid} \implies \Delta\mu_i \leq 0, \tag{1}$$

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TABLE I. Charge carrier effective masses in units of m_e. For the holes (m_h) at the valence band top, the masses are uniform and we include the heavy and light bands. For electrons (m_e) at the conduction band bottom there are two components in the effective mass tensor, a fast and a slow direction. (All masses are in m_e)

Effective masses (m_e)	m_h^{light}	m_h^{heavy}	m_e^{fast}	m_e^{slow}
Cs_2TiBr_6	1.14	2.84	1.76	7.62
Cs_2TiI_6	0.62	1.55	0.98	8.91
Cs_2ZrBr_6	1.12	2.82	1.27	11.29
Cs_2ZrI_6	0.60	1.45	0.86	11.55

where $\mu_i = \mu_i^{solid}$ indicates the atom i-rich limit of the phase diagram. Secondly, the stability condition of the VODP Cs_2BX_6 is taken into account through:

$$2\Delta\mu_{Cs} + \Delta\mu_B + 6\Delta\mu_X = \Delta H(Cs_2BX_6), \tag{2}$$

where B=Ti, Zr, X=Br, I and $\Delta H(Cs_2BX_6)$ is the heat of formation of compound Cs_2BX_6. Thirdly, we derive a set of equations which address the stability of all competing phases. Imposing that the sum of the chemical potentials of constituent atoms is less than the heat of formation of these means that there will be no formation of these compounds. Therefore, the analysis of the common solution of these set of inequalities lends to the thermodynamically stable region on which the compound of interest forms with no competition. The structures of all the stable competing compounds were identified using the Materials Project database[41] and for each material of the VODP family the set of inequalities (complete set in the SI) have the form:

$$m\Delta\mu_{Cs} + n\Delta\mu_B + l\Delta\mu_X \leq \Delta H(Cs_mB_nX_l). \tag{3}$$

The obtained stable chemical potential limits for each of the four explored materials are shown in Fig. 4(a) and Fig. S7(a) as the grey shaded area. First, we find that all binary compounds that do not contain Cs are stable within the $Cs - poor$ region of the diagrams while the ones containing Cs are placed within the $B - poor$ limit, which shows the consistency of these diagrams. Regarding the stability with respect to VODP decomposition to their competing phases, all plots show a region for which the materials are predicted to be stable (grey shaded). The position of the region is practically in the middle of the plots; hence we expect these to be more easily synthesized on a

balanced chemical environment. A comparison between the size of these regions reveals that the Zr family of compounds are expected to be more stable against decomposition when compared to the Ti family, and within each of these families the materials containing iodine are expected to be less stable with respect to bromides. To quantify their relative stability, we also define the formation energy of each material with respect to their salts (i.e. CsX, TiX$_4$, and ZrX$_4$ with X=Br,I). The formation energies per atom of Cs$_2$TiBr$_6$, Cs$_2$TiI$_6$, Cs$_2$ZrBr$_6$ and Cs$_2$ZrI$_6$ are -49 meV, -21 meV, -122 meV and -58 meV, respectively. These values are consistent with the stability trends reported, for which Zr- and Br-based compounds are more favorable than Ti- and I-based, respectively. We also address the mechanical stability of the explored structural phases by computing the phonon dispersion relations within DFT-PBE. The absence of modes with imaginary frequencies confirms that these materials are indeed stable, as shown on Fig. 4(b) and Fig. S7(b). Furthermore, we observe a red-shift of the phonon modes that is consistent with the masses of compounds going from the lighter Ti-based bromide, to Zr-based iodide. Interestingly, we can track the lowest frequency mode at the X-point, which red-shifts at just 9 cm^{-1} for the case of Cs$_2$ZrI$_6$. The mode is shown in Fig. S8, and can be described as an in-plane out-of-phase rotation of adjacent octahedra in the lattice.

To conclude, within this work we investigated the physico-chemical properties of Zr- and Ti-based VODP materials. We found that the not corner-sharing BX_6 octahedra effectively behave fundamentally like isolated structures, exhibiting the very same type of band splitting of tetrahedrally coordinated Zr and Ti atomic species as predicted within the crystal field theory. Yet, the charge carrier effective masses reported can be relatively low (i.e., below 1m$_e$), especially for the case of iodides. The importance of SOC interactions for the description of the allowed optical transitions is shown, together with a detailed symmetry analysis of the electronic band structure for the most prominent compounds in this VODP family: well-known Cs$_2$TiBr$_6$ and newly proposed Cs$_2$ZrI$_6$. Furthermore, we probe the limitation of ab-initio calculations and show that in order to compute meaningful quasi-particle corrections one needs to careful treat the conduction edge states due to strong correlations effects of d-orbitals, which can lead to largely overestimated band-gaps at the GW level. The optical absorption is very similar between these materials, due to their similar electronic band structures, hence alloying these could be an interesting parameter to fine tune the optical onset, without changing the rest exhibited properties. Finally, all compounds are predicted to be stable with respect to decomposition to competing phases and show that all VODP within this family are mechanically stable. Overall, this work explains the atom-
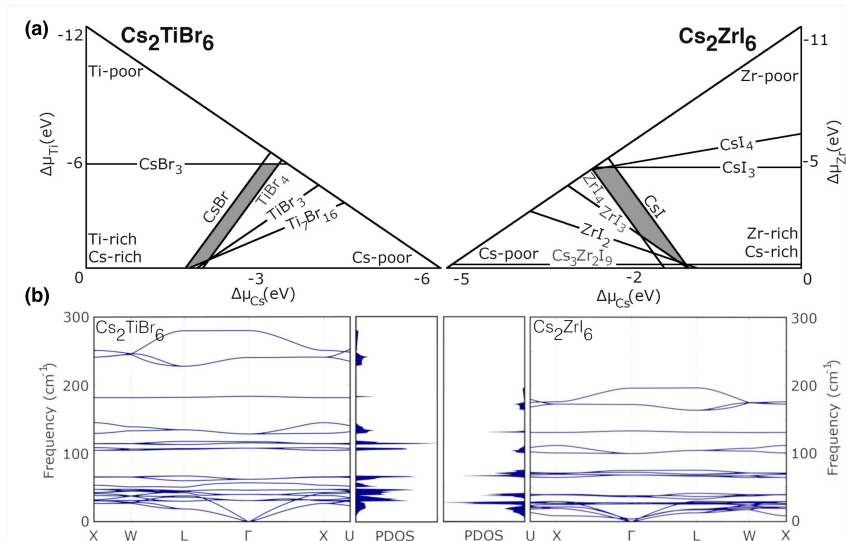
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FIG. 4. (a) Decomposition pathway diagrams indicating all the known stable competing phases with stability region represented as the grey shaded area. (b) Phonon dispersion and phonon density of states, the absence of imaginary(or soft) modes indicates dynamical stability

istic details of the electronic and optical properties of the VODP family with d^0 valency, within which Cs_2ZrI_6 remains unexplored to-date, and exhibits a band-gap within the visible range and the lightest charge carrier effective masses. Our findings support the possibility of forming a stable zirconium-iodine VODP with photo-active properties.

SUPPLEMENTARY MATERIAL

See supplementary material for the complete electronic structure of the studied $Cs_2TiX_6; X = Br, I$ and $Cs_2ZrX_6; X = Br, I$ family of materials, including computational methods, band-gaps and effective masses tables, equations for the chemical stability, projected band structures, effective mass tensor, character tables, decomposition pathways diagrams, phonon dispersion, interpolated G_0W_0 and DFT-HSE band structures.

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AUTHOR DECLARATIONS SECTION

Conflict of interest

The authors have no conflicts to disclose.

AIP PUBLISHING DATA SHARING POLICY

The data that supports the findings of this study are available within the article and its supplementary material.

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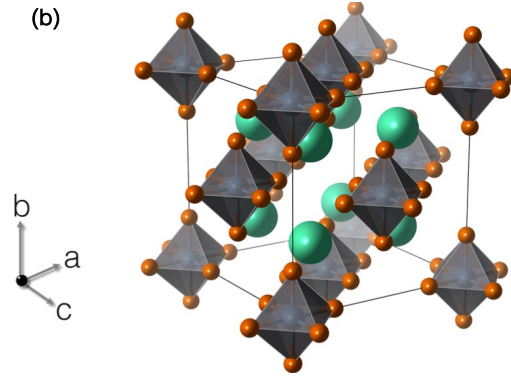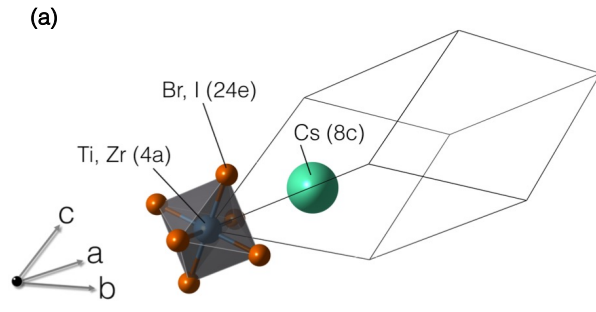[33]G. Volonakis, N. Sakai, H. J. Snaith, and F. Giustino, J. Phys. Chem. Lett. **10**, 1722 (2019).

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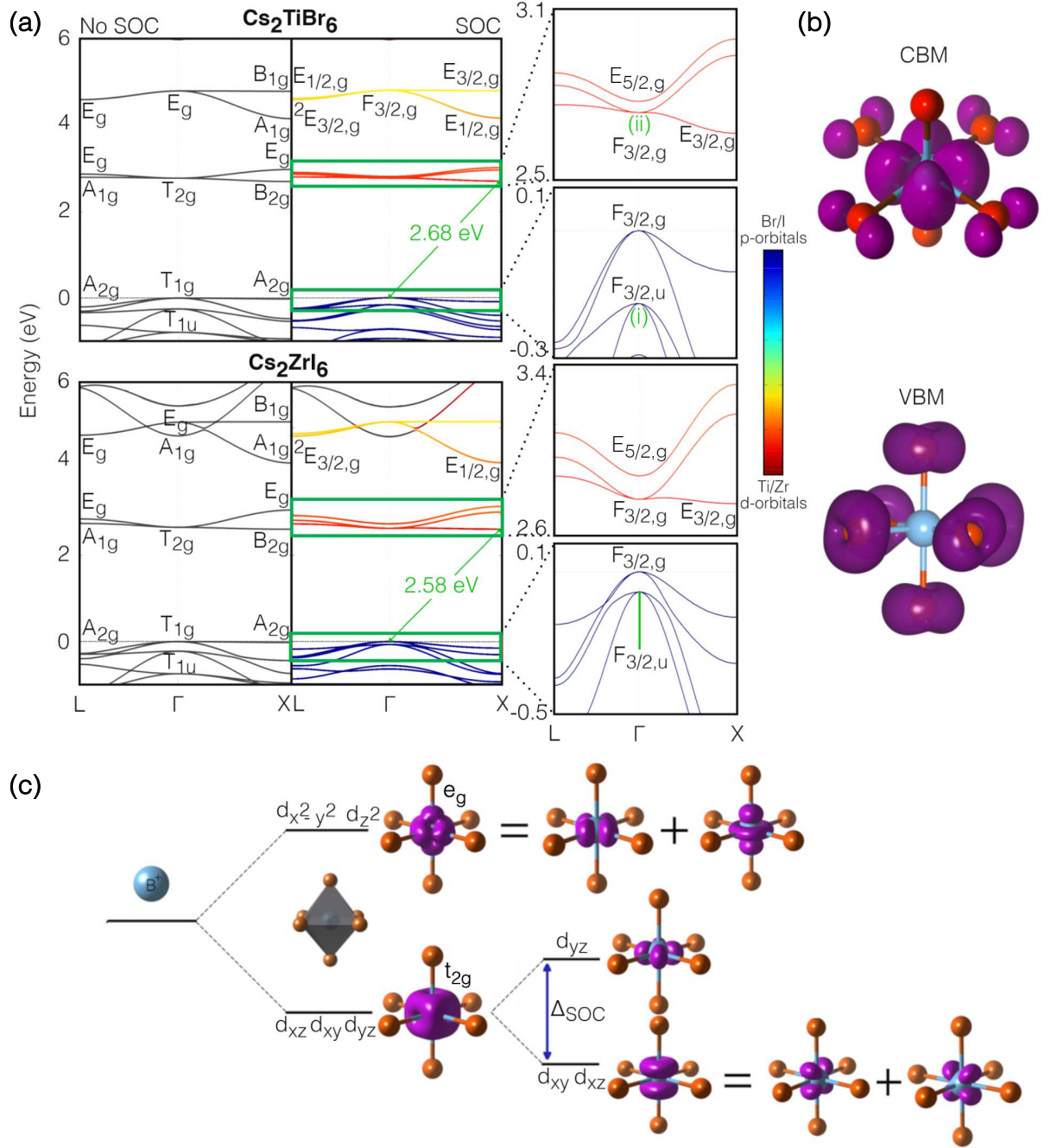
(a)

Br, I (24e)

Ti, Zr (4a)

Cs (8c)

c

a

b

(b)

b

a

c

(a) (ii) (i)

(b) Cs_2TiBr_6 Cs_2ZrI_6

$\alpha(10^5 cm^{-1})$

E_{gap}

Energy (ev)

(a)

Cs$_2$TiBr$_6$

Cs$_2$ZrI$_6$

Δμ$_{Ti}$(eV)

Δμ$_{Zr}$(eV)

Ti-poor

Zr-poor

CsBr$_3$

CsI$_4$

CsI$_3$

CsBr

TiBr$_4$

TiBr$_3$

Ti$_7$Br$_{16}$

ZrI$_4$

ZrI$_3$

CsI

ZrI$_2$

Ti-rich
Cs-rich

Cs-poor

Cs-poor

Cs$_3$Zr$_2$I$_9$

Zr-rich
Cs-rich

Δμ$_{Cs}$(eV)

Δμ$_{Cs}$(eV)

(b)

Cs$_2$TiBr$_6$

Cs$_2$ZrI$_6$

Frequency (cm^{-1})

Frequency (cm^{-1})

X   W   L   Γ   X   U   PDOS

PDOS   U   X   Γ   L   W   X